

Title: PSI 2018/2019 - Cosmology Review - Lecture 9

Date: Jan 17, 2019 09:00 AM

URL: <http://pirsa.org/19010010>

Abstract:

CMB

$$\left(\frac{n_H}{n_{eq}}\right) = \left(\frac{1-X}{X^2}\right)_{eq} = \underbrace{\left(\frac{2S(2)}{\pi^2}\right)}_{10^{-9}} \left(\frac{4\pi T}{m_e}\right)^{3/2} \underbrace{e^{\frac{\mu_H}{T}}}_{\text{recombination}}$$

when photon  
Decouple:

$$P \sim H$$

$$\Gamma = n_e \underbrace{\sigma v}_{1} = X n_b \sigma = X \left(\frac{2S(2)}{\pi^2}\right) T^3 \underbrace{\sigma}_{\text{number}}$$

CMB

$$\left(\frac{n_H}{n_{\text{ph}}}\right) = \left(\frac{1-X}{X^2}\right)_{\text{eq}} = \eta \frac{2S(2)}{\pi^2} \left(\frac{4\pi T}{m_e}\right)^{3/2} e^{-\frac{B_H}{T}} X(T)$$

$\underbrace{\quad}_{10^{-9}}$ 
 $\underbrace{\quad}_{\text{recombination}}$ 
 $\underbrace{\quad}_{T \sim 0.3 \text{ eV}}$

when photon  
Decouple:

$$P \sim H$$

$$v=m \quad z \sim 3 \times 10^3$$

$$\Gamma = n_e \sigma_{\text{Th}} = X n_b \sigma = X \eta \frac{2S(2)}{\pi^2} T^3 \sqrt{\text{number}}$$

$$H = \frac{a \propto t^{3/2}}{a^{3/2} \propto t} \sim a^{-3/2} \propto T^{3/2}$$

$$\frac{H}{H_0} = \left(\frac{T}{T_0}\right)^{3/2}$$

$$P \sim H$$

$$T \approx 0.25 \text{ eV} \quad X=0.01$$

$$a \propto t^{2/3} \quad a \propto \frac{1}{T}$$

$$H = \frac{\dot{a}}{a} \sim \frac{1}{t} \sim a^{-3/2} \propto T^{3/2}$$

$$\frac{H}{H_0} = \left( \frac{T}{T_0} \right)^{3/2}$$

orange  
universe

$$P \sim H$$

$$T \approx 0.25 \text{ eV} \quad X=0.01$$

Anisotropy

$$\frac{\delta T}{T} \sim 10^{-5}$$

$$C(\theta) = \left\langle \frac{\delta T}{T}(\hat{n}_1) \frac{\delta T}{T}(\hat{n}_2) \right\rangle_{\cos \theta = \hat{n}_1 \cdot \hat{n}_2}$$

$$\frac{\delta T}{T} = \sum_{l=1}^{\infty} \sum_{m=-l}^l a_{lm} Y_{lm}(\theta, \phi)$$

$$a \propto \frac{1}{T^{\frac{3}{2}}}$$

orange universe

Anisotropy

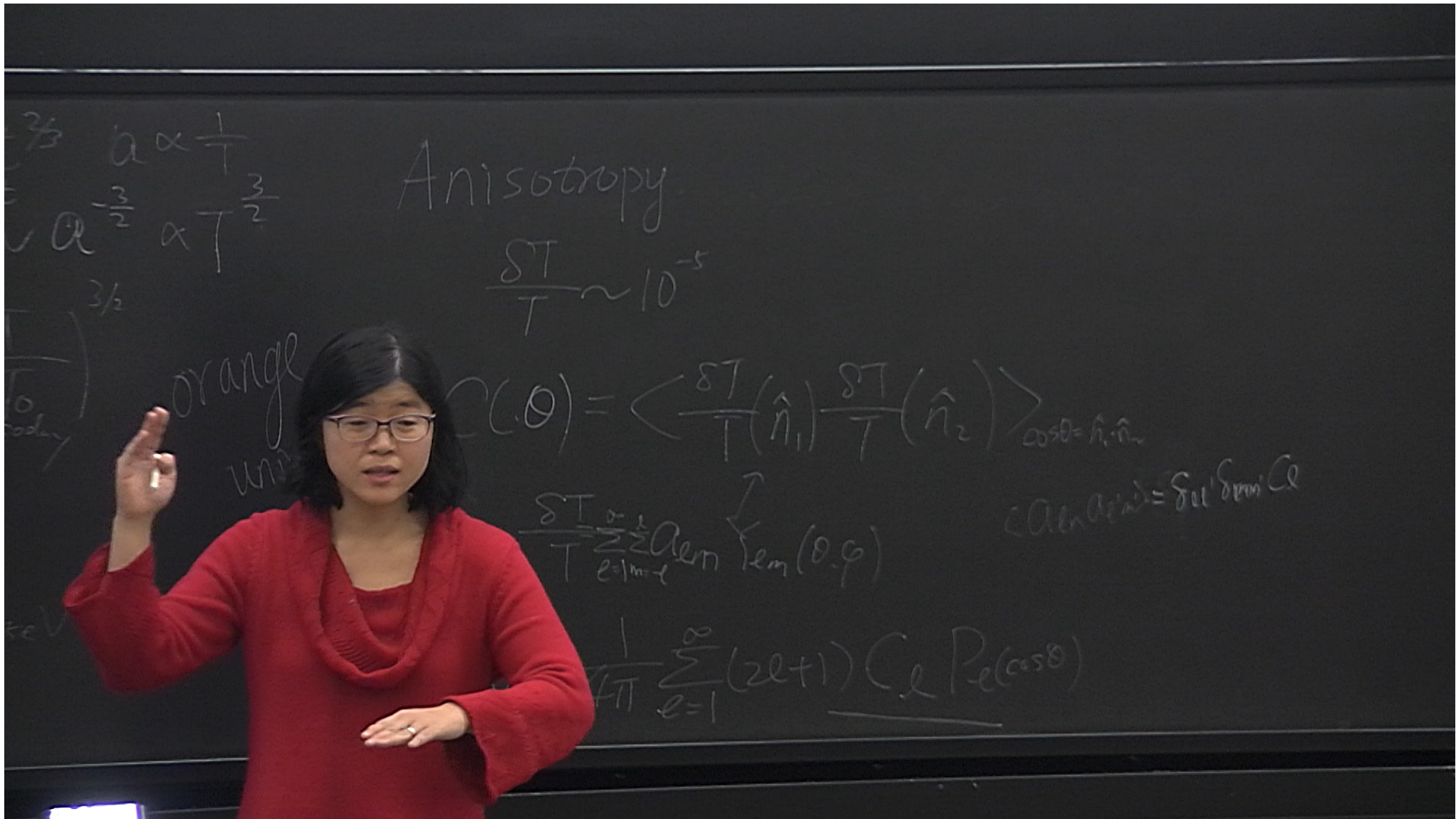
$$\frac{\delta T}{T} \sim 10^{-5}$$

$$C(\theta) = \left\langle \frac{\delta T}{T}(\hat{n}_1) \frac{\delta T}{T}(\hat{n}_2) \right\rangle_{\cos \theta = \hat{n}_1 \cdot \hat{n}_2}$$

$$\frac{\delta T}{T} = \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$\langle a_{\ell m} a_{\ell' m'} \rangle = \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

$$C(\theta) = \frac{1}{4\pi} \sum_{\ell=1}^{\infty} (2\ell+1) C_{\ell} P_{\ell}(\cos \theta)$$



Anisotropy

$$\frac{\delta T}{T} \sim 10^{-5}$$

$$a \propto T^{-\frac{3}{2}}$$

orange  
unit

$$C(\theta) = \left\langle \frac{\delta T}{T}(\hat{n}_1) \frac{\delta T}{T}(\hat{n}_2) \right\rangle_{\cos\theta = \hat{n}_1 \cdot \hat{n}_2}$$

$$\frac{\delta T}{T} = \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

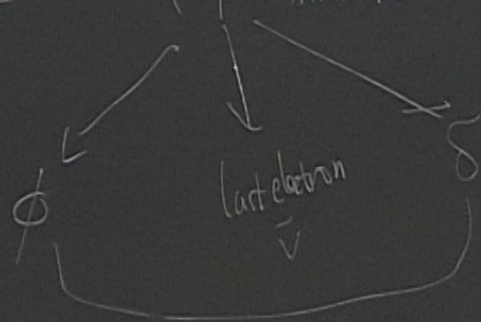
$$C(\theta) = \sum_{\ell} \frac{2\ell+1}{4\pi} C_{\ell} P_{\ell}(\cos\theta)$$

$$\frac{1}{4\pi} \sum_{\ell=1}^{\infty} (2\ell+1) C_{\ell} P_{\ell}(\cos\theta)$$

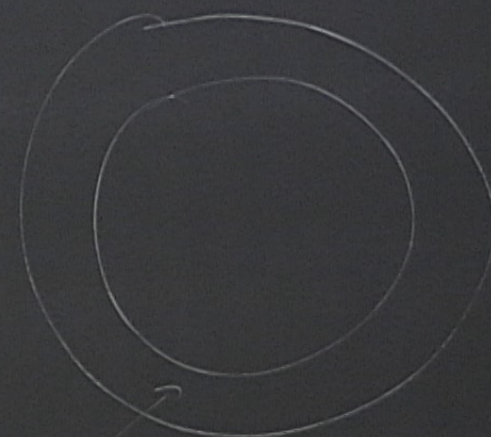
$$\sqrt{\frac{(C_e - C_{obs})^2}{Q}} \propto \frac{1}{\sqrt{2l+1}}$$

Cosmic variance

$$\frac{\delta T}{T} = \left( \frac{\delta T}{T} \right)_{\text{intrinsic}} + \left( \frac{\delta T}{T} \right)_{\text{Sunyaev}}$$

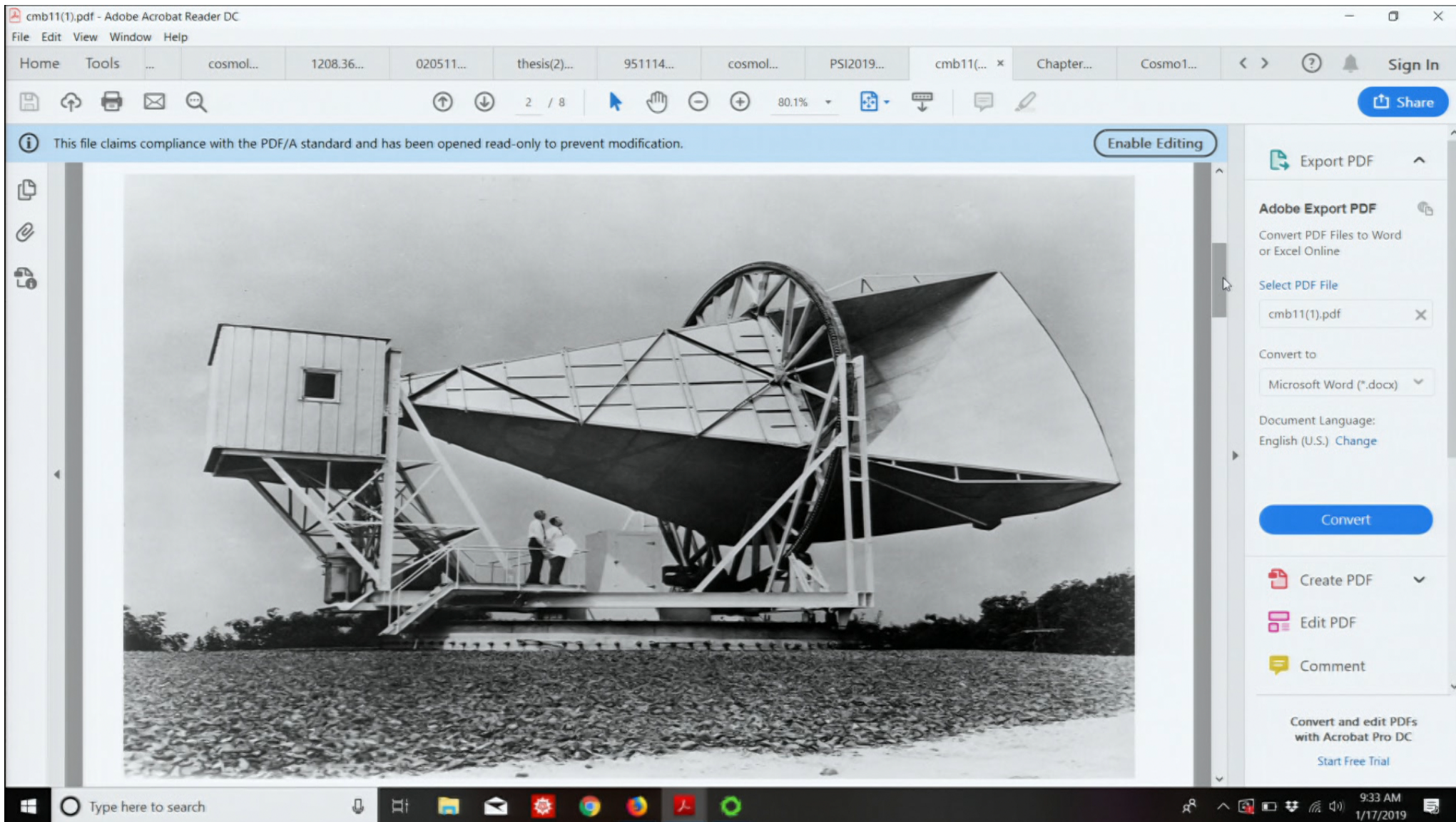


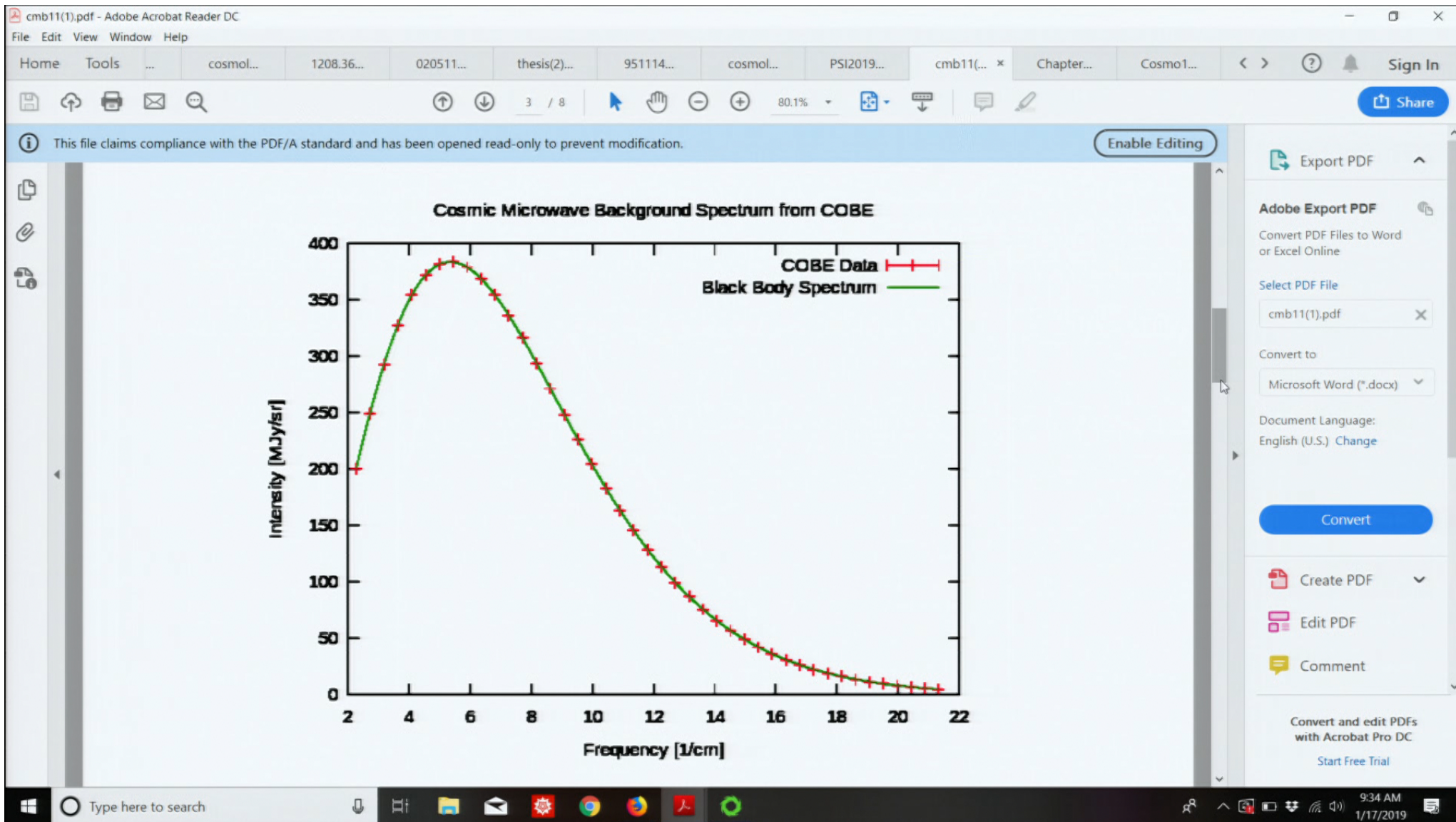
$$\int \dot{\phi} dt$$



finite thickness

CAMB





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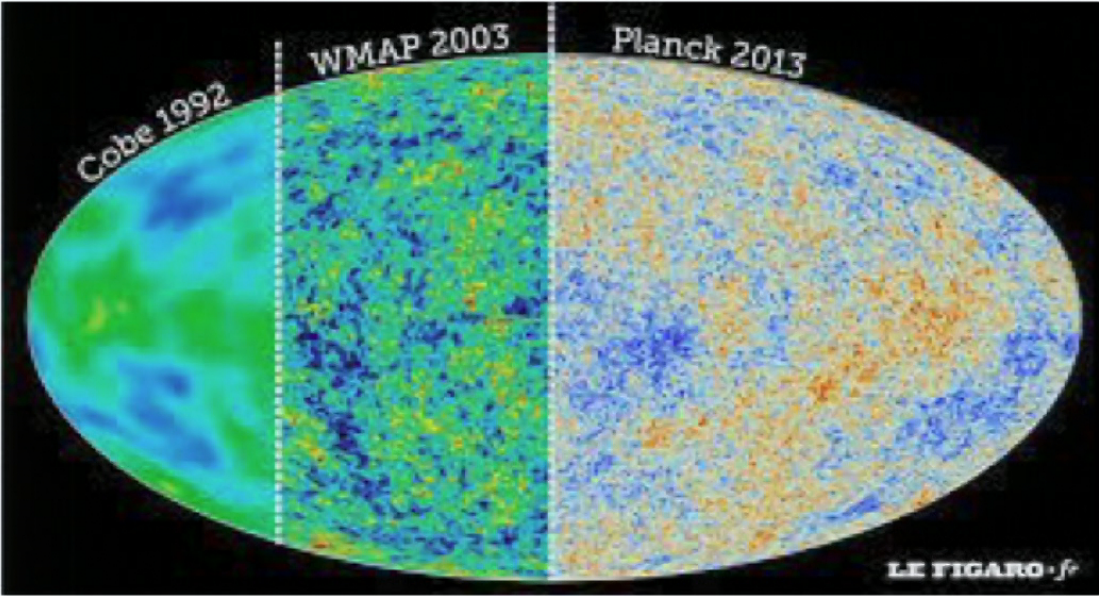
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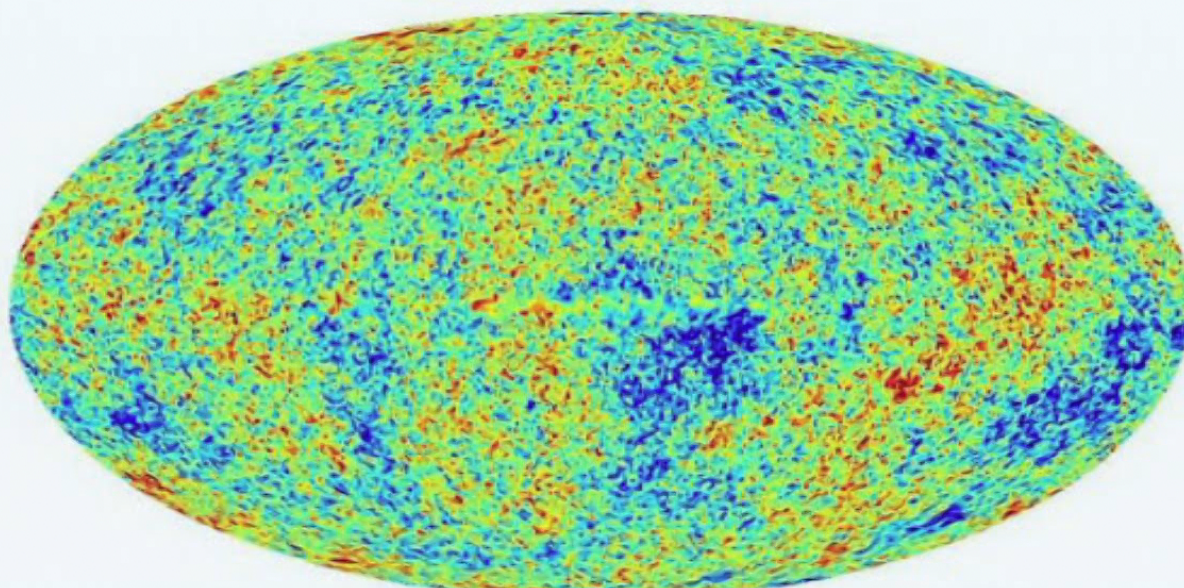
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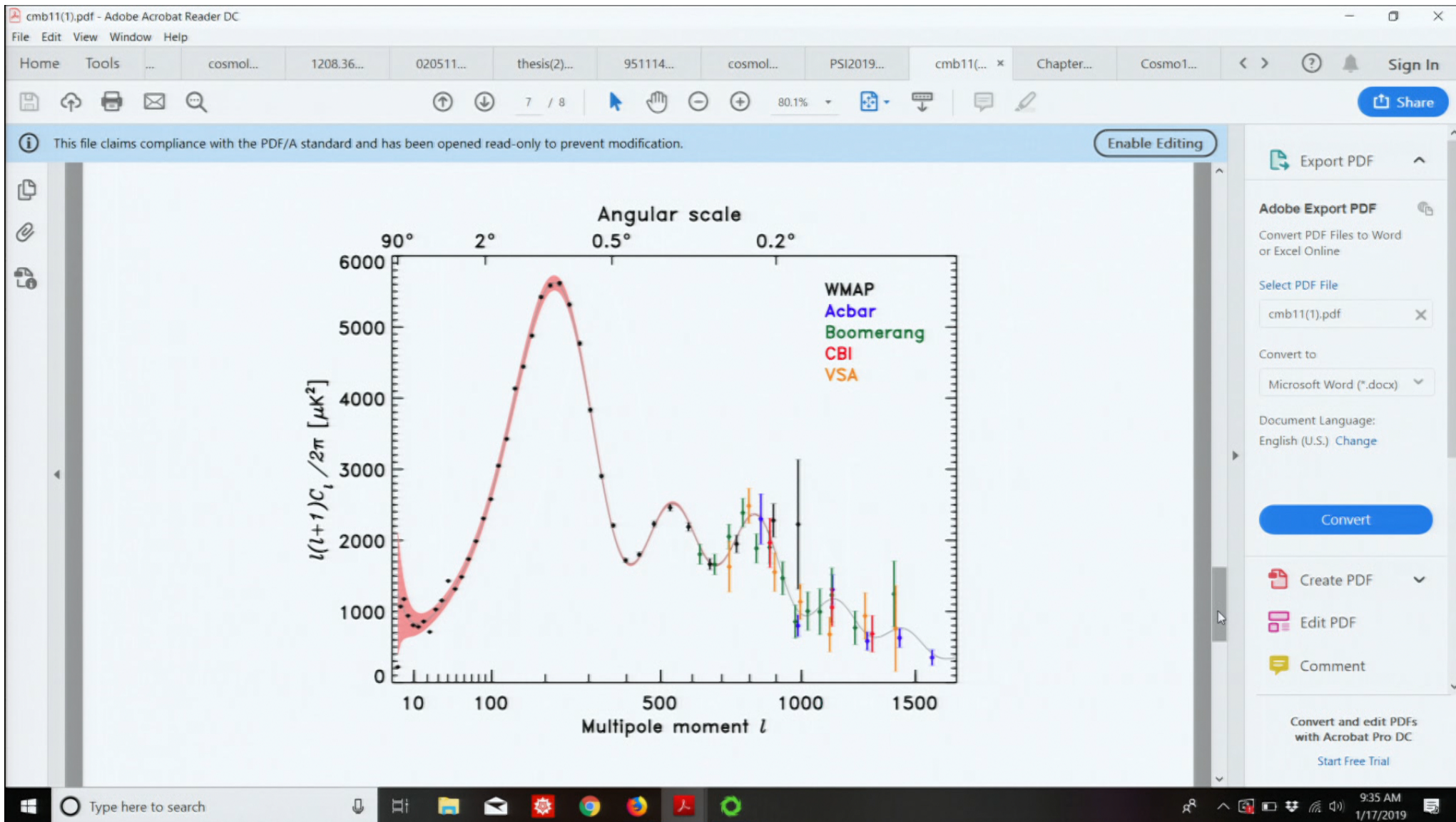
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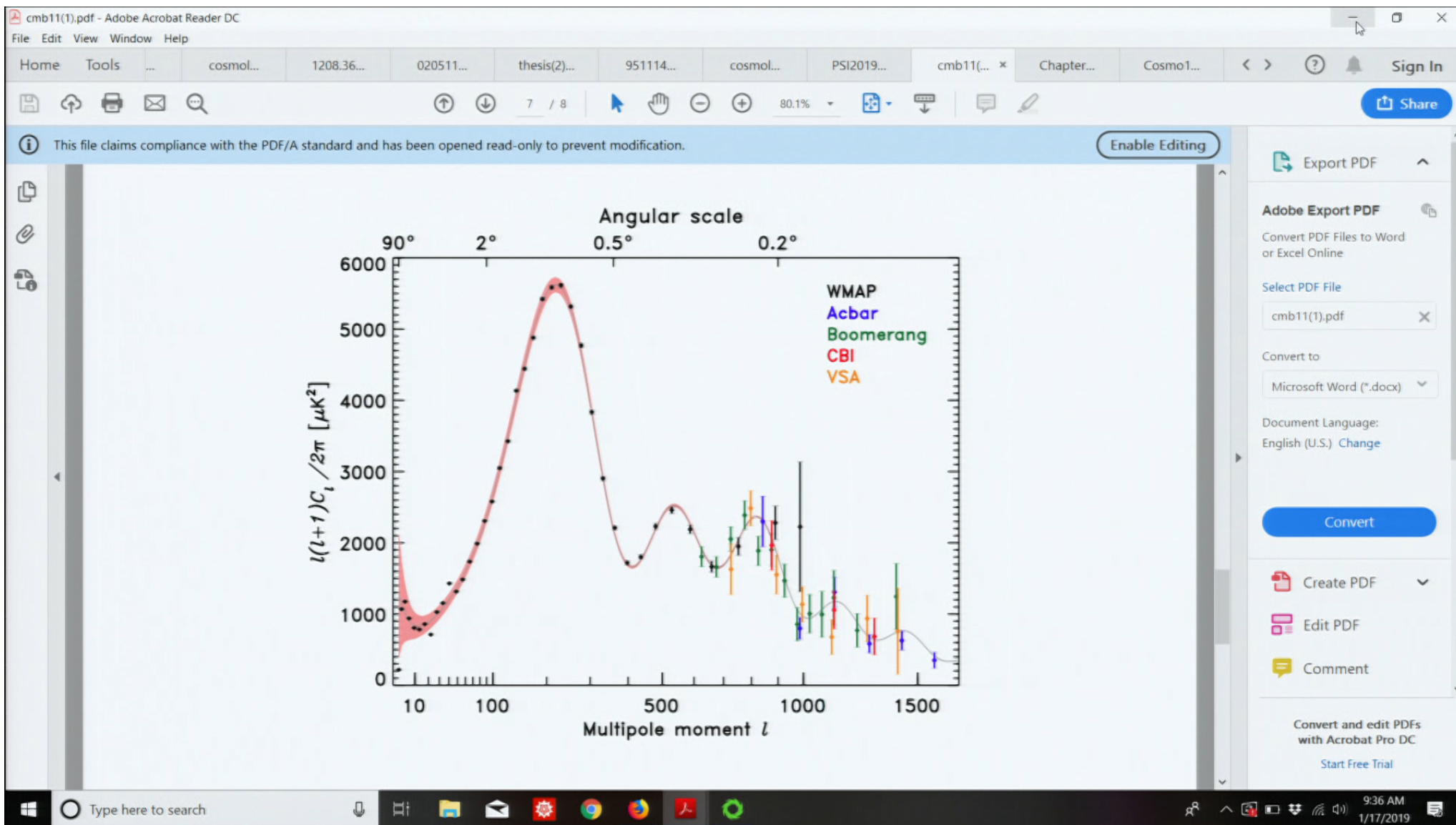
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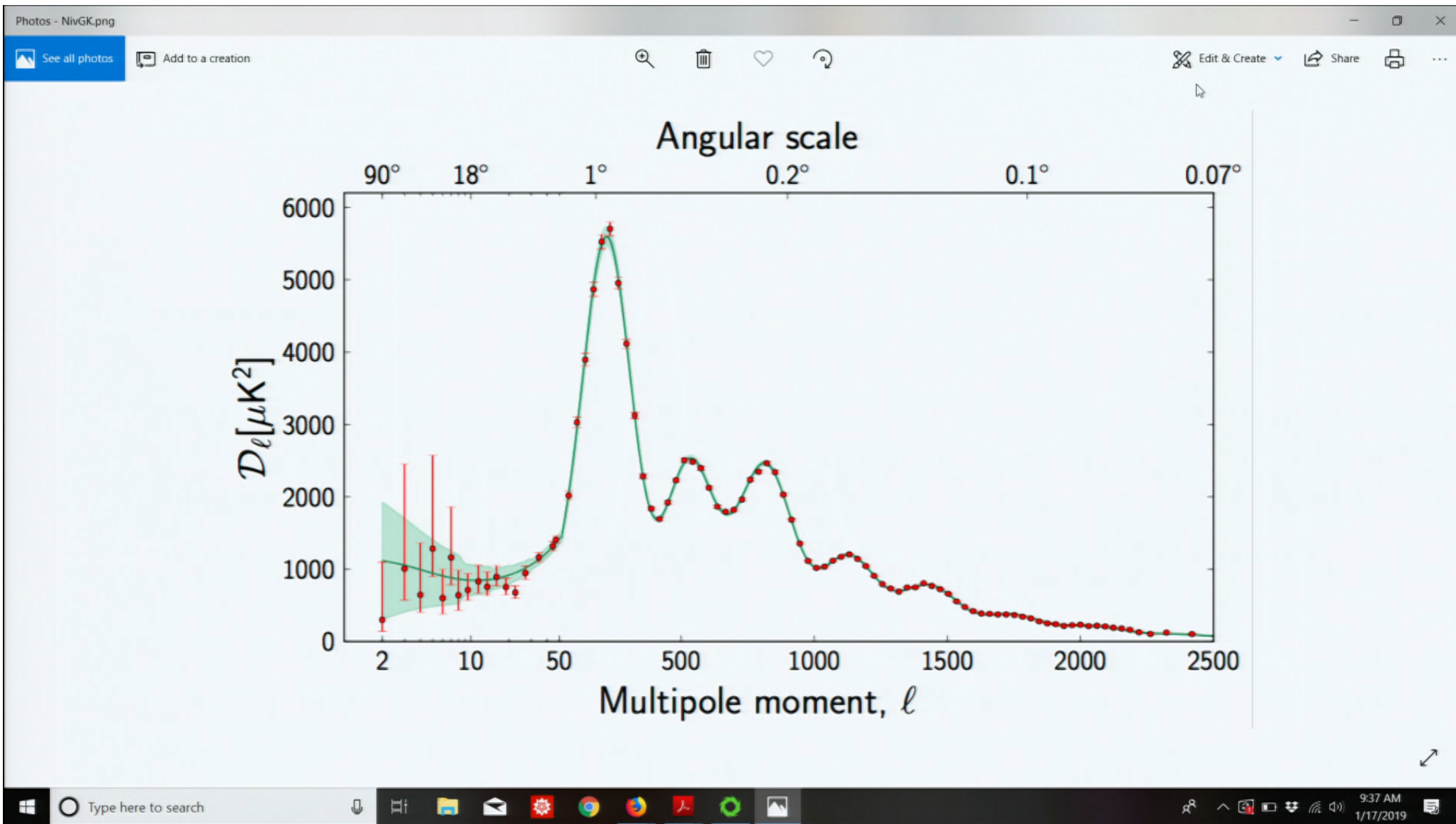
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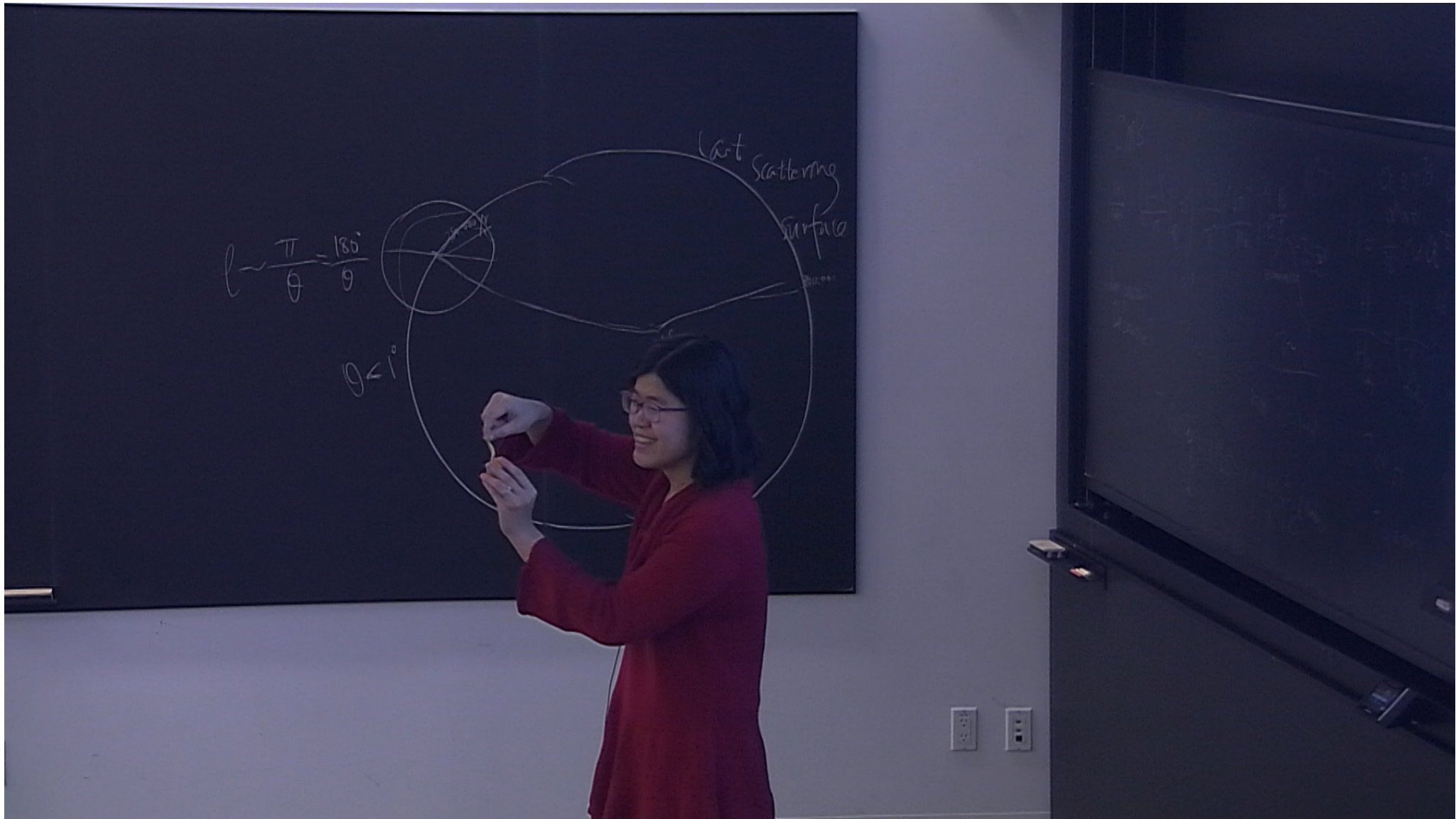
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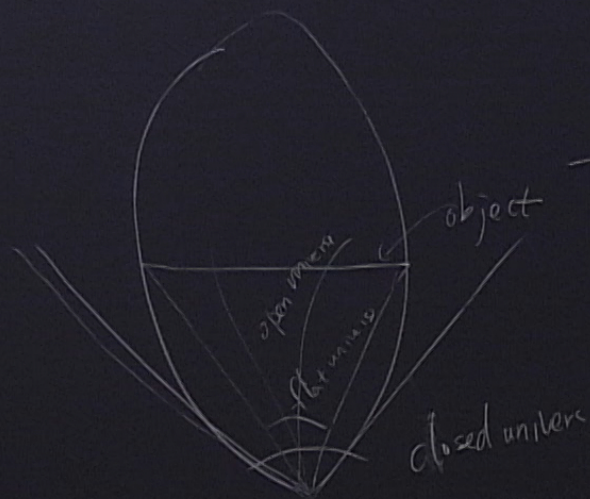
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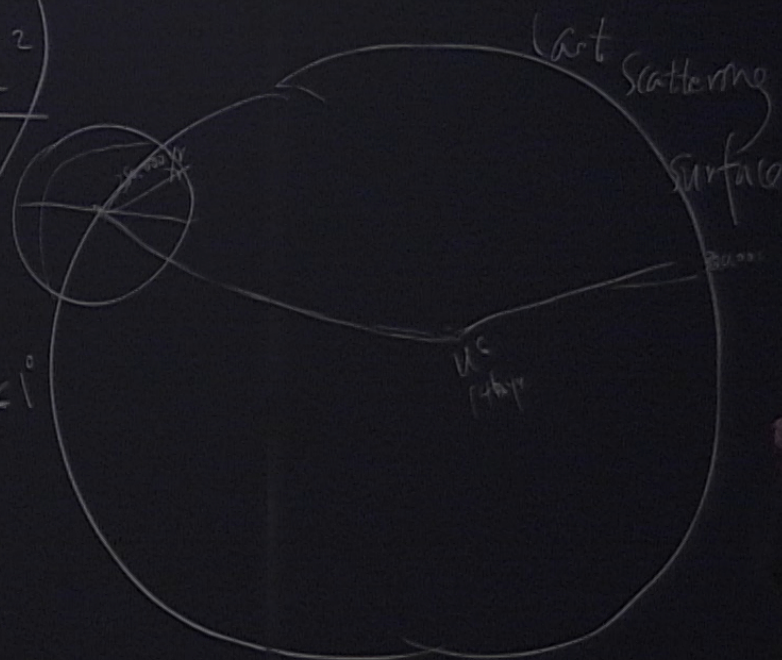


$$-dt^2 + dr^2 \left( \frac{1}{1-kr^2} \right) + r^2 d\Omega^2$$

$a(t=0)=1$

$$l \sim \frac{\pi}{\theta} = \frac{180^\circ}{\theta}$$

$$\theta < 1^\circ$$



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and many more parameters. To learn more about the parameters you are playing with and how they affect power spectrum, check out the [WMAP mission pages](#). Clues to the correct answer can also be found in the [News](#) and [Technical](#) portions of the WMAP web site.

USE THE SLIDERS TO MATCH THE **BLUE LINE** TO THE **RED LINE**

### CMB Analyzer

**Universe Content**

Atoms: 4 %

Cold Dark Matter: 22 %

Dark Energy: 74 %

**Additional Properties**

Hubble Constant: 84

Reionization redshift: 22

Spectral Index: 0.8

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

**Sky map:** This image shows the variation in CMB temperature across the entire sky. The map is shown in a Mollweide projection in Galactic coordinates. Temperature variations are scaled between -0.4 milliKelvin to 0.4 milliKelvin from a mean temperature of 2.73 Kelvin. There may be a small delay while the images loads.

**Age:** 11.7 billion years

**Flatness:** 1.00

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### CMB Analyzer

Universe Content

Atoms 4 %

Cold Dark Matter 74 %

Dark Energy 4 %

Additional Properties

Hubble Constant 84

Reionization redshift 22

Spectral Index 0.8

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

Atoms: The amount of ordinary matter (atoms) in your universe, as a percentage of the critical density.

Age: .2 billion years

Flatness: 0.2

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#### The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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### CMB Analyzer



Universe Content

Atoms 4 %

Cold Dark Matter 22 %

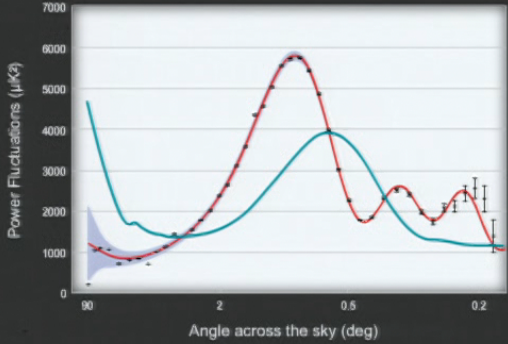
Dark Energy 4 %

Additional Properties

Hubble Constant 84

Reionization redshift 22

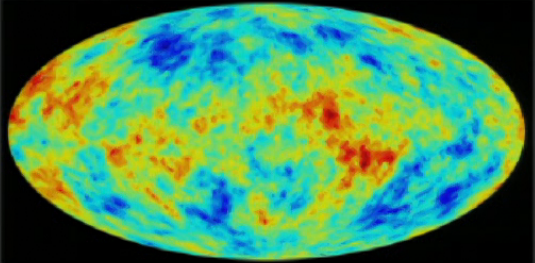
Spectral Index 0.8



Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

**Cold Dark Matter:** The amount of cold dark matter in your universe, as a percentage of the critical density. Cold dark matter cannot be seen or felt, and has not been detected in the laboratory, but it does exert a gravitational pull.



Age: 9.7 billion years

Flatness: 0.30

ANSWER RESET

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#### The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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CMB Analyzer

Universe Content

Atoms

4 %

Cold Dark Matter

22 %

Dark Energy

4 %

Additional Properties

Hubble Constant

84

Reionization redshift

22

Spectral Index

0.8

7000

6000

5000

4000

3000

2000

1000

0

90

2

0.5

0.2

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

Dark Energy: The amount of dark energy in your universe, as a percentage of the critical density. Unlike cold dark matter, dark energy exerts a gravitational push (a form of anti-gravity) that is causing the expansion of the universe to accelerate or speed up.

Age: 9.7 billion years

Flatness: 0.30

ANSWER

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The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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### CMB Analyzer



Universe Content

Atoms 4 %

Cold Dark Matter 22 %

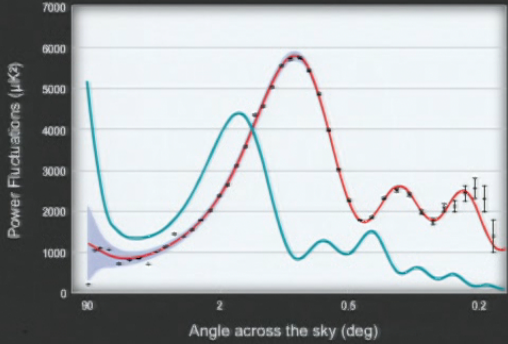
Dark Energy 100 %

Additional Properties

Hubble Constant 84

Reionization redshift 22

Spectral Index 0.8



Power Fluctuations ( $\mu K^2$ )

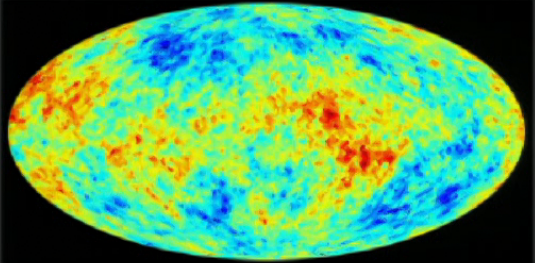
Angle across the sky (deg)

**Dark Energy:** The amount of dark energy in your universe, as a percentage of the critical density. Unlike cold dark matter, dark energy exerts a gravitational push (a form of anti-gravity) that is causing the expansion of the universe to accelerate or speed up.

**Age:** 13.0 billion years

**Flatness:** 1.26

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#### The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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### CMB Analyzer

Universe Content

Atoms 4 %

Cold Dark Matter 22 %

Dark Energy 74 %

Additional Properties

Hubble Constant 84

Reionization redshift 22

Spectral Index 0.8

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

**Dark Energy:** The amount of dark energy in your universe, as a percentage of the critical density. Unlike cold dark matter, dark energy exerts a gravitational push (a form of anti-gravity) that is causing the expansion of the universe to accelerate or speed up.

**Age:** 11.7 billion years

**Flatness:** 1.00

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#### The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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### CMB Analyzer

Universe Content

Atoms 4 %

Cold Dark Matter 22 %

Dark Energy 74 %

Additional Properties

Hubble Constant 84

Reionization redshift 22

Spectral Index 0.8

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

**Dark Energy:** The amount of dark energy in your universe, as a percentage of the critical density. Unlike cold dark matter, dark energy exerts a gravitational push (a form of anti-gravity) that is causing the expansion of the universe to accelerate or speed up.

**Age:** 11.7 billion years

**Flatness:** 1.00

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#### The Graph

The early structure of the universe as seen in the CMB can be represented by an angular power spectrum, a plot that shows how the temperature pattern in the early universe varies with progressively measuring smaller and smaller patches of the sky. This in turn reveals the amount of energy emitted by different sized "ripples" of sound echoing through the early matter of

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Universe Content

Atoms

4 %

Cold Dark Matter

22 %

Dark Energy

74 %

Additional Properties

Hubble Constant

73

Reionization redshift

22

Spectral Index

0.8

7000

6000

5000

4000

3000

2000

1000

0

90

2

0.5

0.2

Power Fluctuations ( $\mu K^2$ )

Angle across the sky (deg)

Hubble Constant:

The current expansion rate of your universe, in km/sec per megaparsec. It is a measure of how fast of an object is moving away from us based upon its distance from the Earth today.

Age:

13.7 billion years

Flatness:

1.00

ANSWER

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The Graph

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