Title: Measuring time with stationary quantum clocks

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Collection: Quantizing Time

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Abstract: Time plays a fundamental role in our ability to make sense of the physical laws in the world around us. The nature of time has puzzled people $\hat{a} \in$ "- from the ancient Greeks to the present day $-\hat{a} \in$ " resulting in a long running debate between philosophers and physicists alike to whether time needs change to exist (the so-called relatival theory), or whether time flows regardless of change (the so-called substantival theory). One way to decide between the two is to attempt to measure the flow of time with a stationary clock, since if time were substantival, the flow of time would manifest itself in the experiment. Alas, conventional wisdom suggests that in order for a clock to function, it cannot be a static object, thus rendering this experiment seemingly impossible. We show that counter-intuitively, a quantum clock can measure the passage of time, even while being switched off, lending support for the substantival theory of time.

Measuring time with stationary quantum clocks arXiv:2106.07684

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Overview:

- Philosophy of time: two competing viewpoints
- Interaction-free measurements
- Introduce counterfactual clocks
- Implications for the debate on time



The nature of time:

- Two competing theories:
 - Substantival theory:

Time exists independently of motion; it forms an invisible contain in which matter lives.

- Relative theory:

Time is merely a consequence of motion; it is a result of the relationships between events of physical things.

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History (highlights):

- Greek atomists: substantivalists? (no written account has survived)
- Aristotle: proponent of relative theory



"But neither does time exist without change; ..."

[Aristotle, 350 BC]

- Newton: on the Substantival camp
- Leibnitz: on the Relative camp



Leibnitz vs Newton

- Ernst Mach: attached Newtons views
- Einstein credits Ernst Mach as a source of his inspiration for relativity
- Alive today: Paul Davies (Relative theory), Tim Maudlin (Substantival theory). Carlo Rovelli, Lee Smolin, Julian Barbour, Fay Dowker.

History (highlights):

- Why is there no consensus after more than 2 millennia of debate?
 - Our theories appear to allow both a substantival and relative interpretation of time

- Natural experiment:
 - Try to measure time with a stationary clock
 - If time is substantival, time should be measurable!
 - If time is relative, clock won't record anything!



History (highlights):

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- Natural experiment:
 - Try to measure time with a stationary clock
 - If time is substantival, time should be measurable!
 - If time is relative, clock won't record anything!
 - Problem: clocks appear to need dynamics to function



- Invented by A. Elitzur and L. Vaidman (E.-V. bomb tester):
- Have a bomb but not sure if its live or a dud:
 - If live:



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- <u>Objections</u>: system has certainly been in a superposition exploded and live bomb *before* measurement
- <u>But</u>: outcome "D1 ticks" can only be observed if we collapse to a branch of the wave function orthogonal to exploded bomb
- Interpretation uses *retrodiction*: measurement collapse determines past events



$$|\text{alive}\rangle \longrightarrow \frac{1}{\sqrt{2}} (|\text{alive}\rangle + |\text{dead}\rangle)$$

- Other examples:
 - The Penrose bomb-testing device: [R. Penrose, Phys. Rev. Lett. (1994)]
 - Interaction-free imaging: [A. White et. al. (1998)]
 - Counterfactual computing: [G. Mitchison and R. Jozsa, Proc. Roy. Soc. (1992)]
 - The Hardy paradox: [Lucien Hardy, Phys. Rev. Lett. (1992)]



- Many experimental realizations: e.g. [O. Hosten et. al., Nature (2006)]

Setup

 $|\psi(t)
angle \in \mathcal{H}$, $\dim\left(\mathcal{H}
ight) = N_T + 1$

 $| au_0
angle,\,| au_1
angle,\ldots,\,| au_{N_T}
angle$ at times $au_0, au_1,\ldots, au_{N_T}$

- Two external events separated by elapsed time t

 $t \in \{\tau_0, \tau_1, \tau_2, \ldots, \tau_{N_T}\}$

- What is t ?

- Protocol:
 - > At 1st event prepare $|\psi(0)\rangle$
 - \succ At 2nd event measure in basis $|\tau_0\rangle, |\tau_1\rangle, \ldots, |\tau_{N_T}\rangle$
 - \blacktriangleright Measurement outcome determines t

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- Using it to tell the time when off
 - New protocol using interaction-free measurement ($N_T=1$): $t\in\{ au_0, au_1\}$





- Using it to tell the time when off
 - Analyze protocol:

• If
$$t = \tau_0$$
. $|E\rangle \xrightarrow{\tau_0} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
• $s |\psi\rangle \xrightarrow{\tau_0} s |\tau_0\rangle \xrightarrow{U_{\mathrm{m}}} -cA_2^0 |A\rangle + sA_3^1 |\tau_0\rangle + sA_4^1 |\tau_1\rangle$

• If
$$t = \tau_1$$
. $|E\rangle \xrightarrow{\tau_1} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
• $t = \tau_1$
• $s |\psi\rangle \xrightarrow{\tau_1} s |\tau_1\rangle \xrightarrow{U_{\mathrm{m}}} -cA_1^0 |E\rangle + sA_3^{1'} |\tau_0\rangle + sA_4^{1'} |\tau_1\rangle$

- If
$$|E\rangle$$
 outcome: $\begin{bmatrix} - \text{ If } t = \tau_0. \text{ Clock was off} \\ - \text{ If } t = \tau_1. \text{ No outcome} \end{bmatrix}$



- Using it to tell the time when off
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• If
$$t = \tau_1$$
. $|E\rangle \xrightarrow{\tau_1} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
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• $s |\psi\rangle \xrightarrow{\tau_1} s |\tau_1\rangle \xrightarrow{U_{\mathrm{m}}} -cA_1^0 |E\rangle + sA_3^{1'} |\tau_0\rangle + sA_4^{1'} |\tau_1\rangle$

- If
$$|E\rangle$$
 outcome: $\begin{cases} -\text{ If }t= au_0. \text{ Clock was off}\\ -\text{ If }t= au_1. \text{ No outcome} \end{cases}$

- If
$$|A\rangle$$
 outcome: $\begin{bmatrix} - \text{ If } t = \tau_0. \text{ No outcome} \\ - \text{ If } t = \tau_1. \text{ Clock was off} \end{bmatrix}$



- Using it to tell the time when off
 - Analyze protocol:

• If
$$t = \tau_0$$
. $|E\rangle \xrightarrow{\tau_0} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
• $t = \tau_0$
• $s |\psi\rangle \xrightarrow{\tau_0} s |\tau_0\rangle \xrightarrow{U_{\mathrm{m}}} -cA_2^0 |A\rangle + sA_3^1 |\tau_0\rangle + sA_4^1 |\tau_1\rangle$

• If
$$t = \tau_1$$
. $|E\rangle$

$$\begin{array}{c} \overset{\tau_1}{\longrightarrow} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle \\ & t = \tau_1 \\ & s |\psi\rangle \xrightarrow{\tau_1} s |\tau_1\rangle \xrightarrow{U_{\mathrm{m}}} -cA_1^0 |E\rangle + sA_3^{1'} |\tau_0\rangle + sA_4^{1'} |\tau_1\rangle \end{array}$$

- If
$$|E\rangle$$
 outcome: $\begin{bmatrix} - \text{ If } t = \tau_0. \text{ Clock was off} \\ - \text{ If } t = \tau_1. \text{ No outcome} \end{bmatrix}$

- If
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 outcome: $\begin{bmatrix} - \text{ If } t = \tau_0. \text{ No outcome} \\ - \text{ If } t = \tau_1. \text{ Clock was off} \end{bmatrix}$

Timing of unitaries: no external clock needed

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- Properties:
 - Theorem: One Ancilla $|A\rangle$ is necessary and sufficient in one tick case.
 - Optimal prob. is 1/6

$$c=s=\frac{1}{\sqrt{2}}$$

• Multiple ticks: $|\tau_0\rangle, |\tau_1\rangle, \ldots, |\tau_{N_T}\rangle$

$$\overset{\tau_l}{\longrightarrow} c \left| E \right\rangle \overset{\tau_l}{\longrightarrow} c \left| E \right\rangle \overset{U_{\mathrm{m}}}{\longrightarrow} cA_0^0 \left| E \right\rangle + \sum_{j=1}^{N_T} cA_j^0 \left| \tau_j \right\rangle + cA_{N_T+1}^0(\tau_l) \left| \tau_0 \right\rangle + \sum_{k=1}^m cB_{-1,k} \left| A_k \right\rangle$$

 $|E\rangle$

 $s |\psi\rangle \xrightarrow{\tau_l} s |\tau_l\rangle \xrightarrow{U_{\mathrm{m}}} sA_0^1(\tau_l) |E\rangle + \sum_{j=1}^{N_T} sA_j^1(\tau_l) |\tau_j\rangle + sA_{N_T+1}^1(\tau_l) |\tau_0\rangle + \sum_{k=1}^m sB_{l,k} |A_k\rangle$

• Unitary $U_{\rm m}$:

	$ E\rangle$	$ \tau_1\rangle$	$ \tau_2\rangle$	$ \tau_3\rangle$	 $ au_{N_T}\rangle$	$ au_0\rangle$		$ A_1 angle$		$ A_m angle$
$ E\rangle$	A_{0}^{0}	A_{1}^{0}	A_{2}^{0}	A_3^0	 $A^0_{N_T}$	γ_0	ł	$B_{-1,1}$		$B_{-1,m}$
$ au_1 angle$	0	$-A_{1}^{0} r$	$-A_{2}^{0} r$	$-A_{3}^{0} r$	 $-A^0_{N_T} r$	γ_1	ł	$B_{1,1}$		$B_{1,m}$
$ \tau_2\rangle$	$-A_{0}^{0} r$	0	$-A_{2}^{0} r$	$-A_{3}^{0}r$	 $-A^0_{N_T} r$	γ_2	ł.	$B_{2,1}$		$B_{2,m}$
$ \tau_3\rangle$	$-A_{0}^{0} r$	$-A_{1}^{0} r$	0	$-A_{3}^{0} r$	 $-A^0_{N_T} r$	γ_3	ł	$B_{3,1}$		$B_{3,m}$
÷	:	:	÷	:	:	:		:		÷
$ \tau_{N_T}\rangle$	$-A_{0}^{0} r$	$-A_1^0r$	$-A_2^0 r$	$-A_{3}^{0} r$	 $-A^0_{N_T} r$	γ_{N_T}	ł	$B_{N_T,1}$		$B_{N_T,m}$
$ \tau_0\rangle$	$-A_0^0 r$	$-A_{1}^{0} r$	$-A_{2}^{0} r$	$-A_{3}^{0} r$	 0	γ_{N_T+1}	ł	$B_{N_T+1,1}$		$B_{N_T+1,m}$
$ A_1\rangle$	$B_{N_T+2,0}$	$B_{N_T+2,1}$	$B_{N_T+2,2}$	$B_{N_T+2,3}$	 B_{N_T+2,N_T}	B_{N_T+2,N_T+1}		B_{N_T+2,N_T+2}		B_{N_T+2,N_T+m+1}
÷	÷	÷	÷	÷	:	÷				:
$ A_m\rangle$	$B_{N_T+m+1,0}$	$B_{N_T+m+1,1}$	$B_{N_T+m+1,2}$	$B_{N_T+m+1,3}$	 B_{N_T+m+1,N_T}	B_{N_T+m+1,N_T+}	1	B_{N_T+m+1,N_T+1}	-2 · · ·	B_{N_T+m+1,N_T+m+1}

$$r := c/s$$

Theorem: For all $N_T \in \mathbb{N}$, there exists a solution

Engineered clocks

• Recall: $|\tau_0\rangle, |\tau_1\rangle, \dots, |\tau_{N_T}\rangle$ at times $\tau_0, \tau_1, \dots, \tau_{N_T}$

 $t \in \{\tau_0, \tau_1, \tau_2, \dots, \tau_{N_T}\}$

• Improvement: $|\tau_0\rangle$ for $t \in [0, t_1)$, $|\tau_1\rangle$ for $t \in [t_1, 2t_1)$, ... $|\tau_{N_T}\rangle$ for $t \in [N_T t_1, (N_T + 1)t_1)$.



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Is time Sustantival or Relative?

Assumptions:

(A) Interaction-free measurements exist

(B) If a clock can measure time while switched off, then time is substantival

Theorem: if (A) and (B) hold, then time is substantival

- Alternative interpretations:
 - Many worlds interpretation: in the world we inhabit, the clock was never on, but it was on in another world
 - Implications for substantival theory of time: for time to be of a substantival nature in our world, we need dynamics in another world

Conclusions and open questions: arXiv:2106.07684

- Philosophy of time:
 - Aristotle to present
- Interaction-free measurements:
 - Bomb tester (Elitzur & Vaidman 93, Penrose 94, Kwit et al 95, Hosten et al 06)
 - Counterfactual computation (R. Jozsa 99, G. Mitchilson & R. Jozsa 01)
- Introduced counterfactual clocks:
 - Elementary clocks
 - Type engineered clocks
- Implications for the debate on time: Substantival theory vs Relative theory
 - Our results led support for the substantival theory
- Experimental implementations?
 - Harmonic oscillator?





Using it to tell the time when off

- Analyze protocol:
• If
$$t = \tau_0$$
. $|E\rangle$ $\stackrel{\tau_0}{\longrightarrow} c |E\rangle \stackrel{U_{\rm m}}{\longrightarrow} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
• $t = \tau_0$ \downarrow $t = \tau_0$ \downarrow $t = \tau_0$ \downarrow $cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$

• If
$$t = \tau_1$$
. $|E\rangle \xrightarrow{\tau_1} c |E\rangle \xrightarrow{U_{\mathrm{m}}} cA_1^0 |E\rangle + cA_2^0 |A\rangle + cA_3^0 |\tau_0\rangle + cA_4^0 |\tau_1\rangle$
• $t = \tau_1$
• $s |\psi\rangle \xrightarrow{\tau_1} s |\tau_1\rangle \xrightarrow{U_{\mathrm{m}}} -cA_1^0 |E\rangle + sA_3^{1'} |\tau_0\rangle + sA_4^{1'} |\tau_1\rangle$

- If
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