

Title: A voyage through undulating dark matter and the GUTs of $u(48)$

Speakers: Joseph Tooby-Smith

Series: Particle Physics

Date: December 15, 2020 - 1:00 PM

URL: <http://pirsa.org/20120025>

Abstract: This talk will be split into two distinct halves: The first half will be based on the paper [arxiv:2007.03662](https://arxiv.org/abs/2007.03662) and suggest that an interplay between microscopic and macroscopic physics can lead to an undulation on time scales not related to celestial dynamics. By searching for such undulations, the discovery potential of light DM search experiments can be enhanced.

The second half will look at some currently unpublished work into finding all the semi-simple subalgebras of $u(48)$ which contain the SM. Such algebras (in a loose sense of the term) form GUTs and studying them has relevance to family unification, proton decay etc. Although there has been previous work into the classification of GUTs, we believe this is the first this broad question has been answered.

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A voyage through undulating dark matter and the GUTs of $u(48)$

Joseph Tooby-Smith
University of Cambridge, UK

Perimeter Institute, 15th December 2020

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Joseph Tooby-Smith



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Overview

Undulating DM based on:

2007.03662

with Joe Davighi and Matthew McCullough.

GUTs of $u(48)$

21xx.xxxxx

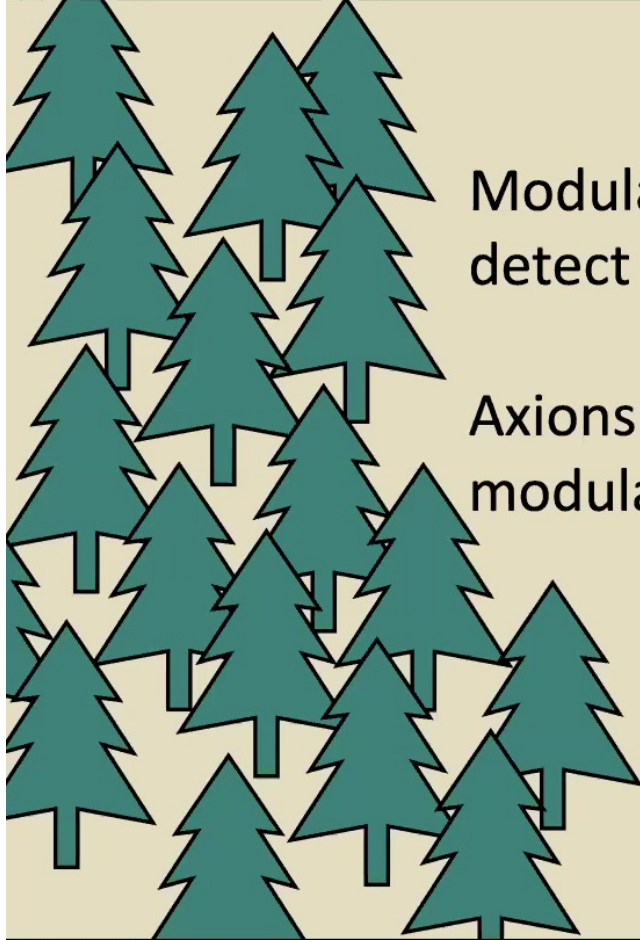
with Ben Gripaios and Ben Allanach.

The 1st half: Undulating DM

- Motivation
- Model
- UV extensions

The 2nd half: GUTs of $u(48)$

- The problem
- Why it's interesting
- The solution



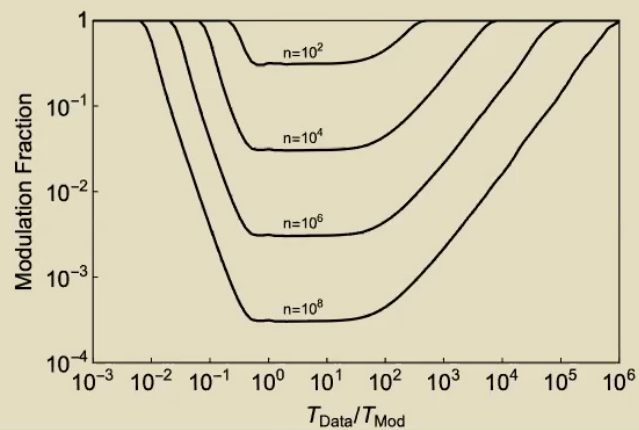
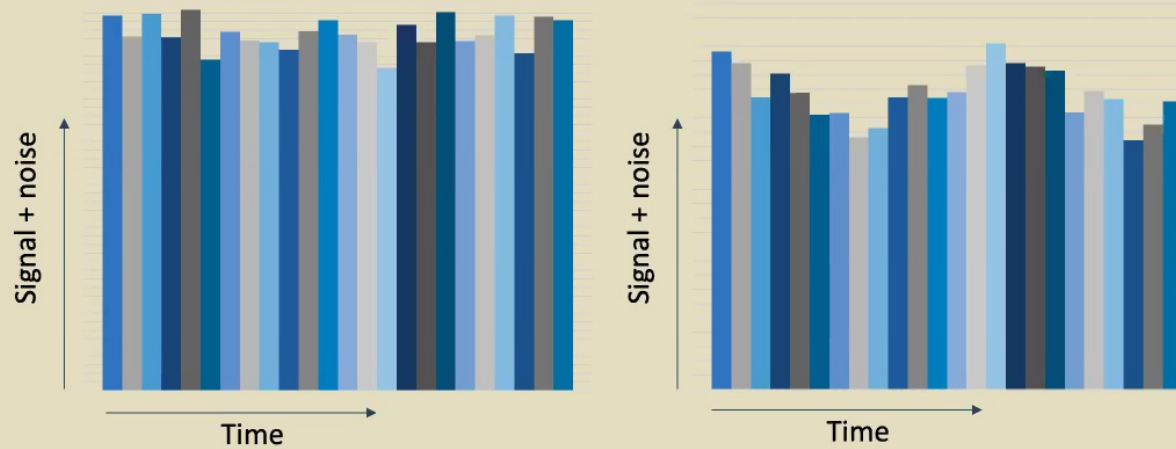
Modulations are easier to detect

Axions plus EDMs cause a modulation

The forest for the trees

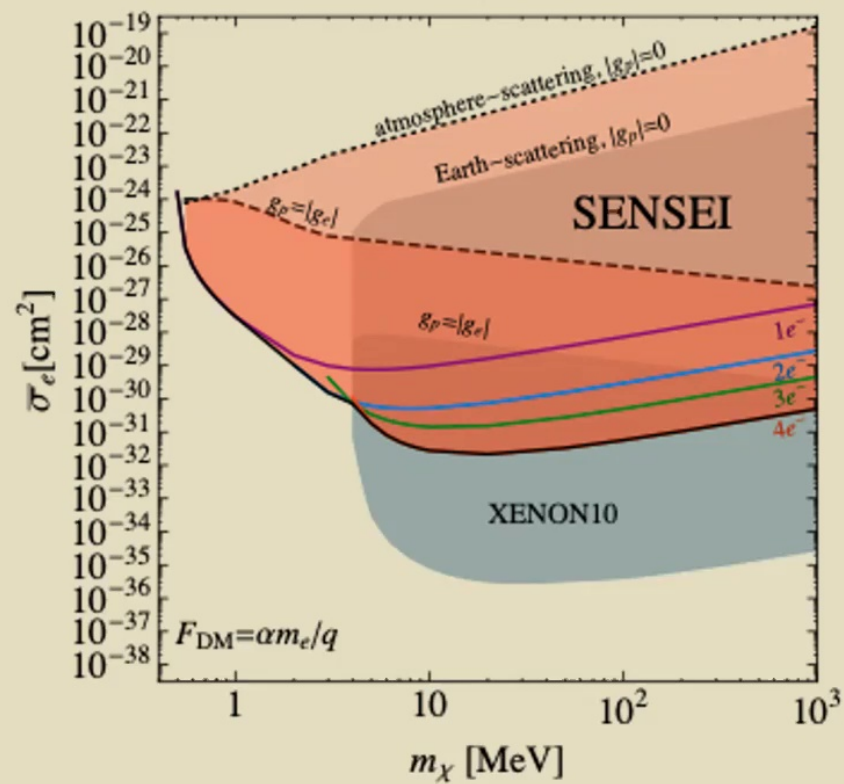


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Motivation:
Large
backgrounds





Motivation: Direct detection

- Plot taken from:
1804.00088 (SENSEI
collab)



CP-odd axion like particle

$$\phi \rightarrow -\phi$$

Cosmologically abundant

$$\ddot{\phi} + 3H\dot{\phi} + m_{\phi}^2\phi = 0$$

Gives a dark fermion EDM

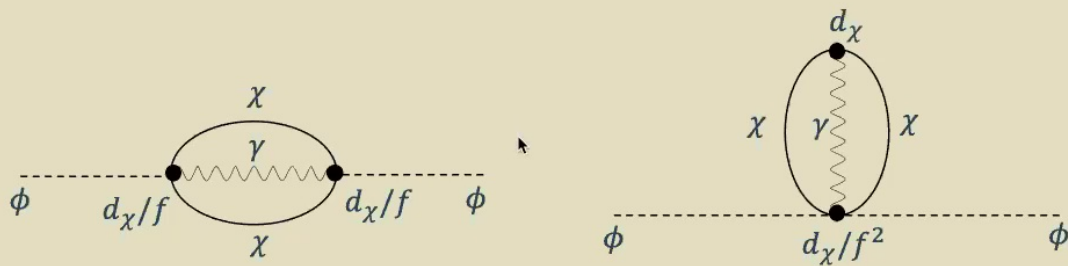
$$\mathcal{L}_{DM} \supset -c \underbrace{\frac{e}{2\Lambda} \sin\left(\frac{\phi}{f}\right)}_{d_{\chi}} \bar{\chi} \sigma^{\mu\nu} i\gamma_5 \chi F_{\mu\nu} + \text{MDM}$$

d_{χ}^{eff}

The Model:
Copying QCD



Corrections to axion mass

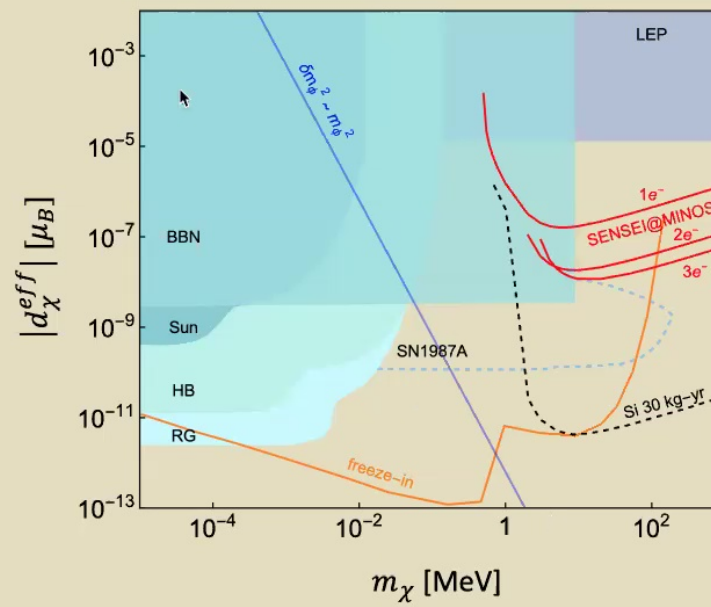


Fine tuning condition

$$\delta m_\phi^2 \lesssim m_\phi^2 \quad \Rightarrow \quad \frac{|d_\chi^{eff}|}{\mu_B} \lesssim 2 \times 10^{-12} \left(\frac{\text{MeV}}{m_\chi} \right)^3 \sqrt{r}$$

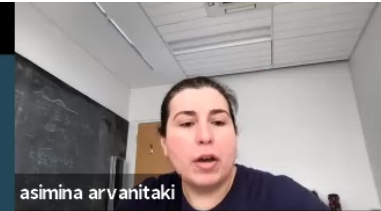
The Model:
Fine tuning



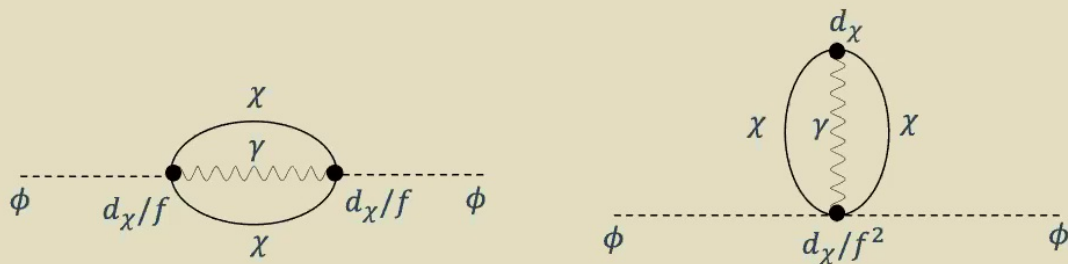


The Model: Other constraints

- 1911.03389 (Chang, Essig, Reinert)
- 1811.04095 (Chu, Pradler, Semmelrock)
- 2004.11378 (SENSEI collab)



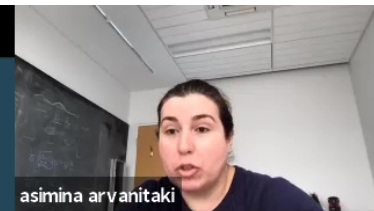
Corrections to axion mass



Fine tuning condition

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The Model:
Fine tuning



CP-odd axion like particle

$$\phi \rightarrow -\phi$$

Cosmologically abundant

$$\ddot{\phi} + 3H\dot{\phi} + m_{\phi}^2\phi = 0$$

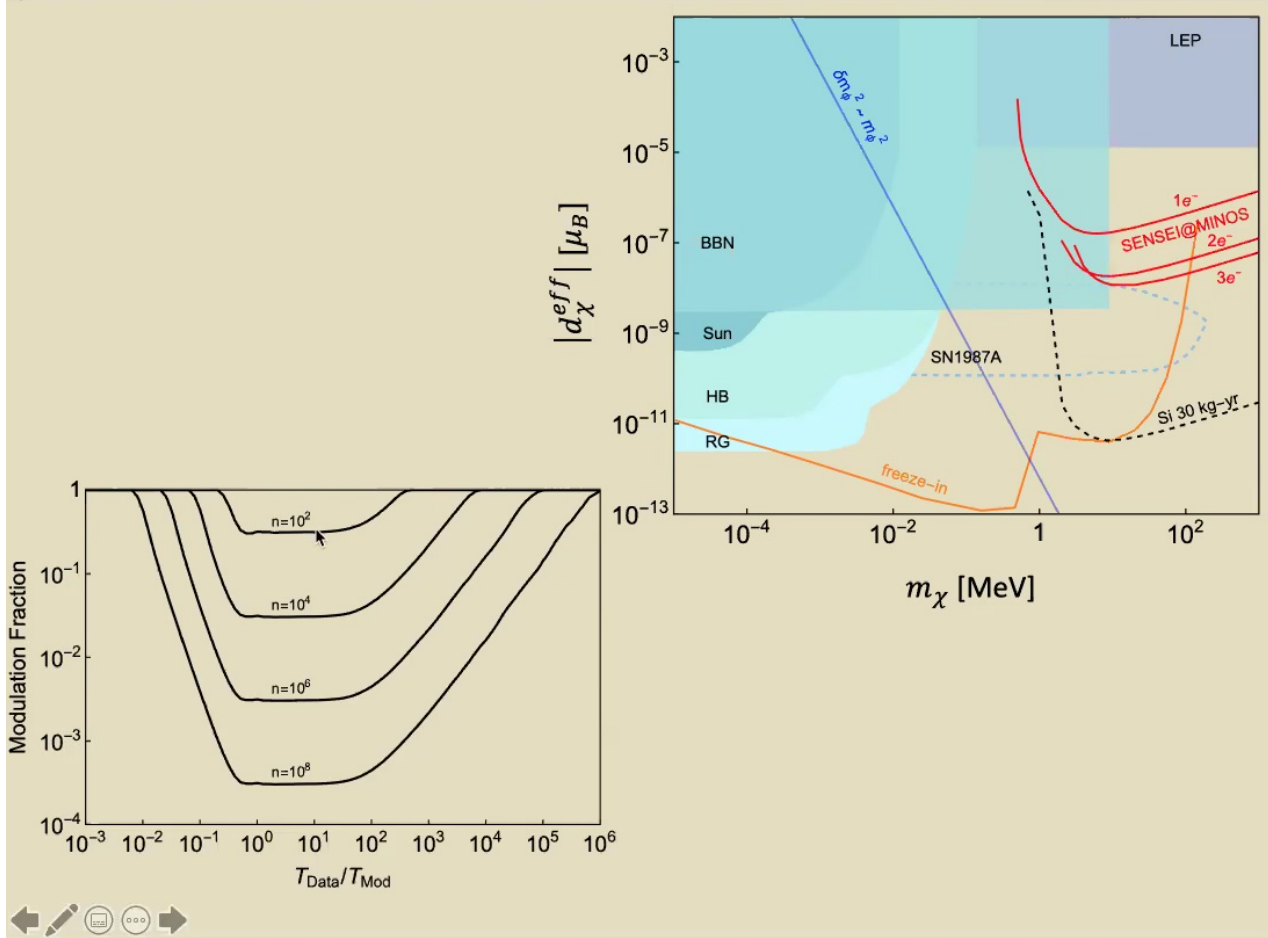
Gives a dark fermion EDM

$$\mathcal{L}_{DM} \supset -c \underbrace{\frac{e}{2\Lambda} \sin\left(\frac{\phi}{f}\right)}_{d_{\chi}} \bar{\chi} \sigma^{\mu\nu} i\gamma_5 \chi F_{\mu\nu} + \text{MDM}$$

$\underbrace{\hspace{10em}}_{d_{\chi}^{eff}}$

The Model:
Copying QCD





The Model: Other constraints

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EDM to take the form

$$d_\chi \approx \frac{e}{m_\chi^2} \frac{m_q^{\text{dark}}}{2}$$

Dark axion mass and fermionic

$$m_\phi^2 \approx \frac{m_q^{\text{dark}} |\langle \bar{q}q \rangle_d|}{f^2} \quad m_\chi^3 \approx 8\pi^2 \langle \bar{q}q \rangle_d$$

Overall

$$d_\chi \approx 4\pi^2 e \frac{m_\phi^2 f^2}{m_\chi^5}$$

UV
Extensions:
QCD-like
baryon

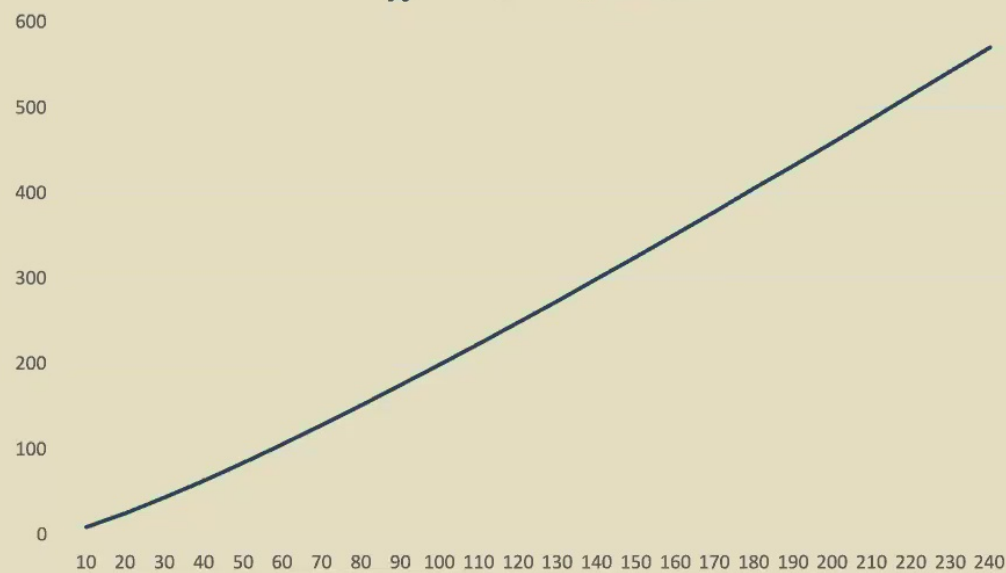
- /hep-ph/0504231 (Pospelov, Ritz)
- Ioffe 1981
- $10^{-20} \text{eV} \leq m_\phi \leq 10^{-15} \text{eV}$



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Large N_c and chiral limit

$$d_\chi \sim N_c \log(N_c)$$



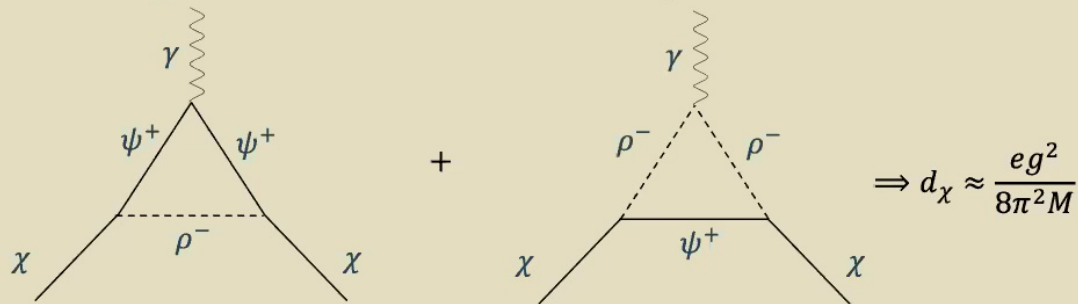
UV
Completions:
Large N_c

- /hep-ph/9212273
(Riggs, Schnitzer)

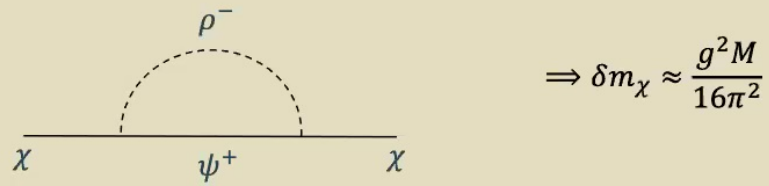


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Charged scalar and fermion, mass $\sim M$



Fine tuning



UV
completions:
Elementary
Fermion

- 1203.2531 (Graham et al)



Modulations are easy to detect

Coupling of ALP to fermion
EDM creates such modulations

1st half
summary



{ Time to stop thinking }



Modulations are easy to detect

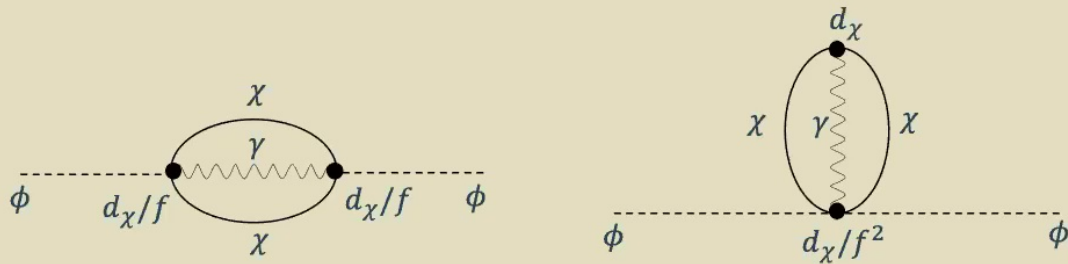
Coupling of ALP to fermion
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Corrections to axion mass



Fine tuning condition

$$\delta m_\phi^2 \lesssim m_\phi^2 \Rightarrow \frac{|d_\chi^{eff}|}{\mu_B} \lesssim 2 \times 10^{-12} \left(\frac{\text{MeV}}{m_\chi} \right)^3 \sqrt{r}$$

The Model:
Fine tuning



The origin of the word 'Academy'

- Gymnasiums were where Greek boys studied, and fought.
- Athens had three gymnasiums: the Lyceum, the Cynosarges, and the Academy
- After meeting Socrates, Plato formed a school of philosophy at the Academy.
- His student, Aristotle, later formed one at the Lyceum.



{ The GUTs of $u(48)$ }



The forest for
the trees

Find every semi-simple
subalgebra of
 $u(48)$ containing the SM



Setup: Anomaly Work

- See my BSM
Pandemic talk
(indico:950669)

Z' model – extend SM by $u(1)$

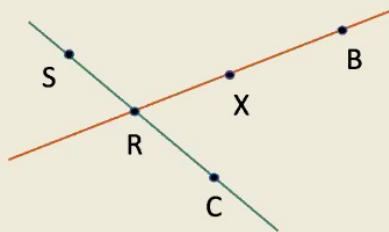
$$su(2) \oplus su(3) \oplus u(1) \oplus u(1)$$

Get a set of Diophantine equations

$$0 = \sum_{j=1}^3 (2Q_j + U_j + D_j), 0 = \sum_{j=1}^3 (3Q_j + L_j), 0 = \sum_{j=1}^3 (Q_j + 8U_j + 2D_j + 3L_j + 6E_j), \quad 0 = \sum_{j=1}^3 (6Q_j + 3U_j + 3D_j + 2L_j + E_j + N_j)$$

$$0 = \sum_{j=1}^3 (Q_j^2 - 2U_j^2 + D_j^2 - L_j^2 + E_j^2), 0 = \sum_{j=1}^3 (6Q_j^3 + 3U_j^3 + 3D_j^3 + 2L_j^3 + E_j^3 + N_j^3)$$

Use number theory



Setup: Algebras

Sub-algebras of $u(48)$

Allows for e.g. a kinetic term

Reductive

$$g_1 \oplus g_2 \oplus g_3 \oplus u(1) \oplus u(1)$$



Setup: Algebras

Sub-algebras of $u(48)$

Allows for e.g. a kinetic term

Reductive

$$g_1 \oplus g_2 \oplus g_3 \oplus u(1) \oplus u(1)$$

Semi-simple

$$g_1 \oplus g_2 \oplus g_3$$



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Setup: The Problem

Find every anomaly free semi-simple subalgebra of $u(48)$ which contains the SM



What has
been done
before?

e.g. Gell-Mann, Ramond and Slansky: one
independent gauge coupling

$$g \text{ or } g \oplus g$$

Method: The
two steps

1) Find every semi-simple subalgebra of $u(48)$

2) Which of these contain the SM





Method:
Subalgebras



Find every irrep $\dim \leq 48$ of simple algebras

$$g_n: (a_1, a_2, \dots, a_n)$$

Combine reducible reps $\dim \leq 48$

$$g_n: (a_1, a_2, \dots, a_n), (b_1, b_2, \dots, b_n)$$

$$g_n \oplus g'_l: (a_1, a_2, \dots, a_n, b_1, b_2, \dots, b_l)$$

$$g_n \oplus g'_l: (a_1, a_2, \dots, a_n, 0, \dots, 0), (0, \dots, 0, b_1, b_2, \dots, b_l)$$



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Method:
Subalgebras



Find every irrep $\dim \leq 48$ of simple algebras

$$g_n: (a_1, a_2, \dots, a_n)$$

Combine reducible reps $\dim \leq 48$

$$g_n: (a_1, a_2, \dots, a_n), (b_1, b_2, \dots, b_n)$$

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$$g_n \oplus g'_l: (a_1, a_2, \dots, a_n, 0, \dots, 0), (0, \dots, 0, b_1, b_2, \dots, b_l)$$

Anomaly free



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Method: A
slight
problem



As an estimate there are about

$$\sim 10^9 - 10^{10}$$

(1 a second – 40 years)



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Method:
Solution to
problem

1) Find every semi-simple subalgebra of $u(48)$

1) Find every semi-simple subalgebra of $u(48)$
without $su(2)$ ideals

$$g_1 \oplus g_2 \oplus g_3$$



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SM+RHN

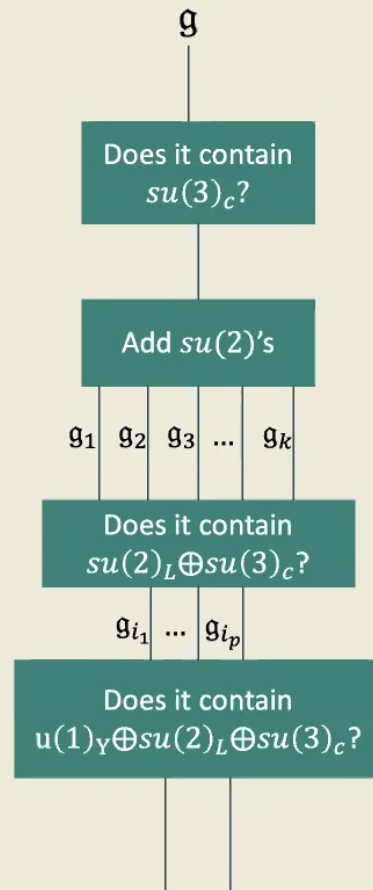
Q	$(2,3)_1$	$(2,3)_1$	$(2,3)_1$
U	$(1, \overline{3})_{-4}$	$(1, \overline{3})_{-4}$	$(1, \overline{3})_{-4}$
D	$(1, \overline{3})_2$	$(1, \overline{3})_2$	$(1, \overline{3})_2$
L	$(2,1)_{-3}$	$(2,1)_{-3}$	$(2,1)_{-3}$
E	$(1,1)_6$	$(1,1)_6$	$(1,1)_6$
N	$(1,1)_0$	$(1,1)_0$	$(1,1)_0$

$$su(2) \oplus su(3) \oplus u(1)$$



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Method: Containing SM



Results: The full results

- $A_n = \text{su}(n)$
- $B_n = \text{so}(2n+1)$
- $C_n = \text{sp}(2n)$
- $D_n = \text{so}(2n)$
- (Q, U, D, L, E, N)

1) A_4 $3(\bar{5} \rightarrow (0, 0, 1, 1, 0, 0))$ $3(10 \rightarrow (1, 1, 0, 0, 1, 0))$	2) D_5 $3(1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$	3) D_5 $3(1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$
4) $A_4 A_1$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $\bar{5}, 2 \rightarrow (0, 0, 2, 2, 0, 0)$ $10, 3 \rightarrow (3, 3, 0, 0, 3, 0)$	5) $A_4 A_1$ $\bar{5}, 3 \rightarrow (0, 0, 3, 3, 0, 0)$ $10, 3 \rightarrow (3, 3, 0, 0, 3, 0)$	6) $A_4 A_1$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $\bar{5}, 2 \rightarrow (0, 0, 2, 2, 0, 0)$ $3(10, 1 \rightarrow (1, 1, 0, 0, 1, 0))$
7) $A_4 A_1$ $3(\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0))$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$ $10, 2 \rightarrow (2, 2, 0, 0, 2, 0)$	8) $A_4 A_1$ $3(\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0))$ $10, 3 \rightarrow (3, 3, 0, 0, 3, 0)$	9) $A_4 A_1$ $\bar{5}, 3 \rightarrow (0, 0, 3, 3, 0, 0)$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$ $10, 2 \rightarrow (2, 2, 0, 0, 2, 0)$
10) $A_4 A_1$ $\bar{5}, 3 \rightarrow (0, 0, 3, 3, 0, 0)$ $3(10, 1 \rightarrow (1, 1, 0, 0, 1, 0))$	11) $A_4 A_1$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $\bar{5}, 2 \rightarrow (0, 0, 2, 2, 0, 0)$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$ $10, 2 \rightarrow (2, 2, 0, 0, 2, 0)$	12) $A_4 A_4$ $2(1, \bar{5} \rightarrow (0, 0, 1, 1, 0, 0))$ $2(1, 10 \rightarrow (1, 1, 0, 0, 1, 0))$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$
13) $A_4 D_5$ $1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1)$ $2(\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0))$ $2(10, 1 \rightarrow (1, 1, 0, 0, 1, 0))$	14) $A_4 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$	15) $A_4 D_5$ $1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1)$ $2(\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0))$ $2(10, 1 \rightarrow (1, 1, 0, 0, 1, 0))$
16) $A_4 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $\bar{5}, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $10, 1 \rightarrow (1, 1, 0, 0, 1, 0)$	17) $D_5 A_1$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$ $1\bar{6}, 2 \rightarrow (2, 2, 2, 2, 2, 2)$	18) $D_5 A_1$ $1\bar{6}, 3 \rightarrow (3, 3, 3, 3, 3, 3)$
19) $D_5 A_1$ $1\bar{6}, 3 \rightarrow (3, 3, 3, 3, 3, 3)$	20) $D_5 A_1$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$ $1\bar{6}, 2 \rightarrow (2, 2, 2, 2, 2, 2)$	21) $D_5 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$
22) $D_5 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$	23) $D_5 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$	24) $D_5 D_5$ $2(1, 1\bar{6} \rightarrow (1, 1, 1, 1, 1, 1))$ $1\bar{6}, 1 \rightarrow (1, 1, 1, 1, 1, 1)$
25) $A_{11} A_1 A_1$ $1\bar{2}, 2, 1 \rightarrow (0, 3, 3, 0, 3, 3)$ $1\bar{2}, 1, 2 \rightarrow (3, 0, 0, 3, 0, 0)$	26) $A_3 A_1 A_1$ $3(\bar{4}, 2, 1 \rightarrow (0, 1, 1, 0, 1, 1))$ $3(\bar{4}, 1, 2 \rightarrow (1, 0, 0, 1, 0, 0))$	27) $A_3 A_3 A_1$ $3(1, 4, 2 \rightarrow (1, 0, 0, 1, 0, 0))$ $6, \bar{4}, 1 \rightarrow (0, 3, 3, 0, 3, 3)$
28) $A_3 A_3 C_3$ $1, 4, 6 \rightarrow (3, 0, 0, 3, 0, 0)$ $6, \bar{4}, 1 \rightarrow (0, 3, 3, 0, 3, 3)$	29) $A_3 C_3 A_1$ $\bar{4}, 6, 1 \rightarrow (0, 3, 3, 0, 3, 3)$ $3(\bar{4}, 1, 2 \rightarrow (1, 0, 0, 1, 0, 0))$	30) $A_3 C_3 A_1$ $3(\bar{4}, 1, 2 \rightarrow (0, 1, 1, 0, 1, 1))$ $4, 6, 1 \rightarrow (3, 0, 0, 3, 0, 0)$
31) $A_3 C_3 C_3$ $\bar{4}, 1, 6 \rightarrow (0, 3, 3, 0, 3, 3)$ $4, 6, 1 \rightarrow (3, 0, 0, 3, 0, 0)$	32) $A_4 A_1 A_1$ $\bar{5}, 3, 1 \rightarrow (0, 0, 3, 3, 0, 0)$ $10, 1, 3 \rightarrow (3, 3, 0, 0, 3, 0)$	33) $A_4 A_1 A_1$ $\bar{5}, 1, 1 \rightarrow (0, 0, 1, 1, 0, 0)$ $\bar{5}, 2, 1 \rightarrow (0, 0, 2, 2, 0, 0)$ $10, 1, 1 \rightarrow (1, 1, 0, 0, 1, 0)$ $10, 1, 2 \rightarrow (2, 2, 0, 0, 2, 0)$

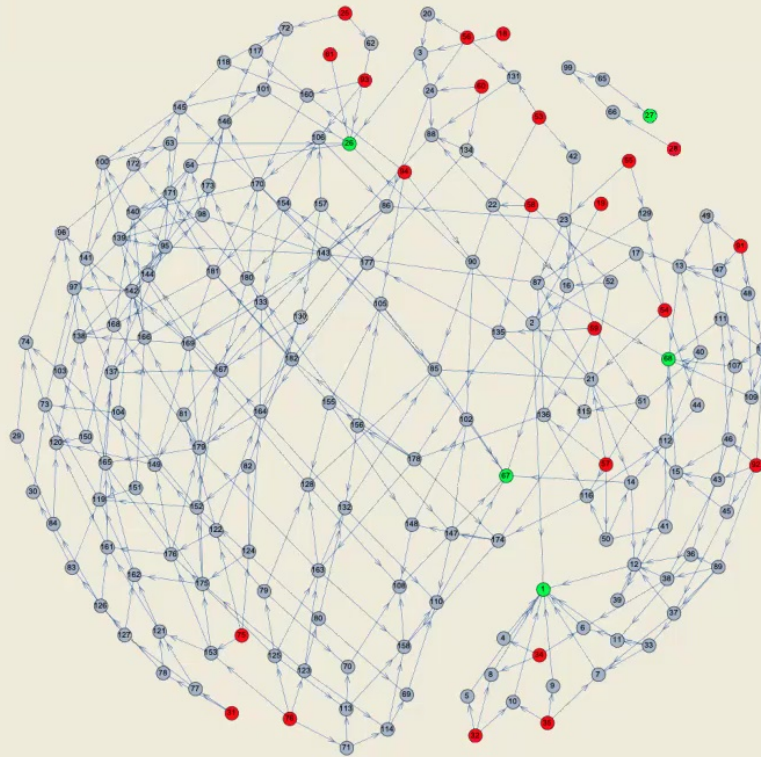
182 all together



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Results:
Maximal and
Minimal

Maximal: no g' such that $g \subset g' \subset u(48)$
Minimal: no g' such that $g' \subset g \subset u(48)$



Maximal
28) A3A3C3
31) A3C3C3
58) D5D5D5
94) A7D5A1A1

Minimal
1) A4
27) A3A3A1
67) A3A4A1A1



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The future:
Checks

The Mathematica program LieART

Embeddings branch reps

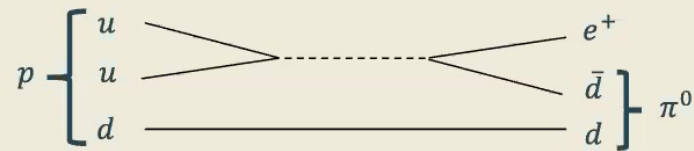
Check for known things



The future:
Further
analysis

Relationship to the unification group $U(3)^6$

Proton decay



Analytic approach



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2nd half
summary

Aim: Find all semi-simple subalgebras of $u(48)$ which contain the SM

Conclusion: There are 182 of them



Thank you for your
attention!

