

Title: PSI 2019/2020 - Quantum Matter Part 2 - Lecture 2

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# What is Quantum Complexity?

## part 2

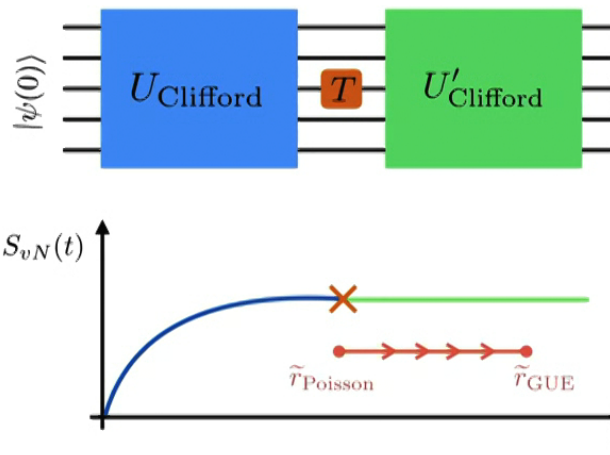
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PSI - Quantum Matter  
February 2020



# TRANSITION TO QUANTUM COMPLEXITY BY DOPING WITH T GATES



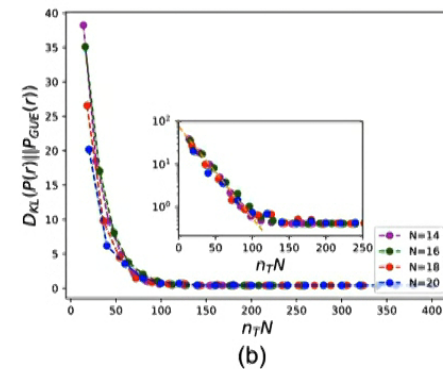
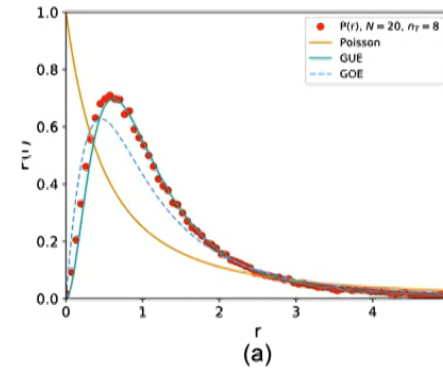
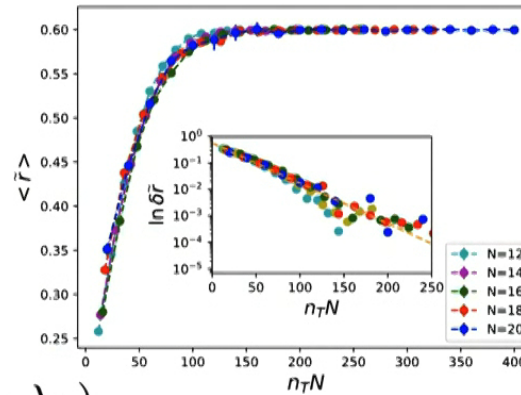
- We place  $n$  (possibly just one)  $T$  gates sandwiched by Clifford circuits
- $n=0$  will be just a Clifford circuit: ESS will be Poisson
- Can we drive a transition to Universal (GUE) ESS?
- Is integrability immediately destroyed?
- What does Universal GUE correspond to?

# RESULTS

$$r_k = \frac{\lambda_{k-1} - \lambda_k}{\lambda_k - \lambda_{k+1}}$$

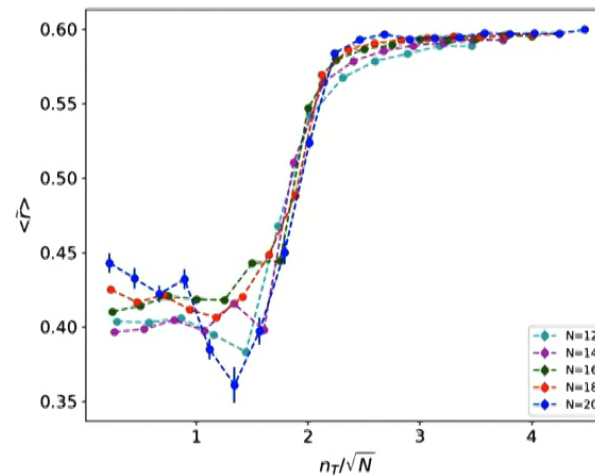
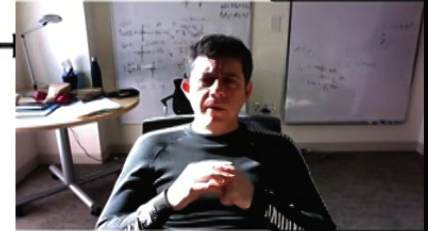
$$\tilde{r}_k = \frac{\min(\lambda_{k-1} - \lambda_k)}{\max(\lambda_k - \lambda_{k+1})}$$

- A single T gate can drive to universal ESS
- Therefore irreversibility and unlearnability ensue
- Operator spreading and scrambling are involved
- the fate of T-designs and entanglement fluctuations depends on this transition



## A QUANTUM KAM, THE ONSET OF QUANTUM CHAOS

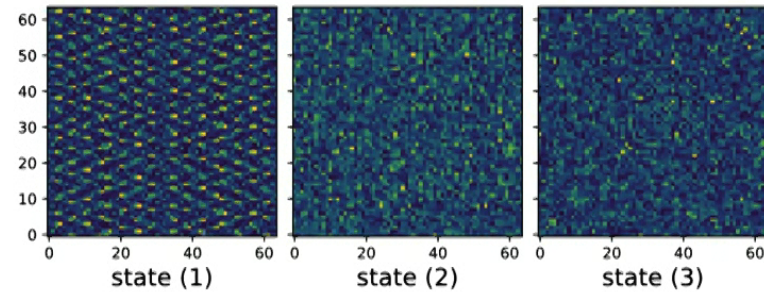
$$(T^\dagger)U_{\text{Clifford}} T U_{\text{Clifford}}^\dagger$$



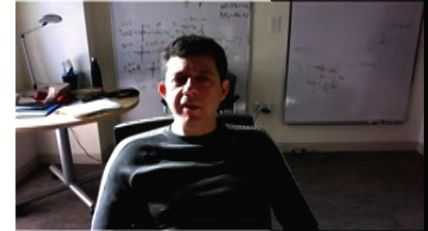
- There is a threshold  $\sim \sqrt{N}$  before Clifford goes into chaos
- This quantity is akin to a OTOC

$$|\Psi\rangle = \sum_{x_A, x_B} \Psi(x_A, x_B) |x_A x_B\rangle$$

$$|\Psi(x_A, x_B)|^2$$



- 1) Clifford gates
- 2) Clifford gates + Sqrt(N) T gates
- 3) Random unitaries




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## CLASSIFICATION BY MACHINE LEARNING

The 4-point out-of-time-order (OTO) correlation function for the local operators  $V, W$  evolved by a RQC  $U$  is given

$$\mathcal{F}_U(V, W) := \langle U^\dagger W^\dagger U V^\dagger U^\dagger W U V \rangle$$

$$W(t) = \sum_k \frac{(it)^k}{k!} [H, \dots [H, W] \dots]$$

for  $k \sim 2N/q$  we get  $2^{2N}$  terms with similar non-negligible weight

For a chaotic circuit, the value of the  $\mathcal{F}_U(V, W)$  reaches the value where  $U^\dagger W U \mapsto \int dU U^\dagger W U$

Does the OTOC  $\mathcal{F}_U(V, W)$  transitions from non-chaotic to chaotic behavior for a RQC doped by T gates? If yes, with what scaling  $n_T$ ?

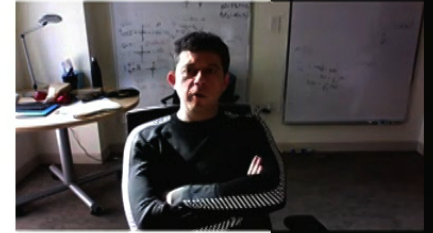



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## Out of Time-Order Correlators



- Black holes are efficient information scramblers
- Information initially localized will quickly thermalize and mix across the full system
- Fastest scrambling = random unitary evolution
- Chaotic dynamics  $\Rightarrow$  scrambling



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## SCRAMBLING AND BLACK HOLES





$$\frac{1}{K} \sum_j p_t(U_j) = \int dU p(U)$$

Unitary t-design

$$\Phi_t(\{U_j\}) = \frac{1}{K^2} \sum_{j,k} |\langle U_j | U_k \rangle|^{2t} \quad \text{Frame Potential}$$

$\Phi_t$  is a t-design iff  $\Phi_t = t!$

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**TRANSITION IN DESIGN**

- When does the onset of complexity happen by universal gates? Is it  $\sqrt{N}$ ?
- What is the role of time fluctuations of the entropy in the effectiveness of cooling?
- When does the unlearnability transition happen?
- When does the transition to 4-designs happen?
- Can you dope anything to a 4-design?
- Can you dope Clifford to Universal by  $\sqrt{N}$ ?



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## QUESTIONS