

Title: PSI 2018/2019 - Beyond Standard Model - Lecture 6

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Collection: PSI 2018/2019 - Beyond Standard Model (Boyle)

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URL: <http://pirsa.org/19040021>

	SU(3)	SU(2)	U(1)
$q_L$	3	2	$1/6$
$u_R$	3	1	$2/3$
$d_R$	3	1	$-1/3$
$l_L$	1	2	$-1/2$
$\nu_R$	1	1	0
$e_R$	1	1	-1
$h$	1	2	$1/2$

	SU(3)	SU(2)	U(1)
$q_L$	3	2	$1/6$
$u_R$	3	1	$2/3$
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$l_L$	1	2	$-1/2$
$[ \nu_R ]$	1	1	0
$e_R$	1	1	-1
$h$	1	2	$1/2$

SM: omit  $\nu_R$  row, omit NR terms

SMEFT: omit  $\nu_R$  row, include NR terms

vSM: include  $\nu_R$  row, omit NR terms.

terms

SM:

- i) neutrino masses/oscillations
- ii) cosmic matter/antimatter asym.
- iii) DM.

terms

SMEFT:

explains (i), but not (ii) + (iii)

terms.

terms

SM:  
i) neutrino masses/oscillations  
ii) cosmic matter/antimatter asym.  
iii) DM.

terms

SMEFT: explains (i), but not (ii) + (iii)

terms.

$\nu$ SM:  
• explains (i), (ii), (iii)  
• reduces SMEFT  
• sets stage for GUT

$h$	$1$	$2$	$1/2$
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$$\tilde{h} = i\sigma^2 h^*$$

SMEFT:

$$\psi_L = \tilde{h}^+ \chi_L$$

$$\psi_{L,c} = -i\sigma^2 \psi_L^*$$

$$-\frac{1}{2\Lambda} \tilde{h}^i \chi_{L,c}^j \gamma^5 \psi_L^k$$

h	1	2	3/2
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$$\tilde{h} = i\sigma^2 h^*$$

SMEFT:

$$\psi_L = \tilde{h}^+ \chi_L$$

$$\psi_{L,c} = -i\sigma^2 \psi_L^*$$

$$-\frac{1}{2\Lambda} \left[ \psi_{L,c}^i \gamma^j \psi_L^j + h.c. \right]$$

$\begin{pmatrix} \nu + \mu \\ 0 \end{pmatrix}$

50s stage for GLLT

\*  
L

$$-\frac{1}{2\lambda} \left[ \bar{\nu}_{Lc}^i y^{ij} \bar{\nu}_L^j + \text{h.c.} \right] \quad y^{ij} = y^{ji}$$
$$\rightarrow -\frac{1}{2} \left[ \bar{\nu}_{Lc}^i M^{ij} \bar{\nu}_L^j + \text{h.c.} \right] \leftarrow M^{ij} = \frac{\nu}{\sqrt{2}} y^{ij} = U^T \hat{M}^{ij} U$$

5th stage for GUT

$$\begin{aligned}
 & -\frac{1}{2\Lambda} [\bar{\nu}_{Lc}^i \gamma^{ij} \nu_L^j + \text{h.c.}] \quad \gamma^{ij} = \gamma^{ji} \\
 & \rightarrow -\frac{1}{2} [\bar{\nu}_{Lc}^i M^{ij} \nu_L^j + \text{h.c.}] \leftarrow M^{ij} = \frac{v}{\sqrt{2}} \gamma^{ij} = U^T \hat{M}^{ij} U, \quad \nu_L' = U \nu_L \\
 & \rightarrow -\frac{1}{2} [\bar{\nu}_{Lc}^i \hat{M}^{ij} \nu_L'^j + \text{h.c.}] \leftarrow \nu' = \begin{pmatrix} \nu_{Lc}' \\ \nu_L' \end{pmatrix} \quad \nu_c = -i\gamma^2 \nu'^* = \nu' \\
 & = -\frac{1}{2} [\bar{\nu}' \hat{M}^{ij} \nu'] \leftarrow \text{"Majorana mass"}
 \end{aligned}$$

$\varphi^* = \varphi$

h | 1 | 2 | 1/2

$$\tilde{h} = i\sigma^2 h^* = \frac{1}{\sqrt{2}} \begin{pmatrix} v + h \\ -0 \end{pmatrix}$$

SMEFT:

$$\psi_L = \tilde{h}^+ l_L$$

$$\psi_{L,c} = -i\sigma^2 \psi_L^*$$

$$l_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$$

$$\begin{aligned}
 & -\frac{1}{2\Lambda} \tilde{v}_{L,c}^i \gamma^{ij} \nu_L^j + h \\
 & \rightarrow -\frac{1}{2} \left[ \tilde{v}_{L,c}^i M^{ij} \nu_L^j + h \right] \\
 & \rightarrow -\frac{1}{2} \left[ \tilde{v}_{L,c}^i \hat{M}^{ij} \nu_L^j + h \right] \\
 & = -\frac{1}{2} \left[ \tilde{v}^i \hat{M}^{ij} \nu^j \right] \leftarrow
 \end{aligned}$$



5th stage for GUT

$$-\frac{1}{2\Lambda} [\bar{\nu}_{L,c}^i \gamma^{ij} \nu_L^j + h.c.] \quad \gamma^{ij} = \gamma^{ji}$$

$$-\frac{1}{2} [\bar{\nu}_{L,c}^i M^{ij} \nu_L^j + h.c.] \leftarrow M^{ij} = \frac{v^2}{2\Lambda} \gamma^{ij} = U^T \hat{M}^{ij} U, \quad \nu_L' = U \nu_L$$

$$\varphi^* = \varphi$$

$$-\frac{1}{2} [\bar{\nu}_{L,c}^i \hat{M}^{ij} \nu_L^j + h.c.] \leftarrow \nu' = \begin{pmatrix} \nu_{L,c}' \\ \nu_L' \end{pmatrix}$$

$$\nu_c' = -i\sigma^2 \nu'^* = \nu'$$

$$= -\frac{1}{2} [\bar{\nu}' \hat{M}^{ij} \nu'] \leftarrow \text{"Majorana mass"}$$

$$1 \quad 1 \quad 2 \quad 1/2$$

$$\tilde{h} = i\sigma^2 h^* = \frac{1}{\sqrt{2}} \begin{pmatrix} \nu + H \\ -0 \end{pmatrix}$$

$$V'_L = U V_L$$

$$d'_L = V_{CKM} d_L$$

↑  
mass  
eigenstates

↑  
weak  
eigenstates

$h \mid 1 \mid 2 \mid 1/2$

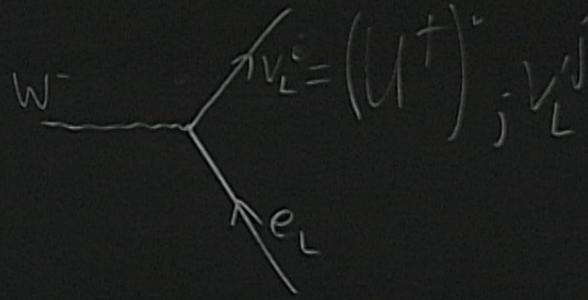
$$\tilde{h} = i\sigma_2 h^* = \frac{1}{\sqrt{2}} \begin{pmatrix} \nu + \mu \\ -\mu \end{pmatrix}$$

$$\nu'_L = U \nu_L$$

$$d'_L = V_{CKM} d_L$$

mass eigenstates

weak eigenstates



5th stage for GUT

next in SMEFT: dim 6:  $\mathcal{B}$ ,  $p^+$  decay.

$$q \quad B = \frac{1}{3}$$

$$l \quad B = 0$$

$$h, \text{ gauge bosons} = 0$$

5th stage for GUT

next in SMEFT:

$$q \quad B = \frac{1}{3}$$

$$l \quad B = 0$$

$$h, \text{ gauge bosons} = 0$$

dim 6:  $B, p^+$  decay

$$\text{dim 5: } \frac{1}{\Lambda}$$

$$\text{dim 6: } \frac{1}{\Lambda^2}$$

Can't explain:

i) B

50's stage for GUT

next in SMEFT:

$$q \quad B = \frac{1}{3}$$

$$l \quad B = 0$$

$$h, \text{ gauge bosons} = 0$$

dim 6.  $B, p^+$  decay.

$$\text{dim 5} = \frac{O(2)}{\Lambda}$$

$$\text{dim 6} = \frac{O(1)}{\Lambda^2}$$

Can't explain:  
i)  $B, CP, \text{Therm}$

ii) ~~DMA~~

vSM

$\mathcal{L} =$  (bosonic terms)

$$+ i \left[ \bar{q}_L \not{D} q_L + \bar{u}_R \not{D} u_R + \bar{d}_R \not{D} d_R + \bar{l}_L \not{D} l_L + \bar{\nu}_R \not{D} \nu_R + \bar{e}_R \not{D} e_R \right]$$

$$- \left[ \bar{q}_L \gamma_d h d_R + \bar{q}_L \gamma_u \tilde{h} u_R + \bar{l}_L \gamma_e h e_R + \bar{l}_L \gamma_\nu \tilde{h} \nu_R \right] -$$

SM

$L =$  (bosonic terms)

$$+ i \left[ \bar{q}_L \not{D} q_L + \bar{u}_R \not{D} u_R + \bar{d}_R \not{D} d_R + \bar{l}_L \not{D} l_L + \bar{\nu}_R \not{D} \nu_R + \bar{e}_R \not{D} e_R \right]$$

$$- \left[ \bar{q}_L \gamma_d h d_R + \bar{q}_L \gamma_u \tilde{h} u_R + \bar{l}_L \gamma_e h e_R + \bar{l}_L \gamma_\nu \tilde{h} \nu_R \right] - \frac{1}{2} \left[ \bar{\nu}_R c M_{mR}^{ij} \nu_R^j + \text{h.c.} \right]$$

$$\equiv \left. \begin{matrix} \vdots \\ \vdots \\ \vdots \end{matrix} \right\} v_R, M_m$$

$$M_m \left[ \begin{matrix} \vec{v}_R \\ \vec{v}_L \\ \vdots \end{matrix} + h c \right]$$

$$\equiv \left. \begin{matrix} \vdots \\ \vdots \\ \vdots \end{matrix} \right\} v_L, \frac{v^2}{M_m}$$

$$v_R: -\bar{L}_L Y_L \tilde{h} - \nabla_{R,c} M_m = 0 \quad \text{Solve for } v_R$$

$$-\frac{1}{2} \left[ \nabla_{L,c}^i \underbrace{M^{ij}}_1 v_L^j + h.c. \right]$$

$$M^{ij} = -M_v M_m^{-1} M_v^T$$

$$M_m$$

$$M_v = \frac{v}{\sqrt{2}} Y$$

$$ii) N = \begin{pmatrix} \nu_R \\ \nu_{Rf} \end{pmatrix} \quad N \begin{matrix} \rightarrow h l \\ \rightarrow (h l)_c \end{matrix}$$

$$T < m_N \quad e^{-m_N/T}$$

"leptogenesis"

iii) DM candidate 1 of 3  $N$ 's.  
 $\rightarrow$   $\nu$ MSM (Shaposhnikov) 1 keV  
 $\rightarrow$  CPT

