

Title: Measuring Quantum Discreteness of Time in the Lab with Gravity Entanglement Interference

Speakers: Carlo Rovelli

Collection: Quantizing Time

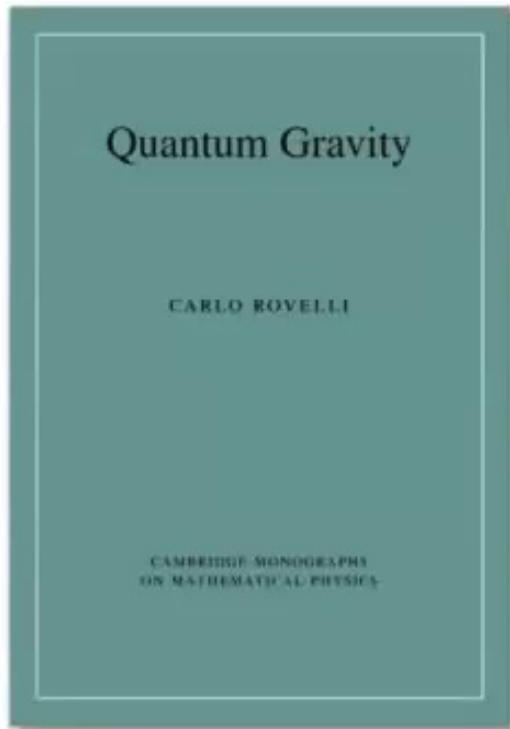
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URL: <http://pirsa.org/21060110>

Abstract: The concrete perspective of using interference to measure Gravity Induced Entanglement in the lab is a very exciting development for quantum gravity. While the measurements considered so far only test the nonrelativistic regime, the same technique might allow access to genuine relativistic quantum effects. Among these, there might be the possibility of direct detection of time quantum discreteness.

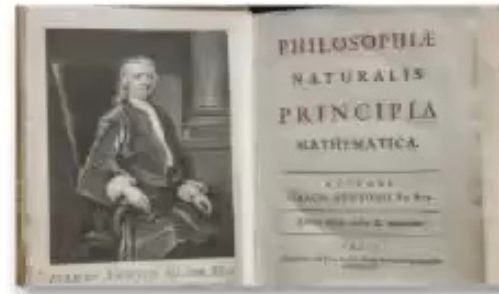
# Time in quantum gravity

Carlo Rovelli



Quantum Gravity  
CR  
Cambridge UP 2004

## Time



**Traditional** notion of time:

Any way of counting successions of events happening (day, night, day,...)

**Remains the same in quantum gravity!**

**Newtonian** time used in physics:

An entity flowing independent from anything else,  
which can (always imprecisely) measured by clocks

**Changes in quantum gravity!**

## Pre-relativistic formulation of evolution

Physical variables  $q_n(T)$  evolve with respect to the time variable  $T$

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$$\frac{dq_n(T)}{dT} = \{H, q_n(T)\}$$

Measuring apparatus measure variables

Clocks measure the time variable

This logic **does not work** in (general) relativistic physics

## Time in general relativity

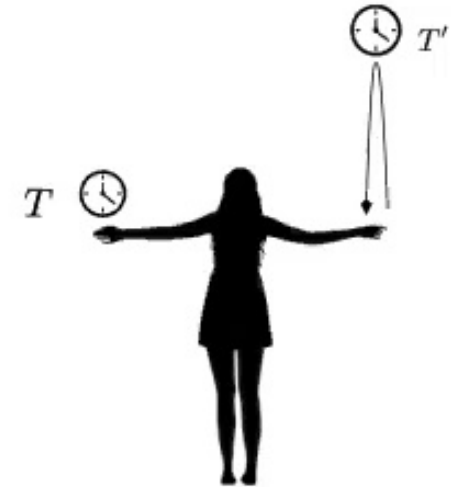
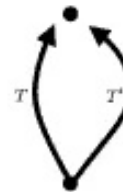
*"The difficulty for developing general relativity was to struggle with the meaning of the coordinates"*



Coordinates in non general relativistic field theories  $T$  :  
distances and time intervals measured by rods and clocks.

Coordinates in general relativistic field theories  $t \in (\vec{x}, t) = x$  :  
no measurable meaning at all.

Clocks measure proper time  $T = \int_{\gamma} \sqrt{g_{ab}(x) dx^a dx^b}$



These fact of nature are incompatible with

$$\left[ \begin{array}{l} \frac{dq_n(T)}{dT} = \{H, q_n(T)\} \\ \text{Measuring apparata measure variables} \\ \text{Clocks measure the time variable} \end{array} \right.$$

Physical variables  $q_n(T)$  evolve with **respect to the time variable**  $T$  .



Physical variables  $q_n, T, T' \dots$  evolve **with respect to one another** .  
⤴

## Generalize the formalism

Variables  $q_n$

Time  $T$

Evolution  $q_n = q_n(T)$

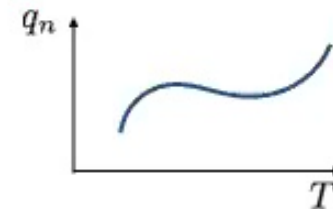
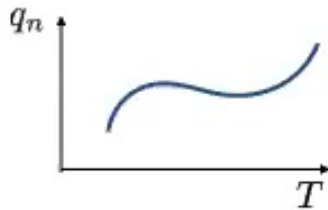
Equations  $\frac{dq_n(T)}{dT} = \{H, q_n\}$



Partial observables  $q^i = (q_n, T, T', T'', \dots)$

Evolution  $Q(q^i) = 0$

Equations  $\{C, Q(q^i)\} = 0$



$$C = p_T + H$$

$$Q_n = q_n - q_n(T) = 0$$

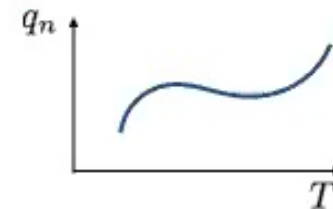
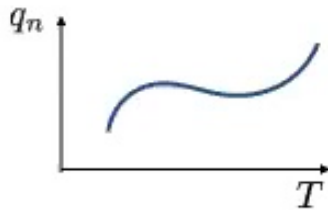


## Generalize the formalism

Variables  $q_n$   
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 Evolution  $q_n = q_n(T)$   
 Equations  $\frac{dq_n(T)}{dT} = \{H, q_n\}$



Partial observables  $q^i = (q_n, T, T', T'', \dots)$   
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$$C = p_T + H$$

$$Q_n = q_n - q_n(T) = 0$$

Relativistic dynamics is not “frozen”!

It is simply described in a different (and more general) language.



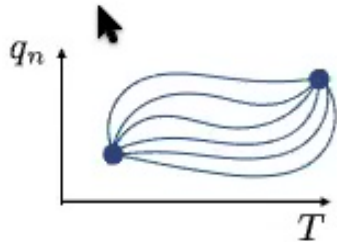
## Generalize the formalism

Observables  $q_n$  on  $\mathcal{H}$   
 Time  $T$   
 Evolution  $q_n = q_n(T)$   
 Equations  $\frac{dq_n(T)}{dT} = \frac{i}{\hbar}[H, q_n]$   

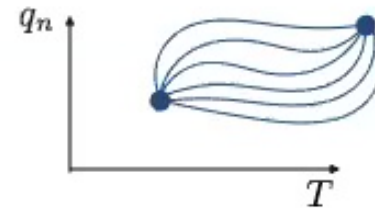
$$i\hbar \frac{\partial \psi}{\partial T} = H\psi$$



Partial observables  $q^i = (q_n, T, T', T'', \dots)$  on  $\mathcal{K}$   
 Evolution  $f(q^i) = 0$   
 Equations  $[C, Q(q^i)] = 0$   
 $C\psi = 0$  Wheeler de Witt equation



$$C = p_T + H$$



## General covariant transition amplitudes

Partial observables  $q^i$  on  $\mathcal{K}$

$C\psi = 0$  defines  $\mathcal{H}$

$P = \mathcal{K} \rightarrow \mathcal{H}$

$q^i |q^i\rangle = q^i |q^i\rangle$

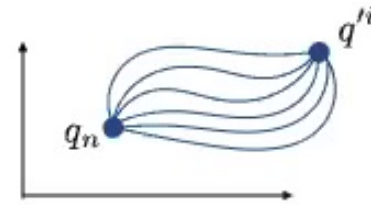
$W(q'^i, q^i) = \langle q'^i | P | q^i \rangle$

$$C = p_T + H$$

$$q^i = (x, t)$$

$$\psi(x, t) \in \mathcal{K}$$

$$W(x't', xt) = \langle x't' | P | xt \rangle = \langle x' | e^{iH(t'-y)} | x \rangle$$



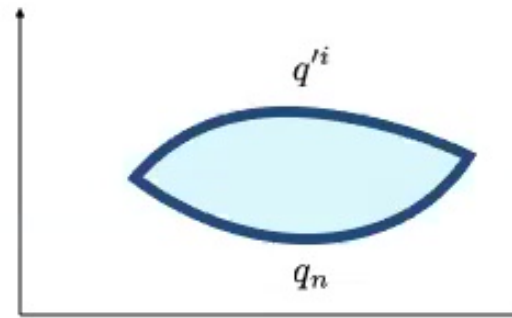
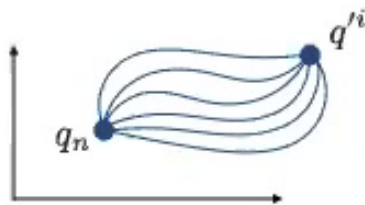
## Application to general relativity (formal)

Partial observables  $q_{ab}(\vec{x})$  on  $\mathcal{K}$

$C\psi = 0$  defines  $\mathcal{H}$

$P = \mathcal{K} \rightarrow \mathcal{H}$   $W(\mathbf{q}'^i, \mathbf{q}^i) = \langle q'^i | P | q^i \rangle$

$$W(q, q') \sim \int_{\partial g=(q, q')} dg e^{iS[g]}$$



## Application to general relativity (non formal)

$\mathcal{H}$  Truncation:  $\mathcal{H}_\Gamma \subset \mathcal{H} \quad \mathcal{H}_\Gamma = L^2[SU(2)^L/SU(2)^N]_\Gamma$

$q^i$  Operators:  $\vec{E}_l = il_p^2 \vec{L}_l \quad L^i \psi(h) \equiv \left. \frac{d}{dt} \psi(h e^{t\tau_i}) \right|_{t=0}$

$\mathcal{W}_C : \mathcal{H}_\Gamma \rightarrow \mathbb{C} \quad \partial C = \Gamma$

Transition amplitudes  $W_C(h_l) = N_C \int_{SU(2)} dh_{vf} \prod_f \delta(h_f) \prod_v A(h_{vf})$

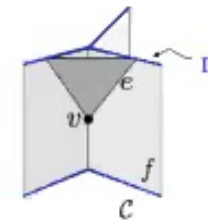
Vertex amplitude  $A(h_{vf}) = \int_{SL(2,\mathbb{C})} dg'_e \prod_f \sum_j (2j+1) D_{mn}^j(h_{vf}) D_{j_m j_n}^{\gamma(j+1)j}(g_e g_e^{-1})$

$h_f = \prod_v h_{vf} \quad W = \lim_{C \rightarrow \infty} W_C$



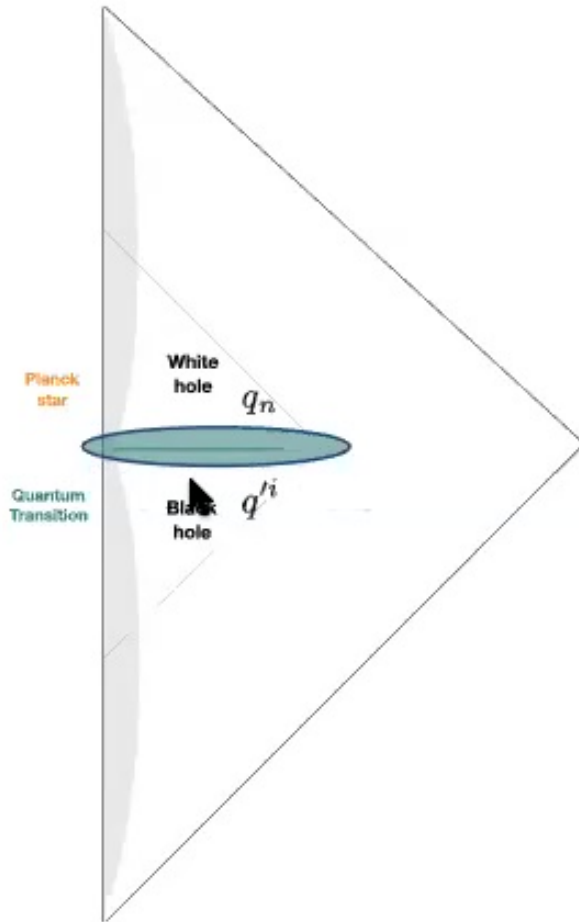
**spin network**  
(nodes, links)

1995



**spinfoam**  
(vertices, edges, faces)

2005



$$W(\mathbf{q}^i, \mathbf{q}^i) = \langle q^i | P | q^i \rangle$$

## Issues:

Where is the time variable?

Which time variable? (GR!)

Where are probabilities?

Probabilities is what the theory gives

Where is evolution, change?

The theory is about evolution, change

Is causal structure fixed?

No, not can obviously be in superpositions

Do we need quantum reference frames?

We do not need reference frames at all

Is the geometry locally flat?

Yes at large scales, at small scales it is fuzzy

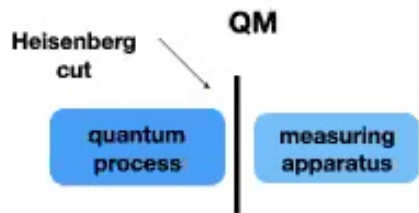
Is there a “manifold”?

No.

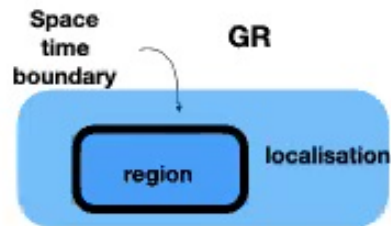


# Issues:

Where is the observation?



**QG Spacetime boundary = Heisenberg cut**

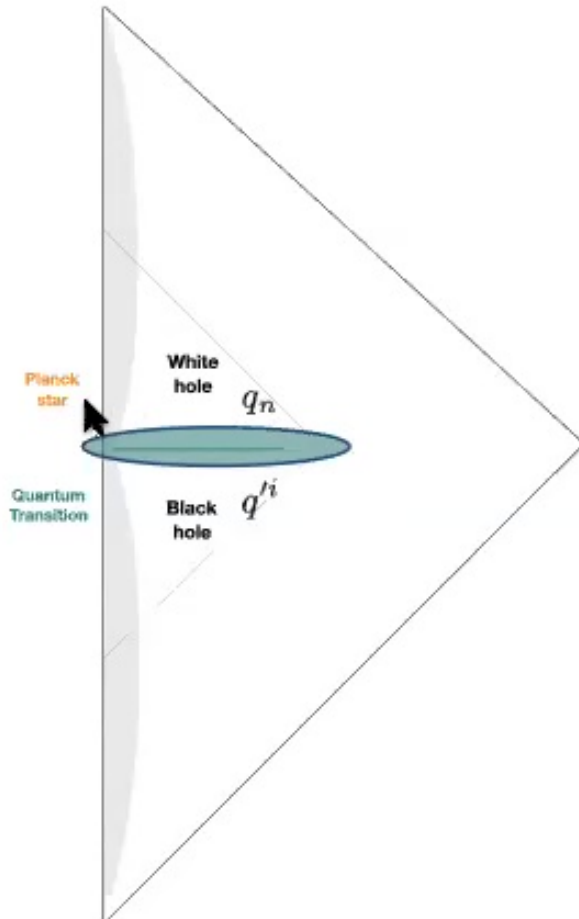


Does spacetime “emerge”?

In the same sense in which an electromagnetic wave “emerges” from photons, namely as a standard classical approximation.

Is this dramatic?

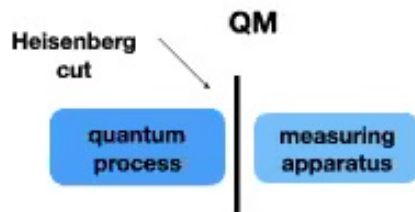
No.



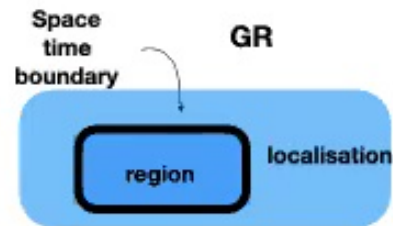
$$W(\mathbf{q}^i, \mathbf{q}^i) = \langle q'^i | P | q^i \rangle$$

## Issues:

Where is the observation?



**QG** Spacetime boundary = Heisenberg cut



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In the same sense in which an electromagnetic wave “emerges” from photons, namely as a standard classical approximation.

Is this dramatic?

No.

## So, what is “time”:

- The name we give to the fact that events “happen”: Same in quantum gravity
- A way of counting (local sequences of events): Exists in quantum gravity
- The reading of a clock: As in GR: there are many cooks
- A complete ordering of events: Does not exactly exist in Nature (SR)
- Minkowski spacetime: Only approximately in QG
- Newtonian time: Only an approximation
- Oriented time: It is a macroscopic, statistical phenomenon  
Quantum gravity is not going to change this!

## Quantum time?

Time variables are many, are measurable, are on the same footing as other variables.

There is nothing “frozen” in the Wheeler DeWitt equation.  
No need to invoke quantum theory to see time “emerge”.

There is no mystery about “emergence of time”

Can we have **superposition** of “times”? Of course

Can time be **fuzzy**? Of course, it is a variable like others.

Can time be **discrete**? Of course, and the discreteness of time can be measurable!

**See the talk of [Marios Christodoulous](#) !**

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