

Title: A non-minimal perspective on the misalignment mechanism

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Series: Particle Physics

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Abstract: Non minimal couplings of scalar fields to gravity are a generic feature of Lagrangian formulations of gravity. Although challenging to probe at low energies and small curvature, such couplings can play a crucial role in cosmological setups. We focus on their impact in the production of scalar dark matter and its interplay with inflationary physics. We show how the standard non-thermal production mechanism of scalar dark matter, the misalignment mechanism, is modified, and explore how alternative scenarios like production from inflationary fluctuations become viable. We study potentially observable features of these scenarios, such as the enhancement of dark matter substructure at small scales and the generation of an isocurvature component in the fluctuations of the CMB.

05.09.836

→ Non-thermal production of DM

→ Axions / ALPs - misalignment

→ Gravitational interactions

$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2} M_p^2 R + \mathcal{L}_\phi \right) \rightarrow G_{\mu\nu} = \frac{1}{M_p^2} T_{\mu\nu}$$

→ Axions / ALPs - misalignment
↳ Gravitational interactions

$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2} M_p^2 R + \mathcal{L}_\phi \right) \rightarrow G_{\mu\nu} = \frac{1}{M_p^2} T_{\mu\nu}$$

BUT:

- EFT of gravity: R^2 , $R_{\mu\nu} R^{\mu\nu}$, $\phi^2 R$, $R^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$.

A non-minimal perspective on the misalignment mechanism

Gonzalo Alonso-Alvarez 1807.09785
w/ T. Hugel & J. Jaeckel 1905.09836

OUTLINE

- * Introduction & motivation
- * Light (coherent) ...

→ Gravitational interactions

$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2} M_p^2 R + \mathcal{L}_\phi \right) \rightarrow G_{\mu\nu} = \frac{1}{M_p^2} T_{\mu\nu}$$

BUT:

- EFT of gravity: $R^2, R_{\mu\nu} R^{\mu\nu}, \phi^2 R, R^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$
- Quantisation in classical curved background
- QG: Asymptotic safety, ...

OUTLINE

- * Introduction & motivation
- * Light (coherent) DM
- * Non-minimal couplings
- * Non-thermal production
 - Misalignment
 - Fluctuations
 - Stochastic
- * Observables
- * Summary & outlook

$S =$
BUT
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OUTLINE

- * Introduction & motivation
- * Light (coherent) DM
- * Non-minimal couplings
- * Non-thermal production

IVATION

ence for DM $\rightarrow$ gravitational

weakly interacting

Non-thermal production of DM

$\rightarrow$ Axions / ALPs - misalignment

Gravitational interactions

$$\mathcal{G} \left(\frac{1}{2} M_P^2 R + \mathcal{L}_\phi \right) \rightarrow G_{\mu\nu} = \frac{1}{M_P^2} T_{\mu\nu}$$

T of gravity: $R^2, R_{\mu\nu} R^{\mu\nu}, \phi^2 R, R^{\mu\nu} \nabla_\mu \phi \nabla_\nu \phi$

* LIGHT DM

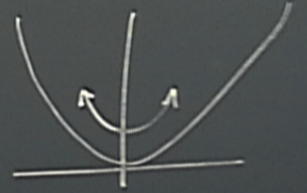
Very light bosons $\rightarrow$ high occupation #

$\rightarrow$ Classical fields

Classical EOM:

$$\text{Scalar: } \ddot{\phi} + 3H\dot{\phi} + m_\phi^2 \phi = 0$$

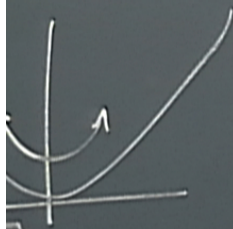
$$\text{Vector: } \ddot{\chi}_i + 3H\dot{\chi}_i + m_\chi^2 \chi_i = 0$$



$$\chi_i = \frac{x_i}{a}$$

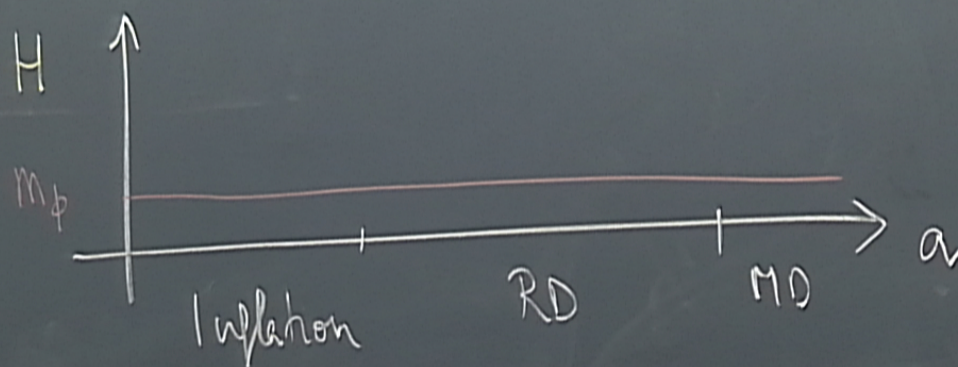
$$\Rightarrow \rho_\phi, \rho_\chi \propto a^{-3} \Rightarrow \text{Very CDM}$$

pation #



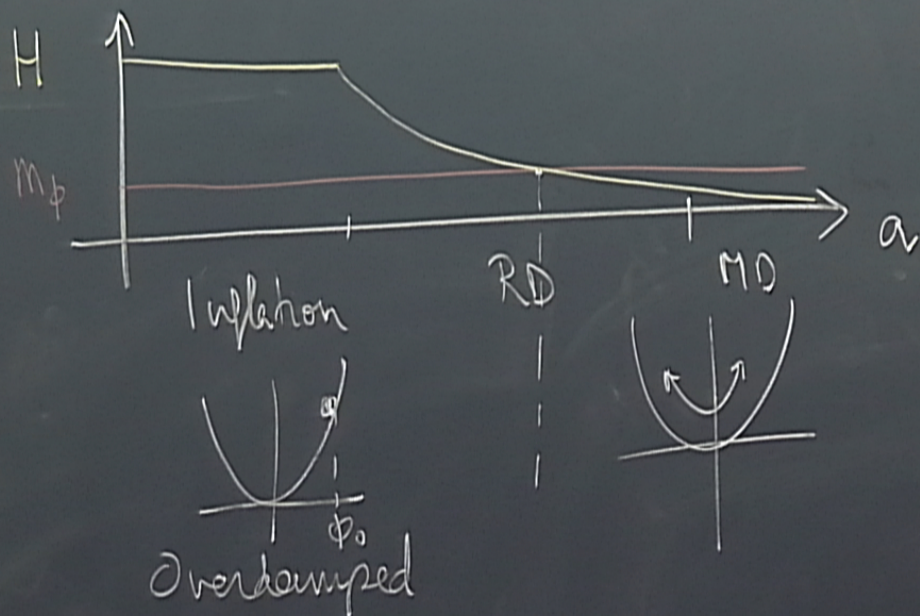
$$x_i = \frac{x_i}{a}$$

Misalignment mechanism



Misalignment mechanism

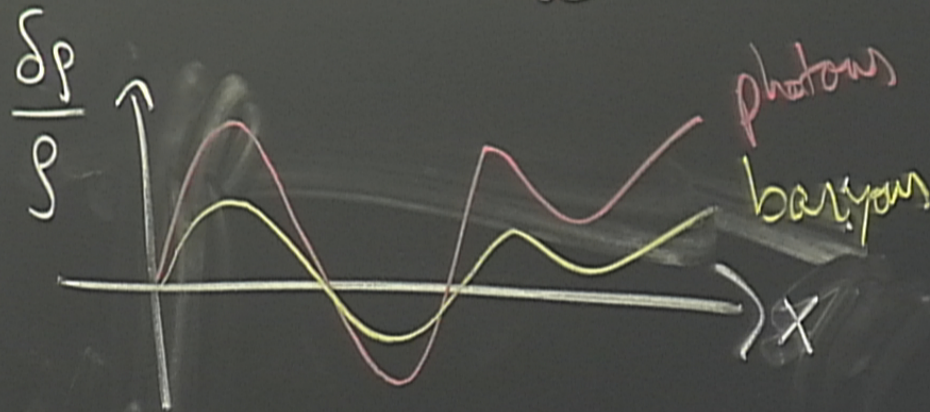
Fluctuations



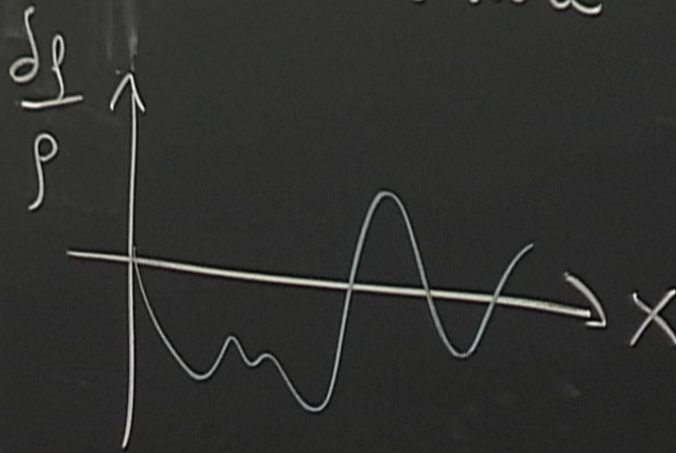
$$\frac{\Omega_\phi}{\Omega_{CDM}} \sim \left(\frac{\phi_0}{10^{16} \text{ GeV}} \right)^2 \sqrt{\frac{m}{1 \text{ eV}}}$$

Fluctuations

→ Adiabatic



→ Isocurvature



Planck

$$\Rightarrow \frac{\delta p^2_{\text{iso}}}{\delta p^2_{\text{adh}}} \lesssim 3\% @$$

$$K_{\text{cmb}}^{-1} \sim 20 \text{ Mpc}$$

nt mechanism

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* NON-MINIMAL COUPLINGS

$$S_{\phi} = \int d^4x \sqrt{-g} \left[\frac{1}{2} (M_{Pl}^2 - \xi \phi^2) R - \frac{1}{2} (\partial_{\mu} \phi)^2 - \frac{1}{2} m_{\phi}^2 \phi^2 \right]$$

$$S_X = \int d^4x \sqrt{-g} \left[\frac{1}{2} (M_{Pl}^2 + \frac{\kappa}{6} X_{\mu} X^{\mu}) R - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{1}{2} m_X^2 X_{\mu} X^{\mu} \right]$$

→ GI?

$$(\mathcal{D}_{\mu} \Phi)^2 + V(\Phi, R)$$

$\Phi \in \mathbb{R}$

vec $\langle \phi \rangle \propto R$

* LIGHT

Very light

→ Class

Classical

Scalar:

Vector:

⇒ f

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$$S_X = \int d^4x \sqrt{-g} \left[\frac{1}{2} (M_p^2 + \frac{K}{6} X_\mu X^\mu) R - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{1}{2} m_X^2 X_\mu X^\mu \right]$$

$\rightarrow G I?$

$$(\mathcal{D}_\mu \Phi)^2 + V(\Phi, R)$$

$\Phi^2 R$
 Φ

Vec $\langle \Phi \rangle \propto R$
 $\Phi \rightarrow \langle \Phi \rangle + \tilde{\Phi}$

$R(T_{\mu\nu})$

Very light
 $\rightarrow$ Class

Classical

Scalar:

Vector:

$\Rightarrow f_\phi, f_\psi$

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→ GI? → Ghost instability?

$$(\mathcal{D}_\mu \Phi)^2 + V(\Phi, R)$$

vev $\langle \phi \rangle \propto R$

$$\Phi \rightarrow \langle \phi \rangle + \tilde{\phi}$$

$$\frac{\partial^2 R}{\partial \tilde{\phi}^2}$$

$$\tilde{g}_{\mu\nu} = \Omega^2 g_{\mu\nu}$$

$$R(T_{\mu\nu})$$

$$\Omega^2 = \left(1 - \frac{3\phi^2}{M_p^2} \right)$$

$$\left| \frac{\delta \phi}{M_p} \right| \ll 1$$

$$\Rightarrow m_{\phi}^2 = m_p^2 + \xi R$$

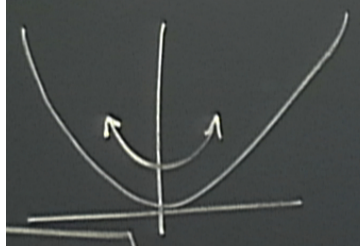
Classical

Scalar:

Vector:

$$\Rightarrow f_{\phi}, f_{\psi}$$

oscillation #

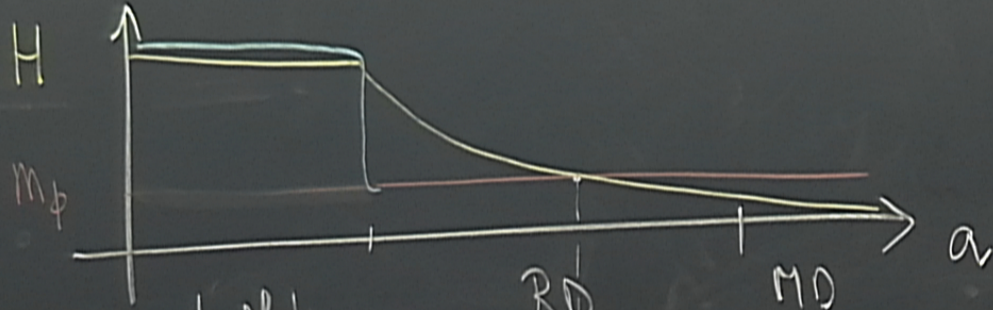


$$\phi = 0$$

$$\dot{\phi} = 0$$

$$\chi_i = \frac{x_i}{a}$$

DM

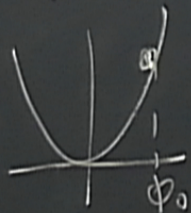


Inflation



Slow-roll

$$\phi_e \sim \phi_0 e^{-\frac{2\pi}{f} N}$$

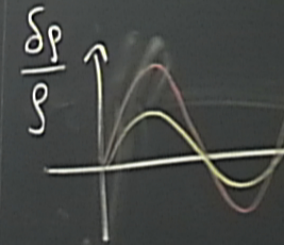


Overdamped

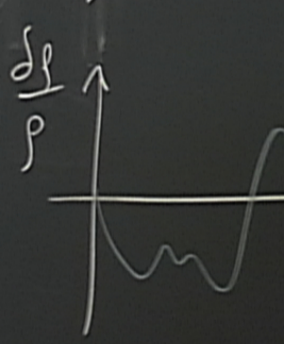


$$\frac{\Omega_\phi}{\Omega_{CDM}} \sim \left(\frac{\phi_0}{10^{16} \text{ GeV}} \right)^2 \sqrt{\frac{m}{1 \text{ eV}}}$$

→ Adiab



→ Iso



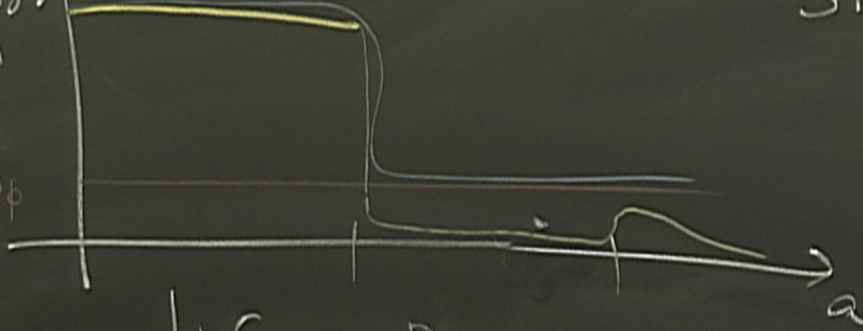
Planck

$$\Rightarrow \frac{\delta \rho^2}{\rho^2} \sim$$

m_{eff}

$S=1$

m_p



inf

$w=-1$

RD

$w=1/3$

Mn, Ad

$w=0$

$$m_{eff}^2 = m_p^2 + \mathcal{E}R$$

$\mathcal{E}R$

$$R = 3(1-3w)H^2$$

$$H_{eq} \sim 10^{-28} \text{ eV}$$

Classical

Scalar:

Vector:

$$\Rightarrow f_\phi, f_\psi$$

DM:

$$(\Box + m_a^2)\phi = 0$$

$$\Box \chi_i + m_{\chi_i}^2 \chi_i = 0$$

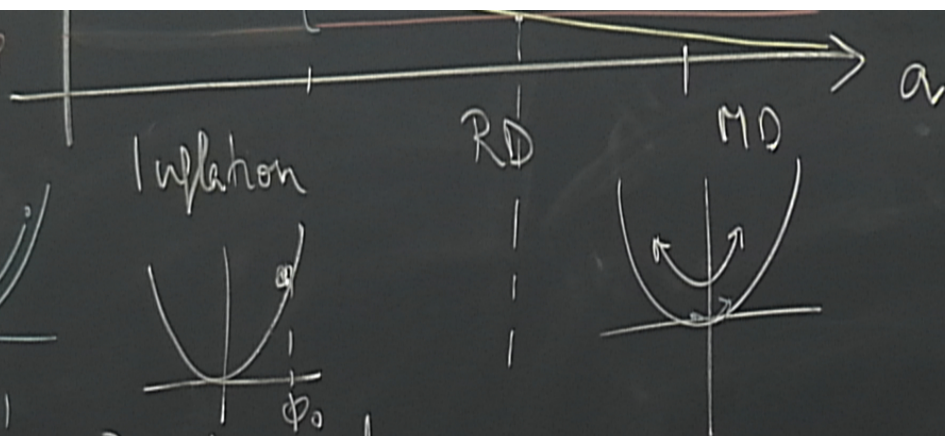
$\Rightarrow$ Very CDM

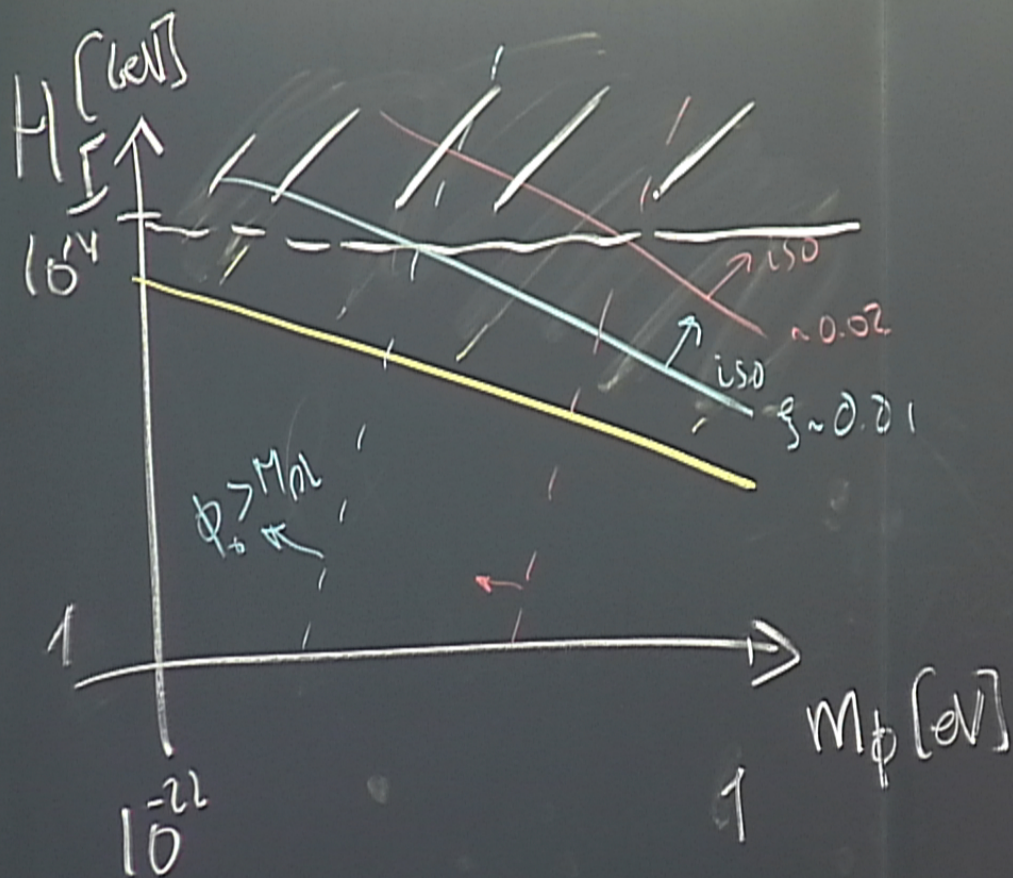
$$\chi_i = \frac{x_i}{a}$$

Slow-roll
 $\phi_e \sim \phi_0 e^{-\frac{2}{3}N}$

Overdamped

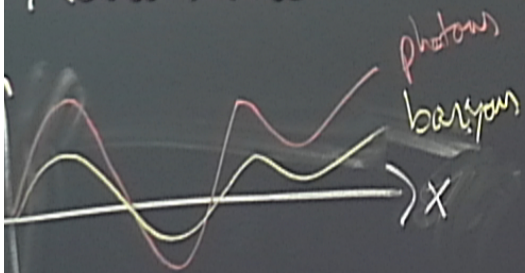
$$\frac{\Omega_\phi}{\Omega_{\text{CDM}}} \sim \left(\frac{\phi_0 e^{\frac{2}{3}N}}{10^{16} \text{ GeV}} \right)^2 \sqrt{\frac{m}{1 \text{ eV}}}$$



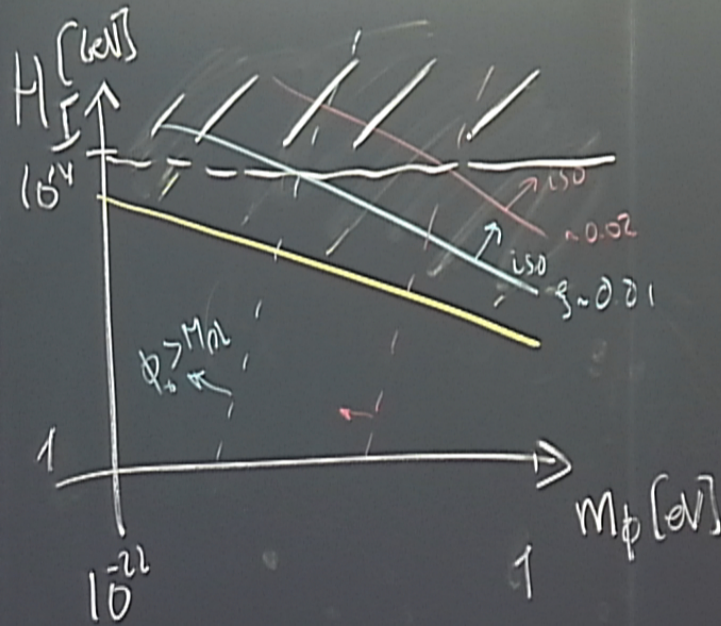
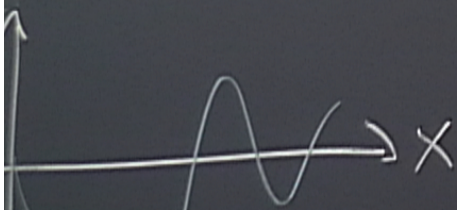


Instructions

Adiabatic



Signature



$$N \in N_{\min} \sim 60$$

$$R = \frac{1}{4} \dot{X}_m \dot{X}_m - \frac{1}{2} m^2 X_m X_m$$

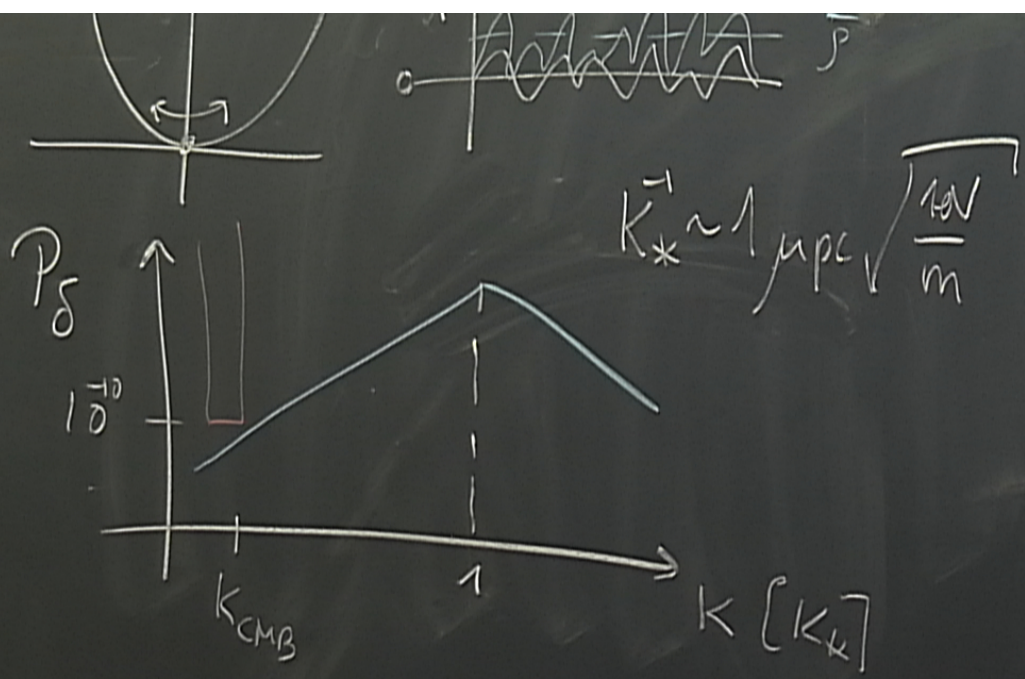
SR

$$R = 3(1-3w)H^2$$

$$\rightarrow a \quad H_{eq} \sim 10^{-28} \text{ eV}$$

$\rho, \Lambda D$

$U=0$



- large $H_I \approx 10^{14}$ GeV
- large $m \gtrsim 1$ eV
- $\xi \sim \mathcal{O}(10^{-2})$

Slow-roll

$$\phi_e \sim \phi_0 e^{-\xi N}$$

Over

$$\frac{\Omega_\phi}{\Omega_{DM}} \sim$$

x^4

SR

$$R = 3(1-3w)H^2$$

$$H_{eq} \sim 10^{-28} \text{ eV}$$

M_D, Λ_D

$$w = 1/3 \quad w = 0$$

$$\ddot{\phi}_k + 3H\dot{\phi}_k + \frac{k^2}{a^2}\phi_k = 0$$

$$\phi_k \propto \frac{1}{a}$$

P_δ

10^{-10}

k_{CMB}

1

$k [k_k]$

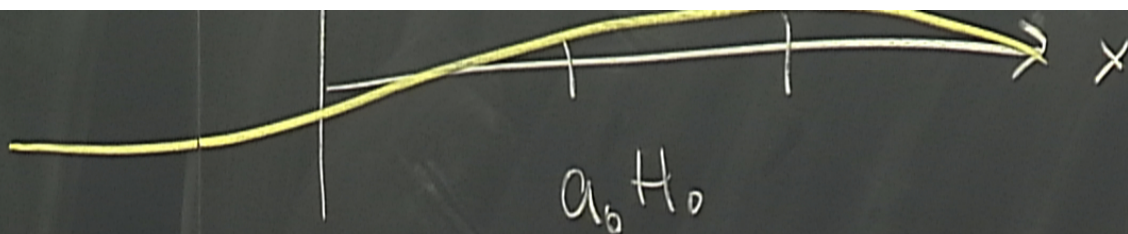
$$K_*^{-1} \sim 1 \mu pc \sqrt{\frac{10V}{m}}$$

$$t_l = m$$

$$ka > m$$

- large $H_I \approx 10^{14} \text{ GeV}$
- large $m \gtrsim 1 \text{ eV}$
- $\xi \sim \mathcal{O}(10^{-2})$

$$n_{iso} = 1 + \delta \xi$$



$$\sigma^2 \sim \int \frac{d^3 k}{(2\pi)^3} \sigma_k^2$$

$a_I H_I$

$\langle \phi^2 \rangle$ $\langle \phi_k^2 \rangle$

$$\begin{array}{c}
 a_0 H_0 \\
 \sigma^2 \sim \int \frac{d^3 k}{(2\pi)^3} \sigma_k^2 \sim \left(\frac{H_I^2}{m} \right)^2 \sim \frac{H_I^2}{\epsilon} \\
 \langle \phi^2 \rangle \quad a_I H_I \quad \langle \phi_k^2 \rangle
 \end{array}$$

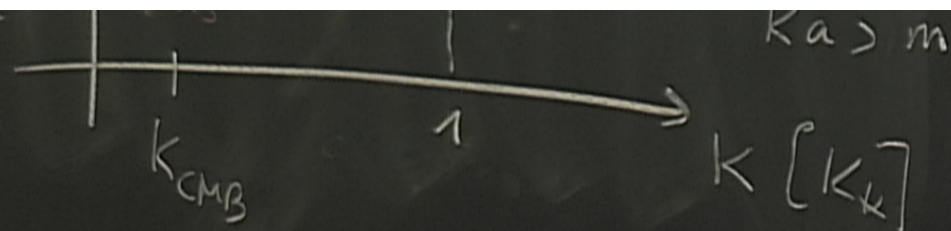
$$\Rightarrow \frac{\sigma^2}{\sigma_k^2} \sim \frac{H_I^2/\epsilon}{H_I^2} \sim 1/\epsilon$$

$$\sigma^2 \sim \frac{1}{(2H)^3} \quad \sigma_K^2 \sim \left(\frac{m}{\sqrt{\frac{2}{3}} H_I} \right)^2$$

$$\langle \Phi^2 \rangle \sim a_I H_I$$

$$\Rightarrow \frac{\sigma^2}{\sigma_K^2} \sim \frac{H_I^2 / 3}{H_I^2} \sim \frac{1}{3}$$

$$\rightarrow P_{150} \sim \frac{\sigma_{K_{MB}}^2}{\sigma^2} \sim \xi < 10^{-10}$$



- large $H_I \approx 10^{14}$ GeV $\eta_{150} = 1 + \delta \xi$
- large $m \gtrsim 1$ eV
- $\xi \sim \mathcal{O}(10^{-2})$

$$\phi_k = 0$$

$$\ell \sim \frac{k_*^{-1}}{E_g} \sim 10^4 \text{ km} \sqrt{\frac{\alpha}{\eta}}$$

$$M \sim 10^{-25} M_\odot \left(\frac{\alpha}{\eta} \right)^{3/2}$$

$$\Rightarrow \frac{1}{\sigma_k^2} \sim \frac{1}{H^2}$$

$$\rightarrow P_{150} \sim \frac{\sigma_{k_{\text{CMB}}}^2}{\sigma^2}$$

CMB

- large $H_I \approx 10^{14}$ GeV
- large $m \gtrsim 1$ eV
- $g \sim 6(10^{-2})$

$$n_{iso} = 1 + 8\epsilon$$

$$+\frac{k^2}{q^2}\phi_k=0$$

$$n = \frac{\rho}{M} \sim \frac{0.3 \text{ GeV/cm}^3}{10^{32} \text{ GeV}}$$

$$n_{\sigma\nu} \sim 10^{-33} / \text{cm}^3$$

$$l \sim \frac{k_*^{-1}}{\bar{\epsilon}_g} \sim 10^4 \text{ km} \sqrt{\frac{\sigma}{m}}$$

$$M \sim 10^{-25} M_\odot \left(\frac{\sigma}{m}\right)^{3/2}$$

& motivation
 (ent) DM
 l couplings
 oduction
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 ous
 & outlook

$$m_p \left(\frac{\mathcal{L} \phi^2}{M_p^2} \right)$$

$$\sim \mathcal{L} \frac{\rho}{m^2 M_p^2}$$

