

Title: Precision Islands for ABJM theory from Mixed Correlator Bootstrap

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Collection: Bootstrap 2019

Date: July 19, 2019 - 11:30 AM

URL: <http://pirsa.org/19070060>

Bootstrapping M-theory

based on 1711.07343

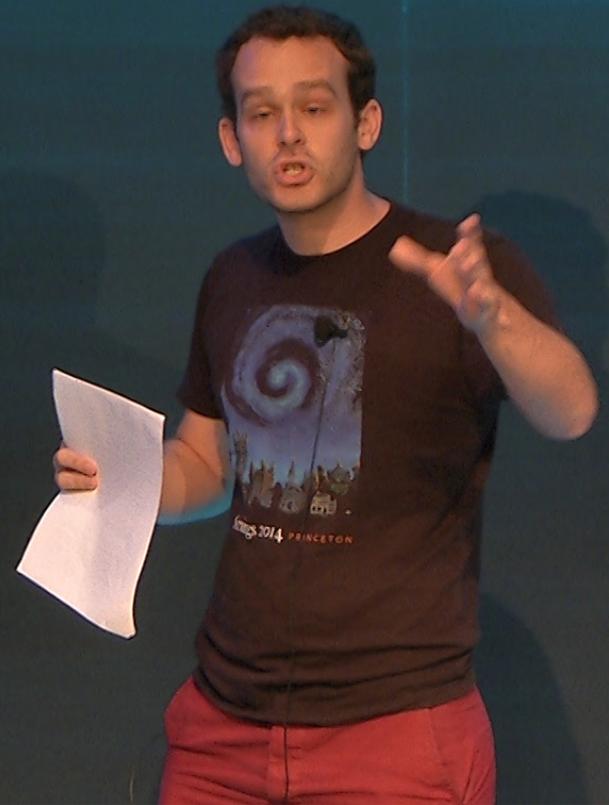
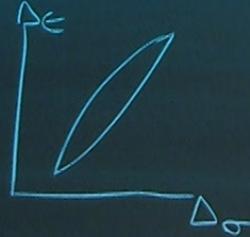
w/ Agmon Pufu

and TBA w/ " "

and old work w/ Lee, Pufu, Yacoby

1. $O(N)$, $N=1$ Ising
 $N=1$ Ising

Mixed correlators



Bootstrapping M-theory

based on 1711.07343

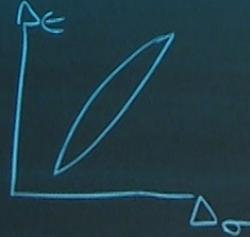
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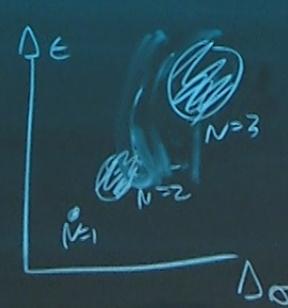
and old work w/ Lee, Pufu, Yacoby

1. $O(N)$, $N=1$ Ising
 $N=1$ Ising

Mixed correlators



$\Delta\sigma$
 $N=1: .004\%$
 $N=2: .12\%$
 $N=3: .24\%$

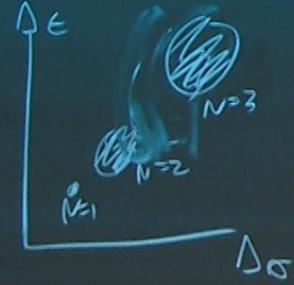
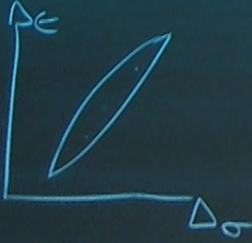


$$e\% = \frac{U-L}{(U+L)/2}$$



1. $O(N)$, $N=1$ Ising
 $N=1$ Ising

Mixed correlators



$\Delta\sigma$
 $N=1$: .004%
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$$e\% = \frac{U-L}{(U+L)/2}$$

2. Extremal Functions I

$$c_T \sim \frac{1}{\lambda_{\text{stress}}^2} \quad \text{min}$$

3d max susy CFTs $\mathcal{N}=8$



1. ABJM $U(N) \times U(N)_{-k}$ $k=1,2$

2. ABJ $U(N+1) \times U(N)_{-2}$

3. PLG $SU(2) \times SU(2)_{-k}$ $k=1,2,3,4$
 dual ABJM $k=N$

SYM $U(N) \rightarrow ABJM_N^1$
 $SU(2N) \rightarrow ABJM_N^2$
 $SU(2N+1) \rightarrow ABJ_N$

M-theory on $A/S_4 \times S^2/\mathbb{Z}_k$
 $\cong ABJM_N^k$

N coincident M2 branes

1. $SO(8)_R$

2. 1/2-BPS rank-9 Transverse sy

$U(N)_k$
 $U(N)_{-2}$
 $SU(2)_k$

1. $SO(8)_R$

2. $1/2$ -BPS rank- q Traceless sym $\Delta = \frac{q}{2}$

$q=1$: free

$q=2$: stress

$q=3$: ~~free~~ $k=2$ ABJM
 also PLG except $k=3$

$c_T \sim \frac{1}{\lambda_{\text{size}}^2}$

$\Rightarrow k=1$ ABJM when $N \geq 3$

$\langle 2222 \rangle$, $\langle 3333 \rangle$, $\langle 2233 \rangle$

ABJM: $c_T \sim N^{2/c} \sqrt{k}$

2 stable limits: free $c_T = 16$

2 GFT $N \rightarrow \infty$ ABJM: SUBRA
 $c_T \rightarrow \infty$



$k=9$ Traceless sym $\Delta = \frac{9}{2}$

$k=2$ ABJM
 also BLG except $k=3$
 $=1$ ABJM when $N \geq 3$

(2233)

$r=16$
 $\rightarrow \infty$ ABJM: SU(6)A
 $\rightarrow \infty$

$\mathcal{G} \in 2 \times 2$: Long $D \geq j+2$

consistent — $\left[\begin{array}{l} 1/8 - \text{bps } (A_{j+1}) \quad D = j+2 \text{ even } j \\ 1/16 - \text{bps } (A_{j+2}) \quad D = j+2 \text{ odd } j \end{array} \right.$

Short — $\left[\begin{array}{l} 1/4 - \text{bps } (b_{j+2}) \quad D=2 \quad \bar{j}=0 \\ 1/2 - \text{bps } (b_{j+1}) \quad D=2 \quad \bar{j}=0 \end{array} \right.$

st $D=1$
 Id

my

$N=3$

$N=2$

$\Delta\sigma$

L

$(L)/2$

$N=8$

$$\langle zzzz \rangle = \sum_M \chi_M^z G_M$$

$$G_M = \sum_{(D_2)_{\text{dim}}} A_{(D_2)_{\text{dim}}} g_{(D_2)_{\text{dim}}}$$

$N=8$ W or A = 1/2-RPS - $\mathcal{N} \ln$, Gubit - Sakitda $\} K$

$S(8) : 6$ (crossing equations m)

$(mk=2)$ $\xrightarrow{\text{susy}}$ \uparrow $(z \rightarrow \bar{z})$

\downarrow $(z, 0)$

1. 50

2. 1/2-RPS

$q=1$

$q=2$

$q=3$

$$c_T \sim \frac{1}{\chi_{\text{size}}^z}$$

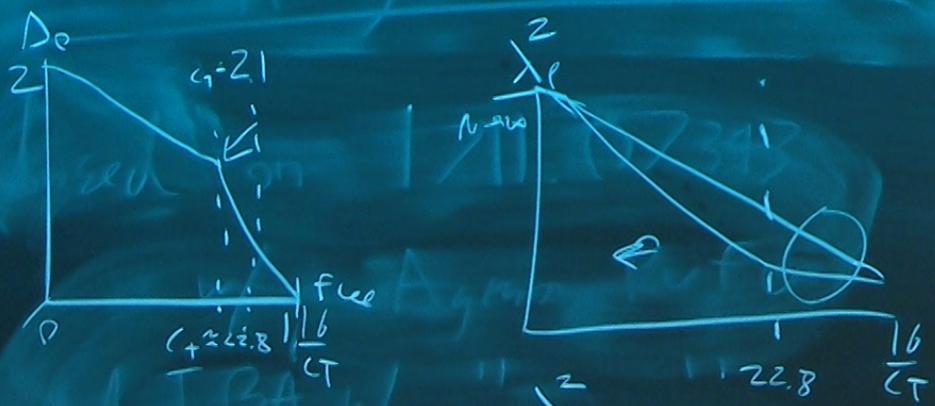
$\langle zzzz \rangle, \langle 3 \rangle$

ABJM: $c_T \sim N^3$

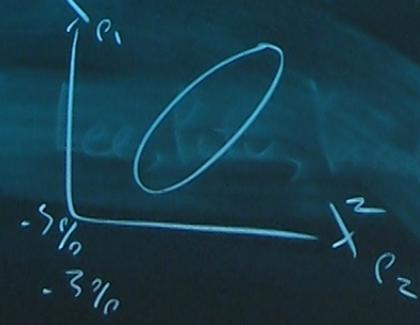
2 stable limits: J.F.M.

$z G$

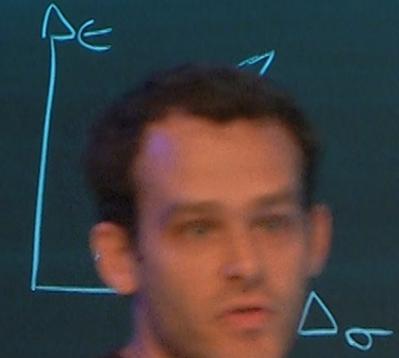
1. $O(N)$, $N=1$
 $N=2$



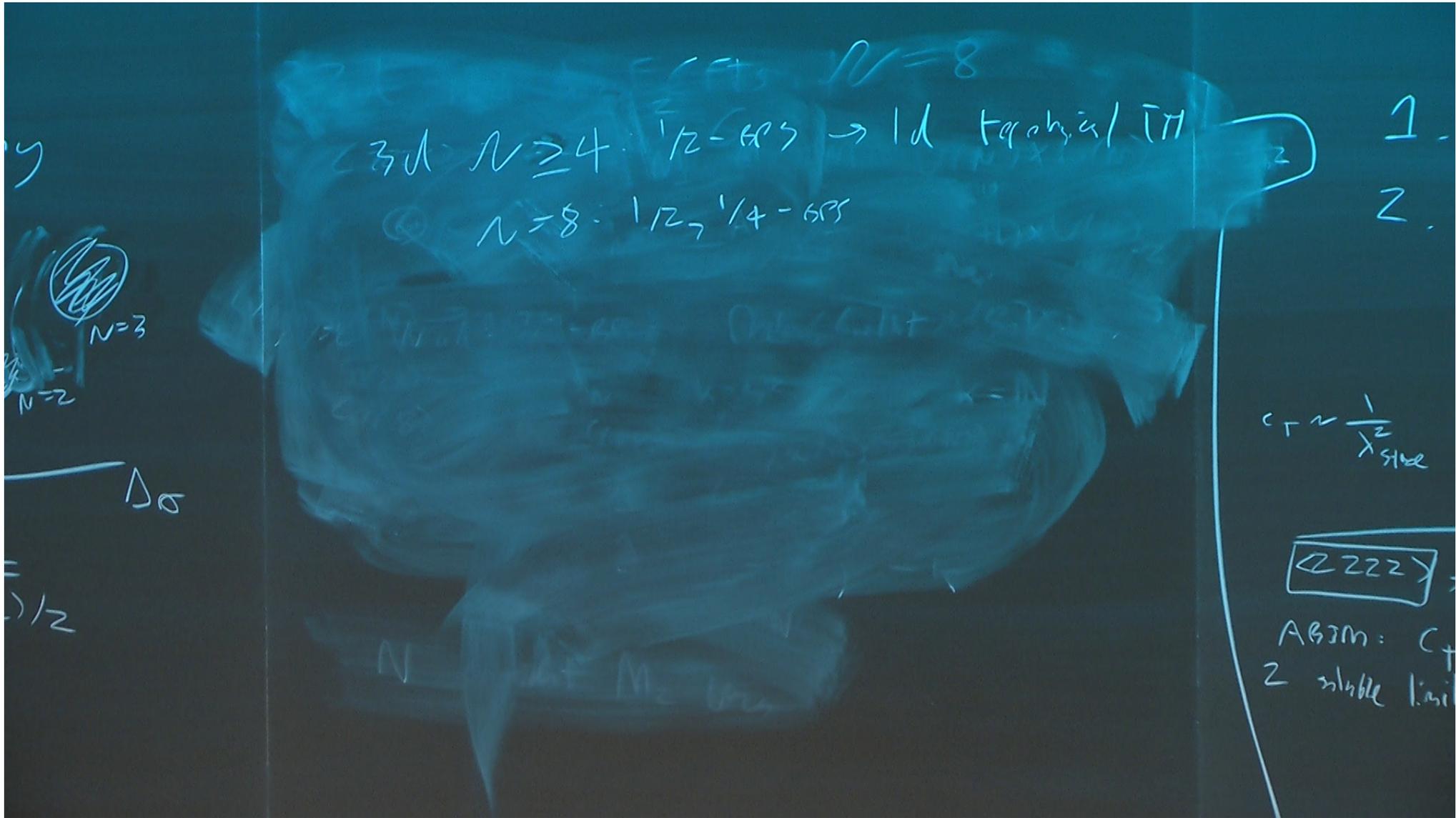
(A, x) $s_{p1} = 0$
 $s_{p2} = 2$
 $(x, 5)$



Mixed correlator



Δ_σ
 $N=1$
 $N=2$



3d $N \geq 4$ $1/2$ -6PS \rightarrow 1d topological TM
① $N = 8$ $1/2, 1/4$ -6PS

- 1.
- 2.

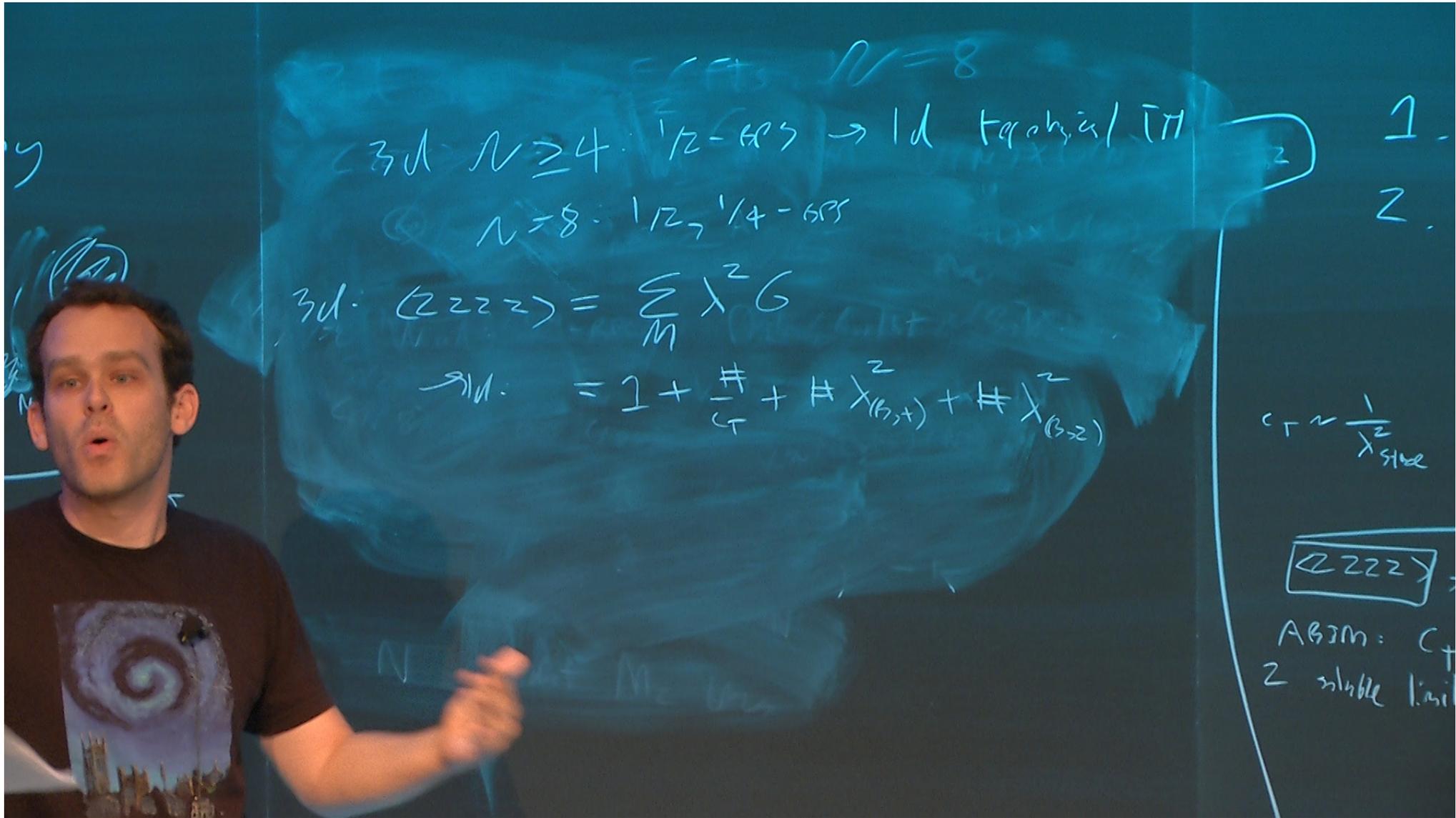
~~scribble~~
 $N=3$
 $N=2$

$\Delta\sigma$
 $1/2$

$$c_T \sim \frac{1}{2} \times X_{size}$$

$\langle 2222 \rangle$

ABJM: c_T
Z stable limit



3d: $N \geq 4$ 1/2-eps \rightarrow 1d topological TM

$N = 8$ 1/2, 1/4-eps

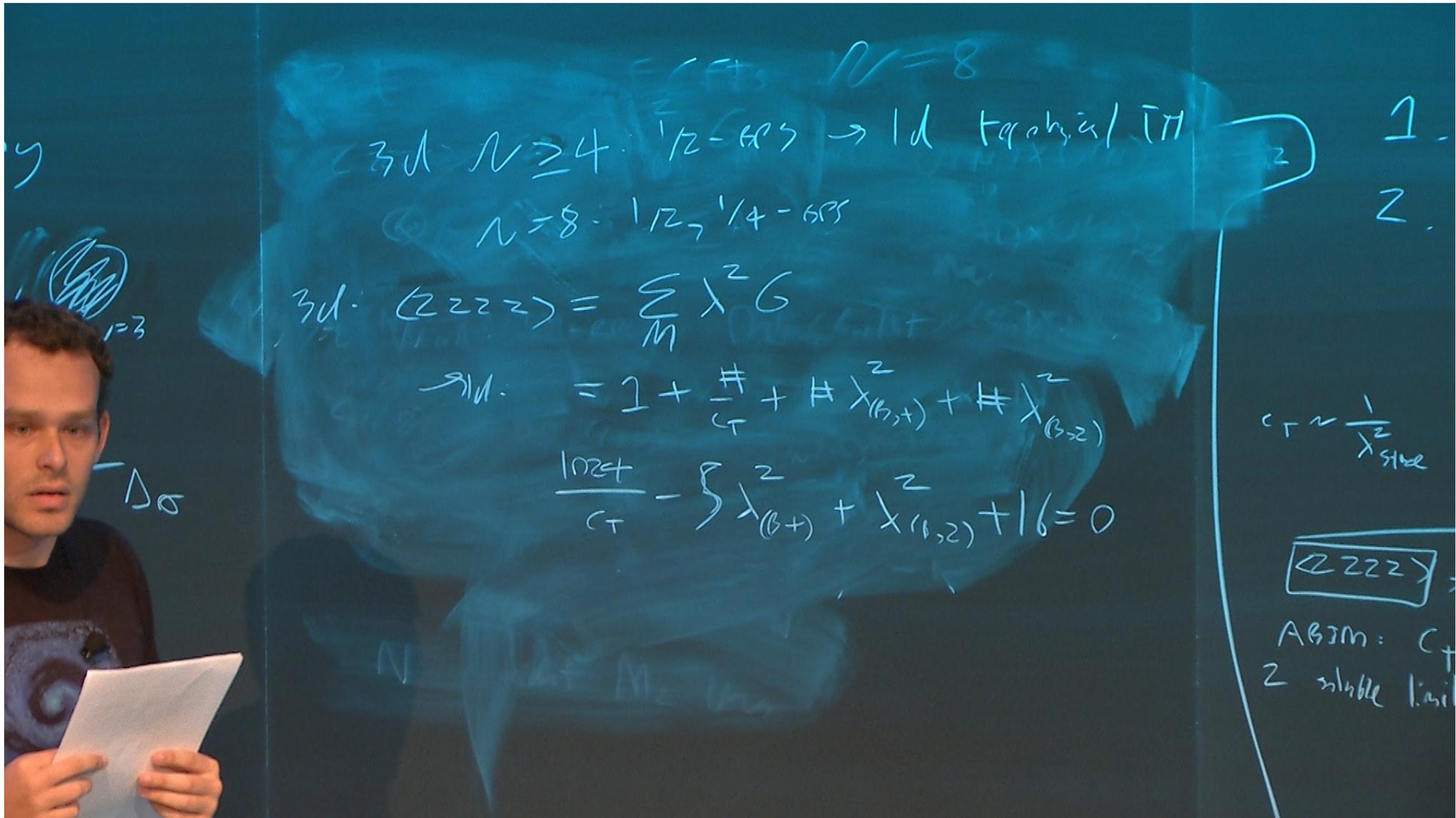
$$3d: \langle 2222 \rangle = \sum_M \chi^2 G$$

$$\rightarrow 1d: = 1 + \frac{\#}{G} + \# \chi_{(B,t)}^2 + \# \chi_{(B-z)}^2$$

$$c_T \sim \frac{1}{\chi_{state}^2}$$

$\langle 2222 \rangle$

ABJM: c_T
2 stable lines



$N=8$
 3d: $N \geq 4$ 1/2-eps \rightarrow 1d toroidal IM
 $N=8$ 1/2, 1/4-eps

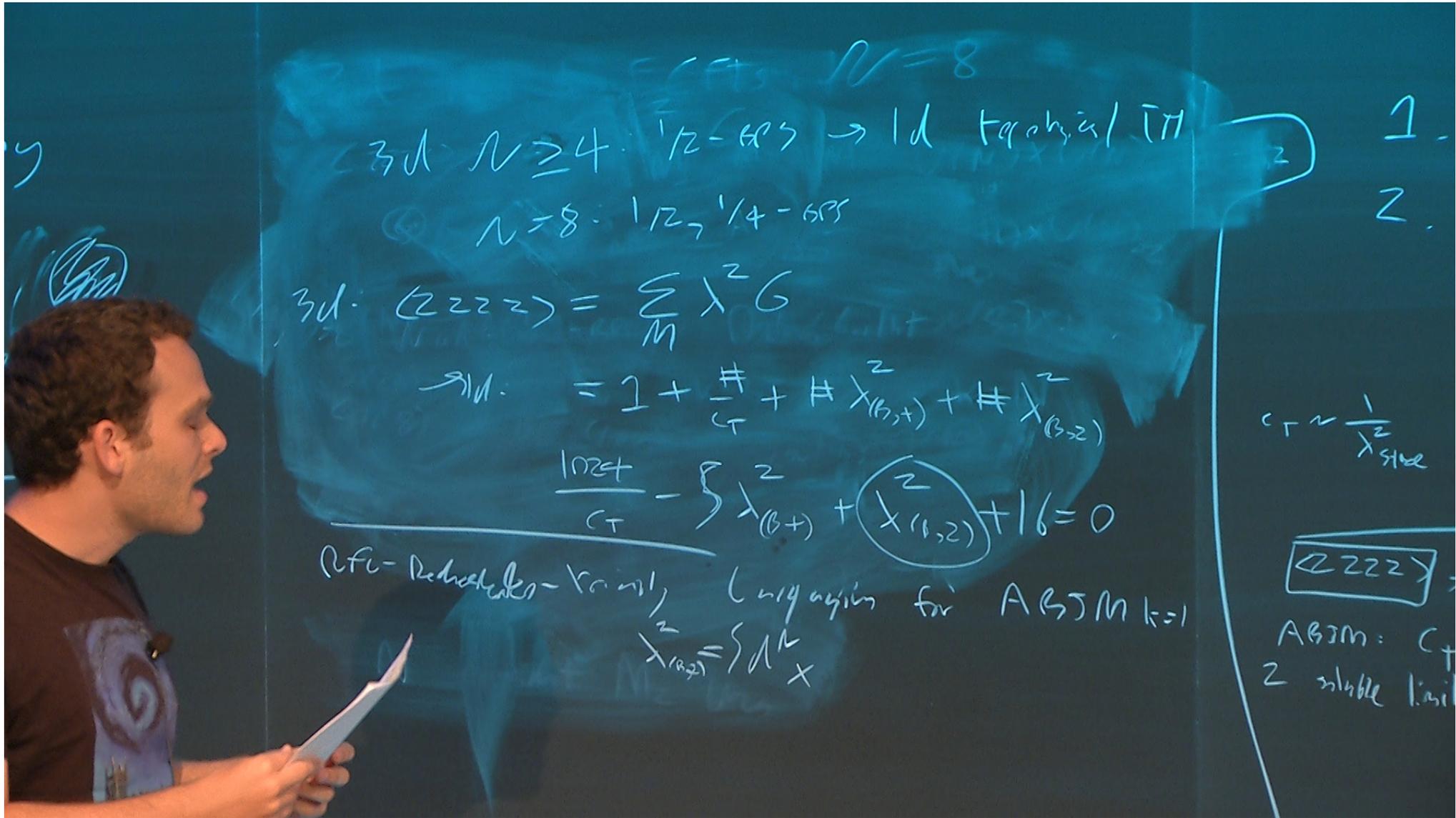
$$3d: \langle 2222 \rangle = \sum_M \chi^2 G$$

$$\begin{aligned}
 \rightarrow 1d: &= 1 + \frac{\#}{c_T} + \# \chi_{(b,+)}^2 + \# \chi_{(b,-)}^2 \\
 \frac{\log 4}{c_T} - \sum \chi_{(b,+)}^2 + \chi_{(b,-)}^2 + 16 &= 0
 \end{aligned}$$

$$c_T \sim \frac{1}{\chi_{st}^2}$$

$\langle 2222 \rangle$

ABJM: c_T
 2 stable limit



3D $N \geq 4$ 12-edges \rightarrow 1d topological TM

$N=8$ 12, 14-edges

$$3d: \langle 2222 \rangle = \sum_M \chi^2 G$$

$$\rightarrow 1d: = 1 + \frac{\#}{c_T} + \# \chi_{(3,+)}^2 + \# \chi_{(3,-2)}^2$$

$$\frac{1024}{c_T} - \sum \chi_{(3,+)}^2 + \chi_{(1,2)}^2 + 16 = 0$$

Ref: Reducible-krystal, Luygen for ABJM $k=1$

$$\chi_{(1,2)}^2 = \sum \chi^2$$

- 1.
- 2.

$$c_T \sim \frac{1}{\chi_{str}^2}$$

$\langle 2222 \rangle$

ABJM: c_T
2 stable limit

3d. $N \geq 4$. $1/2$ -GFS \rightarrow Id. topological TM

$N=8$. $1/2, 1/4$ -GFS

3d. $\langle 2222 \rangle = \sum_M \chi^2 G$

3d. $= 1 + \frac{\#}{c_T} + \# \chi_{(B,+)}^2 + \# \chi_{(B,-2)}^2$

$\frac{\ln Z}{c_T} - \sum \chi_{(B,+)}^2 + \chi_{(1,2)}^2 + 1/6 = 0$

(Feynman-Hellmann-Klein), Lagrangian for ABJM $k=1$

$\chi_{(B,+)}^2 = \sum \chi^2$

(Putrov-Murthy Nasrullah): $F(N)$ on S^3 3d
to $1/N$ S^1 Id

$c_T \sim \frac{1}{\chi_{S^2}^2}$

$\langle 2222 \rangle$

ABJM: c_T
2 stable lines

1
2

$N=3$

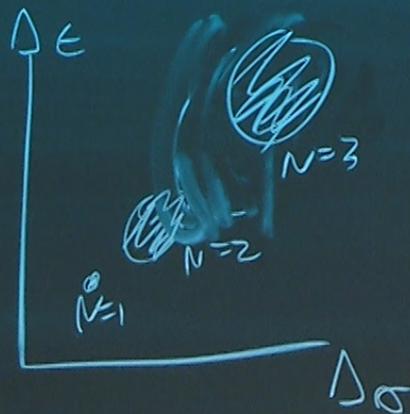
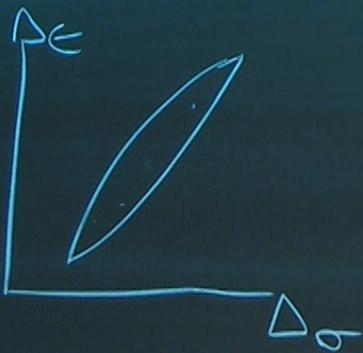
$N=2$

Δ_5

$1/2$

1. $O(N)$, $N=1$ using $\pm \sin y$

Mixed correlators



- $N=1$: -0.04%
- $N=2$: -12%
- $N=3$: -24%

$$e\% = \frac{U-L}{(U+L)/2}$$

$$d_m^n F(m) = \langle \underbrace{2 \dots 2}_m \rangle$$

$\chi_{(2^m)}^2, \chi_{(2^{m+1})}^2$ to $\mathcal{H}^1(N: A_i(N+1))$

3d $N \geq 4$

$N=8$

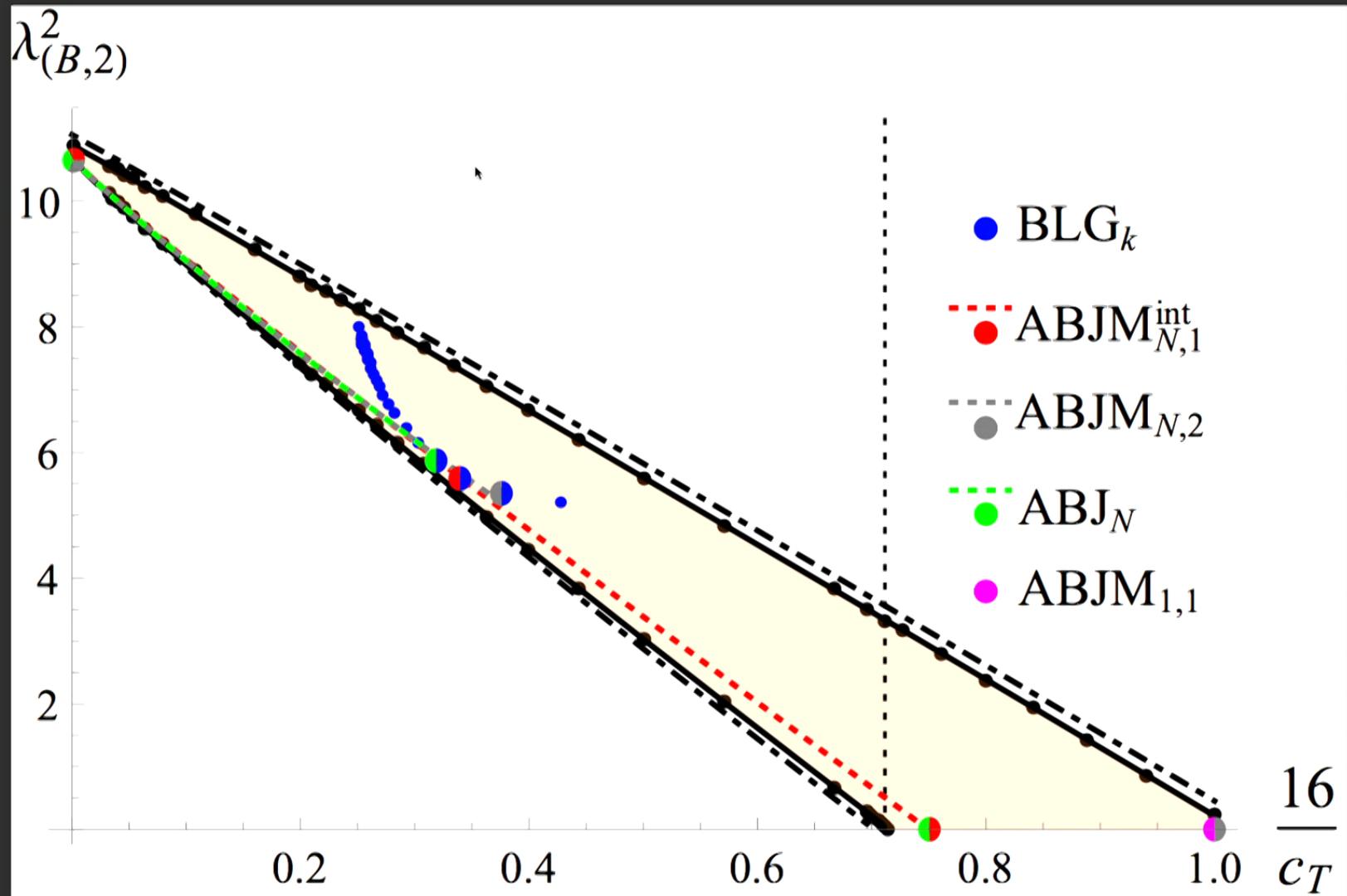
3d $\langle 2222 \rangle =$

9d $=$

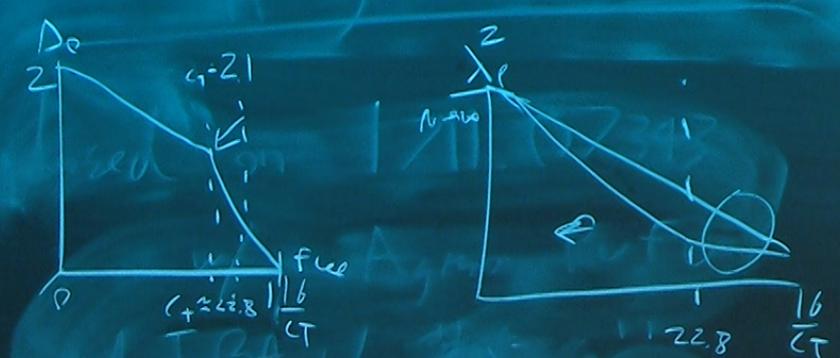
1024

(Ref - Reduct)

(Put in - Mod)



Optimizing M-theory

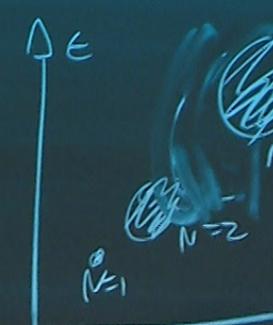
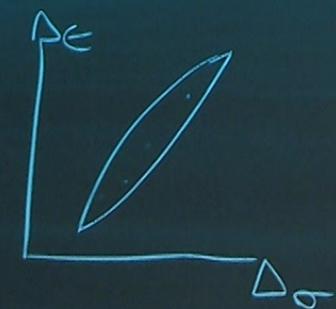


$\Delta\sigma = 2 + \frac{-109}{CT}$
 $\Delta\epsilon = 4 - \frac{42}{CT}$
 $\Delta n = -60$

$\frac{Pb/CT}{SUGRA: (2h\omega)}$
 $\frac{-1120}{H^2} \sim 113.98$
 $\frac{-59488}{35H^2} \sim -49.9311$

1. $O(N)$, $N=1$ Ising
 $N=1$ Ising

Mixed correlators



- $N=1: -0.04\%$
- $N=2: -12\%$
- $N=3: -24\%$

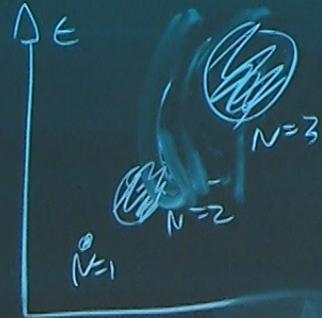
$\Delta_{10} = H + \frac{-61949}{10H^2} \sim -62.949$

$$e\% = \frac{U-L}{(U+L)/2}$$

$$d_m^n F(m) = \int \langle \dots \rangle$$

N) , N=1 Ising
 N=1 Ising

correlators



470
 2%
 24%
 51944
 2111

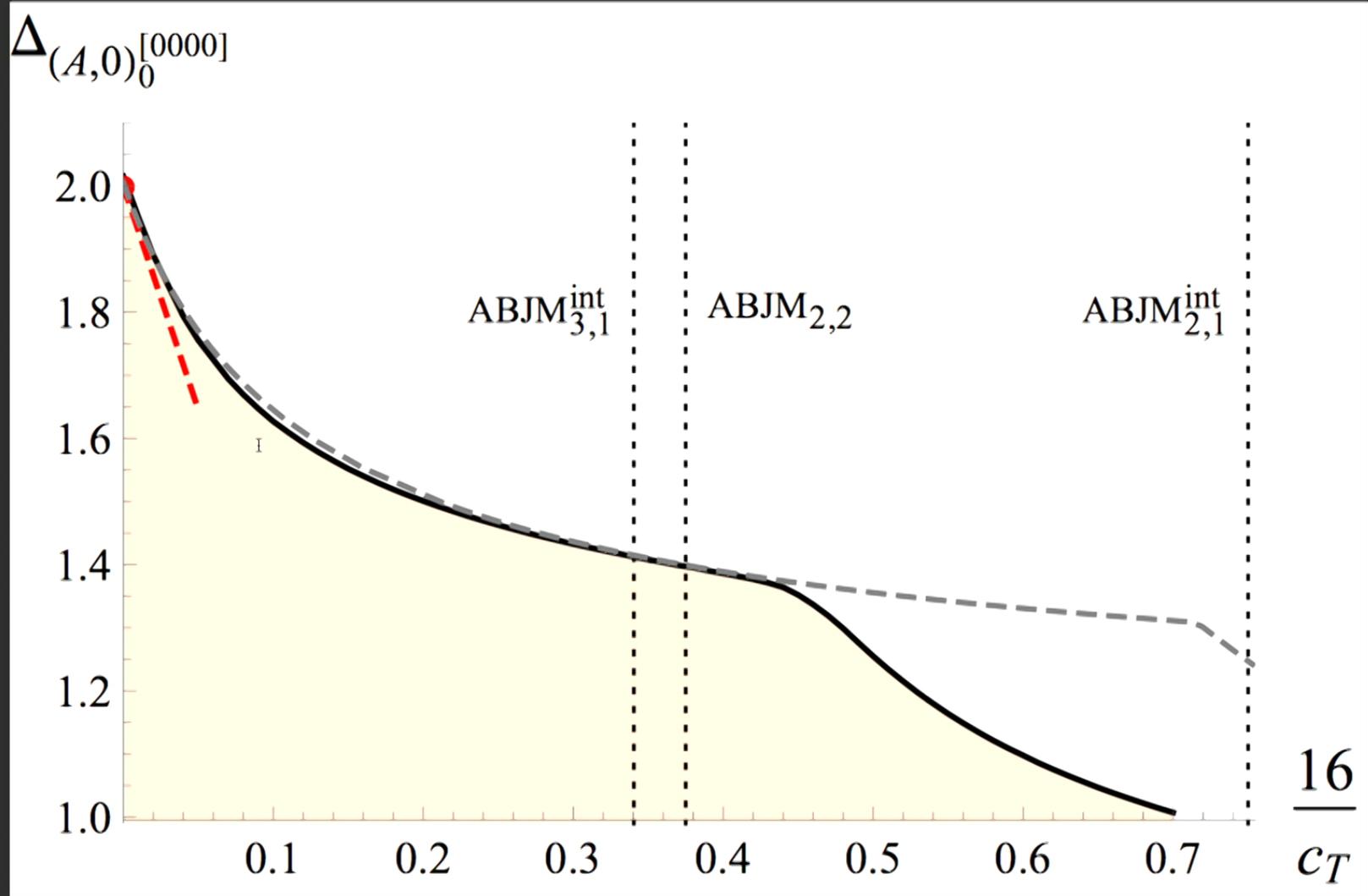
$d_m f(m) =$

$(2222), (3222), (2233)$
 $(3222), N=2, (2222) \rightarrow$ all terms

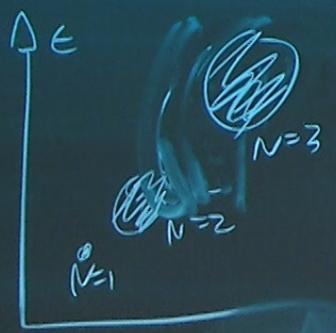
1. ~~$K=2$~~
2. $2 \times 3 = 1$ ~~file~~
3. 10 starts > 3

- 34 dists \rightarrow
- $\nearrow (2,2)$
 - $\nearrow (2,0)$
 - $\nearrow (0,0)$

1. $(2222) \cdot 8$



sing
I sing



(2222) , (3222) , (2233)
 $N=4$, $N=5$, $N=6$, $N=7$, $N=8$

1. ~~$k=2$~~
2. $2 \times 3 = 1$ ~~file~~
3. 10 starts > 3

- 34 \rightarrow
1. $(2,2)$
 2. $(2,0)$
 3. $(0,0)$

$ATM^k_{N=2} = ABT, \overline{ABT}$
ABT

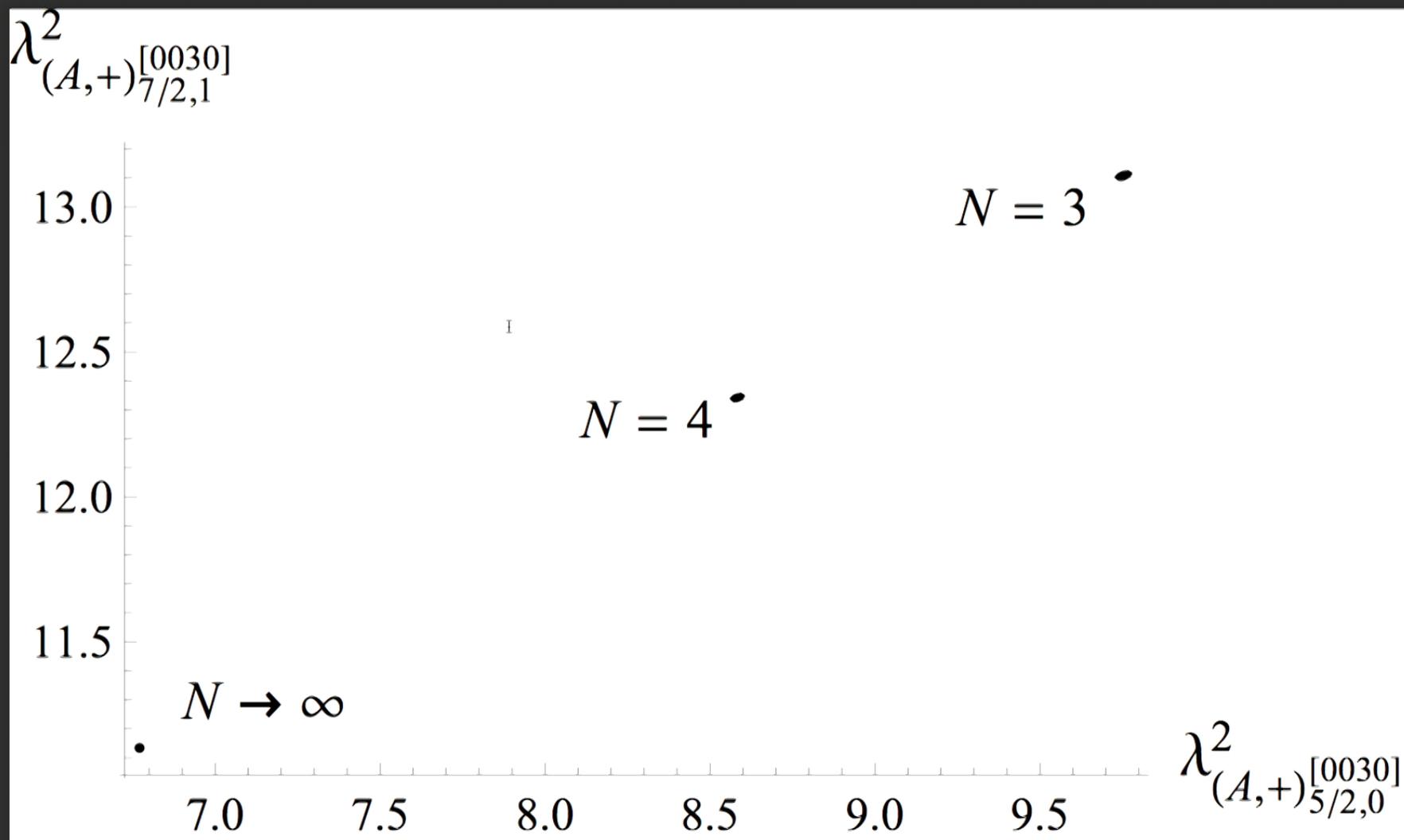
(2222)

1. 50
2. $1/2$
- $q=1$
- $q=2$
- $q=3$

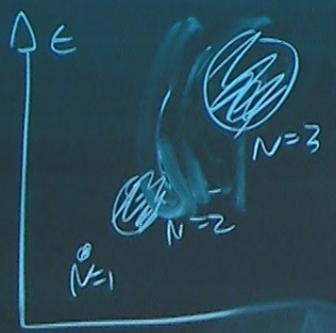
$c_T \sim \frac{1}{\lambda_{size}^2}$

(2222), (3222)

ABJM: $c_T \sim N$
 2 stable limits: FN
 2 G



Ising
 Ising



(2222) , $(3 \rightarrow 2)$, (2233)
 $N=2$, $N=3$, $N=4$, $N=8$

1. ~~$k \rightarrow$~~
2. $2 \times 3 = 1$ ~~file~~
3. 10 starts > 3

3d display \rightarrow $(2 \rightarrow 2)$
 $N=3$: $g_{m=0} = 30\%$
 $g_{m=1} = 10\%$
 $N=4$: $g_{m=0} = 25\%$
 $g_{m=1} = 10\%$

$ATM^k_{N=2} = ABT, \overline{ABT}$
ABT

$c_T \sim \frac{1}{\lambda_{size}^2}$

(2222)

ABJM:
 $2 \rightarrow 1/4$

1. 50
2. $1/2 -$
 $g=1$