

Title: Gravitational waves in the inhomogeneous Universe

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Collection: Cosmological Frontiers in Fundamental Physics 2019

Date: September 03, 2019 - 2:00 PM

URL: <http://pirsa.org/19090019>

Abstract: The discovery of gravitational waves from a binary black hole merger in 2015 opened up a new window to study the Universe, including the origin of black holes, the nature of dark matter, and the expansion history of the Universe. However, gravitational waves emitted from binary mergers propagate through the inhomogeneous Universe, which can have a considerable impact on observations of gravitational waves, in good or bad ways. I will highlight some examples of the effects of the inhomogeneity on gravitational wave observations, including their possible applications and implications.

Gravitational waves in the inhomogeneous Universe

Masamune Oguri

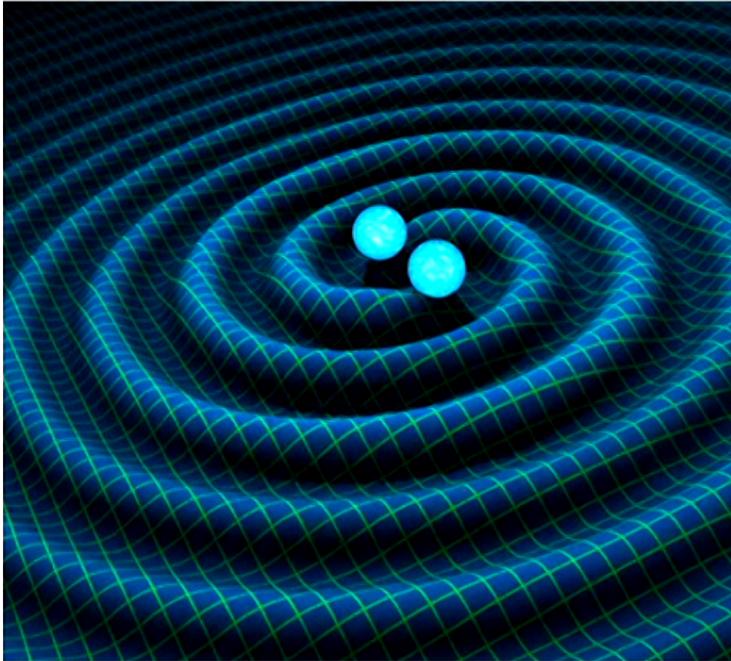
RESCEU/Physics/Kavli IPMU
University of Tokyo

2019/9/3 Cosmological Frontiers in Fundamental Physics@Perimeter

Plan of this talk

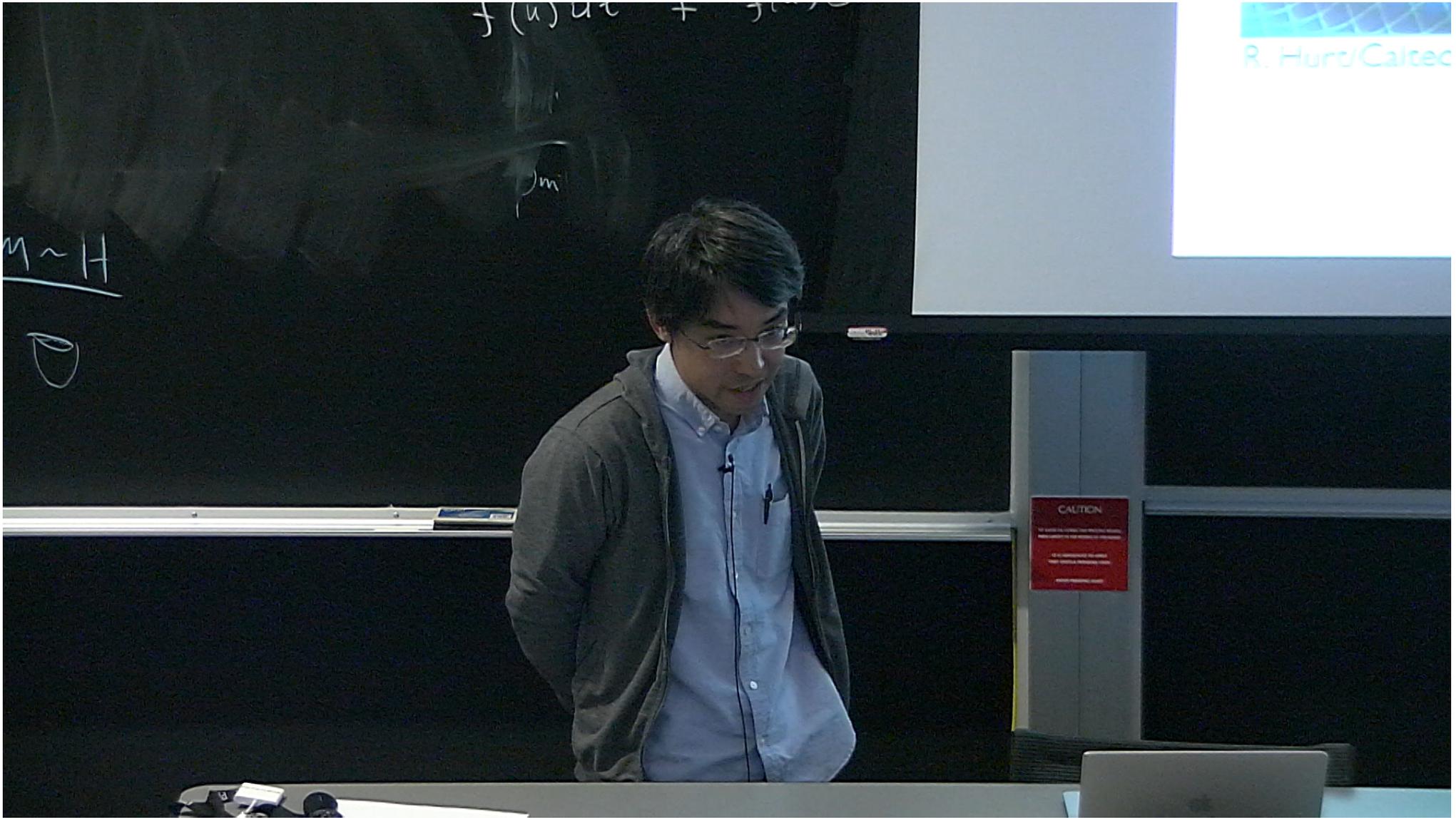
- standard siren without redshift info with cross-correlation approach
[[MO Phys. Rev. D 93\(2016\)083511](#)]
- effect of gravitational lensing on the distribution of binary black hole mergers
[[MO MNRAS 480\(2018\)3842](#)]

Gravitational waves (GW)



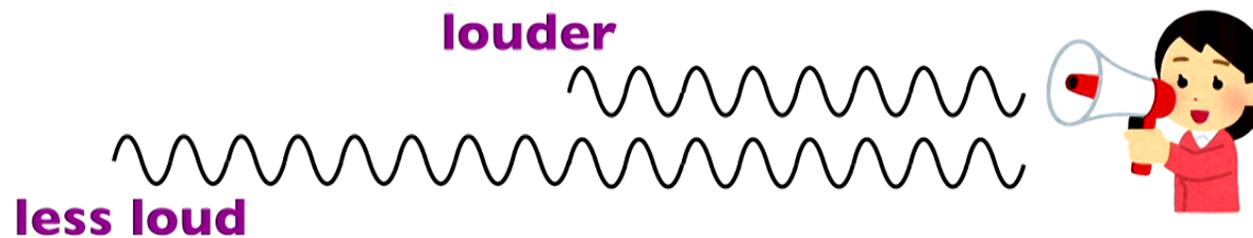
R. Hurt/Caltech-JPL/EPA

- observed for the first time in 2015
- mergers of compact binaries such as black hole (BH) and neutron star (NS)
- **very useful probe of cosmology and astrophysics!**

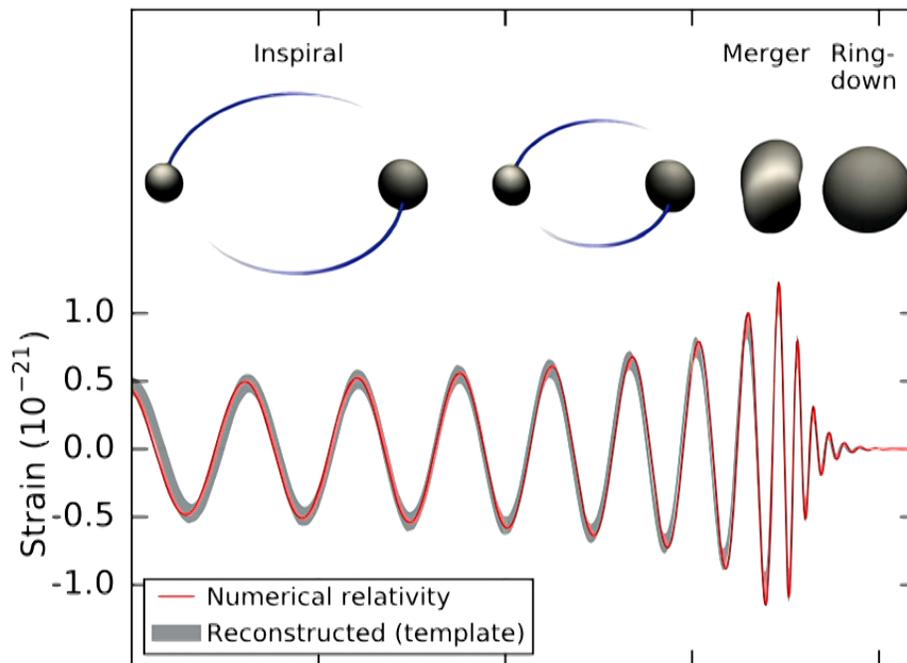


Gravitational wave standard sirens

- we can infer mass (\rightarrow GW amplitude) of inspiraling compact binary from the waveform
- by comparing with observed amplitude, we can measure **luminosity distance** (incl. H_0) directly (Schutz 1986)



Abbott+2016



Inspiral

$$h \propto \frac{M_z^{5/3}}{D_L(z)} f^{2/3}$$

$$\dot{f} \propto M_z^{5/3} f^{11/3}$$

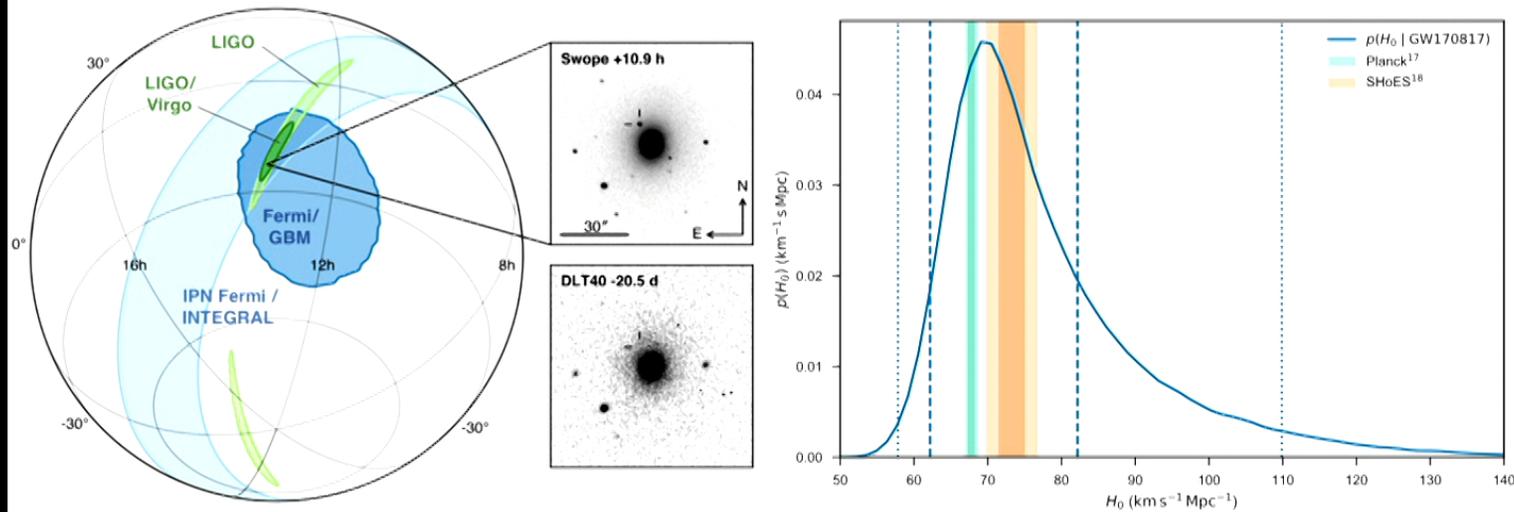
→ **chirp mass M_z**
and **distance D_L**

analytic (post-Newtonian) numerical relativity analytic (QNM)

Redshift information

- standard siren can constrain H_0 and other cosmological parameters *if* the **redshift** is known
- usually detection of **EM counterpart** and/or **host galaxy** is needed for the redshift
- this is challenging because of the poor localization accuracy (currently $>10-100 \text{ deg}^2$)

GW170817 (NS-NS merger)



- GRB and kilonova detected, host galaxy identified
- first constraint on H_0 from gravitational waves

Future?

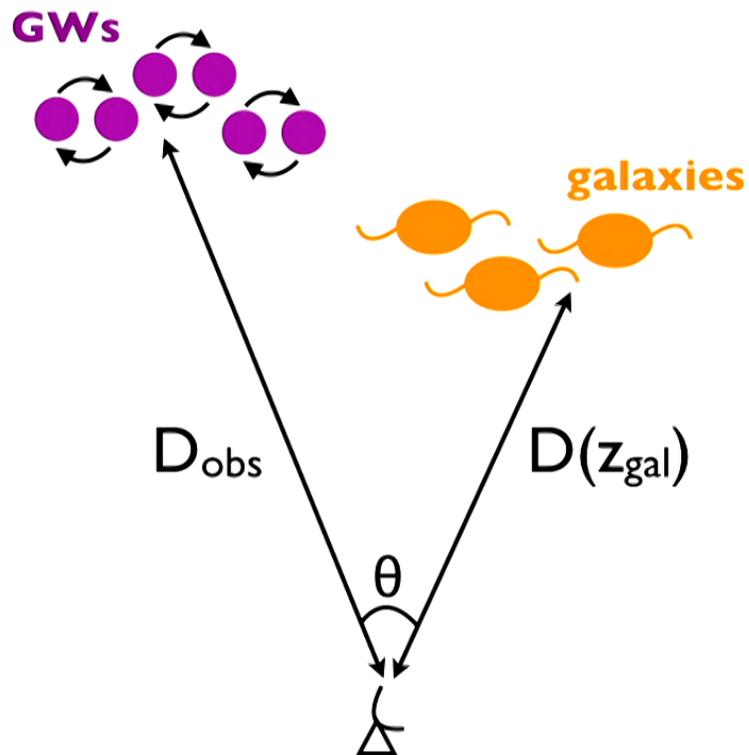
- kilonova is faint (~ 24 mag @ 400 Mpc)
- short GRB observed only on-axis
(e.g., Dalal+2006, Nissanke+2010)
- what about BH-BH mergers?

standard siren without redshift?

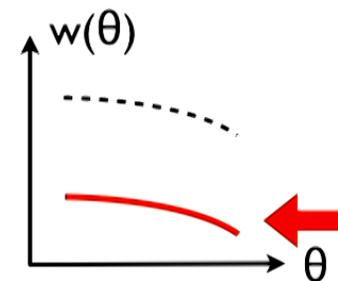
Cross-correlation approach

- **idea**: constrain distance-redshift relation with **cross-correlation** of GW sources (**known D_L**) and galaxies (**known z**)
- similar to “clustering redshift” (e.g., Newman 2008)
- no follow-up of GW sources needed

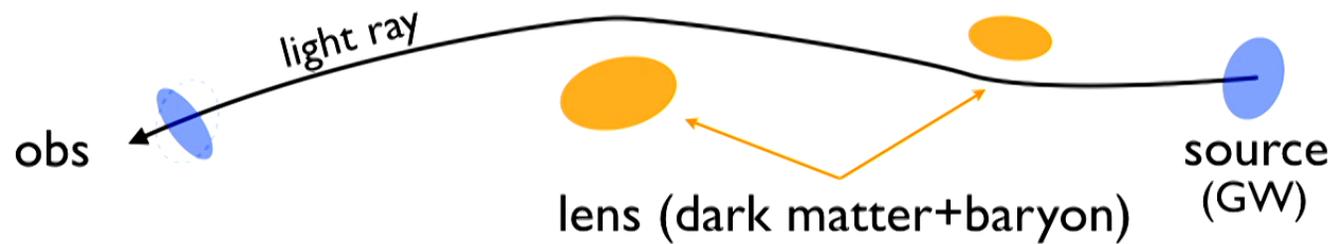
Cross-correlation approach



- cross-correlation of spatial distributions
- $$w(\theta) = \langle \delta_{\text{GW}}(\vec{\theta}') \delta_{\text{gal}}(\vec{\theta}' + \vec{\theta}) \rangle$$
- when $\mathbf{D}_{\text{obs}} > \mathbf{D}(\mathbf{z}_{\text{gal}})$ cross-correlation is **small**



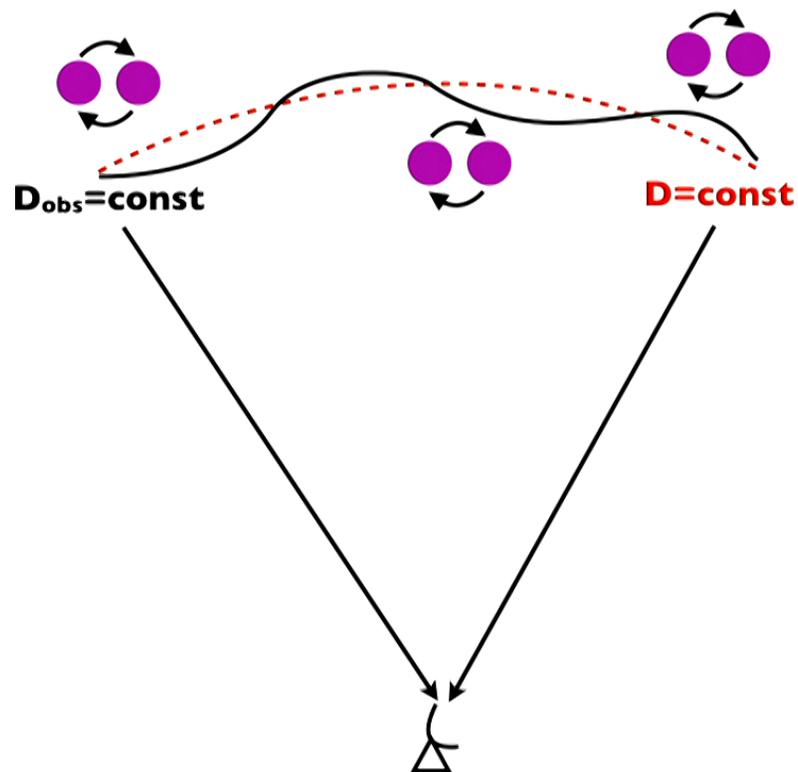
Gravitational lensing as noise



- gravitational lensing magnification μ **changes the observed luminosity distance**

$$D_{\text{obs}} = \bar{D} \mu^{-1/2} \approx \bar{D} \left[1 - \kappa(\vec{\theta}, z) \right]$$

Apparent clustering due to lensing



- lensing depends on sky position
- induces additional clustering pattern on the sky

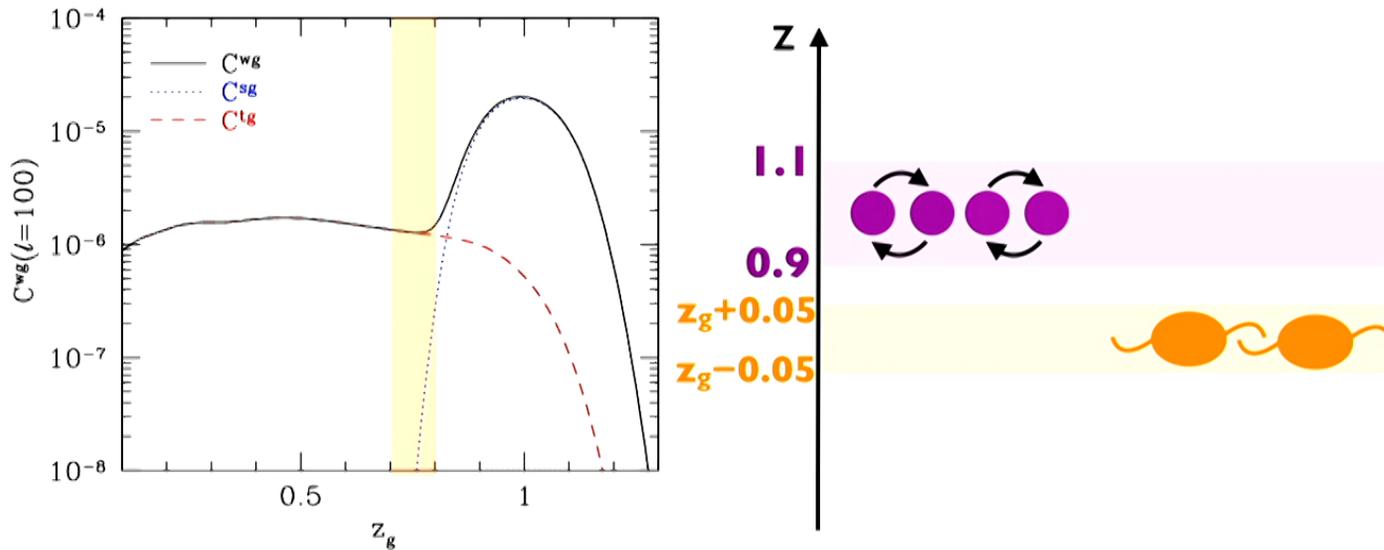
Cross-correlation signals

$$\overline{C^{w_i g_j}(\ell)} = C^{s_i g_j}(\ell) + C^{t_i g_j}(\ell)$$

$$\underline{C^{s_i g_j}(\ell)} = \int_0^\infty dz W_i^s(z) W_j^g(z) \frac{H(z)}{\chi^2} b_{\text{GW}} b_g P_m \left(\frac{\ell + 1/2}{\chi}; z \right) \quad \text{physical spatial correlation}$$

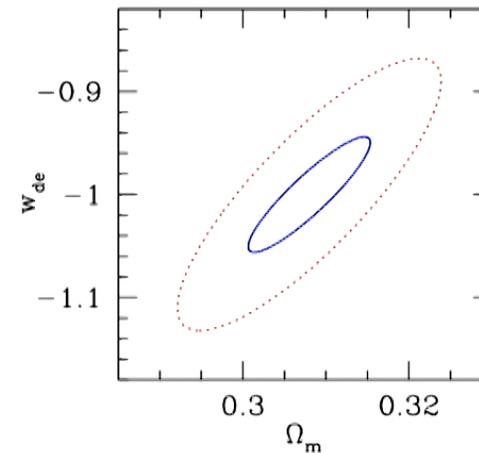
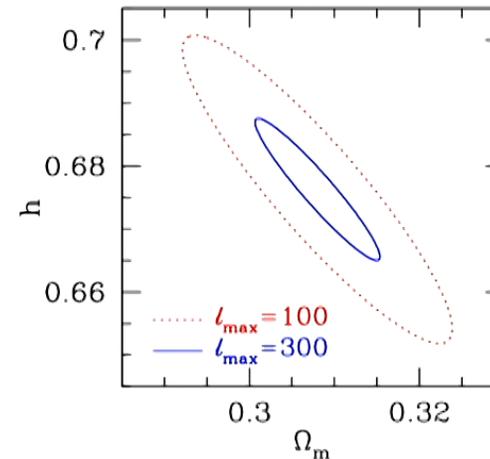
$$\underline{C^{t_i g_j}(\ell)} = \int_0^\infty dz W_i^t(z) \int_0^z dz' W_j^g(z') W^\kappa(z'; z) \frac{H(z')}{\chi'^2} b_g P_m \left(\frac{\ell + 1/2}{\chi'}; z' \right)$$

apparent clustering due to weak lensing



Forecast

- GWs from 3rd-generation exp. + galaxies from Euclid ($0.3 < z < 1.5$)
- l_{\max} is related with accuracy of GW localizations
- **tight constraints on H_0 and w possible with the cross-correlation!**

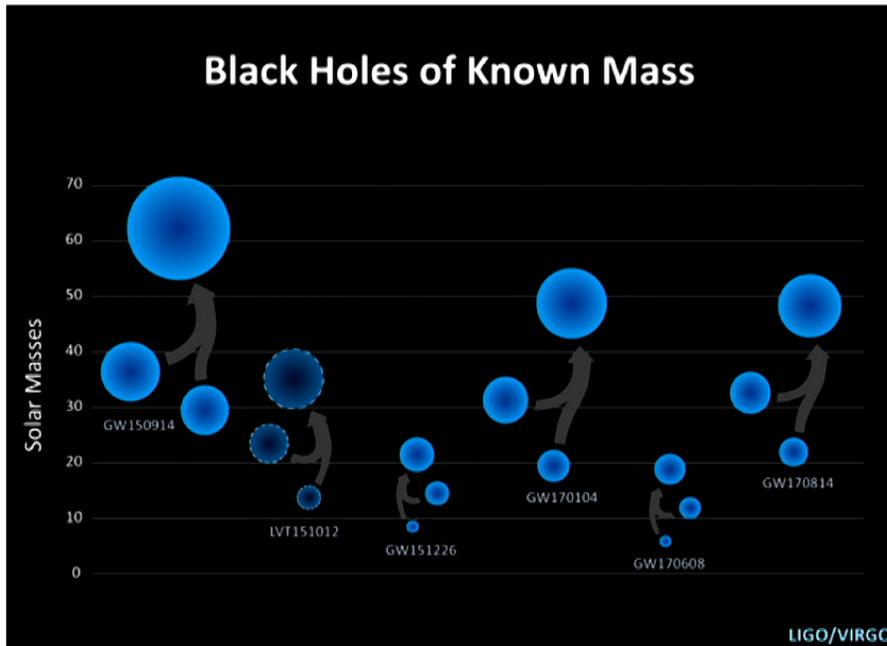


Cross-correlation: Summary

- **proposed cross-correlation of GW sources and galaxies with known z** to constrain H_0 and other cosmological parameters
- standard siren cosmology without redshift and even at high- z
- other applications of cross-correlation?
 - infer progenitor from bias (e.g., Raccanelli+2016)
 - 3D clustering in distance space (e.g., Zhang 2018)

a lot of room to explore!

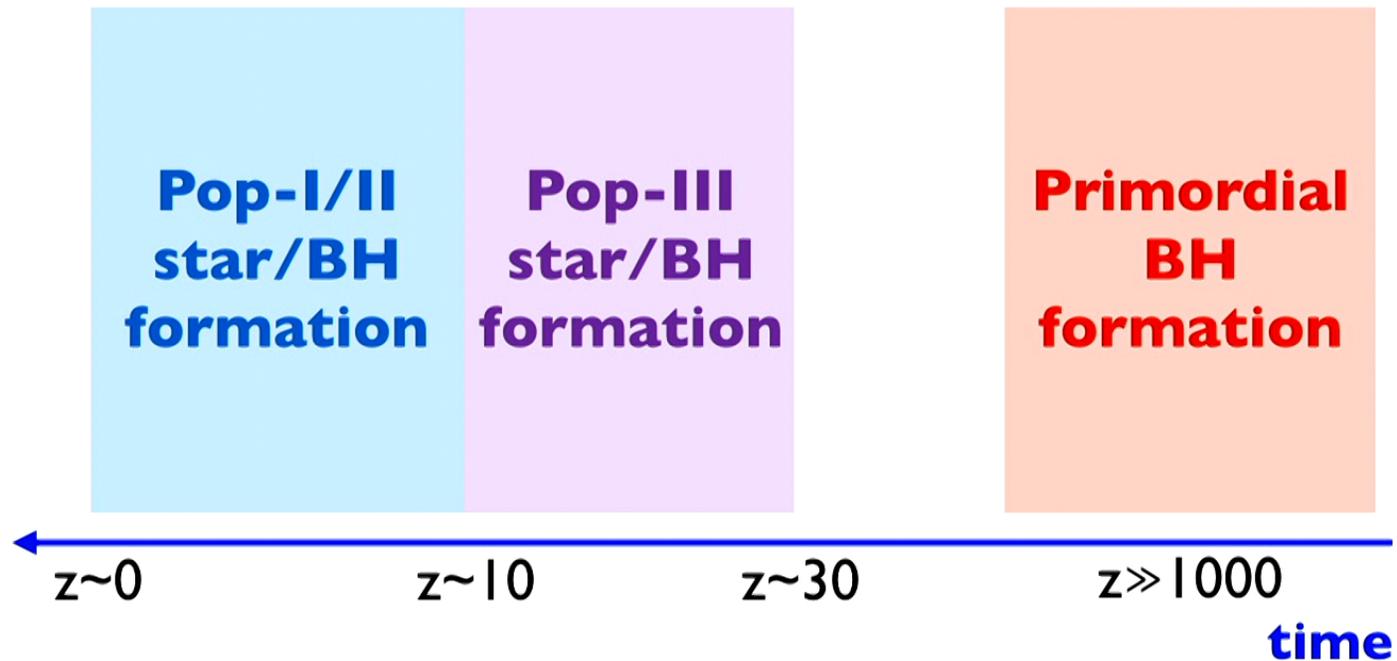
Origin of binary BHs?



<https://www.ligo.caltech.edu>

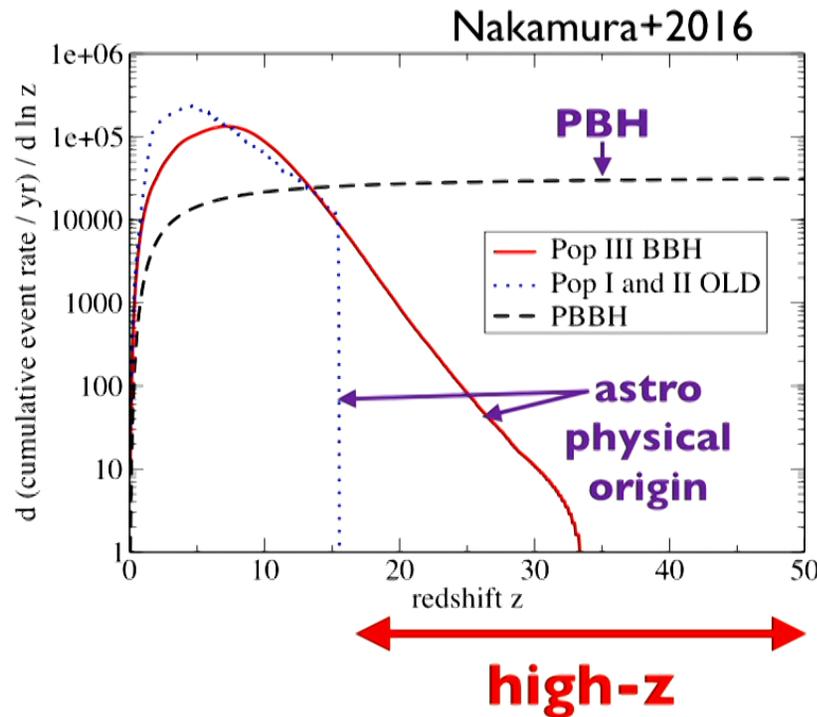
- ~10-30 M_{\odot} BHs discovered by LIGO/VIRGO
- their origin still unknown
 - **Pop-I/II?**
 - **Pop-III?**
 - **PBH?**

Models of BH formation



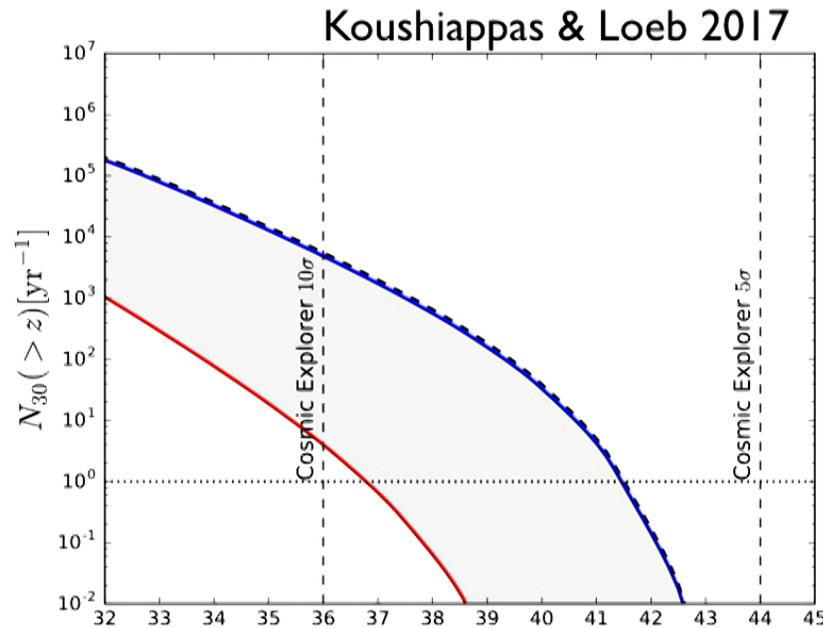
- GW observed at $z=0$ due to long **delay time**

Key observation: high-z events



- different scenarios predict different event rates at $z \gtrsim 15$
- accessible in 3rd-gen. experiments

Key observation: high-z events



- different scenarios predict different event rates at $z \gtrsim 15$
- accessible in 3rd-gen. experiments

**maximum $z \sim 40$
for astrophysical origin**

“High-z” events?

- from GW observations we do not directly measure their redshifts
- we measure **luminosity distance**, which is affected by gravitational lensing
- **lensing magnification μ** can bias redshift inferred from the luminosity distance, and also chirp mass

Observed redshift and mass

- “**observed redshift**” z_{obs} defined as

$$D_L(z_{\text{obs}}) = \frac{D_L(z)}{\sqrt{\mu}} \quad \mu: \text{magnification factor}$$

- “**observed chirp mass**” M_{obs} defined as

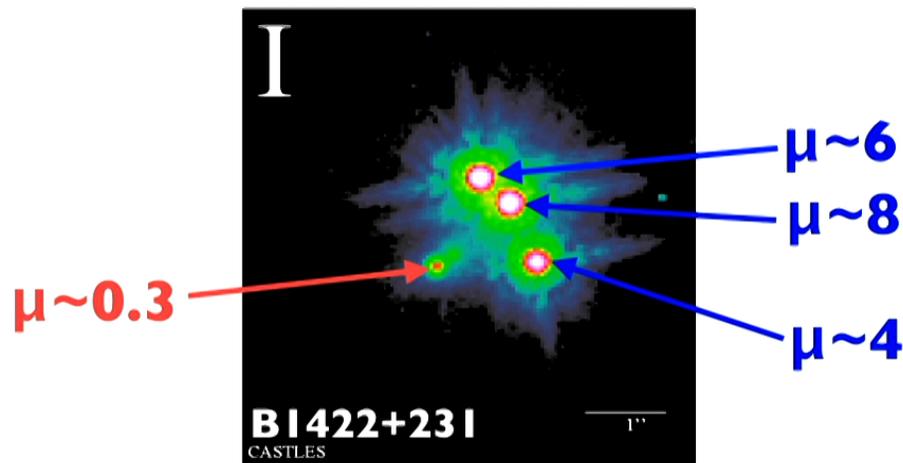
$$\mathcal{M}_{\text{obs}} = \frac{1+z}{1+z_{\text{obs}}} \mathcal{M}$$

Distributions with lensing effects

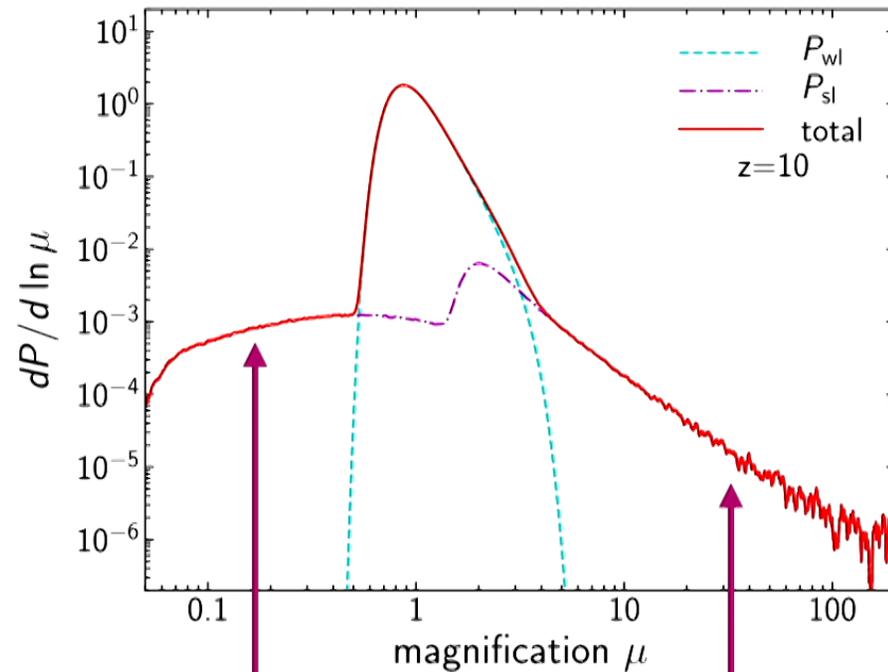
- redshift and mass dist. of binary BH mergers taking full account of gravitational lensing
- various scenarios: **Pop I/II, Pop-III, PBH**
- various experiments: **aLIGO, KAGRA, ET, CE, B-DECIGO**
- check how lensing (de-)magnification modify these distributions

Strong lensing of BH mergers

- difficult to identify multiple images given the poor localization on the sky
 - **treat multiple images as distinct events**
- some images **magnified** and some **demagnified**



Magnification PDF

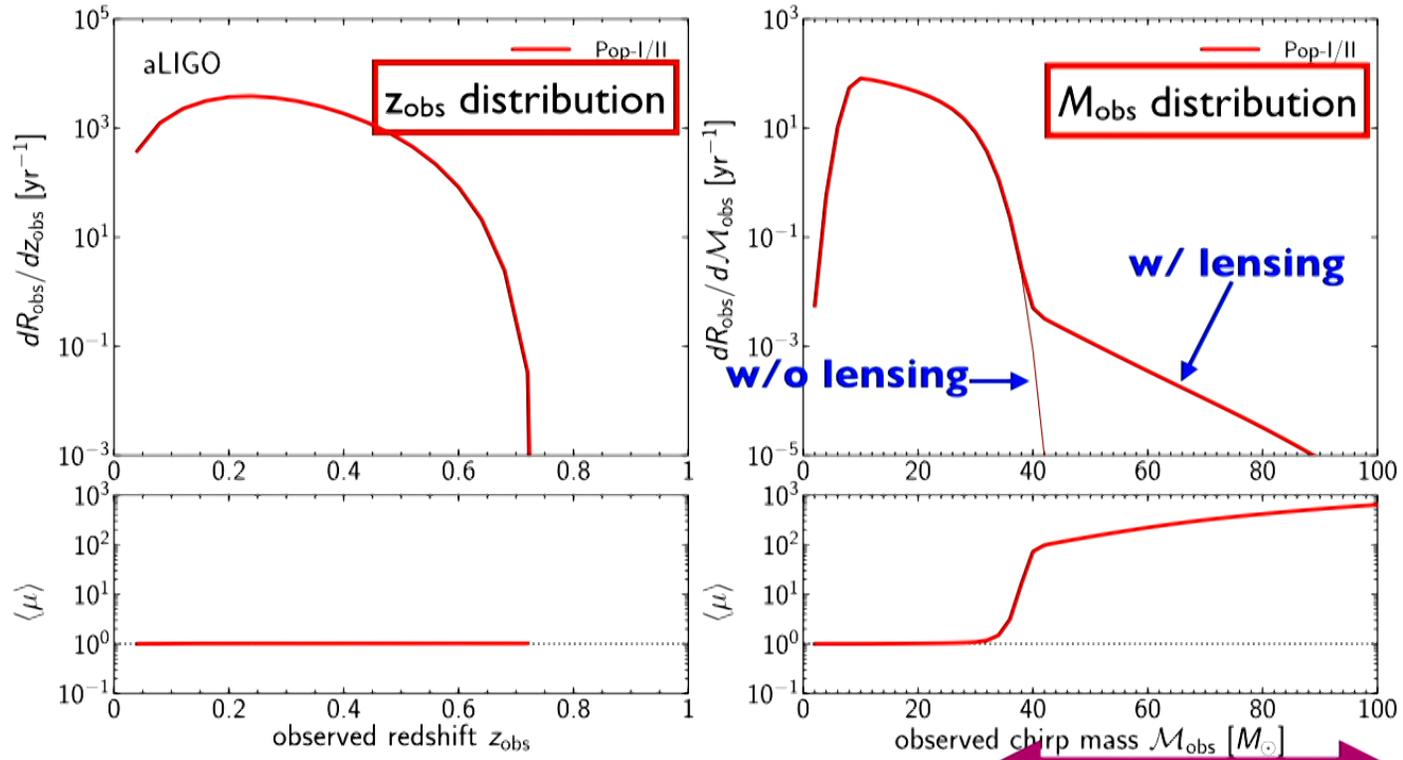


demagnified

magnified

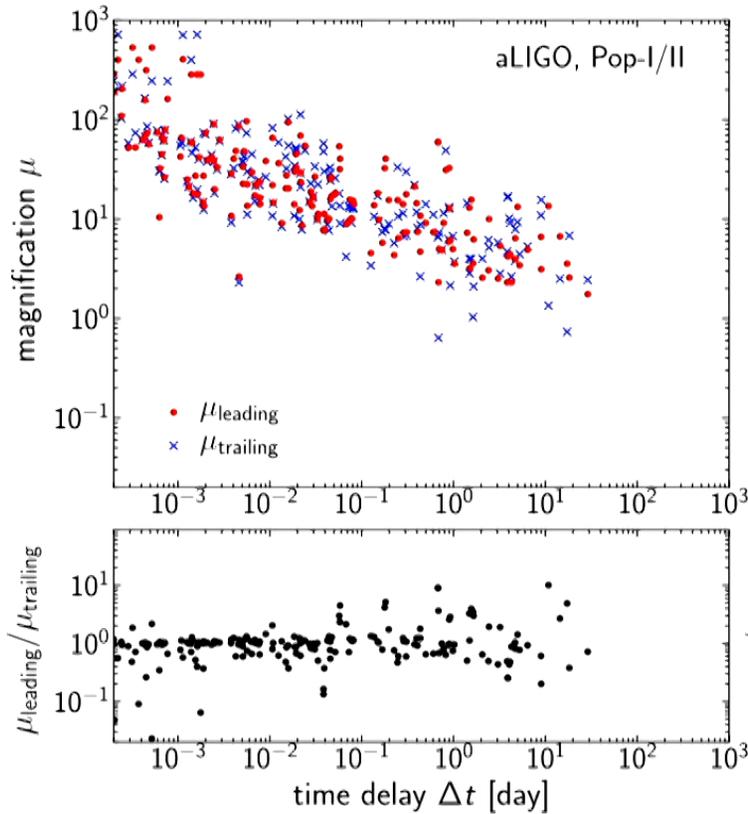
- **new hybrid model** combining weak+strong lens
- weak lens from analytic model, strong lens from Monte Carlo
- long tails at high and low μ

Result: advanced LIGO

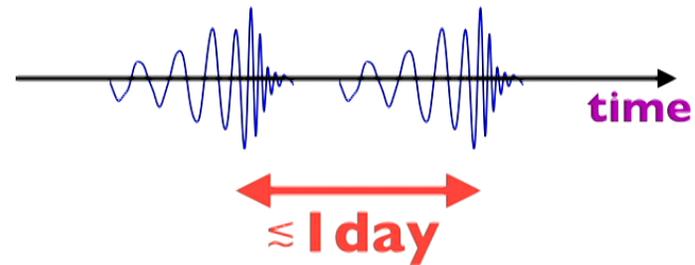


← excess due to magnified events (see also Dai+2017) →

Expected multiple image pairs

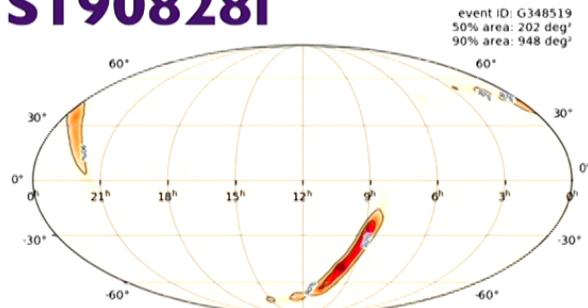


- **advanced LIGO**
 - time delay \approx **1 day**
 - high, similar μ
 - $R_{\text{obs}} < 1 \text{ yr}^{-1}$



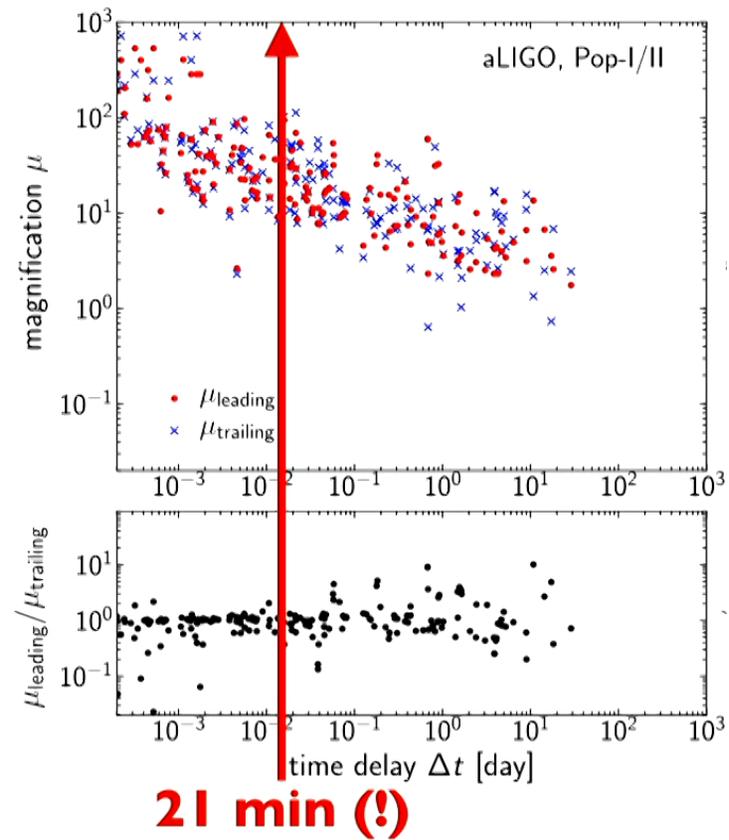
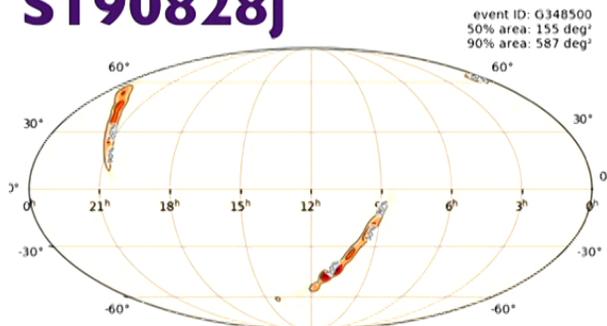
Gravitationally lensed GW??

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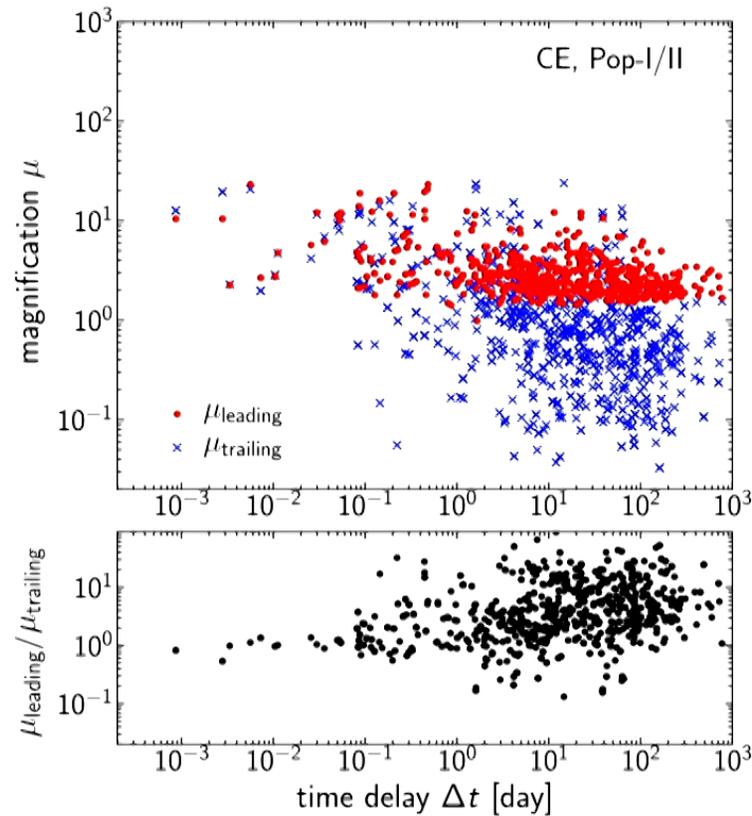


**separated
by 21 min**

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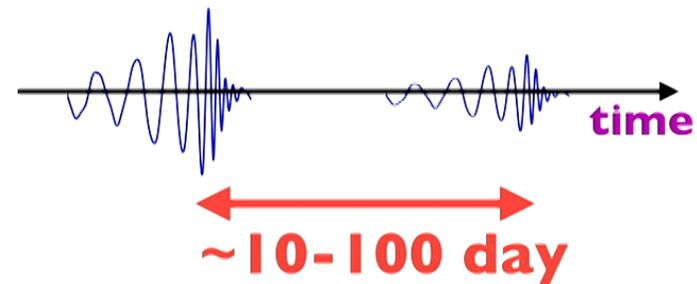


Expected multiple image pairs



- **Cosmic Explorer**

- time delay
 $\sim 10-100$ days
- different μ
- $R_{\text{obs}} \sim O(10^3) \text{ yr}^{-1}$



Binary BH distribution: Summary

- **pronounced lensing effect at high z_{obs} and M_{obs}**
- the discovery of apparently very high- z events does not necessarily support PBH scenario
- predictions on multiple image pairs
- see the paper for detailed results for different BH merger scenarios and GW experiments

Conclusion

- **interesting synergies** between **GW** and **large-scale structure/gravitational lensing**
 - spatial clustering of GW sources
 - observables affected by weak and strong gravitational lensing
- more work needed to fully exploit the potential of GW observations!