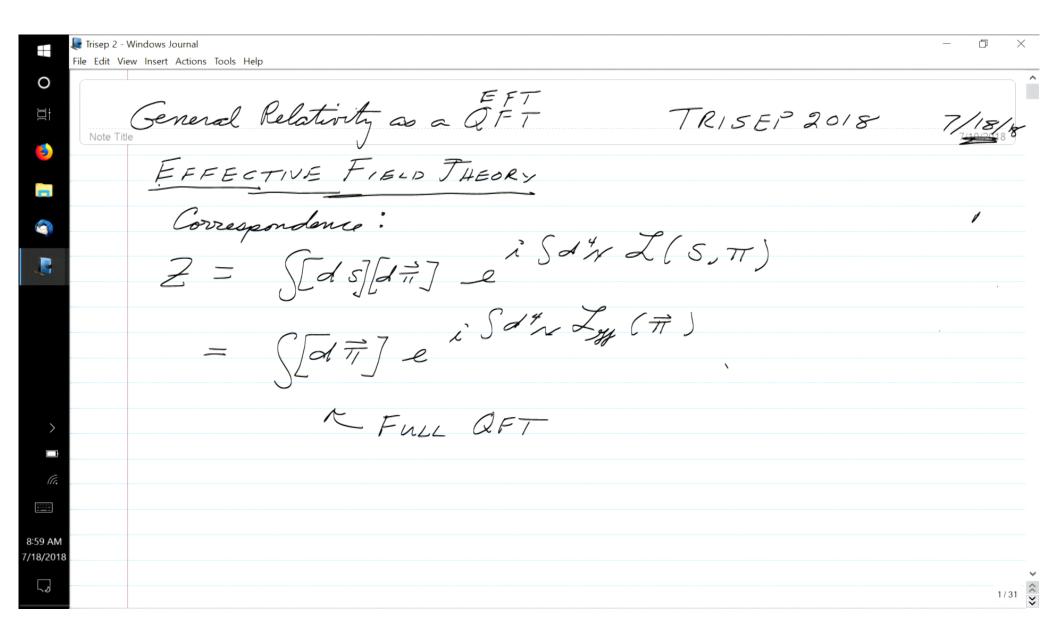
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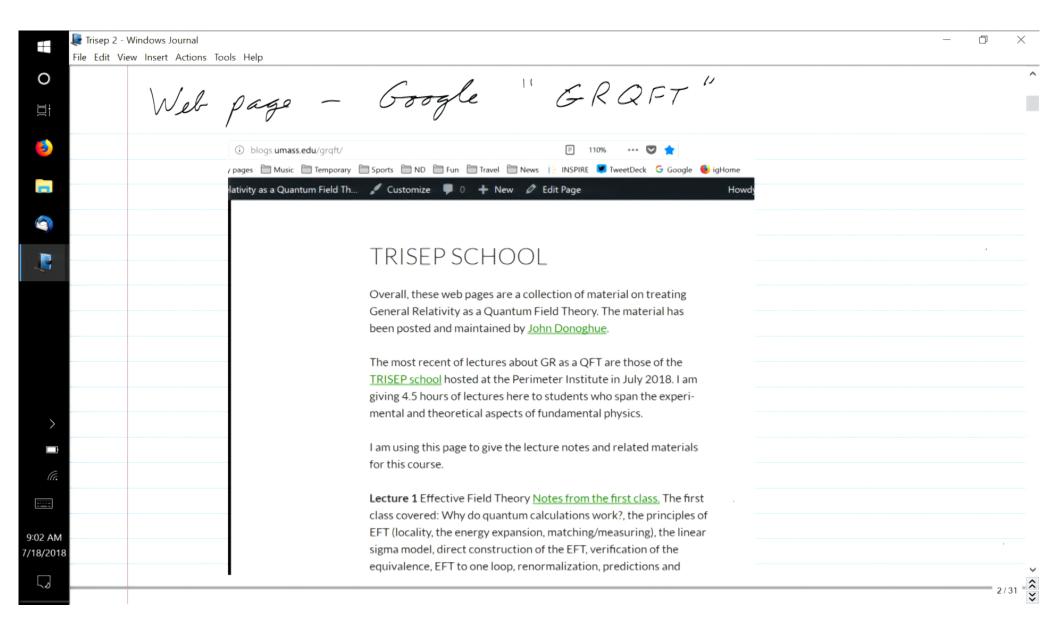
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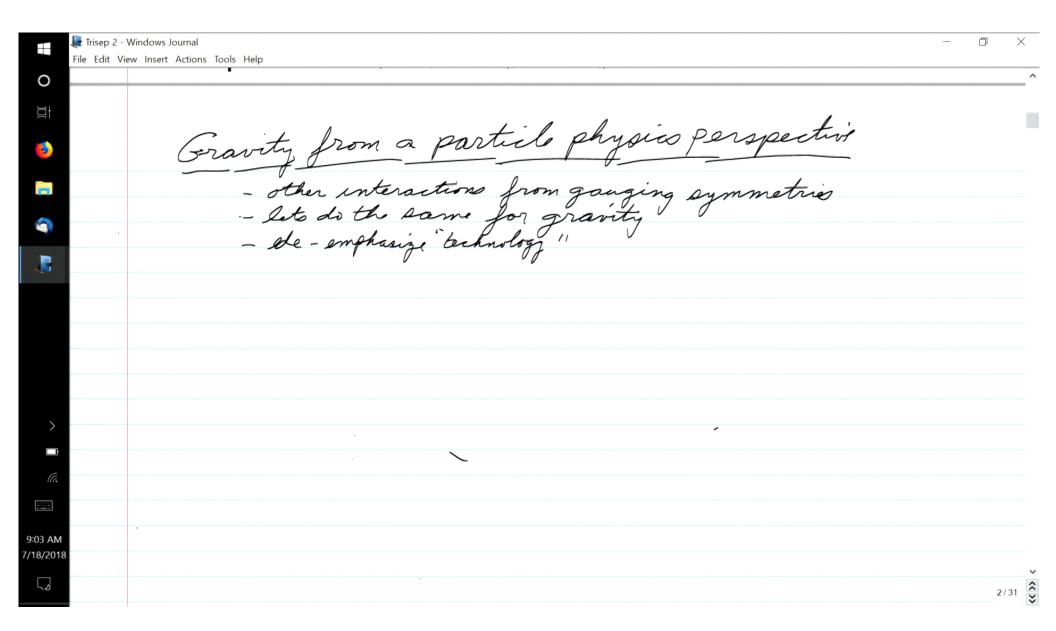
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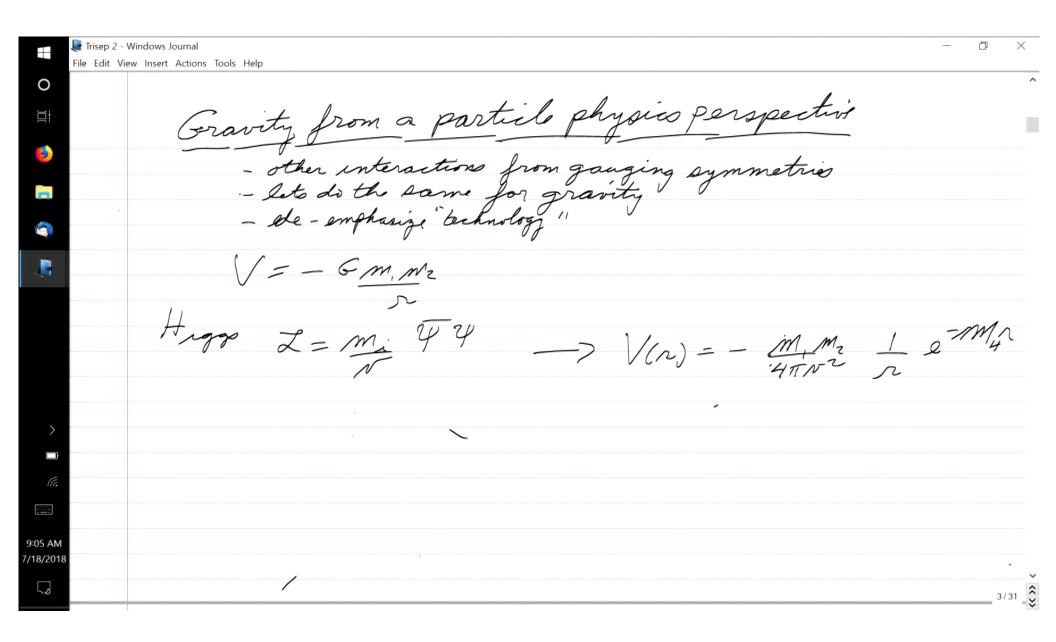


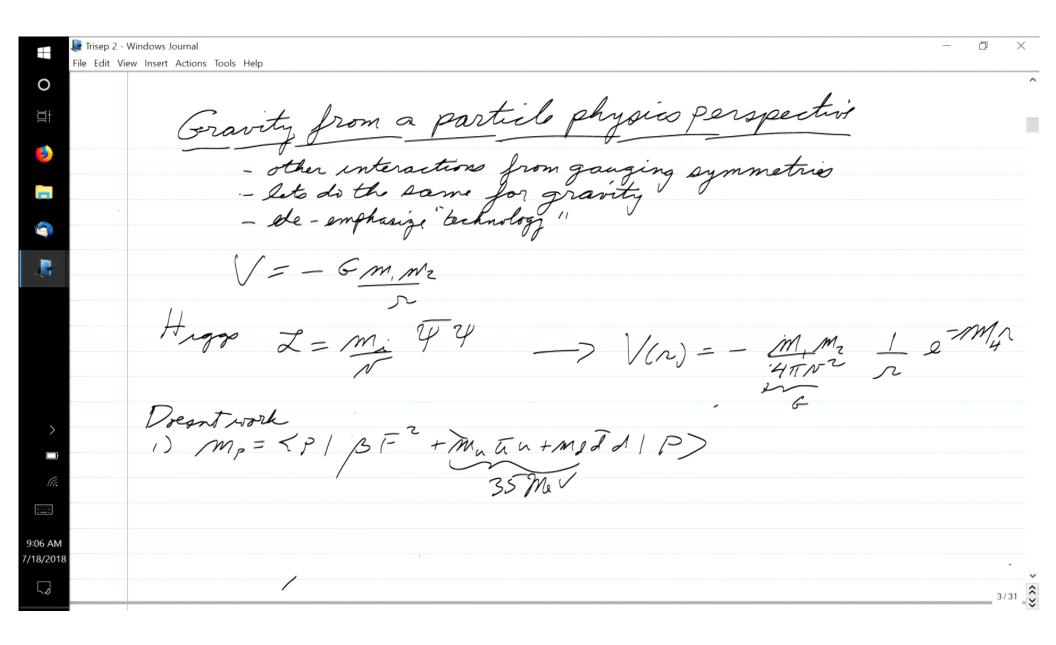


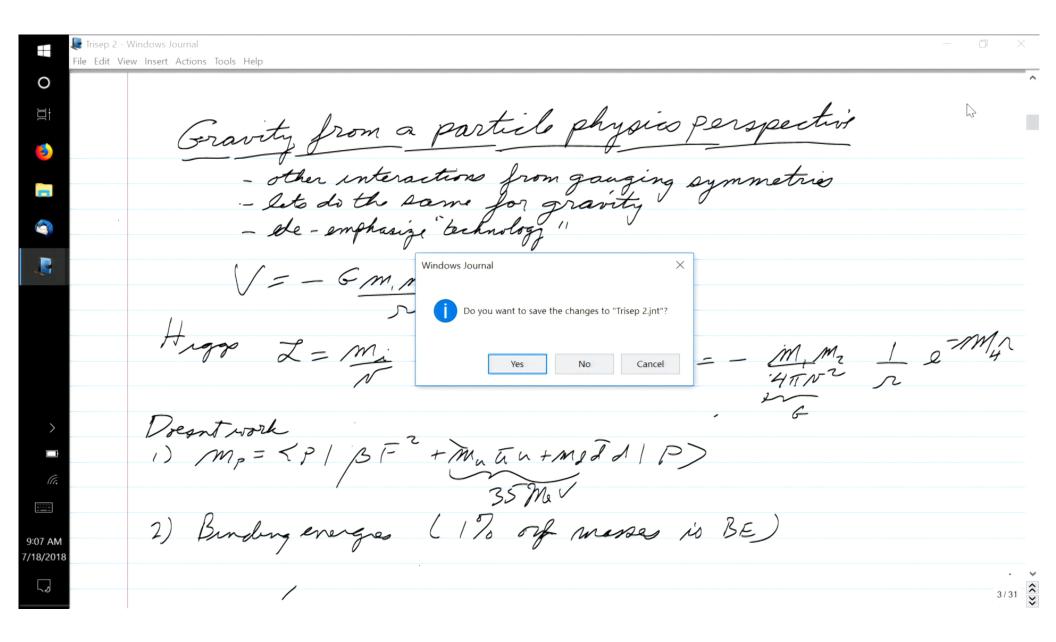


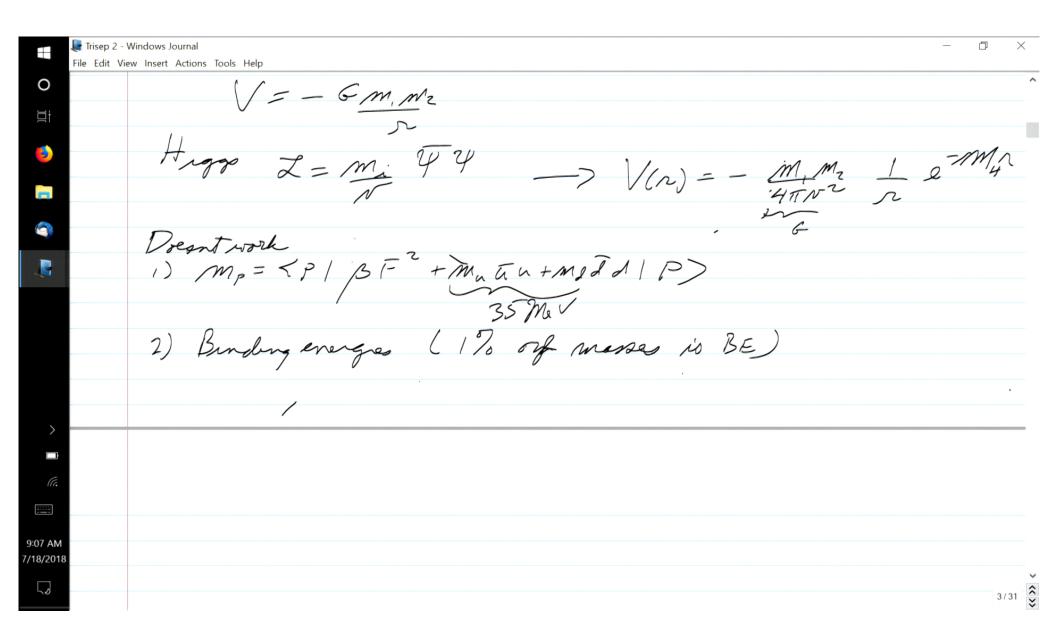
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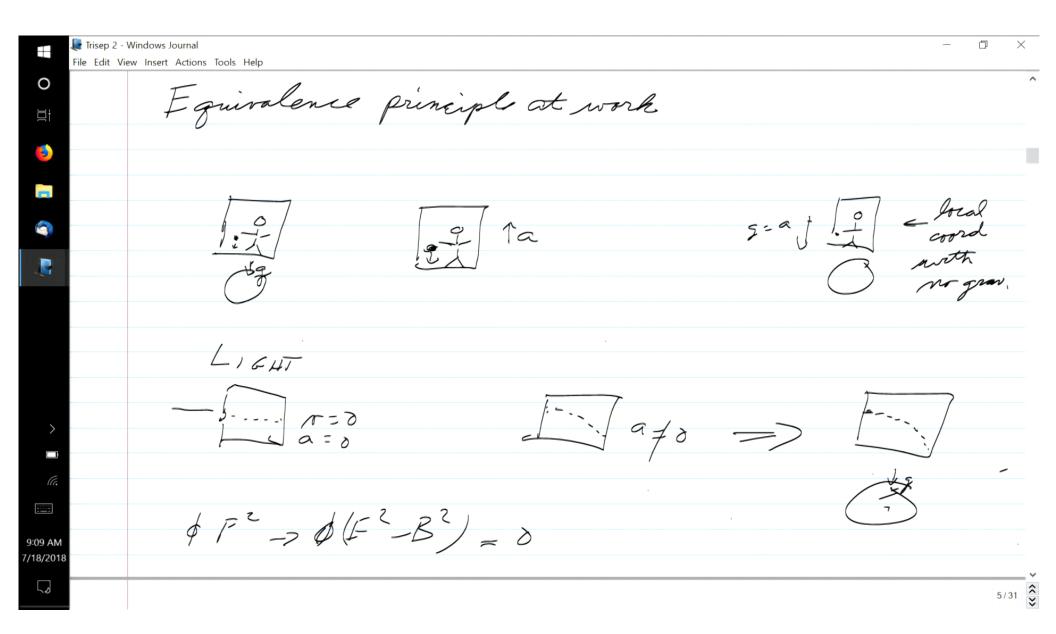


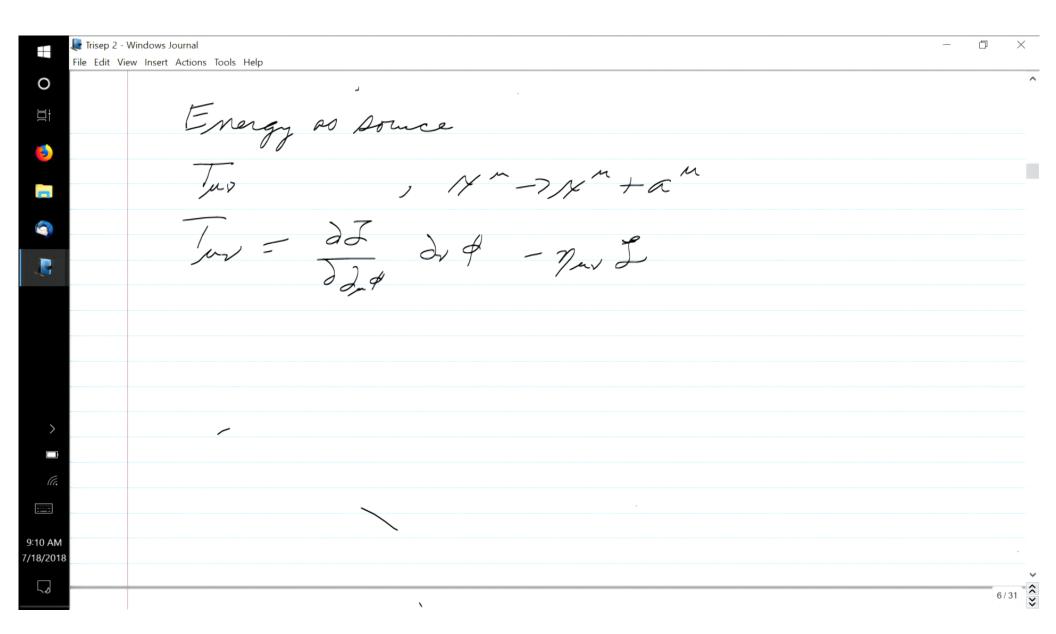


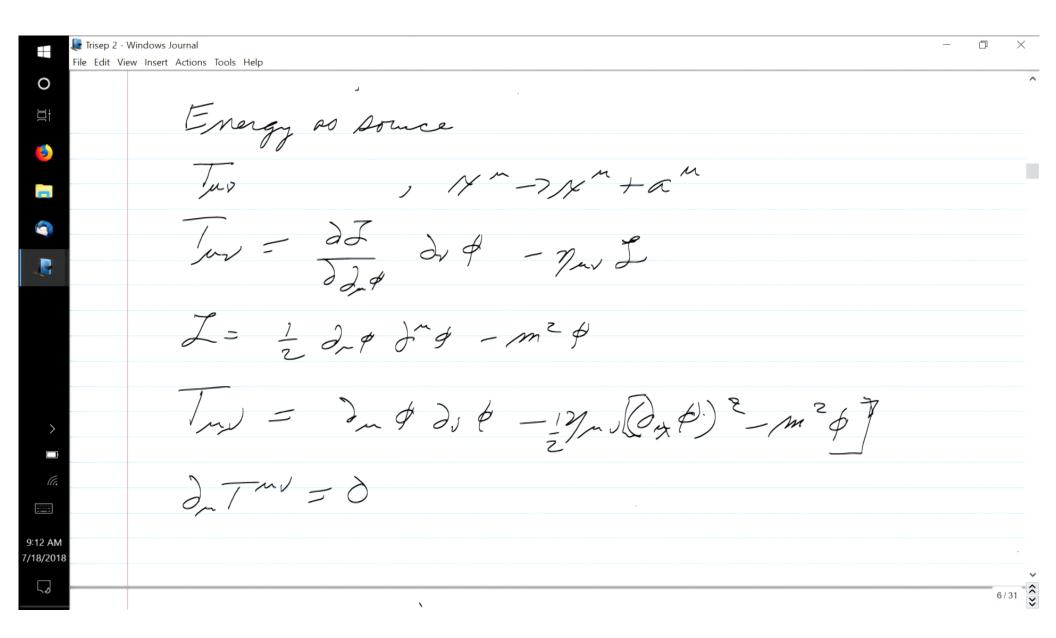


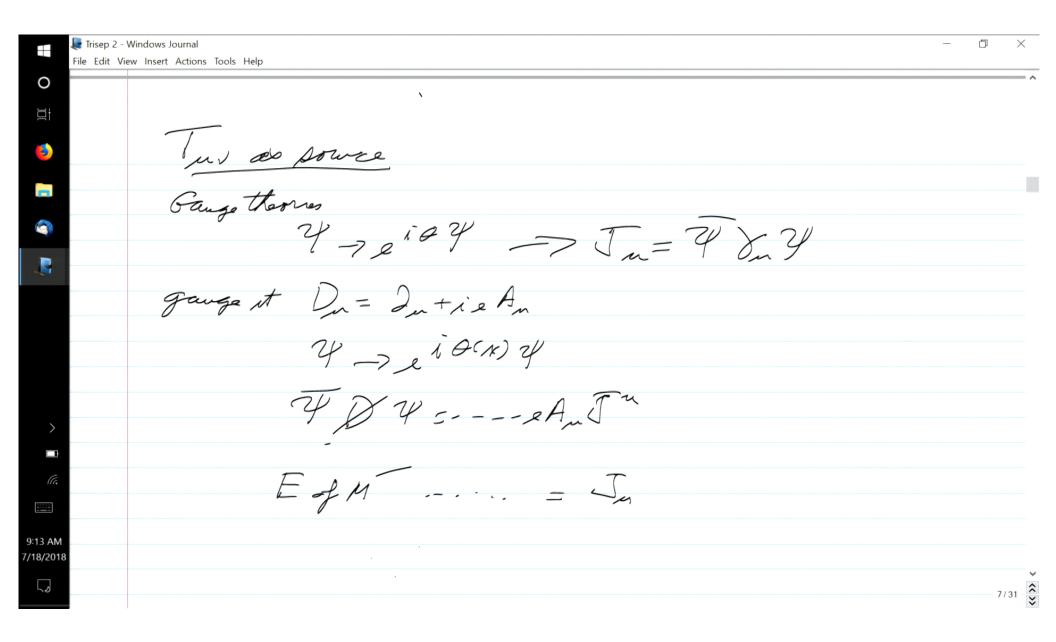


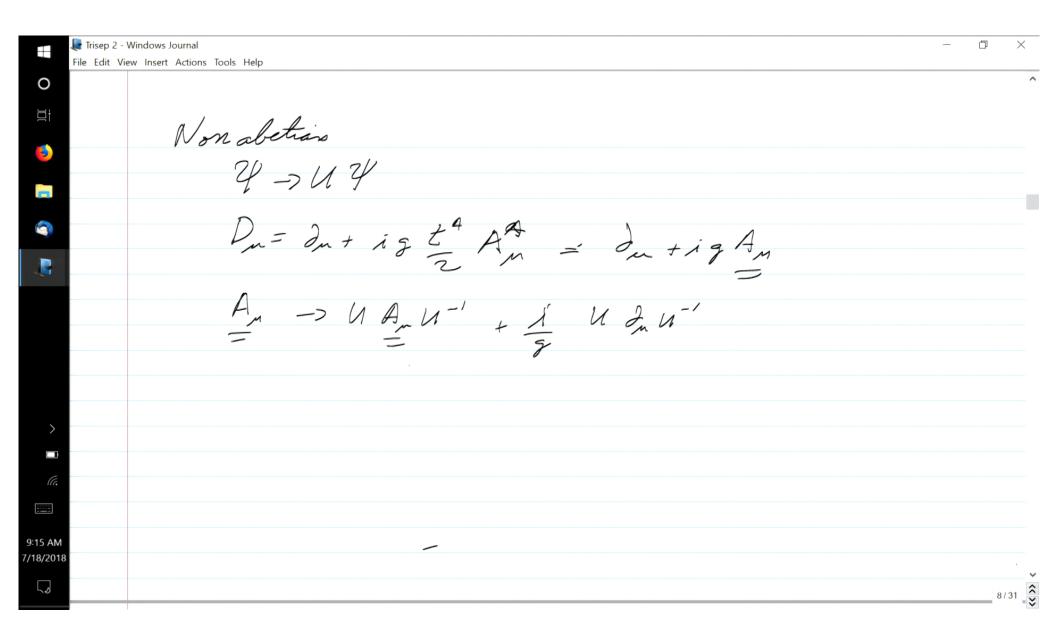


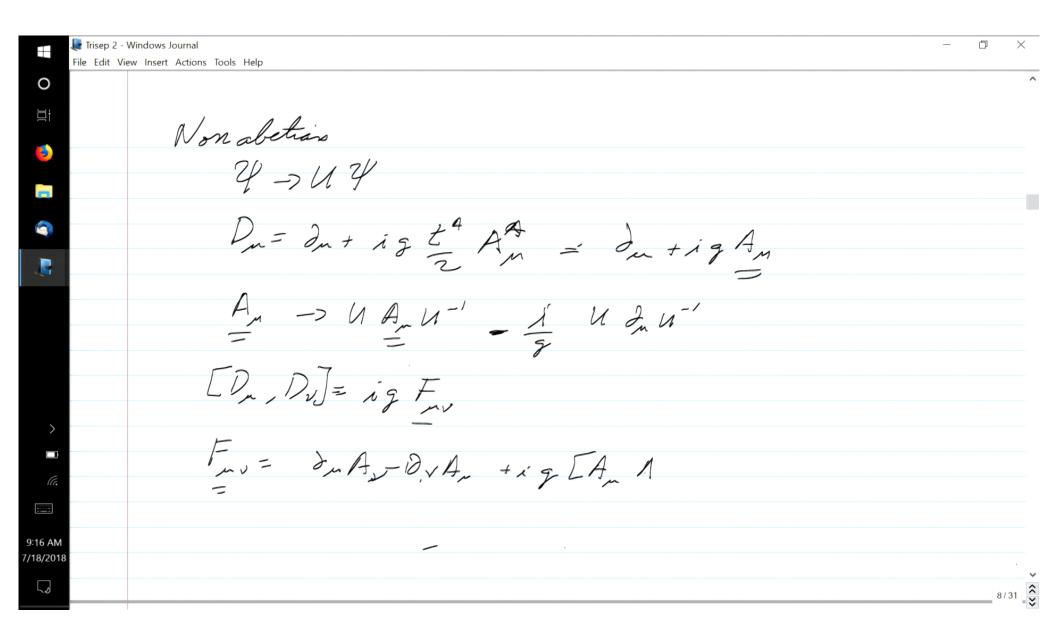


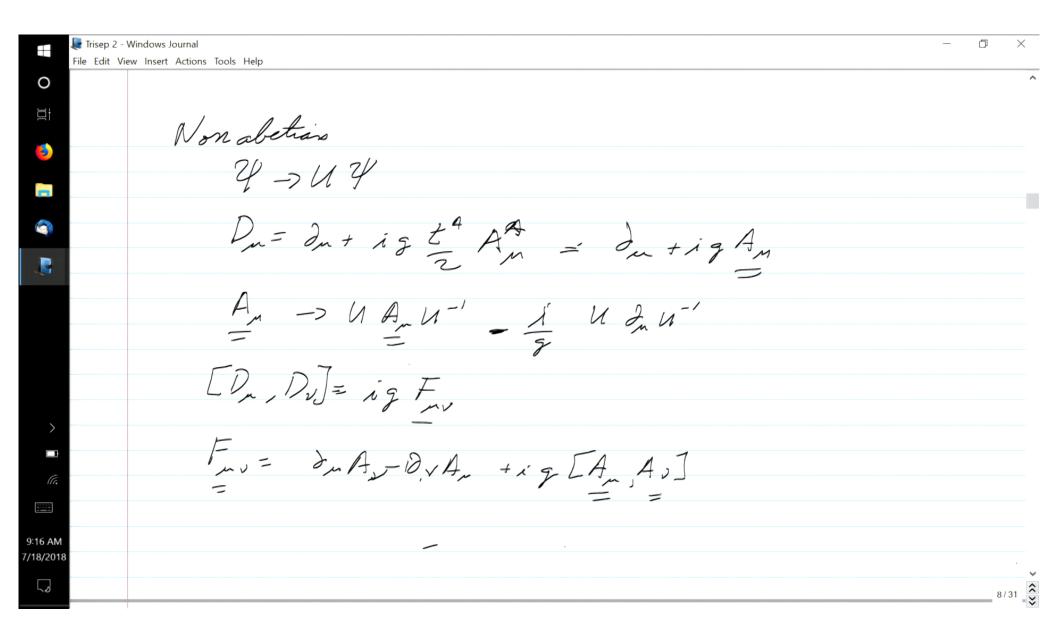


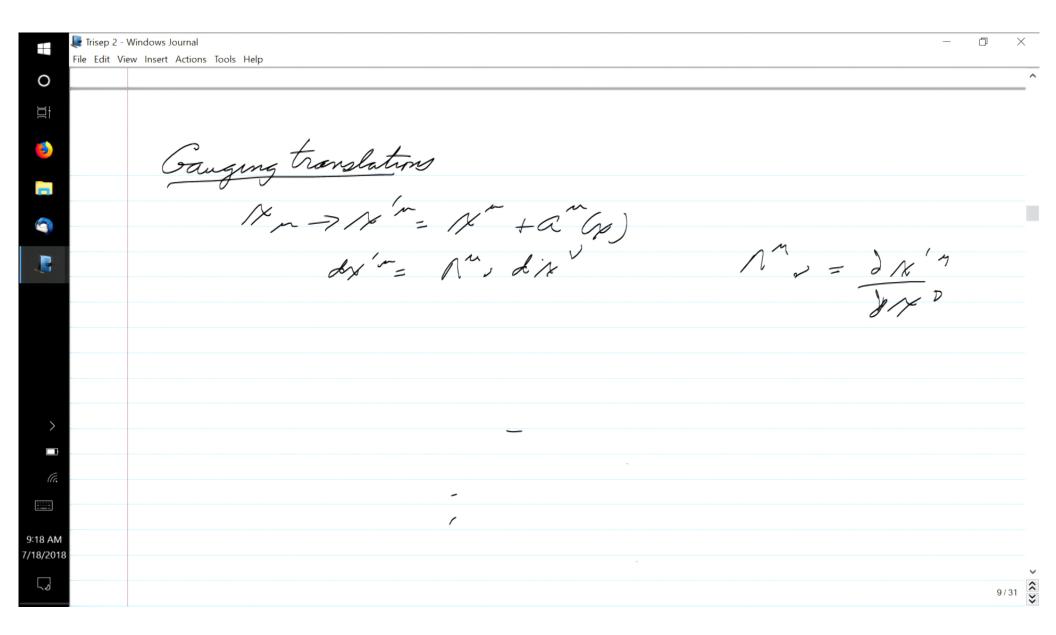


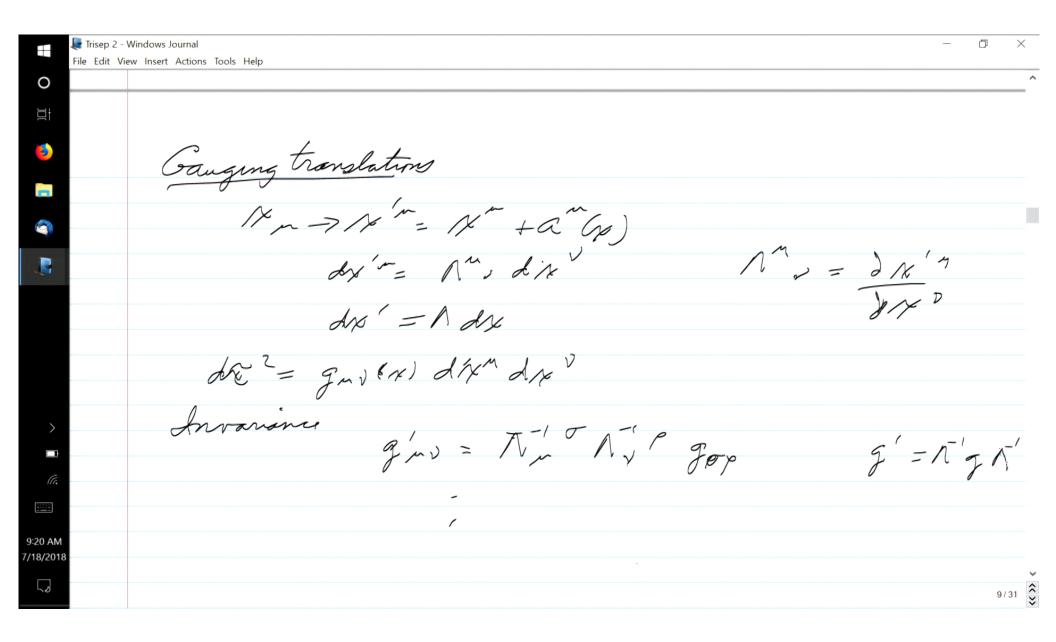


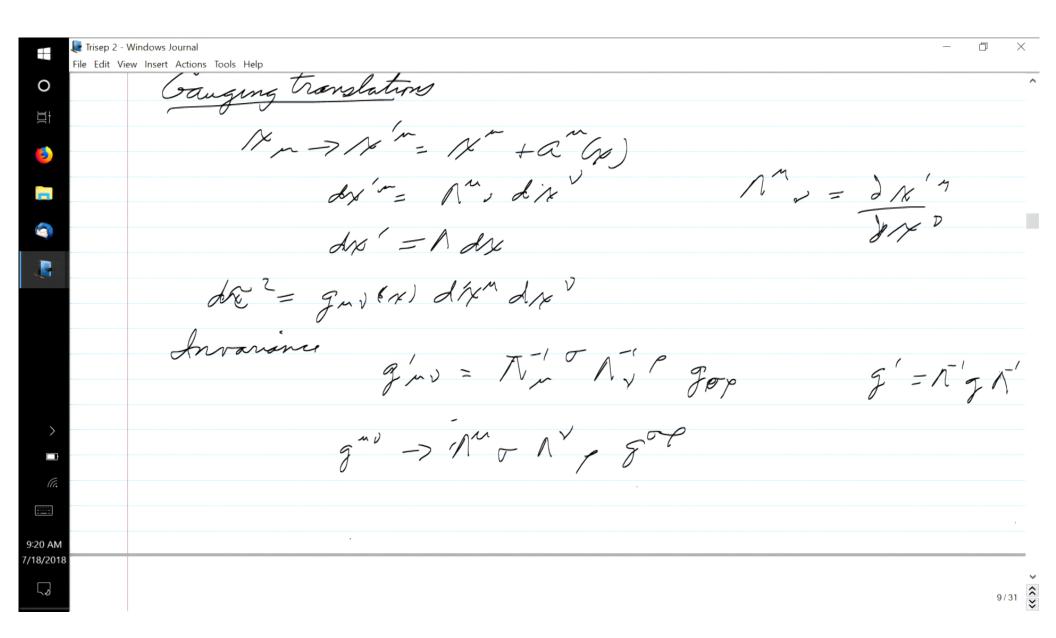


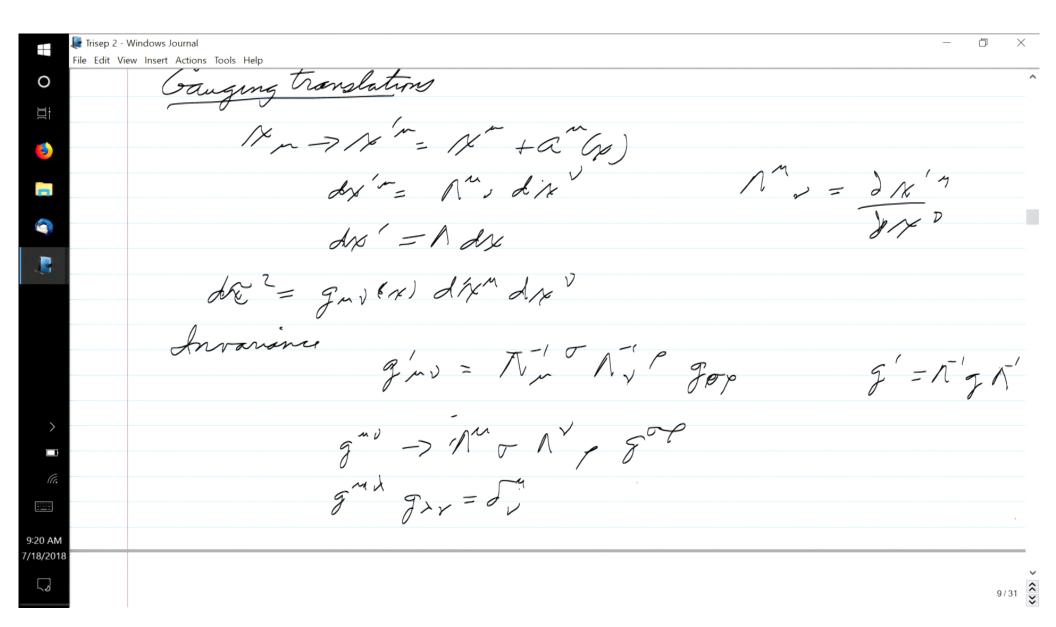


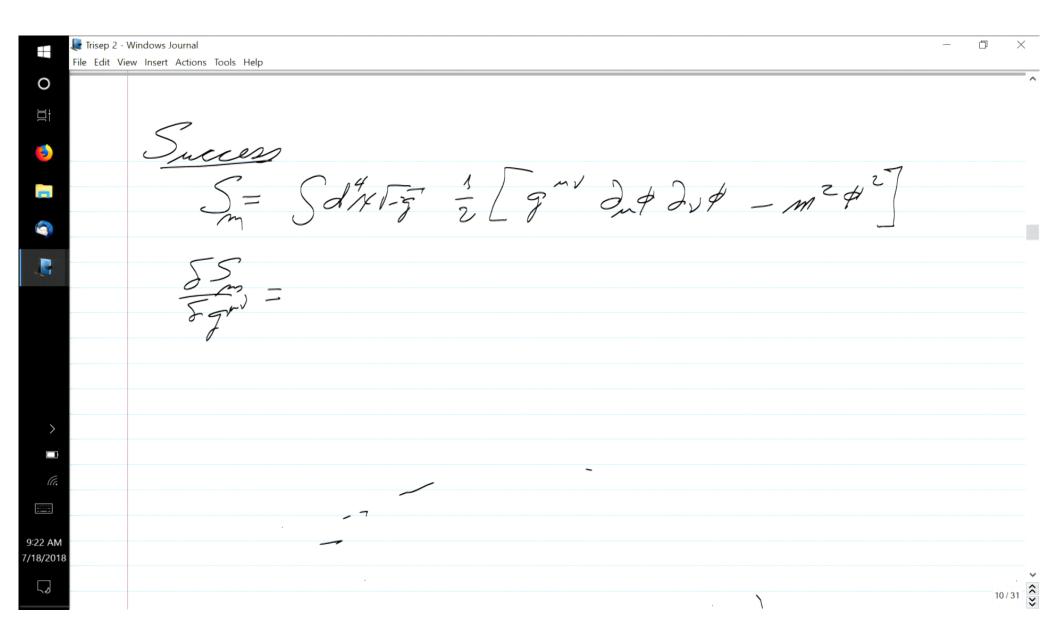


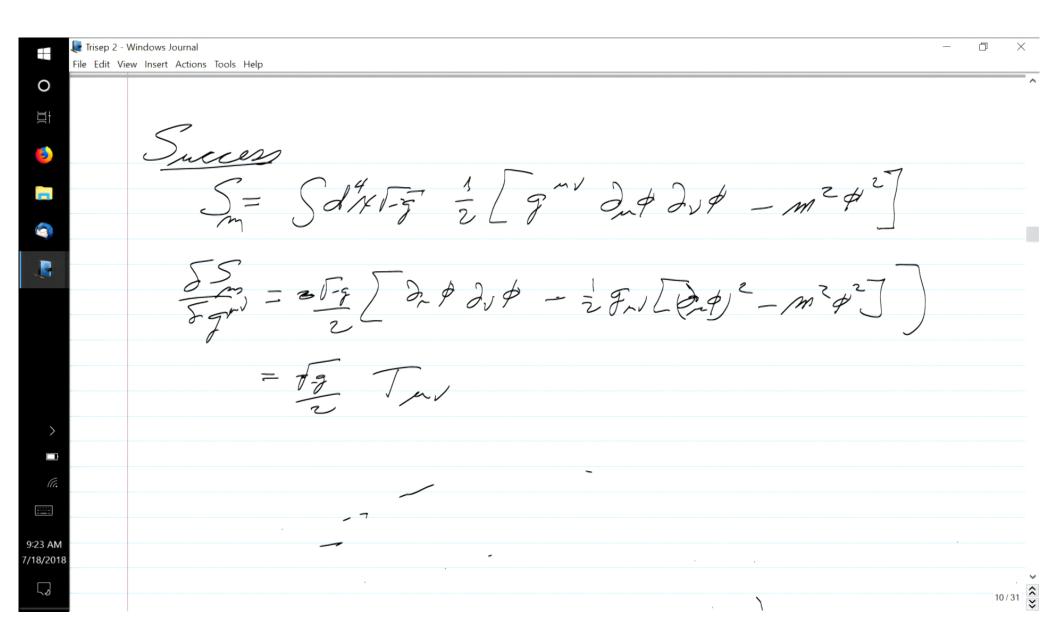


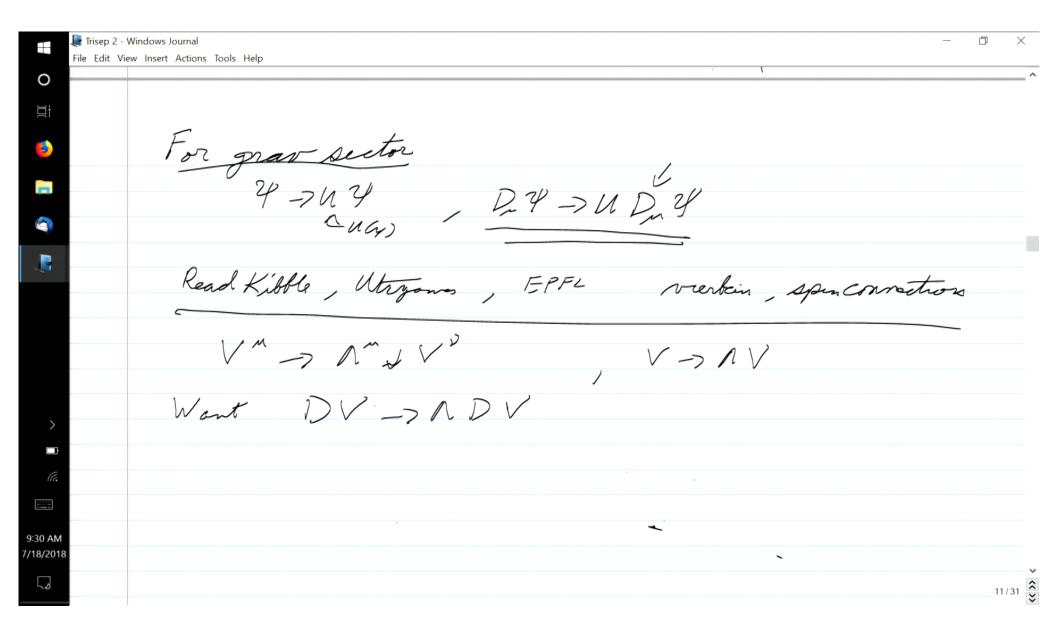


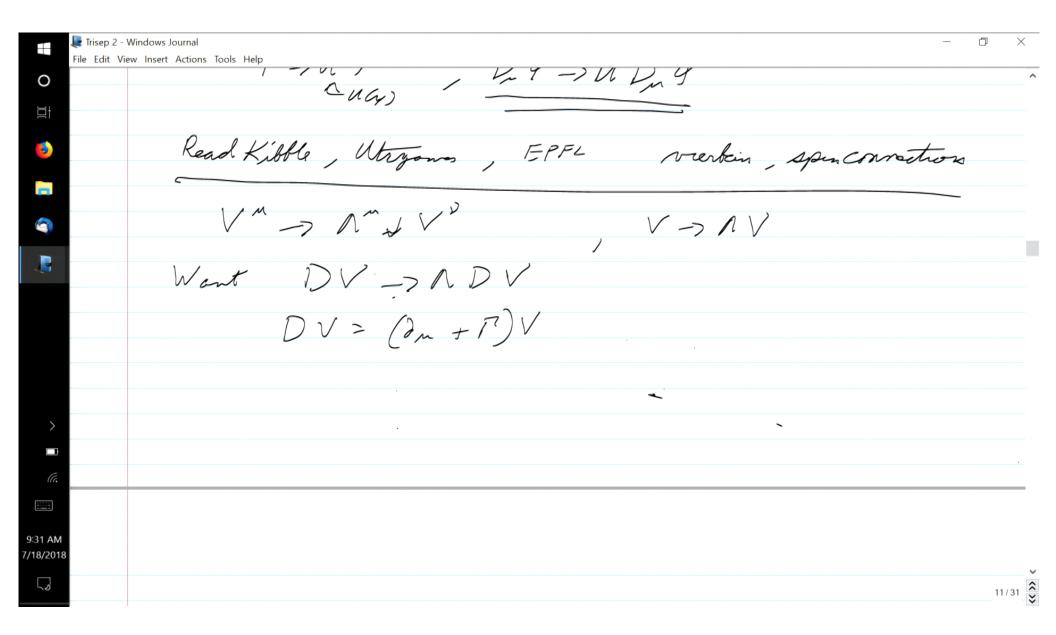


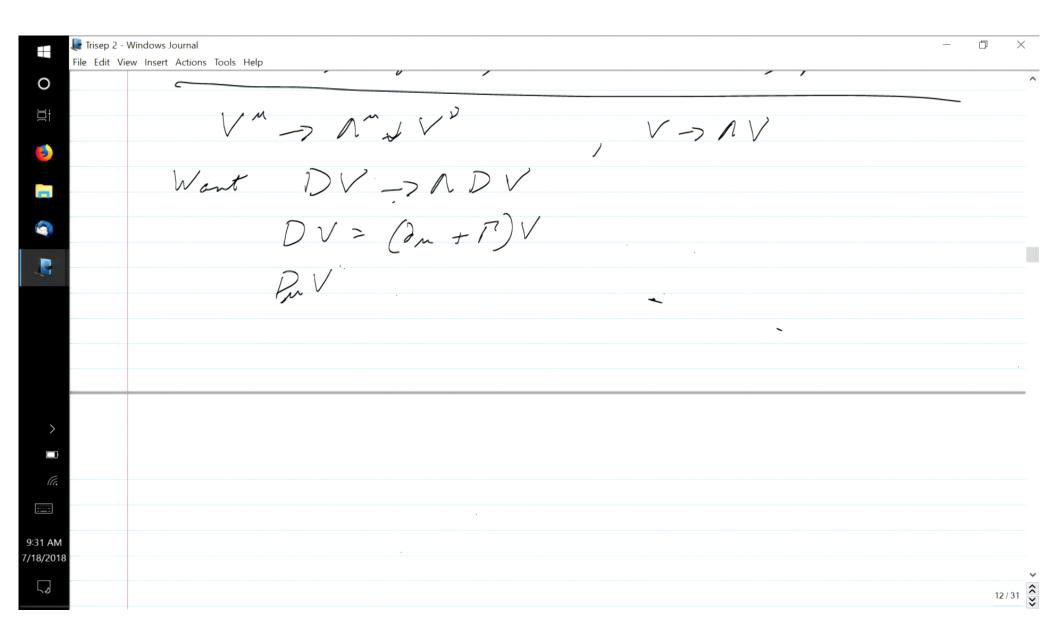


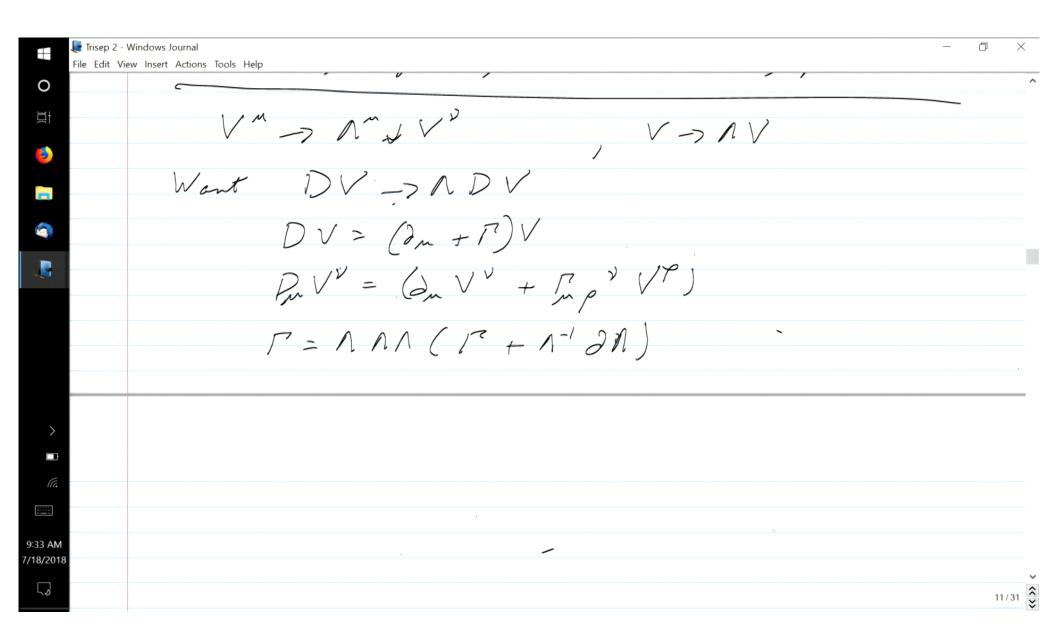


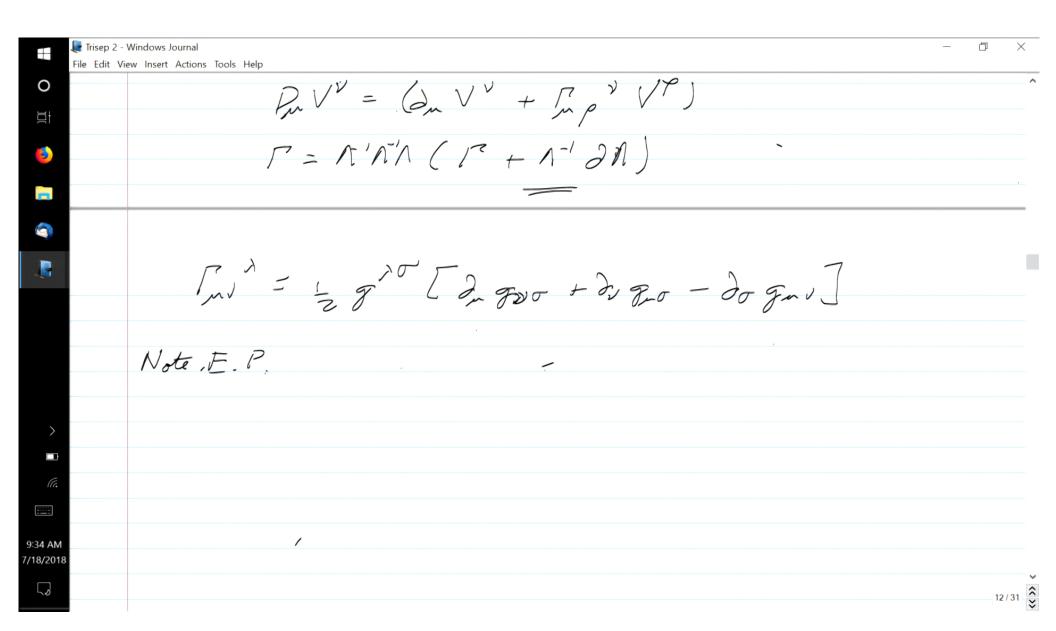


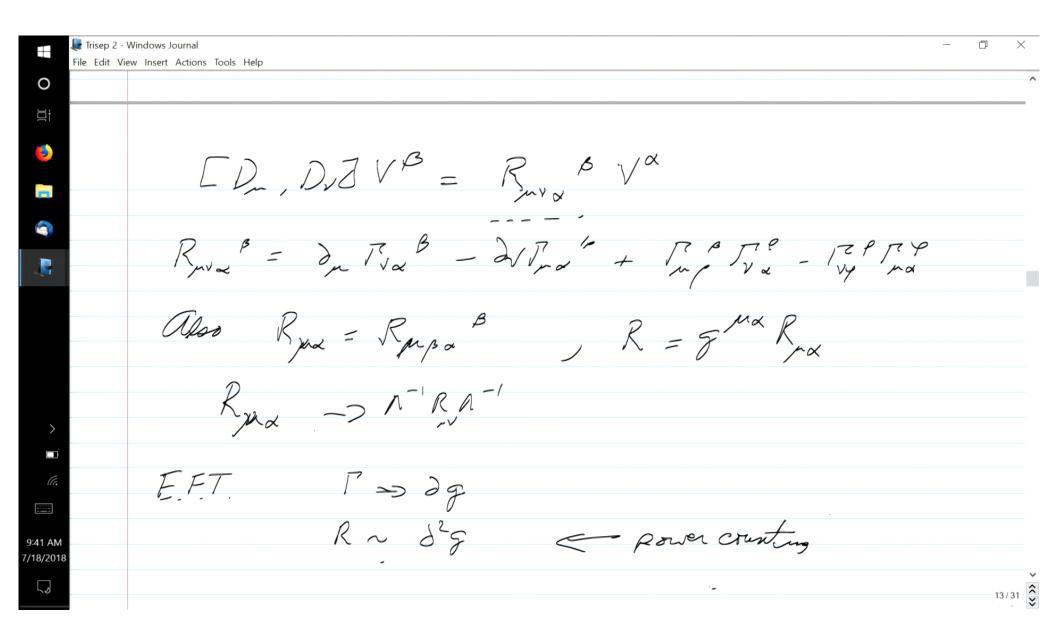


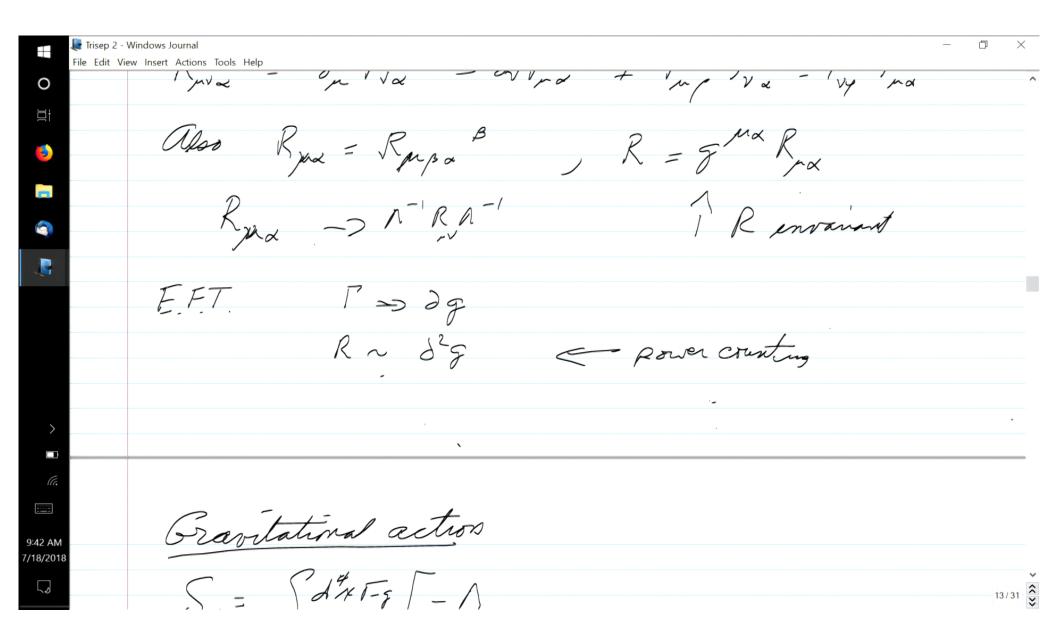


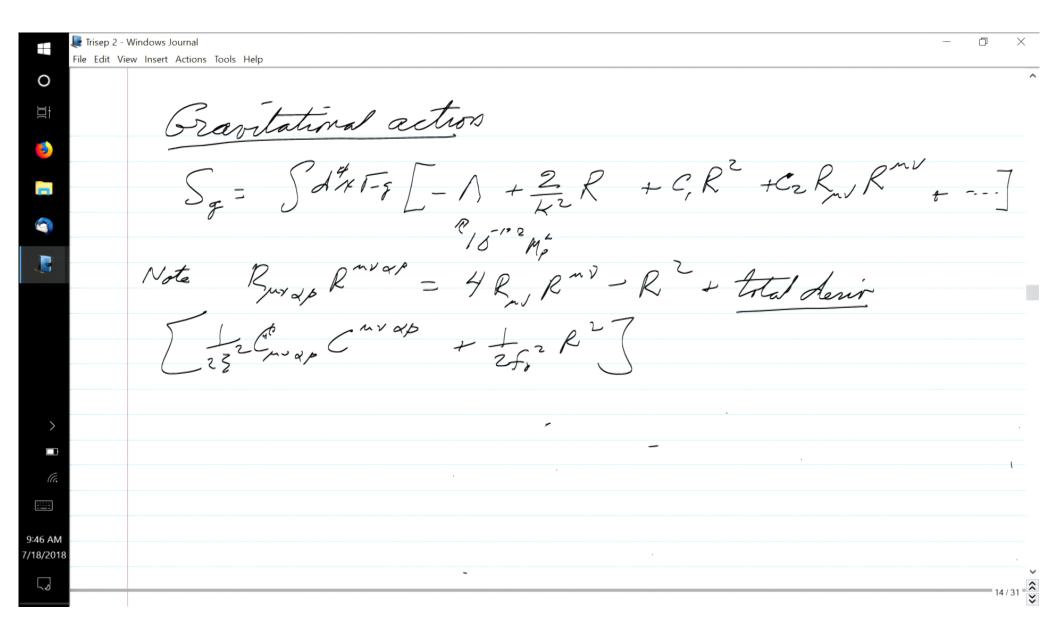


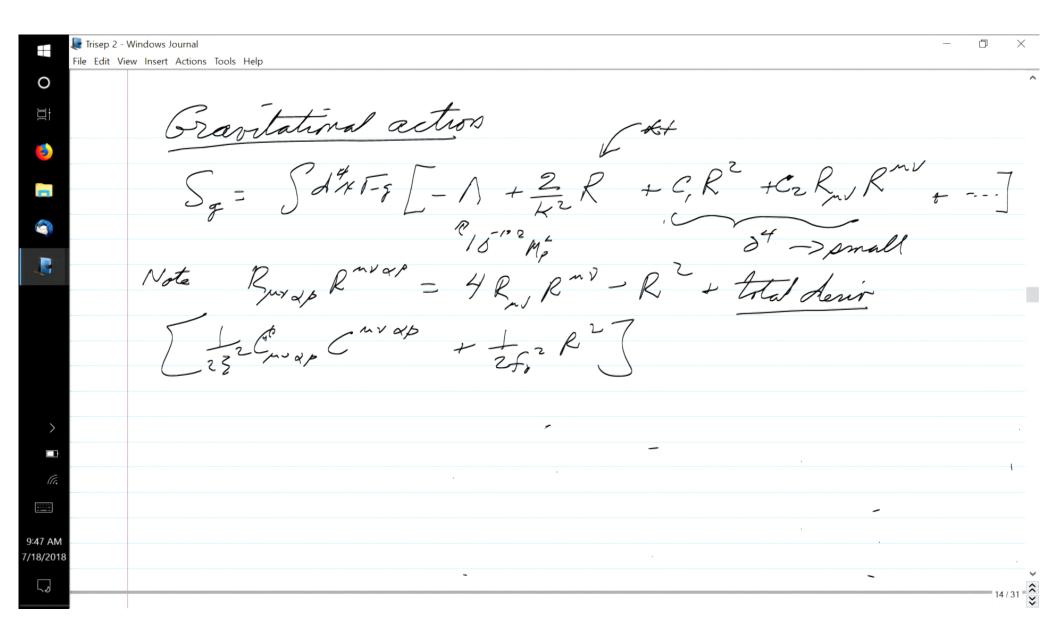


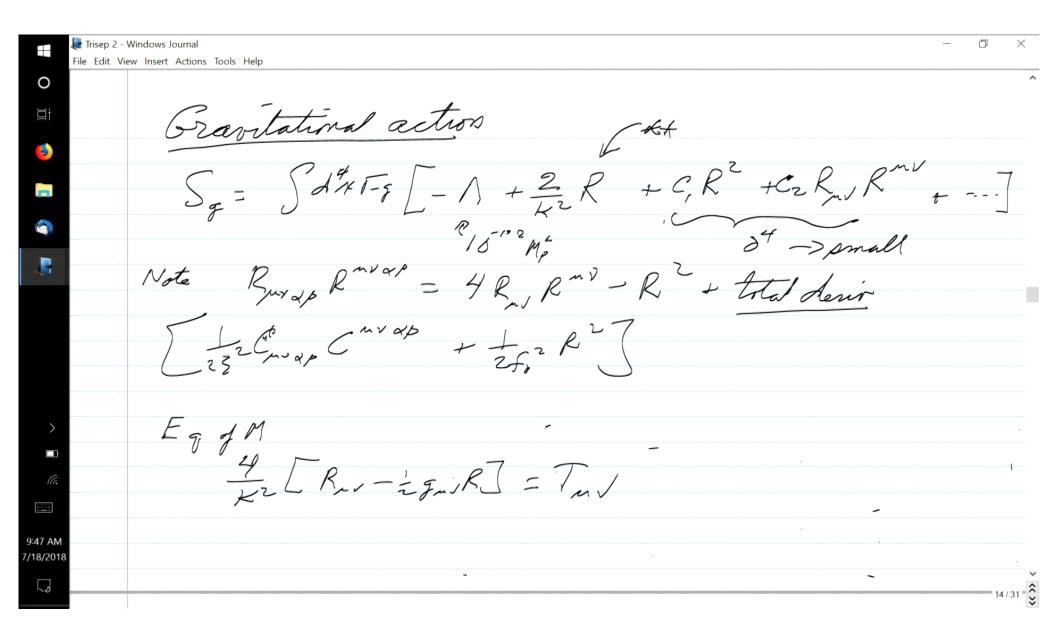


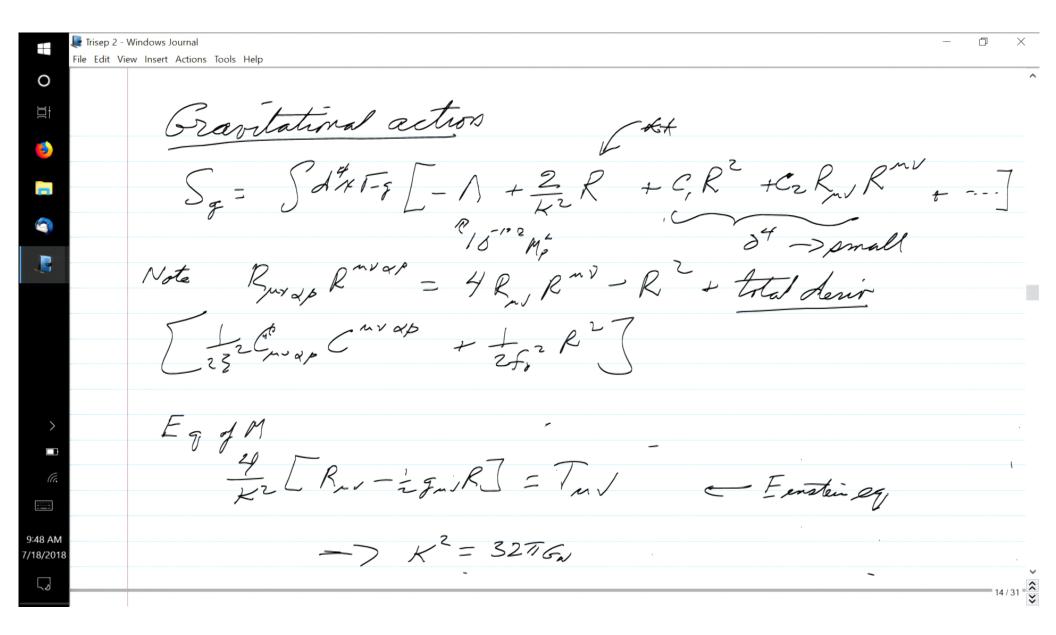


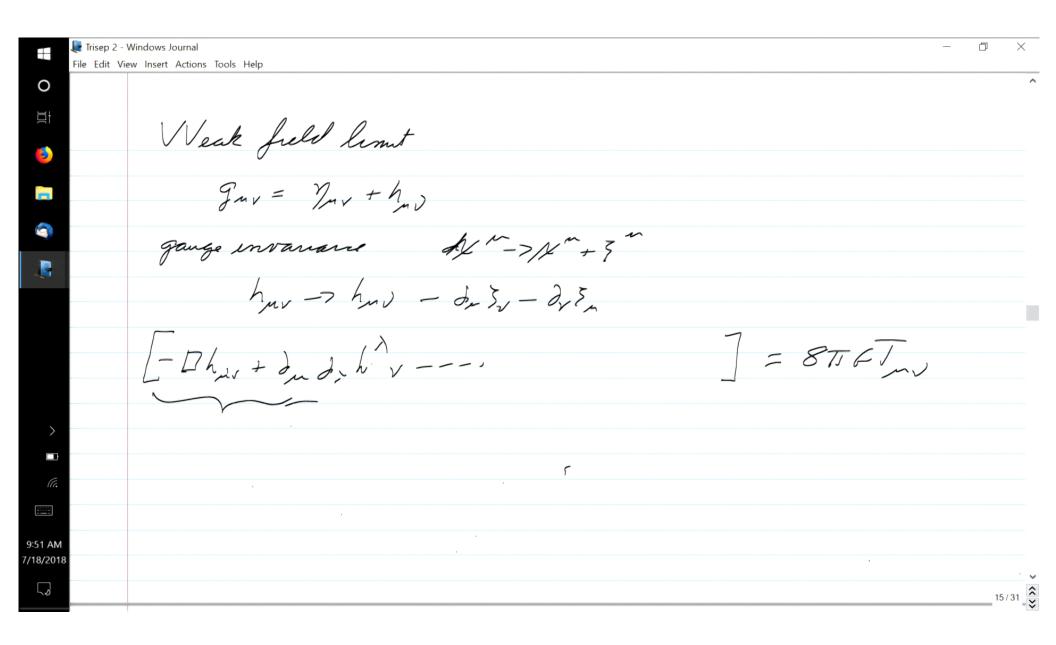


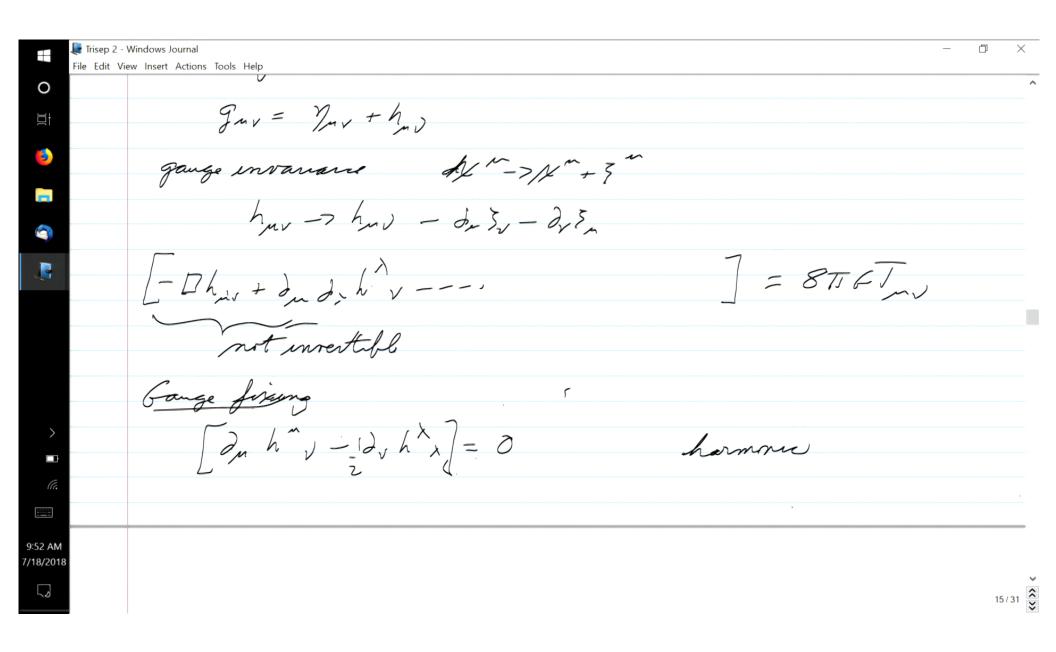


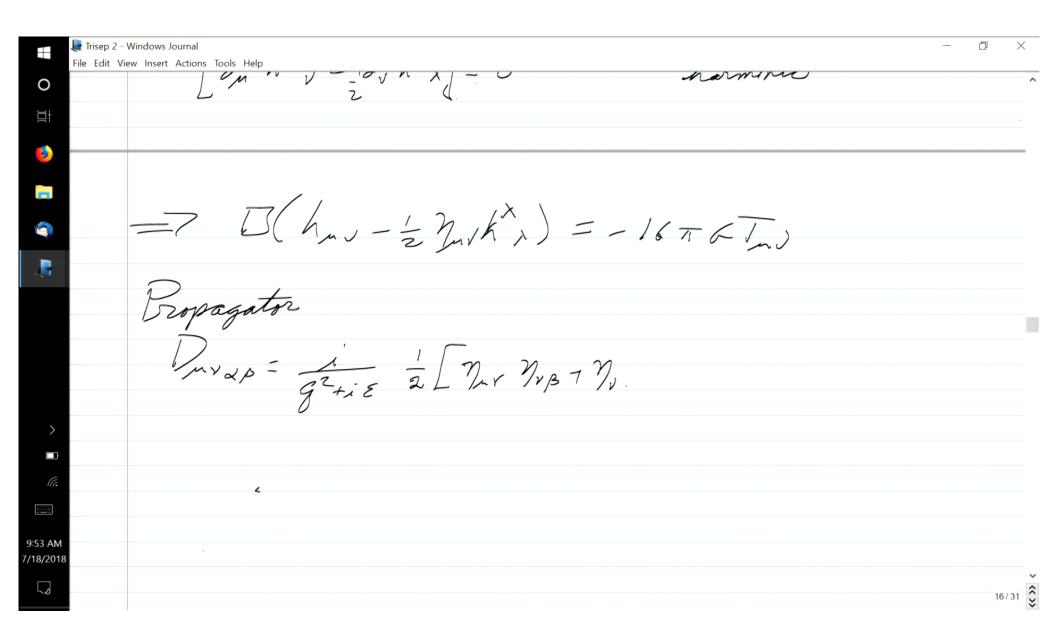


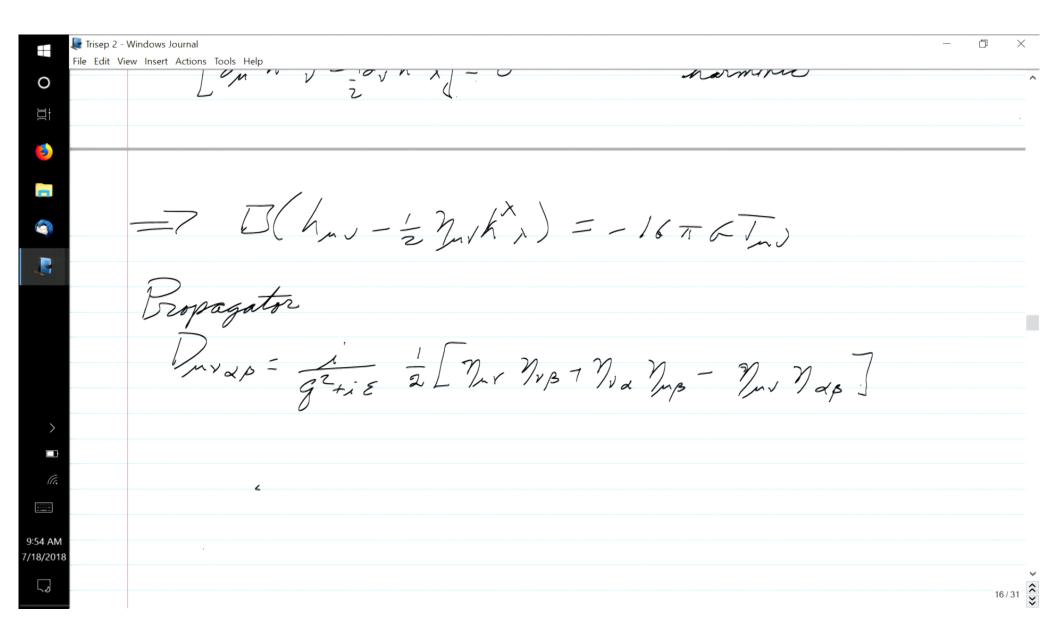


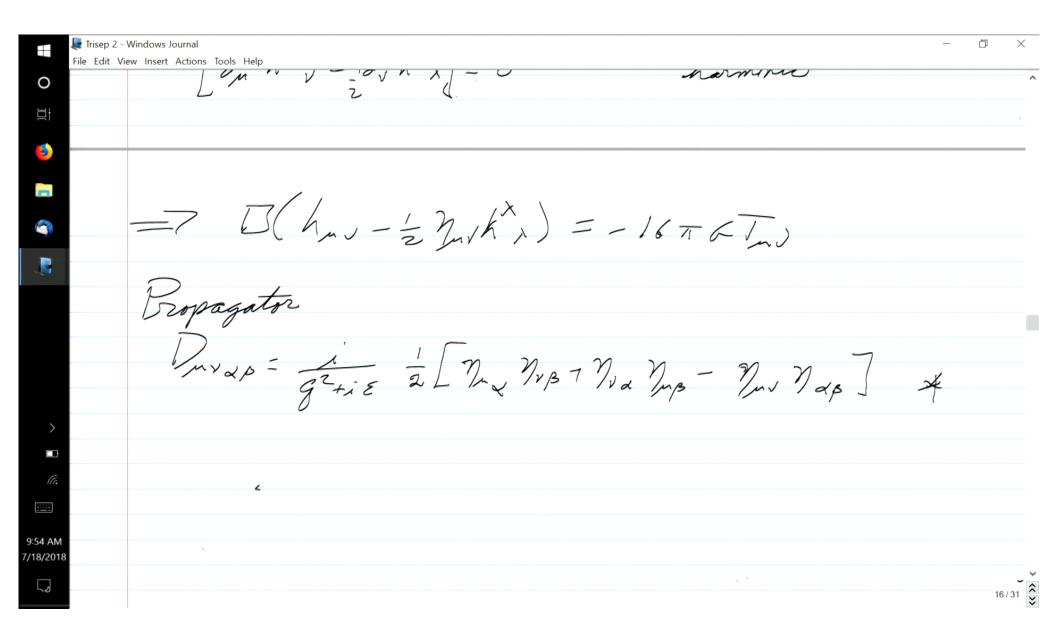


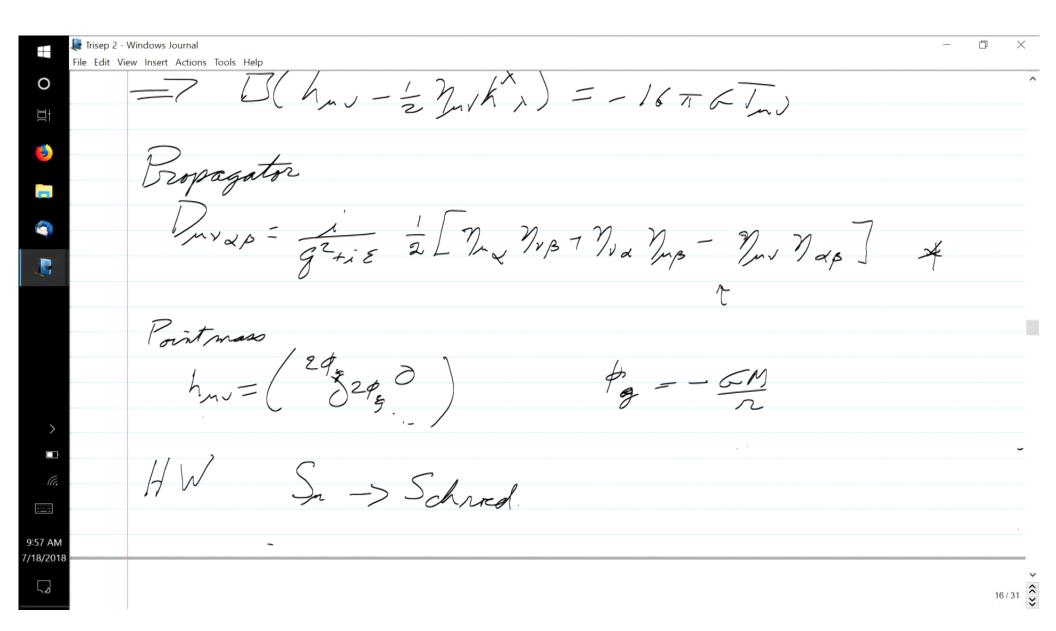












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Feynman rules:

A.1 Scalar propagator

The massive scalar propagator is:

$$=\frac{i}{q^2-m^2+}$$

A.2 Graviton propagator

The graviton propagator in harmonic gauge can be written in the form:

$$\alpha \beta \sim \gamma \delta$$
 = $\frac{i P^{\alpha \beta \gamma \delta}}{q^2 + i \epsilon}$
 $P^{\alpha \beta \gamma \delta} = \frac{1}{2} \left[\eta^{\alpha \gamma} \eta^{\beta \delta} + \eta^{\beta \gamma} \eta^{\alpha \delta} - \eta^{\alpha \beta} \eta^{\gamma \delta} \right]$

A.3 2-scalar-1-graviton vertex

The 2-scalar-1-graviton vertex is discussed in the literature. We write it as:

$$= \tau_1^{\mu\nu}(p,p',m)$$

where

$$\tau_1^{\mu\nu}(p,p',m) = -\frac{i\kappa}{9} \left[p^\mu p'^\nu + p^\nu p'^\mu - \eta'^\mu \left((p\cdot p') - m^2 \right) \right]$$

A.4 2-scalar-2-graviton vertex

The 2-scalar-2-graviton vertex is also discussed in the literature. We write it here with the full symmetry of the two gravitons:



$$= \tau_2^{\eta\lambda\rho\sigma}(p, p', m)$$

$$\begin{split} \tau_2^{\eta\lambda\rho\sigma}(p,p') &= i\kappa^2 \bigg[\left\{ I^{\eta\lambda\alpha\delta} I^{\rho\sigma\beta}_{\quad \ \, \delta} - \frac{1}{4} \left\{ \eta^{\eta\lambda} I^{\rho\sigma\alpha\beta} + \eta^{\rho\sigma} I^{\eta\lambda\alpha\beta} \right\} \right\} \left(p_\alpha p'_\beta + p'_\alpha p_\beta \right) \\ &- \frac{1}{2} \left\{ I^{\eta\lambda\rho\sigma} - \frac{1}{2} \eta^{\eta\lambda} \eta^{\rho\sigma} \right\} \left[(p\cdot p') - m^2 \right] \bigg] \end{split}$$

with

$$I_{\alpha\beta\gamma\delta} = \frac{1}{2}(\eta_{\alpha\gamma}\eta_{\beta\delta} + \eta_{\alpha\delta}\eta_{\beta\gamma}).$$

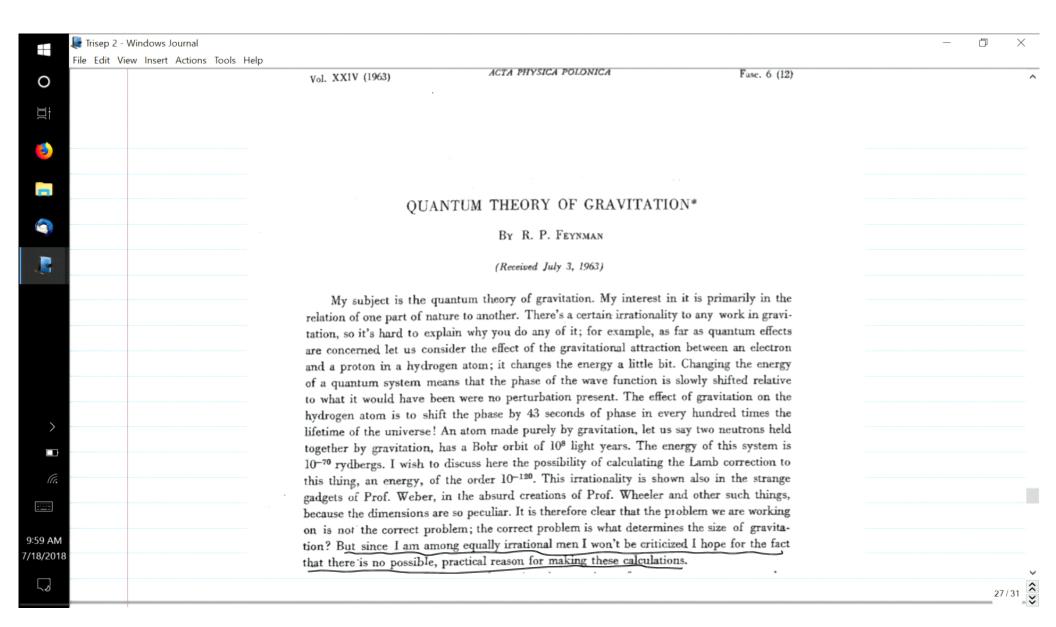
A.5 3-graviton vertex

The 3-graviton vertex can be derived via the background field method and has the form[9],[10]

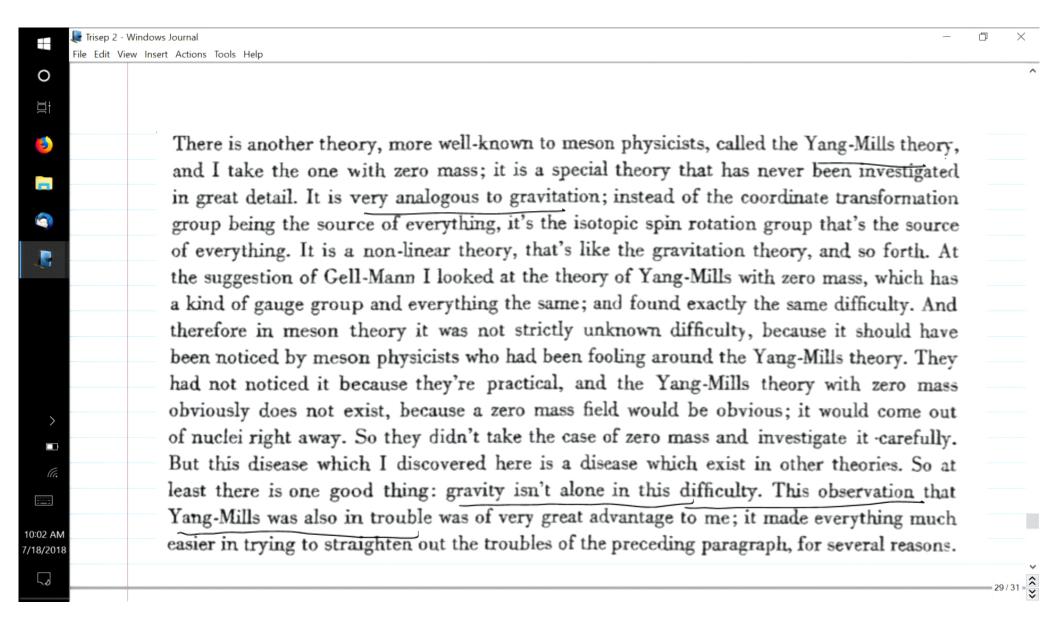
where

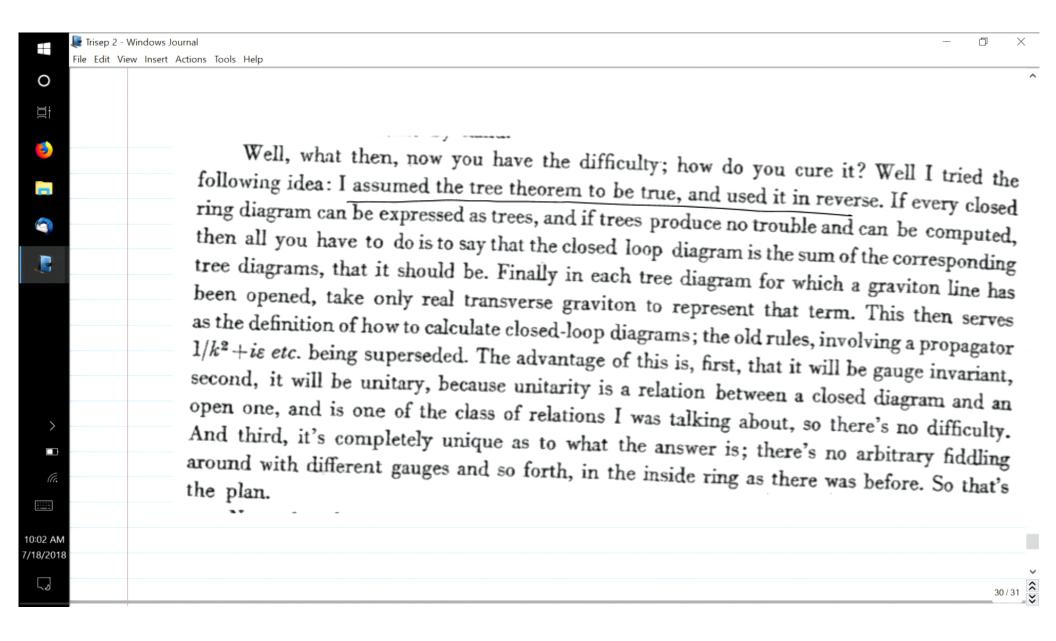
$$\begin{split} \tau g^{\mu\nu}_{\alpha\beta\gamma\delta}(k,q) &= -\frac{i\kappa}{2} \times \left(\mathcal{P}_{\alpha\beta\gamma\delta} \bigg[k^{\mu} k^{\nu} + (k-q)^{\mu} (k-q)^{\nu} + q^{\mu} q^{\nu} - \frac{3}{2} \eta^{\mu\nu} q^{2} \bigg] \right. \\ &+ 2q_{\lambda}q_{\sigma} \bigg[I_{\alpha\beta}^{} {}^{\lambda} I_{\gamma\delta}^{} {}^{\mu\nu} + I_{\gamma\delta}^{} {}^{\lambda} I_{\alpha\beta}^{} {}^{\mu\nu} - I_{\alpha\beta}^{} {}^{\mu\sigma} I_{\gamma\delta}^{} {}^{\nu\lambda} - I_{\gamma\delta}^{} {}^{\mu\sigma} I_{\alpha\beta}^{} {}^{\nu\lambda} \bigg] \\ &+ \bigg[q_{\lambda}q^{\mu} \left(\eta_{\alpha\beta} I_{\gamma\delta}^{} {}^{\nu\lambda} + \eta_{\gamma\delta} I_{\alpha\beta}^{} {}^{\nu\lambda} \right) + q_{\lambda}q^{\nu} \left(\eta_{\alpha\beta} I_{\gamma\delta}^{} {}^{\mu\lambda} + \eta_{\gamma\delta} I_{\alpha\beta}^{} {}^{\mu\lambda} \right) \\ &- q^{2} \left(\eta_{\alpha\beta} I_{\gamma\delta}^{} {}^{\mu\nu} - \eta_{\gamma\delta} I_{\alpha\beta}^{} {}^{\mu\nu} \right) - \eta^{\mu\nu} q_{\sigma} q_{\lambda} \left(\eta_{\alpha\beta} I_{\gamma\delta}^{} {}^{\sigma\lambda} + \eta_{\gamma\delta} I_{\alpha\beta}^{} {}^{\sigma\lambda} \right) \bigg] \\ &+ \bigg[2q_{\lambda} \big(I_{\alpha\beta}^{} {}^{\lambda\sigma} I_{\gamma\delta\sigma}^{} {}^{\nu} (k-q)^{\mu} + I_{\alpha\beta}^{} {}^{\lambda\sigma} I_{\gamma\delta\sigma}^{} {}^{\mu} (k-q)^{\nu} - I_{\gamma\delta}^{} {}^{\lambda\sigma} I_{\alpha\beta\sigma}^{} {}^{\nu} k^{\mu} - I_{\gamma} \bigg] \\ &+ q^{2} \left(I_{\alpha\beta}^{} {}^{\mu} I_{\gamma\delta}^{} {}^{\nu\sigma} + I_{\alpha\beta}^{} {}^{\nu\sigma} I_{\gamma\delta\sigma}^{} \right) + \eta^{\mu\nu} q_{\sigma} q_{\lambda} \left(I_{\alpha\beta}^{} {}^{\lambda\rho} I_{\gamma\delta\rho}^{} {}^{\sigma} + I_{\gamma\delta}^{} {}^{\lambda\rho} I_{\alpha\beta\rho}^{} \bigg] \\ &+ \bigg\{ (k^{2} + (k-q)^{2}) \big[I_{\alpha\beta}^{} {}^{\mu\sigma} I_{\gamma\delta\sigma}^{} + I_{\gamma\delta}^{} {}^{\mu\sigma} I_{\alpha\beta\sigma}^{} - \frac{1}{2} \eta^{\mu\nu} \mathcal{P}_{\alpha\beta\gamma\delta} \bigg] \\ &- \left(I_{\gamma\delta}^{} {}^{\mu\nu} \eta_{\alpha\beta} k^{2} + I_{\alpha\beta}^{} {}^{\mu\nu} \eta_{\gamma\delta} (k-q)^{2} \right) \bigg\} \bigg) \end{split}$$

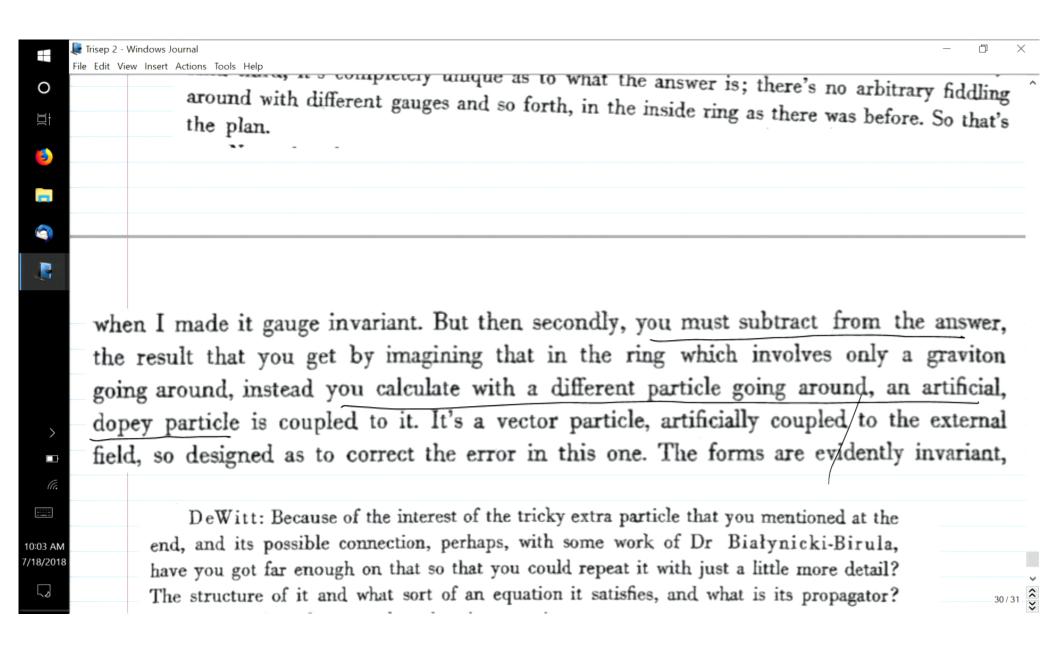
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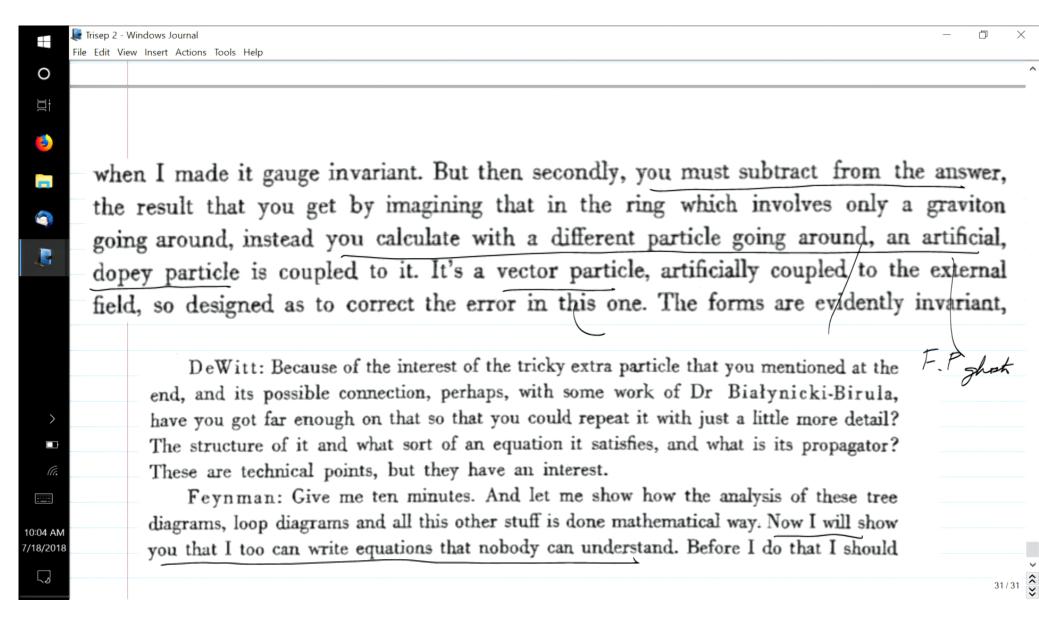


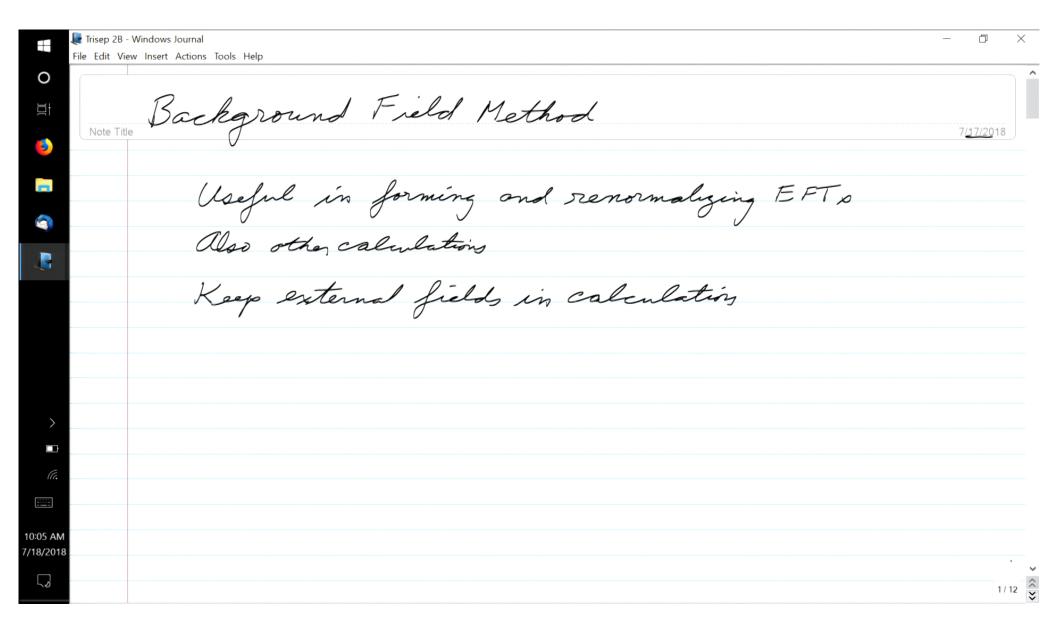
	Tre theorem
	This made me investigate the entire subject in great detail to find out what the troul
	is. I discovered in the process two things. First, I discovered a number of theorems, which
	far as I know are new, which relate closed loop diagrams and diagrams without closed lo
,	diagrams (I shall call the latter diagrams "trees"). The unitarity relation which I have ju
4	been describing, is one connection between a closed loop diagram and a tree; but I four
4	a whole lot of other ones, and this gives me more tests on my machinery. So let me just to
	you a little bit about this theorem, which gives other rules. It is rather interesting. As a matt
	of fact, I proved that if you have a diagram with rings in it there are enough theorem
ξ	altogether, so that you can express any diagram with circuits completely in terms of diagram
1	with trees and with all momenta for tree diagrams in physically attainable regions and of
t	the mass shell. The demonstration is remarkably easy. There are several ways of demonstration
t	ting it: I'll only chose one. Things propagate from one place to another, as I said, wi
٦	



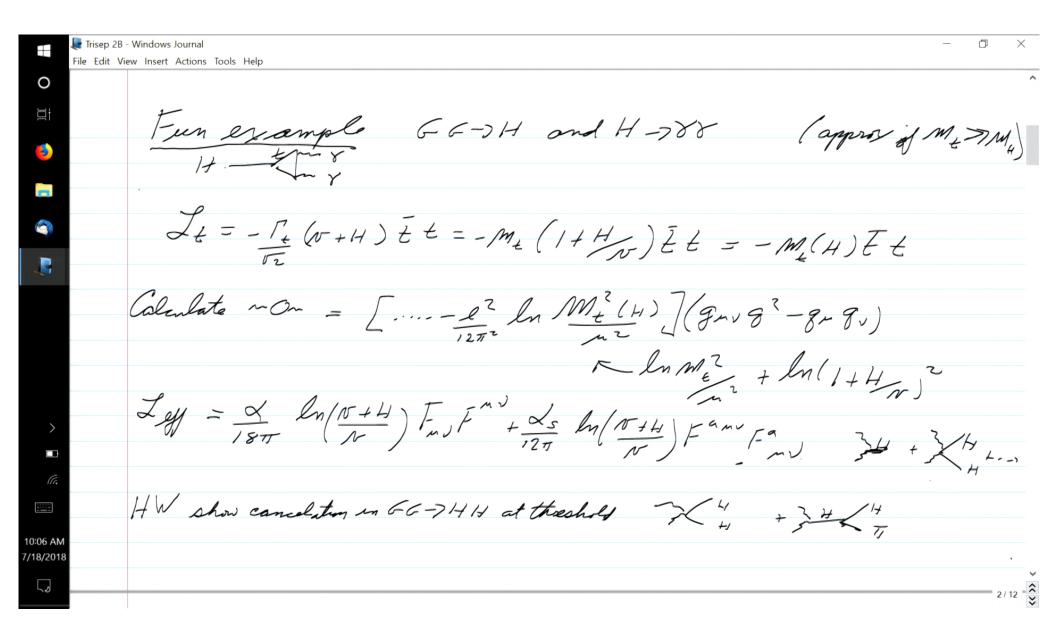


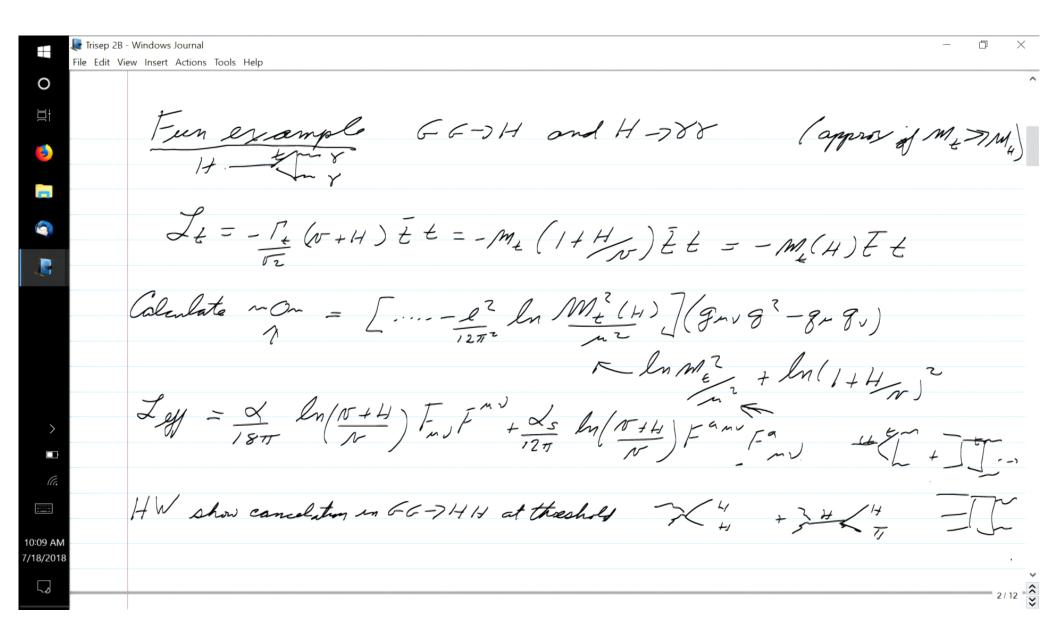


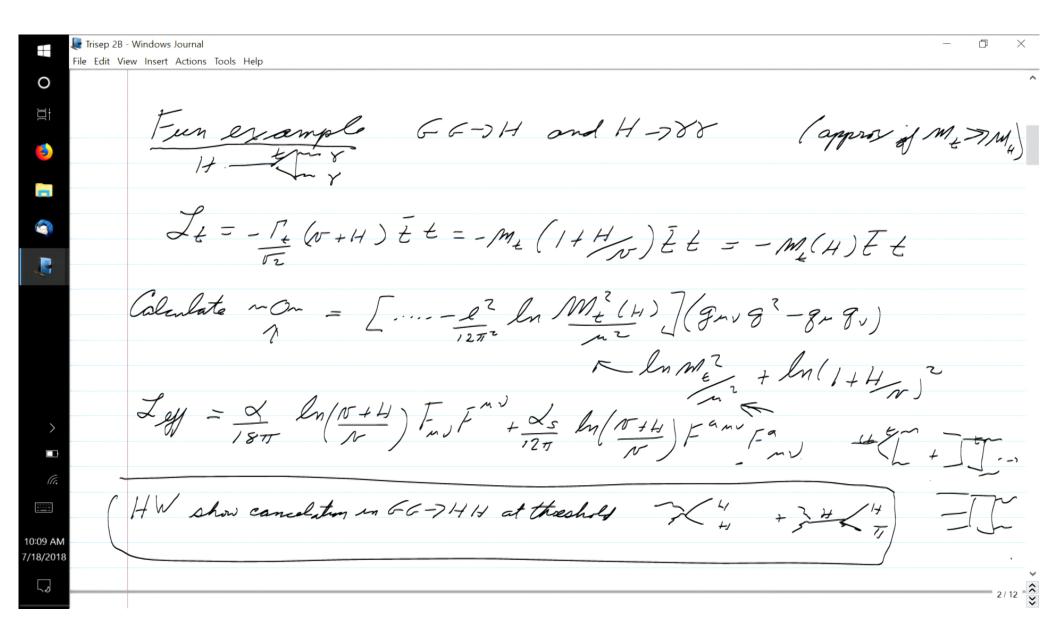


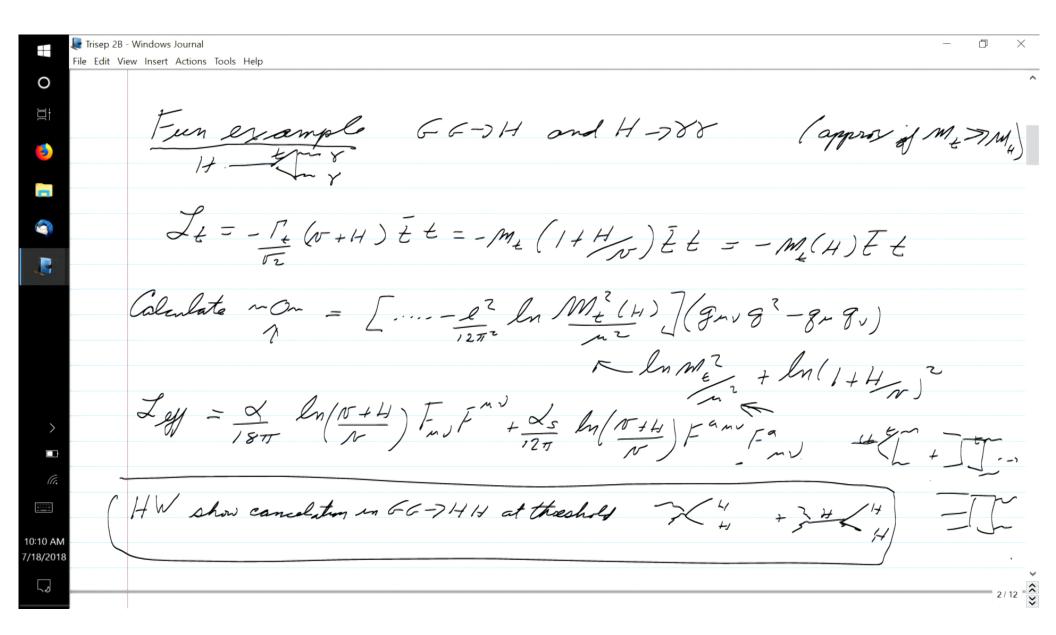


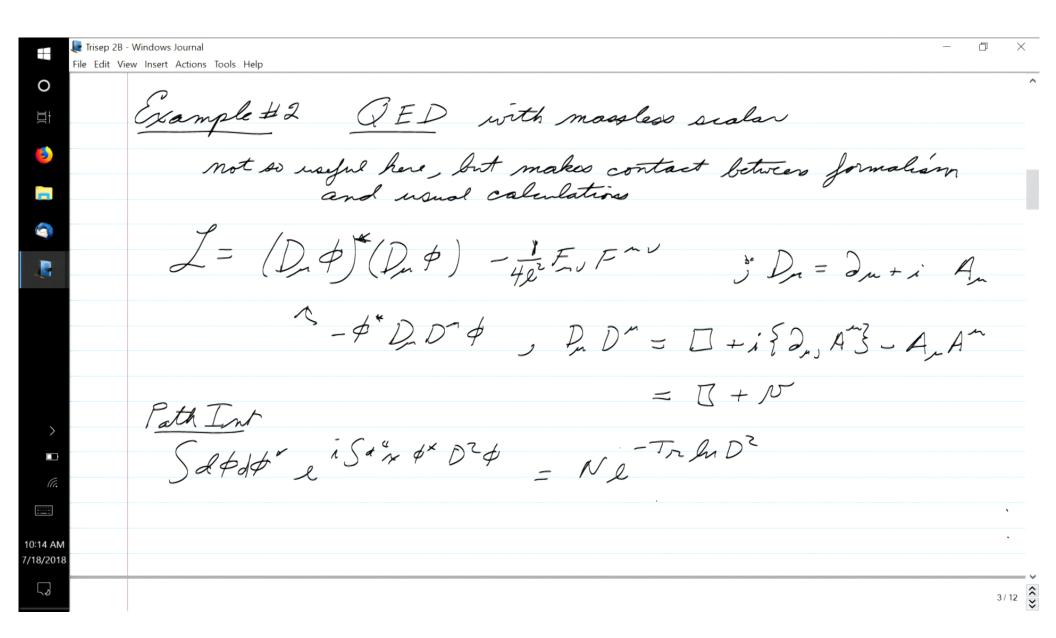
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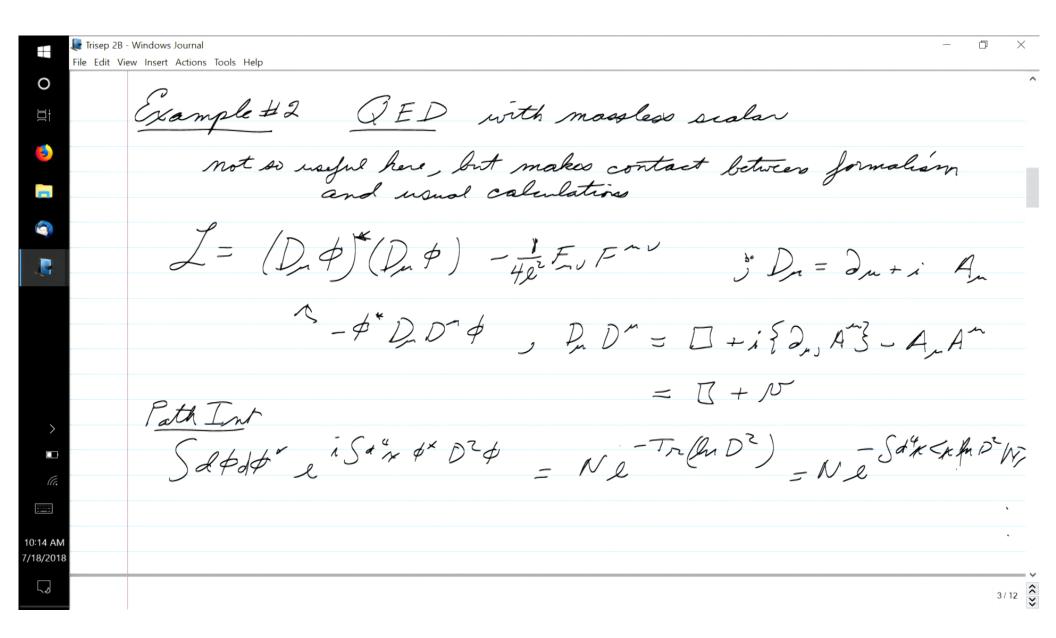


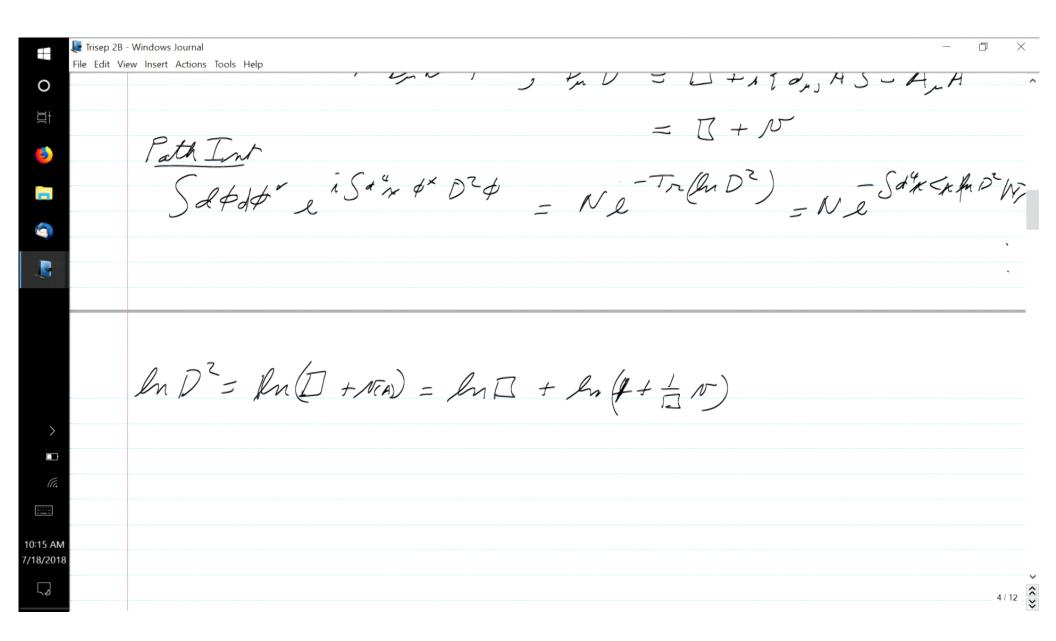


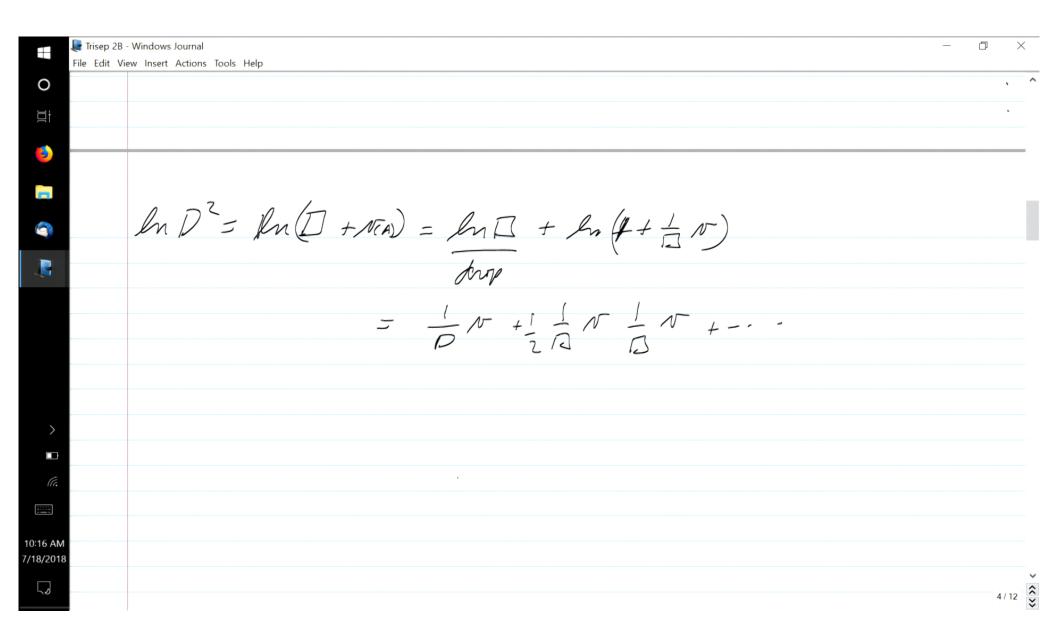












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