

Title: Soft photons, gravitons, and their quantum information content

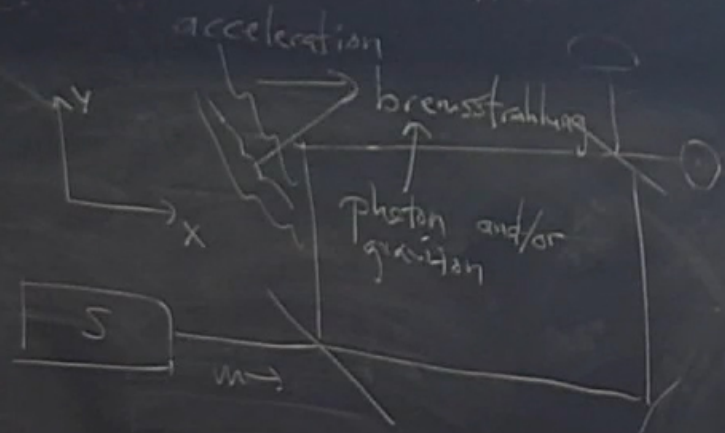
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URL: <http://pirsa.org/18060003>

Abstract:

In brief

$$|p\hat{x}\rangle \rightarrow \frac{1}{\sqrt{2}} |p\hat{x}\rangle + \int_{rad} d\omega_{rad} |p\hat{y}, rad\rangle$$



Radiation is massless

- can radiate arb. large # quanta  
(arb. small energy each)

IR catastrophe

- $E_{\text{detector}} > 0 \Rightarrow$  can't detect rad

$\Rightarrow$  since

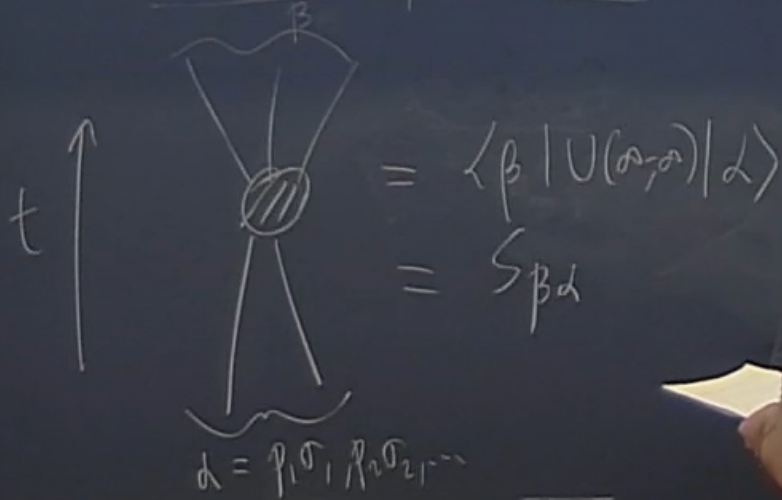
$\Rightarrow$  decouple massive "hard" particles

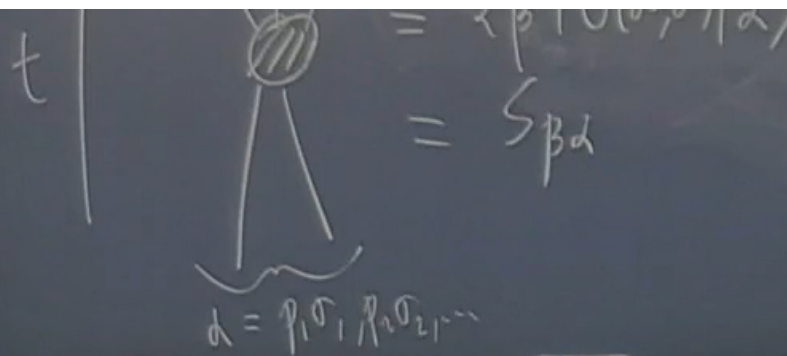
# IR catastrophe

- $E_{\text{detector}} > 0 \Rightarrow$  can't detect red  $\Rightarrow$  trace  $\Rightarrow$  decohere massive "hard" particles

## IR catastrophe redux

(Bloch-Nordsieck QED, Weinberg Pert. grav)





$\lambda = \text{IR regulator}$   
 goal  $\lambda \rightarrow 0$  at end  
 $\Lambda = \text{define virtual soft}$   
 $E = \text{define soft emitted (detector resolution)}$   
 ~~$\chi_{\text{soft}} \Lambda$~~   
 ~~$\chi_{\text{soft}} E$~~

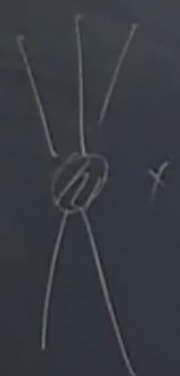
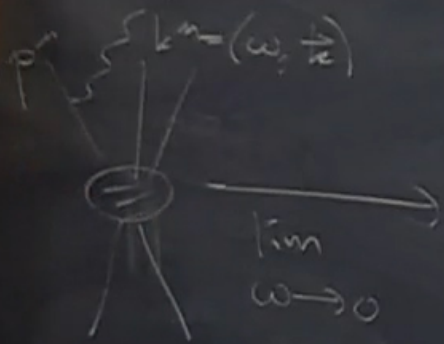
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IR catastrophe

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 $\Rightarrow$   $\delta$  iace  
 $\Rightarrow$  decohere massive "hard" particles

Soft theorem



photon

$$\left( \frac{e p^\mu \cdot \epsilon_\nu(k)}{p \cdot k} \right)$$

graviton

$$\text{or } \left( \frac{p^\mu p^\nu \epsilon_{\mu\nu}}{M_{\text{pl}}^2 p \cdot k} \right)$$

poles as  $\omega \rightarrow 0$

Soft thms  $\Rightarrow$  return all soft contributions

$$\sum_{\text{loops w/ } \lambda \text{ w/ } \Lambda} = \underbrace{\int \beta d}_{\text{no IR loop}} \times \binom{\lambda}{\Lambda} A+B$$

$$(EM) \quad A = \sum_{n,m} e_n e_m \gamma_n \gamma_m f_{nm}(\beta_{nm}) \geq 0$$

inward particles

+1 inc.  
-1 out.

relative velocity

$$\Rightarrow \int_{\beta < 0} \rightarrow 0$$

$$(GR) \quad B = \sum_{nm} \frac{m_n m_m}{M_p} \gamma_n \gamma_m g_{nm}(\beta_{nm}) \geq 0 \quad (IR \text{ catastrophe})$$



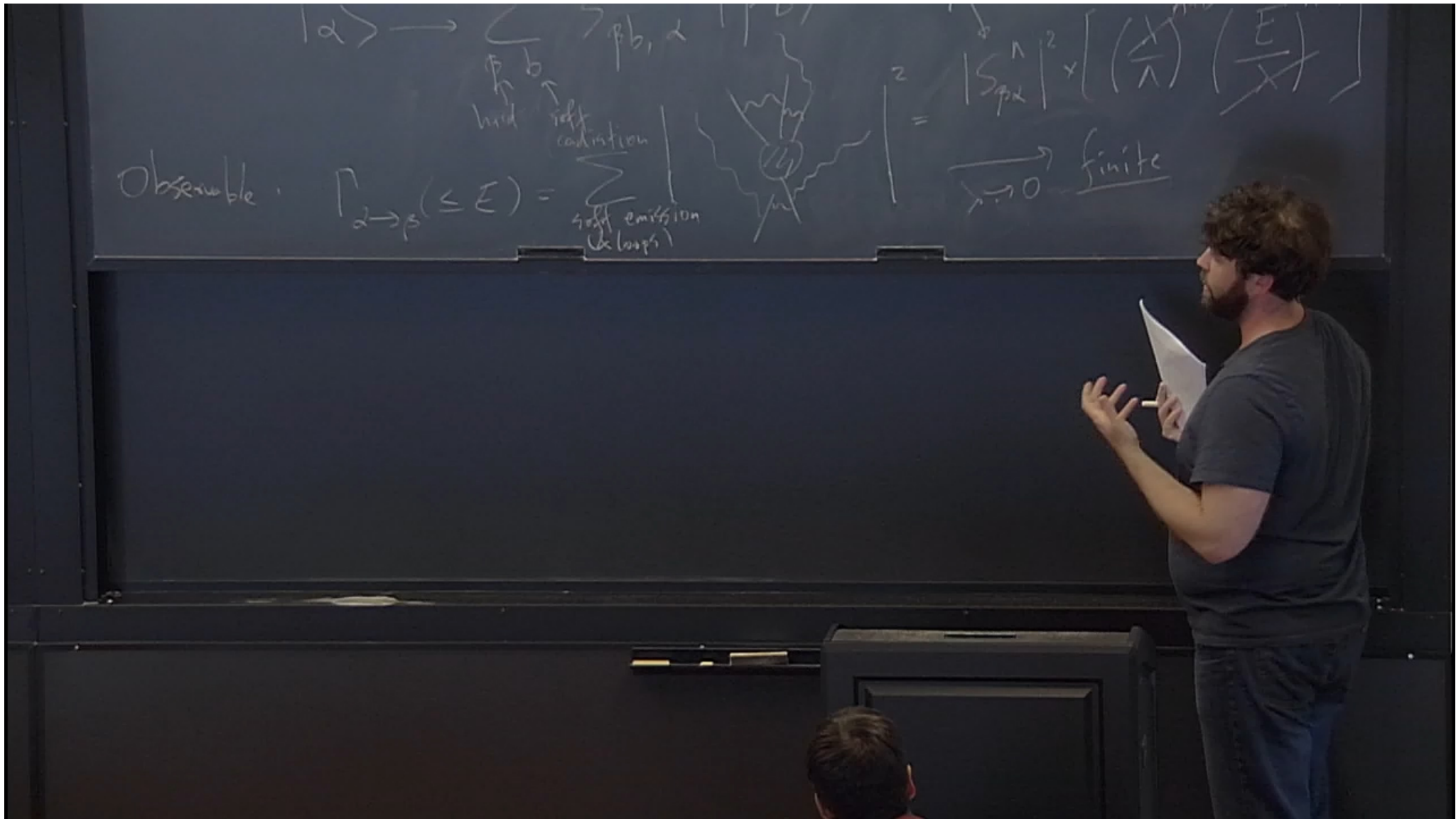
Solution: finite energy resolution  $\rightarrow$  should include soft emission

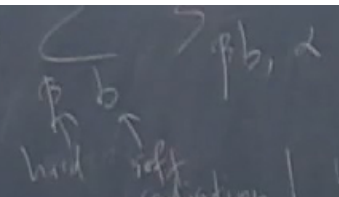
• Form inclusive quantities

$$|\alpha\rangle \rightarrow \sum_{\beta} S_{\beta\alpha} |\beta\rangle$$

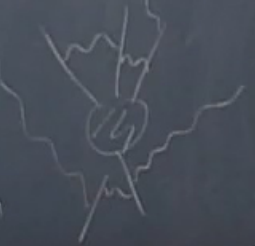
$\beta$   
 $\uparrow$   
hard

$b$   
 $\uparrow$   
soft radiation



$|\alpha\rangle \rightarrow$  

Observable:  $\Gamma_{\alpha \rightarrow \beta}(\leq E) = \sum_{\text{soft emission (loops)}} |S_{\beta\alpha}|^2$

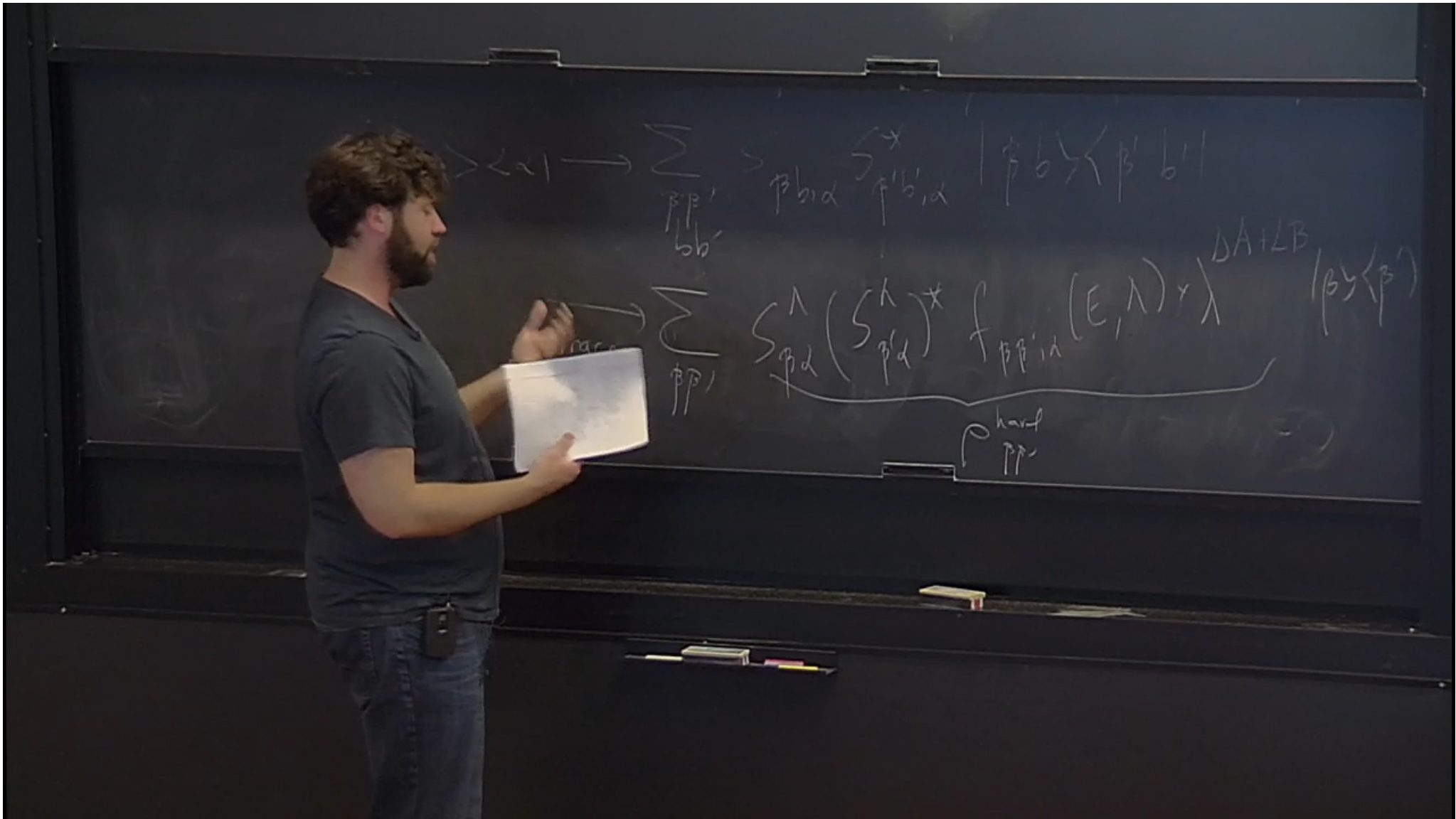


$\xrightarrow{\lambda \rightarrow 0}$  finite  $\left( \text{factor } \left( \frac{E}{\lambda} \right)^{A+B} \right)$

Decoherence What does this say about DM?

$$\rho = |\alpha\rangle\langle\alpha| \rightarrow \sum_{\substack{p,p' \\ b,b'}} S_{b|\alpha\rangle}^p S_{p'|b\rangle}^{*\alpha} |\beta\rangle\langle\beta|$$

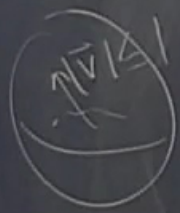
trace soft  $\rightarrow \sum_{p,p'} S_{p|\alpha\rangle}^\Lambda (S_{p'|\alpha\rangle}^\Lambda)^* f_{p,p'}(E, \Lambda) \lambda^{\Delta A + \Delta B}$



Observable  $\Gamma_{\alpha \rightarrow \beta}(\leq E) = \sum_{\text{soft emission (loops)}} \dots \xrightarrow{\lambda \rightarrow 0} \text{finite} \left( \frac{E}{\lambda} \right)^{A+B}$

→ What superpositions  $\beta, \beta'$  survive  $\lambda \rightarrow 0$ ?

• Basically nothing For each  $\vec{v}$ , let



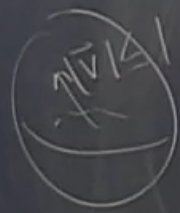
$$j_{\vec{v}}^{EM} = \sum_{\text{species}} e_i a_{\vec{v}}^+ a_{\vec{v}}^- = \text{total electric charge coming out w/ velocity } \vec{v}$$

$$j_{\vec{v}}^{GR} = \sum_i m_i a_{\vec{v}}^+ a_{\vec{v}}^- = \text{total mass}$$

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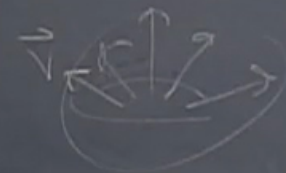
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Thm:  $\lim_{\lambda \rightarrow 0} \rho_{pp'}^{\text{hard}} \neq 0$  iff  $\exists \rho \equiv \rho' \forall \Delta$ .

outgoing state:

$$\rho \sim \begin{pmatrix} |S_{p\alpha}|^2 \left(\frac{\epsilon}{\lambda}\right) & 0 & 0 \\ 0 & |S_{p\beta}|^2 \left(\frac{\epsilon}{\lambda}\right) & 0 \\ 0 & 0 & \dots \\ & & S_{i_2}^{\text{soft}} \left(\frac{\epsilon}{\lambda}\right) \end{pmatrix}$$

mostly diagonal



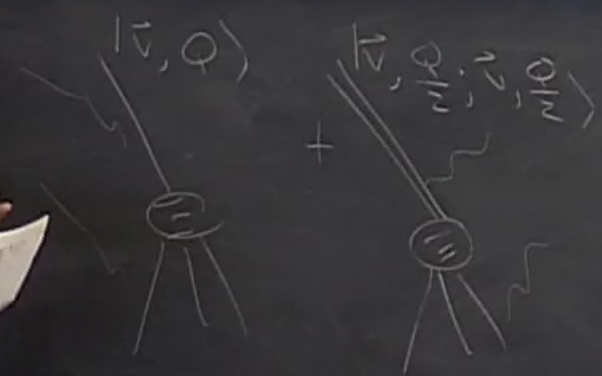
soft  $\rho_{pp'}$   $\lambda^{\alpha}$   $\rho_{pp'}^{\text{hard}}$



mostly  
diagonal

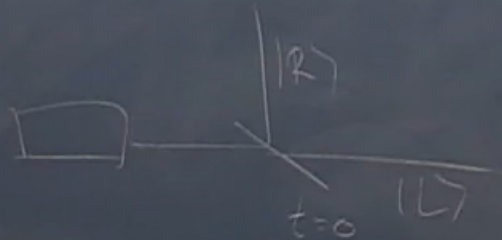
$$\begin{pmatrix} 0 & |S|^2 \frac{\epsilon}{\lambda} & 0 \\ 0 & 0 & \vdots \\ \vdots & \vdots & S_1^* S_2^* \frac{\epsilon}{\lambda} \end{pmatrix}$$

ex survival:

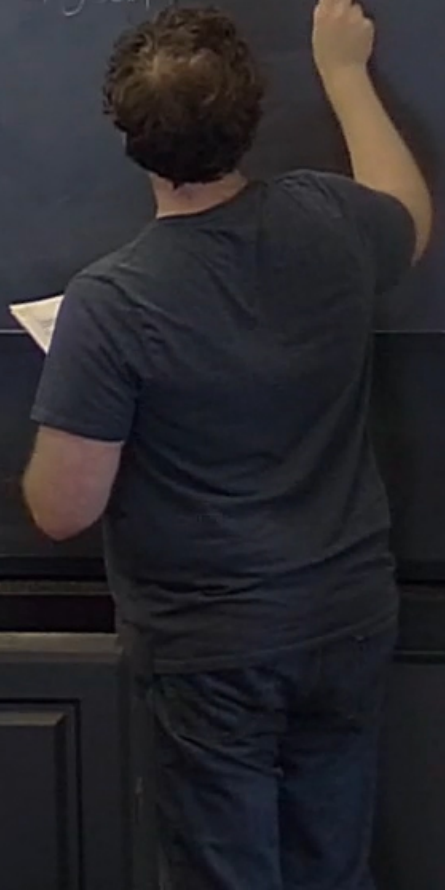


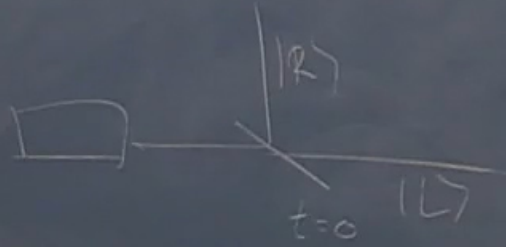
Remarks

- Real life: (LHC): finite time.  $T$  cuts off radiation spectrum.



$$P_{LR}(T) \sim P_{LR}(0) e^{-\left\{ \left( \frac{p}{M_{\text{pc}}} \right)^2 + \alpha^2 \right\} \ln / mc^2}$$

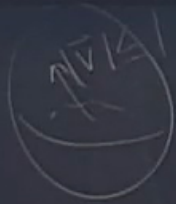




$$\rho_{ER}(T) \sim \rho_{ER}(0) e^{\left\{ \left( \frac{p}{M_p c} \right)^2 + Q^2 \right\} \ln \left( \frac{m c^2 \gamma}{\hbar} \right)}$$

nearly = 1 realist

$$M_p c \sim \text{kg m/s}$$



$\sum_i$  species

coming out w/ velocity

$$j_{GR}^{\vec{v}} = \sum_i E_i \vec{a}_i^{\vec{v}} \vec{a}_i^{\vec{v}} = \text{total mass}$$

$M_{pl} \sim \frac{kg}{m^2}$

Black hole info loss (cf. Strominger)

Make BH:  $|4\rangle \rightarrow$  (Hawking) (thermal)

$\rightarrow$  (Strominger)  $\sum_n c_n |n\rangle_{\text{soft}} |n\rangle_{\text{hard}}$   
s.t. trace soft  $\rightarrow$  (thermal) (hard) (?)