

Title: Representing time and time's arrow

Speakers: Bryan Roberts

Collection: Quantizing Time

Date: June 18, 2021 - 11:20 AM

URL: <http://pirsa.org/21060118>

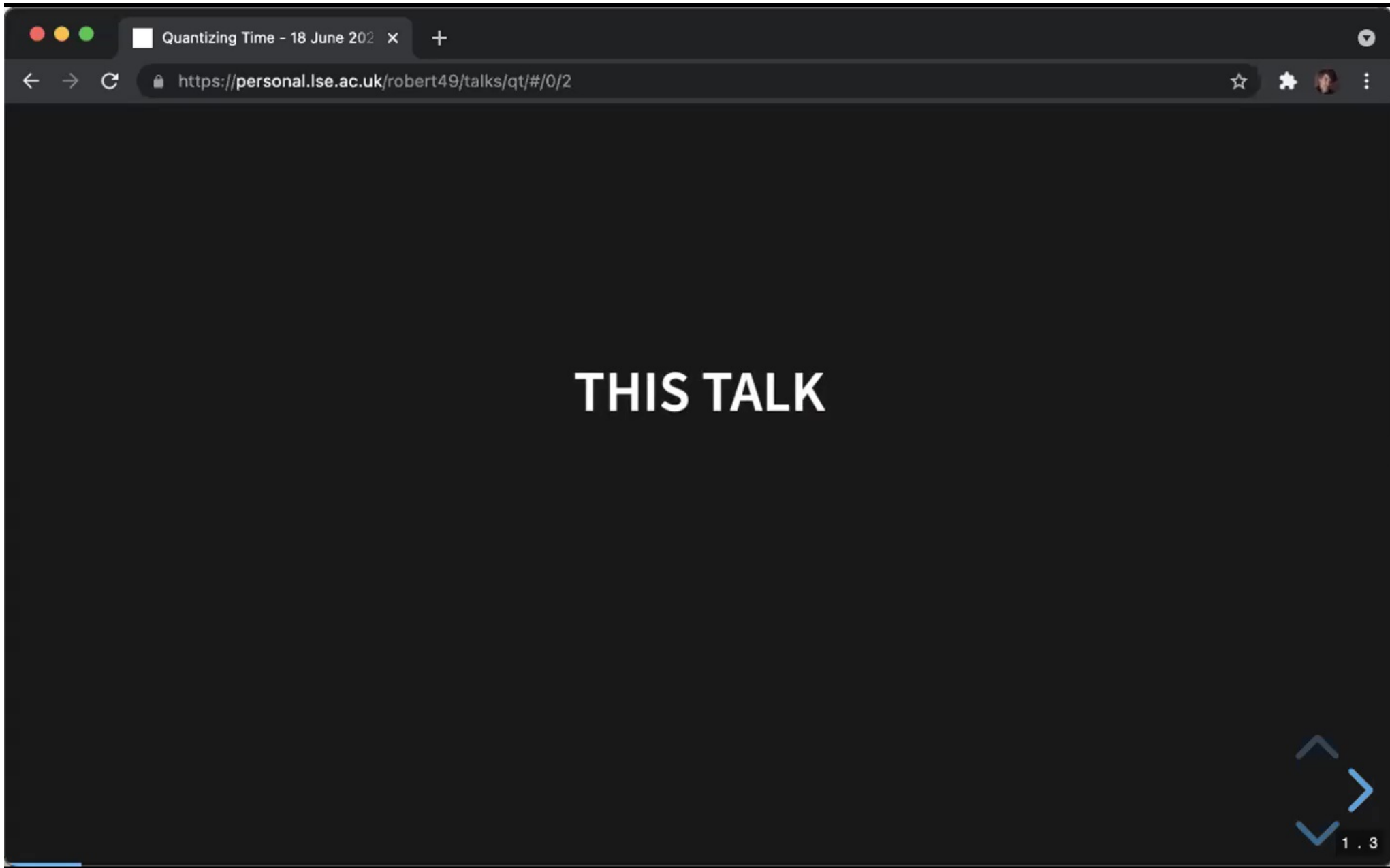
Abstract: What does it mean to say that a curve in state space describes change with respect to time, as opposed to space or any other parameter? What does it mean to say it's time is asymmetric? Inspired by the Wigner-Bargmann analysis of the Poincaré group, I discuss a general framework for understanding the meaning of time evolution and temporal symmetry in terms of the representation of a semigroup that includes "time translations", amongst the automorphisms of a state space. I discuss the structuralist and functionalist philosophical underpinnings of this view, and show how time reversal, parity, matter-antimatter exchange, and CPT are best viewed as extensions of a representation of continuous symmetries, whose existence is sensitive to the underlying structure of state space. I conclude with some comments on how an arrow of time can be defined in this framework, as well as prospects for such an arrow in the context of gravitation.

REPRESENTING TIME AND TIME'S ARROW

Bryan W. Roberts | [LSE](#)

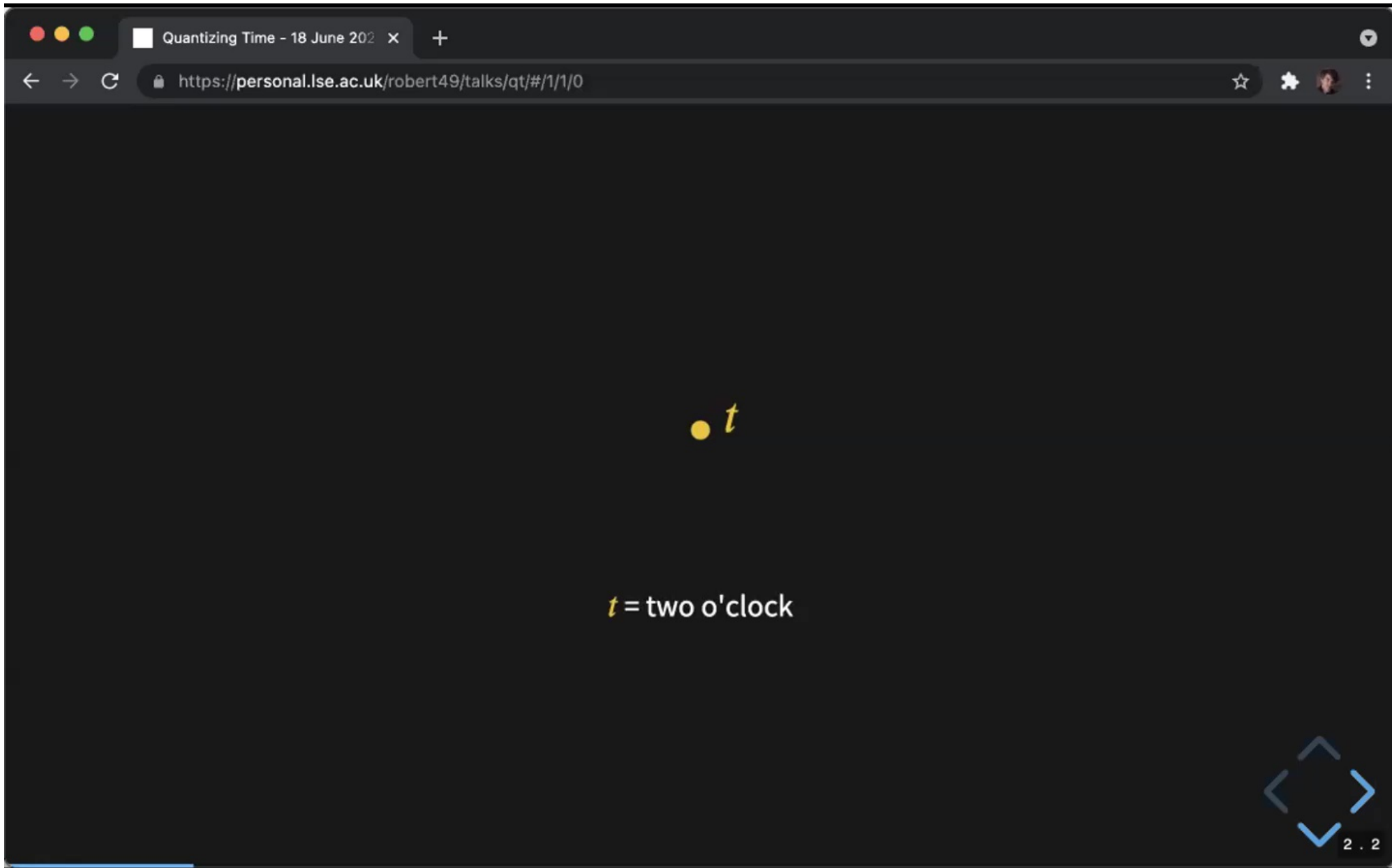
What captures time? Perspectives from this conference

- **Clock operators**
(Magdalena, Lorenzo, others)
- **Causal order**
(Veronika, Rob)
- **Causal creation**
(Lee)
- **S-matrix**
(Abhay)
- **Spacetime branching**
(Bianca)
- **Quantum reference frame**
(Časlav, Esteban)
- **Laws constraining clocks**
(Harvey)
- **Inference rules relating states**
(Emily)
- **(Intuitionist) Parminides and Heraclitus**
(Nicolas)
- **Timekeeping systems**
(Mischa)



THIS TALK

- **Thesis 1.** Time has a relational structure, characterised locally by a representation.
- **Thesis 2.** An arrow of time (and a matter-antimatter distinction) emerge from that relational structure.



THE REPRESENTATION VIEW

A great deal of physics is contained in the **representation of time translations**.

Some Motivation:

- **Relationism:** Earman (1989) *World Enough and Spacetime*
- **Spacetime Functionalism:** Knox (2013, 2019), Butterfield and Gomes (2020)
- **Wigner-Bargmann Picture:** Wigner (1939), Bargmann (1954)



THE REPRESENTATION VIEW

A great deal of physics is contained in the **representation of time translations**.

Some Motivation:

- **Parmenides vs Heraclitus?** (Nicolas Gisin)
- **Causal vs. Stochastic structure?** (Veronika Baumann, Lee Smolin, Rob Spekkens)
- **Time translation vs. Time in a QRF?** (Many at this conference)



When do we have a **time translation** as opposed to a **spatial transation**?



- **Sociology:** When we use the letter t .



Quantizing Time - 18 June 2022 x +

https://personal.lse.ac.uk/robert49/talks/qt/#/1/6/0

Time Translations

State Symmetries

ϕ

Representing Time

2 / 7



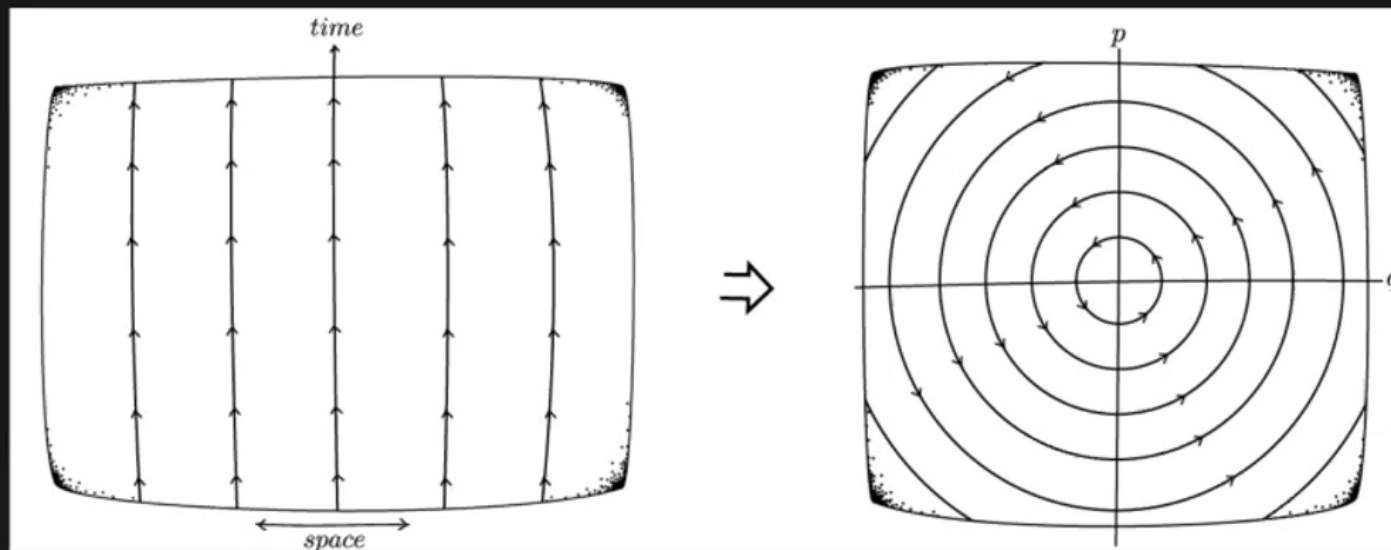
Representing Time



2 / 7

Example

Time translations represented among **State space symmetries**



Example

- Classical Mechanics:
Time translations: $G = (\mathbb{R}, +)$
State symmetries: (anti)symplectics $\phi : \phi^* \omega = |\omega|$
Representing Time: Homomorphism $t \mapsto \phi_t$.



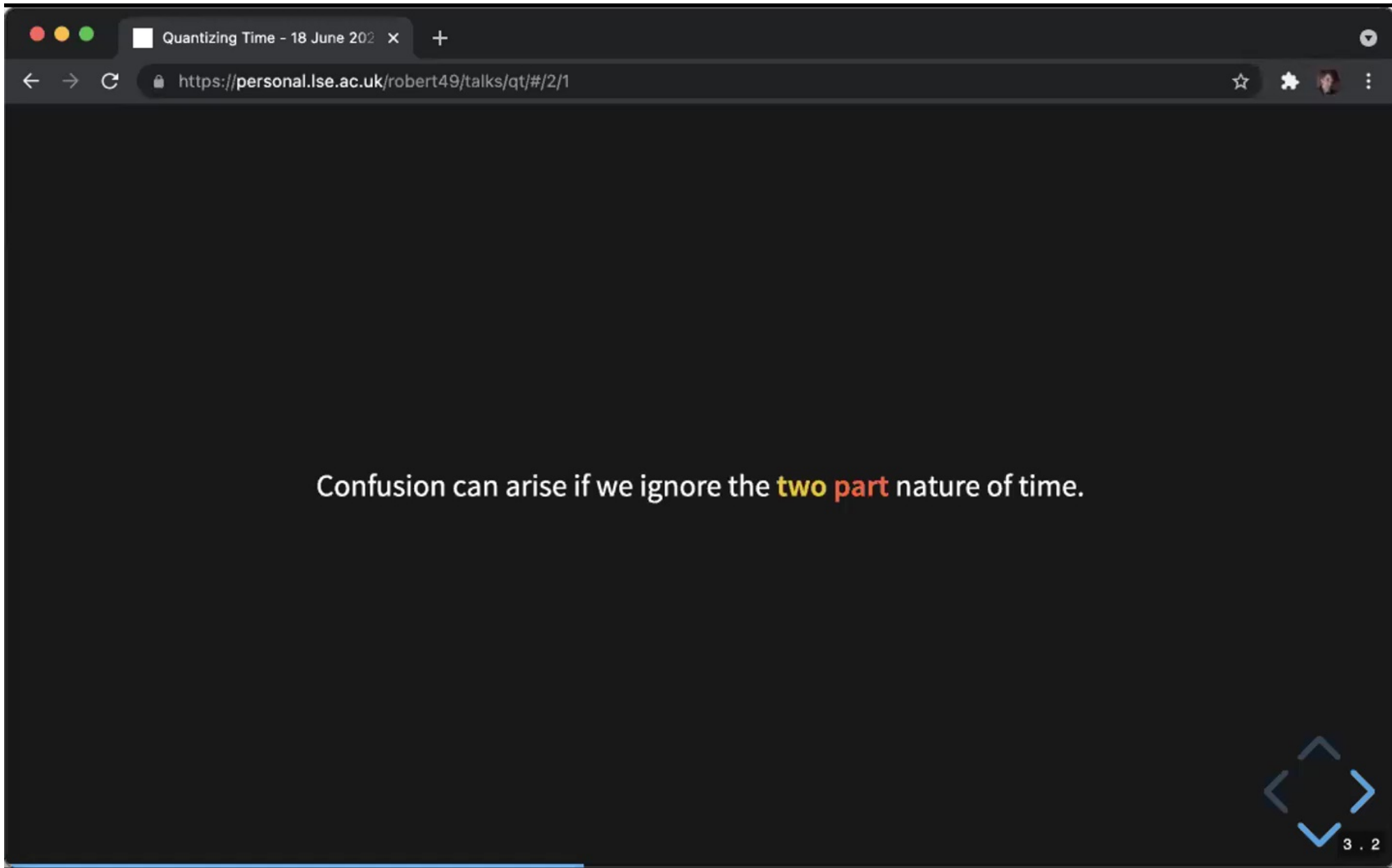
Examples

- **Poincaré group** $P_+^\uparrow \xrightarrow{\phi} \phi(P_+^\uparrow)$ **Unitary Hilbert space Rep**
(Wigner 1939)
- A **discrete group** for discrete time, etc.



THESIS 2(A)

An **arrow of time** emerges from time's relational structure.



Rovelli and Ashtekar discussion on Tuesday:

"Electromagnetism is **not invariant** under $E(t), B(t) \mapsto E(-t), B(-t)$ "

"...but **rather** under $E(t), B(t) \mapsto E(-t), -B(-t)$."



Quantizing Time - 18 June 2022

<https://personal.lse.ac.uk/robert49/talks/qt/#/2/4>

Q: Isn't **'true' time reversal** just

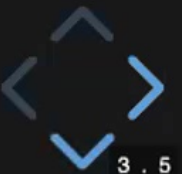
$$t \mapsto -t?$$

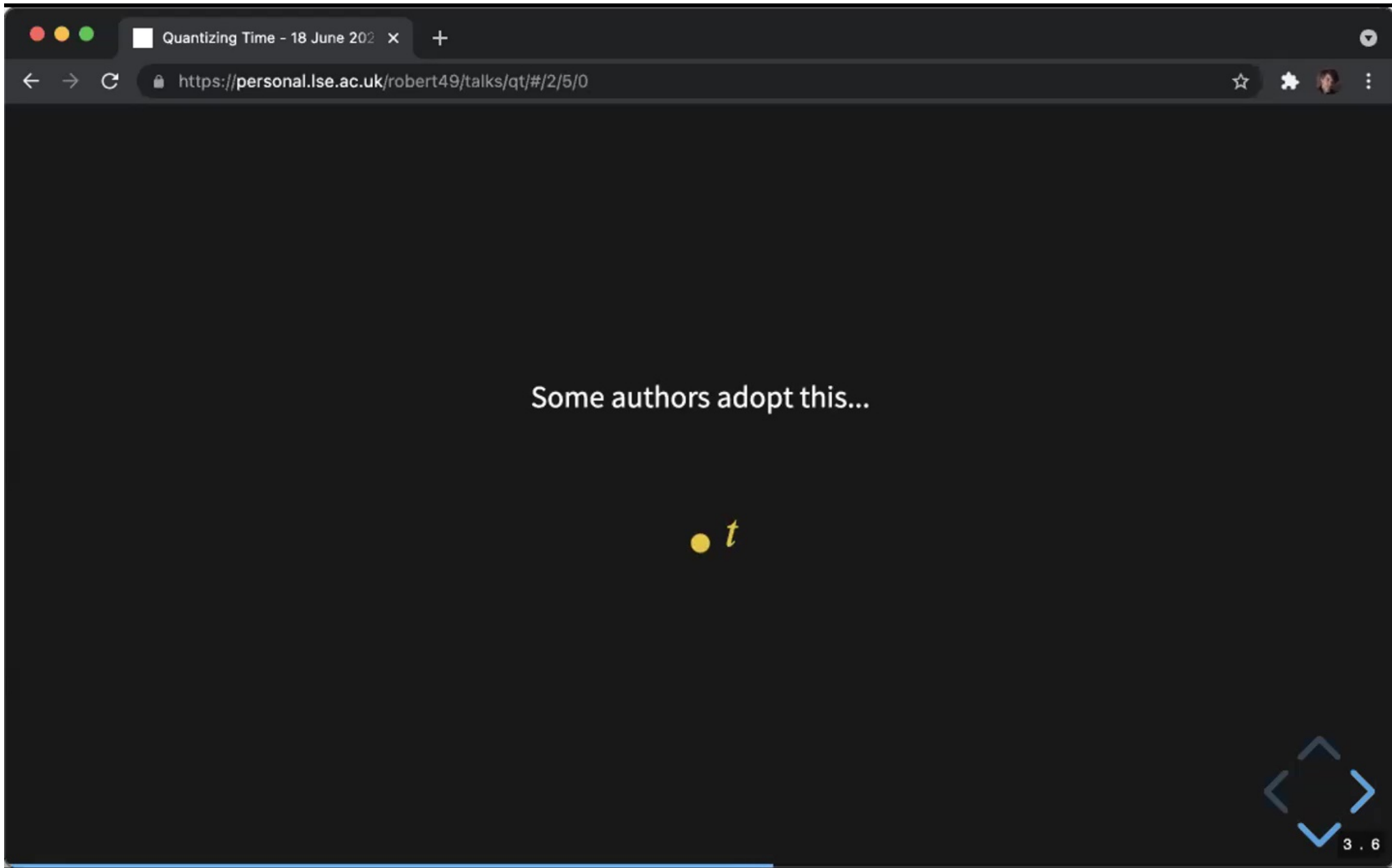
3 / 5

Q: Isn't **'true' time reversal** just

$$t \mapsto -t?$$

A: Yes, including if t is a **time translation**.
Its structure on **state space** follows deductively from this.





A group S of automorphisms of G defines via the **semidirect product** an **extension** of the group to $G \ltimes S$.

- $(\mathbb{R}, +)$ **extends** to time translations w/**time reversal** $\tilde{G} = (\mathbb{R}, +) \ltimes \{I, \tau\}$
- P_+^\uparrow **extends** to the '**full**' **Poincaré** group $P = P_+^\uparrow \ltimes \{I, \tau, \pi, \pi\tau\}$

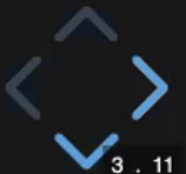
Many references, e.g. Varadarajan (2007)



In these extensions, τ implements time reversal by conjugation:

$$\tau t \tau^{-1} = -t$$

This is the definition of time reversal on the **time side**.



Lesson:

The problem of **defining time reversal** on a state space is just the problem of **extending** a representation of time translations G to a representation of \tilde{G} including time reversal $\tau \in \tilde{G}$.



Non-Existence of an Extension:

Given a representation of **time translations** G , a representation of time reversal **may not exist**. This occurs precisely when there is time-reversal symmetry violation.

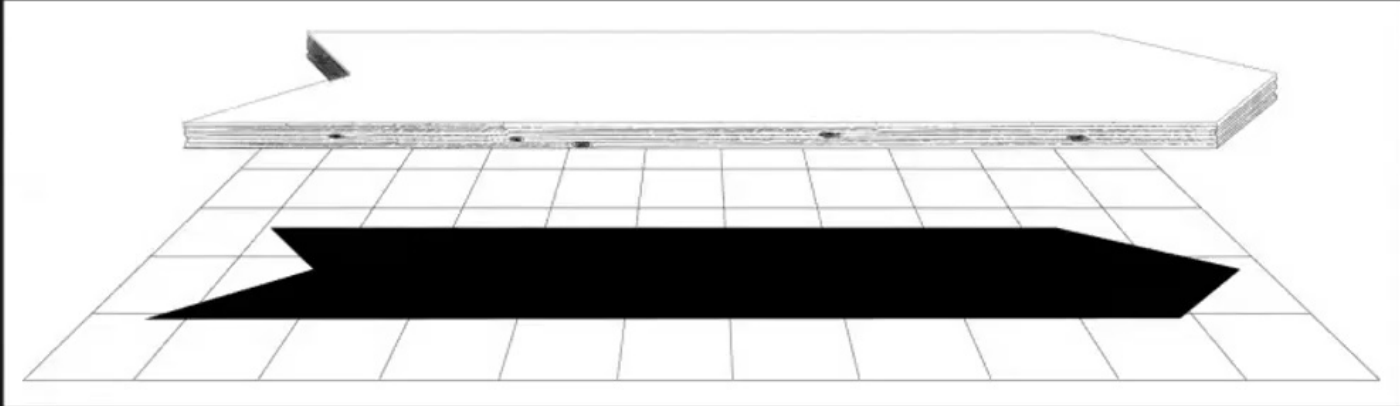
- BWR (2015a, 2015b), Ashtekar (2015)



Quantizing Time - 18 June 2022 x +

https://personal.lse.ac.uk/robert49/talks/qt/#/2/14

T-violation on **state space** holds information about the asymmetries of **time**



...just as a **shadow** holds information about the asymmetries of the **object**.

3 . 15

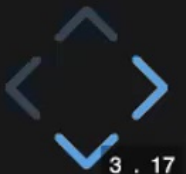
Existence of an Extension

When an extension of time translations to include time reversal **does exist**,
 $\tau : t \mapsto -t$ is generally represented by **a non-trivial** state-space operator.



Proposition 2. Every non-trivial positive-energy representation of $\tau : t \mapsto -t$ in quantum mechanics is **antiunitary** $U_\tau = T$; every such representation in classical mechanics is **antisymplectic** $\phi_\tau = T$.

(Cf. BWR 2017)



Quantizing Time - 18 June 202 x +

← → ↻ <https://personal.lse.ac.uk/robert49/talks/qt/#/3/1> ☆ ⚙️ 👤 ⋮

The local spacetime symmetry group is 'really' $SL(2, \mathbb{C})$, not P_+^\uparrow .

4 . 2

THANK YOU

- **Thesis 1.** Time has a relational structure, characterised locally by a representation.
- **Thesis 2.** An arrow of time (and a matter-antimatter distinction) emerge from that relational structure.