

Title: Muon g-2: the showdown

Speakers: Massimo Passera

Series: Particle Physics

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Abstract: The Muon g-2 experiment at Fermilab has recently confirmed Brookhaven's earlier measurement of the muon anomalous magnetic moment  $a \approx 10^{-9}$ . This new result increases the discrepancy between the Standard Model (SM) prediction and strengthens its "new physics" interpretation as well as the quest for its underlying origin. In this talk I will review the SM prediction of the muon g-2, focusing on some of the latest developments, and discuss the connection of the discrepancy to precision electroweak predictions via their common dependence on hadronic vacuum polarization effects.

# Muon g-2: the showdown

Massimo Passera  
INFN Padova

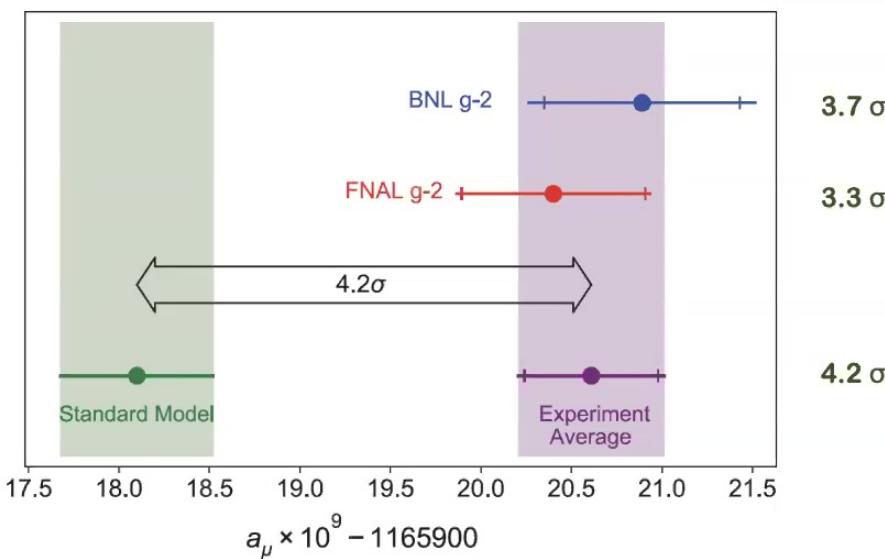
Perimeter Institute  
May 4<sup>th</sup> 2021



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## Muon g-2: FNAL confirms BNL

$\mu$



$$a_\mu^{\text{EXP}} = (116592089 \pm 63) \times 10^{-11} [0.54\text{ppm}] \quad \text{BNL E821}$$

$$a_\mu^{\text{EXP}} = (116592040 \pm 54) \times 10^{-11} [0.46\text{ppm}] \quad \text{FNAL E989 Run 1}$$

$$a_\mu^{\text{EXP}} = (116592061 \pm 41) \times 10^{-11} [0.35\text{ppm}] \quad \text{WA}$$

- FNAL aims at  $16 \times 10^{-11}$ . First 3 runs completed, 4th in progress.
- Muon g-2 proposal at J-PARC: Phase-1 with  $\sim$  BNL precision.

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- ⌚ Muon g-2: the Standard Model prediction
- ⌚ Muon g-2  $\iff$   $\Delta\alpha$  connection
- ⌚ The MUonE project



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## Muon g-2: the Standard Model prediction

WP20 = White Paper of the Muon g-2 Theory Initiative: arXiv:2006.04822

## Muon g-2: the QED contribution

$\mu$

$$a_{\mu}^{\text{QED}} = (1/2)(\alpha/\pi)$$

Schwinger 1948

$$+ 0.765857426 (16) (\alpha/\pi)^2$$

Sommerfield; Petermann; Suura&Wichmann '57; Elend '66; MP '04

$$+ 24.05050988 (28) (\alpha/\pi)^3$$

Remiddi, Laporta, Barbieri ... ; Czarnecki, Skrzypek '99; MP '04;  
Friot, Greynat & de Rafael '05, Ananthanarayan, Friot, Ghosh 2020

$$+ 130.8780 (60) (\alpha/\pi)^4$$

Kinoshita & Lindquist '81, ... , Kinoshita & Nio '04, '05;  
Aoyama, Hayakawa, Kinoshita & Nio, 2007, Kinoshita et al. 2012 & 2015;  
Steinhauser et al. 2013, 2015 & 2016 (all electron &  $\tau$  loops, analytic);  
Laporta, PLB 2017 (mass independent term) **COMPLETED!**

$$+ 750.86 (88) (\alpha/\pi)^5 \text{ COMPLETED!}$$

Kinoshita et al. '90, Yelkhovsky, Milstein, Starshenko, Laporta, ...

Aoyama, Hayakawa, Kinoshita, Nio 2012, 2015, 2017 & 2019.

Volkov 1909.08015:  $A_1^{(10)}$ [no lept loops] at variance, but negligible  $\delta a_{\mu} \sim 6 \times 10^{-14}$

**Adding up, we get:**

$$a_{\mu}^{\text{QED}} = 116584718.931 (19)(100)(23) \times 10^{-11}$$

mainly from 4-loop coeff. unc. ↗ 6-loop ↘ from  $\alpha(\text{Cs})$

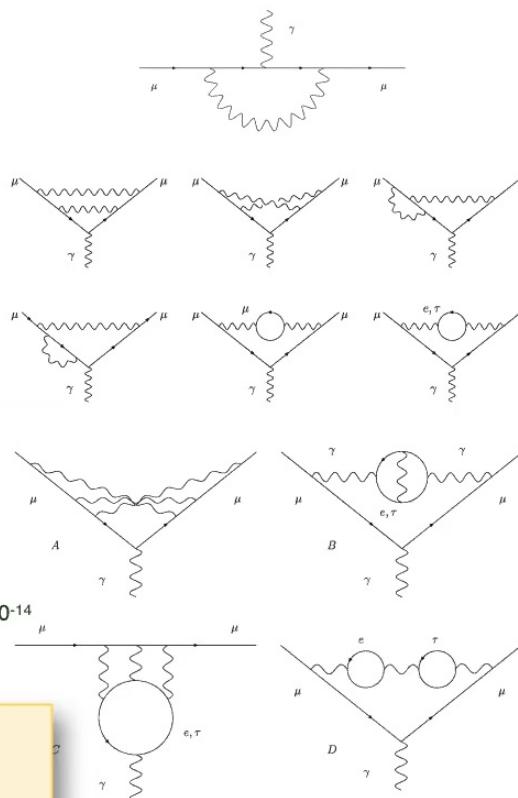
$\alpha = 1/137.035999046(27)$  [0.2ppb] Parker et al 2018

WP20 value

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Shift down in  $a_{\mu}^{\text{QED}} \sim 1.4 \times 10^{-12}$  with new LKB Paris  $\alpha(\text{Rb})$  value (Morel et al 2020)

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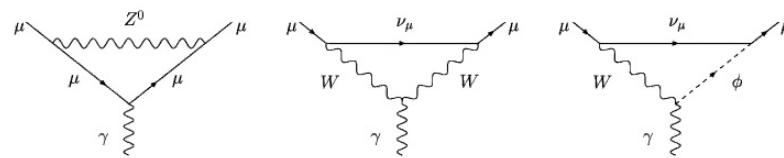


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## The electroweak contribution

$\mu$

- One-loop term:



$$a_\mu^{\text{EW}}(\text{1-loop}) = \frac{5G_\mu m_\mu^2}{24\sqrt{2}\pi^2} \left[ 1 + \frac{1}{5} (1 - 4 \sin^2 \theta_W)^2 + O\left(\frac{m_\mu^2}{M_{Z,W,H}^2}\right) \right] \approx 195 \times 10^{-11}$$

1972: Jackiw, Weinberg; Bars, Yoshimura; Altarelli, Cabibbo, Maiani; Bardeen, Gastmans, Lautrup; Fujikawa, Lee, Sanda; Studenikin et al. '80s

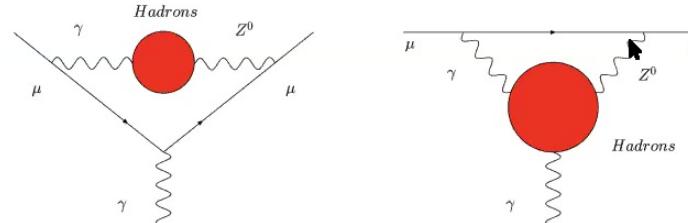
- One-loop plus higher-order terms:

$a_\mu^{\text{EW}} = 153.6 (1.0) \times 10^{-11}$

Hadronic loop uncertainties (and 3-loop nonleading logs).

WP20 value

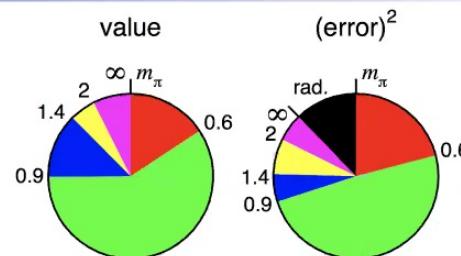
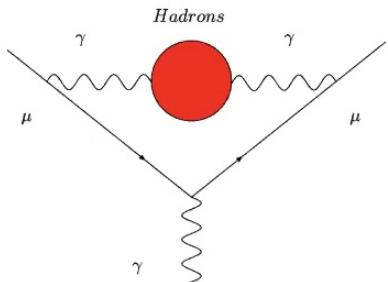
Kukhto et al. '92; Czarnecki, Krause, Marciano '95; Knecht, Peris, Perrottet, de Rafael '02; Czarnecki, Marciano and Vainshtein '02; Degrassi and Giudice '98; Heinemeyer, Stockinger, Weiglein '04; Gribouk and Czarnecki '05; Vainshtein '03; Gnendiger, Stockinger, Stockinger-Kim 2013, Ishikawa, Nakazawa, Yasui, 2019.



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$\mu$

## The hadronic LO contribution



Keshavarzi, Nomura, Teubner 2018

$$a_\mu^{\text{HLO}} = \frac{1}{4\pi^3} \int_{m_\pi^2}^\infty ds K(s) \sigma_{\text{had}}^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2 (1-x)}{x^2 + (1-x) (s/m_\mu^2)}$$

$a_\mu^{\text{HLO}} = 6895 (33) \times 10^{-11}$

F. Jegerlehner, arXiv:1711.06089

$= 6939 (40) \times 10^{-11}$

Davier, Hoecker, Malaescu, Zhang, arXiv:1908.00921

$= 6928 (24) \times 10^{-11}$

Keshavarzi, Nomura, Teubner, arXiv:1911.00367

$= 6931 (40) \times 10^{-11} (0.6\%)$

WP20 value

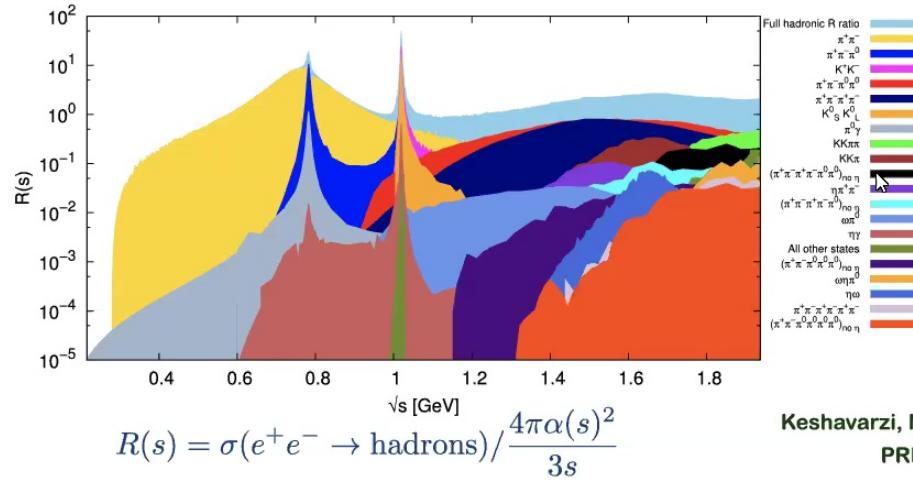
WP20 value obtained conservatively DHMZ + KNT + constraints from CHHKS  
Colangelo, Hoferichter, Hoid, Kubis, Stoffer 2018-19

Radiative Corrections to  $\sigma(s)$  are crucial. S. Actis et al, Eur. Phys. J. C66 (2010) 585

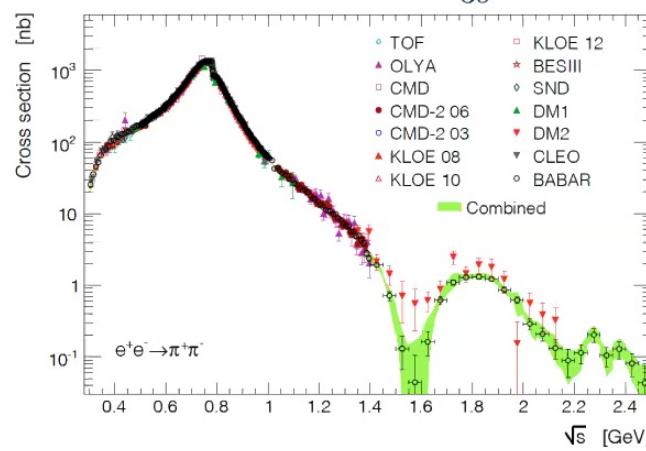


$\mu$

## The low-energy hadronic cross section



Keshavarzi, Nomura Teubner  
PRD 2018



Davier, Hoecker, Malaescu, Zhang  
EPJC 2020

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## The hadronic LO contribution from lattice QCD

$\mu$

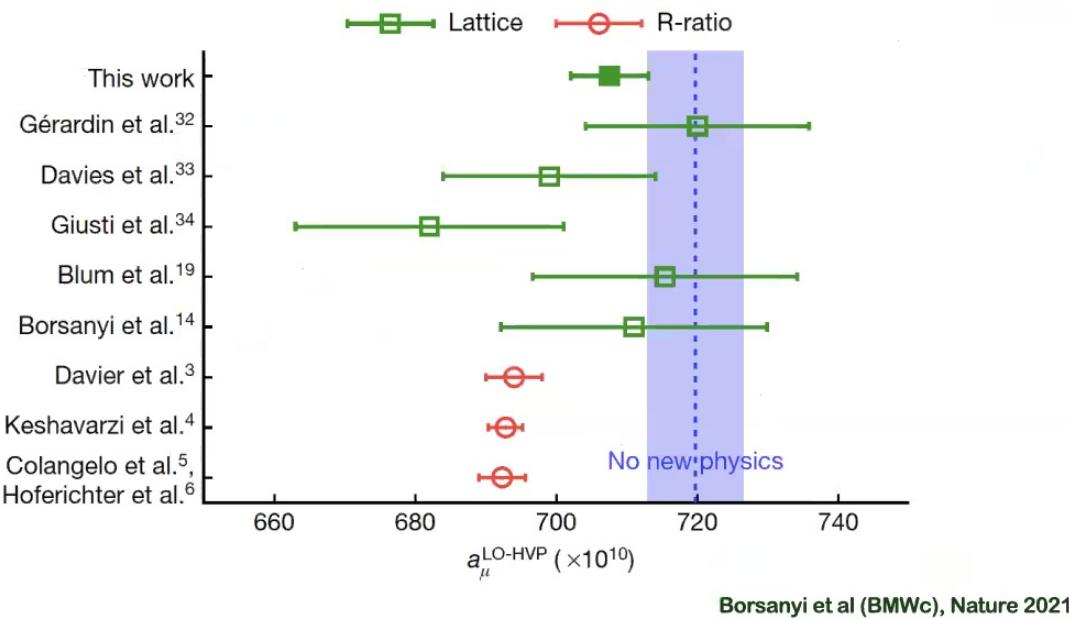


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- Great progress in lattice QCD results. The BMW collaboration reached 0.8% precision:

$$a_\mu^{\text{HLO}} = 7075(23)_{\text{stat}}(50)_{\text{syst}} [55]_{\text{tot}} \times 10^{-11}$$

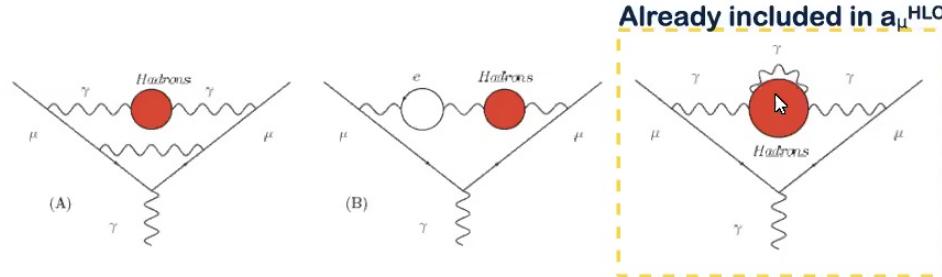
- 2–2.5 $\sigma$  tension with the dispersive evaluations. BMW collaboration 2021



$\mu$

## The hadronic HO VP contribution

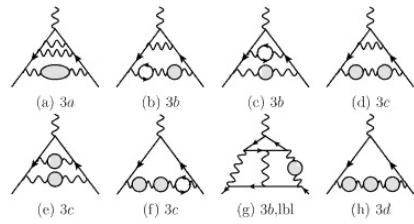
- $O(\alpha^3)$  contributions of diagrams containing HVP insertions:



$$a_\mu^{\text{HNLO(vp)}} = -98.3(7) \times 10^{-11}$$

Krause '96; Keshavarzi, Nomura, Teubner 2019; WP20.

- $O(\alpha^4)$  contributions of diagrams containing HVP insertions:



$$a_\mu^{\text{HNNLO(vp)}} = 12.4(1) \times 10^{-11}$$

Kurz, Liu, Marquard, Steinhauser 2014

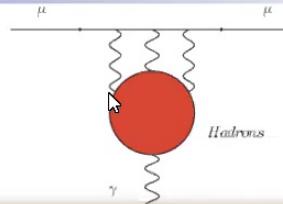
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## The hadronic LbL contribution

$\mu$

- Hadronic light-by-light at  $O(\alpha^3)$

💡 This term had a troubled life! But nowadays:



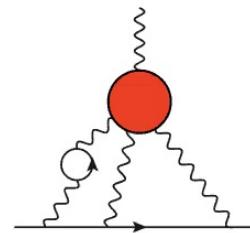
$$\begin{aligned} a_\mu^{\text{HNLO(Lbl)}} &= 80(40) \times 10^{-11} && \text{Knecht \& Nyffeler '02} \\ &= 136(25) \times 10^{-11} && \text{Melnikov \& Vainshtein '03} \\ &= 105(26) \times 10^{-11} && \text{Prades, de Rafael, Vainshtein '09} \\ &= 100(29) \times 10^{-11} && \text{Jegerlehner, arXiv:1705.00263} \\ &= 92(19) \times 10^{-11} && \text{WP20 (phenomenology)} \end{aligned}$$

💡 Significant improvements due to data-driven dispersive approach.  
Colangelo, Hoferichter, Procura, Stoffer, 2014–17; Pauk, Vanderhaeghen 2014.  
💡 Lattice: RBC:  $82(35)\times 10^{-11}$  1911.08123 Mainz:  $110(15)\times 10^{-11}$  2104.02632

- Hadronic light-by-light at  $O(\alpha^4)$

$$a_\mu^{\text{HNNLO(Lbl)}} = 2(1) \times 10^{-11}$$

Colangelo, Hoferichter, Nyffeler, MP, Stoffer 2014; WP20



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## Muon g-2: the discrepancy

$\mu$



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Comparing the SM prediction with the measured muon g-2 value:

$$a_{\mu}^{\text{EXP}} = 116592061 (41) \times 10^{-11}$$

BNL+FNAL

$$a_{\mu}^{\text{SM}} = 116591810 (43) \times 10^{-11}$$

WP20

$$\Delta a_{\mu} = a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}} = 251 (59) \times 10^{-11}$$

4.2  $\sigma$

Is  $\Delta a_{\mu}$  due to new physics <sup>↗</sup> beyond the SM? Could be due to:

- NP at the weak scale and weakly coupled to SM particles
- NP very heavy and strongly coupled to SM particles
- NP very light ( $\Lambda \lesssim 1$  GeV) and feebly coupled to SM particles



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## Muon g-2 $\leftrightarrow$ $\Delta\alpha$ connection

Marciano, MP, Sirlin 2008 & 2010

Keshavarzi, Marciano, MP, Sirlin 2020



## Missed contributions in the hadronic cross section?

$\Delta a$



- Can  $\Delta a_\mu$  be due to **missing contributions** in the hadronic  $\sigma(s)$ ?
- An upward shift of  $\sigma(s)$  also induces an increase of  $\Delta a_{\text{had}}^{(5)}(M_Z)$ .
- Consider:  $\rightarrow$

$$\begin{aligned} a_\mu^{\text{HLO}} \rightarrow & \quad a = \int_{4m_\pi^2}^{s_u} ds f(s) \sigma(s), \quad f(s) = \frac{K(s)}{4\pi^3}, \quad s_u < M_Z^2, \\ \Delta a_{\text{had}}^{(5)} \rightarrow & \quad b = \int_{4m_\pi^2}^{s_u} ds g(s) \sigma(s), \quad g(s) = \frac{M_Z^2}{(M_Z^2 - s)(4\alpha\pi^2)}, \end{aligned}$$

and the increase

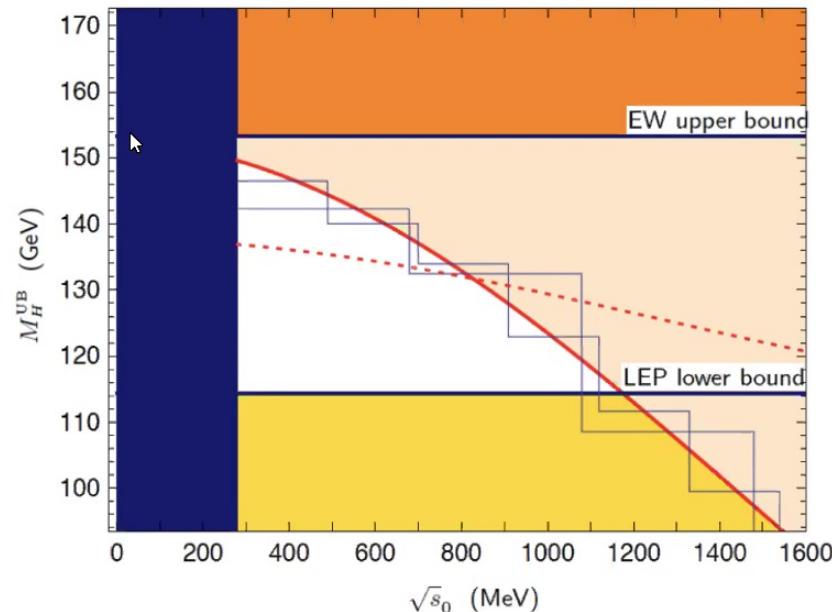
$$\Delta\sigma(s) = \epsilon\sigma(s)$$

$\epsilon > 0$ , in the range:

$$\sqrt{s} \in [\sqrt{s_0} - \delta/2, \sqrt{s_0} + \delta/2] \quad \longrightarrow$$

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How much does the  $M_H$  upper bound from the EW fit change when we shift up  $\sigma(s)$  by  $\Delta\sigma(s)$  [and thus  $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$ ] to fix  $\Delta\alpha_\mu$ ?



Marciano, MP, Sirlin, PRD 2008

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## Muon g-2: connection with the SM Higgs mass (update)

$\Delta\alpha$

**Major update: Higgs discovered, improved EW observables  
( $M_W$ ,  $\sin^2\theta$ ,  $M_{top}$ , ...), updates to  $\sigma(s)$ , theory improvements, global fit, ...**



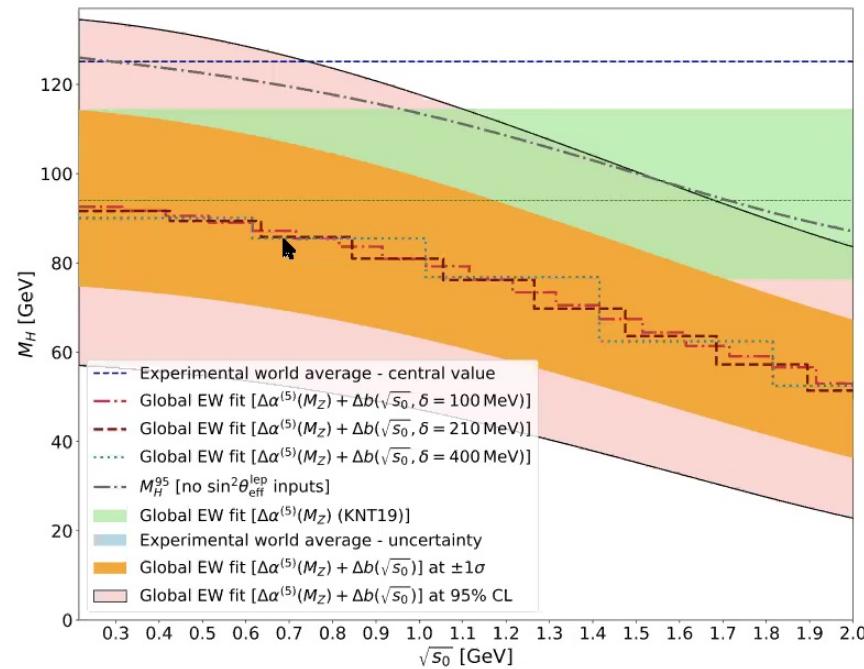
Parameter	Input value	Reference	Fit result	Result w/o input value
$M_W$ (GeV)	80.379(12)	[5]	80.359(3)	80.357(4)(5)
$M_H$ (GeV)	125.10(14)	[5]	125.10(14)	$94^{+20+6}_{-18-6}$
$\Delta\alpha_{had}^{(5)}(M_Z^2) \times 10^4$	276.1(1.1)	[23]	275.8(1.1)	272.2(3.9)(1.2)
$m_t$ (GeV)	172.9(4)	[5]	173.0(4)	...
$\alpha_s(M_Z^2)$	0.1179(10)	[5]	0.1180(7)	...
$M_Z$ (GeV)	91.1876(21)	[5]	91.1883(20)	...
$\Gamma_Z$ (GeV)	2.4952(23)	[5]	2.4940(4)	...
$\Gamma_W$ (GeV)	2.085(42)	[5]	2.0903(4)	...
$\sigma_{had}^0$ (nb)	41.541(37)	[108]	41.490(4)	...
$R_l^0$	20.767(25)	[108]	20.732(4)	...
$R_c^0$	0.1721(30)	[108]	0.17222(8)	...
$R_b^0$	0.21629(66)	[108]	0.21581(8)	...
$\bar{m}_c$ (GeV)	1.27(2)	[5]	1.27(2)	...
$\bar{m}_b$ (GeV)	$4.18^{+0.03}_{-0.02}$	[5]	$4.18^{+0.03}_{-0.02}$	...
$A_{FB}^{0,l}$	0.0171(10)	[108]	0.01622(7)	...
$A_{FB}^{0,c}$	0.0707(35)	[108]	0.0737(2)	...
$A_{FB}^{0,b}$	0.0992(16)	[108]	0.1031(2)	...
$A_\ell'$	0.1499(18)	[75,108]	0.1471(3)	...
$A_c$	0.670(27)	[108]	0.6679(2)	...
$A_b$	0.923(20)	[108]	0.93462(7)	...
$\sin^2\theta_{eff}^{lep}(Q_{FB})$	0.2324(12)	[108]	0.23152(4)	0.23152(4)(4)
$\sin^2\theta_{eff}^{lep}(\text{Had Coll})$	0.23140(23)	[100]	0.23152(4)	0.23152(4)(4)

Keshavarzi, Marciano, MP, Sirlin, PRD 2020 (using Gfitter)



## Muon g-2: connection with the SM Higgs mass (2020)

$\Delta\alpha$



Shifts  $\Delta\sigma(s)$  to fix  $\Delta\alpha_\mu$  are possible,  
but conflict with the EW fit if they occur above  $\sim 1$  GeV

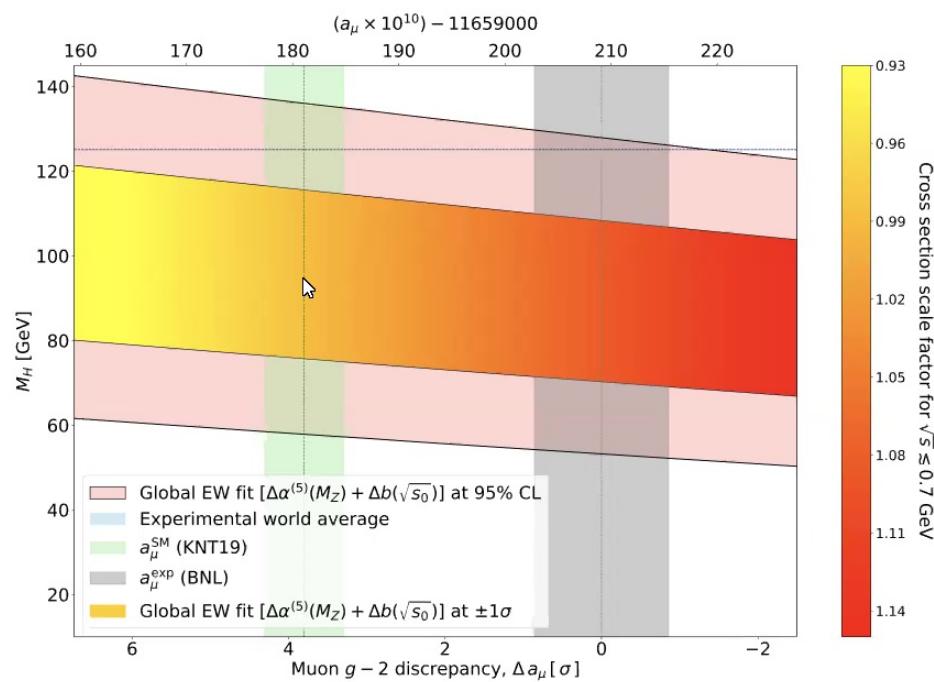
Keshavarzi, Marciano, MP, Sirlin, PRD 2020

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## The muon g-2: connection with the SM Higgs mass (2020) - II

$\Delta\alpha$



Uniform scaling of  $\sigma(s)$  below  $\sim 0.7 \text{ GeV}$ ? +9% required!

Keshavarzi, Marciano, MP, Sirlin, PRD 2020

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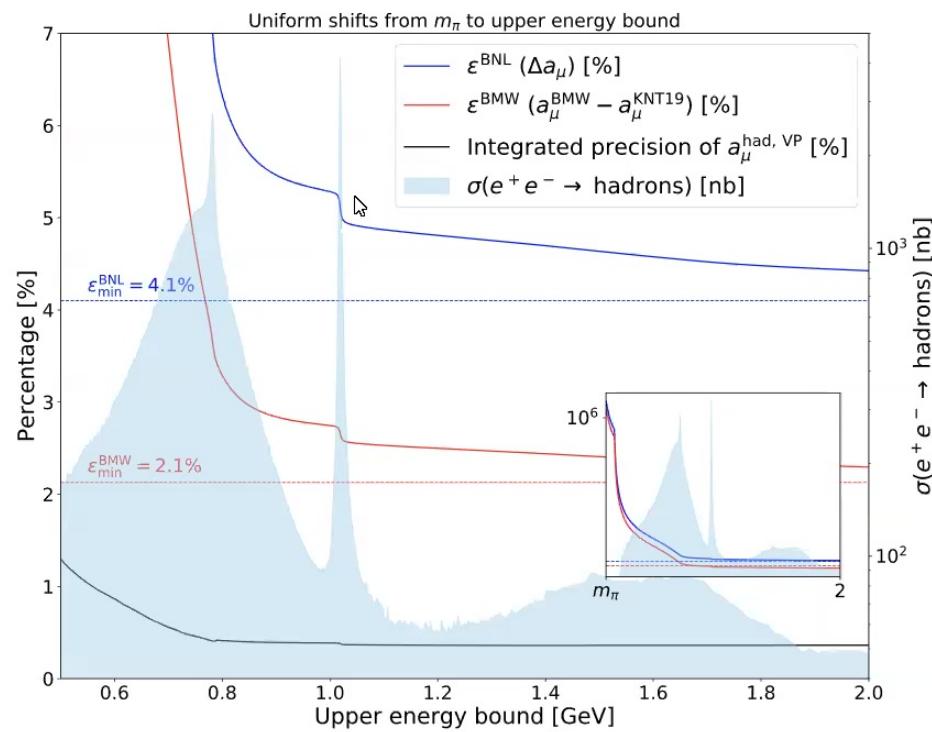
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## How large are the required shifts $\Delta\sigma(s)$ ?

$\Delta\alpha$



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Shifts below  $\sim 1$  GeV conflict with the quoted exp. precision of  $\sigma(s)$

Keshavarzi, Marciano, MP, Sirlin, PRD 2020 (updated 2021)

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## What happens to the electron g-2?

## The electron g-2 no longer provides the best value of $\alpha$

e



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- The 2008 measurement of the electron g-2 is:

$$a_e^{\text{EXP}} = 11596521807.3 \text{ (2.8)} \times 10^{-13} \quad \text{Hanneke et al, PRL100 (2008) 120801}$$

vs. old (factor of 15 improvement,  $1.8\sigma$  difference):

$$a_e^{\text{EXP}} = 11596521883 \text{ (42)} \times 10^{-13} \quad \text{Van Dyck et al, PRL59 (1987) 26}$$

- Equate  $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$  → “ $g_e\text{-2}$ ” determination of alpha:

$$\alpha^{-1} = 137.035\ 999\ 151 \text{ (33)} \quad [0.24 \text{ ppb}]$$

- The best determination of  $\alpha$  is obtained via atomic interferometry:

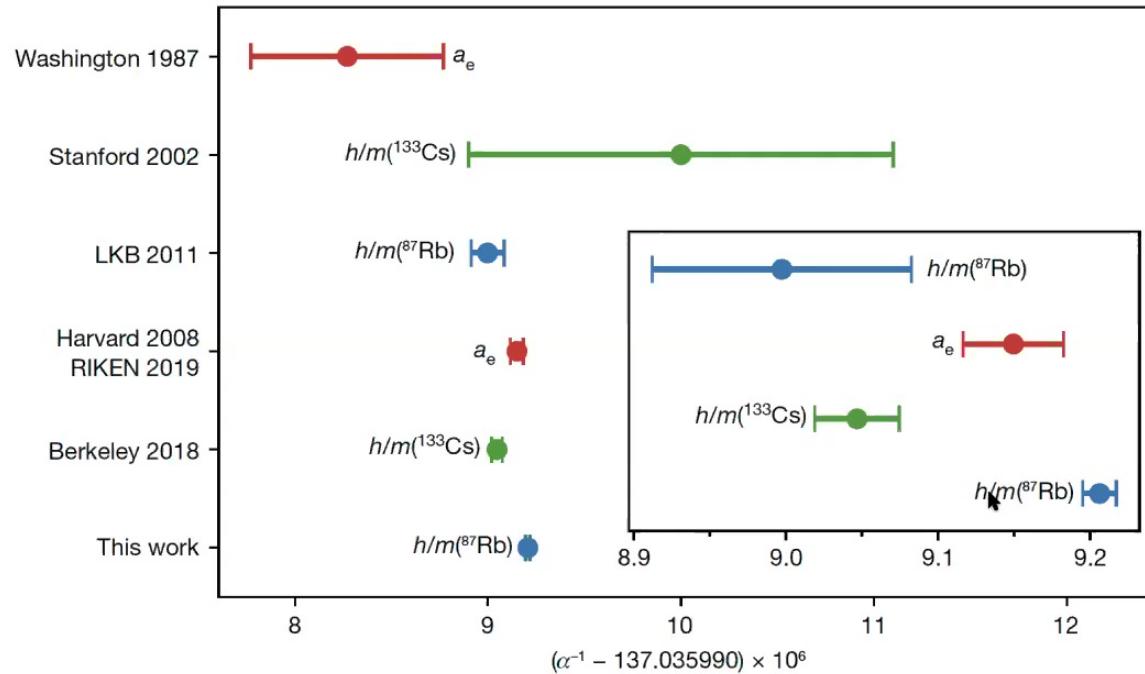
$$\alpha^{-1} = 137.035\ 999\ 046 \text{ (27)} [0.20 \text{ ppb}] \quad \text{Parker et al, Science 360 (2018) 192 (Cs)}$$

$$\alpha^{-1} = 137.035\ 999\ 206 \text{ (11)} [0.08 \text{ ppb}] \quad \text{Morel et al, Nature 588 (2020) 61 (Rb)}$$

2018→2020: improvement in precision, but  $5.4\sigma$  difference!

e

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Morel et al, Nature 588 (2020) 61

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## Electron g-2: SM vs experiment

e



- Using the best determinations of  $\alpha$  (which differ by  $5.4\sigma!$ ):

$$\alpha = 1/137.035\ 999\ 046\ (27) \text{ [Cs 2018]}$$

$$\alpha = 1/137.035\ 999\ 206\ (11) \text{ [Rb 2020]}$$

$$\begin{aligned} a_e^{\text{SM}} &= 115\ 965\ 218\ 16.16\ (0.11)\ (0.08)\ (2.28) \times 10^{-13} \text{ [Cs18]} \\ &= 115\ 965\ 218\ 02.64\ (0.11)\ (0.08)\ (0.93) \times 10^{-13} \text{ [Rb20]} \end{aligned}$$

$\delta C_5^{\text{qed}}$     $\delta a_e^{\text{had}}$    from  $\delta \alpha$

$$a_e^{\text{EXP}} = 115\ 965\ 218\ 07.3\ (2.8) \times 10^{-13} \quad \text{Hanneke et al, PRL 2008}$$

- The (EXP – SM) difference is:

$$\begin{aligned} \Delta a_e &= a_e^{\text{EXP}} - a_e^{\text{SM}} = -8.9\ (3.6) \times 10^{-13} \text{ [2.5}\sigma\text{] [Cs18]} \\ &\quad + 4.7\ (3.0) \times 10^{-13} \text{ [1.6}\sigma\text{] [Rb20]} \end{aligned}$$

QED 5-loop:  $a_e^{\text{QED5}} = 4.6 \times 10^{-13}$

- NP sensitivity limited only by the experimental errors in  $\alpha$  and  $a_e$ .  
May soon play a pivotal role in probing NP in the leptonic sector.

## Testing new physics with the electron g-2

e



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- Using  $\alpha(Rb2020)$ , the sensitivity is  $\delta\Delta a_e = 3.0 \times 10^{-13}$ , ie ( $\times 10^{-13}$ ):

$$\underbrace{(0.1)_{QED5}, (0.1)_{HAD}, (0.9)_{\delta\alpha}}_{(0.2)_{TH}}, (2.8)_{\delta a_e^{\text{EXP}}}$$

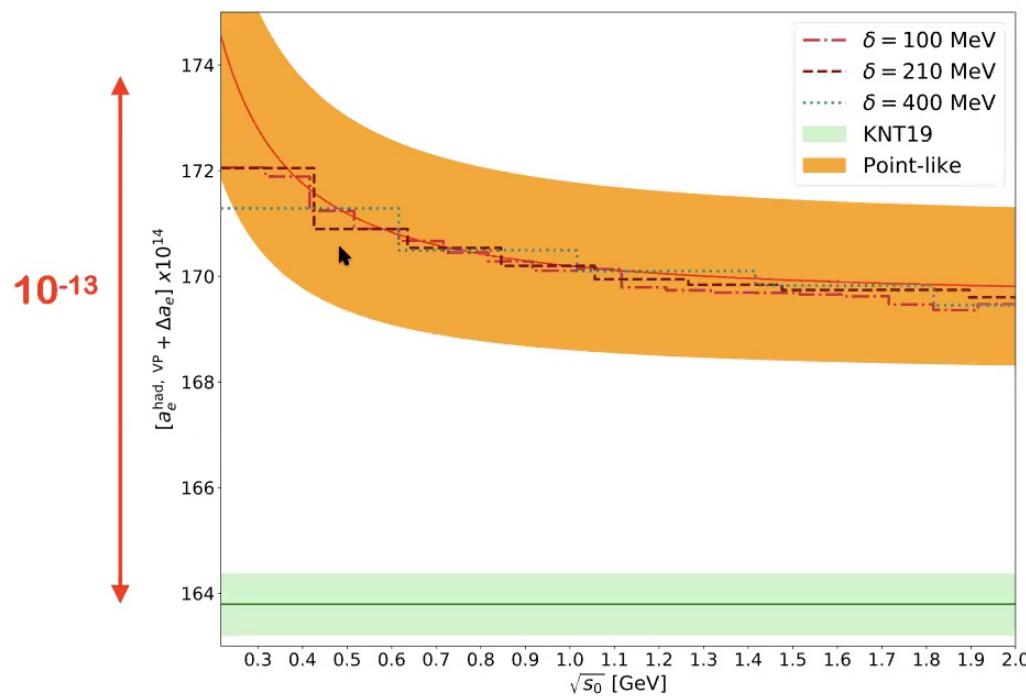
- The  $(g-2)_e$  experimental error may soon drop below  $10^{-13} \rightarrow a_e$  sensitivity below  $10^{-13}$  may soon be reached!
- In a broad class of BSM theories, contributions to  $a_l$  scale as

$$\frac{\Delta a_{\ell_i}}{\Delta a_{\ell_j}} = \left( \frac{m_{\ell_i}}{m_{\ell_j}} \right)^2 \quad \text{This Naive Scaling leads to:}$$

$$\Delta a_e = \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}; \quad \Delta a_\tau = \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.8 \times 10^{-6}$$

Giudice, Paradisi & MP, JHEP 2012

## Shift of the electron g-2



Shifts  $\Delta\sigma(s)$  to fix  $\Delta a_\mu$  only slightly change  $\Delta a_e$

Keshavarzi, Marciano, MP, Sirlin, PRD 2020

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e

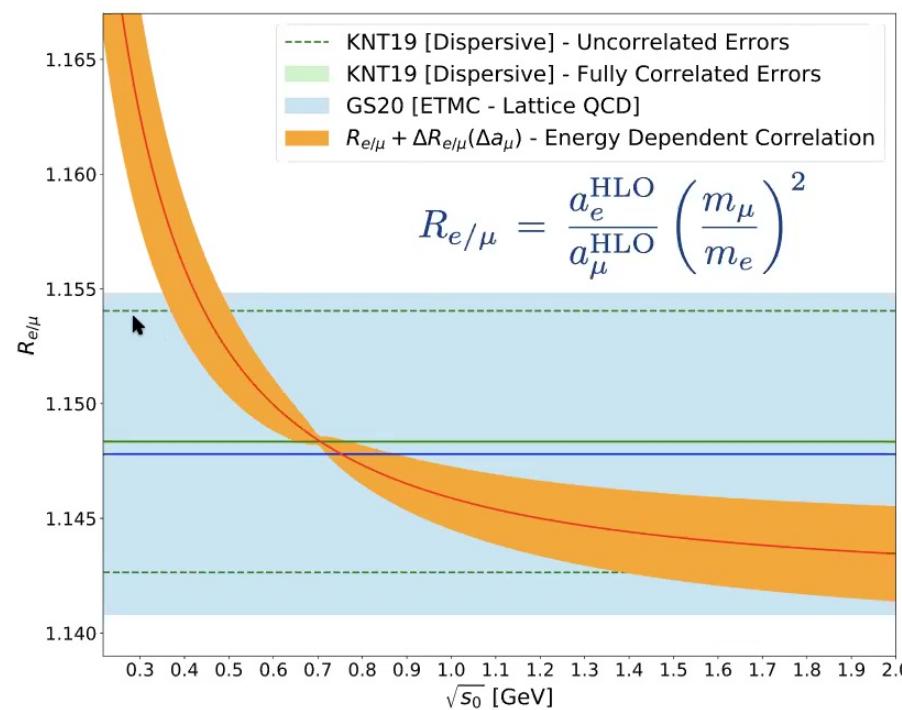


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## Shift of the $e/\mu$ g-2 scaled HLO ratio

$e/\mu$

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Good agreement between lattice [Giusti & Simula 2020] and KNT19.  
Possible future bounds on very low energy shifts  $\Delta\sigma(s)$ ?

Keshavarzi, Marciano, MP, Sirlin, PRD 2020

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- Crivellin, Hoferichter, Manzari and Montull, “Hadronic vacuum polarization:  $(g-2)_\mu$  versus global electroweak fits,” arXiv:2003.04886.
- Eduardo de Rafael, “On Constraints Between  $\Delta a_{had}(M^2)$  and  $(g_\mu-2)_{HVP}$ ,” arXiv:2006.13880.
- Malaescu and Schott, “Impact of correlations between  $a_\mu$  and  $a_{QED}$  on the EW fit,” arXiv:2008.08107.
- Colangelo, Hoferichter and Stoffer, “Constraints on the two-pion contribution to hadronic vacuum polarization,” arXiv:2010.07943.



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## The MUonE project



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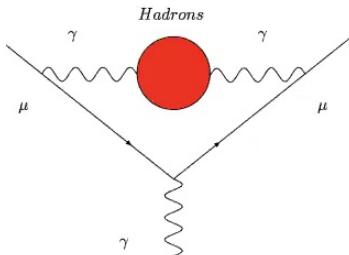
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## Spacelike proposal for $a_\mu^{\text{HLO}}$



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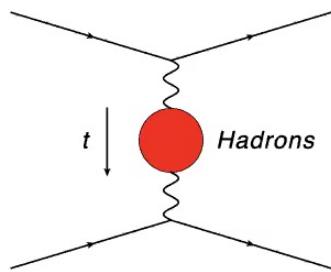
- The leading hadronic contribution  $a_\mu^{\text{HLO}}$  computed via the **timelike** formula:



$$a_\mu^{\text{HLO}} = \frac{1}{4\pi^3} \int_{m_\pi^2}^{\infty} ds K(s) \sigma_{\text{had}}^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2 (1-x)}{x^2 + (1-x)(s/m_\mu^2)}$$

- Alternatively, simply exchanging the  $x$  and  $s$  integrations:



$$a_\mu^{\text{HLO}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)]$$

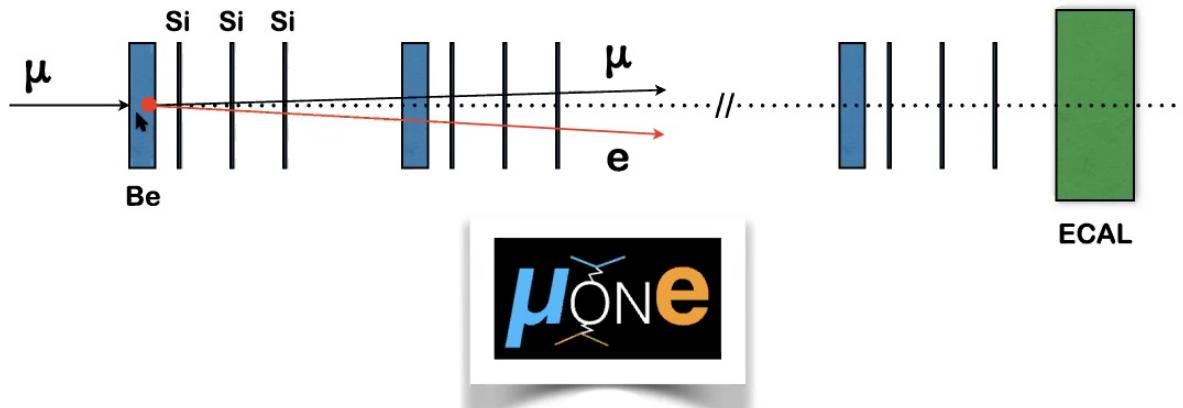
$$t(x) = \frac{x^2 m_\mu^2}{x-1} < 0$$

Lautrup, Peterman, de Rafael, 1972

$\Delta\alpha_{\text{had}}(t)$  is the hadronic contribution to the running of  $\alpha$  in the **spacelike** region:  $a_\mu^{\text{HLO}}$  can be extracted from scattering data!



- $\Delta\alpha_{had}(t)$  can be measured via the elastic scattering  $\mu e \rightarrow \mu e$ .
- We propose to scatter a 150 GeV muon beam, available at CERN's North Area, on a fixed electron target (Beryllium). Modular apparatus: each station has one layer of Beryllium (target) followed by several thin Silicon strip detectors.



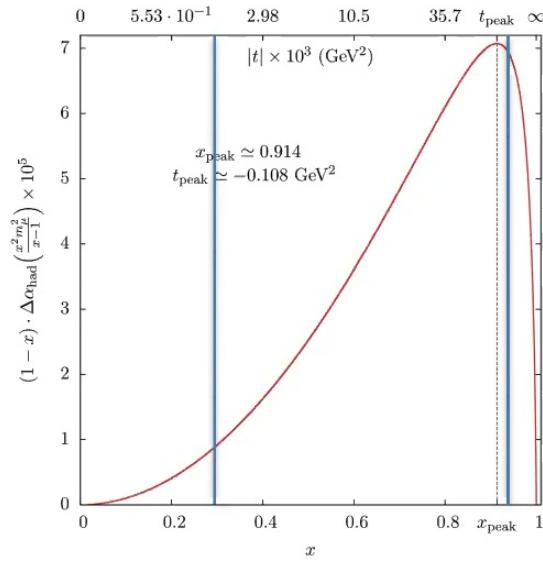
Abbiendi, Carloni Calame, Marconi, Matteuzzi, Montagna,

Nicrosini, MP, Piccinini, Tenchini, Trentadue, Venanzoni

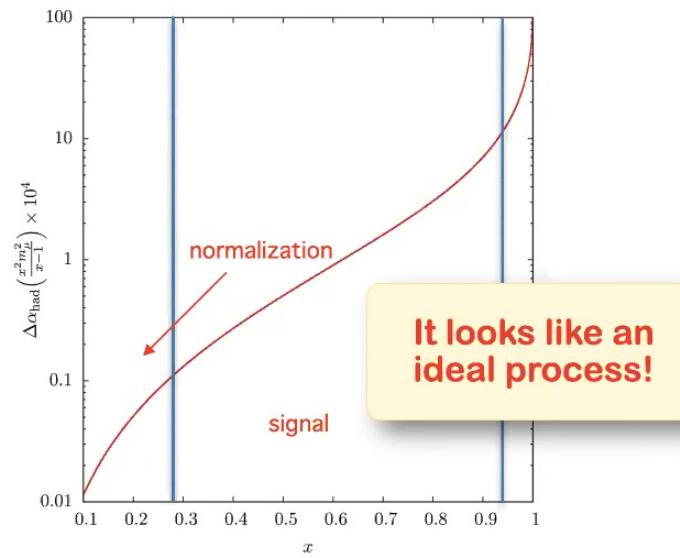
EPJC 2017 - arXiv:1609.08987

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- For a 150 GeV muon beam ( $\sqrt{s} \sim 400$  MeV), MUonE's scan region extends up to  $x=0.932$ , ie beyond the peak! (the peak is at  $x=0.914$ )
- The high-energy region inaccessible to MUonE contributes only 13% of  $a_\mu^{\text{HLO}}$  integral. It can be determined with timelike data and/or lattice QCD results. Already obtained via lattice QCD! Giusti&Simula and Marinkovic&Cardoso 2019



M Passera PI May 4th 2021



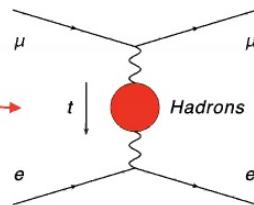
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- **Statistics:** With CERN's 150 GeV muon beam M2 ( $1.3 \times 10^7 \mu/\text{s}$ ), incident on 40 15mm Be targets (total thickness 60cm), 2-3 years of data taking ( $2 \times 10^7 \text{ s/yr}$ ) →  $\mathcal{L}_{\text{int}} \sim 1.5 \times 10^7 \text{ nb}^{-1}$ .
- With this  $\mathcal{L}_{\text{int}}$  we estimate that measuring the shape of  $d\sigma/dt$  we can reach a statistical sensitivity of ~0.3% on  $a_{\mu}^{\text{HLO}}$ , ie  $\sim 20 \times 10^{-11}$ .
- **Systematic** effects must be known at  $\leq 10\text{ppm}!$
- Test beams performed at CERN in 2017 & 2018 arXiv:1905.11677, 2102.11111
- Lol submitted to CERN SPSC in 2019: **Test run approved for 2021.**
- Full-statistics run hopefully in 2022–24.



- To extract  $\Delta\alpha_{\text{had}}(t)$  from MUonE's measurement, the ratio of the SM cross sections in the signal and normalisation regions must be known at  $\leq 10\text{ppm}$ !



- Fully differential fixed-order MC @ NLO ready Pavia and PSI 2018-19
- NNLO QED: Master Integrals for 2-loop box diagrams computed. Full 2-loop amplitude close to completion. Padova 2017 - present
- Two MC built including partial subsets of the NNLO QED corrections due to electron and muon radiation Pavia and PSI 2020
- NNLO hadronic effects computed Padova and KIT 2019
- Extraction of the leading electron mass effects from the massless muon-electron scattering amplitudes PSI 2019-present
- New Physics extracting  $\Delta\alpha_{\text{had}}(t)$  at MUonE? Padova and Heidelberg 2020
- ...

Theory for muon-electron scattering @ 10 ppm:  
A report of the MUonE theory initiative. arXiv:2004.13663

## MUonE — Theory workshops



Padova  
Europe/Rome timezone

### Muon-electron scattering: Theory kickoff workshop

4-5 September 2017

[Overview](#)  
[Venue](#)  
[Timetable](#)  
[Logistic](#)  
[Map](#)

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**MUonE theory workshops: Padova 2017, Mainz 2018, Zurich 2019**  
**Next MUonE theory workshop: MITP Mainz 2020-21 postponed to 2022**

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## Conclusions



- ➊ Fermilab's Muon g-2 experiment confirms BNL's result.
- ➋ The discrepancy between experiment and SM increased to  $4.2\sigma$ .
- ➌ The BMWc lattice QCD result weakens the exp-SM discrepancy.  
It must be confirmed or refuted by other lattice calculations.
- ➍ Is the present  $\Delta a_\mu$  discrepancy due to missed contributions in the hadronic  $\sigma(s)$ ?  
  
Shifts  $\Delta\sigma(s)$  to fix  $\Delta a_\mu$  conflict with the global EW fit above  $\sim 1$  GeV  
Shifts below  $\sim 1$  GeV conflict with the quoted exp. error of  $\sigma(s)$ .
- ➎ Leading hadronic contribution to  $a_\mu$ : dispersive vs lattice?  
**MUonE** will provide a new independent & alternative determination