

Title: Implementing a stochastic dark energy framework into CAMB

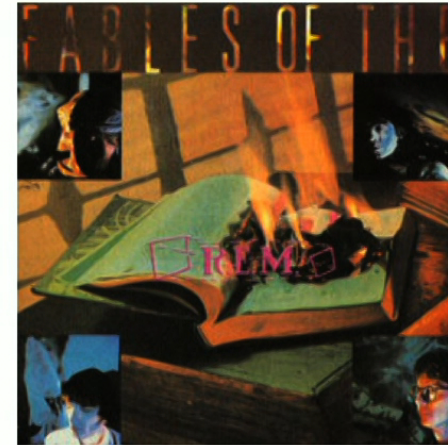
Speakers: Levon Pogosian

Collection: Everpresent Lambda: Theory Meets Observations

Date: November 13, 2019 - 1:30 PM

URL: <http://pirsa.org/19110071>

# Fables of Reconstruction

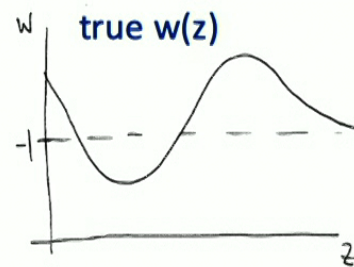


Levon Pogolian  
Simon Fraser University

with Robert Crittenden, Gong-Bo Zhao, Yuting Wang, Alessandra Silvestri, Jian Li and many others

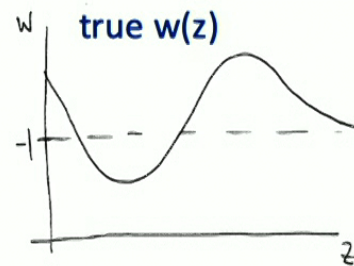






MCMC fit  
using many  $w$ -bins





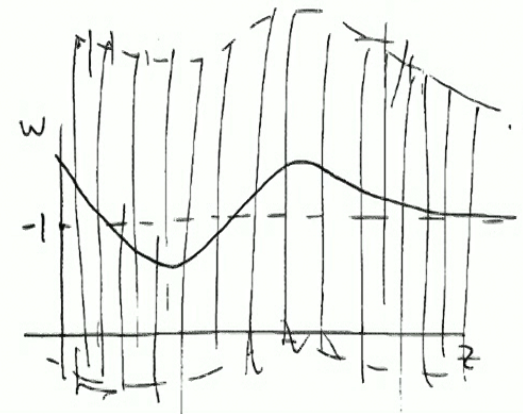
no prior



MCMC fit  
using many  $w$ -bins

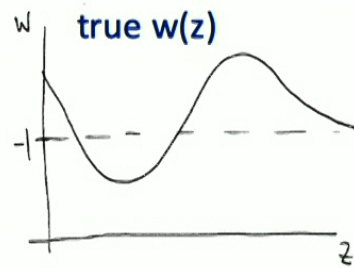


reconstructed  $w(z)$



○ large variance

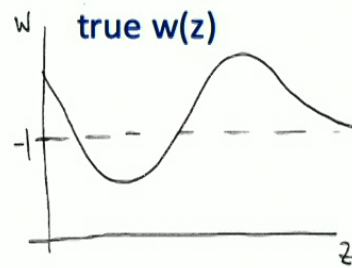
○ zero bias



$$\chi^2_{\text{prior}} = -2 \ln \mathcal{P}_{\text{prior}} = (\mathbf{w} - \mathbf{w}^{\text{fid}})^T \mathbf{C}^{-1} (\mathbf{w} - \mathbf{w}^{\text{fid}})$$

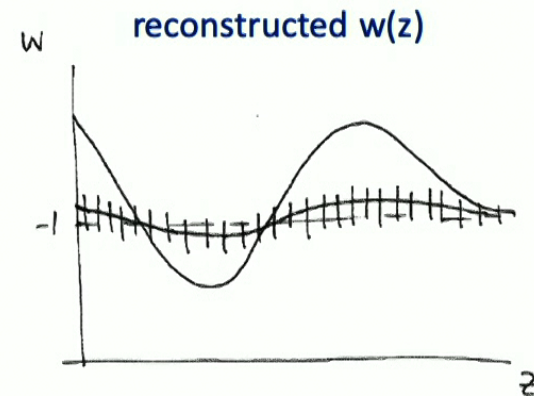


MCMC fit  
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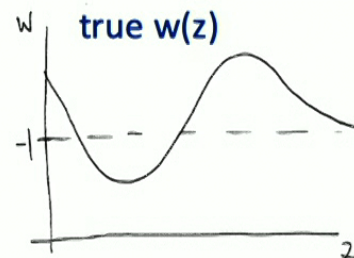
Excessively strong prior

MCMC fit  
using many  $w$ -bins



- tiny error bars (small variance)
- large bias

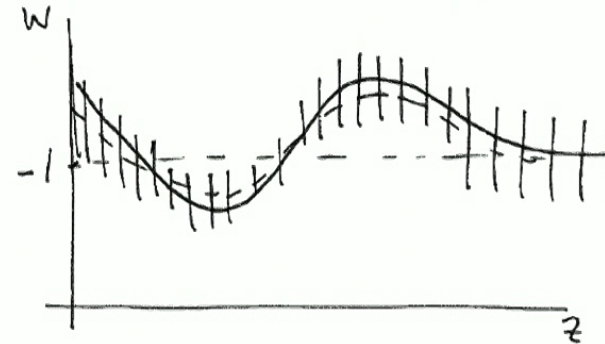




reasonable prior

MCMC fit  
using many  $w$ -bins

reconstructed  $w(z)$



- moderate variance
- insignificant bias, i.e. the bias is smaller than the variance

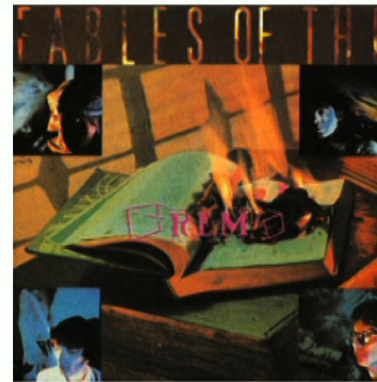
# What is a reasonable prior?

- Informed by theory, e.g. scalar fields

M. Raveri, P. Bull, A. Silvestri, LP, arXiv:1703.05297, PRD

J. Espejo, S. Peirone, M. Raveri, LP, A. Silvestri, K. Koyama, arXiv:1809.01121, PRD

- Smooth features (well constrained by data)  
not biased by the prior
- Noisy features (poorly constrained by data)  
determined by the prior



*Fables of Reconstruction*, R. Crittenden, G.-B. Zhao, LP, L. Samushia, X. Zhang, 1112.1693, JCAP



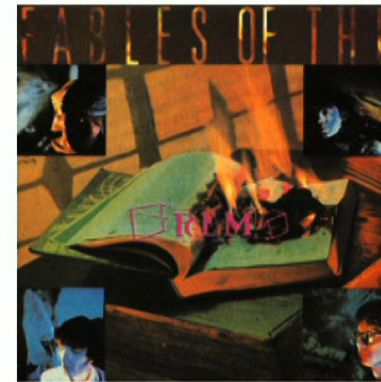
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## Smooth means correlated

- Start with a correlation function:

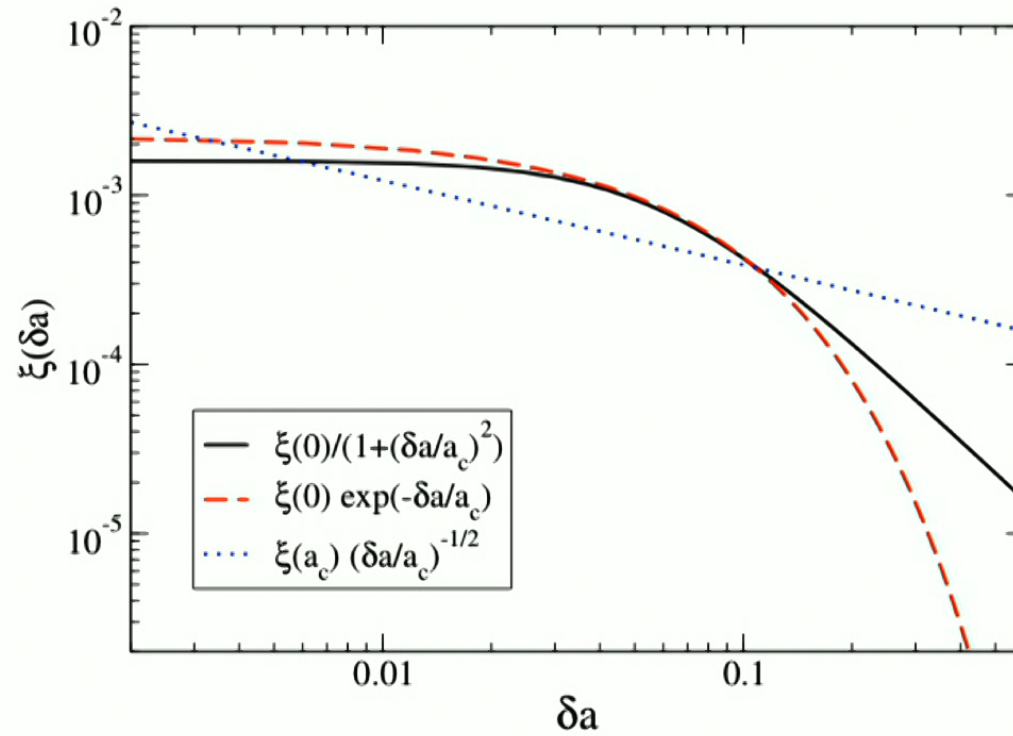
$$\xi_w(|a - a'|) \equiv \langle [w(a) - w^{\text{fid}}(a)][w(a') - w^{\text{fid}}(a')] \rangle$$

- Make a reasonable (not unique) choice of a functional form:

$$\xi_w(\delta a) = \frac{\xi_w(0)}{1 + (\delta a/a_c)^2} \quad \delta a \equiv |a - a'|$$



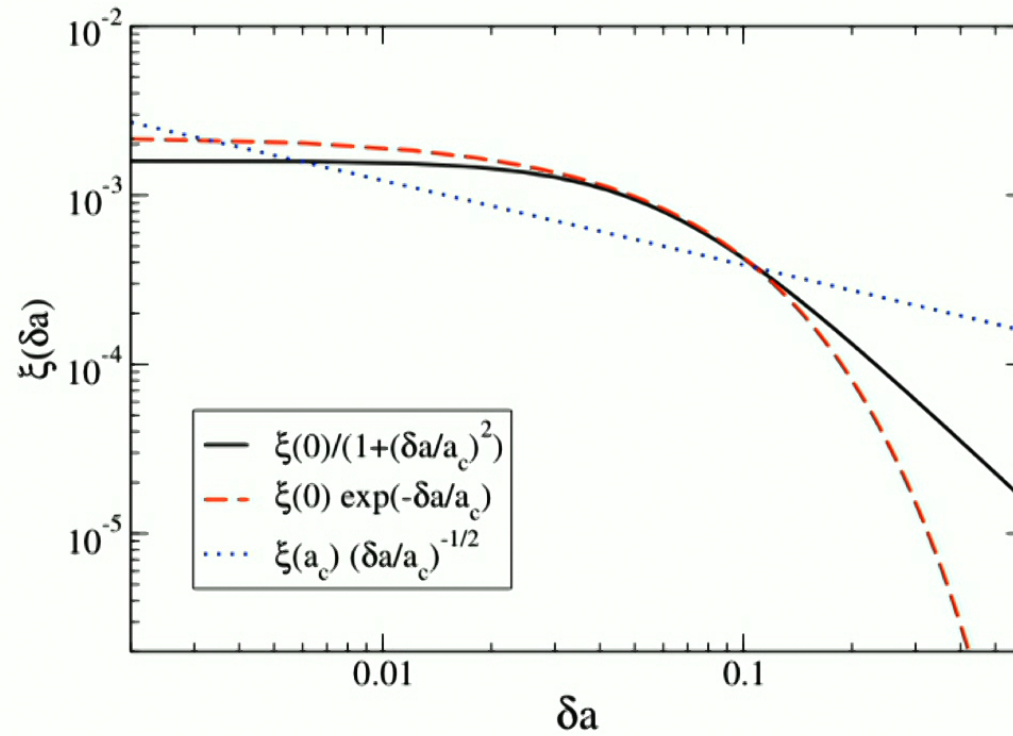
## Correlation functions



- Two control parameters:

“correlation scale” and the overall amplitude

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## The prior covariance matrix

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- Build a covariance matrix from the correlation function

$$C_{ij} \equiv \langle \delta w_i \delta w_j \rangle = \frac{1}{\Delta^2} \int_{a_i}^{a_i + \Delta} da \int_{a_j}^{a_j + \Delta} da' \xi_w(|a - a'|).$$

- Build a correlation prior from the covariance matrix

$$\chi_{\text{prior}}^2 = -2 \ln \mathcal{P}_{\text{prior}} = (\mathbf{w} - \mathbf{w}^{\text{fid}})^T \mathbf{C}^{-1} (\mathbf{w} - \mathbf{w}^{\text{fid}})$$





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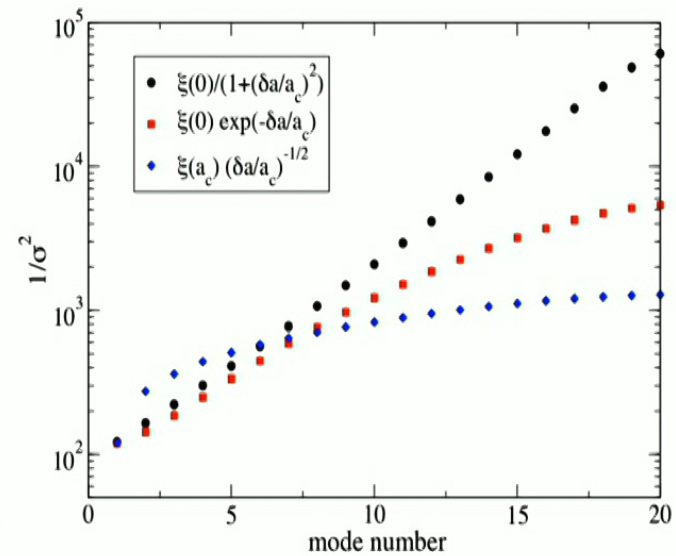
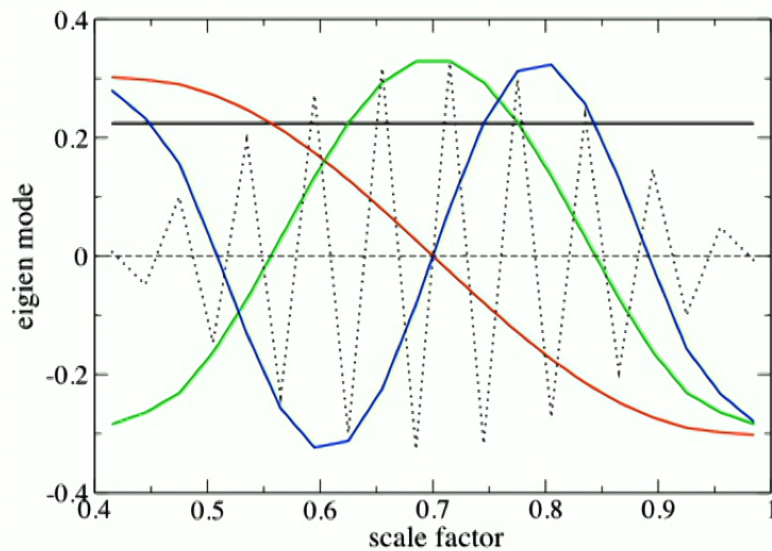
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## Eigenmodes and eigenvalues of the correlated prior



- High frequencies constrained best
- Low frequencies constrained worst

## Wiener Filtering

Posterior:  $\mathcal{P}(\mathbf{w}|\mathbf{w}^{\text{obs}}) = \mathcal{P}(\mathbf{w}^{\text{obs}}|\mathbf{w}) \times \mathcal{P}_{\text{prior}}(\mathbf{w})$

Likelihood:  $\mathcal{P}(\mathbf{w}^{\text{obs}}|\mathbf{w}) \propto e^{-(\mathbf{w}^{\text{obs}} - \mathbf{w})^T \mathbf{F} (\mathbf{w}^{\text{obs}} - \mathbf{w}) / 2}$

Prior:  $\mathcal{P}_{\text{prior}}(\mathbf{w}) \propto e^{-(\mathbf{w} - \mathbf{w}^{\text{fid}})^T \mathbf{C}^{-1} (\mathbf{w} - \mathbf{w}^{\text{fid}}) / 2}$





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$$\mathbf{w}^{\text{recon}} = \underbrace{\mathbf{F}^{-1}(\mathbf{C} + \mathbf{F}^{-1})^{-1} \mathbf{w}^{\text{fid}}}_{\text{High-pass "filter" of the fiducial } \mathbf{w}} + \mathbf{C}(\mathbf{C} + \mathbf{F}^{-1})^{-1} \mathbf{w}^{\text{obs}}$$

High-pass "filter"  
of the fiducial  $\mathbf{w}$

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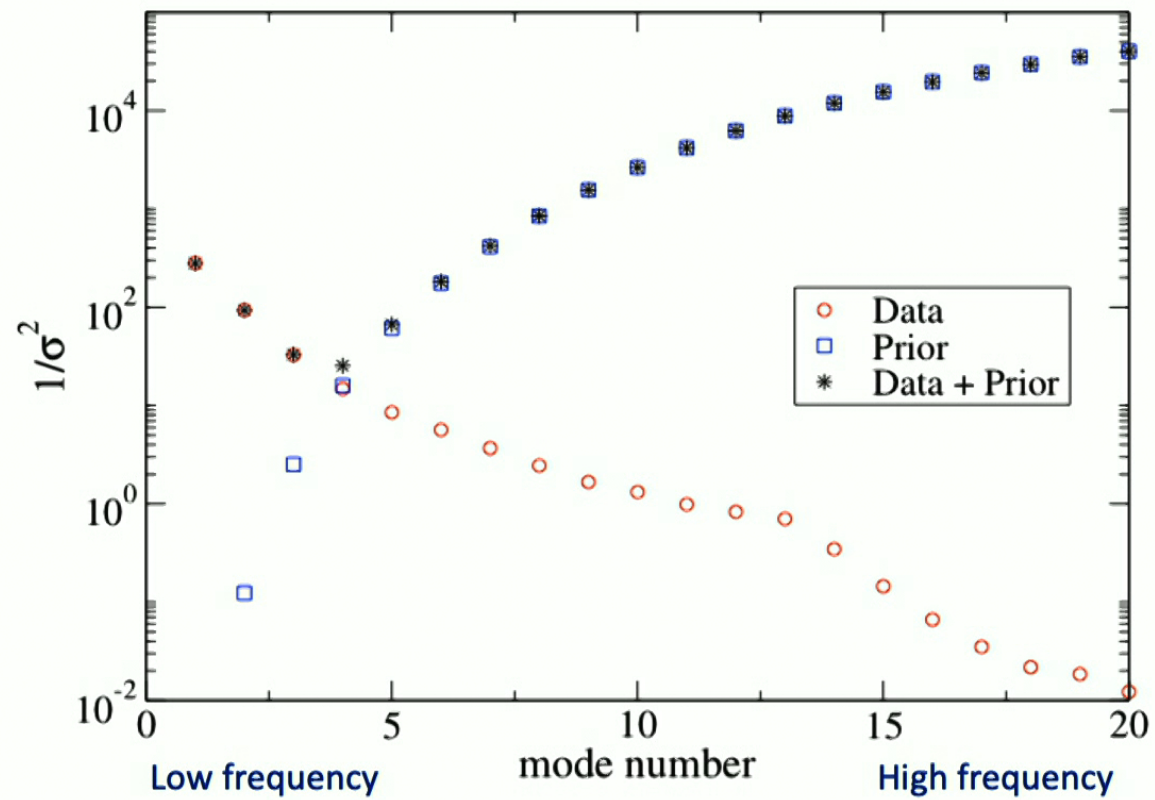
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High-pass "filter"  
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Low-pass "filter"  
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# Data meets Prior

Forecast for EUCLID-like SNe,  $H(z)$ ; Planck CMB





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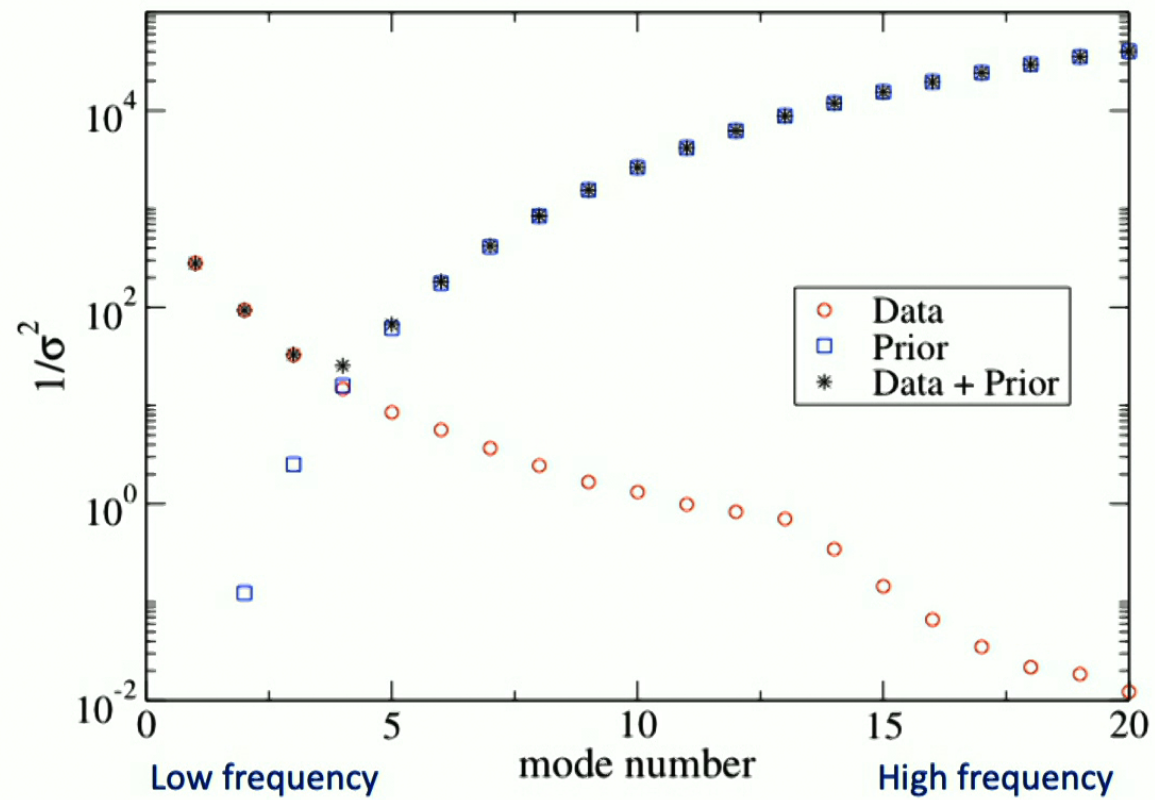
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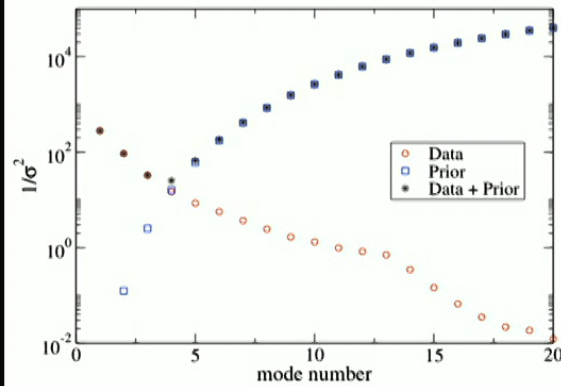


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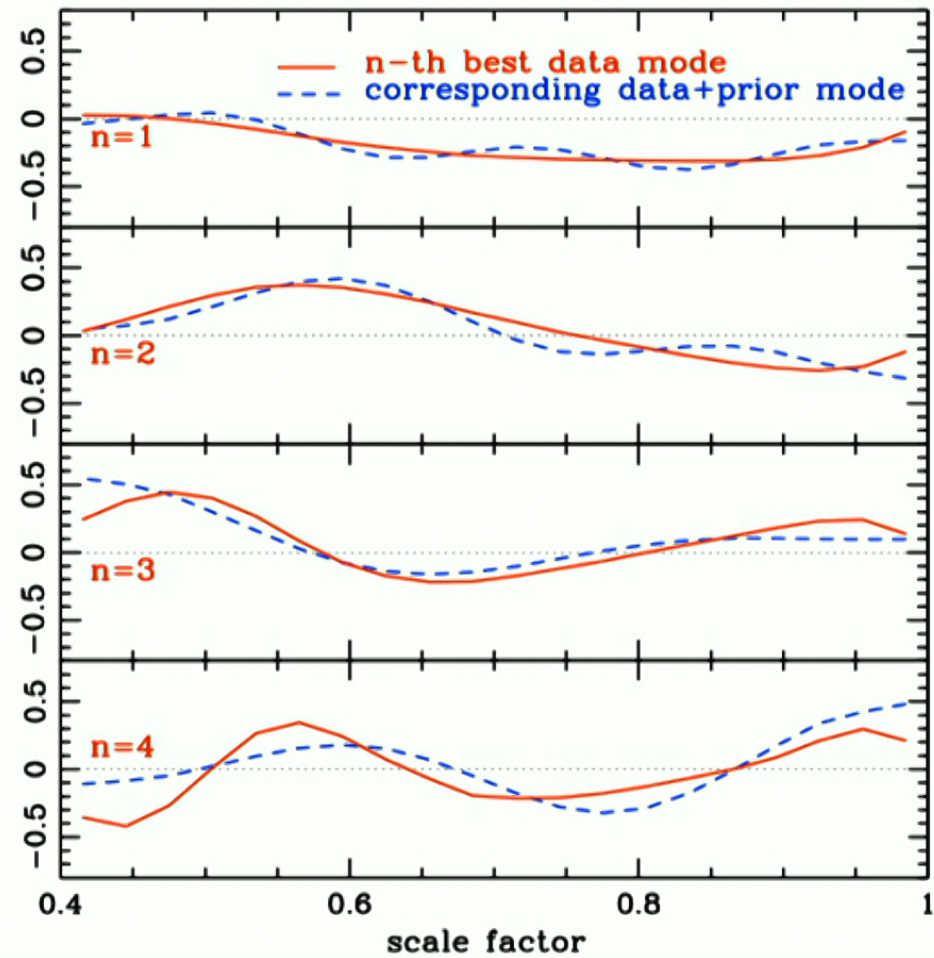
Forecast for EUCLID-like SNe,  $H(z)$ ; Planck CMB



## Surviving data eigenmodes

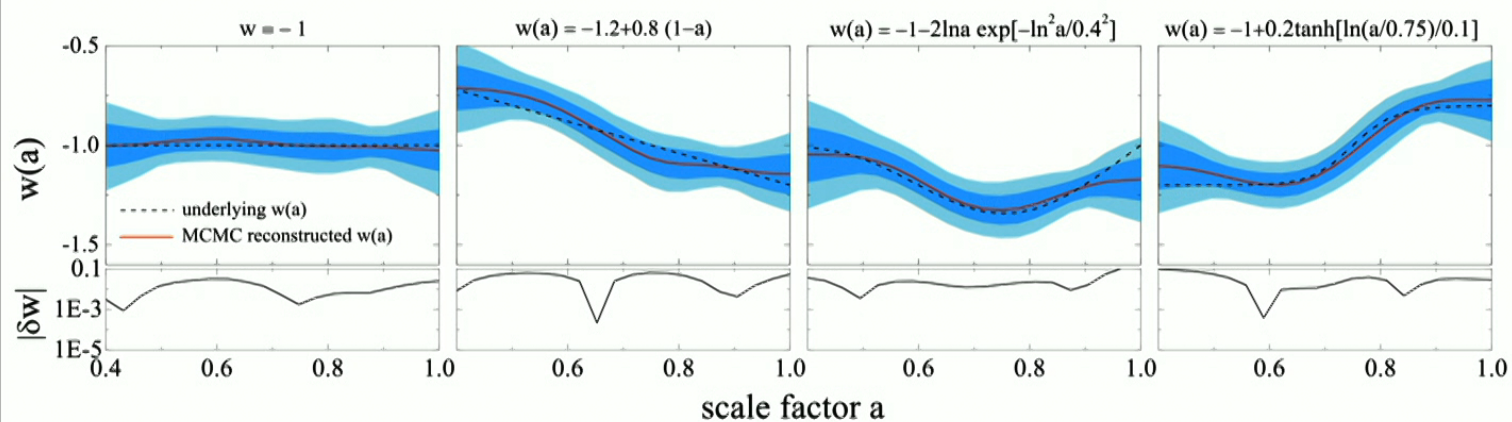


$a_c=0.06$   
prior on mean  $w = 0.02$



# Reconstructions using mock datasets

Planck + Euclid



$$\chi^2 = \chi_{\text{data}}^2 + \chi_{\text{prior}}^2$$



## Reconstruction from the 2012 data

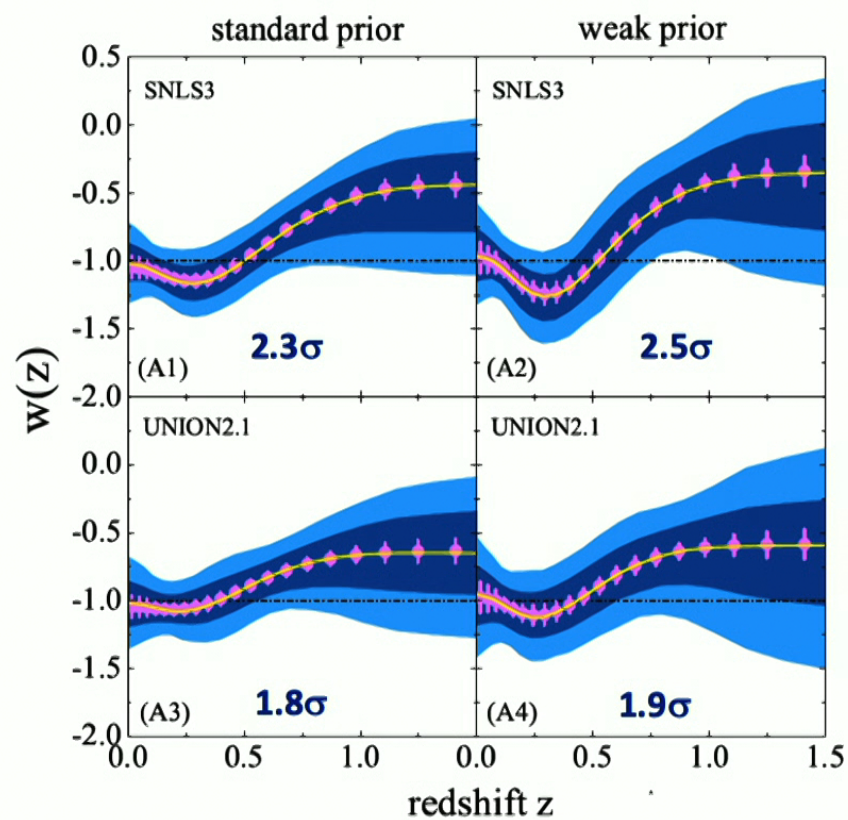
- CMB from WMAP7
- Supernovae
  - Union 2.1, Suzuki et al, ApJ (2012)
  - SNLS 3, Conley et al, ApJS (2011)
- Baryon Acoustic Oscillations
  - SDSS-II, SDSS-III BOSS, 6dF, WiggleZ
- Redshift Space Distortions
  - SDSS-II, SDSS-III BOSS, 6dF, WiggleZ
- $H(z)$  compilation
  - Moresco et al, 1201.6658

G-B Zhao, R. Crittenden, L. Pogosian, X. Zhang, arXiv:1207.3804, PRL



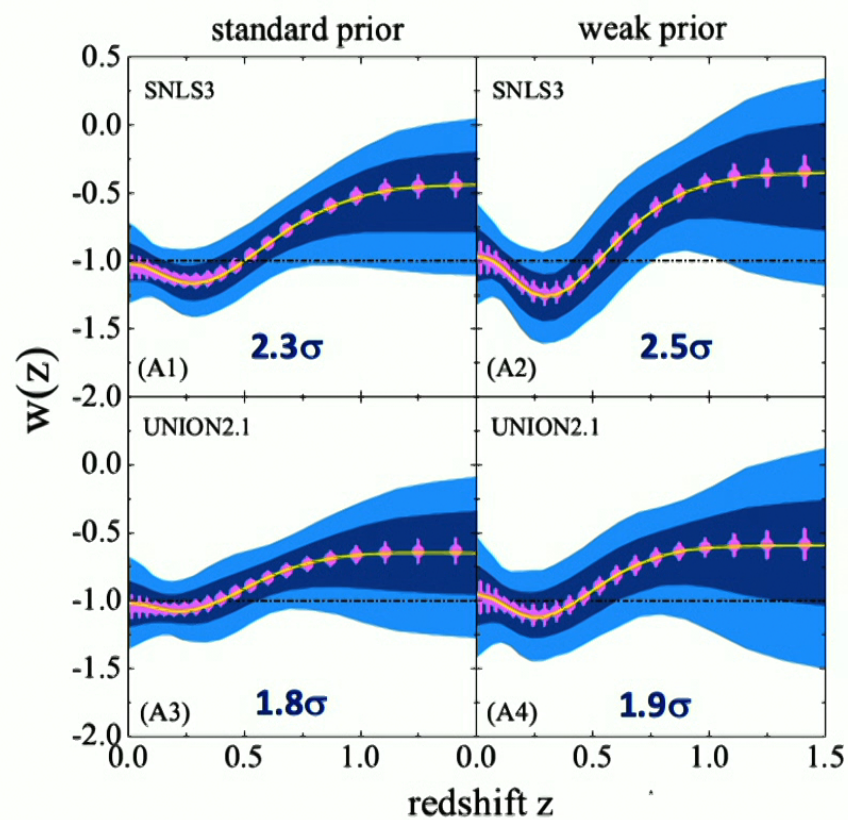


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## Examining the Bayesian evidence

$$E \equiv \int d^n \mathbf{P} \mathcal{P}(\mathbf{D}|\mathbf{P}) \mathcal{P}_{\text{prior}}(\mathbf{P})$$





## Examining the Bayesian evidence

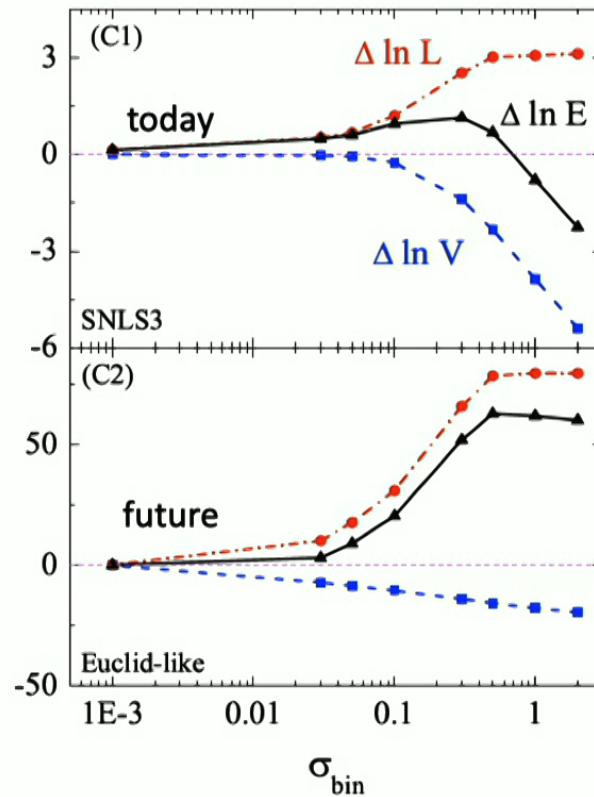
$$E \equiv \int d^n \mathbf{P} \mathcal{P}(\mathbf{D}|\mathbf{P}) \mathcal{P}_{\text{prior}}(\mathbf{P})$$

- The best fit model fits data better than Lambda, but it has more parameters
- Does improvement in the fit justify adding new parameters?
- Note – even though the number of bins is large, the effective number of free parameters is small because the prior constrains most of the degrees of freedom



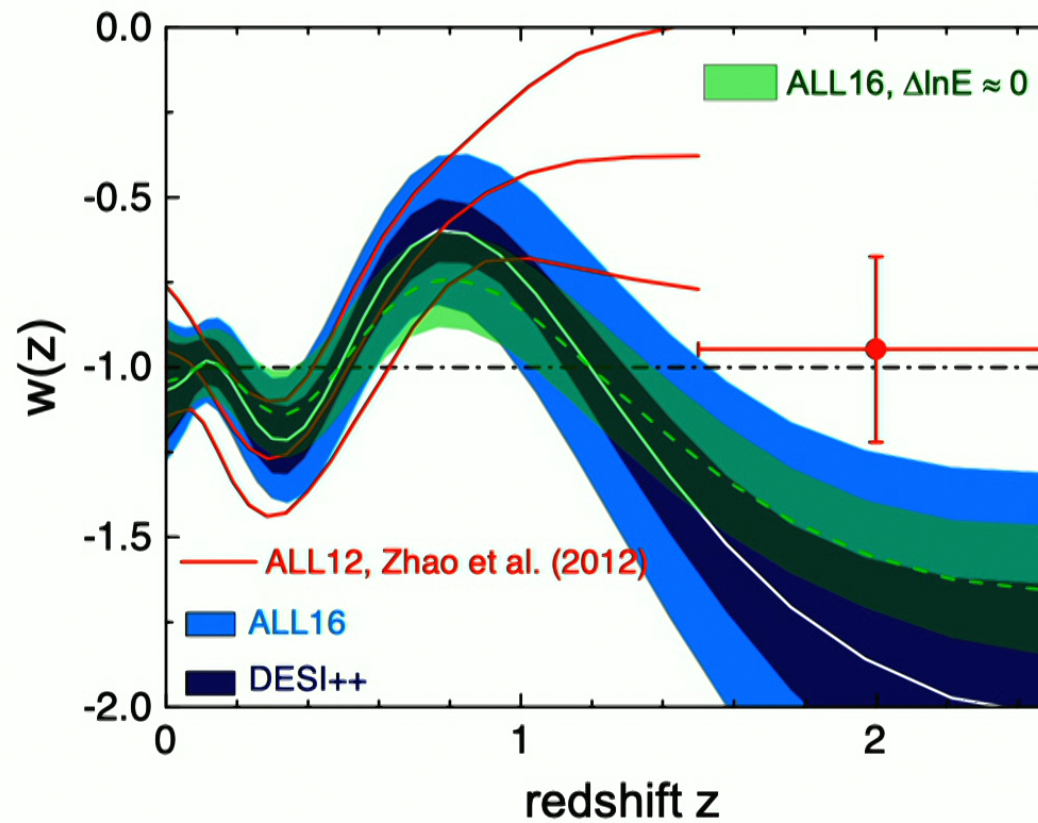


## Ratio of evidences: the Bayes' factor

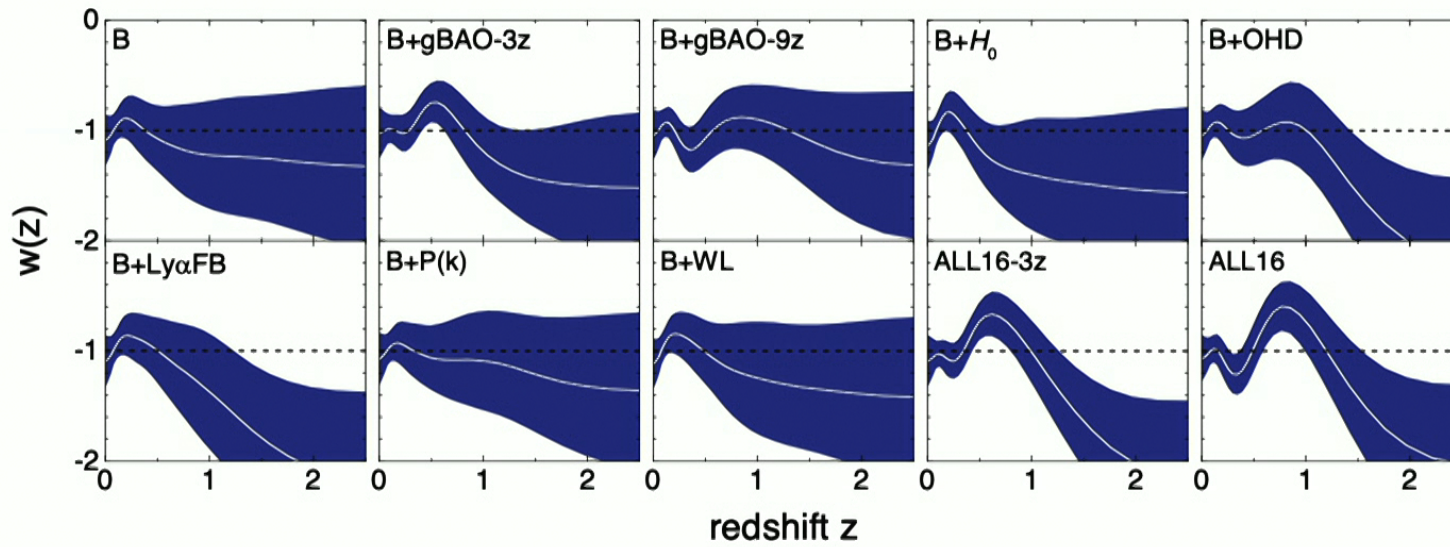


In the absence of a firm theoretical prediction for a prior, the departure from LCDM is considered significant if the Bayes' factor remains large for a wide range of priors parameters, e.g.  $\sigma_{\text{bin}}$ .

## Reconstruction from the 2016 data



G.-B. Zhao et al, arXiv:1701.08165, Nature Astronomy



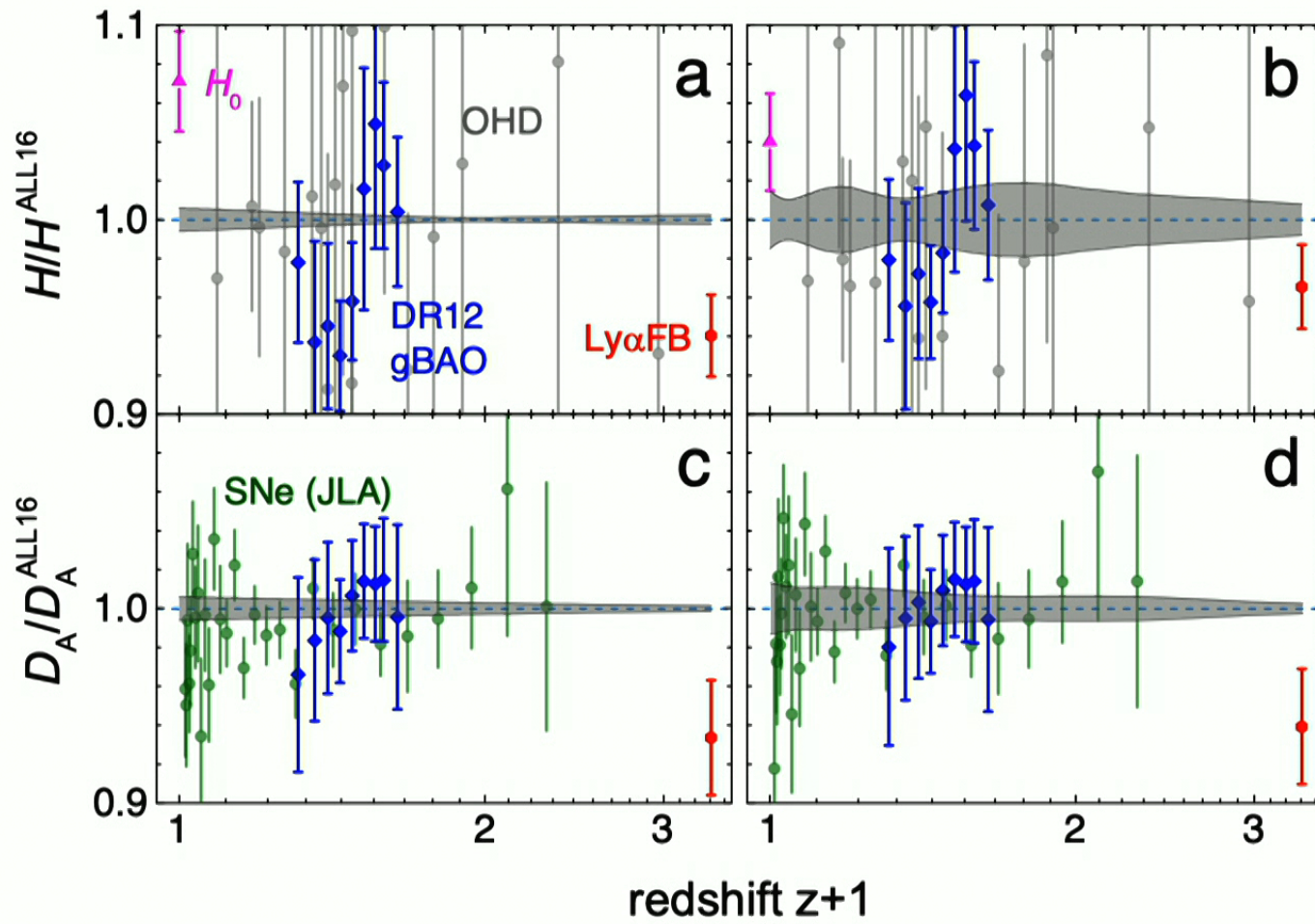
**Table 1 |** The improved  $\chi^2$  with respect to that of the  $\Lambda$ CDM model

|                                                          | P15  | JLA  | gBAO | $P(k)$ | WL   | $H_0$ | Ly $\alpha$ FB | OHD  |
|----------------------------------------------------------|------|------|------|--------|------|-------|----------------|------|
| $\chi^2_{w(z)\text{CDM}} - \chi^2_{\Lambda\text{CDM}}$   | -0.7 | -1.6 | -2.8 | +1.1   | -0.1 | -2.9  | -3.7           | -2.3 |
| $\chi^2_{w\text{CDM}} - \chi^2_{\Lambda\text{CDM}}$      | 0.0  | +0.5 | +0.7 | +0.4   | +0.2 | -2.9  | -0.2           | 0.0  |
| $\chi^2_{w_0w_0\text{CDM}} - \chi^2_{\Lambda\text{CDM}}$ | -0.7 | +0.4 | +0.9 | +0.5   | +0.4 | -2.7  | -0.3           | 0.0  |

The changes in  $\chi^2$  of individual datasets between the ALL16 best-fit  $w(z)$ CDM,  $w$ CDM and  $w_0w_0$ CDM models and the  $\Lambda$ CDM model.

G.-B. Zhao et al, arXiv:1701.08165, Nature Astronomy

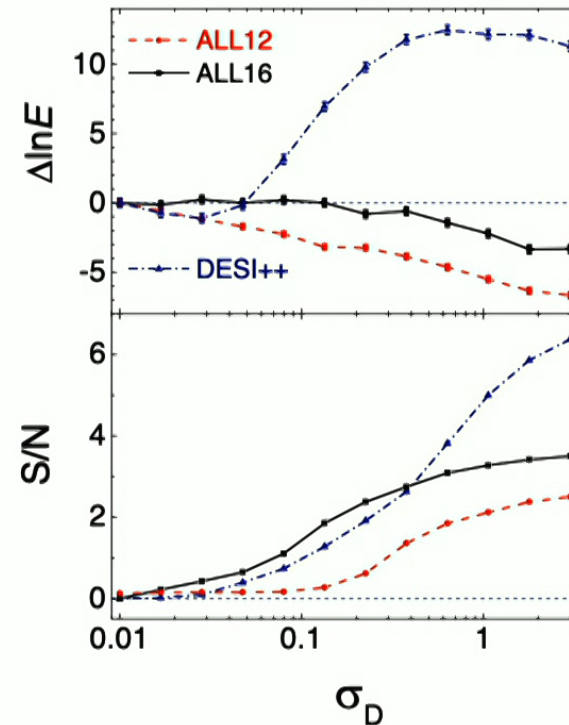




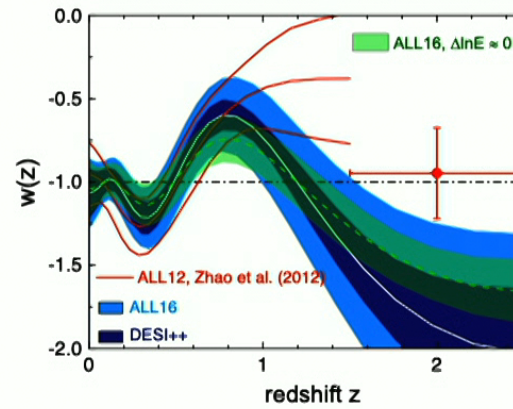


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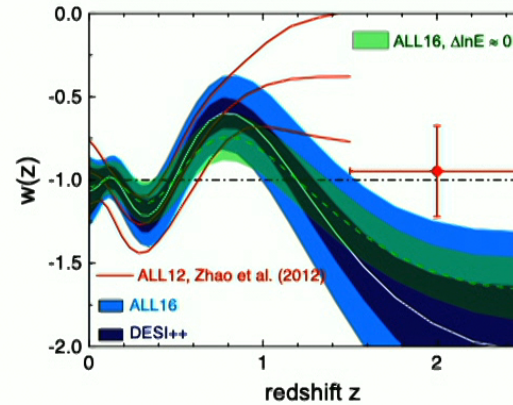
- Dynamical dark energy is preferred at a 3.5-sigma significance level based on the improvement in the fit alone
- Effectively, 4 additional degrees of freedom
- No Bayesian preference for dynamics
- Evidence increased since 2012
- Future data can conclusively confirm or rule out this dynamical dark energy



If this was real, what could it be?



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General Relativity with a minimally coupled scalar field (quintessence)

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{16\pi G} \{ R - \partial^\mu \phi \partial_\mu \phi - 2V(\phi) \} + \mathcal{L}_M(g_{\mu\nu}, \psi) \right]$$

$$w_\phi = \frac{p_\phi}{\rho_\phi} = \frac{\dot{\phi}^2/2 - V(\phi)}{\dot{\phi}^2/2 + V(\phi)} \geq -1$$



## Modified gravity: a scalar-tensor theory

$$S = \int d^4x \sqrt{-g} \left[ \frac{F(\phi)R}{16\pi G} - \frac{1}{2} \partial^\mu \phi \partial_\mu \phi - V(\phi) + \mathcal{L}_M \right]$$

$$\begin{aligned} G_{\mu\nu} &= 8\pi G F^{-1} \{ T_{\mu\nu}^M + T_{\mu\nu}^\phi + \nabla_\mu \nabla_\nu F - g_{\mu\nu} \square F \} \\ &= 8\pi G \{ T_{\mu\nu}^M + (T_{\text{DE}}^{\text{eff}})_{\mu\nu} \} , \end{aligned}$$

Effective dark energy density:

$$\rho_{\text{DE}}^{\text{eff}} = F^{-1} \left\{ \frac{1}{2} \dot{\phi}^2 + V(\phi) - 3H\dot{F} + (1 - F)\rho_M \right\}$$

Effective dark energy equation of state:

$$w_{\text{DE}}^{\text{eff}} = \frac{\dot{\phi}^2/2 - V(\phi) + 2H\dot{F} + \ddot{F}}{\dot{\phi}^2/2 + V(\phi) - 3H\dot{F} + (1 - F)\rho_M}$$



## Is working with $w_{\text{eff}}$ justified when probing modified gravity?

$$\dot{\rho}_{\text{DE}}^{\text{eff}} + 3H(\rho_{\text{DE}}^{\text{eff}} + p_{\text{DE}}^{\text{eff}}) = 0 \quad ? \quad \Rightarrow \quad \rho_{\text{DE}}(a) = \rho_0 \exp \left[ \int_a^1 3(1 + w(a')) \frac{da'}{a'} \right]$$

Working with  $w_{\text{eff}}$  assumes that the effective density doesn't change sign,  
but it can in modified gravity, e.g.

$$\rho_{\text{DE}}^{\text{eff}} = F^{-1} \left\{ \frac{1}{2} \dot{\phi}^2 + V(\phi) - 3H\dot{F} + (1 - F)\rho_M \right\}$$

$$w_{\text{DE}}^{\text{eff}} = p_{\text{DE}}^{\text{eff}} / \rho_{\text{DE}}^{\text{eff}} \quad ?$$



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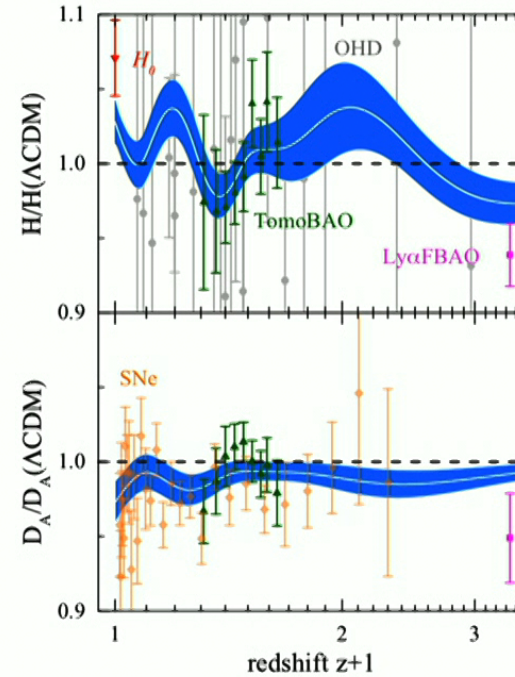
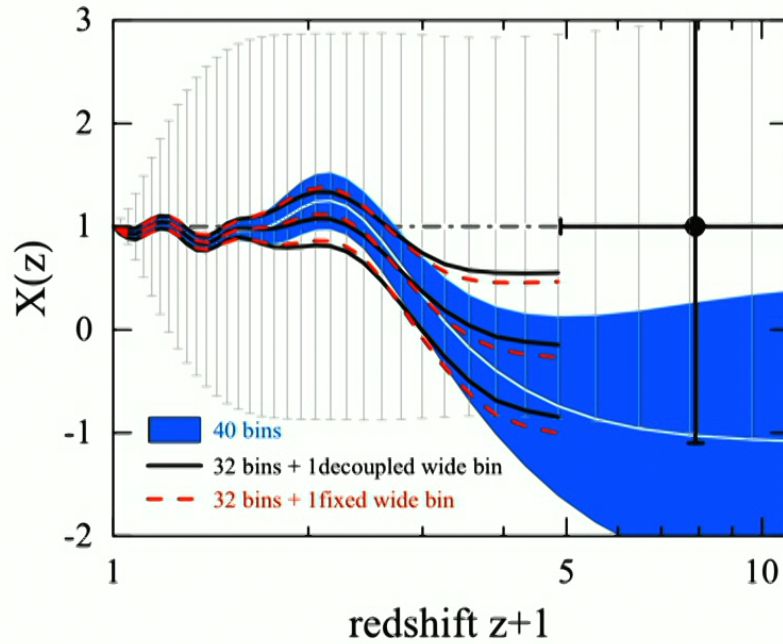
$$w_{\text{DE}}^{\text{eff}} = p_{\text{DE}}^{\text{eff}} / \rho_{\text{DE}}^{\text{eff}} \quad ?$$

Parametrizing the effective dark energy evolution in terms of  $w_{\text{eff}}$  can bias the studies of modified gravity. It's safer to work directly with  $\rho_{\text{eff}}$ :

$$\frac{H^2}{H_0^2} = \frac{\Omega_r}{a^4} + \frac{\Omega_M}{a^3} + \Omega_{\text{DE}} X(a)$$



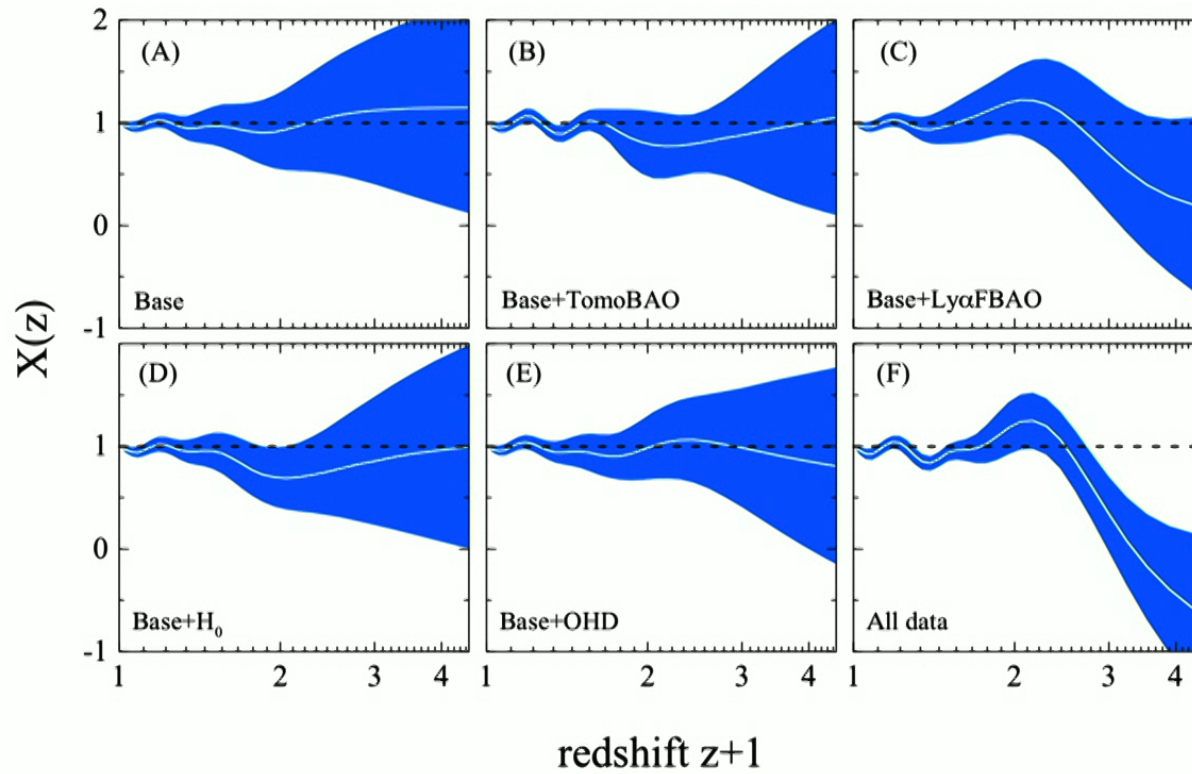
## Reconstructed Effective Dark Energy Density



Y. Wang, G.-B. Zhao, LP and A. Zucca, 1807.03772, Ap J Lett

# Reconstructed Dark Energy Density

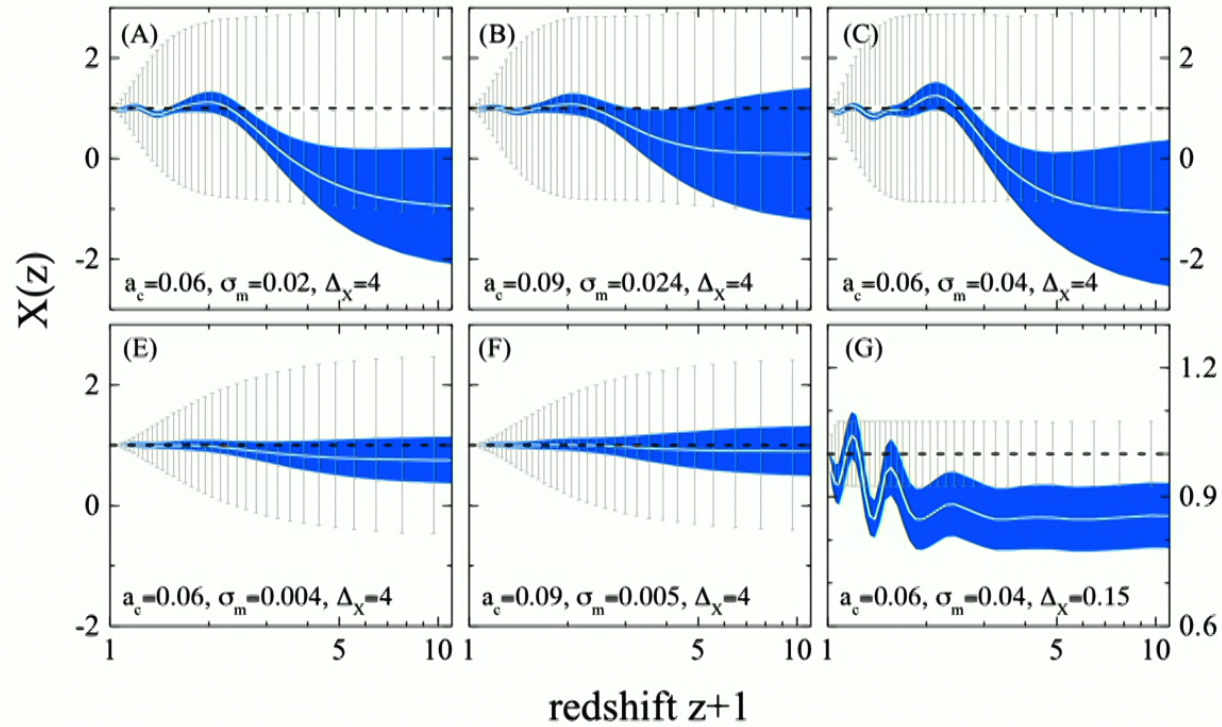
The effect of individual datasets



Y. Wang, G.-B. Zhao and LP, 1807.03772

# Reconstructed Dark Energy Density

The effect of different priors

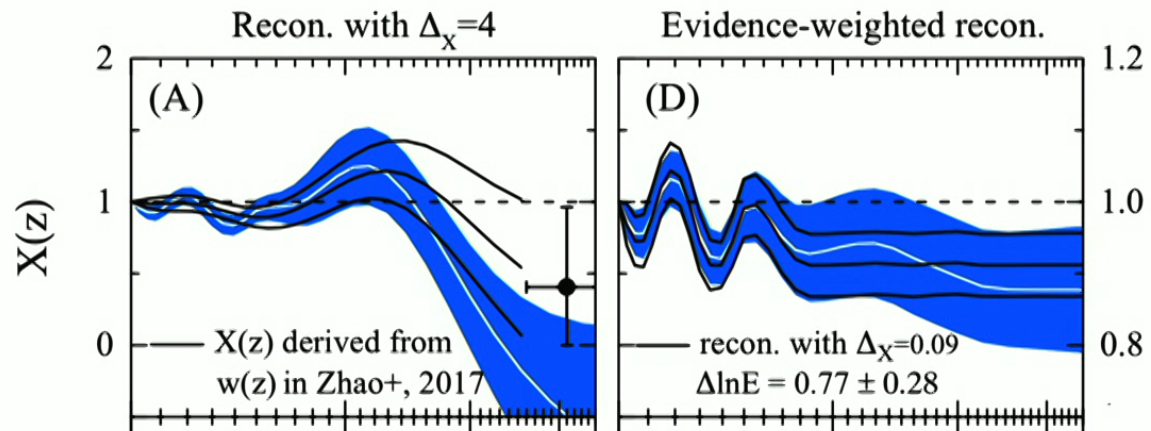
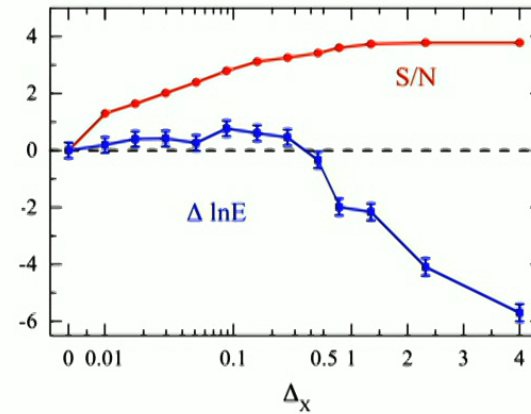


Y. Wang, G.-B. Zhao and LP, 1807.03772



## Evidence weighted reconstruction

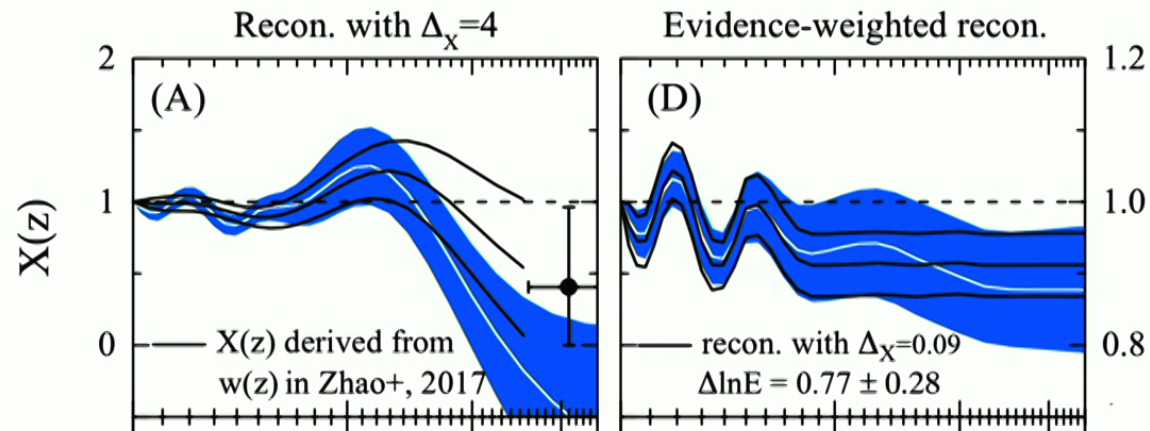
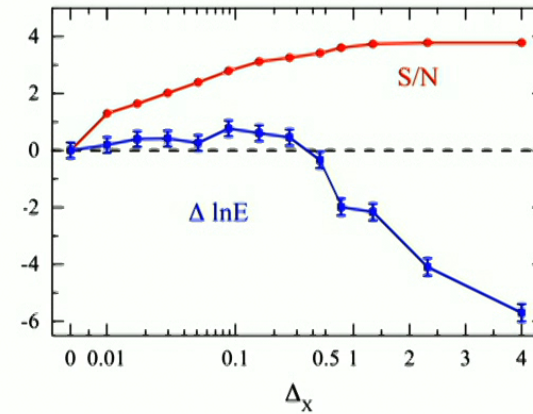
$$Z_W(z) \equiv \frac{\sum_i [Z(z; \Delta_{X_i}) e^{\Delta \ln E(\Delta_{X_i})}]}{\sum_i [e^{\Delta \ln E(\Delta_{X_i})}]}$$



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## Dynamical Dark Energy?

- Dynamical dark energy resolves the tensions between the Planck best fit LCDM model and the local estimates of  $H_0$
- Dynamical dark energy is preferred at a 3.7-sigma significance level based on the improvement in the fit alone
- Mild preference (but no Bayesian evidence) for an increasing dark energy density
- Small Bayesian evidence for oscillatory features at  $z < 1$ , driven by BAO and SNIa data
- Future data (e.g. Euclid) can conclusively confirm or rule out the reconstructed dynamics of Dark Energy





# Phenomenology of Scalar-Tensor Theories

Theories of Jordan-Brans-Dicke type, with a canonical kinetic term  
(e.g. “chameleon”,  $f(R)$ , “symmetron”)

$$S = \int d^4x \sqrt{-g} \left[ \frac{A^{-2}(\phi)}{16\pi G} R - \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi) + \mathcal{L}_M(g_{\mu\nu}, \psi) \right]$$

In the “Einstein” frame:  $\tilde{g}_{\mu\nu} = A^{-2}(\phi) g_{\mu\nu}$

$$S = \int d^4x \sqrt{-\tilde{g}} \left[ \frac{\tilde{R}}{16\pi G} - \frac{1}{2} \tilde{g}^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - \tilde{V}(\phi) + \mathcal{L}_M(A^2(\phi) \tilde{g}_{\mu\nu}, \psi) \right]$$



## Beyond probing the expansion history



# Phenomenology of Scalar-Tensor Theories

*“Spacetime tells matter how to move; matter tells spacetime how to curve.”*

John A. Wheeler (1911-2008)

Photons and matter respond to different spacetimes

Non-relativistic matter

- sources the curvature perturbation  $\Phi$
- responds to the Newtonian potential  $\Psi$
- $\Phi$  and  $\Psi$  are NOT the same in scalar-tensor theories
- feels a “fifth force” mediated by the scalar field  $\vec{f} = -\vec{\nabla}\Psi - \frac{d \ln A(\phi)}{d\phi} \vec{\nabla}\phi$

Photons

- respond to  $(\Phi+\Psi)/2$
- do not feel the “fifth force”





# Phenomenology of Scalar-Tensor Theories

General Relativity

$$\begin{aligned}\Psi &= \Phi \\ -k^2 \Phi &= -k^2 \left( \frac{\Phi + \Psi}{2} \right) = 4\pi G a^2 \delta\rho\end{aligned}$$

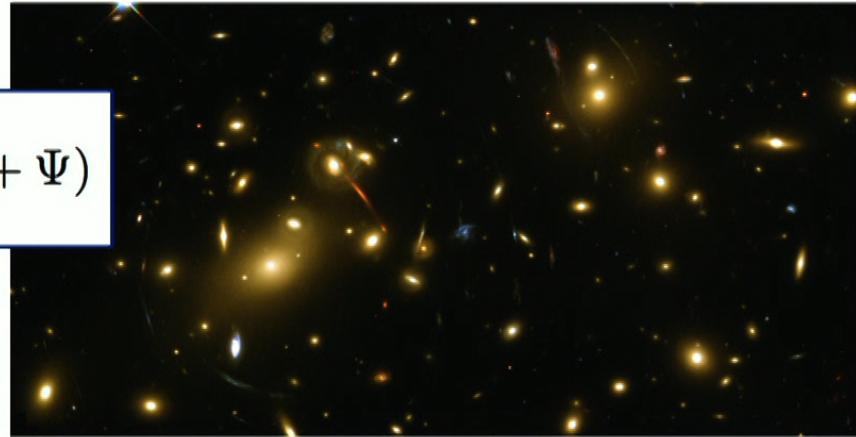
Modified Gravity

$$\begin{aligned}-k^2 \Psi &= 4\pi \mu(a, k) G a^2 \delta\rho \\ \Phi &= \gamma(a, k) \Psi \\ -k^2 \left( \frac{\Phi + \Psi}{2} \right) &= 4\pi \Sigma(a, k) G a^2 \delta\rho\end{aligned}$$

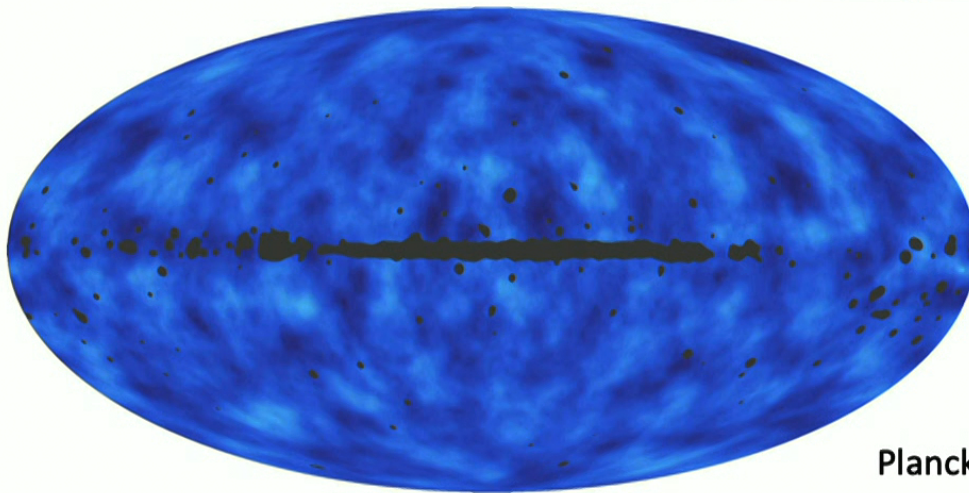


# Gravitational Lensing

$$\text{Distortion} \propto \int dz \partial_{\perp}(\Phi + \Psi)$$



Hubble



Planck

## Phenomenology of Horndeski

$$S = \int d^4x \sqrt{-g} \left\{ \frac{m_0^2}{2} \Omega(t) R + \Lambda(t) - c(t) \delta g^{00} + \frac{M_2^4(t)}{2} (\delta g^{00})^2 - \frac{\bar{M}_1^3(t)}{2} \delta g^{00} \delta K_i^i - \frac{\bar{M}_2^2(t)}{2} \left( \delta K_i^i{}^2 - \delta K_j^i \delta K_i^j + 2 \delta g^{00} \delta R^{(3)} \right) \right\} + S_{matter}[g_{\mu\nu}]$$

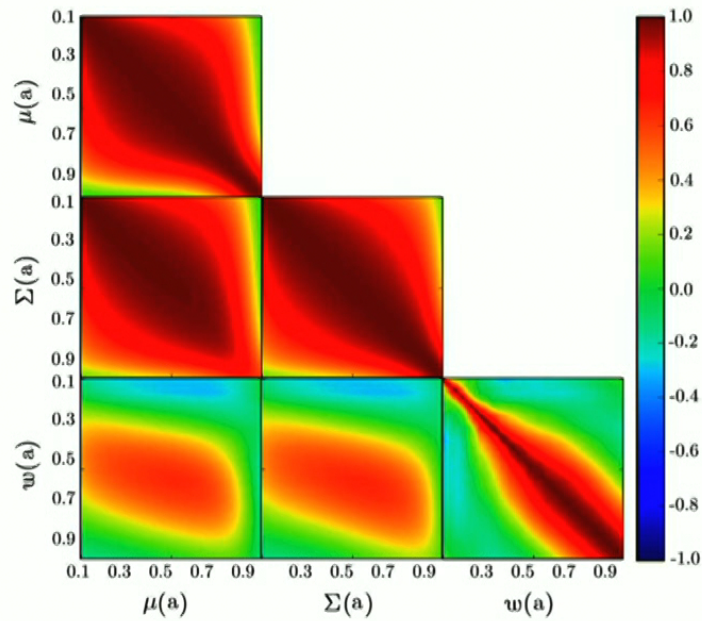
- Generate an ensemble of EFT functions
  - Parameterize the EFT functions as Pade polynomials (9<sup>th</sup> order)
  - Sample the coefficients, filter out unphysical solutions
- Filter out models with
  - unacceptable background expansion histories
  - unacceptable gravitational wave speed
  - unacceptable variations of the Newton's constant

J. Espejo, S. Peirone, M. Raveri, LP, A. Silvestri, K. Koyama, arXiv:1809.01121

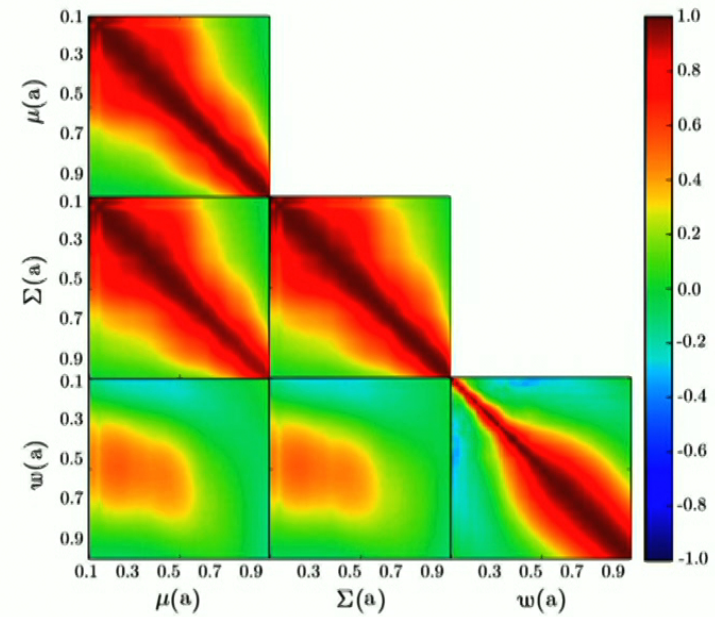


## Prior Correlations (theories with $c_T=1$ )

GBD

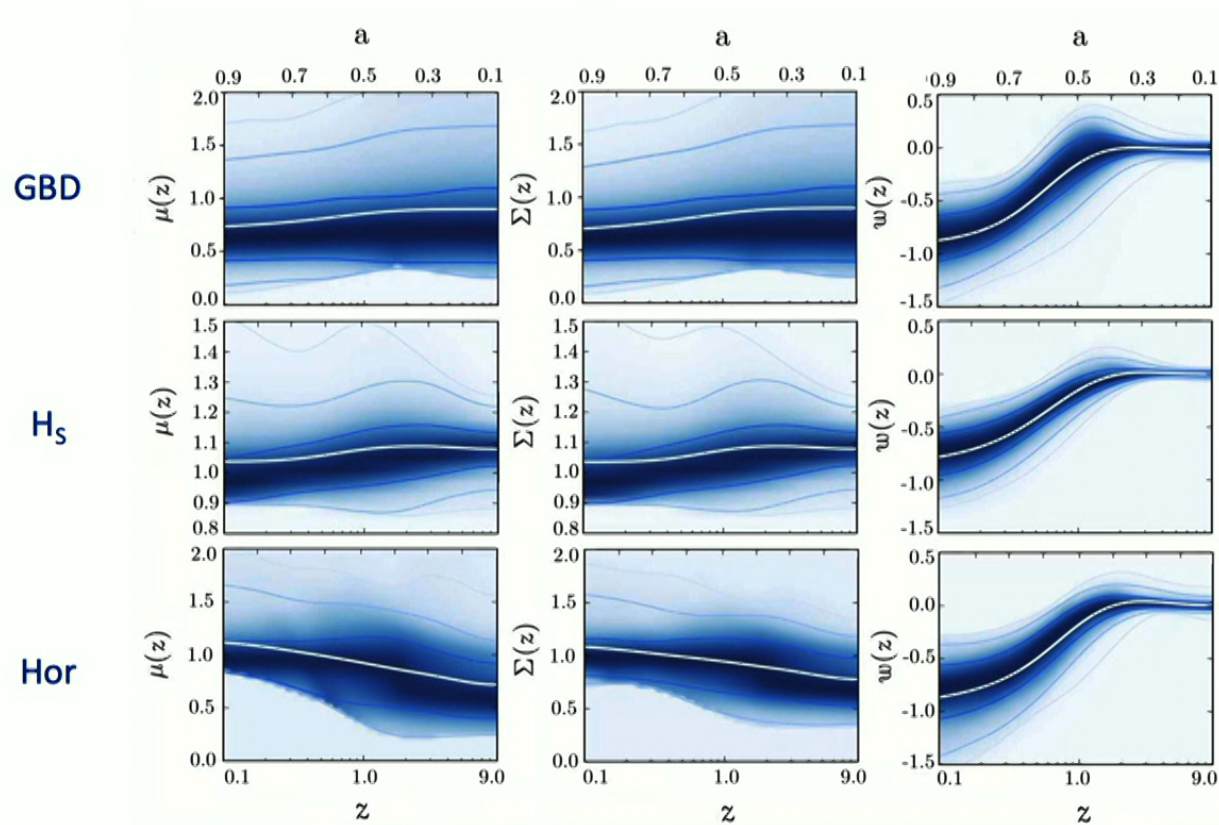


$H_S$



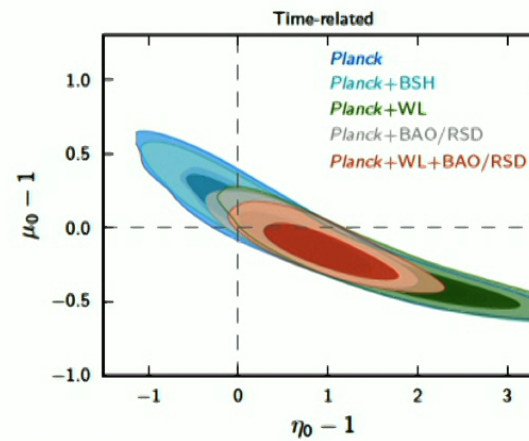
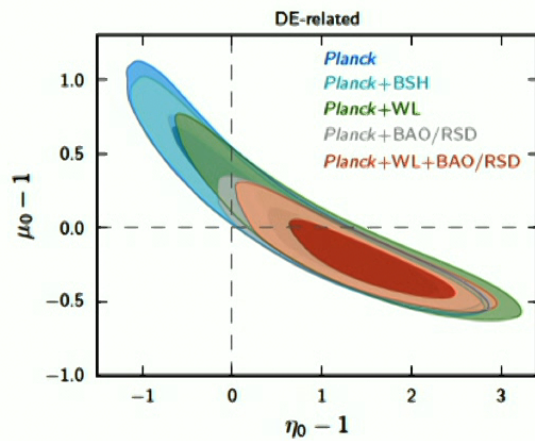
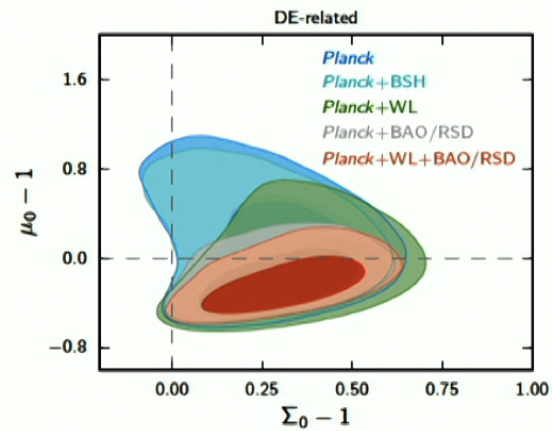
J. Espejo, S. Peirone, M. Raveri, LP, A. Silvestri, K. Koyama, arXiv:1809.01121

## Prior mean and the variance



J. Espejo, S. Peirone, M. Raveri, LP, A. Silvestri, K. Koyama, arXiv:1809.01121

## Planck 2015 results. XIV. Dark energy and modified gravity





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## Beyond probing the expansion history

