Title: Ripples in Spacetime from broken SUSY

Speakers: Diego Redigolo

Series: Particle Physics

Date: March 02, 2021 - 1:00 PM

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Abstract: If we live in a supersymmetric world, SUSY has to be broken at some (high) scale. I will show how the presence of a SUSY-breaking hidden sector can lead to gravitational wave (GW) signals at future interferometers. I will focus on first order phase transitions that can occur along the pseudomodulus universally related to SUSY breaking. Current bounds on the superpartners are compatible with GW signals at future interferometers, while the observation of a GW signal from a SUSY-breaking hidden sector would imply superpartners within the reach of future colliders. Along the way, I will analyze the new field theoretical features of the phase transition along the pseudomodulus direction. These allow us to pinpoint what are the necessary requirements for a SUSY-breaking hidden sector to lead to strong GW signals.

Ripples in Spacetime from broken SUSY

Perimeter Institute

Tuesday March 2nd

Diego Redigolo

work based on

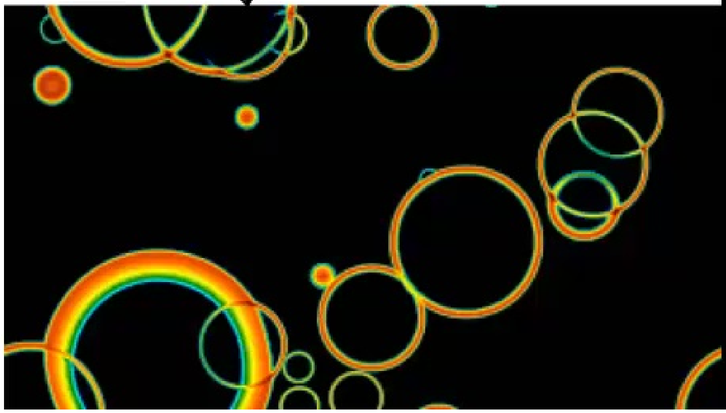
2011.13949 [hep-ph] with N. Craig, A. Mariotti and N. Levi

How we will discover SUSY?

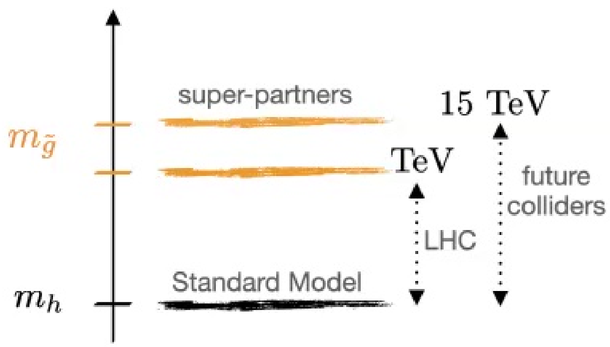
This talk is going to be a journey which starts from this first (vintage) question

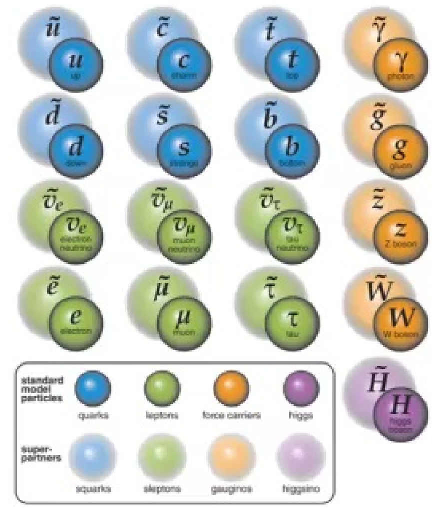
and ends up saying something new about a second (yet-to-be-defined) question

Which QFTs give rise to Gravitational Waves?



How we did not discover natural SUSY

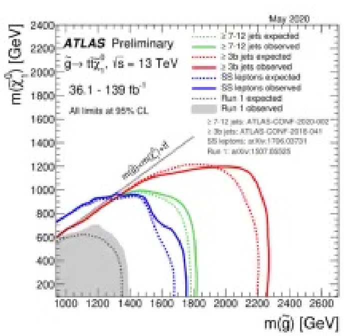




A purely collider perspective on SUSY
has the super-partner scale as a target

and the naturalness of the EW scale
as main motivation

$$m_{\tilde{g}} \lesssim 1 \text{ TeV} \left(\frac{\Delta_h^{-1}}{1\%}\right)^{*} \ldots \qquad \Delta_h \equiv \frac{\delta m_h^2}{m_h^2}$$



LHC results
call into question this perspective

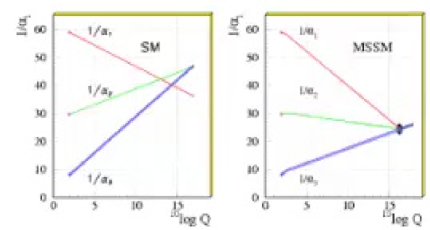
* The gluino mass is a robust proxy
for the LHC and FCC-hh reaches

Which SUSY ?

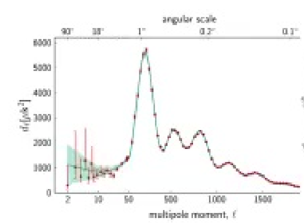
Putting the mystery of the EW scale aside

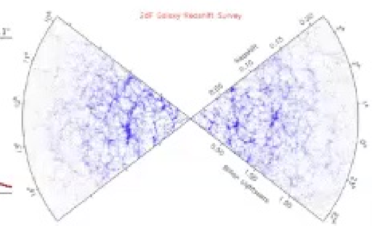
A SUSY Universe at high energies will still be welcome:

perturbative gauge coupling unification

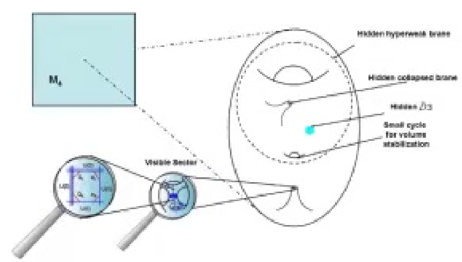


Dark Matter candidates: WIMPs, gravitino, …



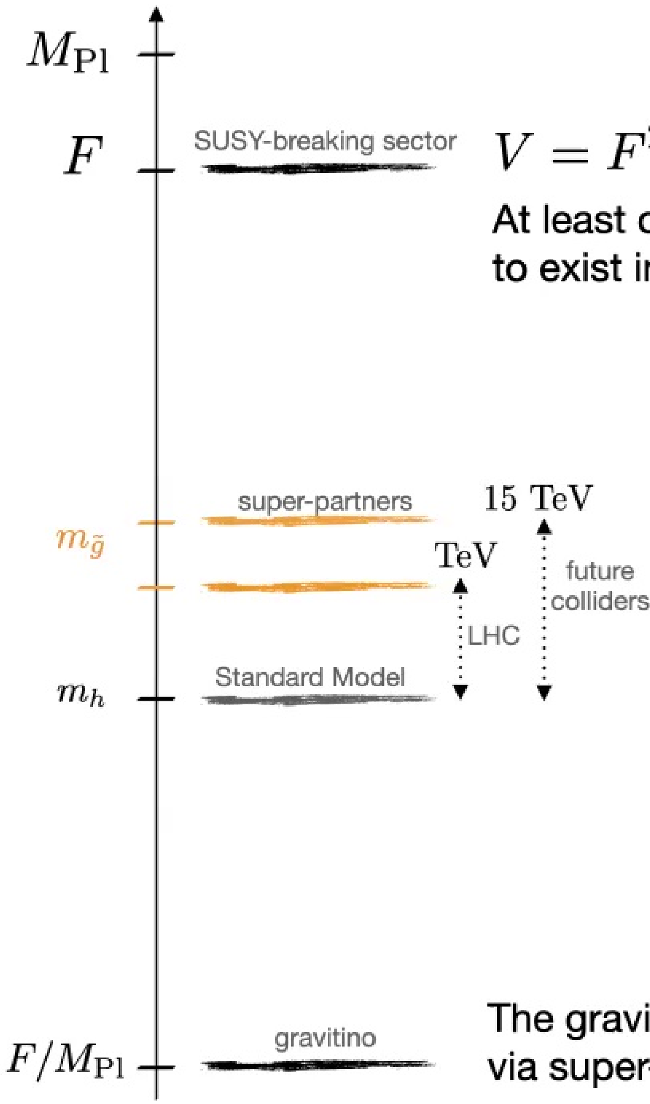


embedding in string theory



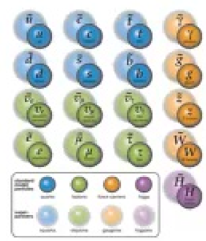
…

How we will discover unnatural SUSY?



$V = F^2$

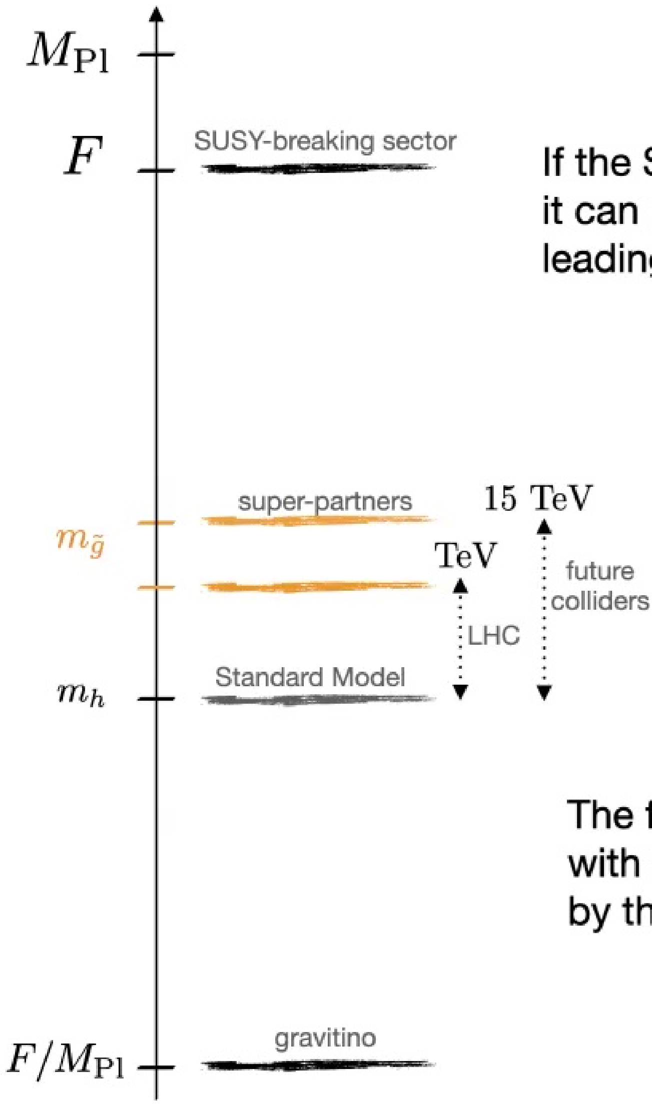
At least one hidden sector breaking SUSY is guaranteed to exist in a SUSY Universe



If fine-tuning is allowed the super-partner scale is a less robust target

The gravitino mass is related to SUSY-breaking scale via super-Higgs mechanism

Our goal here

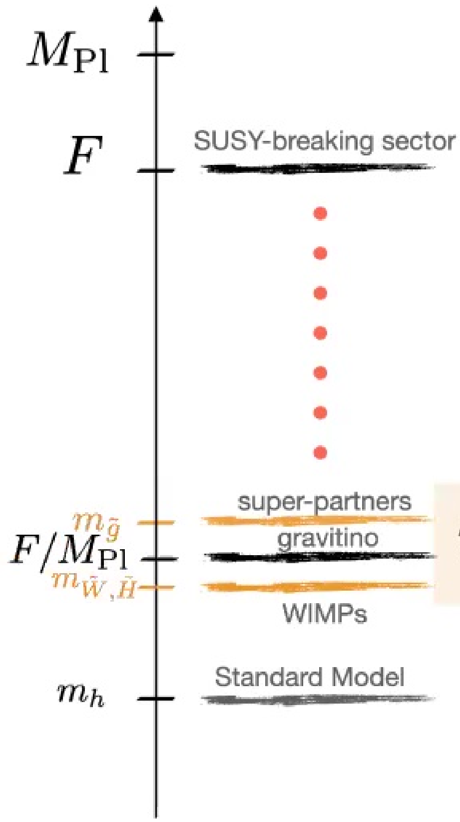


If the SUSY-breaking sector is reheated after inflation,
it can undergo a 1st order PT *
leading to GW signals at future interferometers

The frequency of the signal correlates
with the SUSY-spectrum and it is constrained
by the requirement of a viable cosmology

* the question about the nature of this PT will be the topic of the second part of the talk

Gravity Mediation



$$m_{\tilde g} \sim g_M \times \sqrt{F}$$

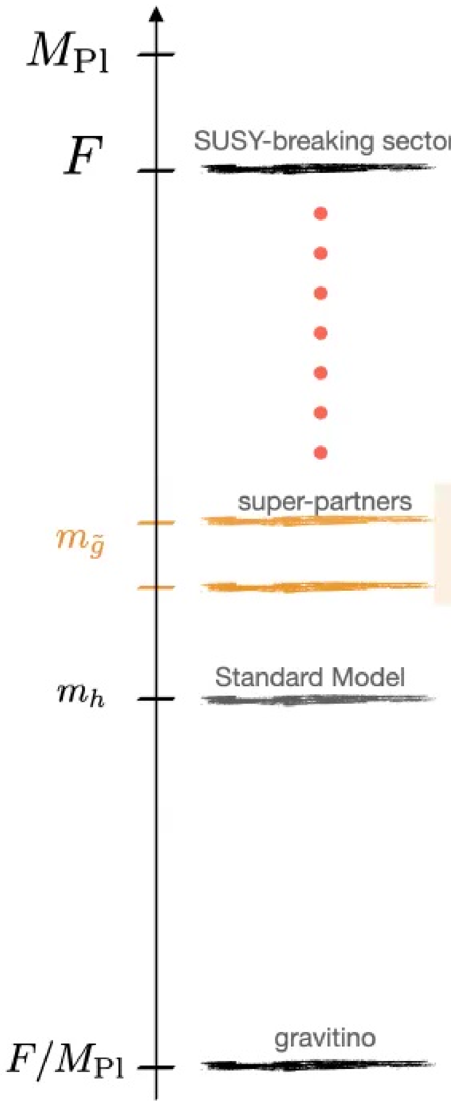
$g_M \sim \sqrt{F}/M_{\rm Pl}$

EWkino Lightest SUSY Particle (LSP)

"Split SUSY"

G.F. Giudice, A. Romanino (2004)
N. Arkani-Hamed, S. Dimopoulos (2004)

The SUSY Universe



$V = F^2$ the minimal dynamics required is a chiral field

$$\langle X \rangle = \frac{f_a}{\sqrt{2}} + \sqrt{2}\theta \tilde{G} + \theta^2 F$$

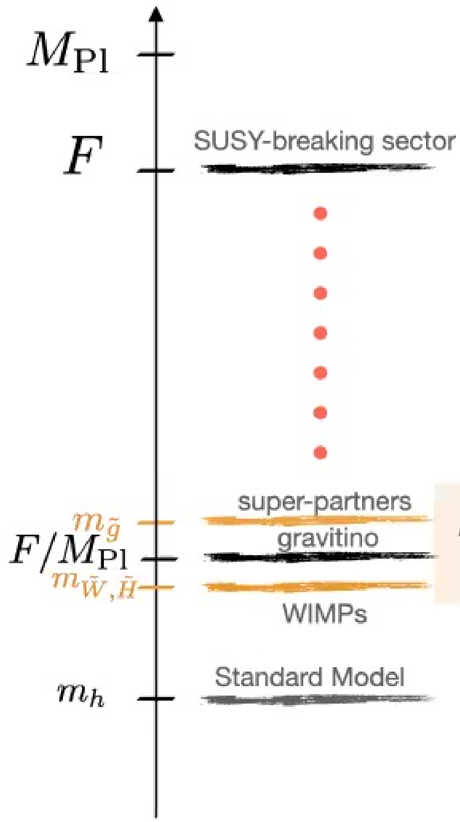
R-symmetry breaking scale; Goldstino; SUSY-breaking scale

$$m_{\tilde g} \sim g_M \times \sqrt{F}$$

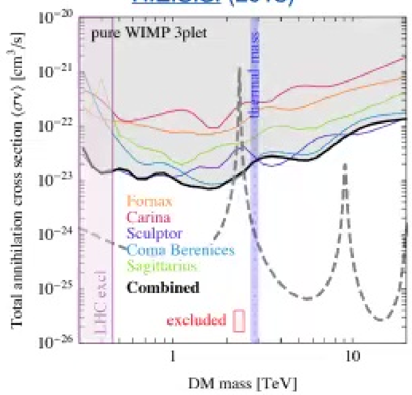
The strength of the hidden sector coupling determines the scheme

The very same force has important cosmological consequences (nature of DM etc…)

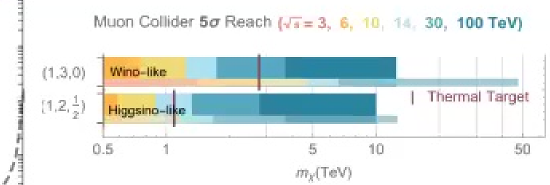
Gravity Mediation



H.E.S.S. (2018)



Han, Liu, Wang,Wang (2020)



$$m_{\tilde g} \sim g_M \times \sqrt{F}$$

⋯⋯▸ $g_M \sim \sqrt{F}/M_{\rm Pl}$

⋯⋯▸ EWkino Lightest SUSY Particle (LSP)

"Split SUSY"

G.F. Giudice, A. Romanino (2004)
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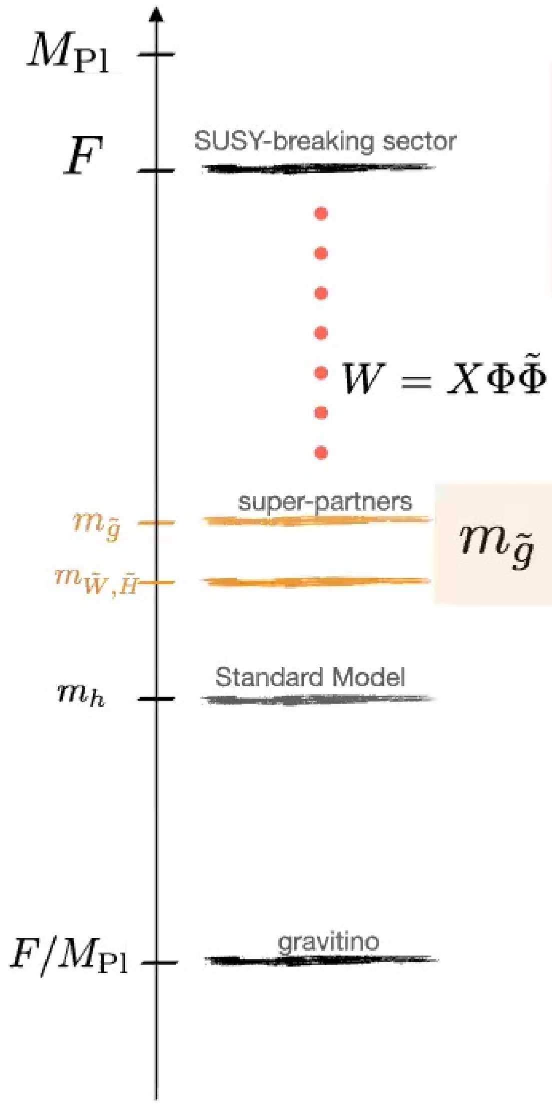
The main signal to hunt for are the WIMPs! (in)direct detection + future colliders

Low-energy SUSY-breaking



$$\langle X \rangle = \frac{f_a}{\sqrt{2}} + \sqrt{2}\theta\tilde{G} + \theta^2 F$$

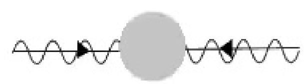
R-symmetry breaking scale — Goldstino — SUSY-breaking scale

$$m_{\tilde{g}} \sim g_M \times \sqrt{F}$$

⋯⋯▶ $g_M \gg \sqrt{F}/M_{\rm Pl}$

⋯⋯▶ ex: gauge mediation

G.F. Giudice, R. Rattazzi (1998)



$$g_M = \frac{\alpha_3 N_{\rm mess}}{4\pi} \times s_M \times \frac{\sqrt{F}}{f_a}$$

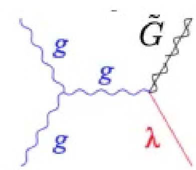
⋯⋯▶ Gravitino LSP

$$\mathcal{L}_{\tilde{G}} \supset \frac{1}{F}\partial^\mu \tilde{G} J_\mu$$

Gravitino cosmology

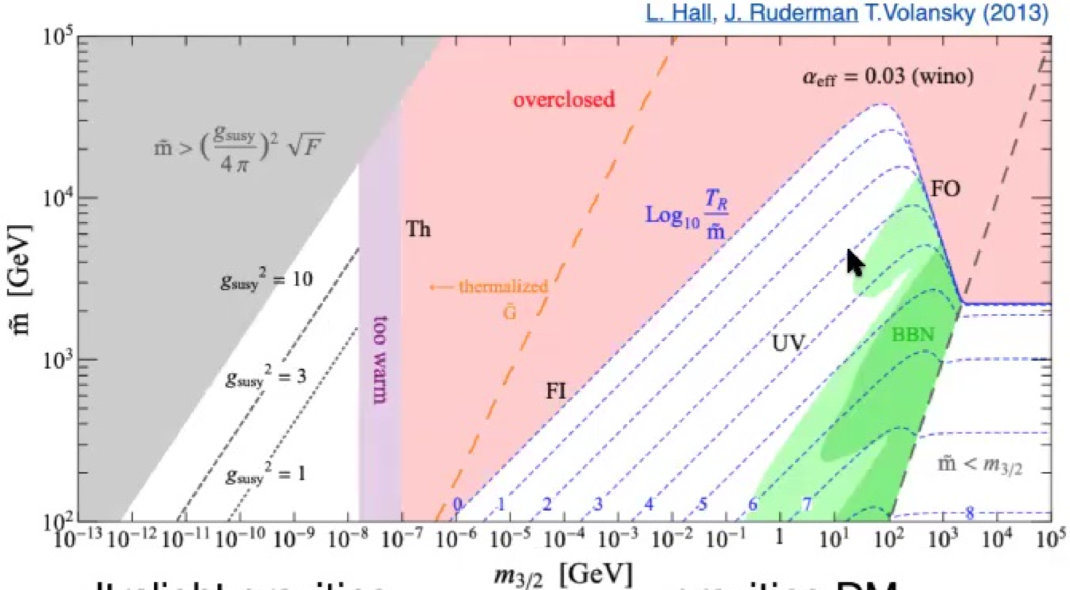
The gravitino cosmology shapes the parameter space if we require $T_{r.h.} \gtrsim \sqrt{F}$

This is known as "gravitino problem" $\mathcal{L}_{\tilde{G}} \supset \frac{1}{F}\partial^{\mu}\tilde{G}J_{\mu}$ ⋯⋯▸



S. Rychkov, A. Strumia (2007)

L. Hall, J. Ruderman T.Volansky (2013)



ultralight gravitino

gravitino DM

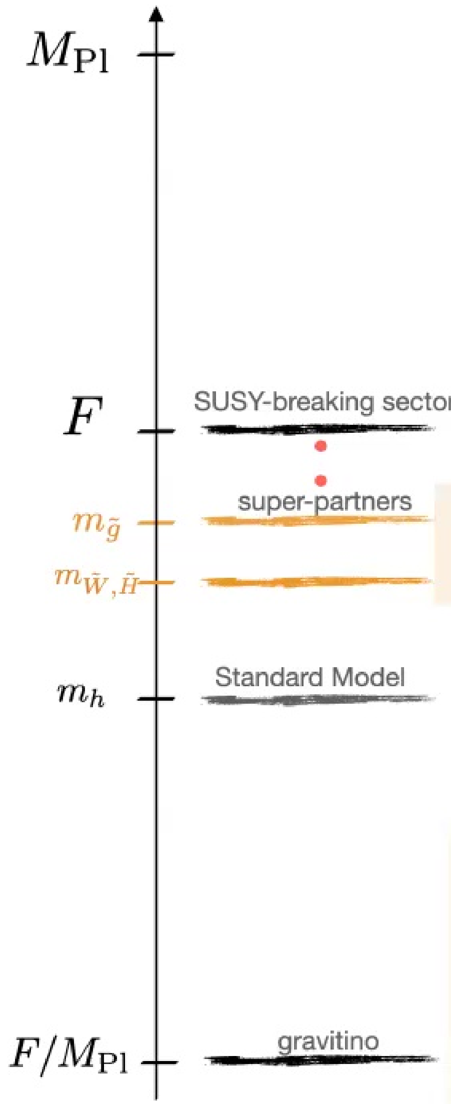
The gravitino production from the plasma is enhanced if it is light

$$Y_{3/2} \sim C_{\rm UV} \frac{M_3^2 T}{m_{3/2}^2 M_{\rm Pl}}$$

This lead generically to problems with Gravitino overabundance

$$m_{3/2} Y_{3/2} < 0.27 T_{\rm eq}$$

Ultralight Gravitino Window



$$\sqrt{F} < \left(M_{\rm Pl} m_{\tilde g}^2\right)^{1/3} \sim 5 \times 10^7 \ {\rm TeV}$$

the gravitino is thermal!

$$V = F^2$$

very low SUSY-breaking scale

$$m_{\tilde g} \sim g_M \times \sqrt{F}$$

large coupling $1 \lesssim g_M \lesssim 100$

model building challenges

A. Hook, H. Murayama (2015, 2018)

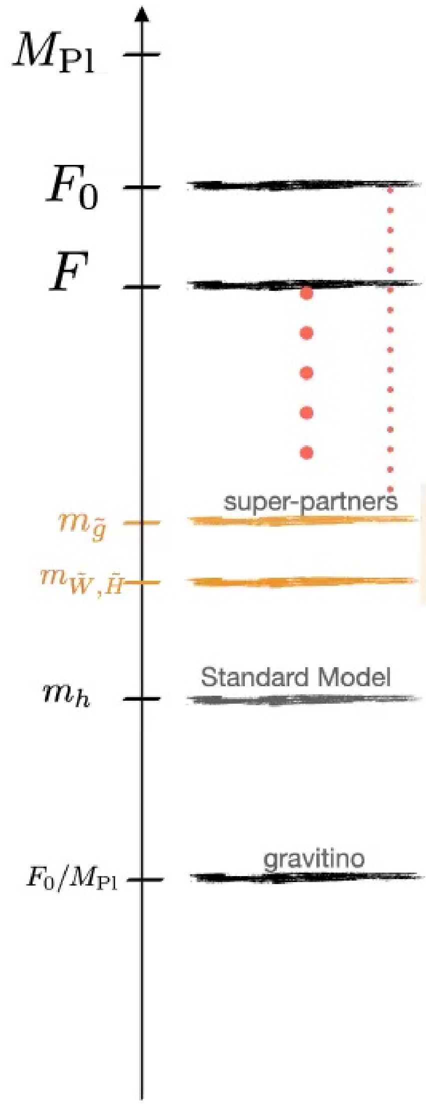
bounded from above by warm DM constraints

$m_{3/2} \lesssim 16 \ {\rm eV} \quad , \quad F \lesssim 260 \ {\rm TeV}$

from below by collider bounds ⋯⋯▸ Planck data + future colliders can close this?

$F \gtrsim {\rm TeV's}$

Gravitino Dark Matter



SUSY-breaking hidden sectors

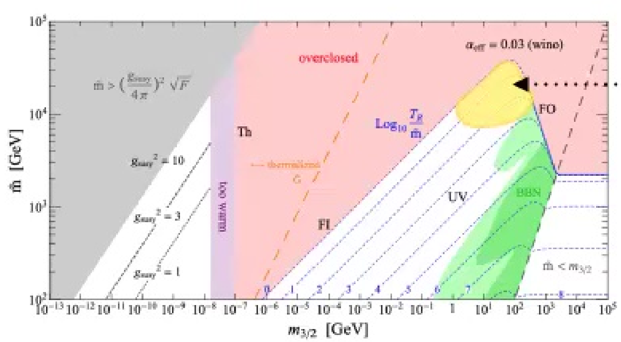
$$F/F_0 \lesssim 10^{-2} \left(\frac{F}{10^7\ \text{GeV}}\right)\left(\frac{0.1}{g_M}\right)$$

to avoid gravitino thermalization

$$m_{\tilde g} \sim g_M \times \sqrt{F}$$

$g_M \ll 1$ standard gauge mediation!

For a fixed gluino mass the UV produced gravitino can match the relic abundance today



we wanna live here!

$$10^5\ \text{GeV} < F < 10^8\ \text{GeV}$$

The pseudomodulus phase transition

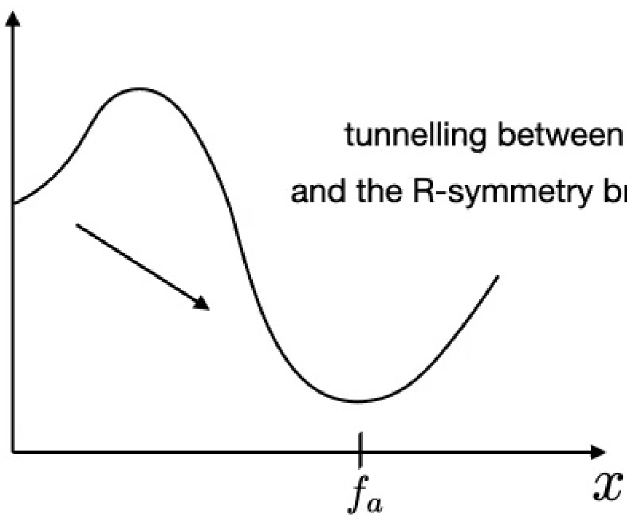
$$X = \frac{x}{\sqrt{2}} e^{2ia/f_a} + \sqrt{2}\theta\tilde{G} + \theta^2 F$$

- x: the complex pseudomoduls
- $\tilde{G}$: Goldstino
- F: SUSY-breaking scale

The R-axion a is the Goldstone of R-symmetry broken spontaneously

The radial mode x is massless at tree-level $W = FX$ $\longrightarrow$ $m_x \sim \frac{\lambda^2}{16\pi^2} F/m_*$

$m_x \ll m_*$ at weak coupling

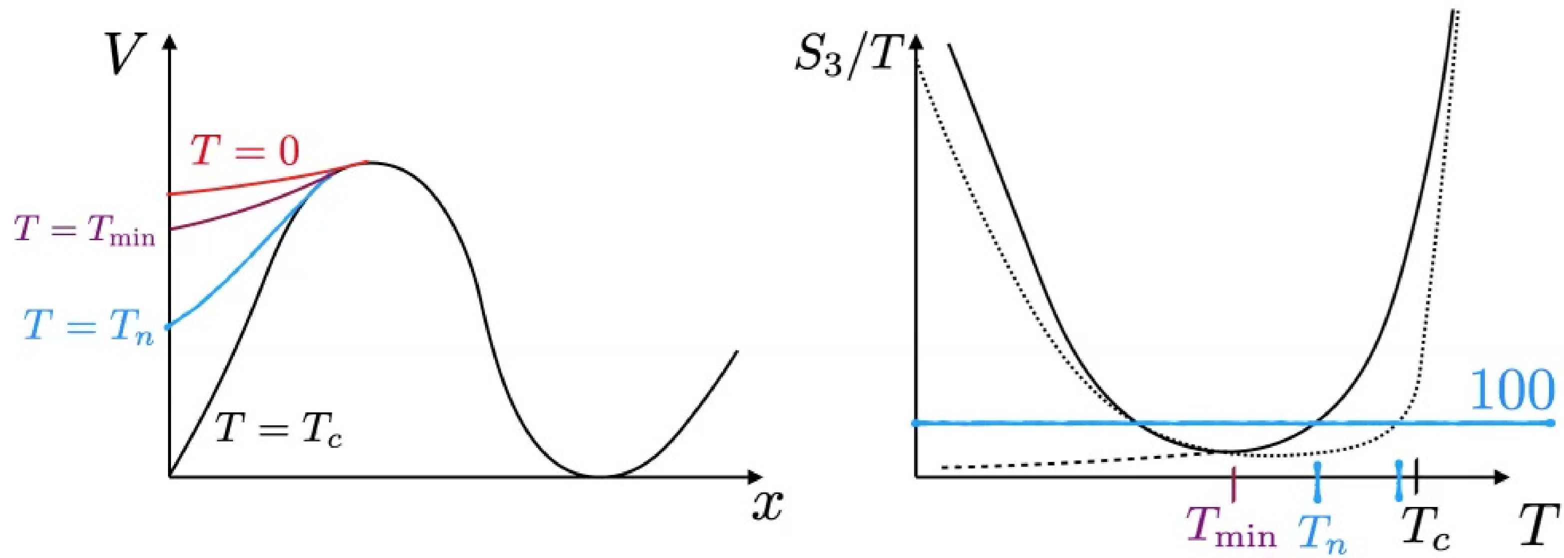


tunnelling between the origin
and the R-symmetry breaking vacuum*

* breaking R-symmetry is necessary to have Majorana gaugino masses

1st order Phase Transitions

Let me assume that the SUSY-breaking sector
produces a first order phase transition *(later we will see how)*



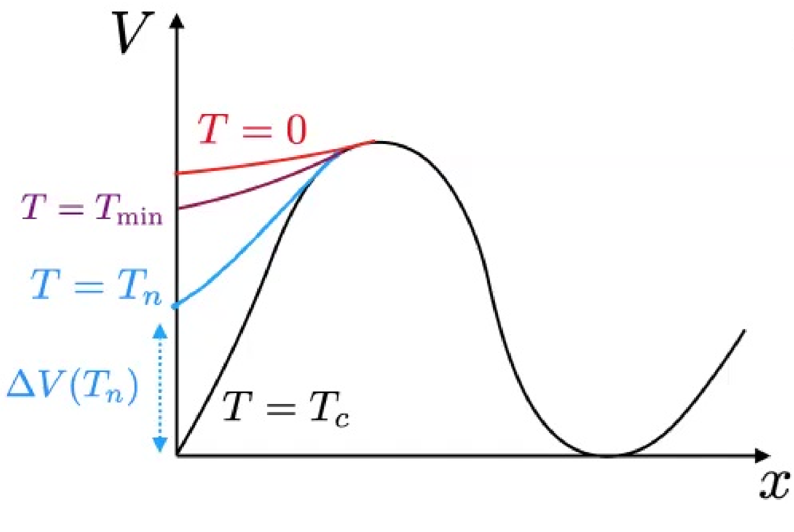
If thermal fluctuations dominate,
the tunnelling probability is encoded in

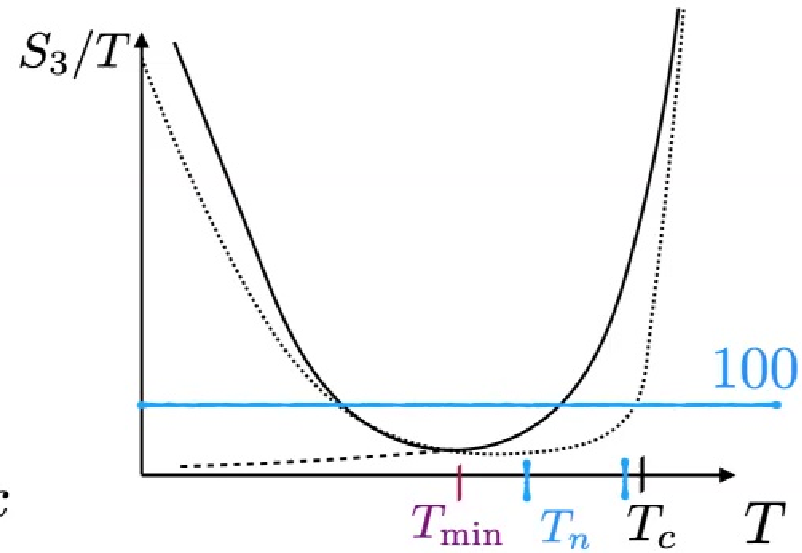
$$\Gamma(T) \simeq T^4 \left(\frac{S_3}{2\pi T}\right)^{\frac{3}{2}} \exp\left(-S_3/T\right)$$

When one bubble per Hubble volume nucleates

$$\frac{S_3(T_n)}{T_n} \simeq 100$$

Gravitational Waves signal from 1st order Phase Transitions



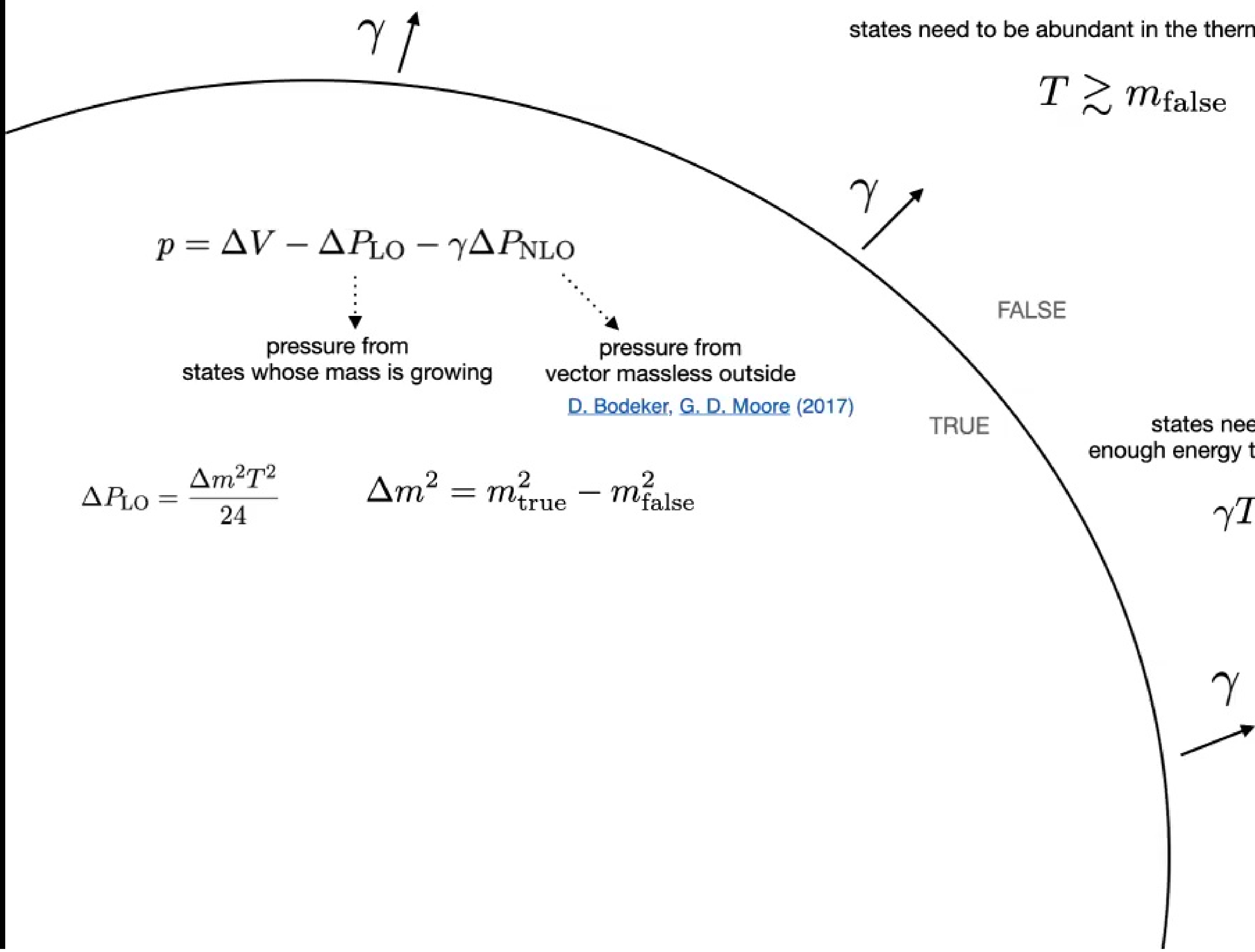


The detectability of the GWs signal depends on:

- The energy released during the PTs $\alpha(T_n) \sim \dfrac{\Delta V(T_n)}{\rho_R(T_n)}$
- The duration of the PTs $\beta_H(T_n) \overset{\text{def}}{=} \dfrac{\beta(T_n)}{H(T_n)} = T_n \dfrac{d}{dT}\left(\dfrac{S_3}{T}\right)\Big|^{*}_{T=T_n}$
- The behavior of the bubbles in the cosmic plasma

$\star$ in PTs with a mass gap there is always a T s.t $\beta_H(T_{\min}) = 0$

Bubble frictions



states need to be abundant in the thermal bath

$$T \gtrsim m_{\rm false}$$

$$p = \Delta V - \Delta P_{\rm LO} - \gamma \Delta P_{\rm NLO}$$

pressure from
states whose mass is growing

pressure from
vector massless outside

D. Bodeker, G. D. Moore (2017)

states need to have
enough energy to cross the wall

$$\gamma T \gtrsim m_{\rm true}$$

$$\Delta P_{\rm LO} = \frac{\Delta m^2 T^2}{24} \qquad \Delta m^2 = m^2_{\rm true} - m^2_{\rm false}$$

Bubble frictions

γ

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D. Bodeker, G. D. Moore (2017)

FALSE

TRUE

states need to have enough energy to cross the wall

$$\gamma T \gtrsim m_{\text{true}}$$

$$\Delta P_{\text{LO}} = \frac{\Delta m^2 T^2}{24} \qquad \Delta m^2 = m^2_{\text{true}} - m^2_{\text{false}}$$

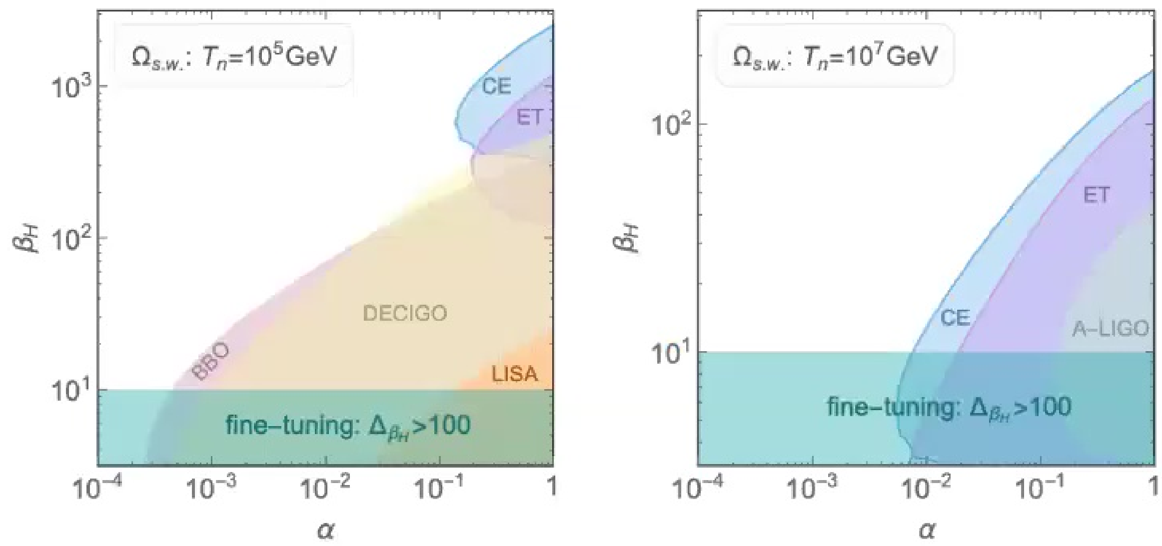
γ

Heavy states can contribute to ΔP_{LO} A. Azatov, M. Vanvlasselaer (2020)

$$\Delta P^{\text{heavy}}_{\text{LO}} \simeq \frac{1}{24}(m^2_{\text{true}} - m^2_{\text{false}}) \; T_n^2 e^{-m_{\text{false}}/T_n}$$

This is generically enough to stop the acceleration for the pseudomodulus

GW signal



Using the nucleation condition the duration of the PT can be written as

$$\beta_H(T_n) \simeq S'(T_n) - \mathcal{C} \ \sim 100$$ unless I tune the two terms to partially cancel

Having a very small duration seems to be a highly non-generic prediction of any PT

$$\Delta_{\beta_H} \stackrel{\text{def}}{=} \text{Max}_{\{p_i\}} \Delta^{p_i}_{\beta_H} = \text{Max}_{\{p_i\}} \left| \frac{d \log \beta_H}{d \log p_i} \right|$$

this “beta-tuning” can be computed in a model a’ la Giudice-Barbieri

The simplest explicit model

O'Raifeartaigh $W = -FX + \lambda X \Phi_1 \tilde{\Phi}_2 + m(\Phi_1 \tilde{\Phi}_1 + \Phi_2 \tilde{\Phi}_2)$

+ R-breaking $W_{\not{R}}(X) = \frac{1}{3}\epsilon X^3$

this matches perfectly to the toy potential with $\kappa_D = 1$

$$V_0(x) = \kappa_D^2 \left(F - \epsilon_{\not{R}} x^2\right)^2 + \frac{\lambda^2}{32\pi^2}|F|^2 \log\left(\frac{\lambda^2 x^2 + m_*^2}{m_*^2}\right)$$

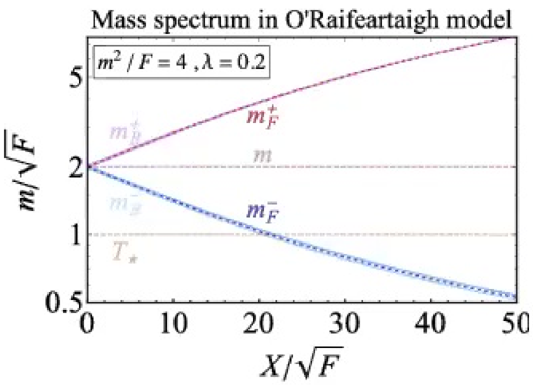
* $\kappa_D = 1$ single scale SUSY-breaking
* $\epsilon_{\not{R}} < 1/\sqrt{\kappa_D}$ to ensure flatness
* never singular = mass gap
* pure log at $x \to \infty$

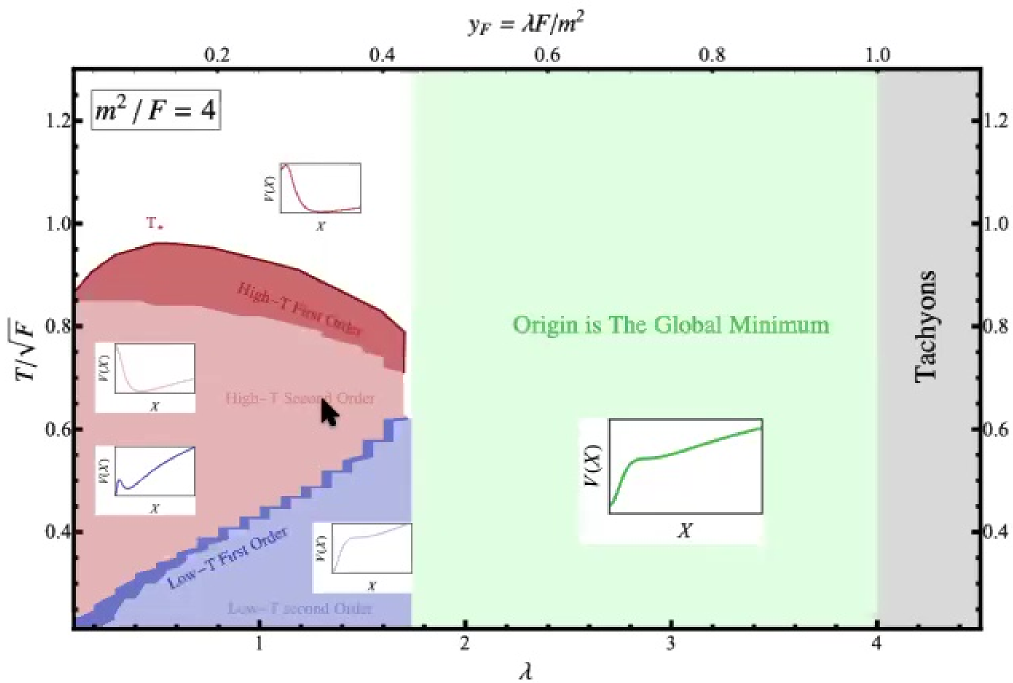
The O'Raifeartaigh phase diagram

see also A. Katz (2009)

$$W = -FX + \lambda X \Phi_1 \tilde{\Phi}_2 + m(\Phi_1 \tilde{\Phi}_1 + \Phi_2 \tilde{\Phi}_2)$$

	X	Φ_1	$\tilde{\Phi}_1$	Φ_2	$\tilde{\Phi}_2$
$U(1)_R$	2	0	2	2	0
$U(1)_D$	0	1	-1	1	-1





The O'Raifeartaigh phase diagram

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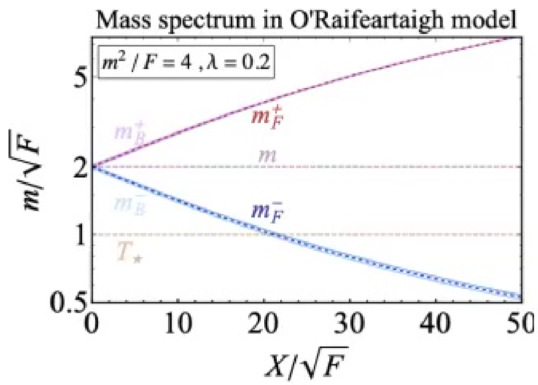

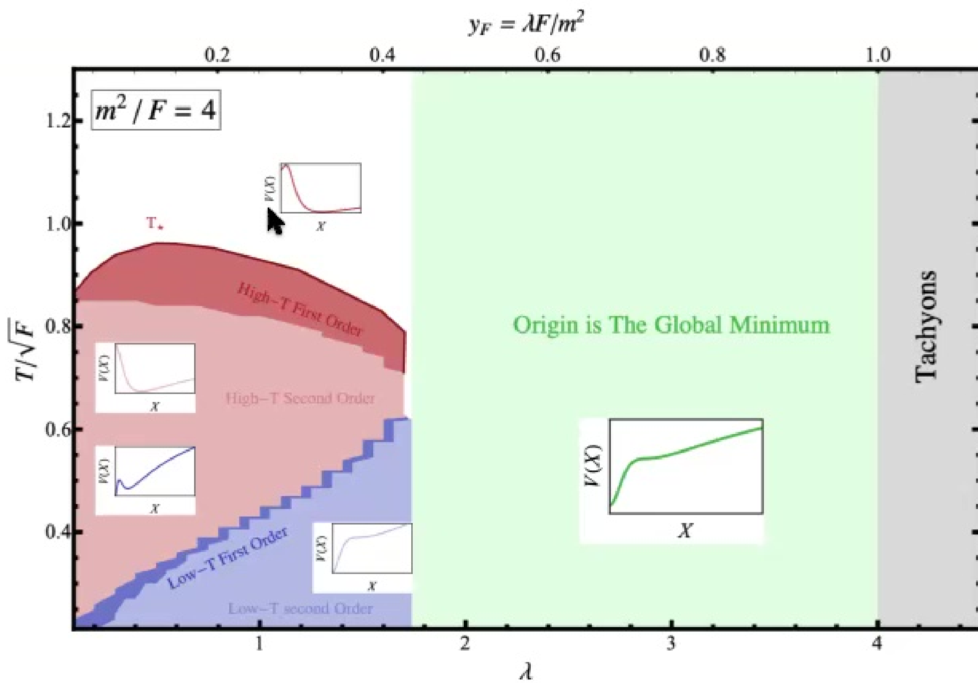

$$x_\star \simeq \frac{2\sqrt{2}\pi T}{\lambda y_F} \quad , \quad T_\star \sim 0.23\sqrt{y_F}\, m \ ,$$

competition between
thermal and loop corrections

Bubble frictions

γ

states need to be abundant in the thermal bath

$$T \gtrsim m_{\text{false}}$$

γ

$$p = \Delta V - \Delta P_{\text{LO}} - \gamma \Delta P_{\text{NLO}}$$

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$$\Delta P_{\text{LO}}^{\text{heavy}} \simeq \frac{1}{24}(m_{\text{true}}^2 - m_{\text{false}}^2)\ T_n^2 e^{-m_{\text{false}}/T_n}$$

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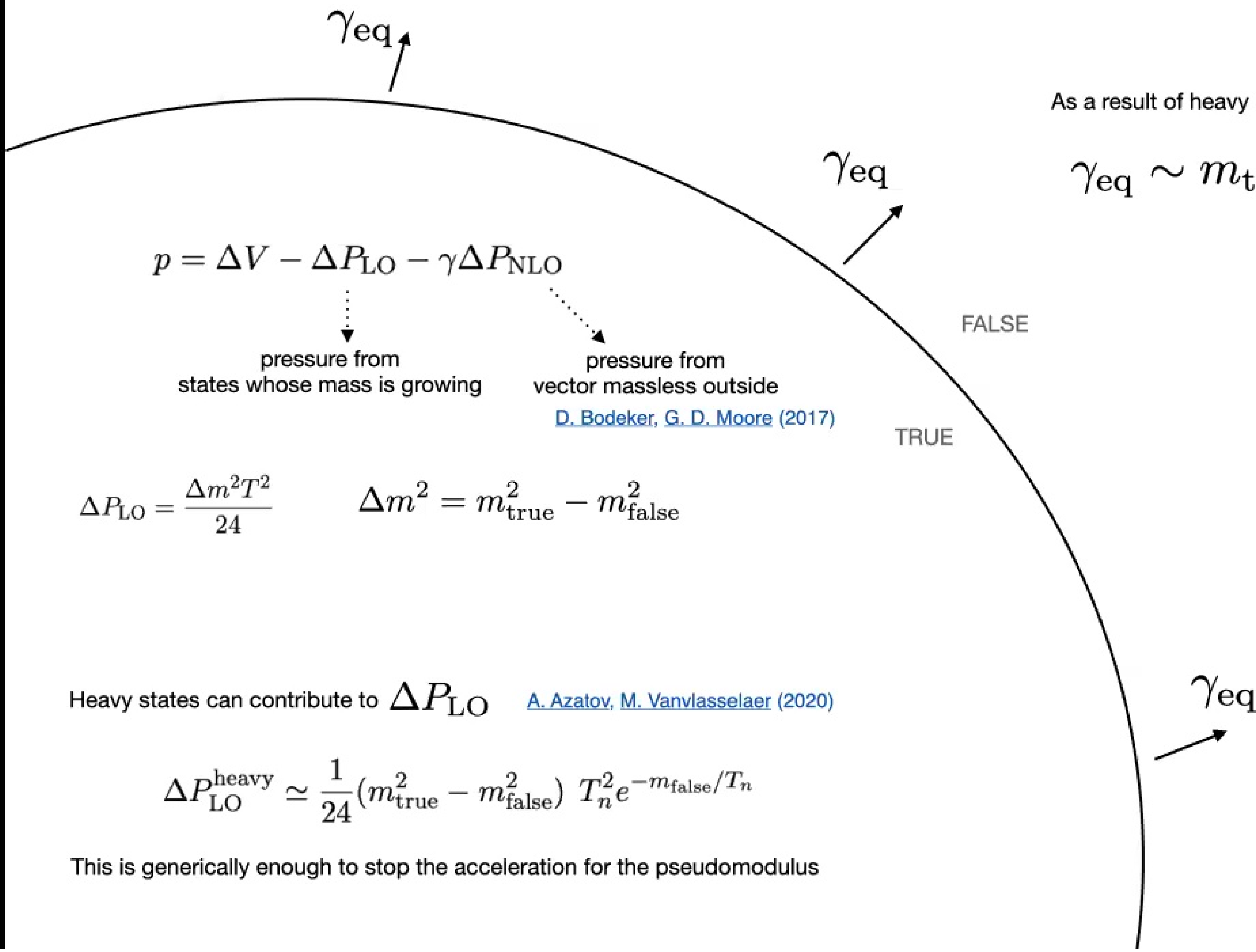
Bubble frictions



As a result of heavy state friction

$$\gamma_{\rm eq} \sim m_{\rm true}/T_n$$

$$p = \Delta V - \Delta P_{\rm LO} - \gamma \Delta P_{\rm NLO}$$

- $\Delta P_{\rm LO}$: pressure from states whose mass is growing
- $\gamma \Delta P_{\rm NLO}$: pressure from vector massless outside — D. Bodeker, G. D. Moore (2017)

$$\Delta P_{\rm LO} = \frac{\Delta m^2 T^2}{24} \qquad \Delta m^2 = m^2_{\rm true} - m^2_{\rm false}$$

Heavy states can contribute to $\Delta P_{\rm LO}$ A. Azatov, M. Vanvlasselaer (2020)

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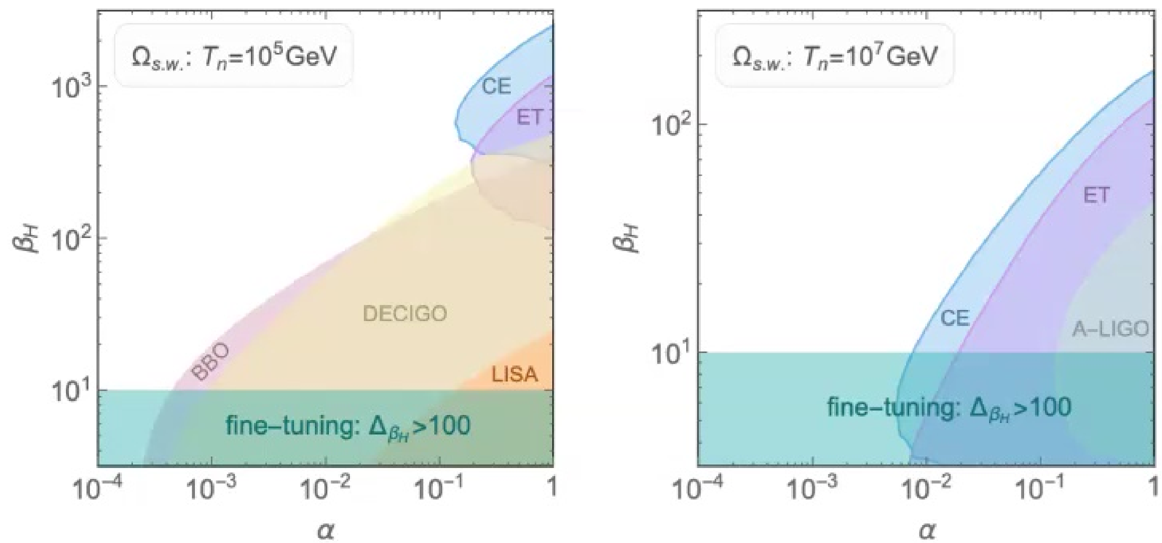
GW signal



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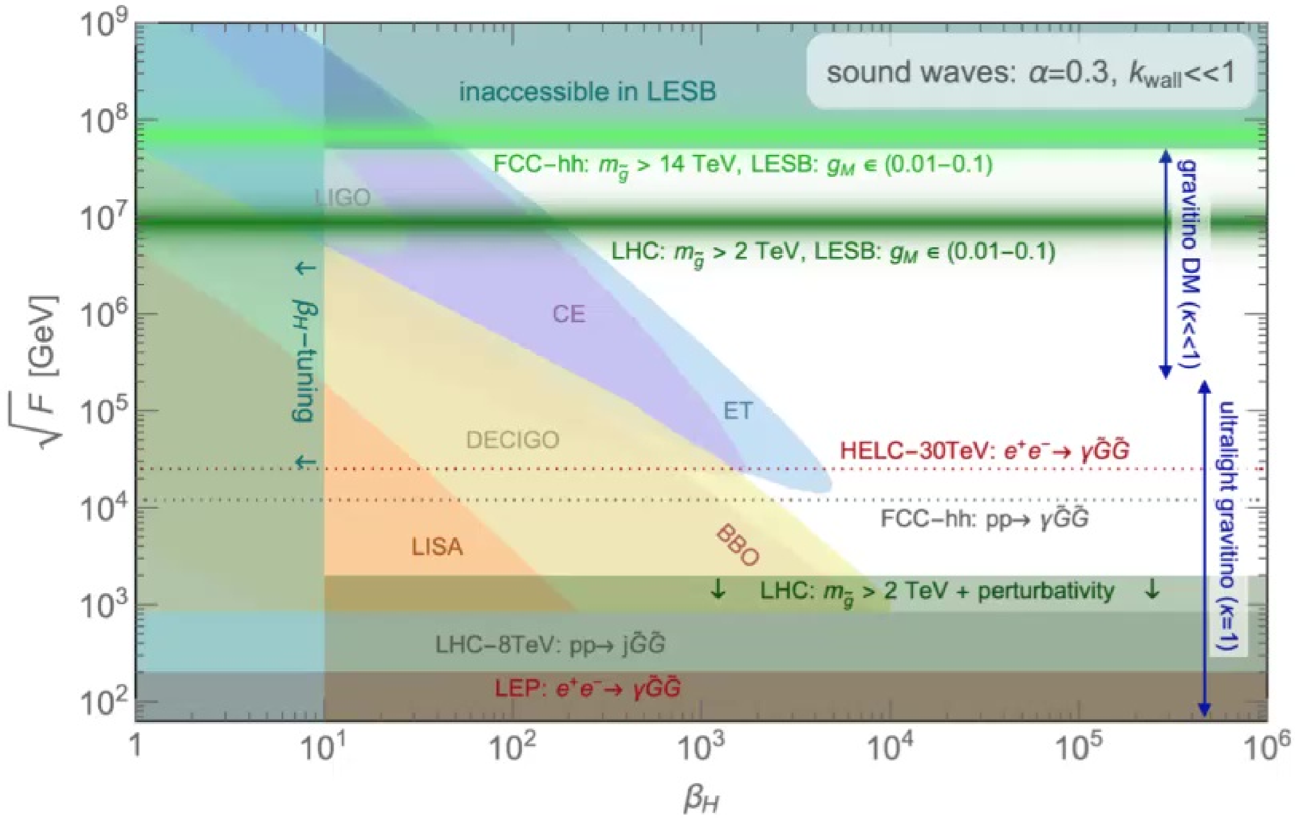
How we will discover Low Energy SUSY breaking

GRAVITINO DM: The gravitino problem bounds the GWs frequency to be always within reach of A-LIGO, CE and ET

Calculable models live at high F

They will be fully tested at FCC-hh!



The nature of the pseudomodulus PT: Goals

- How S_3/T depends qualitatively with temperature?

Higgs ⋯⋯▸ $S_3/T \sim T^\alpha$ high-T expansion

dilaton ⋯⋯▸ $S_3/T \sim 1/\log m/T$ supercooling

pseudomodulus ⋯⋯▸ $S_3/T \sim T^\alpha e^{-m/T}$ low-T expansion

- Can we extract a parametric dependence of S_3/T in terms of theory parameters?

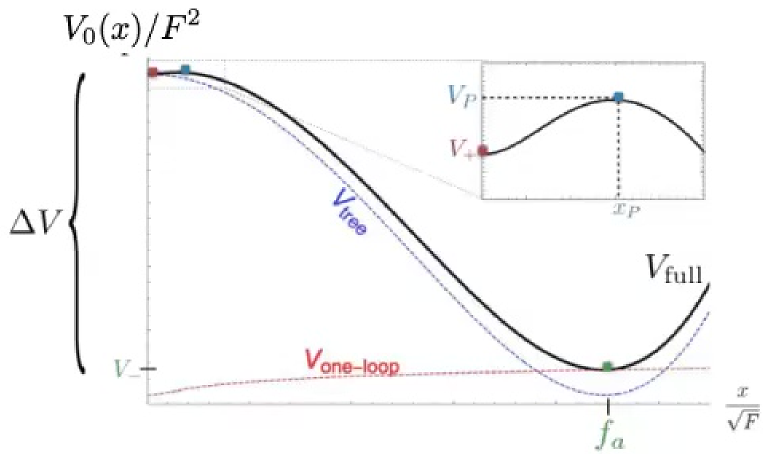
⋯⋯▸ trying to answer the question how generic is a strong first order PT for a given class of models

The pseudomodulus potential at T=0

$$m_x \sim \frac{\lambda^2}{16\pi^2} F/m_* \qquad m_x \ll m_*$$

at weak coupling

$$V_{\text{eff}}(x) = V_0(x) + V_T(x)$$



- **The potential is flat** $f_a^4 \gg \Delta V$ loop corrections asymptote to a Log at large field value
- **The barrier is small** $\frac{V_P}{\Delta V} = \frac{\lambda_{\text{eff}}^2}{16\pi^2}$ $\lambda_{\text{eff}} \sim \mathcal{O}(1)$
- **The position of the barrier** does not affect the bounce much (see later)

The pseudomodulus potential at finite T

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at weak coupling

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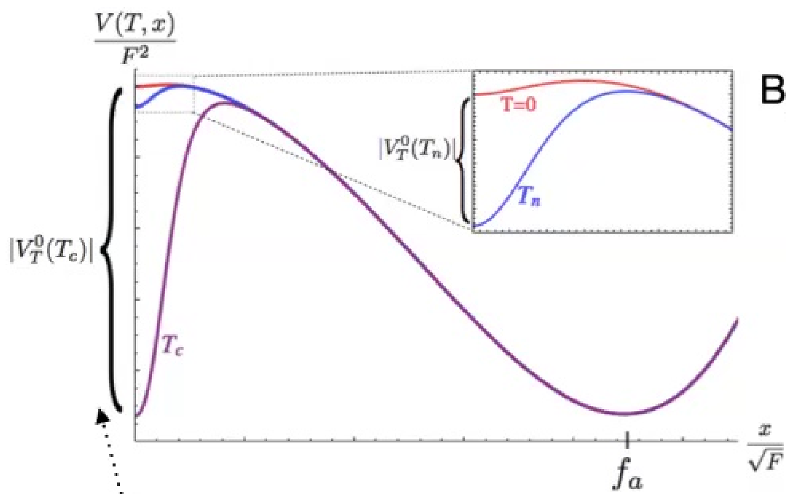


By construction, the scale setting the potential is below the cutoff

$$T_n \sim \sqrt{F} \lesssim m_*$$

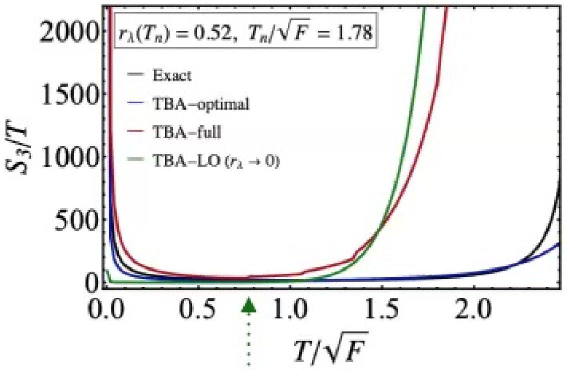
the low-T expansion applies at nucleation

Thermal corrections only make the origin deeper in this limit

$$V_T(x) \simeq -N\, T^4 \left(\frac{\lambda^2 x^2 + m_*^2}{(2\pi T)^2} \right)^{3/4} e^{-\sqrt{\frac{\lambda^2 x^2 + m_*^2}{T^2}}}$$

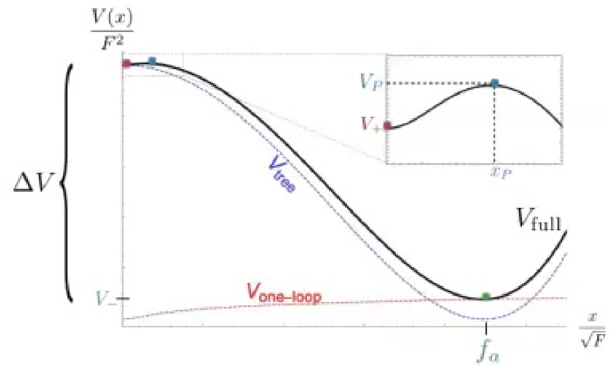
$$N = N_{\rm bosons} + N_{\rm fermions}$$

The pseudomodulus bounce action I



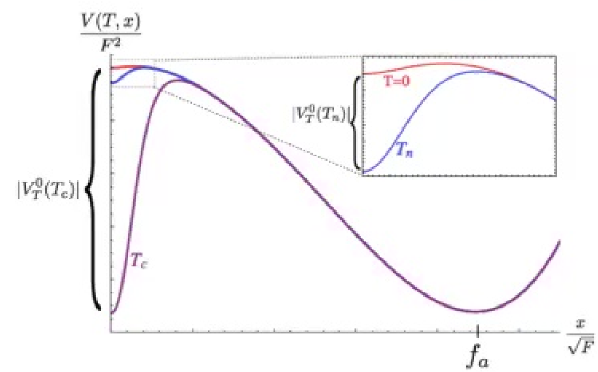
A simple triangular barrier approximates the full bounce quite well

For a fully analytical treatment
we expand for
flat potential + small barrier



x_P-independent!

$$\frac{S_3}{T} \simeq \frac{144\sqrt{2}\pi}{5T} \frac{(V_P - V_T^0)^{5/2} f_a^3}{(\Delta V)^3}$$



The bounce is independent on the position of the barrier in this limit!

The pseudomodulus potential at finite T

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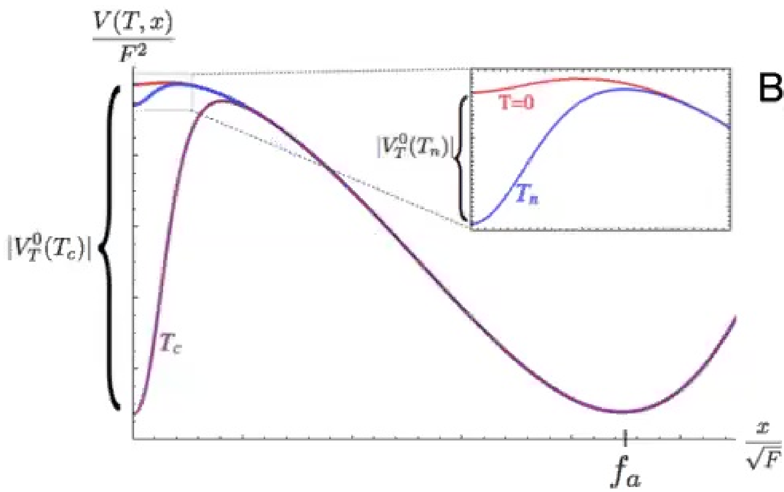

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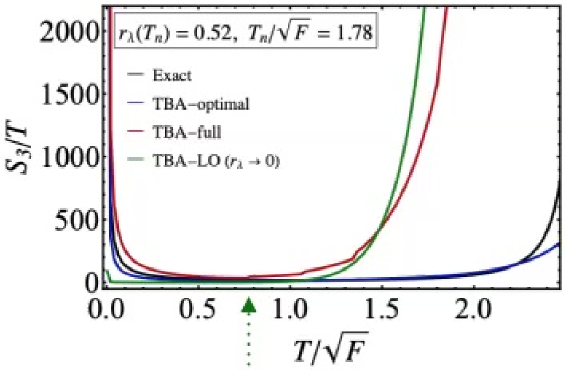

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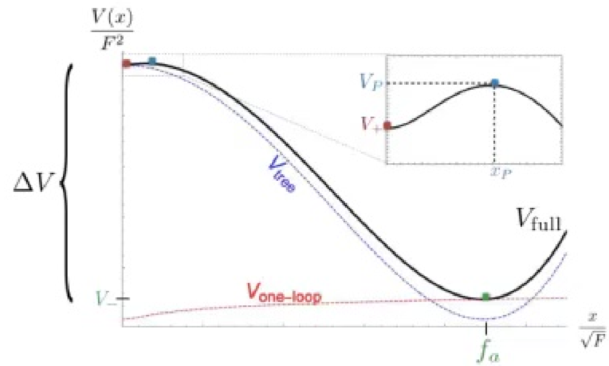

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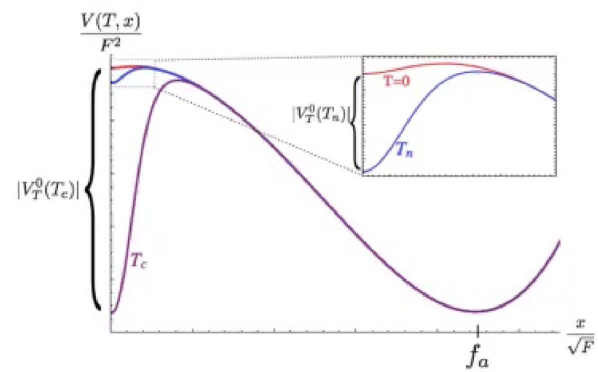
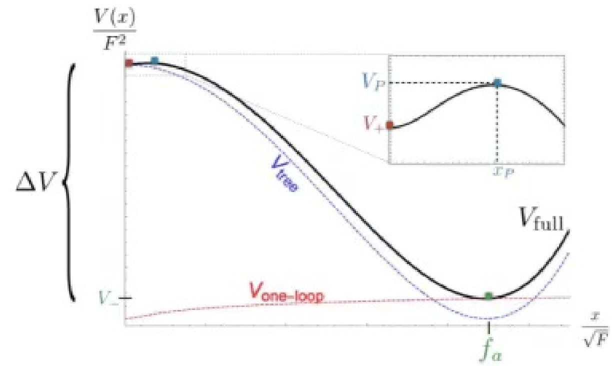


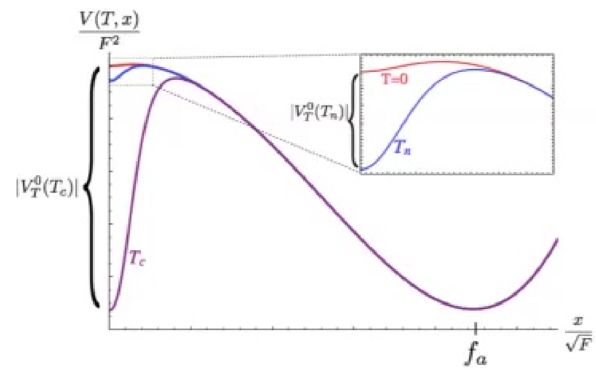
The bounce is independent on the position of the barrier in this limit!

The pseudomodulus bounce action II

$$\frac{S_3}{T} \simeq \frac{144\sqrt{2}\pi}{5T}\frac{(V_P - V_T^0)^{5/2} f_a^3}{(\Delta V)^3}$$



In the same approximation we can get the nucleation temperature analytically in a systematic expansion $V_P/V_T^0 \ll 1$



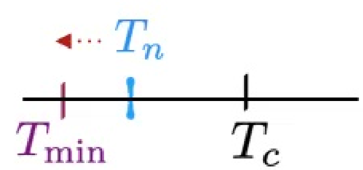
$$T_n \simeq T_n^0 \left(1 - \frac{7}{\mathcal{C}^{2/5}}\frac{V_P}{m_*^4}\left(\frac{T_n^0}{m_*}\right)^{3/5}\left(\frac{f_a m_*^3}{\Delta V}\right)^{6/5}\right)$$

where $T_n^0 \sim m_*/2$

The competition of the two terms shows that the nucleation temperature can be diminished down to the minimal temperature by increasing the barrier or the distance in field space

Since $\alpha \sim \Delta V / T_n^4$

at the boundary of nucleation the signal is enhanced!



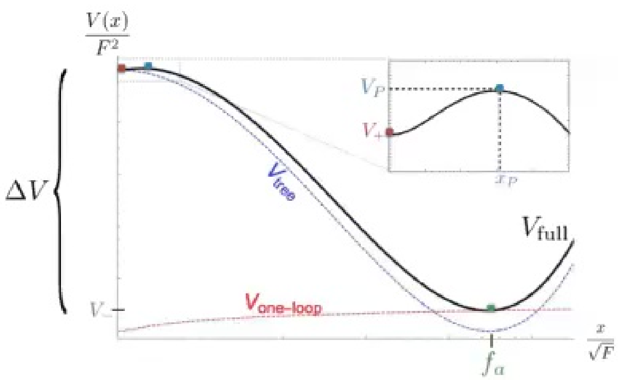
A toy model

$$V_0(x) = \kappa_D^2 \left(F - \epsilon_{\not R}\, x^2\right)^2 + \frac{\lambda^2}{32\pi^2}|F|^2 \log\left(\frac{\lambda^2 x^2 + m_*^2}{m_*^2}\right)$$

* $\kappa_D = 1$
  single scale SUSY-breaking

* $\epsilon_{\not R} < 1/\sqrt{\kappa_D}$
  to ensure flatness

* never singular = mass gap
* pure log at $x \to \infty$



$$\langle x \rangle_{\text{true}} = f_a = \sqrt{\frac{F}{\epsilon_{\not R}}} \quad , \quad \Delta V = (\kappa_D F)^2 \ ,$$

$$\alpha = \frac{30}{g_*(T_n)\pi^2}\left(\frac{\kappa_D F}{T_n^2}\right)^2 \sim 10^{-2}\kappa_D^2 \left(\frac{F}{m_*^2}\right)^2 \left(\frac{230}{g_*(T_n)}\right)$$

no-tuning

$T_n \sim m_*/2$

2 SUSY-breaking scales are needed to have large alpha!

What did we learn

As long as the barrier is *small* and the potential is *flat*
the bounce is *independent* on the position of the barrier

At the *boundary of nucleation* the signal is *enhanced* if we allow for cancellations

For a generic nucleation temperature, 2 SUSY-breaking scales are needed
to get a sizeable GW signal

A toy model

$$V_0(x) = \kappa_D^2 \left(F - \epsilon_{\not R} x^2\right)^2 + \frac{\lambda^2}{32\pi^2}|F|^2 \log\left(\frac{\lambda^2 x^2 + m_*^2}{m_*^2}\right)$$

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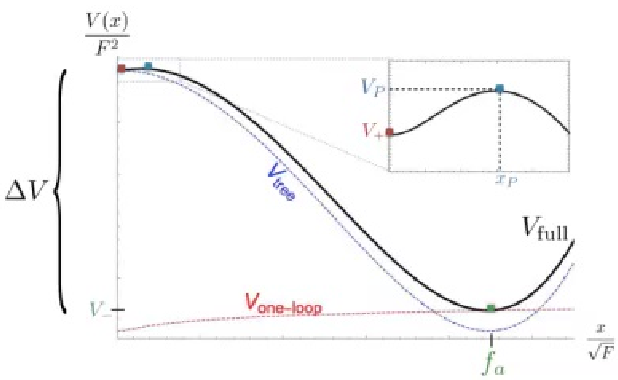

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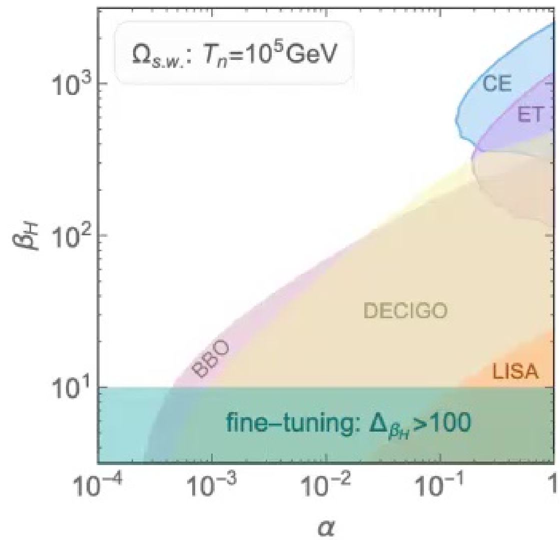
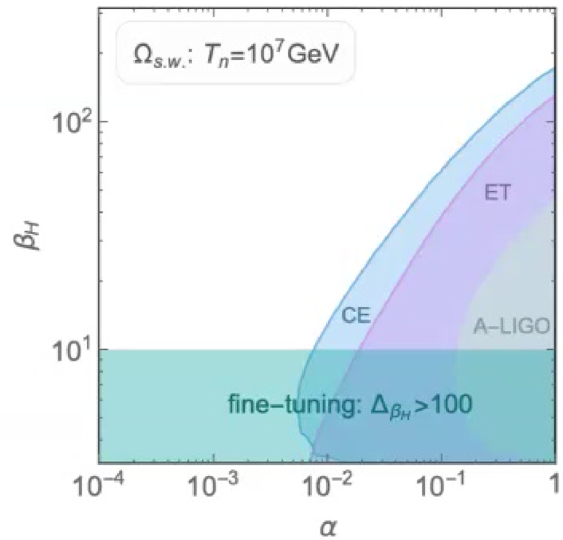
no-tuning $T_n \sim m_*/2$

2 SUSY-breaking scales are needed to have large alpha!

GW signal





Using the nucleation condition the duration of the PT can be written as

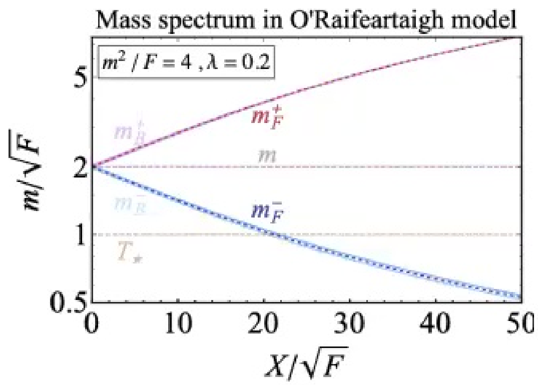
$$\beta_H(T_n) \simeq S'(T_n) - \mathcal{C} \ \sim 100$$ unless I tune the two terms to partially cancel

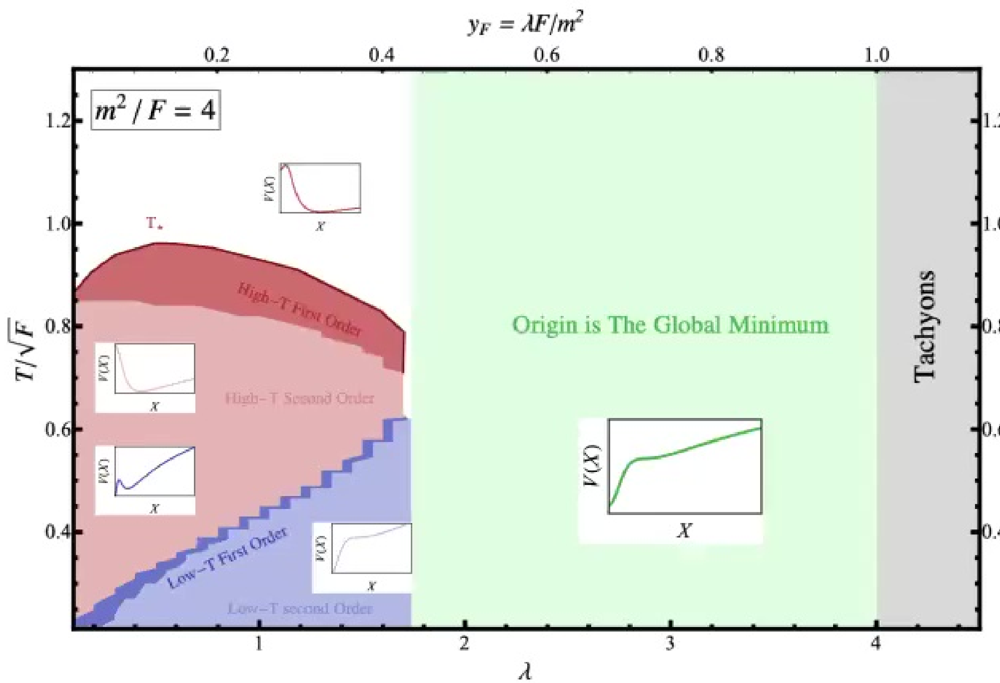
The O'Raifeartaigh phase diagram

see also A. Katz (2009)

$$W = -FX + \lambda X\Phi_1\tilde{\Phi}_2 + m(\Phi_1\tilde{\Phi}_1 + \Phi_2\tilde{\Phi}_2)$$

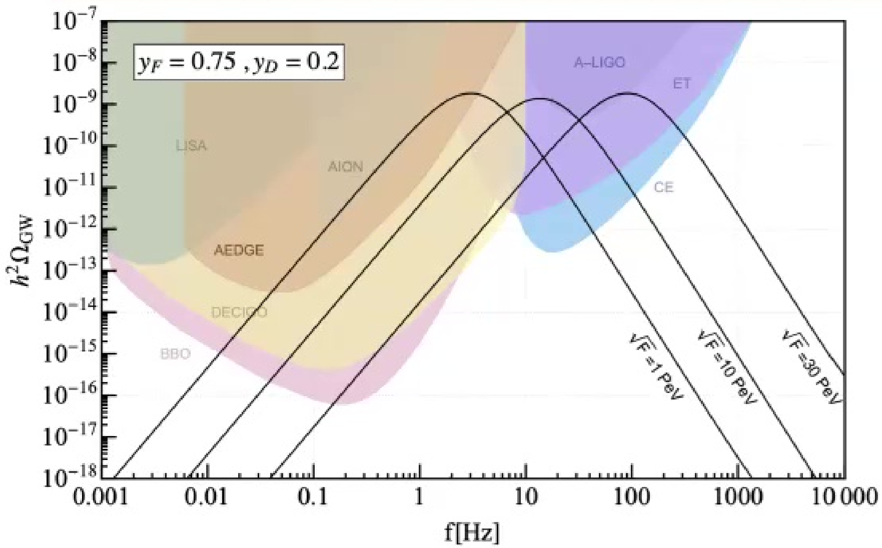
	X	Φ_1	$\tilde{\Phi}_1$	Φ_2	$\tilde{\Phi}_2$
$U(1)_R$	2	0	2	2	0
$U(1)_D$	0	1	-1	1	-1





A full model of Low Energy SUSY breaking

Prediction for GWs



Prediction for the superpatner spectrum

$SU(6)/U(1)_D \supset SU(5)$ and messengers in the $5+\bar{5}$ $\mathcal{M}_{\text{mess}} = \begin{pmatrix} \frac{\lambda f_a}{\sqrt{2}} & m \\ m & 0 \end{pmatrix}^*$

$$m_{\tilde{g}} \simeq 2\ \text{TeV} \left(\frac{F}{30\ \text{PeV}}\right)^{1/2} \left(\frac{y_F}{0.75}\right)^3 \left(\frac{F}{2.5D}\right)^{1/2} \left(\frac{\lambda}{4}\right) \left(\frac{g}{0.4}\right)$$

* gaugino screening is unavoidable since we want to avoid massless messengers along the pseudomodulus

How we will discover SUSY?

Future colliders can possibly nail unnatural SUSY scenarios
if the SUSY-breaking hidden sector is reheated

The frequency of GWs expected from the hidden sector
correlates with the SUSY spectrum

Which QFTs give rise to Gravitational Waves?

The SUSY-breaking pseudomodulus features
a new type of 1st order PTs

*low-T expansion

*pressure from Boltzmann suppressed states

*GWs are unlikely to be detectable in single scale models