

Title: Bayesian Evidence for Echoes

Speakers: Jahed Abedi

Collection: Echoes in Southern Ontario

Date: February 25, 2020 - 9:45 AM

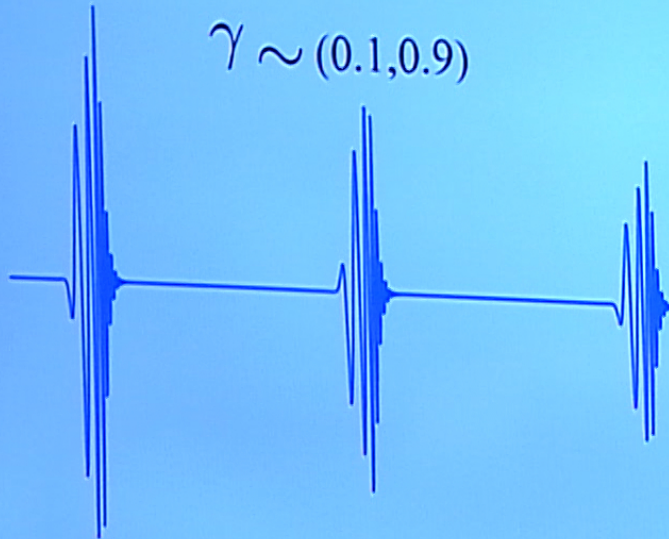
URL: <http://pirsa.org/20020097>

$$t_{0,GW150914} \sim (-0.03s, 0)$$

$$t_{0,GW151226} \sim \frac{\Delta t_{pred,GW151226}}{\Delta t_{pred,GW150914}} \times t_{0,GW150914} = (-0.0104s, 0)$$

$$t_{0,LVT151012} \sim \frac{\Delta t_{pred,LVT151012}}{\Delta t_{pred,GW150914}} \times t_{0,GW150914} = (-0.0182s, 0)$$

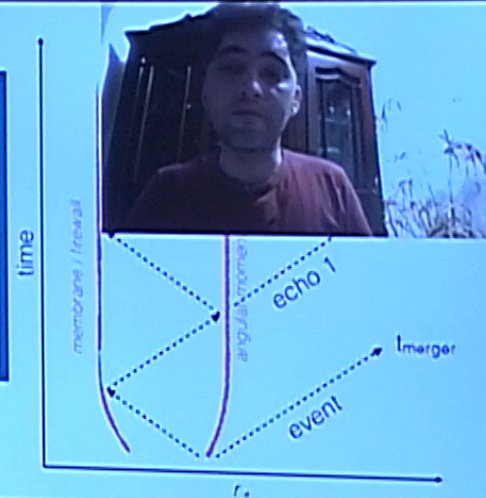
$$\gamma \sim (0.1, 0.9)$$



$$\mathcal{M}_{T,I}(t, t_0) \equiv \Theta_I(t, t_0) \mathcal{M}_I(t).$$

$$\mathcal{M}_{TE,I}(t) \equiv$$

$$A \sum_{n=0}^{\infty} (-1)^{n+1} \gamma^n \mathcal{M}_{T,I}(t + t_{\text{merger}} - t_{\text{echo}} - n \Delta t_{\text{echo}}, t_0)$$





$$SNR_{Total}$$

$$= (SNR_{GW150914}(t_{echoes}/\Delta t_{echoes,GW150914})^2 \\ + SNR_{GW151226}(t_{echoes}/\Delta t_{echoes,GW151226})^2 \\ + SNR_{LVT151012}(t_{echoes}/\Delta t_{echoes,LVT151012})^2)^{\frac{1}{2}}$$



Number of free  
parameters:

$$\gamma \sim (0.1, 0.9)$$

$$\Delta t_{echo,I}(\text{sec}) = \begin{cases} 0.2925 \pm 0.00916 & I = \text{GW150914} \\ 0.1013 \pm 0.01152 & I = \text{GW151226} \\ 0.1778 \pm 0.02789 & I = \text{LVT151012} \end{cases}$$

$$t_{0,GW150914} \sim (-0.03\text{s}, 0)$$

$$t_{0,GW151226} \sim \frac{\Delta t_{pred,GW151226}}{\Delta t_{pred,GW150914}} \times t_{0,GW150914}$$

$$t_{0,LVT151012} \sim \frac{\Delta t_{pred,LVT151012}}{\Delta t_{pred,GW150914}} \times t_{0,GW150914}$$

$$x = \frac{t_{echo} - t_{merger}}{\Delta t_{echo}} \quad -0.01 < \Delta x < 0.01$$

$A$  is the over-all amplitude of the echo template  
(with respect to the main event) which we fit for,  
assuming a flat prior.



- Have a good physical model! (or you won't find them)
- and a simple template (avoid too many arbitrary choices)
- Avoid a posteriori statistics (don't look at data to make your template)





So far seven independent groups looked  
echoes in GW data



Positive results

*Abedi, et al. 2017-18; Conklin, et al. 2018, Uchikata, et al. 2019*

Negative results

*Lo, et al. 2019; Tsnag, et al. 2019; Uchikata, et al. 2019*

Mixed results

*Westerweck, et al. 2018; Nielsen, et al. 2019 ; Salemi, et al. 2019*



# Bayes' theorem:

From the **product rule** of probability it can be shown that

$$P(A \text{ and } B) \equiv P(A, B) = P(A) P(B|A) = P(B) P(A|B)$$

$P(x|y)$  means “the probability that x is true given y is true”

this gives:

$$P(B|A, I) = \frac{P(A|B, I)P(B|I)}{P(A|I)}$$

This is **Bayes' theorem**.



# Bayes' theorem:



Bayes theorem can be cast in terms of a **model, or hypothesis**, and some **observations, or data**.

It tells us how to update our degree of belief about our model based on new data.

$$\underbrace{P(\text{model}|\text{data})}_{\text{Posterior}} = \frac{\overbrace{P(\text{data}|\text{model})}^{\text{Likelihood}} \overbrace{P(\text{model})}^{\text{Prior}}}{P(\text{data})}$$

**Prior:** what we knew, or our degree of belief, about our model before taking data

**Likelihood:** the influence of the data in updating our degree of belief

**Posterior:** our new degree of belief about our model in light of the data

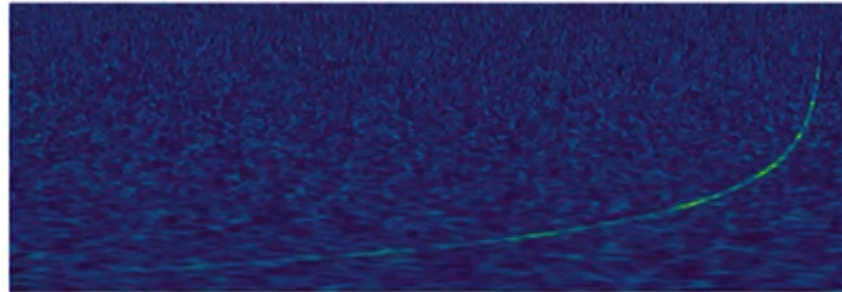


# PyCBC

Free and open software to study gravitational waves.



<https://pycbc.org>



PyCBC is a software package used to explore astrophysical sources of gravitational waves. It contains algorithms that can detect coalescing compact binaries and measure the astrophysical parameters of detected sources. PyCBC was used in the [first direct detection of gravitational waves by LIGO](#) and is used in the ongoing analysis of LIGO and Virgo data. PyCBC was featured in [Physics World](#) as a good example of a large collaboration publishing its research products, including its software.

## Getting Started

You can start using the PyCBC library now in an interactive notebook! [See our tutorials](#)

<https://arxiv.org/pdf/1807.10312.pdf>

[https://github.com/cdcapano/pycbc/tree/echoes\\_update](https://github.com/cdcapano/pycbc/tree/echoes_update)

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Installing PyCBC

- pycbc\_make\_psd\_estimation\_workflow: A workflow generator for noise estimation
- pycbc\_make\_coinc\_search\_workflow: A workflow to search for gravitational waves
- pycbc\_make\_offline\_grb\_workflow: A GRB triggered CBC analysis workflow generator
- PyCBC inference documentation (pycbc.inference)
- PyCBC template bank generation documentation (pycbc.tmbank)
- Hardware injection waveform generation
- Calculating the Effectualness (Fitting Factor) of Template Banks
- Dag Generator for Doing Faithfulness Comparisons
- Uploading triggers to gracedb
- Catalog of Observed Gravitational-wave Mergers
- Query times of valid data, hardware injections, and more.
- Reading Gravitational-wave Frames
- Signal Processing with GW150914
- Gravitational-wave Detectors
- Handling PSDs
- Generating Noise

Docs » PyCBC [View page source](#)

## PyCBC

PyCBC is a software package used to explore astrophysical sources of gravitational waves. It contains algorithms that can detect coalescing compact binaries and measure the astrophysical parameters of detected sources. PyCBC was used in the [first direct detection of gravitational waves \(GW150914\)](#) by LIGO and is used in the ongoing analysis of LIGO and Virgo data. If you use PyCBC in your scientific publications or projects, we ask that you acknowledge our work by citing the papers described on the page:

- [Use of PyCBC in Scientific Publications](#)


## Getting Started

- Get the full PyCBC software suite with one of our Docker Images

If you have [Docker](#) installed, you can get started using PyCBC with just two commands:

```
pycbc — bash — 80x25

$ docker pull pycbc/pycbc-e17:latest
$ docker run -it pycbc/pycbc-e17:latest
(pycbc-software)[pycbc@37184573e664 ~]$ python
Python 2.7.5 (default, Nov 6 2016, 00:28:07)
[GCC 4.8.5 20150623 (Red Hat 4.8.5-11)]
```





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Use of PyCBC in Scientific Publications

Running PyCBC under Docker

Installing PyCBC

pycbc\_make\_psd\_estimation\_workflow: A workflow generator for noise estimation

pycbc\_make\_coinc\_search\_workflow: A workflow to search for gravitational waves

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PyCBC inference documentation (pycbc.inference)

Introduction

Sampling the parameter space (pycbc\_inference)

Examples

Running on an analytic distribution

Simulated BBH example

1. Create the injection
2. Setup the configuration files
3. Run

GW150914 example

Using the single template model

Visualizing the Posteriors

Workflows

easy to read, we will split the data, sampler, and prior settings into their own configuration files

Here are the model and prior settings we will use:


```
[model]
name = gaussian_noise
low-frequency-cutoff = 20.0

[variable_params]
; waveform parameters that will vary in MCMC
delta_tc =
mass1 =
mass2 =
spin1_a =
spin1_azimuthal =
spin1_polar =
spin2_a =
spin2_azimuthal =
spin2_polar =
distance =
coa_phase =
inclination =
polarization =
ra =
dec =

[static_params]
; waveform parameters that will not change in MCMC
approximant = IMRPhenomPv2
f_lower = 20
f_ref = 20
; we'll set the tc by using the trigger time in the data
; section of the config file + delta_tc
trigger_time = ${data|trigger-time}

[prior-delta_tc]
; coalescence time prior
name = uniform
min-delta_tc = -0.1
max-delta_tc = 0.1

[waveform_transforms-tc]
; we need to provide tc to the waveform generator
name = custom
```



Mac OS X dock with various application icons including Finder, Spotlight, Safari, Mail, Messages, Photos, Videos, Music, App Store, and others.





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http:// https://arxiv.or... https://arxiv.or... [1612.00266] E... Echoes in Sout... Inbox (3) - jahe... Launch Meetin... PyCBC 3308fd... Simulated BBH... PyCBC

Hardware injection waveform generation

Calculating the Effectualness (Fitting Factor) of Template Banks

Dag Generator for Doing Faithfulness Comparisons

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Gravitational-wave Detectors

Handling PSDs

Generating Noise

Waveforms

Filtering

Using PyCBC Distributions from PyCBC Inference

Building Bundled Executables

Documenting PyCBC code

Creating Releases of PyCBC

HDF files within the PyCBC workflow

Workflow: the inspiral analysis workflow generator (pycbc.workflow)

pycbc

```

[prior-delta_tc]
; coalescence time prior
name = uniform
min-delta_tc = -0.1
max-delta_tc = 0.1

[waveform_transforms-tc]
; we need to provide tc to the waveform generator
name = custom
inputs = delta_tc
tc = ${data|trigger-time} + delta_tc

[prior-mass1]
name = uniform
min-mass1 = 10.
max-mass1 = 80.

[prior-mass2]
name = uniform
min-mass2 = 10.
max-mass2 = 80.

[prior-spin1_a]
name = uniform
min-spin1_a = 0.0
max-spin1_a = 0.99


[prior-spin1_polar+spin1_azimuthal]
name = uniform_solidangle
polar-angle = spin1_polar
azimuthal-angle = spin1_azimuthal

[prior-spin2_a]
name = uniform
min-spin2_a = 0.0
max-spin2_a = 0.99

[prior-spin2_polar+spin2_azimuthal]
name = uniform_solidangle
polar-angle = spin2_polar
azimuthal-angle = spin2_azimuthal

[prior-distance]
; following gives a uniform volume prior
name = uniform_radius
min-distance = 10

```



Mac OS X dock with various application icons including Finder, Launchpad, Safari, Mail, Calendar, Photos, Music, App Store, Messages, Maps, Reminders, Notes, iMessage, Phone, TV, iTunes, System Preferences, Spotlight, and Trash.



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github.com

https://andv.or... [1612.00268] E... Echoes in Sout... Inbox (3) - jahe... Launch Meetin... PyCBC 3308fd... Simulated BBH... PyCBC

```
--plot-contours \
--plot-marginal \
--z-arg snr
```

In [44]: Image(filename='posterior\_mass1\_mass2.png', width=640, height=480)

Out[44]:

Challenge:

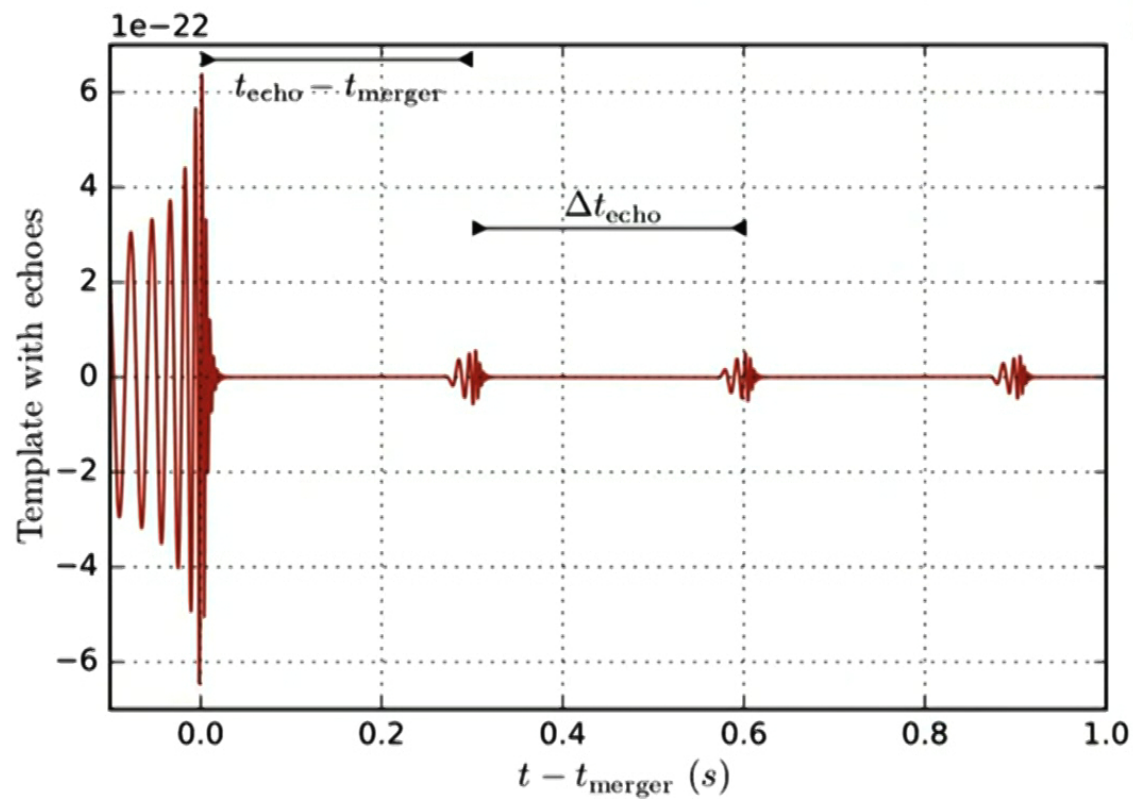
macOS dock icons: Finder, Launchpad, Safari, Spotlight, Calendar (Feb 25), Photos, Mail, Messages, App Store, System Preferences, Docker, PyCharm, VS Code, TeX, JupyterLab, Homebrew, PowerPoint, Slack, Zoom, Trash.



A screenshot of a macOS desktop showing a Safari browser window displaying a JupyterLab interface. The browser's address bar shows 'localhost'. The JupyterLab interface has a menu bar with 'File', 'Edit', 'View', and 'Language'. The main area displays a code editor with a file named 'bbh\_example.ini'. The code is a configuration file for a Bayesian model, likely using BEAST2, defining priors for various parameters. A video call window is visible in the top right corner, showing a man with dark hair and a beard wearing a red shirt. The macOS dock is at the bottom, containing various application icons including Finder, Launchpad, Spotlight, Safari, Mail, Calendar, Photos, Messages, Maps, App Store, System Preferences, and several other utility and development tools.

```
80 ; del_t_echo time prior
81 name = uniform
82 min-del_t_echo = 0.28334
83 max-del_t_echo = 0.30166
84
85 ;[prior-x]
86 ; x=t_echo/del_t_echo prior
87 ;min-x = 0.99
88 ;max-x = 1.01
89
90 [prior-gamma]
91 ; gamma prior
92 name = uniform
93 min-gamma = 0.85
94 max-gamma = 0.95
95
96 [prior-amplitude]
97 ; amplitude prior
98 name = uniform
99 min-amplitude = 0.05
100 max-amplitude = 0.15
101
102
103 ;[prior-tc]
104 ; coalescence time prior
105 ;name = uniform
106 ;min-tc = 1126259462.32
107 ;max-tc = 1126259462.52
108
109 ;[prior-mass1]
110 ;name = uniform
111 ;min-mass1 = 10.
112 ;max-mass1 = 80.
113
114 ;[prior-mass2]
115 ;name = uniform
116 ;min-mass2 = 10.
```

# Parameter estimation of echo



# Parameter estimation and statistical significance of echoes from black hole signals in the first Advanced LIGO observing run

Alex B. Nielsen,<sup>1,2,\*</sup> Collin D. Capano,<sup>1,2,†</sup> Ofek Birnholtz,<sup>3,‡</sup> and Julian W.

<sup>1</sup>*Max-Planck-Institut für Gravitationsphysik, D-30167 Hannover, Germany*

<sup>2</sup>*Leibniz Universität Hannover, D-30167 Hannover, Germany*

<sup>3</sup>*Center for Computational Relativity and Gravitation, Rochester Institute of Technology,  
170 Lomb Memorial Drive, Rochester, New York 14623, USA*



(Received 19 February 2019; published 7 May 2019)

Searching for black hole echo signals with gravitational waves provides a means of probing the near-horizon regime of these objects. We demonstrate a pipeline to efficiently search for these signals in gravitational wave data and calculate model selection probabilities between signal and no-signal hypotheses. As an example of its use we calculate Bayes factors for the Abedi-Dykaar-Afshordi (ADA) model on events in LIGO's first observing run and compare to existing results in the literature. We discuss the benefits of using a full likelihood exploration over existing search methods that used template banks and calculated p-values. We use the waveforms of ADA, although the method is easily extendable to other waveforms. With these waveforms we are able to demonstrate a range of echo amplitudes that is already ruled out by the data.

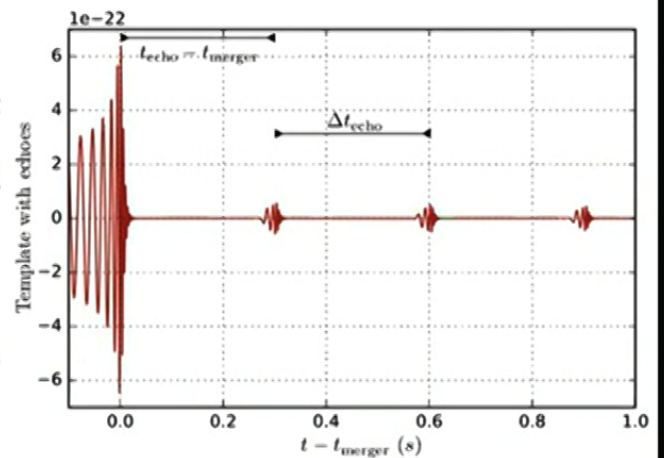
DOI: [10.1103/PhysRevD.99.104012](https://doi.org/10.1103/PhysRevD.99.104012)





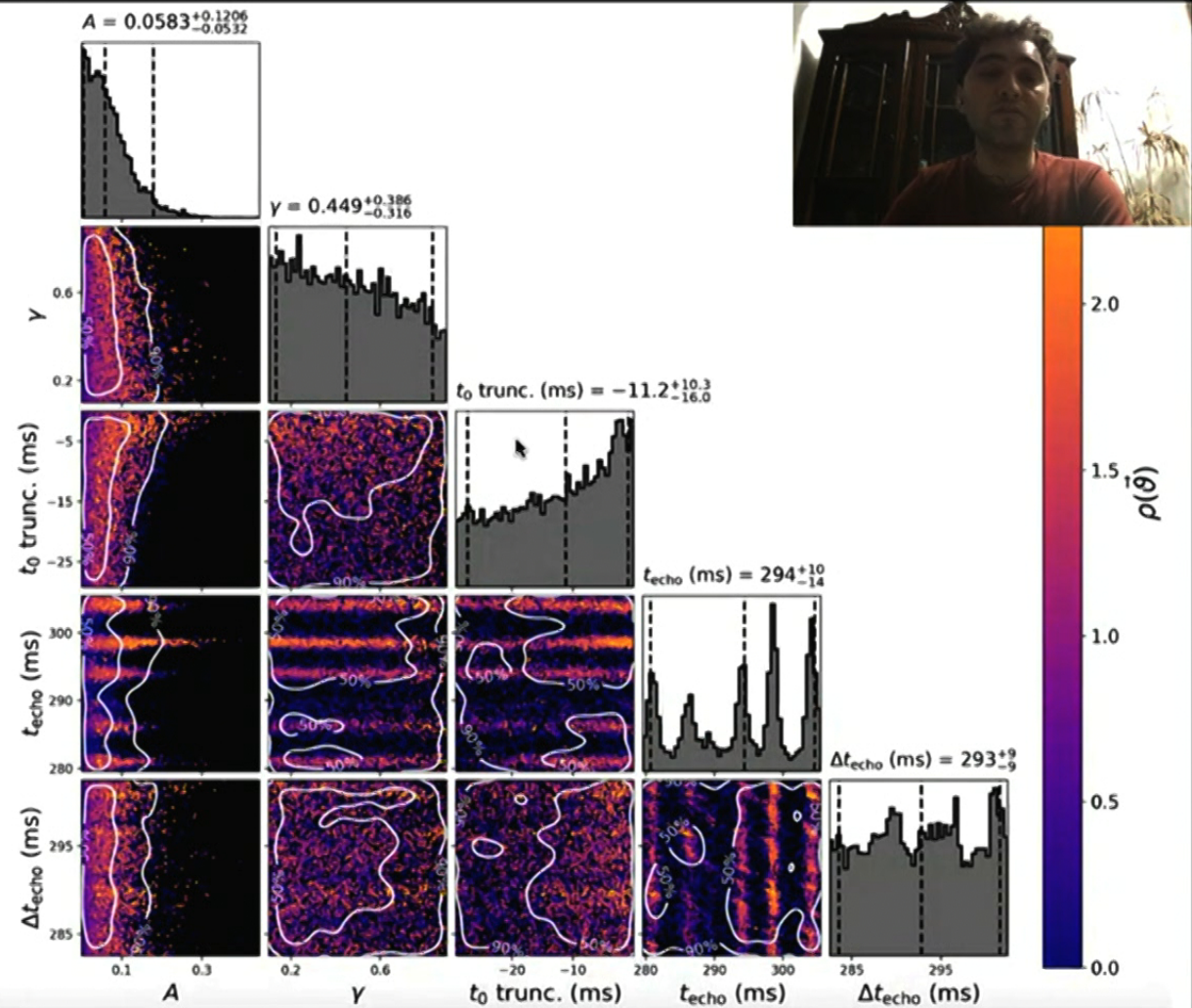
Echo param.	Prior range	GW150914 range
$\Delta t_{\text{echo}}$	Inferred	0.2825 to 0.3025 s
$t_{\text{echo}}$	$\Delta t_{\text{echo}} \pm 1\%$	0.2795 to 0.3055 s
$t_0$ trunc.	$(-0.1 \text{ to } 0)\Delta t_{\text{echo}}$	-0.02925 to 0 s
$\gamma$	0.1 to 0.9	0.1 to 0.9
$A$	Unconstrained	0.00001 to 0.9

Event	Log Bayes factor	Max SNR
GW150914	-1.8056	2.86
GW151012	1.2499	5.57
GW151226	0.4186	4.07



Results of Nielsen et al.  
Phys. Rev. D 99, 104012  
(2019) for GW150914  
are showing preference  
for noise

Log Bayes factor  $\approx -1.8$



## Comment on Nielsen et al. Phys. Rev. D 99, 104012



Comparing two papers of the same group [Westerweck et al. \(Phys. Rev. D 97, 124037 \(2018\)\)](#) and [Nielsen et al. \(Phys. Rev. D 99, 104012 \(2019\)\)](#) it is puzzling that why max SNR that is reported in [Phys. Rev. D 97, 124037 \(2018\)](#) for GW151012 and GW151225 is roughly consistent with what was found by [Abedi, Dykaar & Afshordi \(Phys. Rev. D 96, 082004 \(2017\)\)](#). However, the max SNR found for GW150914 is, much smaller than what we found (4.13), or they found in [\(Phys. Rev. D 97, 124037 \(2018\)\)](#).

Event	Log Bayes factor	Max SNR
GW150914	-1.8056	2.86
GW151012	1.2499	5.57
GW151226	0.4186	4.07



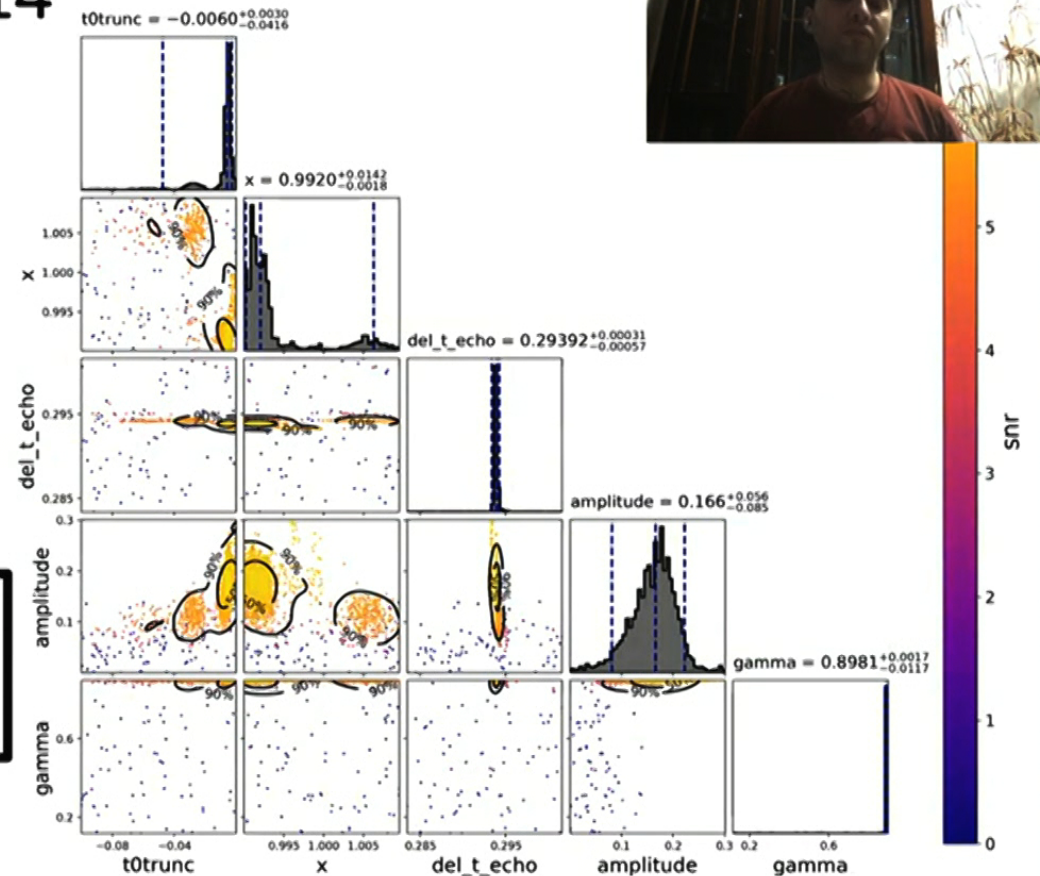
# Our Results for GW150914

Log Bayes factor  $\simeq 3$

We are puzzled by why results of Nielsen et al. are different, given that we are actually using their code!!!

Already, their max SNR in their own two papers are not consistent!!

Preference for signal!!!  
Strong evidence



Thank you

