

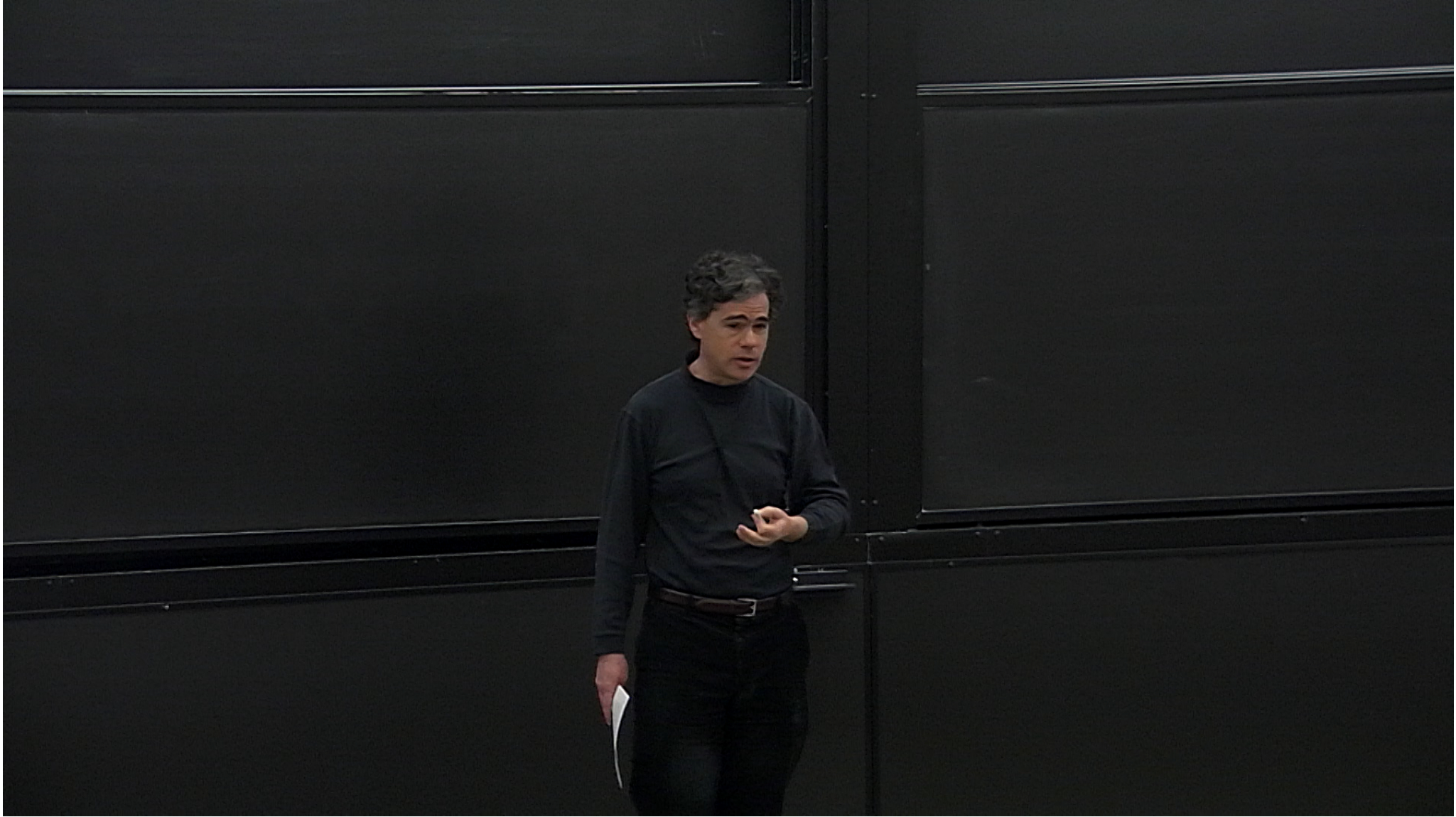
Title: PSI 2018/2019 - Quantum Information Review - Lecture 4

Speakers: Daniel Gottesman

Collection: PSI 2018/2019 - Quantum Information Review (Gottesman)

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DiVincenzo criteria:

1. A scalable physical system with well-characterized qubits.
2. The ability to initialize the state of the qubits to a simple fiducial state, such as $|00\rangle$.
3. Long relevant decoherence times, much longer than the gate operation time.
4. A universal set of gates.

Flying qubits = ones that move

Stationary qubits = ones in computer

6. The ability to interconvert between stationary & flying qubits
7. The ability to faithfully transmit flying qubits between specified locations.

Ion traps:

Atom + charge, 1 electron in outer shell

$$|g\rangle = |0\rangle$$

$$|e\rangle = |1\rangle$$

$$H = H_{\text{atom}} + H_{\text{laser}}$$

$$H_{\text{atom}} = E|e\rangle\langle e|$$

$$H_{\text{laser}} = J(e^{-i\omega t}|g\rangle\langle e| + e^{i\omega t}|e\rangle\langle g|)$$

$$\omega = E/\hbar \text{ frequency of laser}$$

$$|g\rangle \mapsto \cos(Jt/\hbar)|g\rangle + \sin(Jt/\hbar)|e\rangle$$

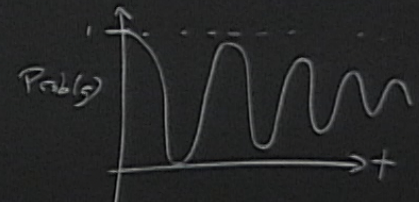
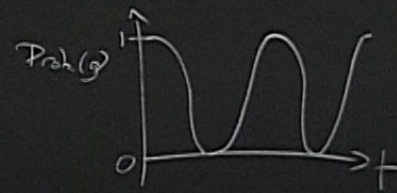
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Rabi oscillations

$$H = H_{\text{atom}} + H_{\text{laser}}$$

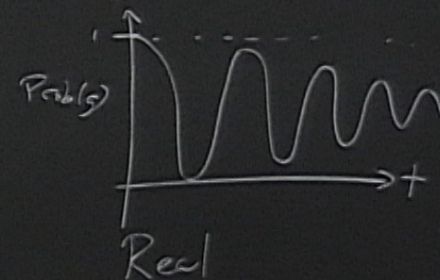
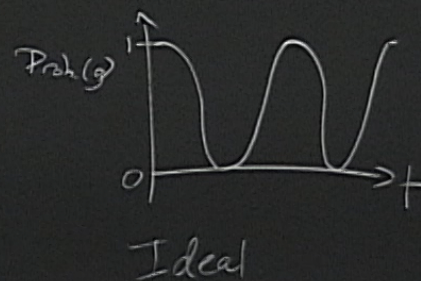
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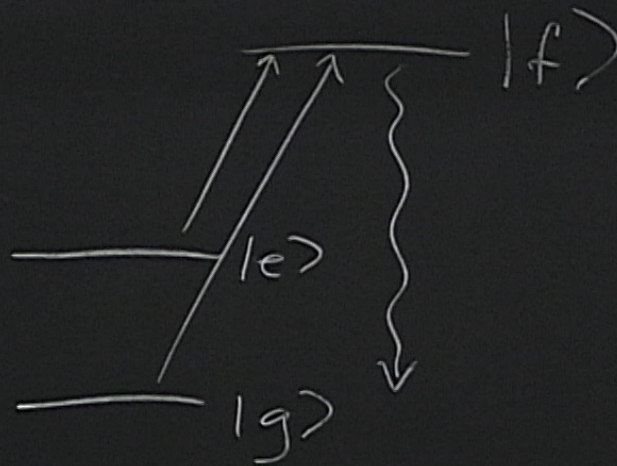
$\omega = E/\hbar$ frequency of laser

- Single-qubit X rotations by turning on laser
- Single-qubit Z rotations by waiting

$$|g\rangle \mapsto \cos(Jt/\hbar)|g\rangle + \sin(Jt/\hbar)|e\rangle$$



Rabi oscillations



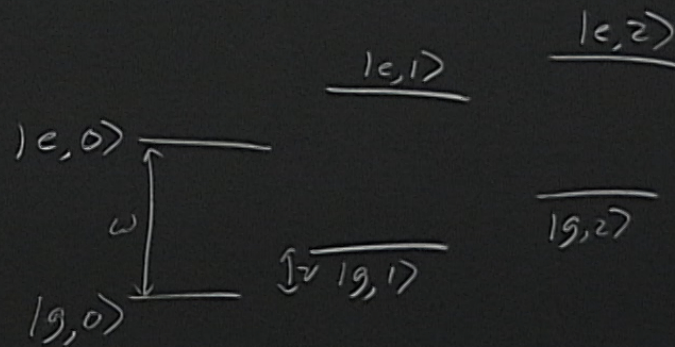
Measurement via cycling transition.
Preparation also.

Two-qubit gates:

($\leftrightarrow$)

Phonon modes

$$H_{\text{phonon}} = \hbar \omega a^\dagger a$$



transition.

$$\omega = E/\hbar \text{ frequency of laser}$$

Rabi oscillations

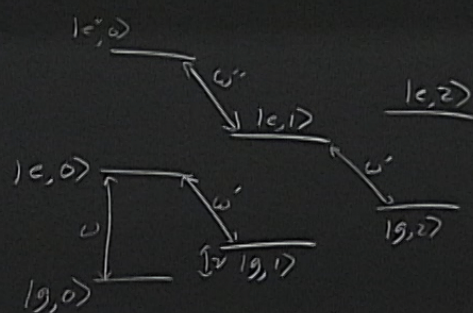
- Single-qubit X rotations by turning on laser
- Single-qubit Z rotations by waiting

Two-qubit gates:

($\leftrightarrow$)

Phonon modes

$$H_{\text{phonon}} = \hbar \nu a^\dagger a$$



$$\hbar \omega' = E - \hbar \nu$$

$$|e''\rangle \text{ w/ energy } E''$$

$$\omega'' = (E'' - E)/\hbar - \nu$$

Cirac-Zoller gate

1. $\pi/2$ pulse on atom 1 w/ frequency ω'
2. π pulse on atom 2 w/ frequency ω''

$$1. \begin{aligned} |e\rangle_1 |0\rangle_p &\rightarrow |g\rangle_1 |1\rangle_p \\ |g\rangle_1 |0\rangle_p &\rightarrow |g\rangle_1 |0\rangle_p \end{aligned}$$

$$2. \begin{aligned} |g\rangle_2 |0\rangle_p &\rightarrow |g\rangle_2 |0\rangle_p \\ |e\rangle_2 |0\rangle_p &\rightarrow |e\rangle_2 |0\rangle_p \\ |g\rangle_2 |1\rangle_p &\rightarrow |g\rangle_2 |1\rangle_p \\ |e\rangle_2 |1\rangle_p &\rightarrow -|e\rangle_2 |1\rangle_p \end{aligned}$$