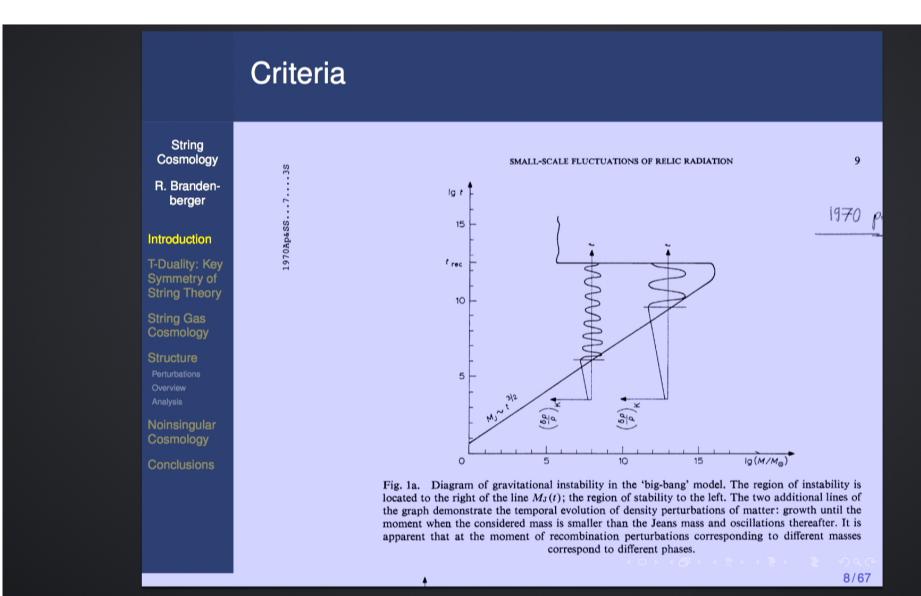
Title: String Theory and Nonsingular Cosmology

Date: Jun 08, 2018 11:00 AM

URL: http://pirsa.org/18060006

Abstract: I will argue that in the context of string theory, the Big Bang singularity of standard and inflationary cosmology is automatically resolved. To see this at the level of an effective field theory, ideas from "Double Field Theory" are useful.

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Key Realization

R. Sunyaev and Y. Zel'dovich, Astrophys. and Space Science **7**, 3 (1970); P. Peebles and J. Yu, Ap. J. **162**, 815 (1970).

String Cosmology

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T-Duality: Key Symmetry of String Theory

String Gas Cosmology

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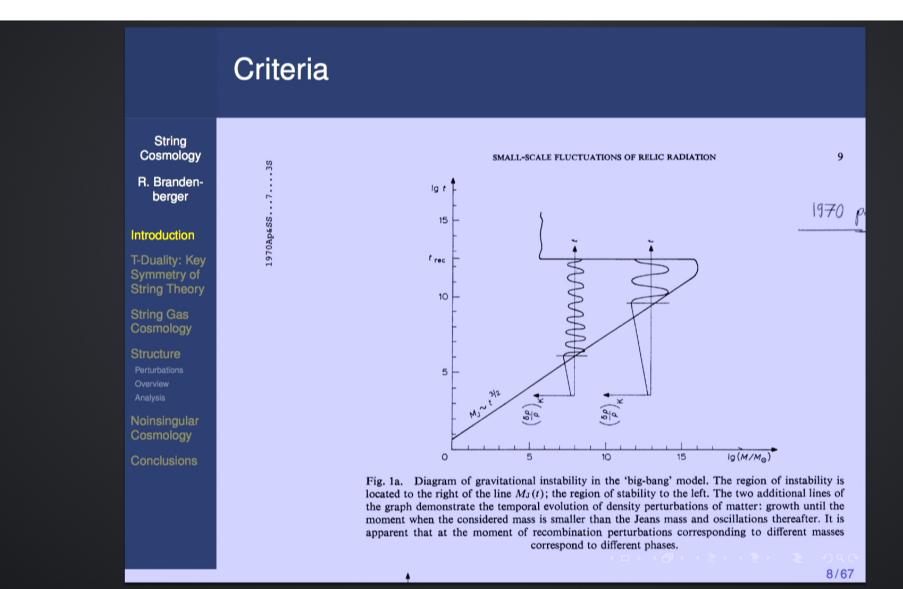
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Conclusions

- Given a scale-invariant power spectrum of adiabatic fluctuations on "super-horizon" scales before t_{eq} , i.e. standing waves.
- → "correct" power spectrum of galaxies.
- → acoustic oscillations in CMB angular power spectrum.

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Key Challenge

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Conclusions

How does one obtain such a spectrum?

- Inflationary Cosmology is the first scenario based on causal physics which yields such a spectrum.
- But it is not the only one.

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Hubble Radius vs. Horizon

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Conclusions

- Horizon: Forward light cone of a point on the initial Cauchy surface.
- Horizon: region of causal contact.
- Hubble radius: $I_H(t) = H^{-1}(t)$ inverse expansion rate.
- Hubble radius: local concept, relevant for dynamics of cosmological fluctuations.
- In Standard Big Bang Cosmology: Hubble radius = horizon.
- In any theory which can provide a mechanism for the origin of structure: Hubble radius ≠ horizon.

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Criteria for a Successful Early Universe Scenario

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Conclusions

- Horizon >> Hubble radius in order for the scenario to solve the "horizon problem" of Standard Big Bang Cosmology.
- Scales of cosmological interest today originate inside the Hubble radius at early times in order for a causal generation mechanism of fluctuations to be possible.
- Squeezing of fluctuations on super-Hubble scales in order to obtain the acoustic oscillations in the CMB angular power spectrum.
- Mechanism for producing a scale-invariant spectrum of curvature fluctuations on super-Hubble scales.

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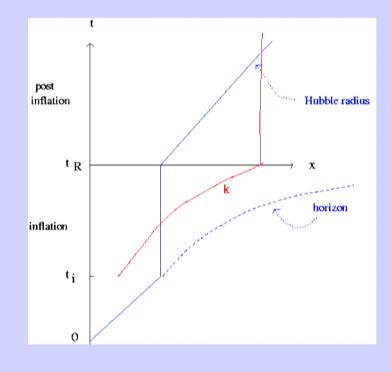
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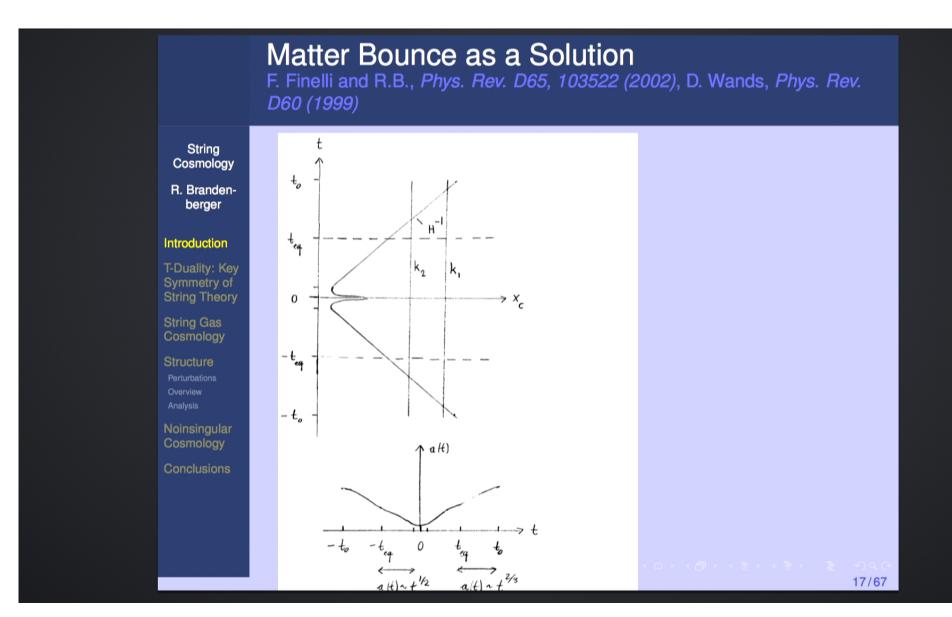
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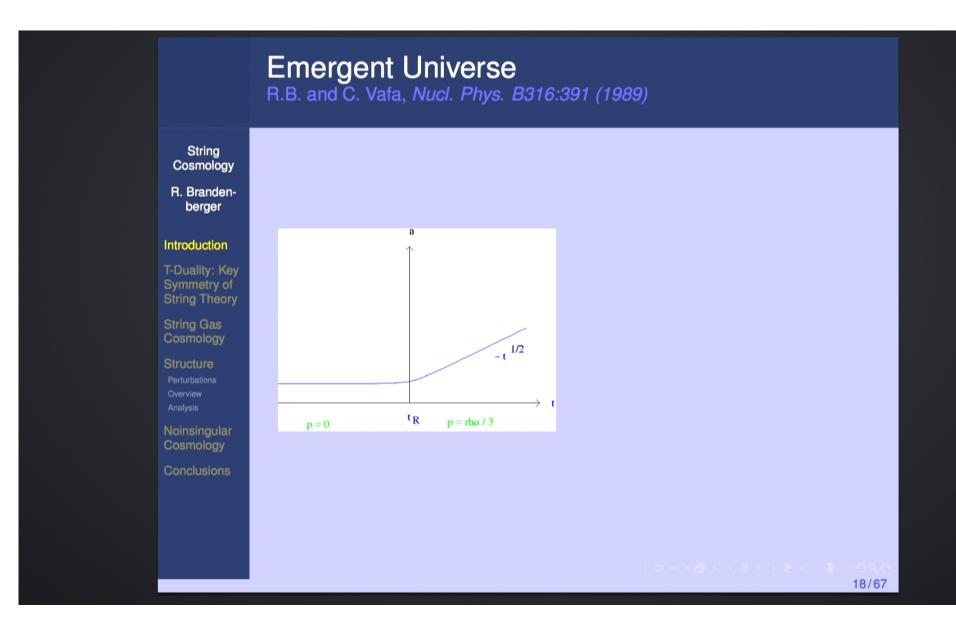
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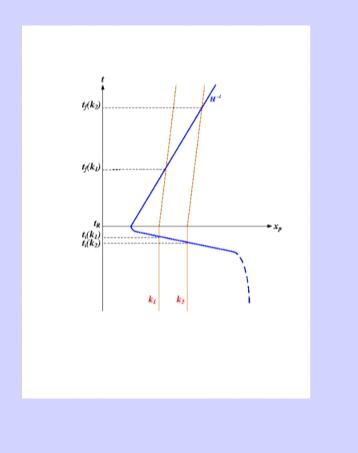
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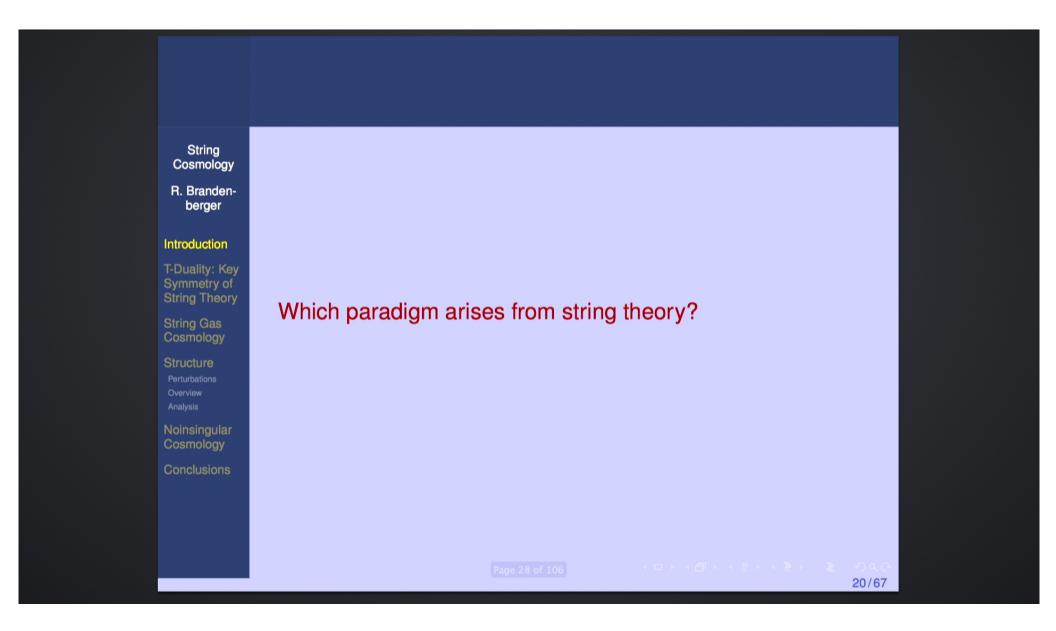
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String States

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Conclusion

Assumption: All spatial dimensions toroidal, radius *R*.

String states:

• momentum modes: $E_n = n/R$

• winding modes: $E_m = mR$

oscillatory modes: E independent of R

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T-Duality

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Conclusions

T-Duality

- Momentum modes: $E_n = n/R$
- Winding modes: $E_m = mR$
- Duality: $R \rightarrow 1/R$ $(n, m) \rightarrow (m, n)$
- Mass spectrum of string states unchanged
- Symmetry of vertex operators
- Symmetry at non-perturbative level → existence of **D-branes**

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Position Operators

R.B. and C. Vafa, Nucl. Phys. B316:391 (1989)

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Conclusions

Position operators (dual to momenta)

$$|x> = \sum_{p} \exp(ix \cdot p)|p>$$

Dual position operators (dual to windings)

$$|\tilde{x}> = \sum_{w} \exp(i\tilde{x}\cdot w)|w>$$

Note:

$$|x> = |x+2\pi R>, |\tilde{x}> = |\tilde{x}+2\pi \frac{1}{R}>$$

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Heavy vs. Light Modes

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Conclusions

- R ≫ 1: momentum modes light.
- R ≪ 1: winding modes light.
- $R \gg 1$: length measured in terms of |x>.
- $R \ll 1$: length measured in terms of $|\tilde{x}>$
- $R \sim 1$: both |x> and $|\tilde{x}>$ important.

Conclusion: At string scale densities usual effective field theory (EFT) based on supergravity will break down.

Conclusion: If an effective field theory description is valid, it must be an EFT in 18 spatial dimensions.

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Physical length operator

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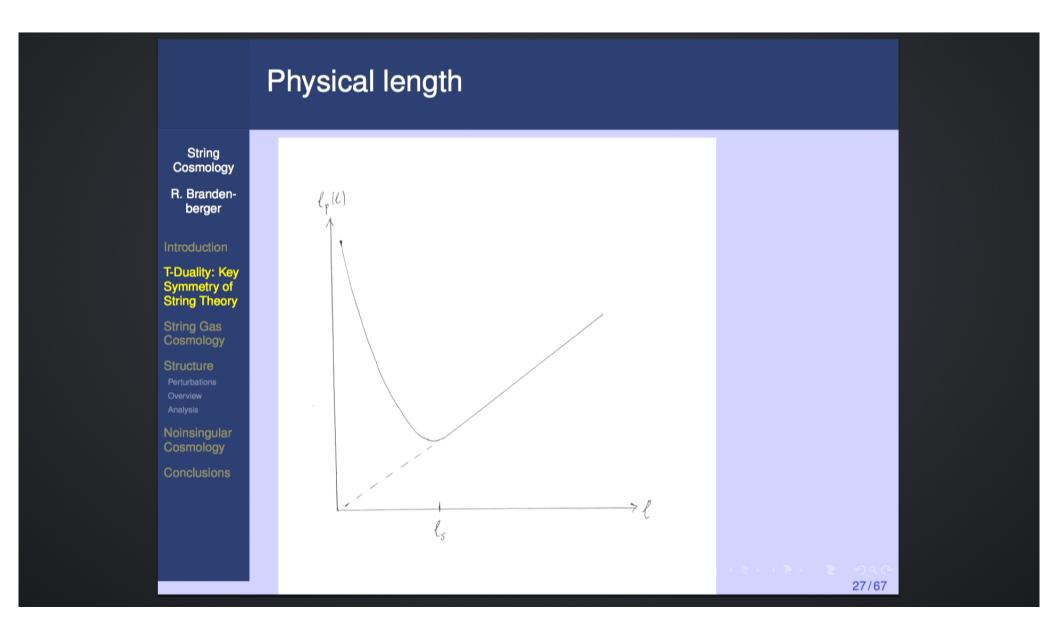
Conclusion

$$I_p(R) = R R \gg 1$$

$$I_p(R) = \frac{1}{R} R \ll 1$$

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String Gas Cosmology

R.B. and C. Vafa, Nucl. Phys. B316:391 (1989)

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Idea: make use of the new symmetries and new degrees of freedom which string theory provides to construct a new theory of the very early universe.

Assumption: Matter is a gas of fundamental strings.

Assumption: $g_s \ll 1$.

Key points:

- New degrees of freedom: string oscillatory modes
- Leads to a maximal temperature for a gas of strings, the Hagedorn temperature
- New degrees of freedom: string winding modes
- Leads to a new symmetry: physics at large R is equivalent to physics at small R

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R.B. and C. Vafa, Nucl. Phys. B316:391 (1989)

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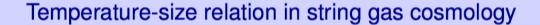
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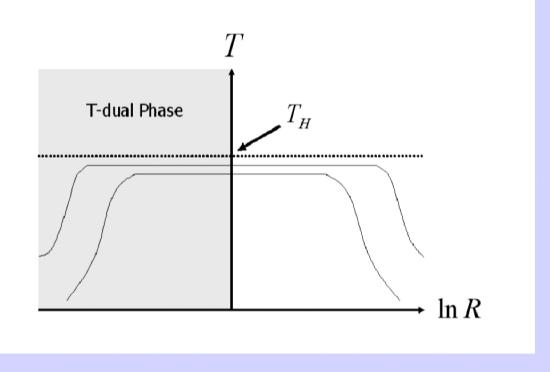
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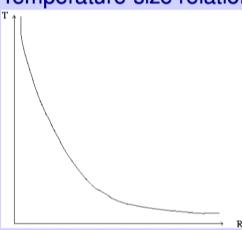
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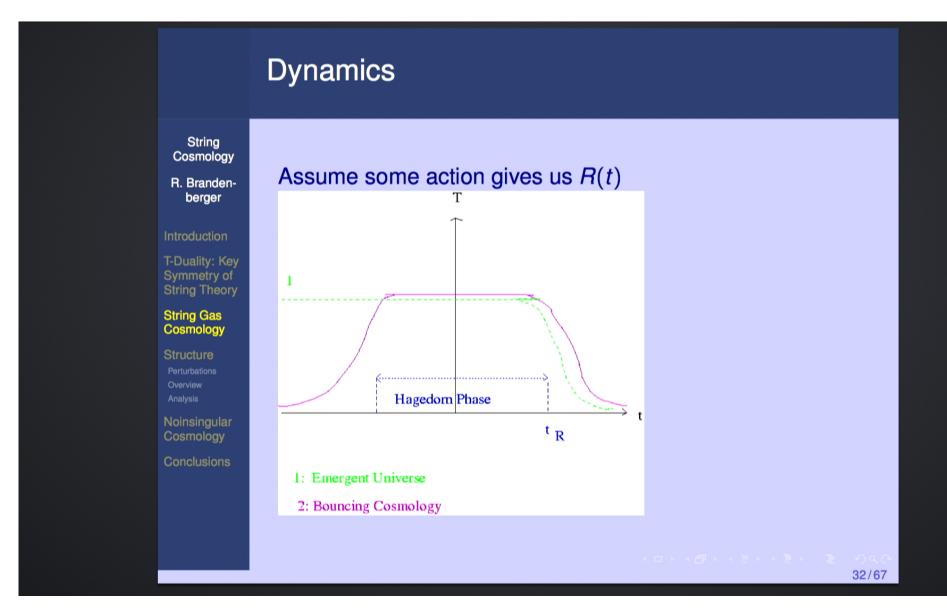
Conclusion

Temperature-size relation in standard cosmology



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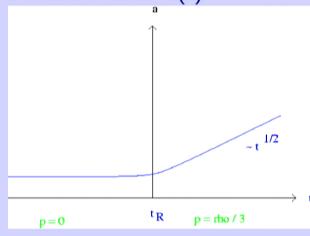
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Conclusions

We will thus consider the following background dynamics for the scale factor a(t):



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Dynamical Decompactification

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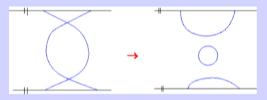
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Conclusions

- Begin with all 9 spatial dimensions small, initial temperature close to $T_H \rightarrow$ winding modes about all spatial sections are excited.
- Expansion of any one spatial dimension requires the annihilation of the winding modes in that dimension.



- Decay only possible in three large spatial dimensions.
- dynamical explanation of why there are exactly three large spatial dimensions.

Note: For $R \to 0$ there is an analogous decompactification mechanism which only allows three dual dimensions to be large.

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Moduli Stabilization in SGC

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Conclusions

Size Moduli [S. Watson, 2004; S. Patil and R.B., 2004, 2005]

- winding modes prevent expansion
- momentum modes prevent contraction
- ullet o $V_{eff}(R)$ has a minimum at a finite value of $R, \ o \ R_{min}$
- in heterotic string theory there are enhanced symmetry states containing both momentum and winding which are massless at R_{min}
- $ightharpoonup V_{eff}(R_{min}) = 0$
- size moduli stabilized in Einstein gravity background

Shape Moduli [E. Cheung, S. Watson and R.B., 2005]

- enhanced symmetry states
- ullet \to harmonic oscillator potential for heta
- → shape moduli stabilized

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Dilaton stabilization in SGC

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Conclusions

- The only remaining modulus is the dilaton.
- Make use of gaugino condensation to give the dilaton a potential with a unique minimum.
- \bullet \rightarrow diltaton is stabilized.
- Dilaton stabilization is consistent with size stabilization [R. Danos, A. Frey and R.B., 2008].
- Gaugino condensation induces (high scale)
 supersymmetry breaking [S. Mishra, W. Xue, R.B. and U. Yajnik, 2012].

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Theory of Cosmological Perturbations: Basics

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Cosmological fluctuations connect early universe theories with observations

- Fluctuations of matter → large-scale structure
- Fluctuations of metric → CMB anisotropies
- N.B.: Matter and metric fluctuations are coupled

Key facts:

- 1. Fluctuations are small today on large scales
- fluctuations were very small in the early universe
- → can use linear perturbation theory
- 2. Sub-Hubble scales: matter fluctuations dominate
- Super-Hubble scales: metric fluctuations dominate

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Quantum Theory of Linearized Fluctuations

V. Mukhanov, H. Feldman and R.B., *Phys. Rep. 215:203 (1992)*

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Conclusions

Step 1: Metric including fluctuations

$$ds^{2} = a^{2}[(1+2\Phi)d\eta^{2} - (1-2\Phi)d\mathbf{x}^{2}]$$
$$\varphi = \varphi_{0} + \delta\varphi$$

Note: Φ and $\delta \varphi$ related by Einstein constraint equations Step 2: Expand the action for matter and gravity to second order about the cosmological background:

$$S^{(2)} = \frac{1}{2} \int d^4x ((v')^2 - v_{,i}v^{,i} + \frac{z''}{z}v^2)$$

$$v = a(\delta\varphi + \frac{z}{a}\Phi)$$

$$z = a\frac{\varphi'_0}{\mathcal{H}}$$

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Step 3: Resulting equation of motion (Fourier space)

$$v_k'' + (k^2 - \frac{z''}{z})v_k = 0$$

Features:

- oscillations on sub-Hubble scales
- squeezing on super-Hubble scales $v_k \sim z$

Quantum vacuum initial conditions:

$$v_k(\eta_i) = (\sqrt{2k})^{-1}$$

Structure formation in inflationary cosmology

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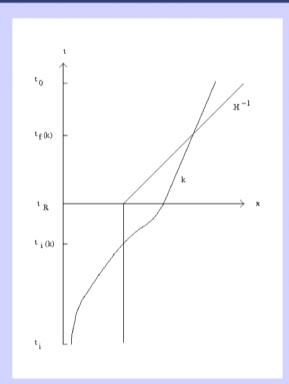
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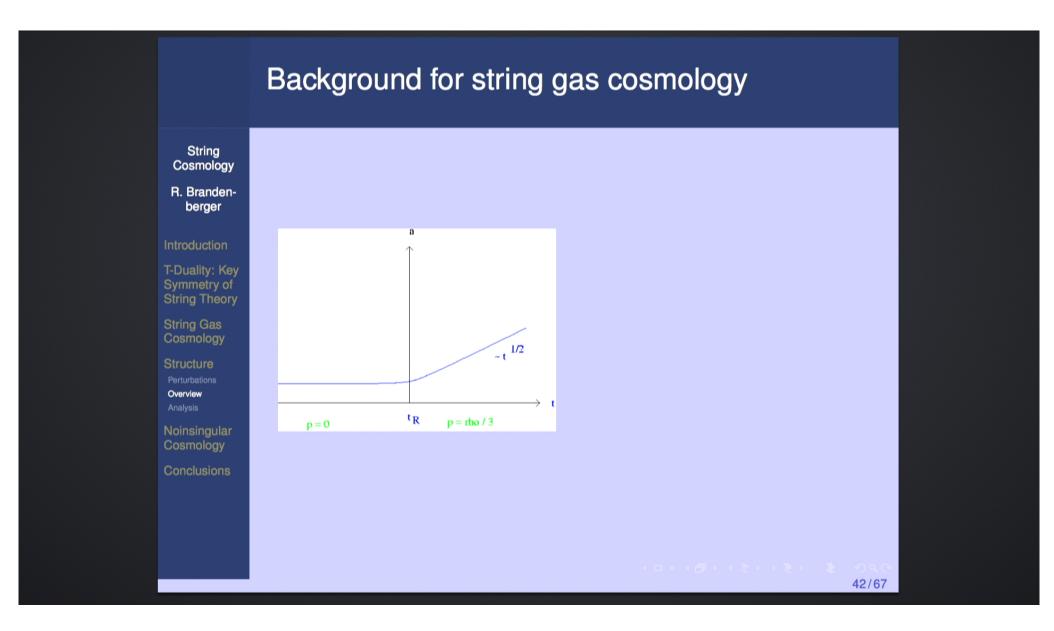
Conclusions



N.B. Perturbations originate as quantum vacuum fluctuations.

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Method

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Conclusion

- Calculate matter correlation functions in the Hagedorn phase (neglecting the metric fluctuations)
- For fixed k, convert the matter fluctuations to metric fluctuations at Hubble radius crossing $t = t_i(k)$
- Evolve the metric fluctuations for $t > t_i(k)$ using the usual theory of cosmological perturbations

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Extracting the Metric Fluctuations

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Ansatz for the metric including cosmological perturbations and gravitational waves:

$$ds^2 = a^2(\eta)((1+2\Phi)d\eta^2 - [(1-2\Phi)\delta_{ij} + h_{ij}]dx^i dx^j)$$
.

Inserting into the perturbed Einstein equations yields

$$\langle |\Phi(k)|^2 \rangle = 16\pi^2 G^2 k^{-4} \langle \delta T^0_0(k) \delta T^0_0(k) \rangle,$$

$$\langle |\mathbf{h}(\mathbf{k})|^2 \rangle = 16\pi^2 G^2 k^{-4} \langle \delta T^i{}_j(\mathbf{k}) \delta T^i{}_j(\mathbf{k}) \rangle.$$

Power Spectrum of Cosmological Perturbations

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Conclusions

Key ingredient: For thermal fluctuations:

$$\langle \delta
ho^2
angle = rac{T^2}{R^6} C_V \, .$$

Key ingredient: For string thermodynamics in a compact space

$$C_V pprox 2rac{R^2/\ell_s^3}{T\left(1-T/T_H
ight)}$$
 .

Extracting the Metric Fluctuations

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 .

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Power spectrum of cosmological fluctuations

$$P_{\Phi}(k) = 8G^{2}k^{-1} < |\delta\rho(k)|^{2} >$$

$$= 8G^{2}k^{2} < (\delta M)^{2} >_{R}$$

$$= 8G^{2}k^{-4} < (\delta\rho)^{2} >_{R}$$

$$= 8G^{2}\frac{T}{\ell_{s}^{3}}\frac{1}{1 - T/T_{H}}$$

Key features:

- scale-invariant like for inflation
- slight red tilt like for inflation

Prediction: Spectrum of Gravitational Waves

R.B., A. Nayeri, S. Patil and C. Vafa, Phys. Rev. Lett. (2007)

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$$P_h(k) = 16\pi^2 G^2 k^{-1} < |T_{ij}(k)|^2 >$$

$$= 16\pi^2 G^2 k^{-4} < |T_{ij}(R)|^2 >$$

$$\sim 16\pi^2 G^2 \frac{T}{\ell_s^3} (1 - T/T_H)$$

Key ingredient for string thermodynamics

$$<|T_{ij}(R)|^2> \sim \frac{T}{l_s^3 R^4}(1-T/T_H)$$

Key features:

- scale-invariant (like for inflation)
- slight blue tilt (unlike for inflation)

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Power spectrum of cosmological fluctuations

$$P_{\Phi}(k) = 8G^{2}k^{-1} < |\delta\rho(k)|^{2} >$$

$$= 8G^{2}k^{2} < (\delta M)^{2} >_{R}$$

$$= 8G^{2}k^{-4} < (\delta\rho)^{2} >_{R}$$

$$= 8G^{2}\frac{T}{\ell_{s}^{3}}\frac{1}{1 - T/T_{H}}$$

Key features:

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$$P_h(k) = 16\pi^2 G^2 k^{-1} < |T_{ij}(k)|^2 >$$

$$= 16\pi^2 G^2 k^{-4} < |T_{ij}(R)|^2 >$$

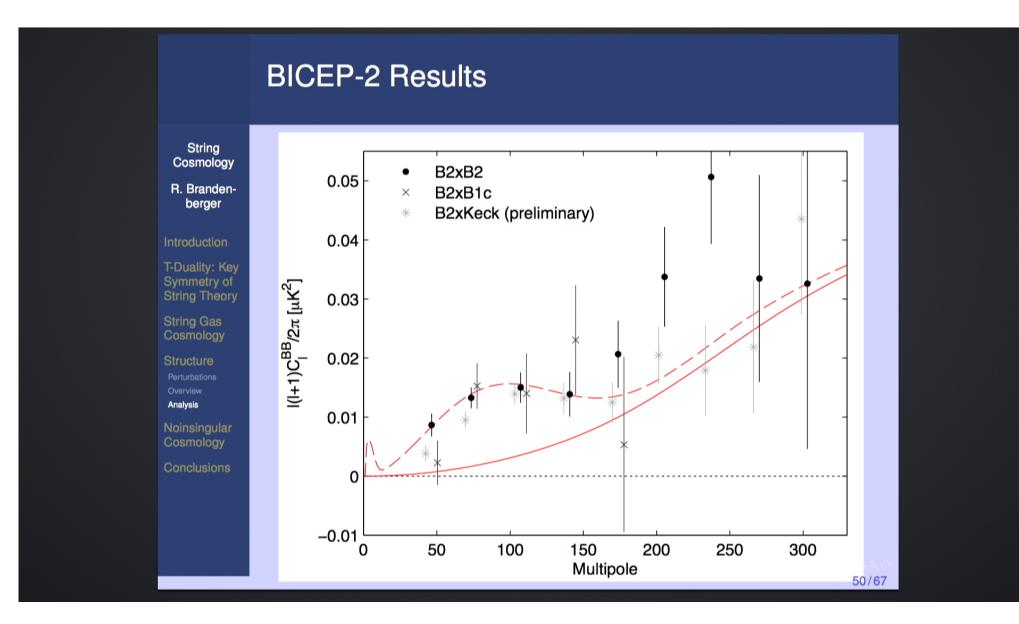
$$\sim 16\pi^2 G^2 \frac{T}{\ell_s^3} (1 - T/T_H)$$

Key ingredient for string thermodynamics

$$<|T_{ij}(R)|^2> \sim \frac{T}{l_s^3 R^4}(1-T/T_H)$$

Key features:

- scale-invariant (like for inflation)
- slight blue tilt (unlike for inflation)



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Prediction: Running of the Spectrum of Cosmological Perturbations R.B., G. Franzmann and Q. Liang, arXiv:1708.06793 [hep-th]

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Running

$$\alpha_s \equiv \frac{d^2 \ln P_{\Phi}(k)}{d \ln k^2}|_{k=aH}$$

- For Inflation: $\alpha_s \sim (1 n_s)^2$
- For String Gas Cosmology: $\alpha_s \sim (1 n_s)$

→ String Gas Cosmology predicts a parametrically larger running.

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Geodesic Completeness

R.B., R. Costa, G. Franzmann and A. Weltman, arXiv:1710.02412 [hep-th]

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Conclusions

Recall: For each dimension of the underlying topological space there are two position operators [R.B. and C. Vafa]:

- x: dual to the momentum modes
- \tilde{x} : dual to the winding modes

We measure **physical length** in terms of the **light** degrees of freedom.

$$I(R) = R \text{ for } R \gg 1$$

$$I(R) = R \text{ for } R \gg 1,$$

 $I(R) = \frac{1}{R} \text{ for } R \ll 1.$

Doubled Space Approach

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 $dS^{2} = dt^{2} - a^{2}(t)\delta_{ij}dx^{i}dx^{j} - a^{-2}(t)\delta_{ij}d\tilde{x}^{i}d\tilde{x}^{j}$

Point particle geodesic:

$$\frac{d}{dS} \left(\frac{dx^{i}}{dS} a^{2} \right) = 0$$

$$\frac{d}{dS} \left(\frac{d\tilde{x}^{i}}{dS} a^{-2} \right) = 0$$

$$\frac{d}{dS}(\frac{d\tilde{x}^i}{dS}a^{-2}) = 0$$

Initial conditions: related by duality.

Proper Time along Geodesic

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Assume a(t) as in Standard Big Bang Cosmology.

Proper distance into the future from some time t_0 to some time $t_2 \gg t_0$:

$$\Delta S = \int_{t_0}^{t_2} a(t) \gamma(t)^{-1} dt + T_2,$$

Proper distance into the past from some time t_0 to some time $t_1 \ll t_0$:

$$\Delta S = \int_{t_1}^{t_0} a(t)^{-1} \tilde{\gamma}^{-1}(t) dt + T_1,$$

Interpretation

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Conclusions

- Expansion of the scale factor in the dual spatial directions as time decreases ≡ expansion in the regular directions as time increases.
- Dynamics of the dual spatial dimensions as t decreases is measured as expansion when the dual time $t_d = \frac{1}{t}$ decreases.

Proposal:

$$t_{\rho}(t) = t \text{ for } t \gg 1,$$

 $t_{\rho}(t) = \frac{1}{t} \text{ for } t \ll 1.$

$$t_p(t) = \frac{1}{t} \text{ for } t \ll 1.$$

Conclusion: Point particle geodesics can be extended in both time directions to infinite proper time.

Nonsingular String Cosmology

R.B., R. Costa, G. Franzmann and A. Weltman, arXiv:1805.06321 [hep-th]

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T-Duality: Key Symmetry of String Theory

String Gas Cosmology

Structure

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Noinsingular Cosmology

Conclusions

Consider Dilaton gravity

$$\left(\dot{\phi} - dH\right)^{2} - dH^{2} = e^{\phi}\rho$$

$$\dot{H} - H\left(\dot{\phi} - dH\right) = \frac{1}{2}e^{\phi}\rho$$

$$2\left(\ddot{\phi} - d\dot{H}\right) - \left(\dot{\phi} - dH\right)^{2} - dH^{2} = 0$$

coupled to string gas matter.

$$w(a) = \frac{2}{\pi d} \arctan \left(\beta \ln \left(\frac{a}{a_0} \right) \right),$$

Limiting Solutions

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Large radius limit:

$$\rho$$
 (a large) $\to \rho_0 (a/a_0)^{-(d+1)}$,

Small radius limit:

$$\rho\left(a\,\mathrm{small}\right)
ightarrow
ho_0\left(a/a_0\right)^{-d+1}$$

Ansatz:

$$a(t) \sim \left(\frac{t}{t_0}\right)^{lpha} \ ar{\phi}(t) \sim eta \ln(t/t_0) \, ,$$

Where

$$\bar{\phi} \equiv \phi - d \ln(a)$$

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Hagedorn phase, w = 0:

$$(\alpha,\beta)=(0,2).$$

Note: Static in string frame.

Large a phase, w = 1/d:

$$(\alpha,\beta) = \left(\frac{2}{D},\frac{2}{D}(D-1)\right).$$

Note: constant dilaton.

Small a phase, w = -1/d:

$$(\alpha,\beta) = \left(-\frac{2}{D},\frac{2}{D}(D-1)\right).$$

Interpretation

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Symmetry of String Theory

String Gas

Noinsingular Cosmology

- Bouncing cosmology in the string frame → nonsingular.
- Contracting cosmology for $t \to 0$ in the Einstein frame.
- As $t \to 0$ the energy of the string gas drifts to winding modes.
- Physical space is measured in terms of winding modes.
- In terms of winding modes the contraction as $t \to 0$ corresponds to expansion.

$$\bullet$$
 $t \to 0 \equiv t_d \to \infty$

- In terms of physical variables: bouncing cosmology.

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- \bullet $t \to 0 \equiv t_d \to \infty$
- In terms of physical variables: bouncing cosmology.
- Conclusion: nonsingular cosmology.

Next Step: Double Field Theory as a Background for String Gas Cosmology

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Idea Describe the low-energy degrees of freedom with an action in doubled space in which the T-duality symmetry is manifest.

Candidate for dynamics in the Hagedorn phase: Double Field Theory [W. Siegel, 1993, C. Hull and B. Zwiebach, 2009], L. Freidel et al., 2017]

$$S = \int dx d\tilde{x} e^{-2d} \mathcal{R},$$

$$\mathcal{R} = \frac{1}{8} \mathcal{H}^{MN} \partial_{M} \mathcal{H}^{KL} \partial_{N} \mathcal{H}_{KL} - \frac{1}{2} \mathcal{H}^{MN} \partial_{M} \mathcal{H}^{KL} \partial_{K} \mathcal{H}_{NL}$$

$$+ 4 \mathcal{H}^{MN} \partial_{M} \partial_{N} d - \partial_{M} \partial_{N} \mathcal{H}^{MN} - 4 \mathcal{H}^{MN} \partial_{M} d \partial_{N} d$$

$$+ 4 \partial_{M} \mathcal{H}^{MN} \partial_{N} d + \frac{1}{2} \eta^{MN} \eta^{KL} \partial_{M} \mathcal{E}^{A}_{K} \partial_{N} \mathcal{E}^{B}_{L} \mathcal{H}_{AB}.$$

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$$\mathcal{H}_{MN} = \begin{bmatrix} g^{ij} & -g^{ik}b_{kj} \\ b_{ik}g^{kj} & g_{ij} - b_{ik}g^{kl}b_{lj} \end{bmatrix}.$$
 $X^{M} = (\tilde{x}_{i}, x^{i}),$
 $\eta^{MN} = \begin{bmatrix} 0 & \delta_{i}^{\ j} \\ \delta^{i}_{j} & 0 \end{bmatrix}.$

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- Cosmology of string theory must take into account the key symmetries of string theory, in particular the T-duality symmetry.
- Standard effective field theory of supergravity will break down in the very early universe.
- Double Field Theory may provide a better description of the background for string cosmology.
- Cosmological evolution is nonsingular.
- Our universe emerges from an early Hagedorn phase.
- Thermal string fluctuations in the Hagedorn phase yield an almost scale-invariant spectrum of cosmological fluctuations.
- Characteristic signal: blue tilt in the spectrum of gravitational waves.

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