

Title: Unconstrained tree tensor simulations for high-dimensional quantum many-body simulations

Speakers: Simone Montangero

Collection: Tensor Networks: from Simulations to Holography III

Date: November 20, 2020 - 9:00 AM

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Abstract: We present some recent results on the development of efficient unconstrained tree tensor networks algorithms and their application to high-dimensional many-body quantum systems. In particular, we present our results on topological two-dimensional systems, two-dimensional Rydberg atom systems, and two- and three-dimensional lattice gauge theories in presence of fermionic matter. Finally, we present their application to the study of open many-body quantum systems and in particular to the computation of the entanglement of formation in critical many-body quantum systems, resulting in the generalization of the Calabrese-Cardy formula to open systems.



UNCONSTRAINED TREE TENSOR NETWORKS SIMULATIONS

Simone Montangelo
University of Padova



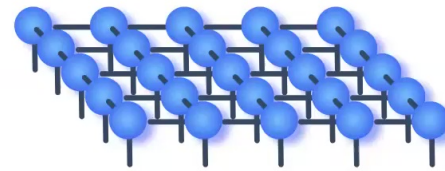
Dipartimento
di Fisica
e Astronomia
Galileo Galilei



UNIVERSITÀ
DEGLI STUDI
DI PADOVA

TENSOR NETWORKS STATES

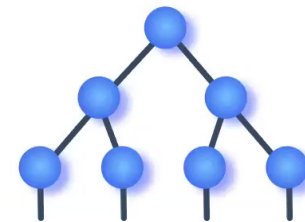
$$\psi_{\alpha_1, \alpha_2, \dots, \alpha_N} \quad \mathcal{O}(d^N)$$



PEPS



$$A_{\alpha_1}^{\beta_1} A_{\alpha_2}^{\beta_1 \beta_2} \dots A_{\alpha_N}^{\beta_{N-1}} \quad \mathcal{O}(Ndm^2)$$

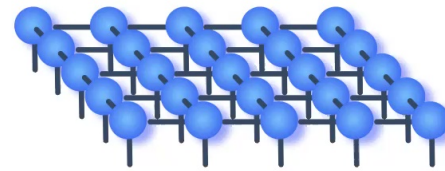


Tree Tensor Network

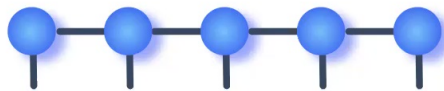


TENSOR NETWORKS STATES

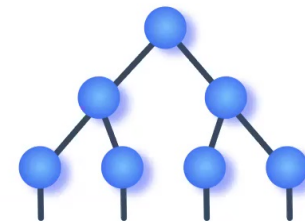
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$$A_{\alpha_1}^{\beta_1} A_{\alpha_2}^{\beta_1 \beta_2} \dots A_{\alpha_N}^{\beta_{N-1}} \quad \mathcal{O}(Ndm^2)$$

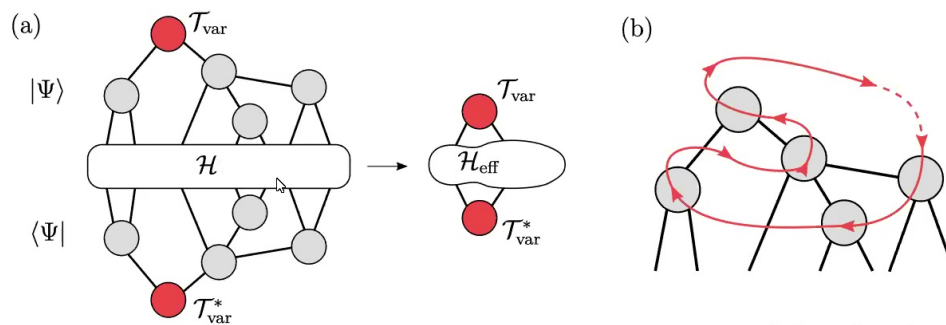
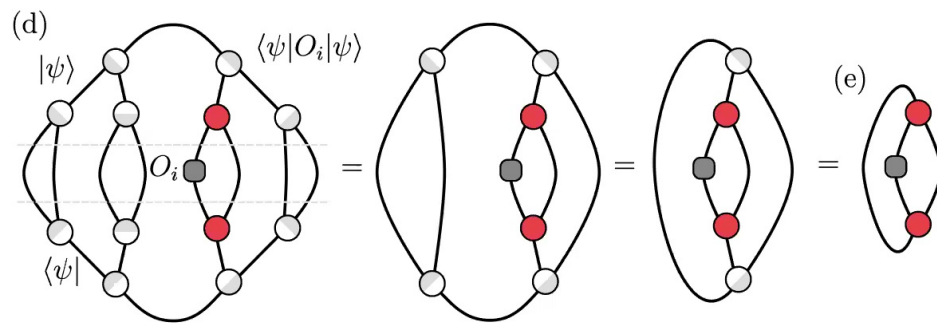
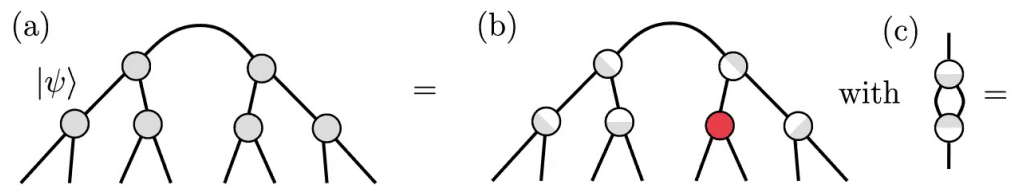


Tree Tensor Network

Tensor networks states are a compressed description of the system tunable between mean field and exact



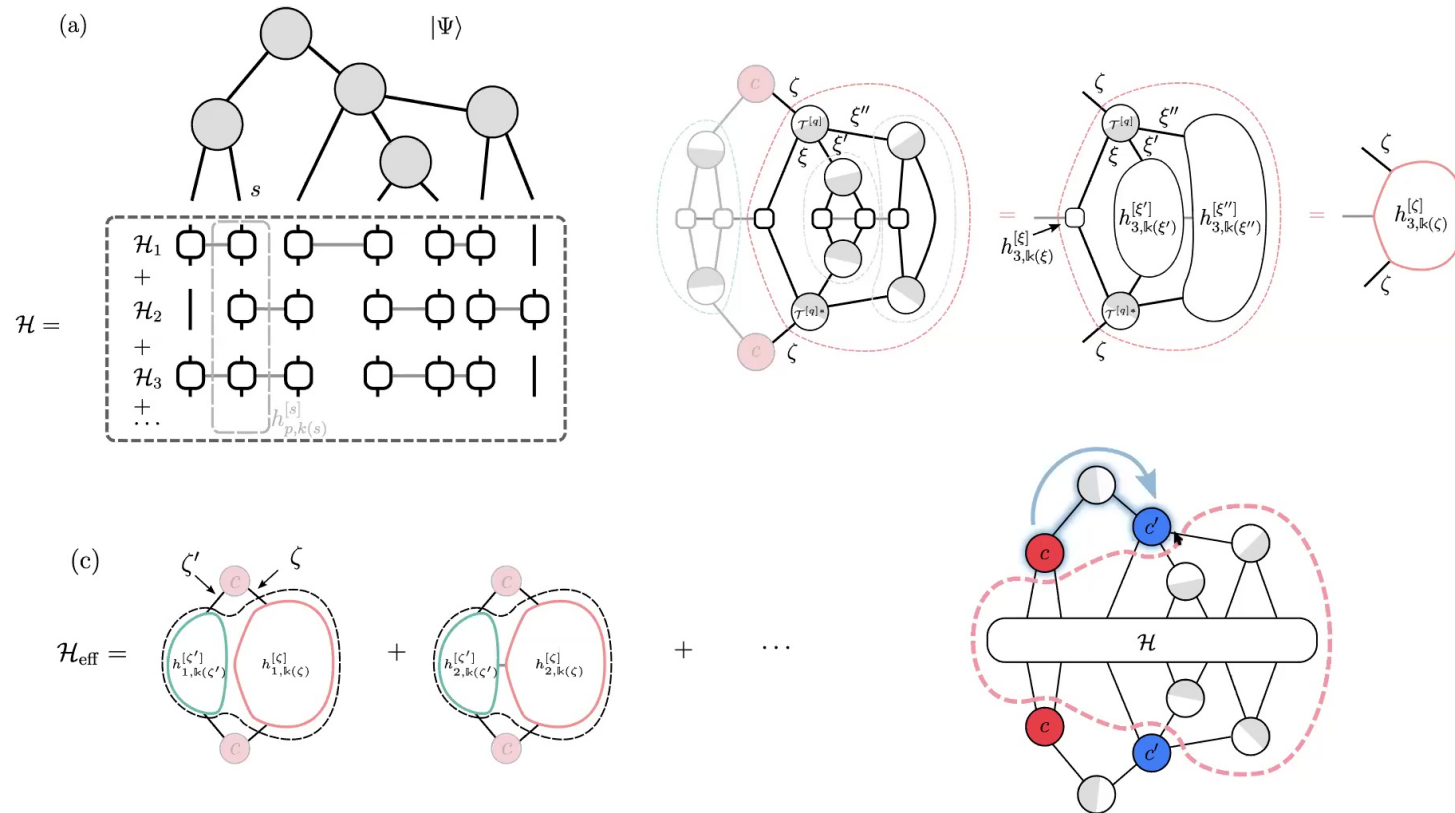
UNCONSTRAINED TREE TENSOR NETWORKS



P. Silvi et al. SciPost Phys. Lect. Notes 8 (2019)



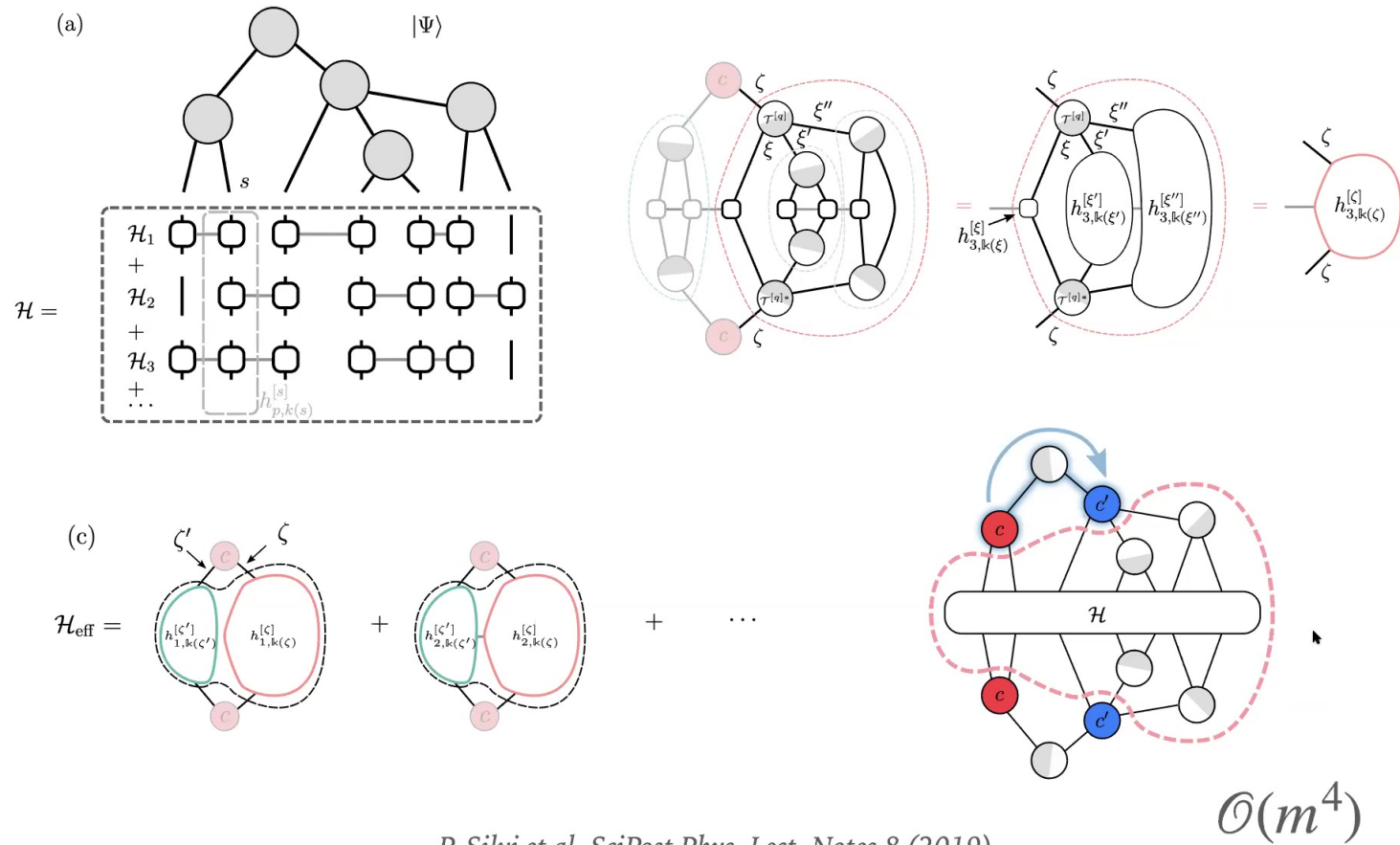
VARIATIONAL MINIMIZATION



P. Silvi et al. *SciPost Phys. Lect. Notes* 8 (2019)



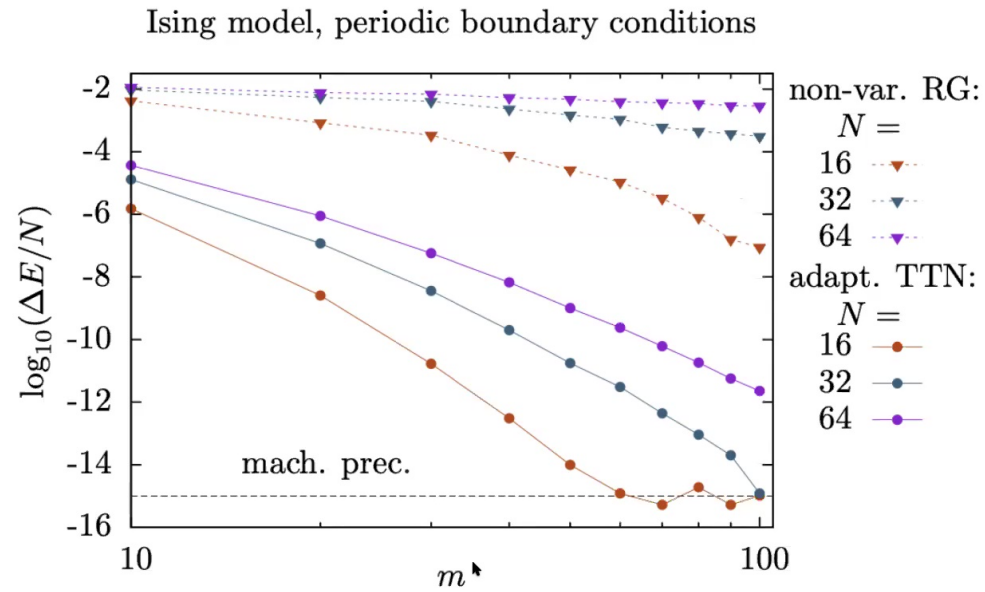
VARIATIONAL MINIMIZATION



P. Silvi et al. SciPost Phys. Lect. Notes 8 (2019)



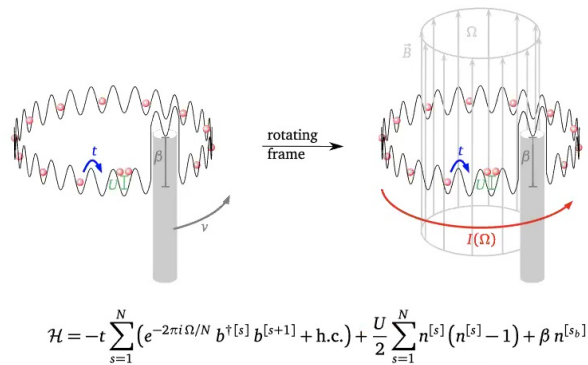
VARIATIONAL MINIMIZATION



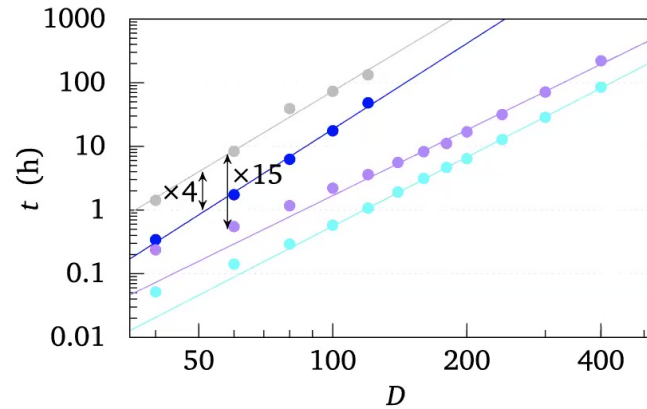
P. Silvi et al. SciPost Phys. Lect. Notes 8 (2019)

$$\mathcal{O}(m^4)$$

PERFORMANCE



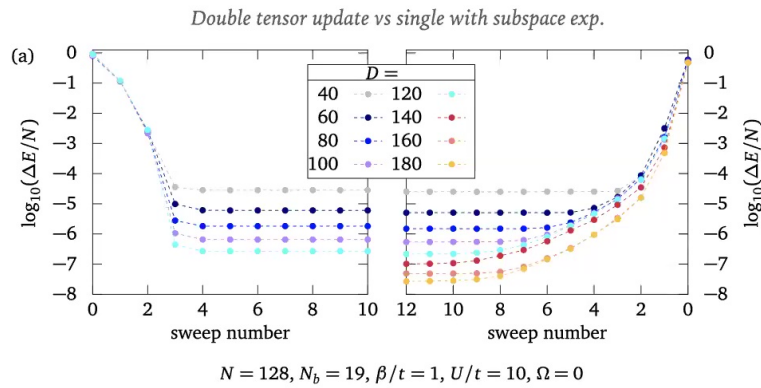
Bose Hubbard Ring



- single-tens. (no sym.)
- double-tens.
- single-tens. with subsp. exp.
- single-tens. (fixed link reps.)

$(t \propto D^\beta), \beta =$

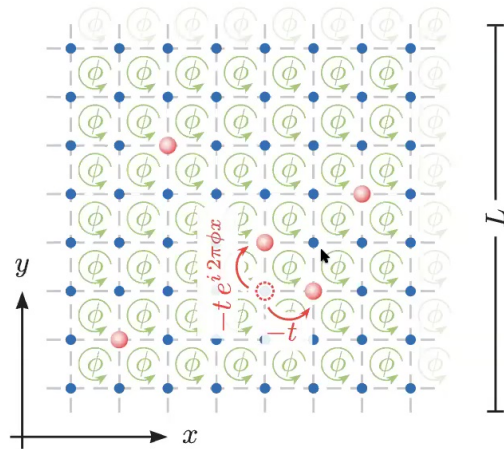
- 4.2
- 4.5
- 3.4
- 3.6



S. White PRB (2005), C. Hubig et al. PRB (2015)



INTERACTING HOFSTADTER MODEL

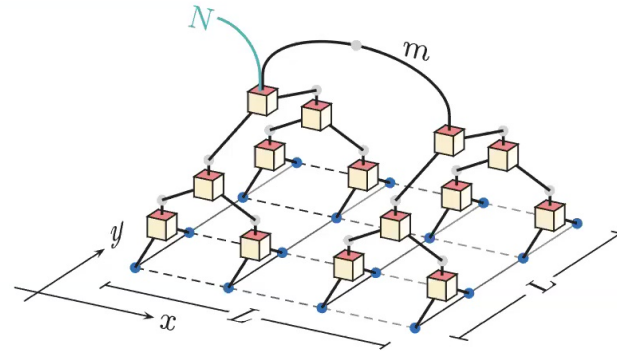
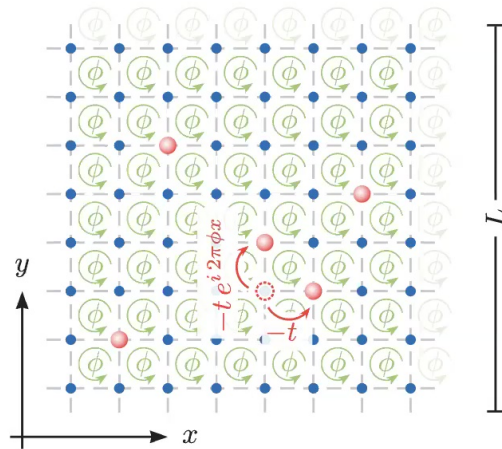


$$H = U \sum_{x,y} n_{x,y} (n_{x,y} - 1) - t \sum_{x,y} \{ a_{x+1,y}^\dagger a_{x,y} e^{-i2\pi\delta_x L \theta_x} + a_{x,y+1}^\dagger a_{x,y} e^{i2\pi(\phi x - \delta_y L \theta_y)} + \text{H.c.} \}$$

*Spinless bosons
with magnetic field*



INTERACTING HOFSTADTER MODEL

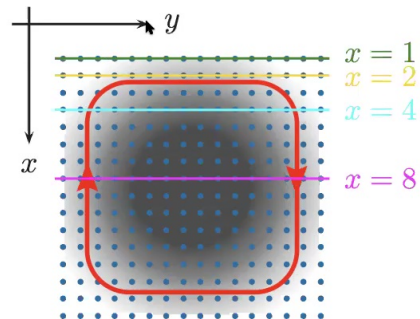


$$H = U \sum_{x,y} n_{x,y} (n_{x,y} - 1) - t \sum_{x,y} \{ a_{x+1,y}^\dagger a_{x,y} e^{-i 2\pi \delta_x L \theta_x} + a_{x,y+1}^\dagger a_{x,y} e^{i 2\pi (\phi x - \delta_y L \theta_y)} + \text{H.c.} \}$$

Filling factor

$$\nu = N / (\phi L^2) = 1/q$$

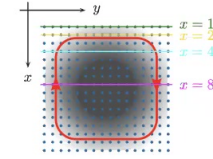
Laughlin wave function?



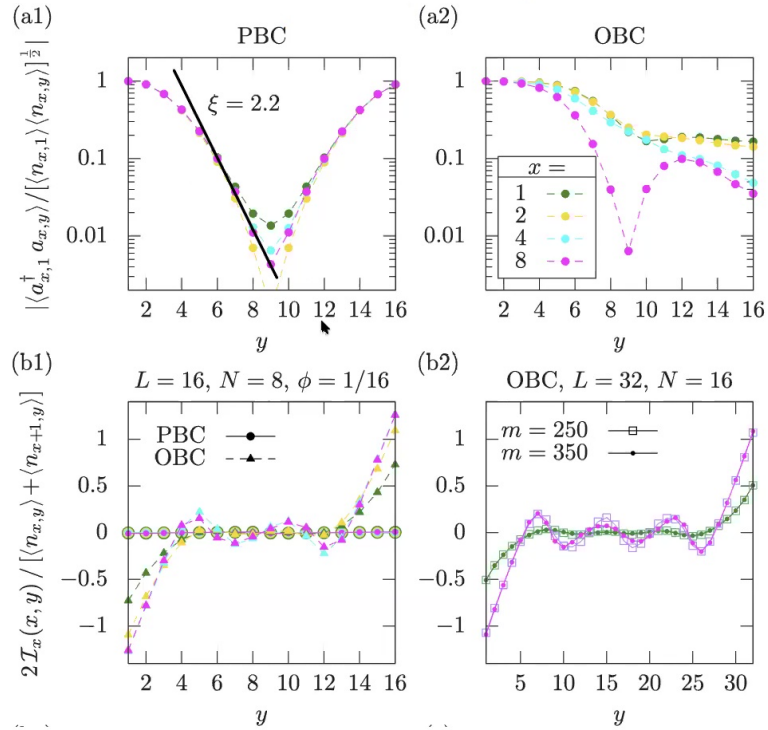
Spinless bosons
with magnetic field



RESULTS

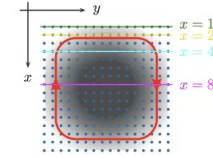


Correlations and Edge Currents

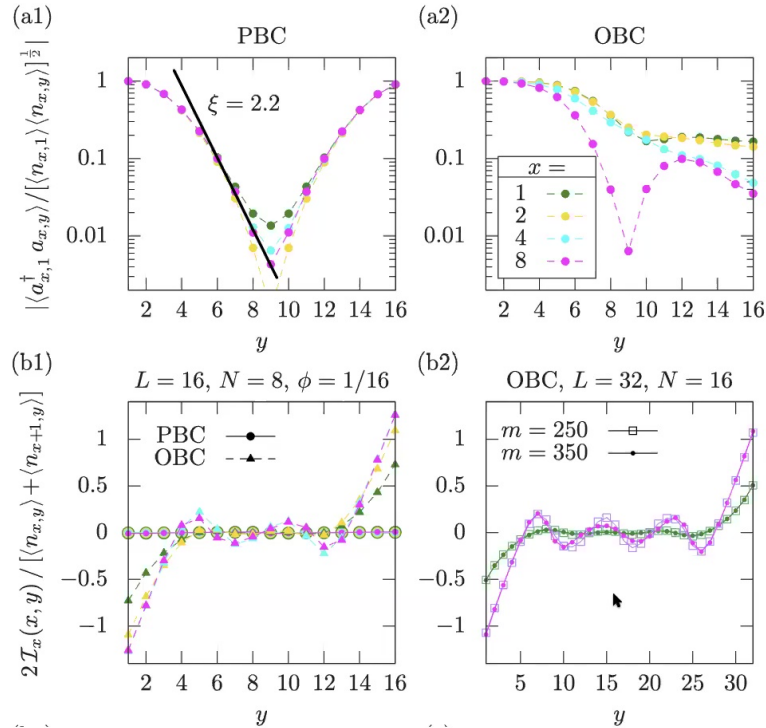


M. Gerster et al. Phys. Rev. B (2017)

RESULTS

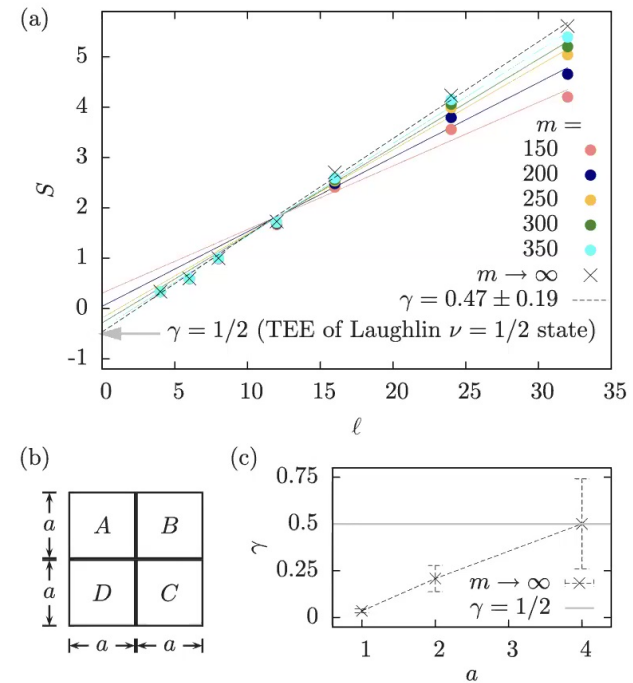


Correlations and Edge Currents



Many-body Cern number

Topological entanglement entropy



Compatible with $\nu = 1/2$ fractional QH

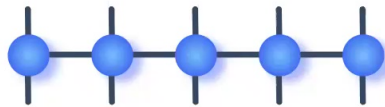
M. Gerster et al. Phys. Rev. B (2017)

TN REPRESENTATION OF MIXED QUANTUM STATES

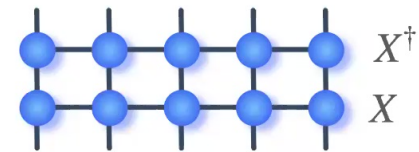


$$\rho = \sum p_j |\psi_j\rangle\langle\psi_j|$$

$$\rho = XX^\dagger$$



MPDO



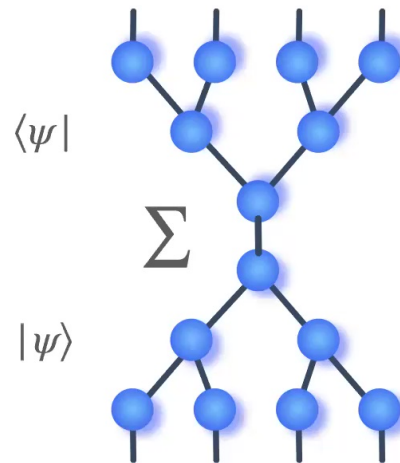
LPTN

Loopless Positive?

F. Verstraete et al. (2004)

G. de las Cuevas et al. (2013)

*Quantum jumps,
Purification...*



TTO

Positive Looped

A. Werner et al (2016)

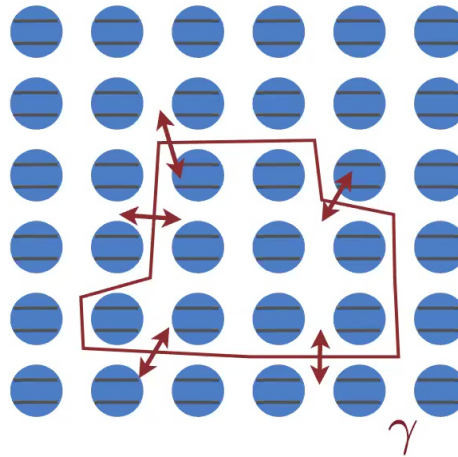
*Loopless
and
positive!*

ENTANGLEMENT OF MIXED QUANTUM SYSTEMS

For pure states:

$$\mathcal{S} = -\text{Tr} \rho \log \rho$$

Von Neumann Entropy



Area law

$$\mathcal{S} \propto \gamma$$

$$\mathcal{S} \propto N^{(D-1)}$$

1D critical systems:

$$\mathcal{S} = \frac{c}{3} \log N$$

For mixed states:

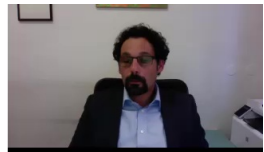
$$E_F(\rho) = \inf_{\{p_j, \psi_j\}} \left\{ \sum_j p_j \mathcal{S}(|\psi_j\rangle) : \rho = \sum_j p_j |\psi_j\rangle\langle\psi_j| \right\}$$

$$E_F(\rho, T) \stackrel{?}{\propto} \log N^{c/3}$$

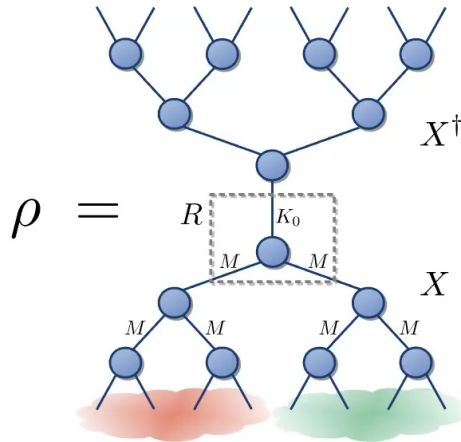
Entanglement of formation

C.H. Bennet et al. PRA 1996

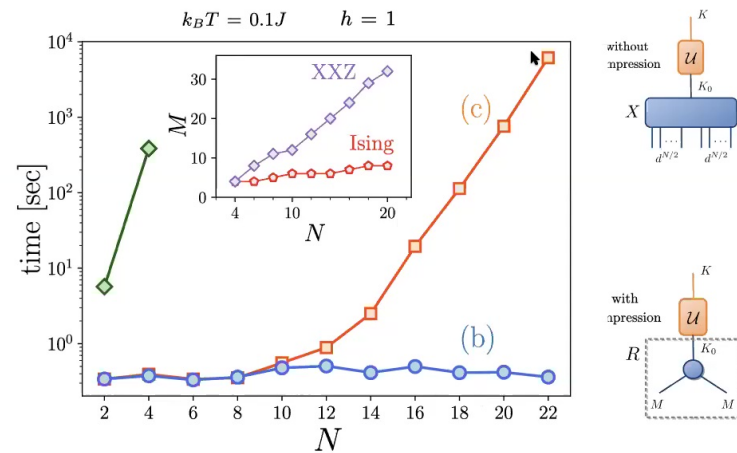
J. Eisert et al. Rev. Mod. Phys. 2009



TREE TENSOR OPERATORS



$$E_F(\rho) = \min_{K \geq K_0} \inf_{\mathcal{U}} \left\{ \sum_{j=1}^K p_j \mathcal{S}(|\psi'_j\rangle) : X' = X\mathcal{U} \right\}$$



$$\hat{H}_{Ising} = J \sum_{i=1}^N (\hat{\sigma}_i^x \hat{\sigma}_{i+1}^x + h \hat{\sigma}_i^z)$$

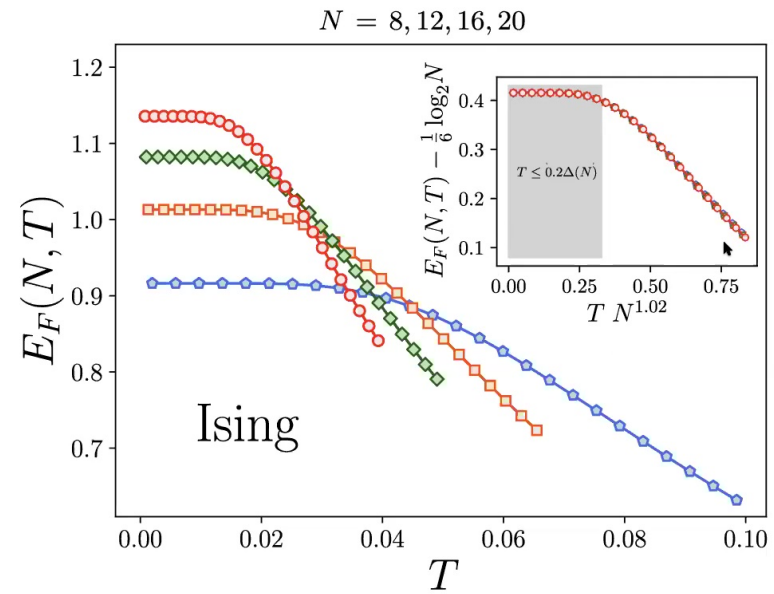
$$\hat{H}_{XXZ} = J \sum_{j=1}^N (\hat{\sigma}_j^x \hat{\sigma}_{j+1}^x + \hat{\sigma}_j^y \hat{\sigma}_{j+1}^y + \xi \hat{\sigma}_j^z \hat{\sigma}_{j+1}^z)$$

Thermal equilibrium state
(Mixture of K_0 Boltzmann factors)

$$X = \frac{1}{\sqrt{Z}} \sum_j^{K_0} e^{-E_j/2T} |\psi_j\rangle \langle j|$$

L. Arceci, P. Silvi, and S. Montangero arXiv:2011.01247

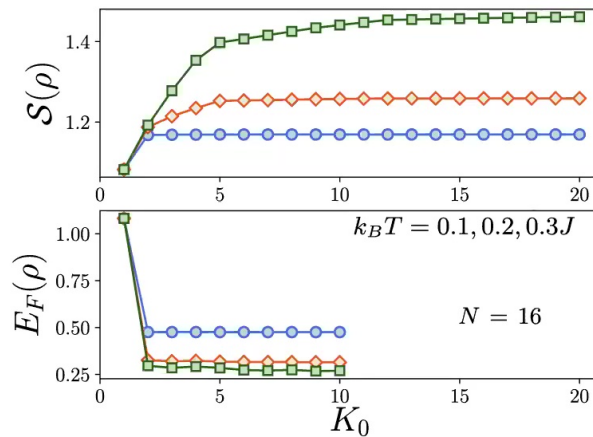
CONFORMAL SCALING OF ENTANGLEMENT OF FORMATION



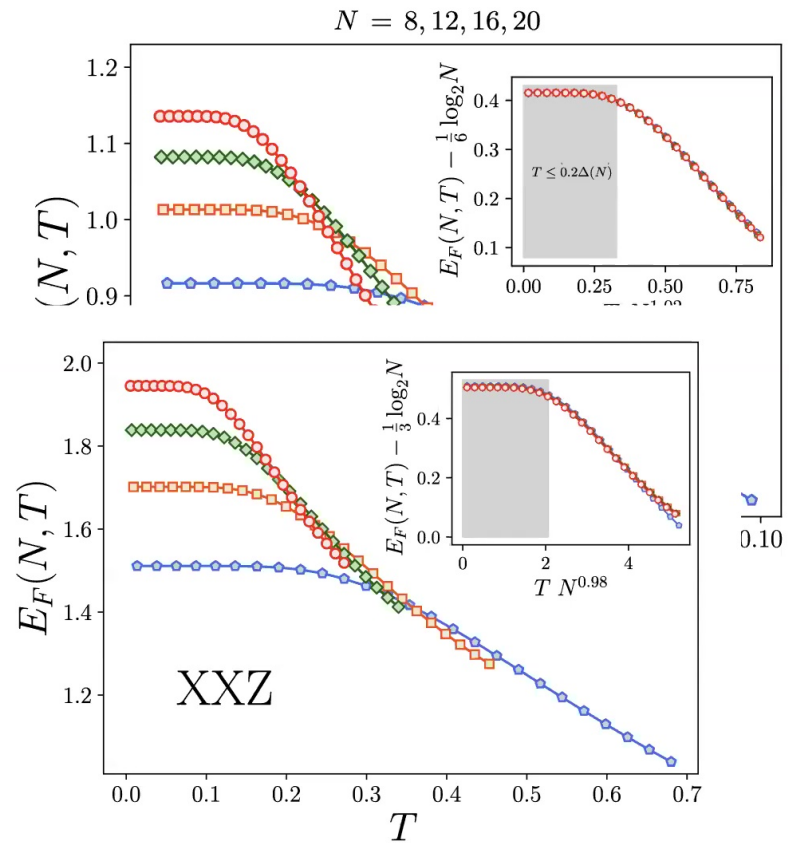
L. Arceci, P. Silvi, and S. Montangero arXiv:2011.01247

CONFORMAL SCALING OF ENTANGLEMENT OF FORMATION

$$E_F = \log(N^{c/3} f(TN^z))$$

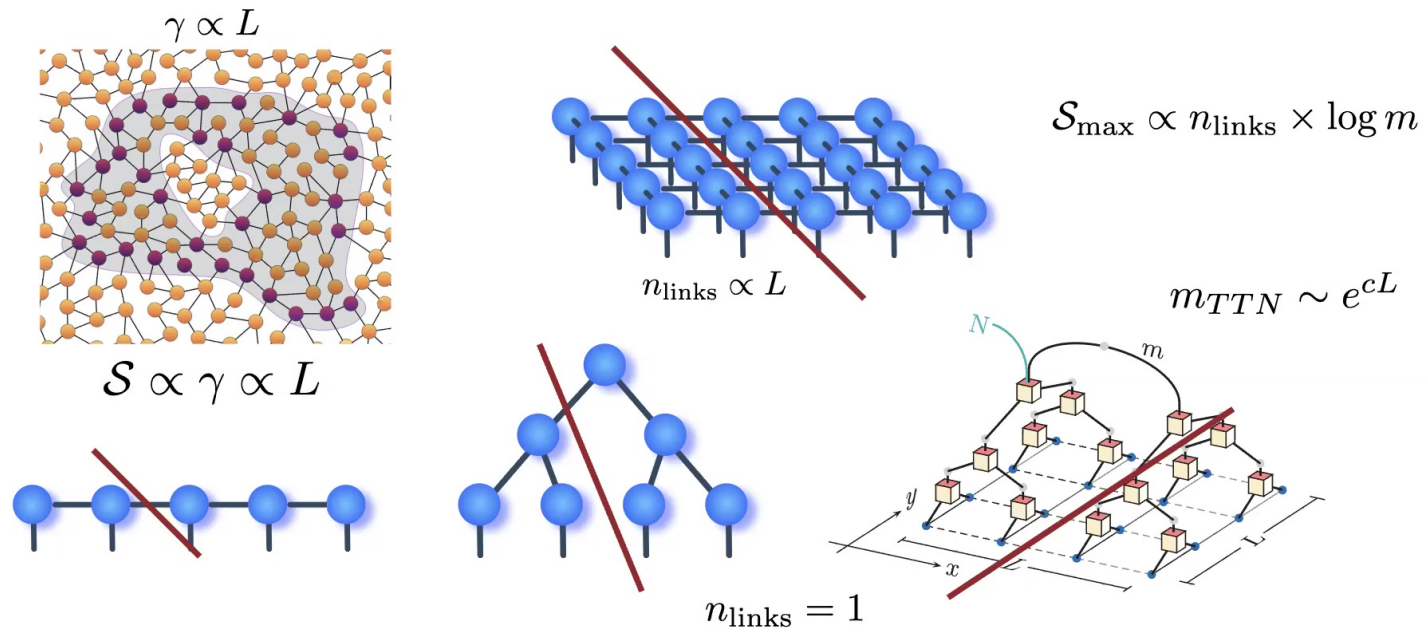


Numerical complexity depends on entropy, not entanglement!



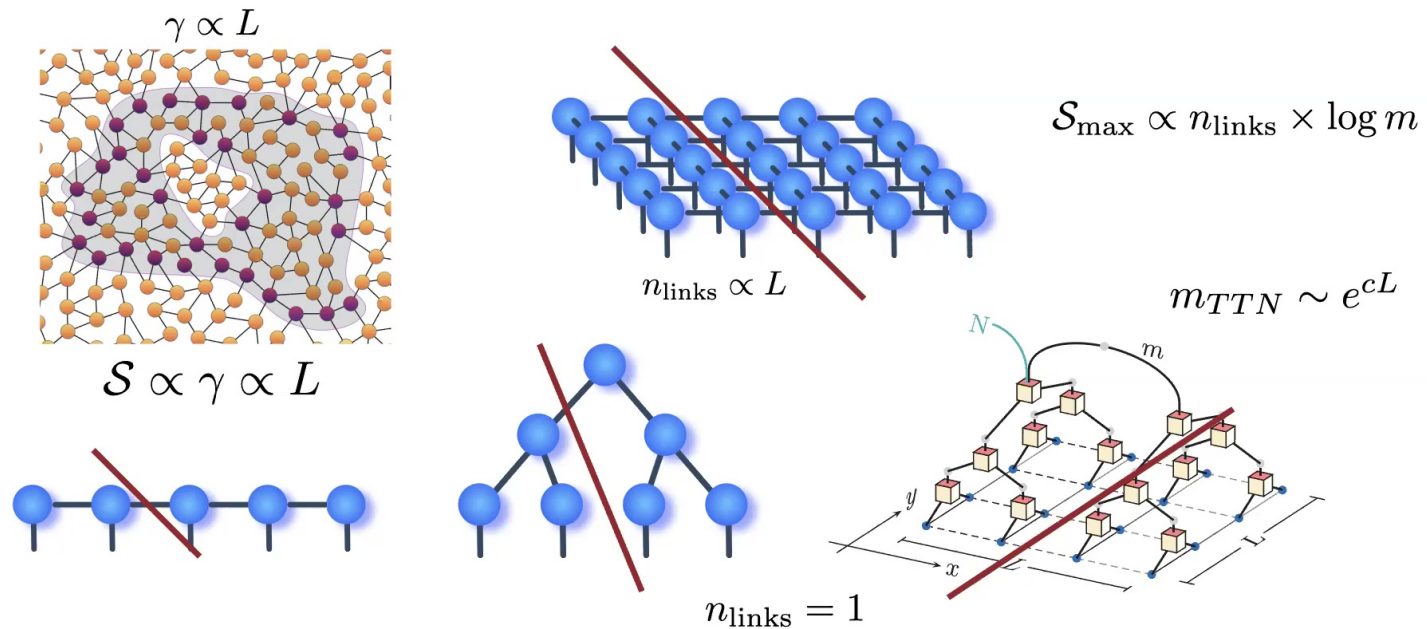
L. Arceci, P. Silvi, and S. Montangero arXiv:2011.01247

AREA LAWS AND TENSOR NETWORKS



Tensor Network	Complexity	Area law in 2D	Typical Bond dimensions	Exact contractable
MPS / DMRG	$\mathcal{O}\{\chi^3\}$	No (Only in 1D)	> 10.000	Yes ($\mathcal{O}\{\chi^3\}$)
TTN	$\mathcal{O}\{\chi^4\}$	No (Only in 1D)	$\approx 1.000 - 2.000$	Yes ($\mathcal{O}\{\chi^4\}$)
PEPS	$\mathcal{O}\{\chi^{10}\}$	Yes	~ 10	No ($\mathcal{O}\{\chi^L\}$)
MERA	$\mathcal{O}\{\chi^8\}$ (1D), $\mathcal{O}\{\chi^{16}\}$ (2D)	Yes	~ 10	Yes ($\mathcal{O}\{\chi^8\}$)

AREA LAWS AND TENSOR NETWORKS



Tensor Network	Complexity	Area law in 2D	Typical Bond dimensions	Exact contractable
MPS / DMRG	$\mathcal{O}\{\chi^3\}$	No (Only in 1D)	> 10.000	Yes ($\mathcal{O}\{\chi^3\}$)
TTN	$\mathcal{O}\{\chi^4\}$	No (Only in 1D)	$\approx 1.000 - 2.000$	Yes ($\mathcal{O}\{\chi^4\}$)
PEPS	$\mathcal{O}\{\chi^{10}\}$	Yes	~ 10	No ($\mathcal{O}\{\chi^L\}$)
MERA	$\mathcal{O}\{\chi^8\}$ (1D), $\mathcal{O}\{\chi^{16}\}$ (2D)	Yes	~ 10	Yes ($\mathcal{O}\{\chi^8\}$)
aTTN	$\mathcal{O}\{\chi^4\}$	Yes*	≈ 500	Yes ($\mathcal{O}\{\chi^4\}$)

AUGMENTED TREE TENSOR NETWORKS

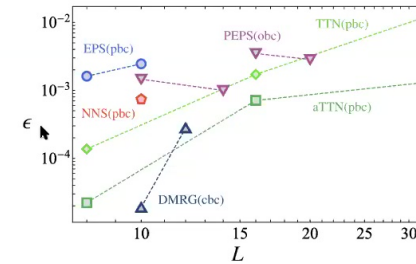
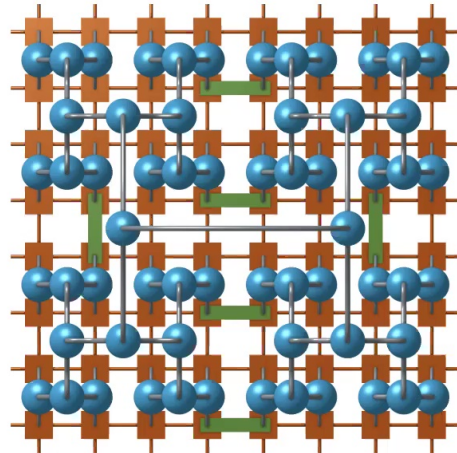
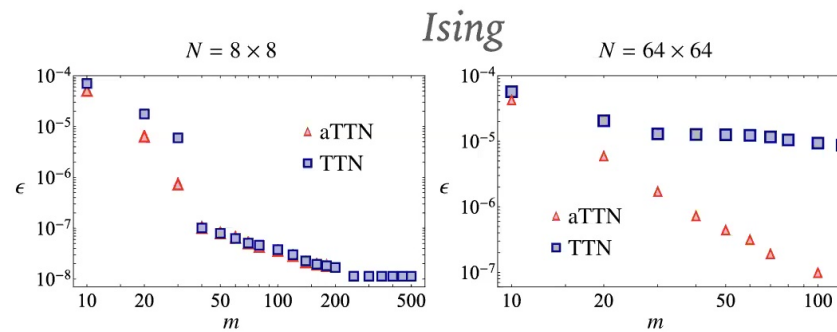
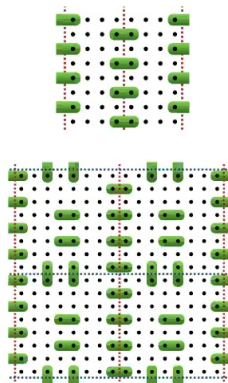


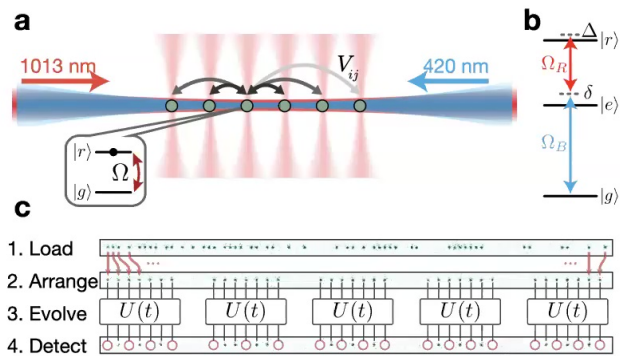
FIG. 2: Relative error ϵ of the 2D Heisenberg ground-state energy as a function of the system linear size L compared with the best available estimates obtained by MC [21] for the TTN, aTTN, NNS [59], EPS [60], PEPS [61], 2D-DMRG [57]. Depending on the method open (abc), cylindrical (cbe) or periodic (pbc) boundary conditions have been chosen. For each datapoint, we compare the Monte Carlo result with the same boundary conditions.



T. Felser, S. Notarnicola, S. Montangero arXiv:2011.08200

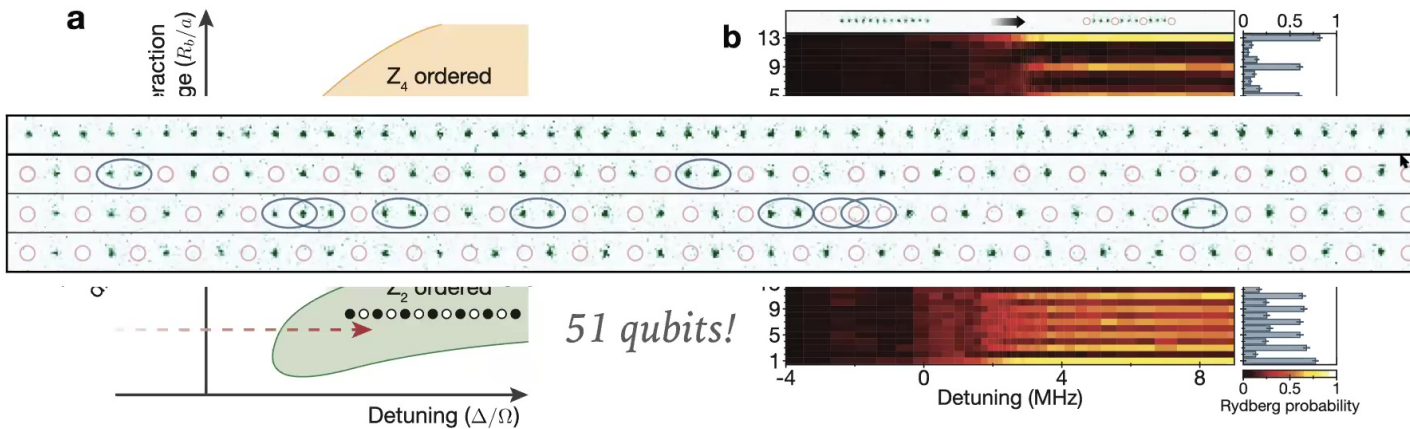


QUANTUM SIMULATION OF MANY-BODY CORRELATED DYNAMICS

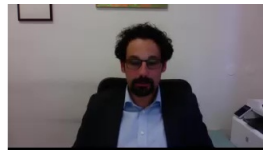


$$\frac{\mathcal{H}}{\hbar} = \sum_i \frac{\Omega_i}{2} \sigma_x^i - \sum_i \Delta_i n_i + \sum_{i < j} V_{ij} n_i n_j,$$

Rydberg Blockade

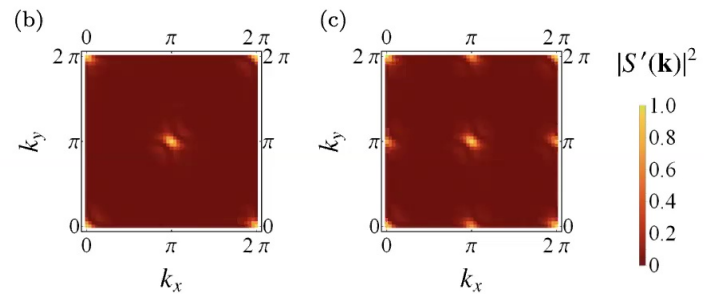
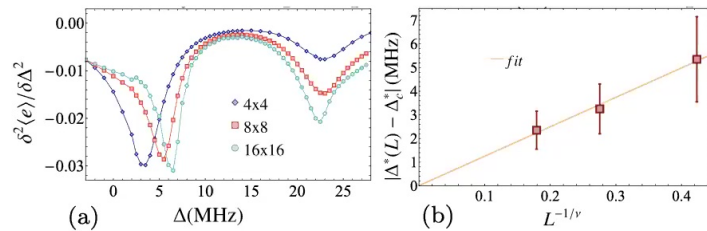
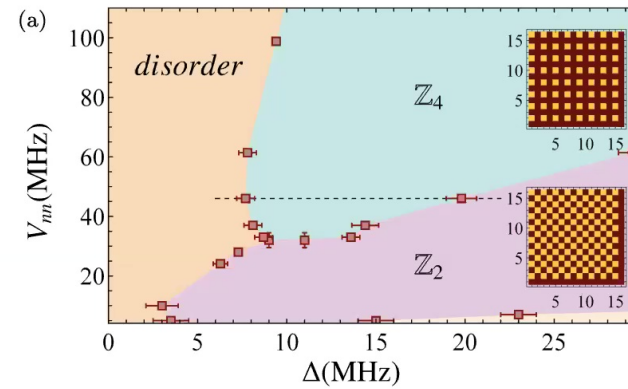
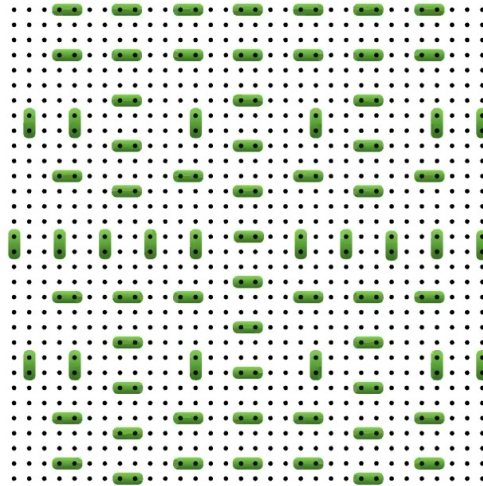


M. Lukin's group Nature (2017)



RYDBERG QUANTUM SIMULATOR

32x32 sites



Quantum Technologies for Lattice Gauge Theories

Simulating Lattice Gauge Theories within Quantum Technologies

M.C. Bañuls^{1,2}, R. Blatt^{3,4}, J. Catani^{5,6,7}, A. Celi^{3,8}, J.I. Cirac^{1,2}, M. Dalmonte^{9,10}, L. Fallani^{5,6,7}, K. Jansen¹¹, M. Lewenstein^{8,12,13}, S. Montangero^{7,14} ^a, C.A. Muschik³, B. Reznik¹⁵, E. Rico^{16,17} ^b, L. Tagliacozzo¹⁸, K. Van Acoleyen¹⁹, F. Verstraete^{19,20}, U.-J. Wiese²¹, M. Wingate²², J. Zakrzewski^{23,24}, and P. Zoller³

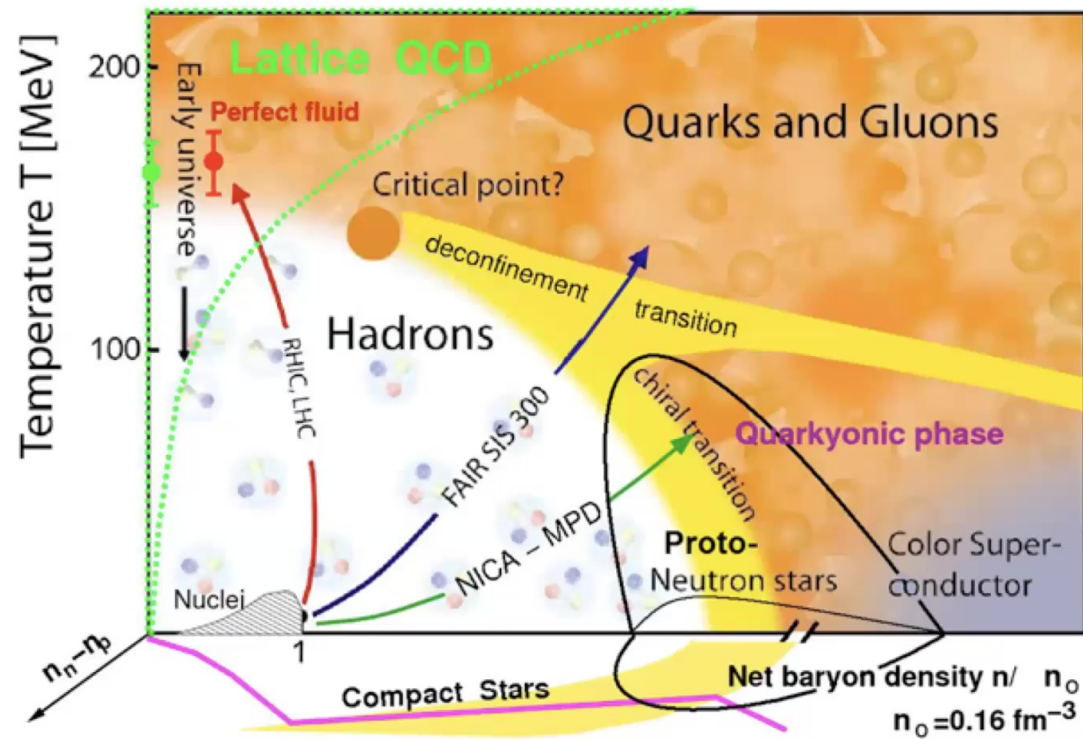


<https://qt.eu/qtflag/>

EPJD (2020)



LATTICE GAUGE THEORIES



The current wisdom on the phase diagram of nuclear matter.

McLerran, L. Nucl.Phys.Proc.Suppl. 195 (2009) 275-280



LATTICE GAUGE TENSOR NETWORKS

Local degrees of freedom

$$[\psi_x^a, U_{x, x+\mu_x}^{ab}]$$

Matter field

Gauge field

Gauge symmetry generator
(Gauss' law)

$$G_x |\varphi_{phys}\rangle = 0$$

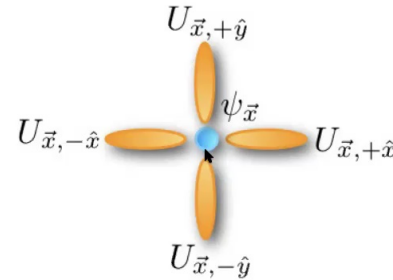
Gauge invariant dynamics

$$H = J \sum_x (\psi_x^\dagger U_{x, x+1} \psi_{x+1} + \text{h.c.})$$

abelian

$$H = t \sum_{x, a, b} [\psi_x^{a\dagger} U_{x, x+1}^{ab} \psi_{x+1}^b + \text{h.c.}]$$

non abelian



Kogut-Susskind

Hamiltonian formulation of LGT

Dynamics commutes with symmetry generator

$$[H_{\text{int}}^{[\text{QED}]}, G_x] = 0 \quad \forall x$$



QUANTUM LINK AND RISHON REPRESENTATION



Link operator

$$U_{x,y} \equiv S_{x,y}^+ = c_y^\dagger c_x$$

Electric field
[U(1) generator]

$$E_{x,y} \equiv S_{x,y}^{(3)} = \frac{1}{2} [c_y^\dagger c_y - c_x^\dagger c_x]$$

$$\{c_x, c_y^\dagger\} = \delta_{x,y} \quad \text{Schwinger fermions (rishons)}$$

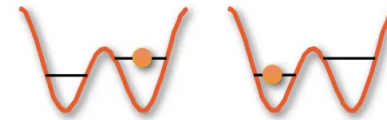
$$[c_x, c_y^\dagger] = \delta_{x,y} \quad \text{Schwinger bosons}$$

Spin representation:

$$N_{x,y} = c_y^\dagger c_y + c_x^\dagger c_x \quad \left[\vec{S}_{x,y} \right]^2 \equiv \frac{N_{x,y}}{2} \left[\frac{N_{x,y}}{2} + 1 \right]$$

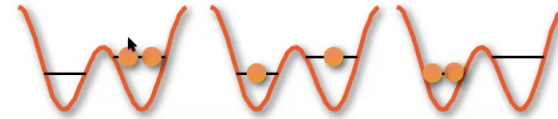
Spin-1/2:

$$E=1/2 \quad \rightarrow \quad E=-1/2 \quad \leftarrow$$



Spin-1:

$$E=+1 \quad \rightarrow\rightarrow \quad E=0 \quad \text{---} \quad E=-1 \quad \leftarrow\leftarrow$$



QUANTUM LINK AND RISHON REPRESENTATION



Link operator

$$U_{x,y} \equiv S_{x,y}^+ = c_y^\dagger c_x$$

Electric field
[U(1) generator]

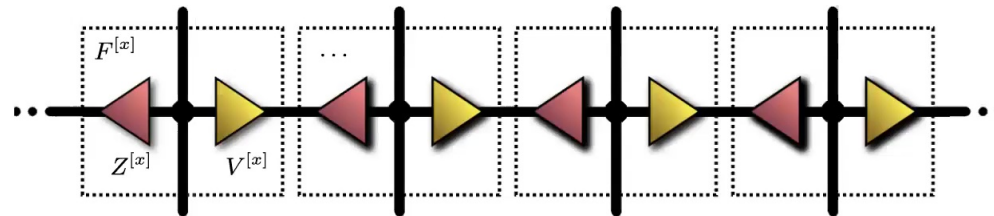
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$$\{c_x, c_y^\dagger\} = \delta_{x,y} \quad \text{Schwinger fermions (rishons)}$$

$$[c_x, c_y^\dagger] = \delta_{x,y} \quad \text{Schwinger bosons}$$

Spin representation:

$$N_{x,y} = c_y^\dagger c_y + c_x^\dagger c_x \quad \left[\vec{S}_{x,y} \right]^2 \equiv \frac{N_{x,y}}{2} \left[\frac{N_{x,y}}{2} + 1 \right]$$



Local projection on a gauge
invariant base

+

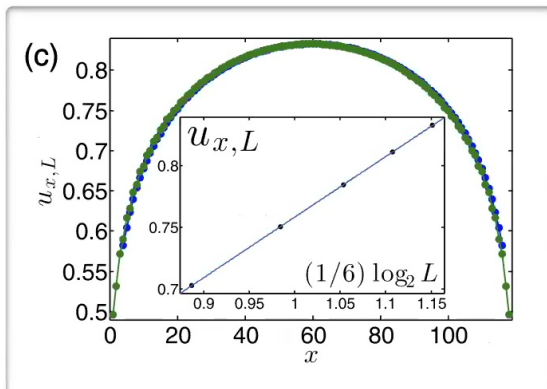
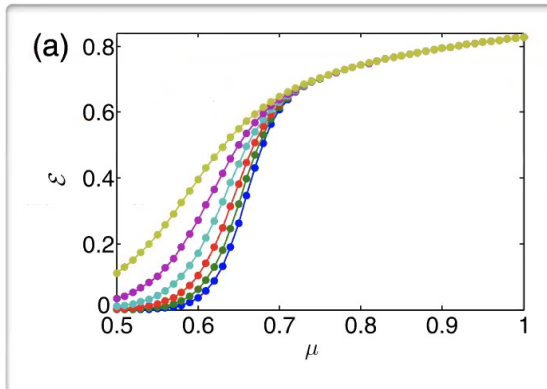
Projection on rishon number

=

Matrix product operator



U(1) LATTICE GAUGE THEORY IN 1+1D

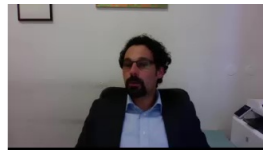


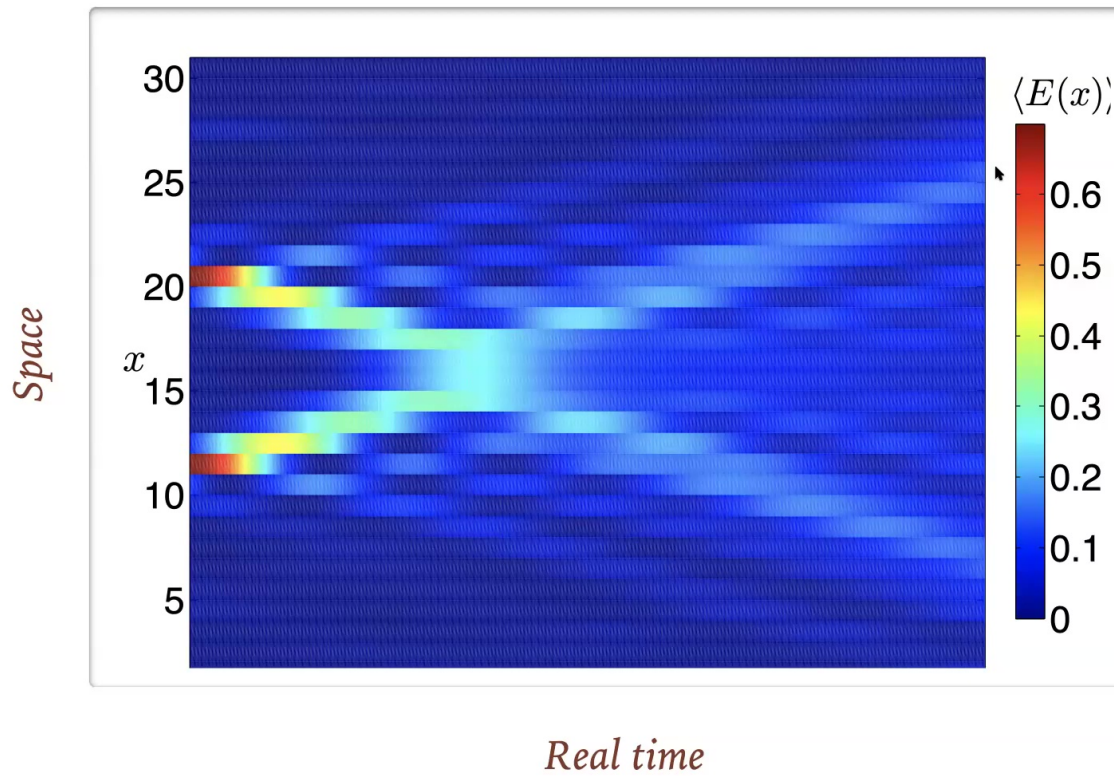
$$H = -t \sum_x \left[\psi_x^\dagger U_{x,x+1}^\dagger \psi_{x+1} + \psi_{x+1}^\dagger U_{x,x+1} \psi_x \right] + m \sum_x (-1)^x \psi_x^\dagger \psi_x + \frac{g^2}{2} \sum_x E_{x,x+1}^2.$$

$$\mathcal{E} = \sum_x \langle E_{x,x+1} \rangle / L$$

- Quantum link representation
- Staggered fermions
- Ising universality class
- Central charge $c = 0.49 \pm 0.01$
- Confirmed by higher-link representation

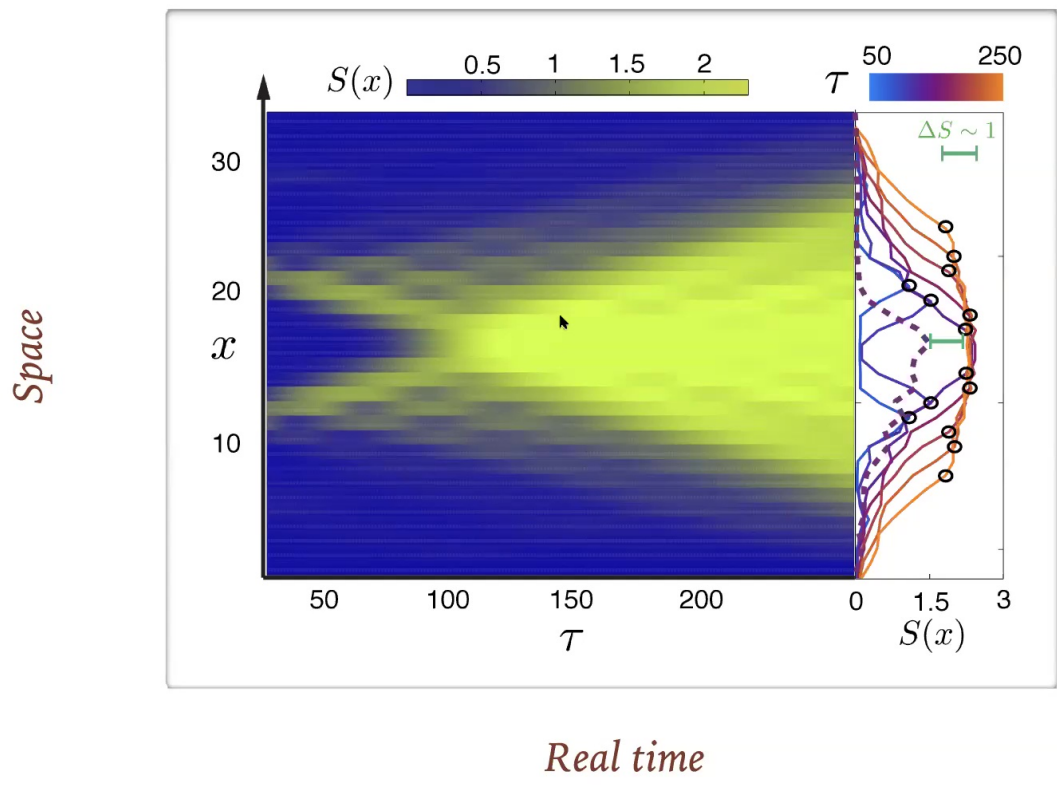
E. Rico, T. Pichler, M. Dalmonte, P. Zoller, and SM, PRL (2014)





MESONS SCATTERING

T. Pichler, E. Rico, M. Dalmonte, P. Zoller, and SM, PRX (2016)

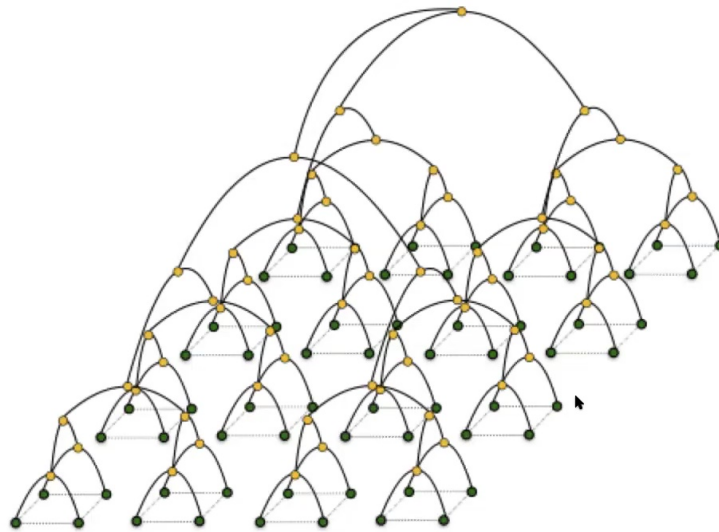
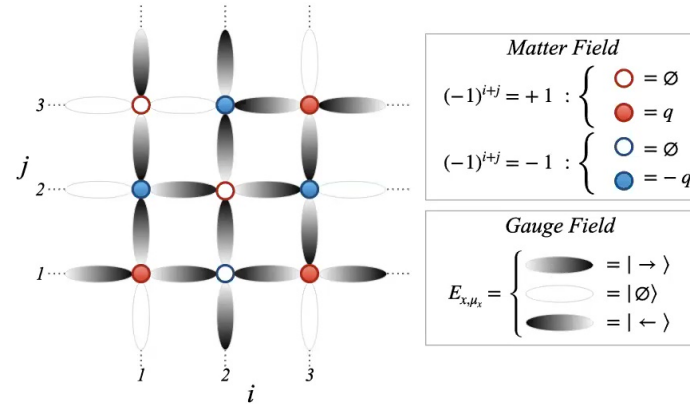


MESONS SCATTERING

T. Pichler, E. Rico, M. Dalmonte, P. Zoller, and SM, PRX (2016)

TWO DIMENSIONAL SIMULATION OF A LGT AT FINITE DENSITY

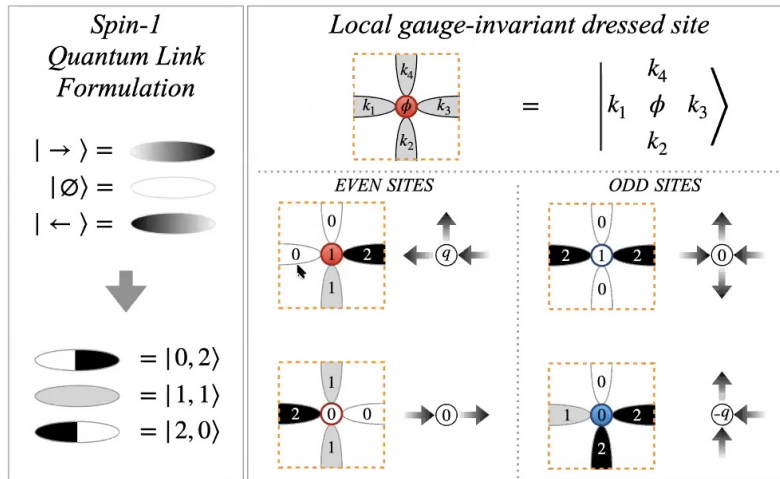
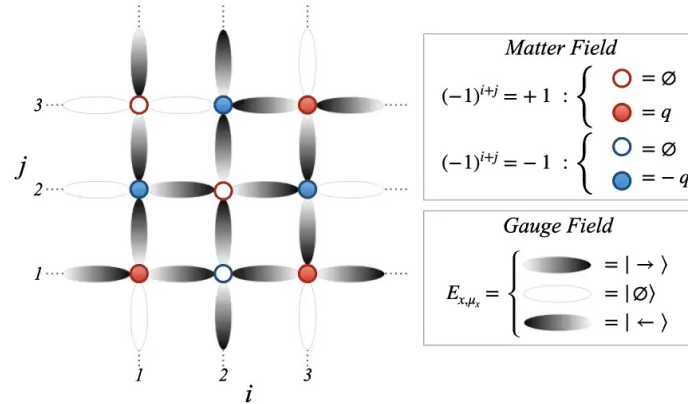
$$\begin{aligned}
 H = & -t \sum_{x,\mu} \left(\psi_x^\dagger U_{x,\mu} \psi_{x+\mu} + h.c. \right) \\
 & + m \sum_x (-1)^x \psi_x^\dagger U_{x,\mu} \psi_x + \frac{g_e^2}{2} \sum_{x,\mu} E_{x,\mu}^2 \\
 & - \frac{g_m^2}{2} \sum_x \left(U_{x,\mu_x} U_{x+\mu_x,\mu_y} U_{x+\mu_y,\mu_x}^\dagger U_{x,\mu_y}^\dagger + h.c. \right)
 \end{aligned}$$



T. Felser, P. Silvi, M. Collura, S. Montangero.
 arXiv:1911.09693
 PRX in press

TWO DIMENSIONAL SIMULATION OF A LGT AT FINITE DENSITY

$$\begin{aligned}
 H = & -t \sum_{x,\mu} \left(\psi_x^\dagger U_{x,\mu} \psi_{x+\mu} + h.c. \right) \\
 & + m \sum_x (-1)^x \psi_x^\dagger U_{x,\mu} \psi_x + \frac{g_e^2}{2} \sum_{x,\mu} E_{x,\mu}^2 \\
 & - \frac{g_m^2}{2} \sum_x \left(U_{x,\mu_x} U_{x+\mu_x,\mu_y} U_{x+\mu_y,\mu_x}^\dagger U_{x,\mu_y}^\dagger + h.c. \right)
 \end{aligned}$$



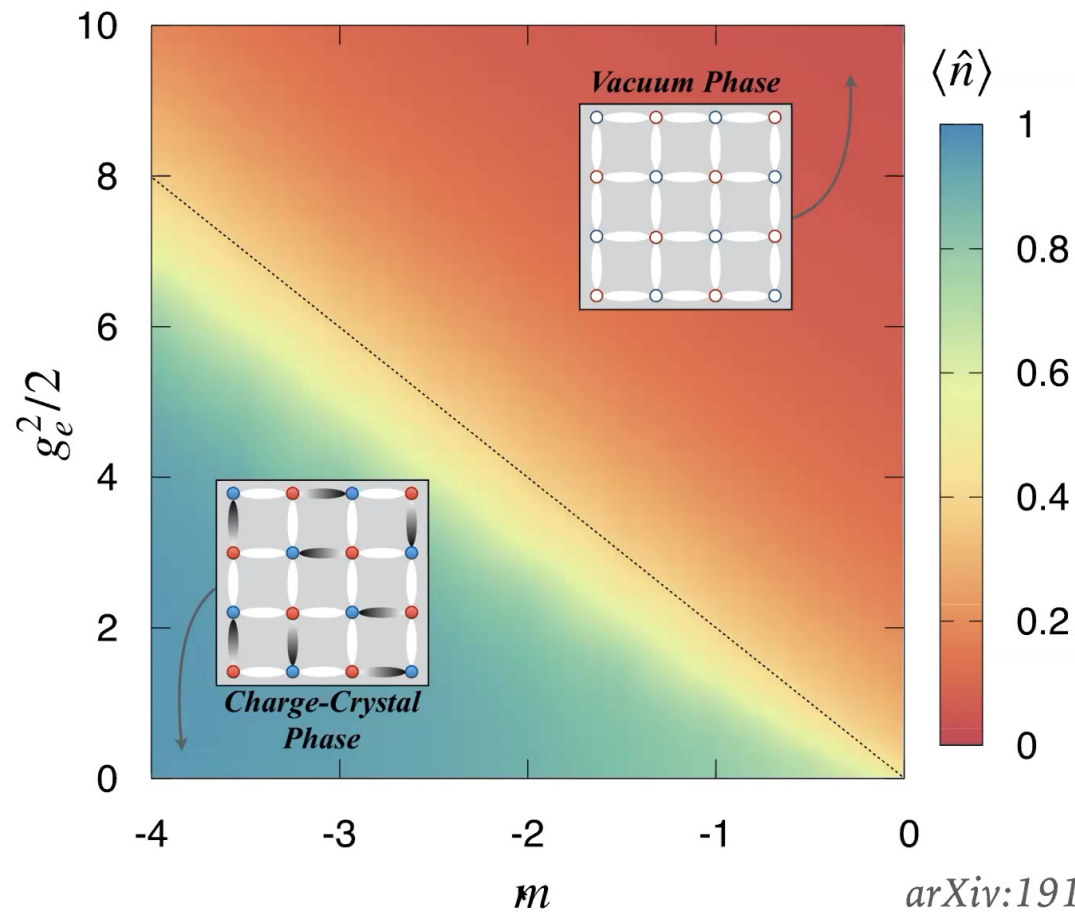
T. Felser, P. Silvi, M. Collura, S. Montangero.
 arXiv:1911.09693
 PRX in press

*Even number of fermions =
 No Jordan-Wigner strings!*

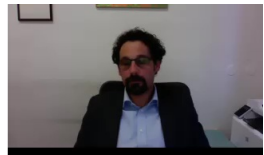
PHASE DIAGRAM

16x16 lattice sites

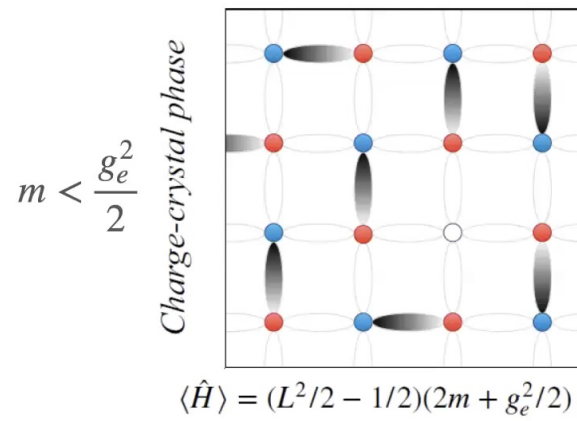
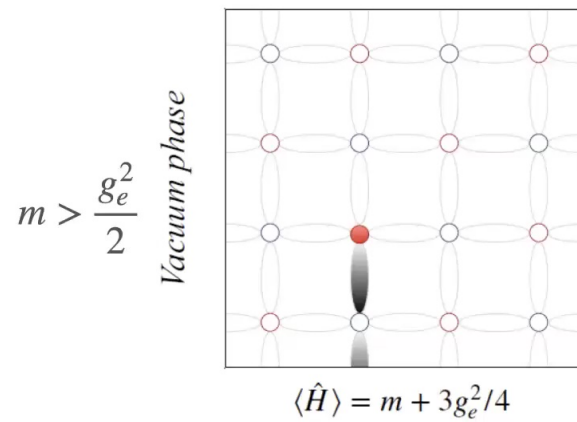
Hilbert space of $\sim 80 \times 80$ qubits



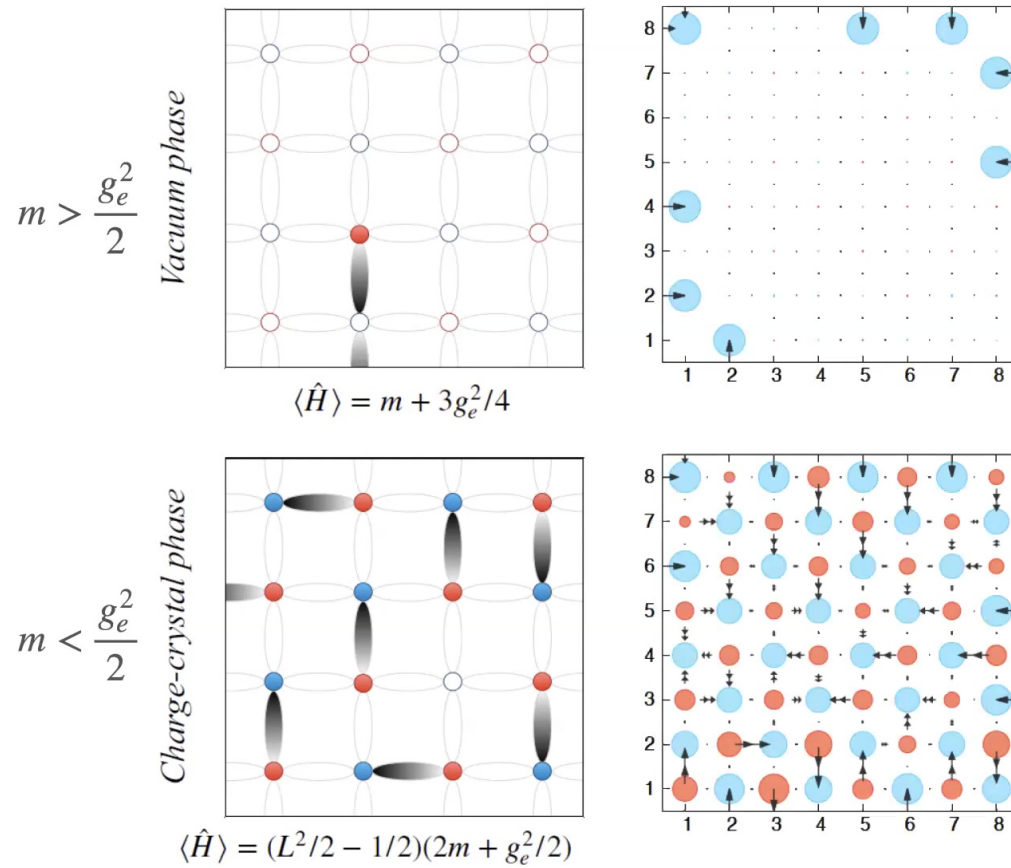
arXiv:1911.09693



FINITE DENSITY



FINITE DENSITY

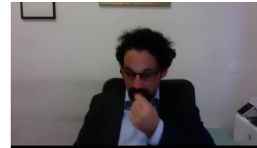
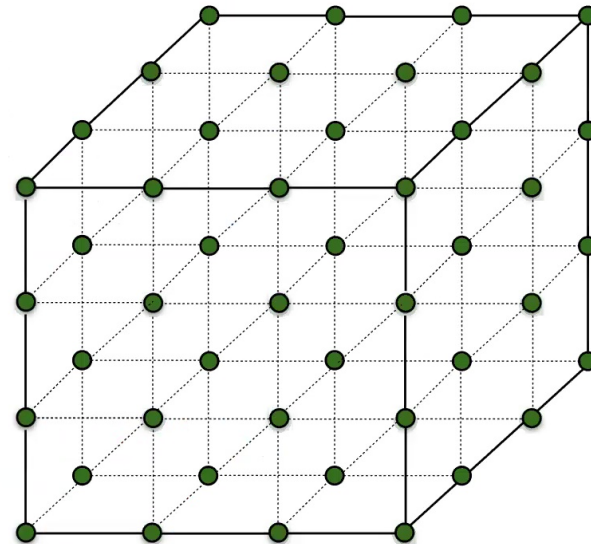


$$Q = -8$$

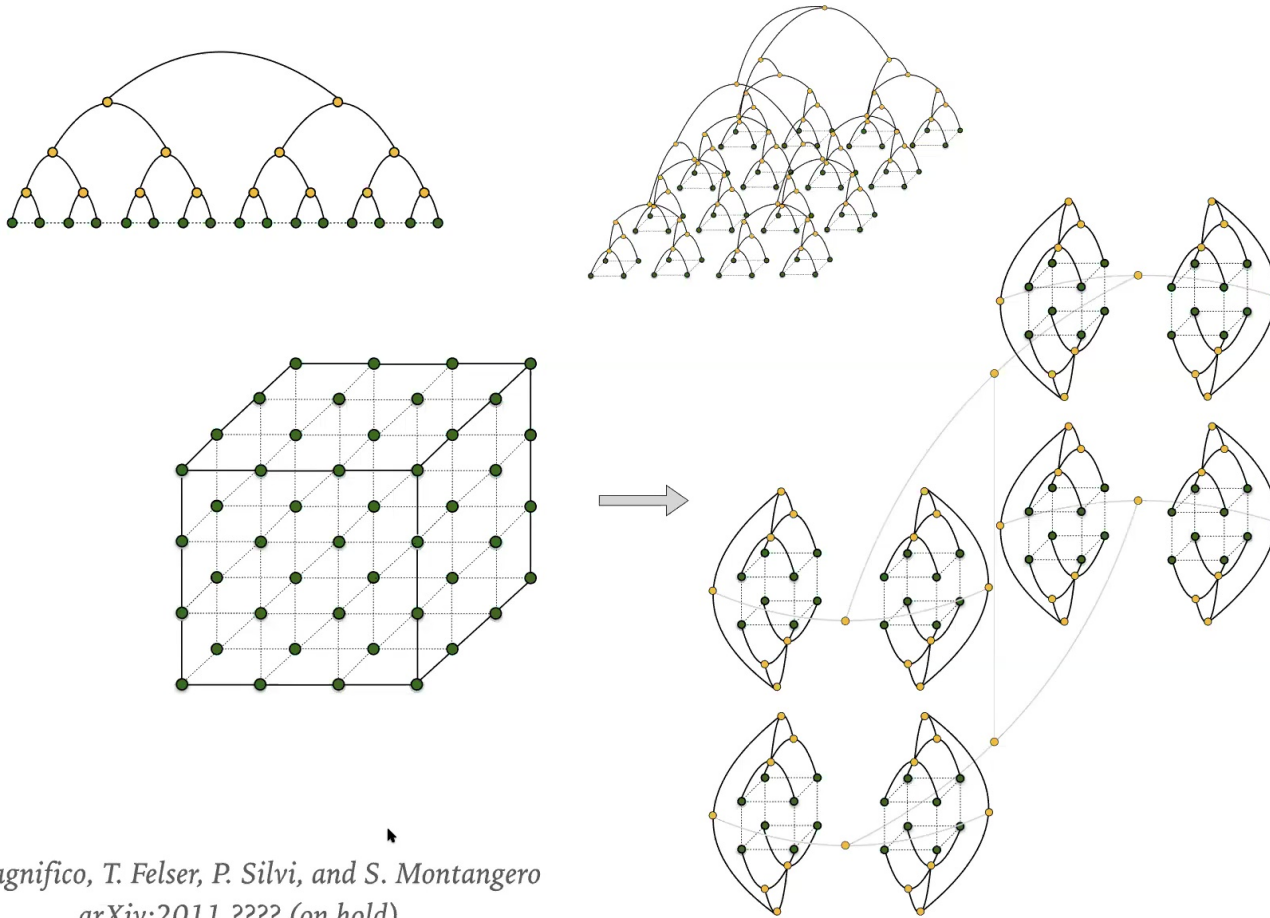


3D LATTICE GAUGE THEORIES

With tree tensor networks



3D TREE TENSOR NETWORK

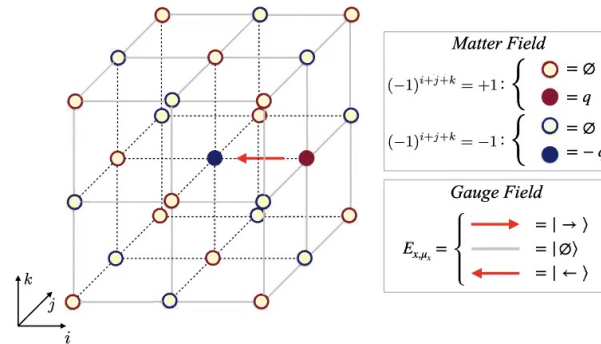


*G. Magnifico, T. Felser, P. Silvi, and S. Montangero
arXiv:2011.???? (on hold)*

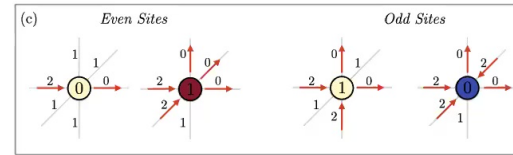


3D QUANTUM-LINK FORMULATION OF QED

$$\hat{H} = -t \sum_{x,\mu} \left(\hat{\psi}_x^\dagger \hat{U}_{x,\mu} \hat{\psi}_{x+\mu} + \text{H.c.} \right) + m \sum_x (-1)^x \hat{\psi}_x^\dagger \hat{\psi}_x + \frac{g_e^2}{2} \sum_{x,\mu} \hat{E}_{x,\mu}^2 - \frac{g_m^2}{2} \sum_x \left(\square_{\mu_x, \mu_y} + \square_{\mu_x, \mu_z} + \square_{\mu_y, \mu_z} + \text{H.c.} \right)$$

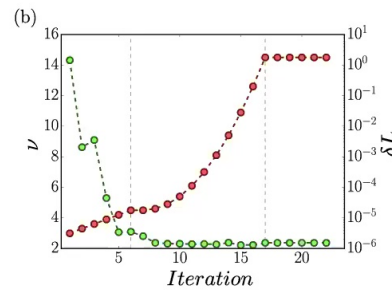
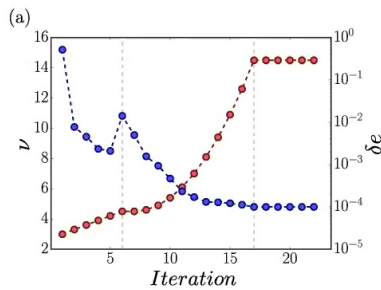


$$\hat{G}_x = \hat{\psi}_x^\dagger \hat{\psi}_x - \frac{1 - (-1)^x}{2} - \sum_{\mu} \hat{E}_{x,\mu}$$

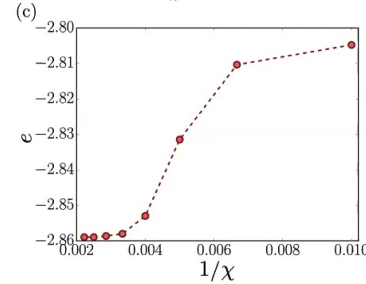


Local dimension 267, up to 12288 Hamiltonian operators

Up to 5 weeks x 64 cores of computational time

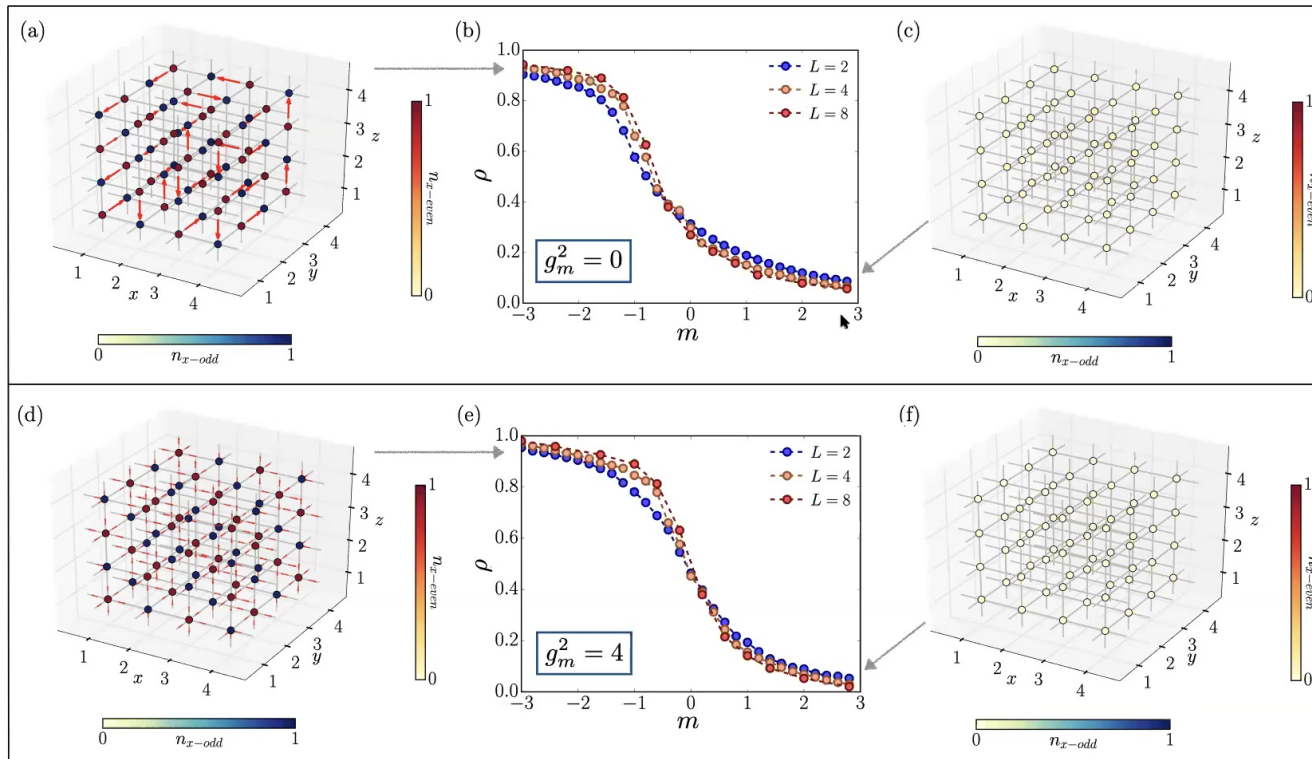


$$H_{pen} = \nu \sum_{x,\mu} \left(1 - \delta_{2, \hat{L}_{x,\mu}} \right)$$



QUANTUM PHASES

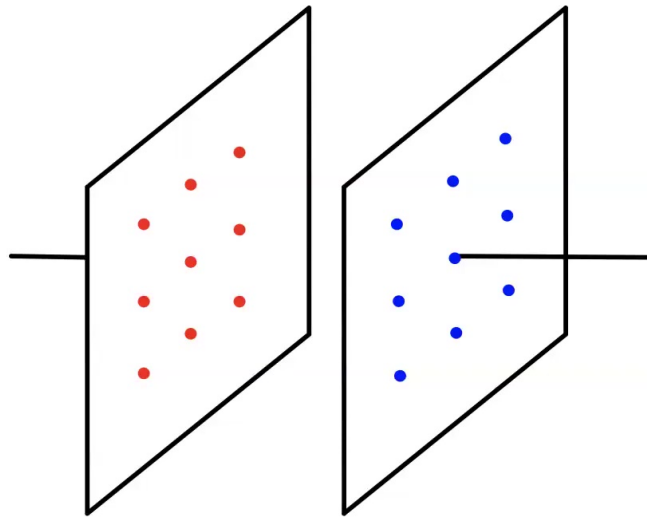
Hilbert space of
~64x64x64 qubits!



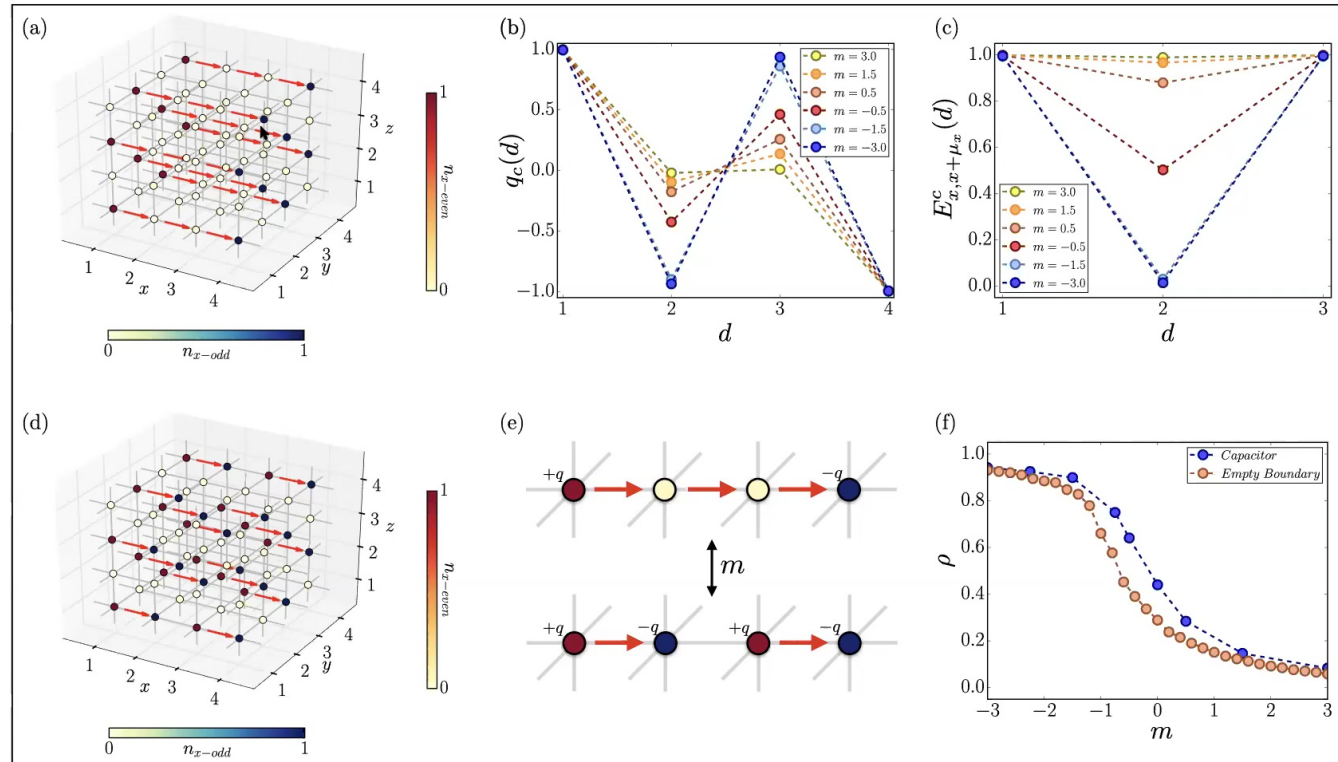
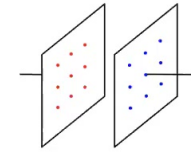
$$m_c \approx +0.22$$

$$g_m^2 = 8/g_e^2$$

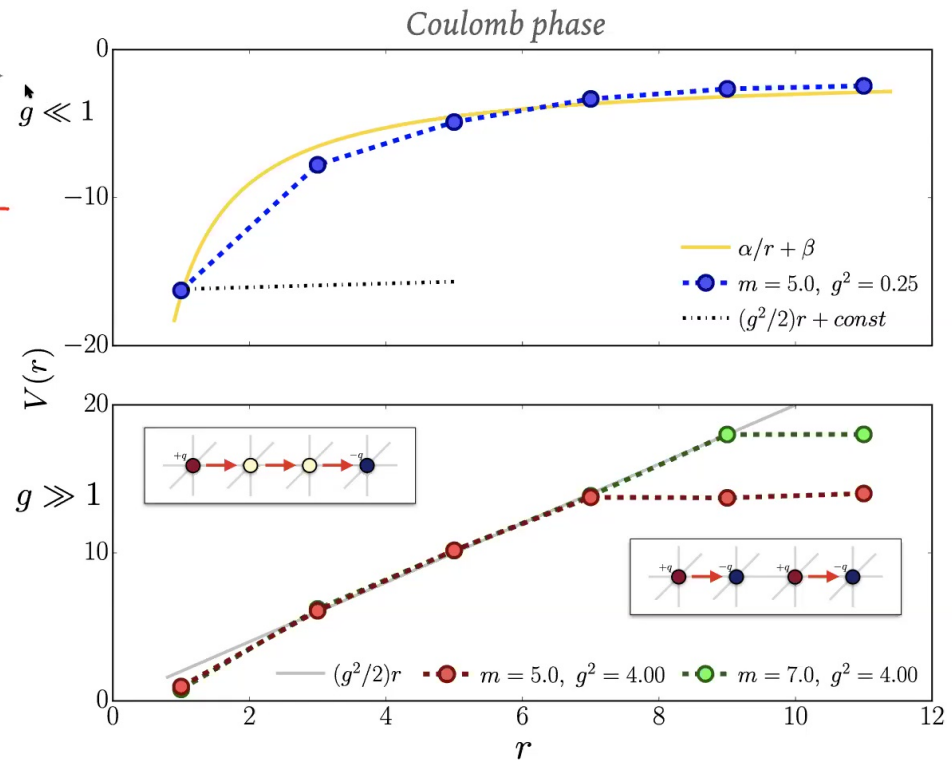
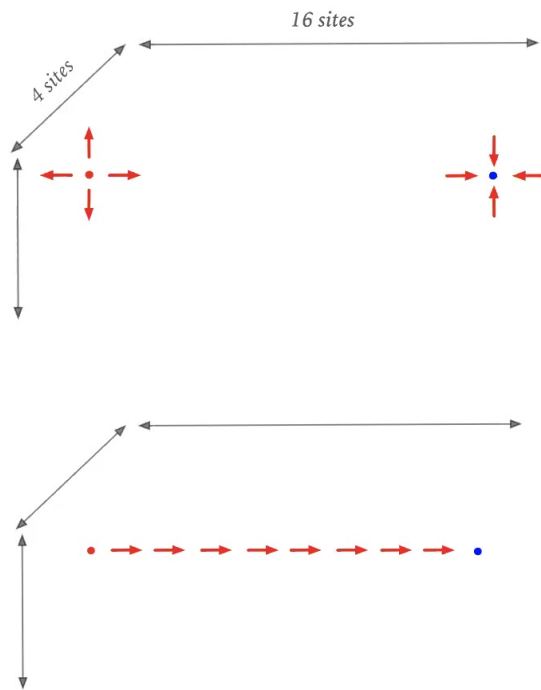
SCREENING



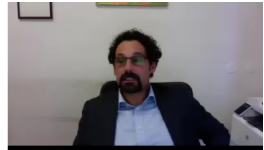
SCREENING



CONFINEMENT



$$g_e^2 = g^2/a, g_m^2 = 8/(g^2a)$$



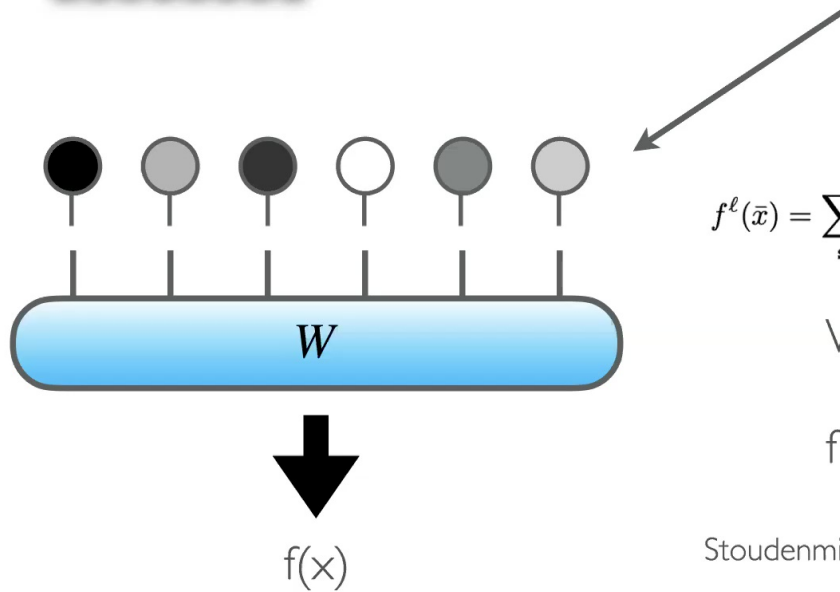
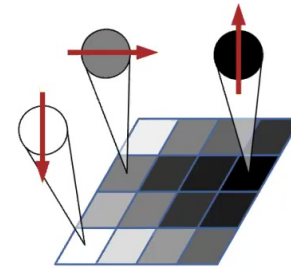
MACHINE LEARNING WITH TENSOR NETWORKS

Raw data

0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2
3	3	3	3	3	3	3	3
4	4	4	4	4	4	4	4
5	5	5	5	5	5	5	5
6	6	6	6	6	6	6	6
7	7	7	7	7	7	7	7
8	8	8	8	8	8	8	8
9	9	9	9	9	9	9	9

Map to "Spins"

$$\Phi(x_j) = \left[\cos\left(\frac{\pi}{2}x_j\right), \sin\left(\frac{\pi}{2}x_j\right) \right]$$

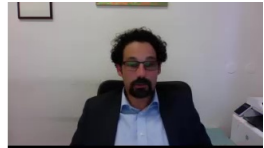


$$f^\ell(\vec{x}) = \sum_{\mathbf{s}} W_{s_1 s_2 \dots s_N}^\ell \phi(x_1)^{s_1} \phi(x_2)^{s_2} \dots \phi(x_N)^{s_N}$$

W : weight tensor

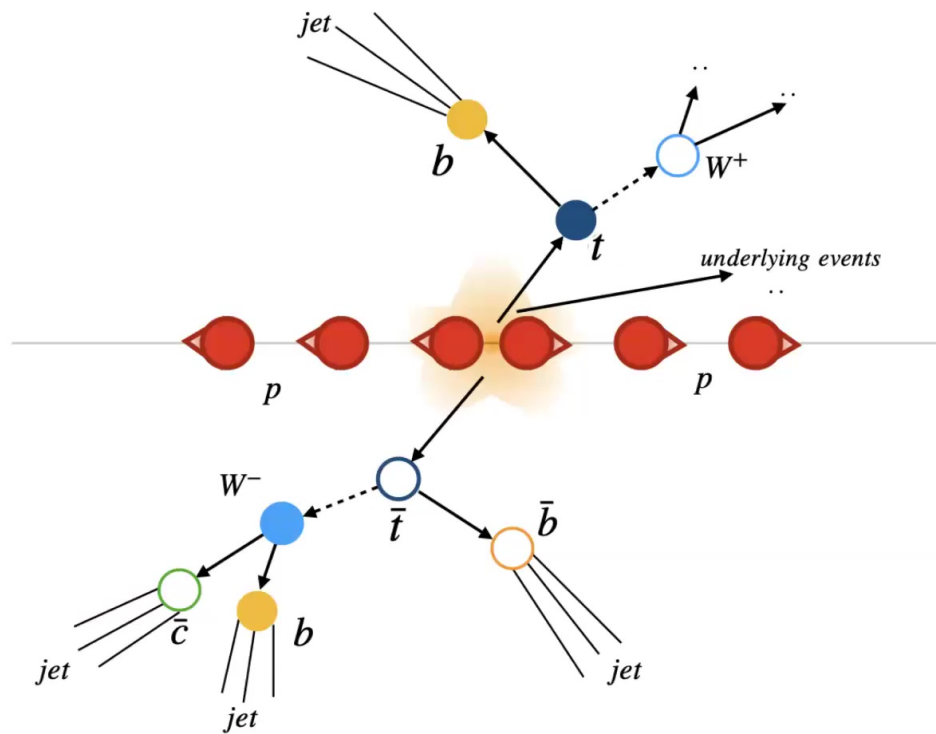
$f(x)$: decision function

Stoudenmire, Advances in Neural IPS 29, 4799 (2016),
arXiv:1605.05775 [stat.ML]



P-P SCATTERING

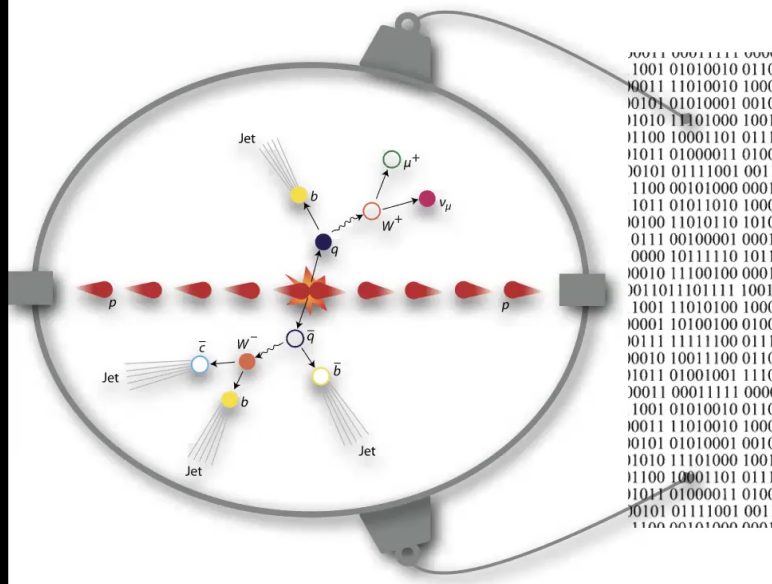
Typical event in LHC



Quarks

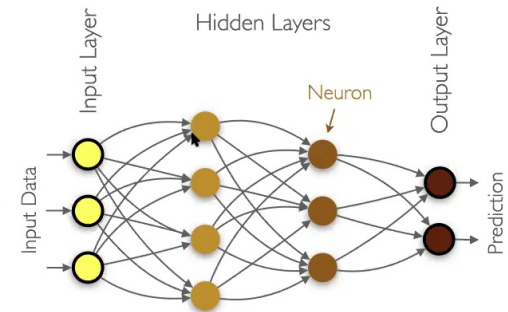
$q \left\{ \begin{array}{l} u \\ d \\ s \\ c \\ b \\ t \end{array} \right.$

MACHINE LEARNING BASED CLASSIFICATION

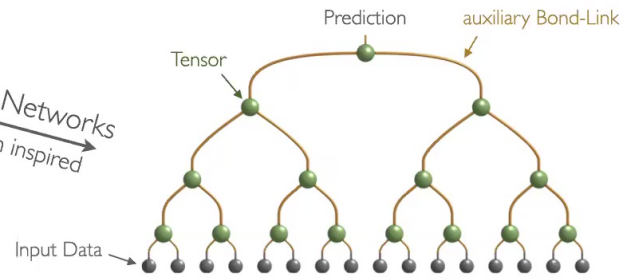


1001 01010010 0110
1001 11010010 1000
1010 01010001 0010
1101 11010000 1001
1100 10001101 0111
1101 01000011 0100
1010 01111001 0011
1100 00101000 0001
1011 01011010 1000
1010 11010110 1010
0111 00100001 0001
0000 10111110 1011
10010 11100100 0001
1011011101111 10011
1001 11010100 1000
10001 10100100 0100
10111 11111100 0111
10010 10011100 0110
11011 01001001 1110
10011 00011111 0000
1001 01010010 0110
10011 11010010 1000
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11010 11101000 1001
1100 10001101 0111
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1100 00101000 0001

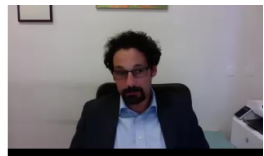
Neural Network
biologic inspired



Tensor Networks
quantum inspired

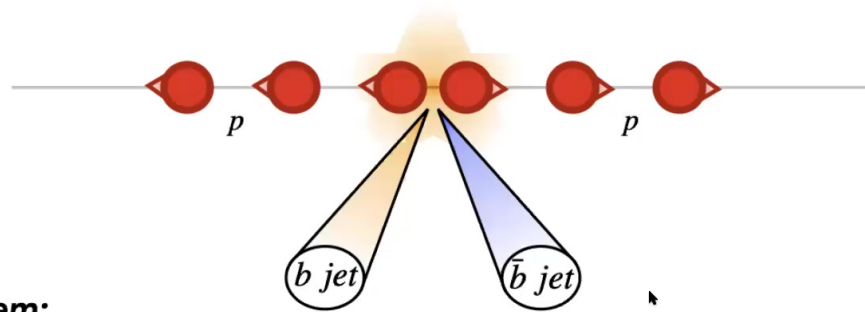


In collaboration with A. Gianelle, D. Lucchesi, L. Sestini, D. Zuliani
arXiv: 2004.13747



BINARY B BBAR CLASSIFICATION

This kind of events are used to measure **asymmetries** between the charge of b and \bar{b} .

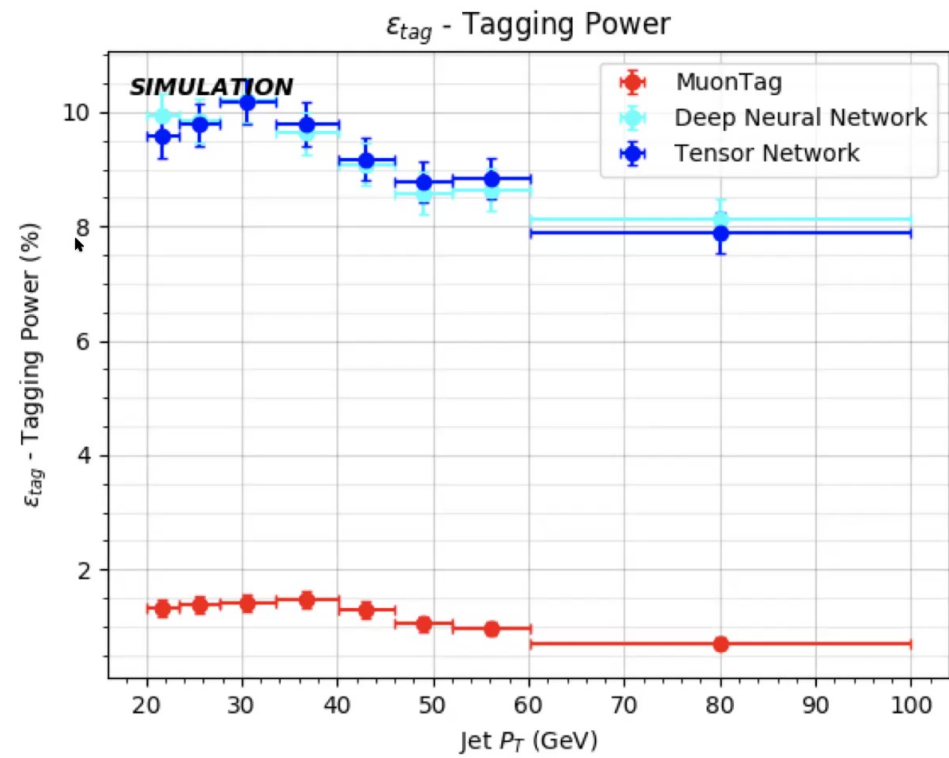


Easier problem:

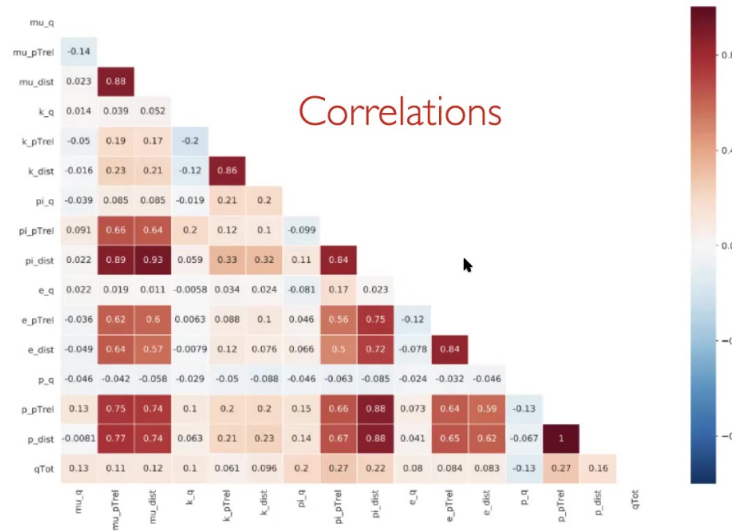
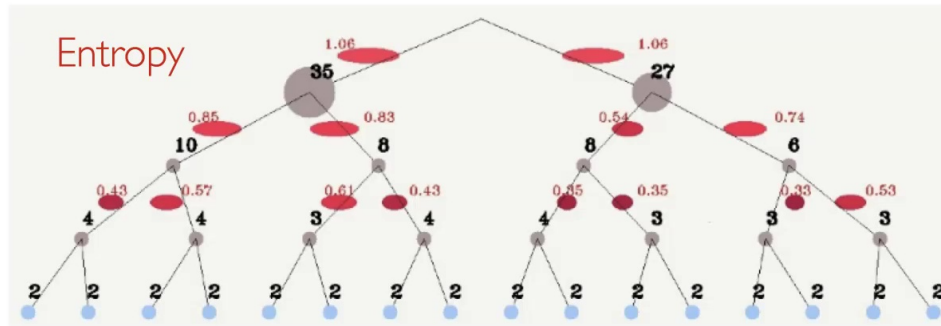
- 16 selected features (most physically relevant)
- $\sim 10^6$ data samples



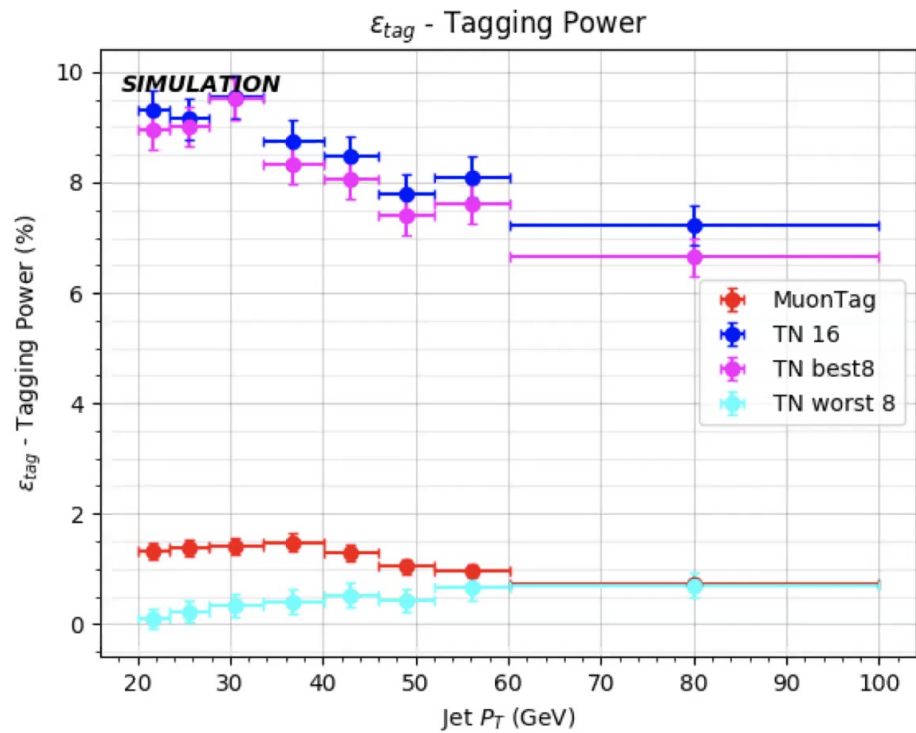
LHCB DATA ANALYSIS



CORRELATIONS



FINAL RESULT

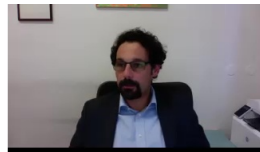


- 4.7 times faster
- Only 0.4% less precise



TAKE HOME MESSAGES

- Tensor network algorithms can be used to benchmark, verify, support and guide quantum simulations/computations
- High-dimensional tensor network simulations are becoming available (PEPS, aTTN,...)
- Entanglement of mixed many-body states can be quantified
- Scalability to HPC is necessary to produce relevant results
- Interaction with HEP is becoming more and more relevant
- Interesting developments also in other directions (classical optimisers/annealers)
- Tensor network machine learning is competitive with DNN





Thank you for your attention!

Simone Montangero
Giuseppe Magnifico
Simone Notarnicola
Luca Arceci
Ferdinand Tschirsich
Timo Felser
Matthias Gerster
Phila Rembold
Marco Rossignolo
Marco Trenti
Marco Rigobello
Samuele Cavinato



quantum.dfa.unipd.it



ECT* Ph.D. School
Trento Summer 2021
<https://indico.ectstar.eu/event/72/>

