

Title: A no-go theorem for observer-independent facts

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Abstract: In his famous thought experiment, Wigner assigns an entangled state to the composite quantum system made up of Wigner's friend and her observed system. While the two of them have different accounts of the process, each Wigner and his friend can in principle verify his/her respective state assignments by performing an appropriate measurement. As manifested through a click in a detector or a specific position of the pointer, the outcomes of these measurements can be regarded as reflecting directly observable "facts". Reviewing arXiv:1507.05255, I will derive a no-go theorem for observer-independent facts, which would be common both for Wigner and the friend. I will then analyze this result in the context of a newly derived theorem in arXiv:1604.07422, where Frauchiger and Renner prove that "single-world interpretations of quantum theory cannot be self-consistent". It is argued that "self-consistency" has the same implications as the assumption that observational statements of different observers can be compared in a single (and hence an observer-independent) theoretical framework. The latter, however, may not be possible, if the statements are to be understood as relational in the sense that their determinacy is relative to an observer.

# A no-go theorem for observer-independent facts

Časlav Brukner

arXiv:1507.05255, 1804.00749

Algorithmic Information, Induction and Observers in Physics,  
Perimeter Institute, Waterloo, April 2018



# Outlook

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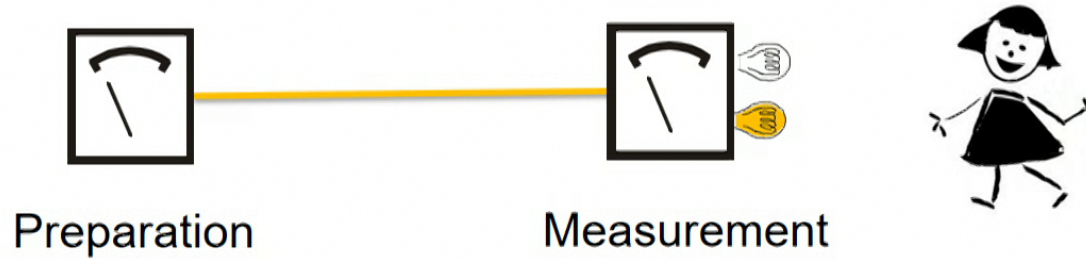
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- Part 2: Remark on Frauchiger-Renner paper

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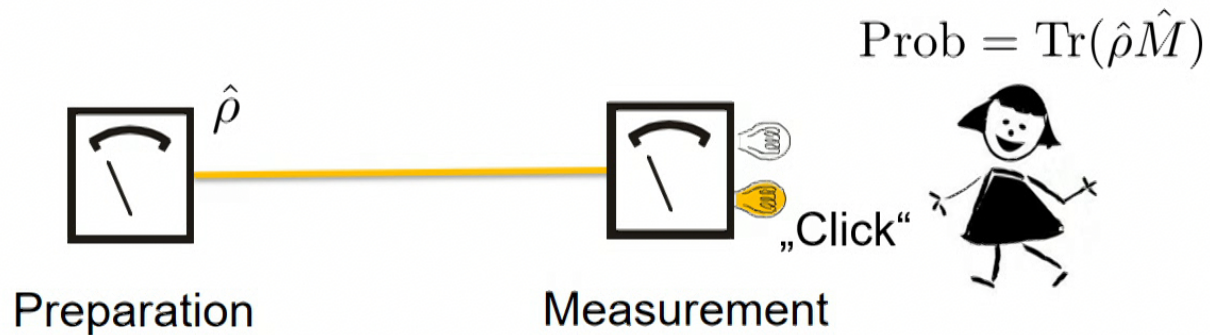
- Part 1:
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  - A no-go theorem for observer-independent facts
  - A way out: observer-dependent „relative facts“?
- Part 2: Remark on Frauchiger-Renner paper
- Part 3: Friend can find out that she is in a superposition state („failure of the standard quantum formalism“)

# Typical experimental situation





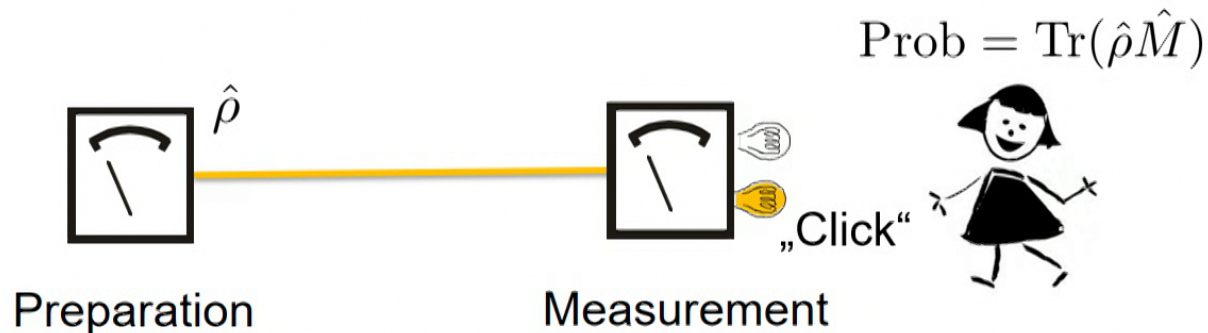
## Typical experimental situation



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- Nonetheless, measurement results, e.g. clicks of the detectors, are considered to be "real". They are "facts".



## „Minimal“ interpretation



“... the state vector is only a shorthand expression of that part of our information concerning the past of the system which is relevant for predicting (as far as possible) the future behaviour thereof.”

E. Wigner, *Symmetries and Reflections* (Indiana University Press, 1967), p. 164

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*Operational requirement:* Observer is able to verify her/his state assignment by performing a suitable measurement on the system.



## The “cut”



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W. Heisenberg in an unpublished response to the EPR paper in 1935.

## The “cut”

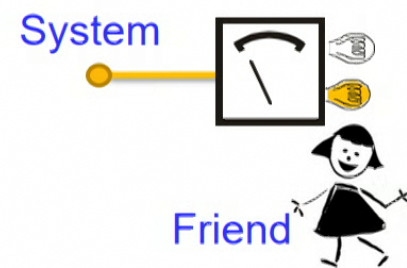


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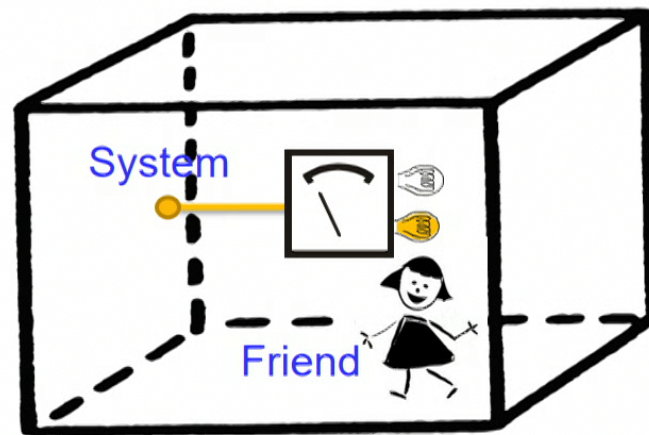
The „cut“ as a functional distinction between object and subject, not a physical one.

# The “cut”

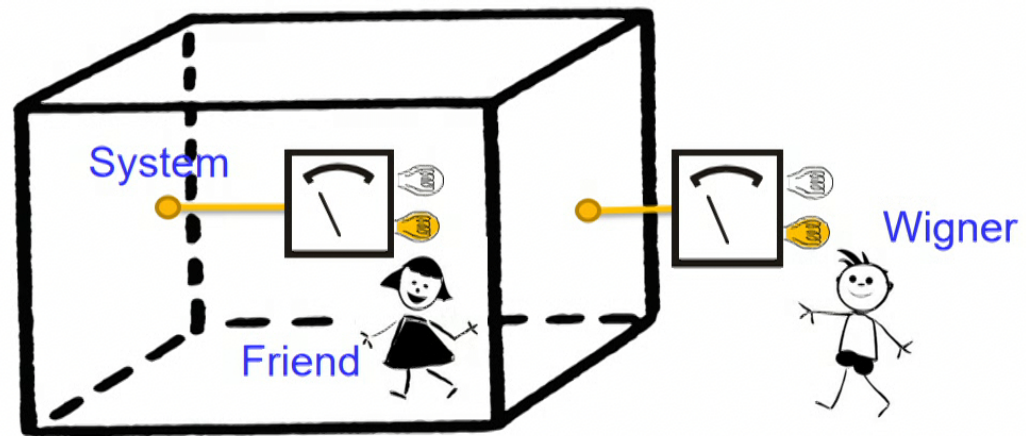




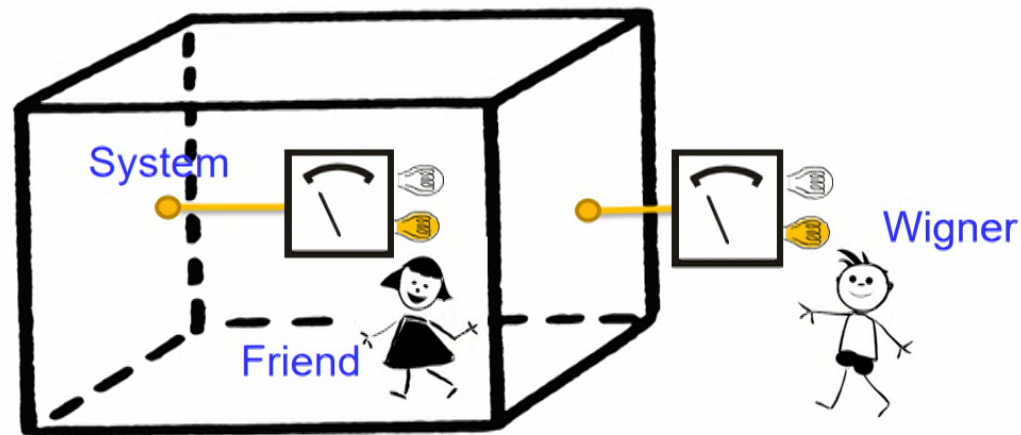
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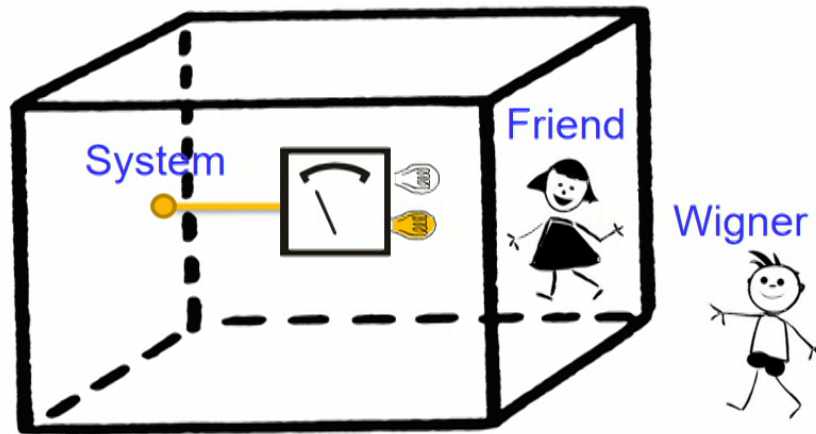
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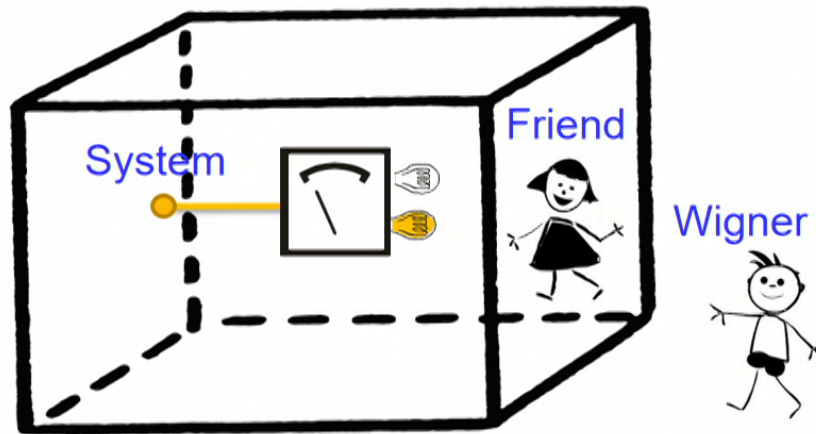
In moving the “cut”, the F’s measurement instrument loses its function and becomes itself a quantum system – an object that can be observed by a further set of W’s measurement instruments.



# Wigner's friend thought experiment



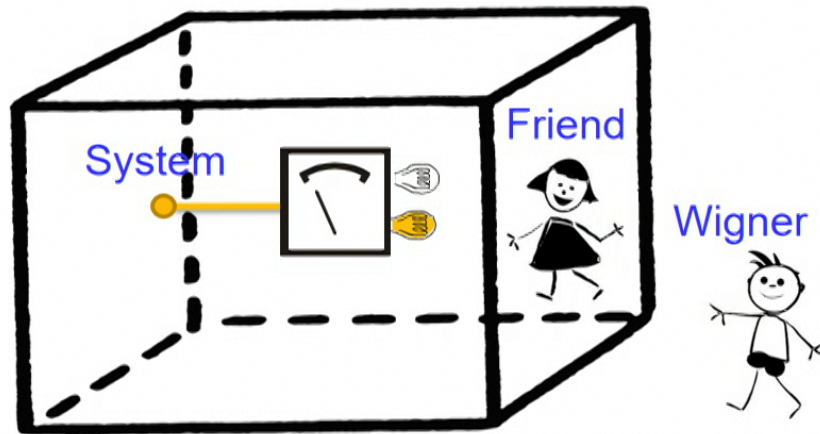
# Wigner's friend thought experiment



$$\text{Wigner: } |\psi_0\rangle^W = \frac{1}{\sqrt{2}}(|z+\rangle_S + |z-\rangle_S)|0\rangle_F$$



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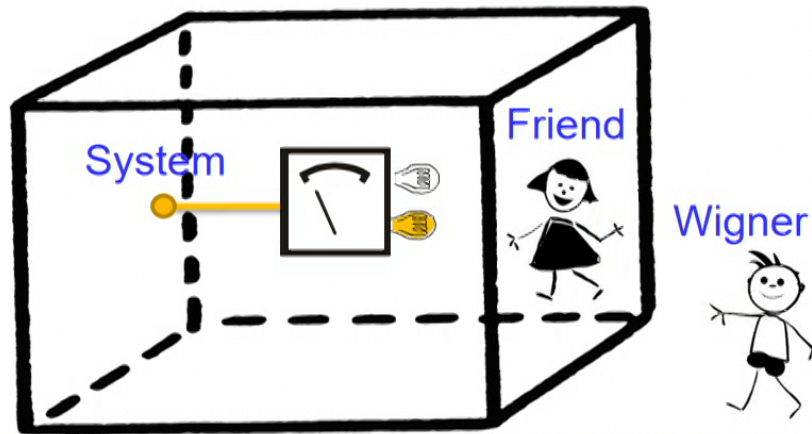
W can verify his state assignment by performing a measurement with outcomes:

$$|\psi_t\rangle^W \langle\psi_t|, \mathbb{1} - |\psi_t\rangle^W \langle\psi_t|$$

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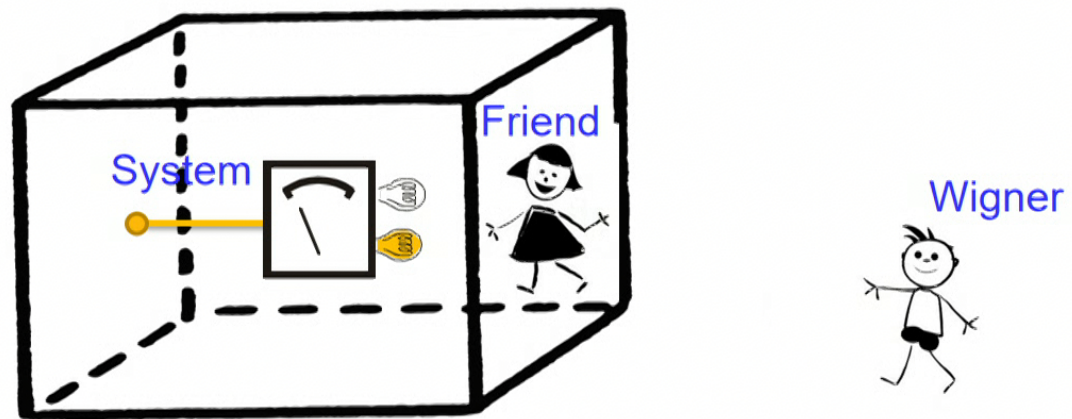
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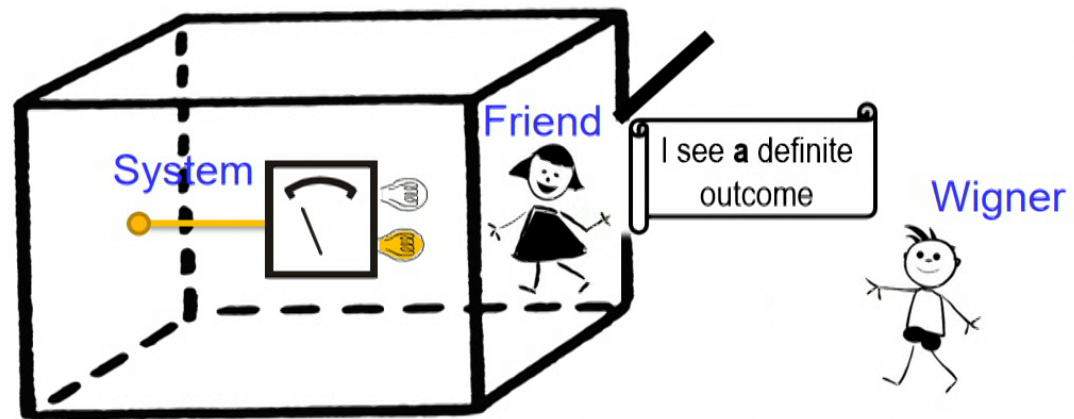
Friend: Either  $|z+\rangle_S|\text{see "up"}\rangle_F$  or  $|z-\rangle_S|\text{see "down"}\rangle_F$

## Deutsch's version of the experiment

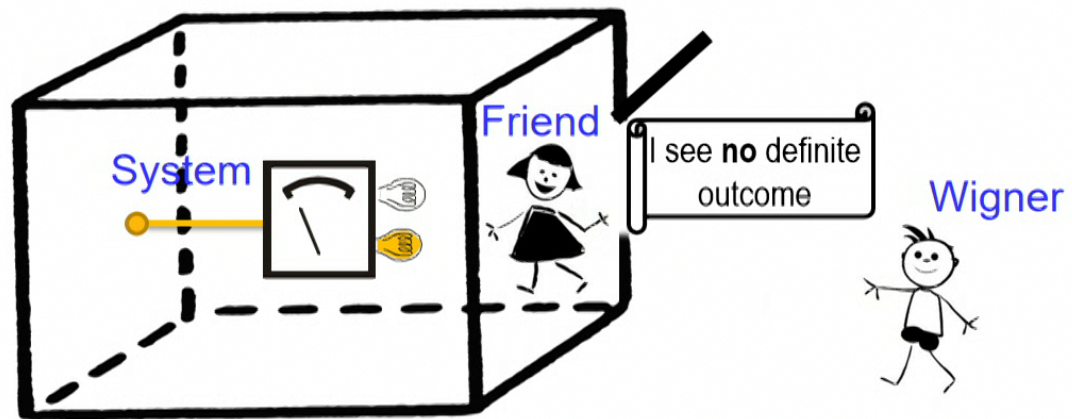




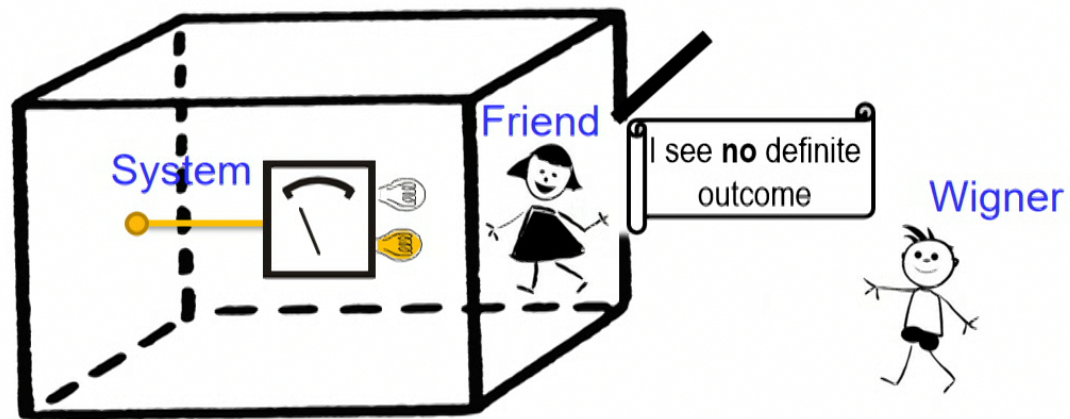
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$$|\psi_t\rangle_W = \frac{1}{\sqrt{2}}(|z+\rangle_S |see\ "up"\rangle_F + |z-\rangle_1 |see\ "down"\rangle_F) \otimes |I\ see\ \dots\rangle$$



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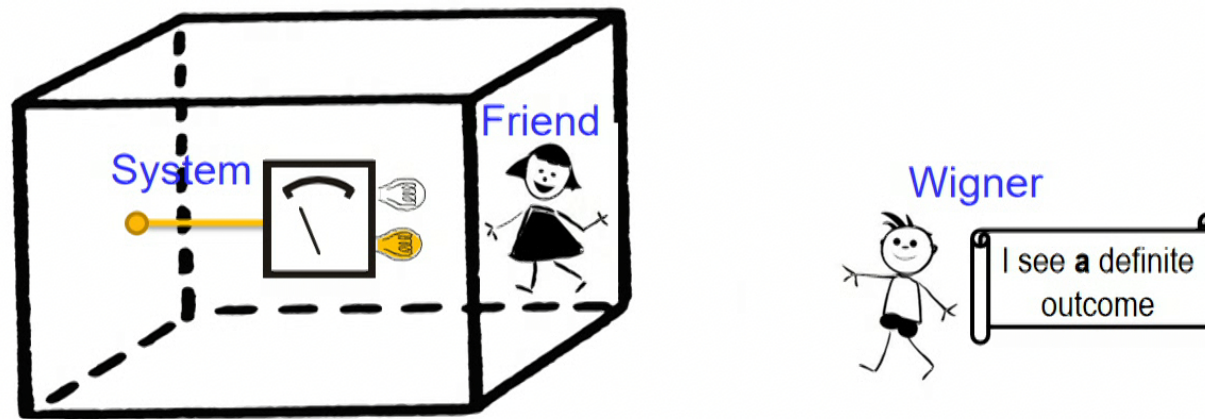
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1. The state collapses due to a breakdown of the quantum-mechanical laws. F observes a definite outcome. W cannot confirm the state.
2. W confirms the state, and yet F observes a definite outcome.

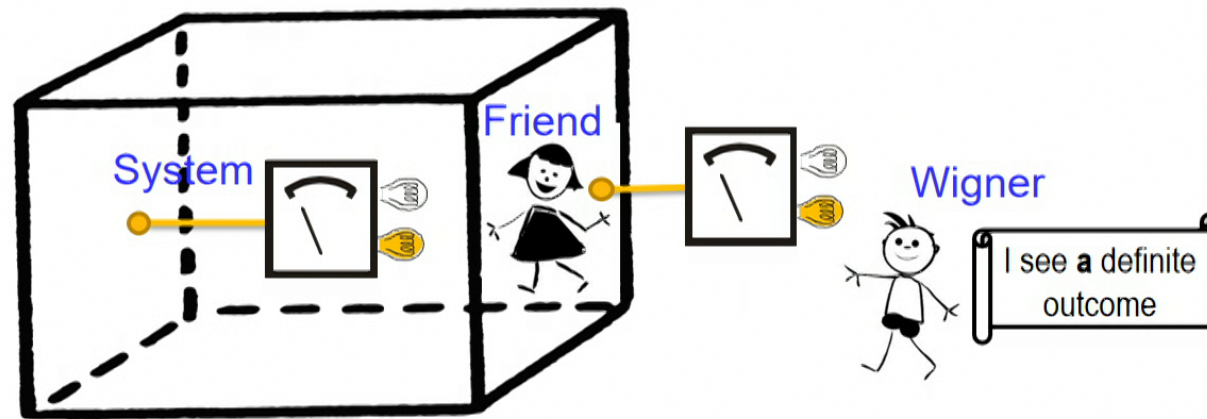


## Deutsch's version of the experiment



- W has a direct evidence that F has observed a definite outcome,

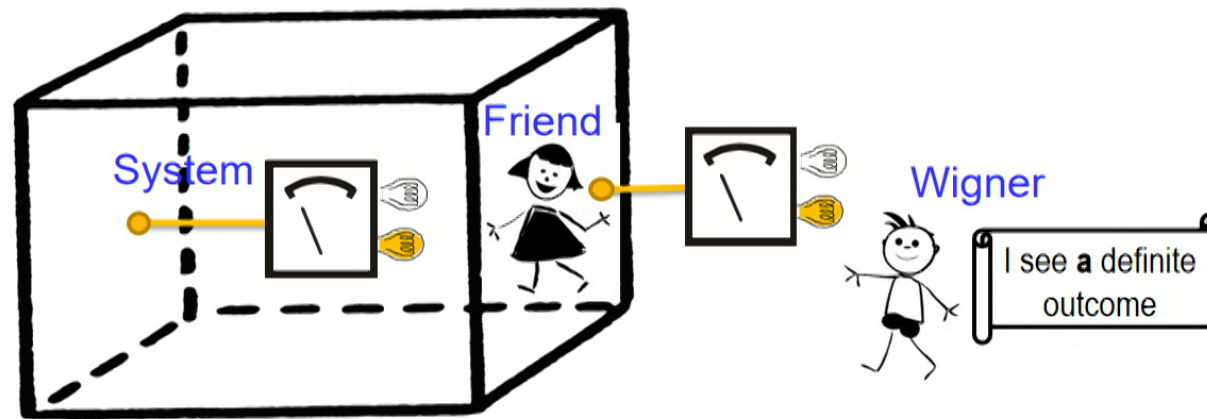
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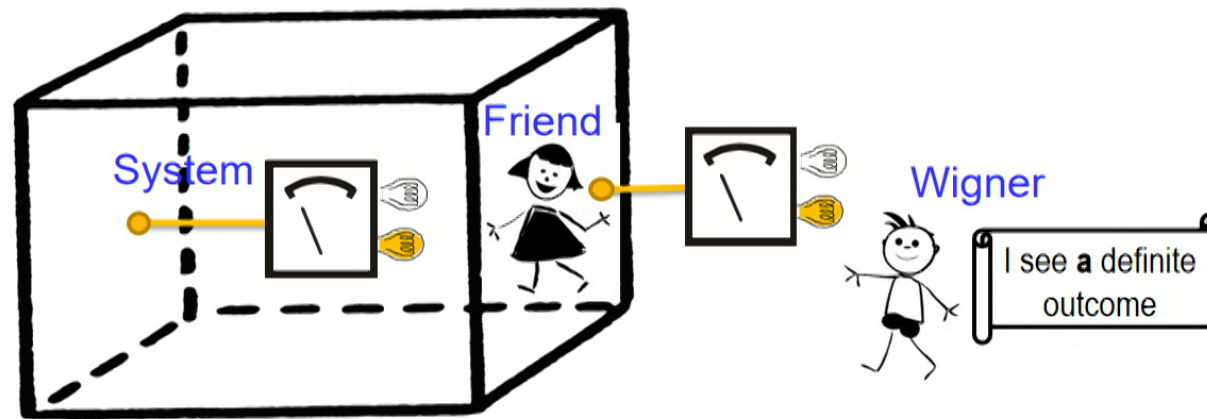
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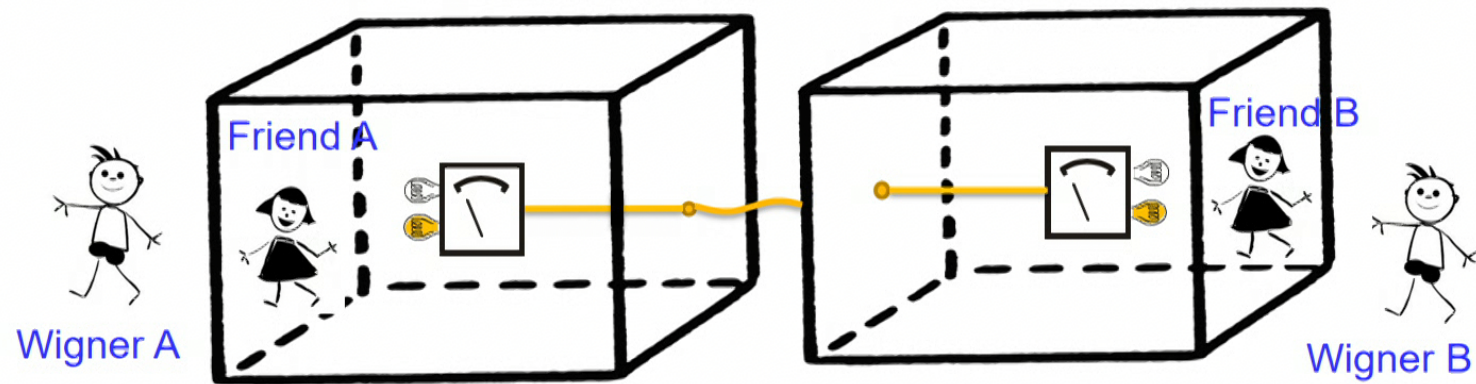
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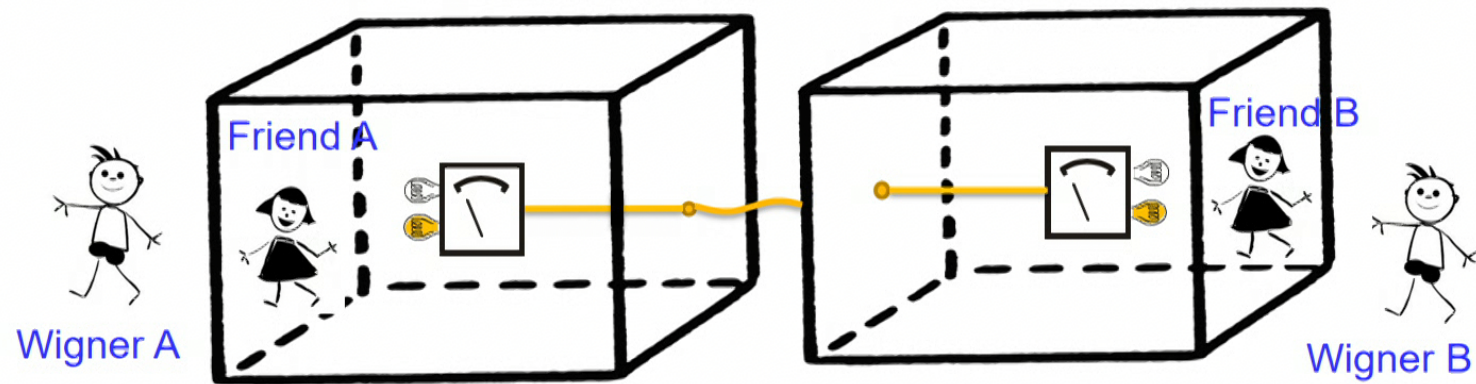


# Bell's test for Wigners & Friends



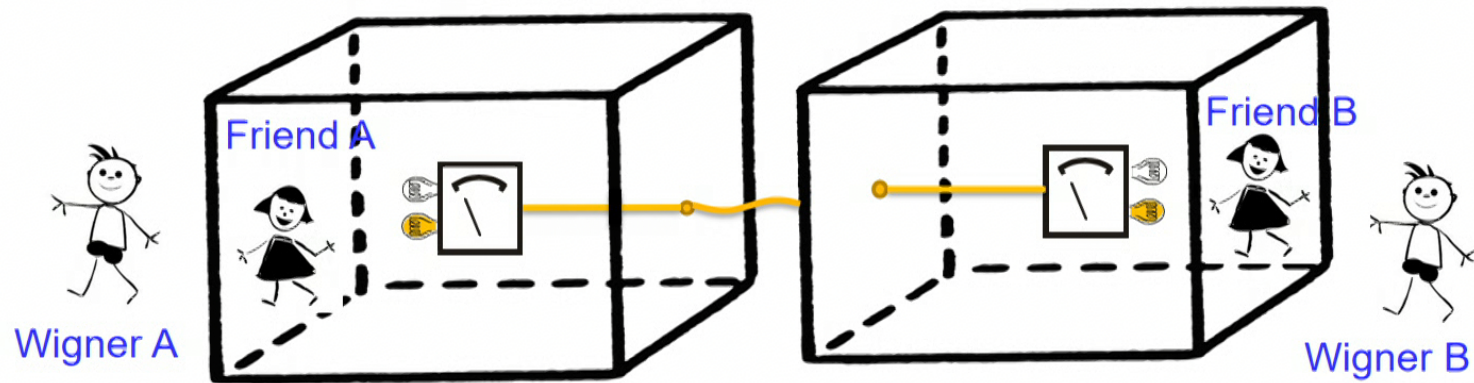


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$$\begin{aligned}
 |\psi\rangle^{W_A W_B} &= [(\mathbb{1} \otimes e^{-\frac{i}{2}\theta\hat{\sigma}_y})|\psi^-\rangle_{S_A S_B}][|0\rangle_{F_A}|0\rangle_{F_B}] \\
 &= (-\sin \frac{\theta}{2}|\phi^+\rangle_{S_A S_B} + \cos \frac{\theta}{2}|\psi^-\rangle_{S_A S_B})|0\rangle_{F_A}|0\rangle_{F_B}
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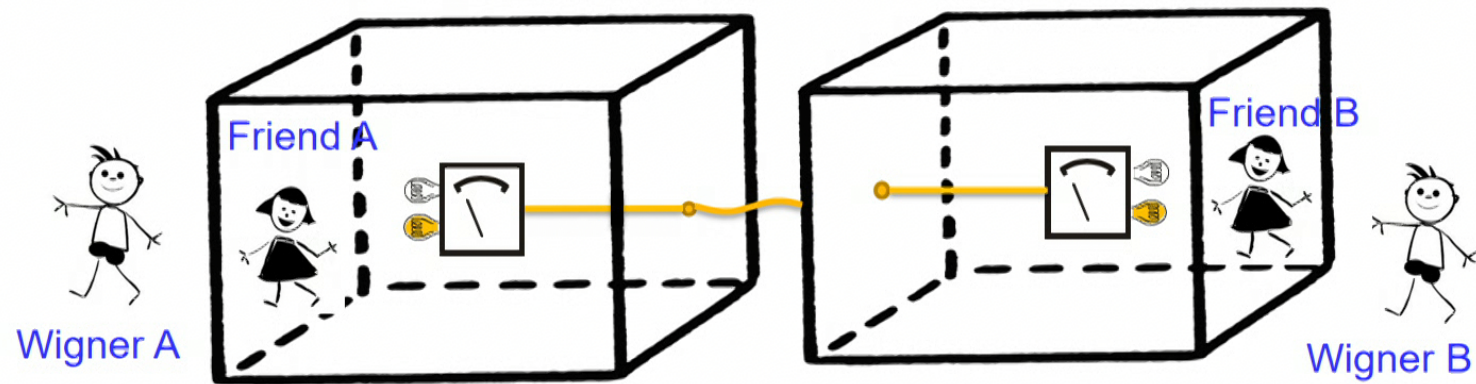
where

$$|\phi^+\rangle_{S_A S_B} = 1/\sqrt{2}(|z+\rangle_{S_A}|z+\rangle_{S_B} + |z-\rangle_{S_A}|z-\rangle_{S_B})$$

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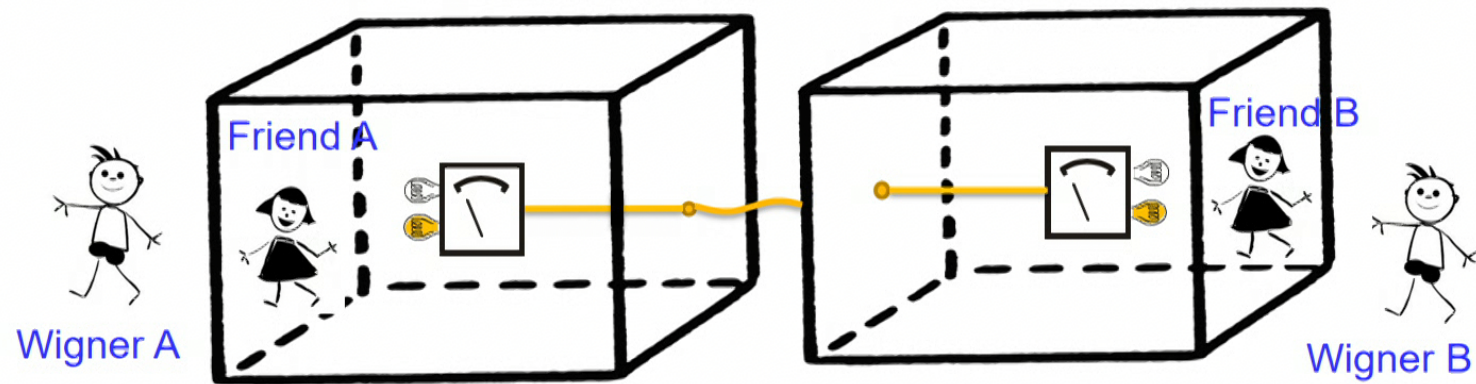
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$F_A$  and  $F_B$  perform measurements of the spins along  $z$ .

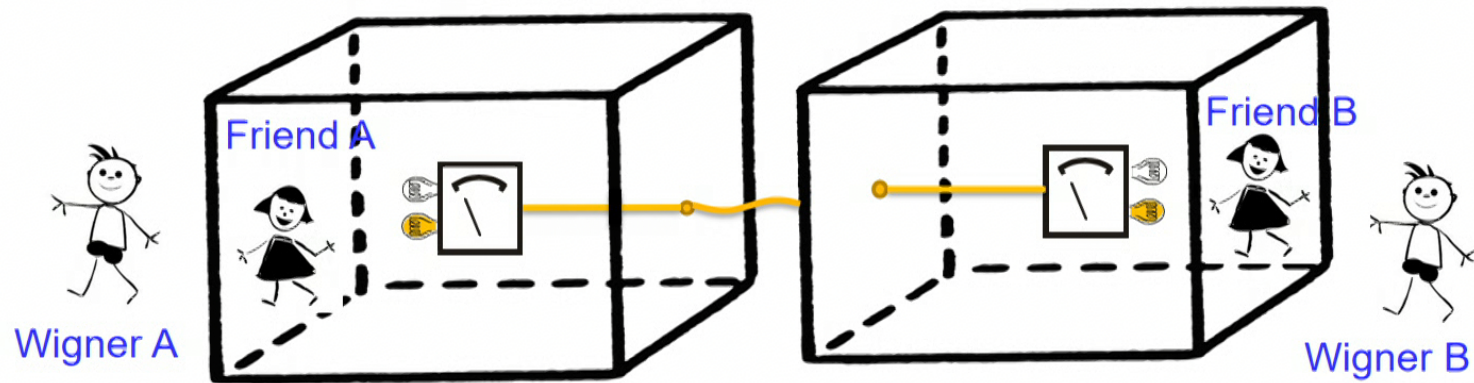


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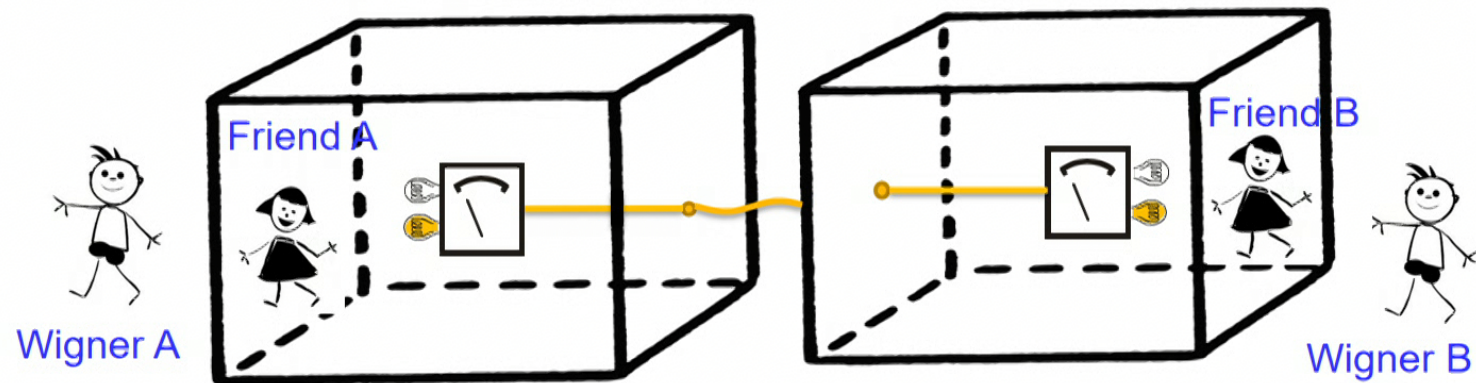
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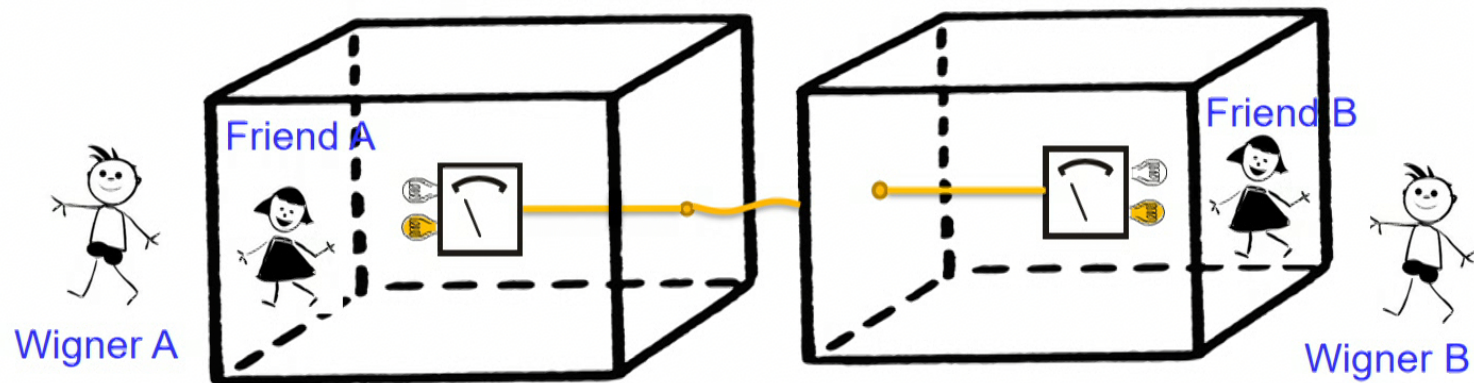


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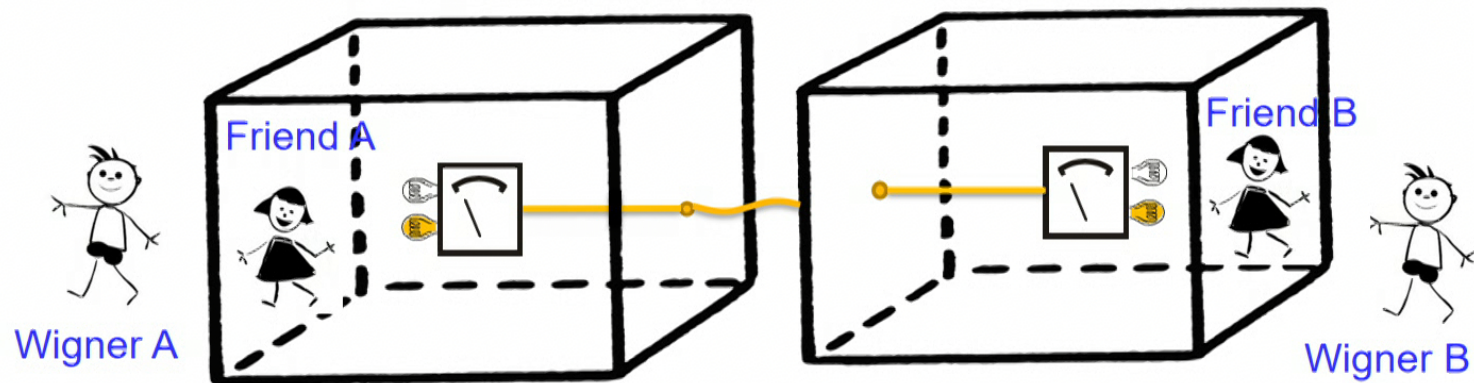
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where

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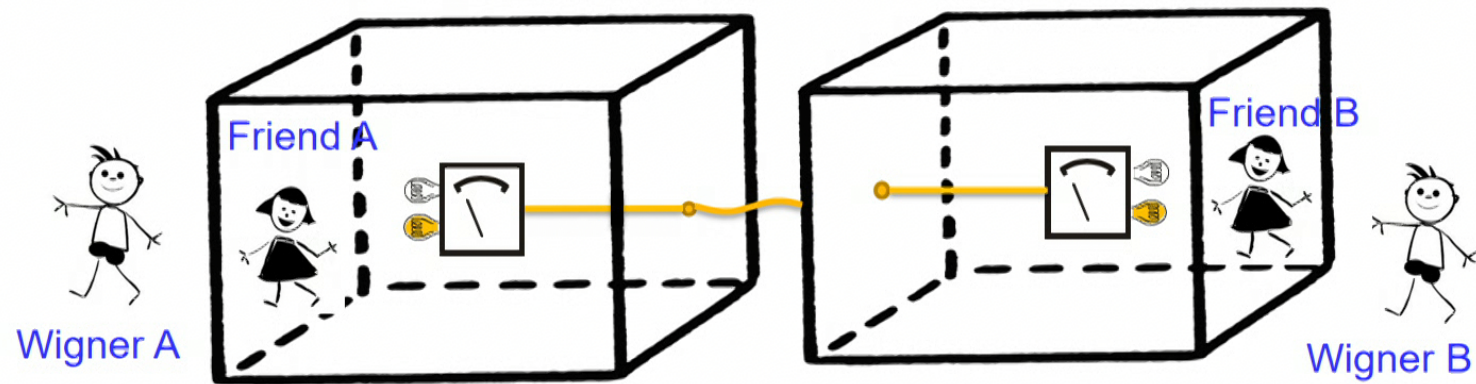
$$|A \text{ "down"}\rangle = |z-\rangle_{S_A} |\text{sees "down"}\rangle_{F_A}$$

$$|B \text{ "up"}\rangle = |z+\rangle_{S_B} |\text{sees "up"}\rangle_{F_B}$$

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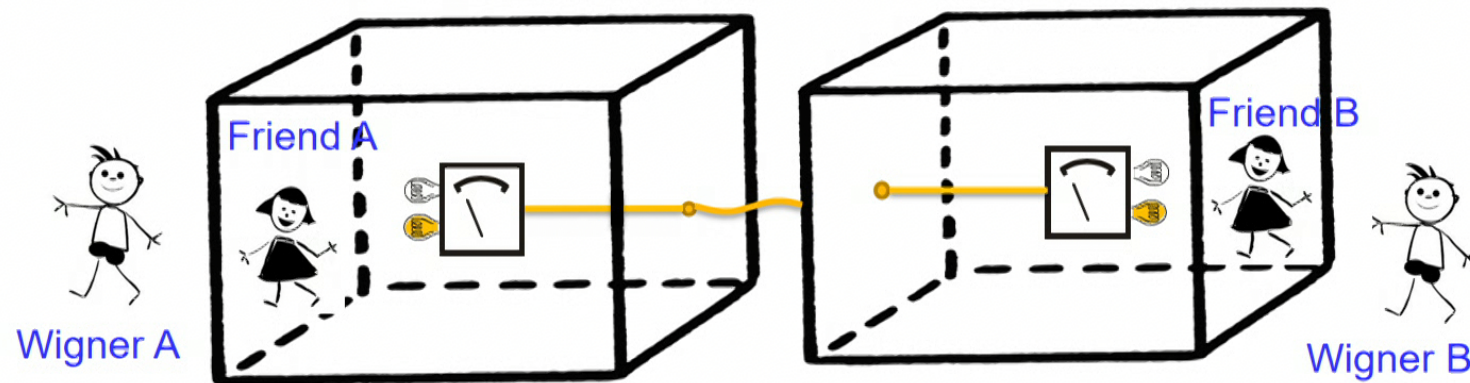


„Observation of the z-spin“: **F's fact**

$$A_1 = A_z = |A \text{ "up"}\rangle \langle A \text{ "up"}| - |A \text{ "down"}\rangle \langle A \text{ "down"}|$$



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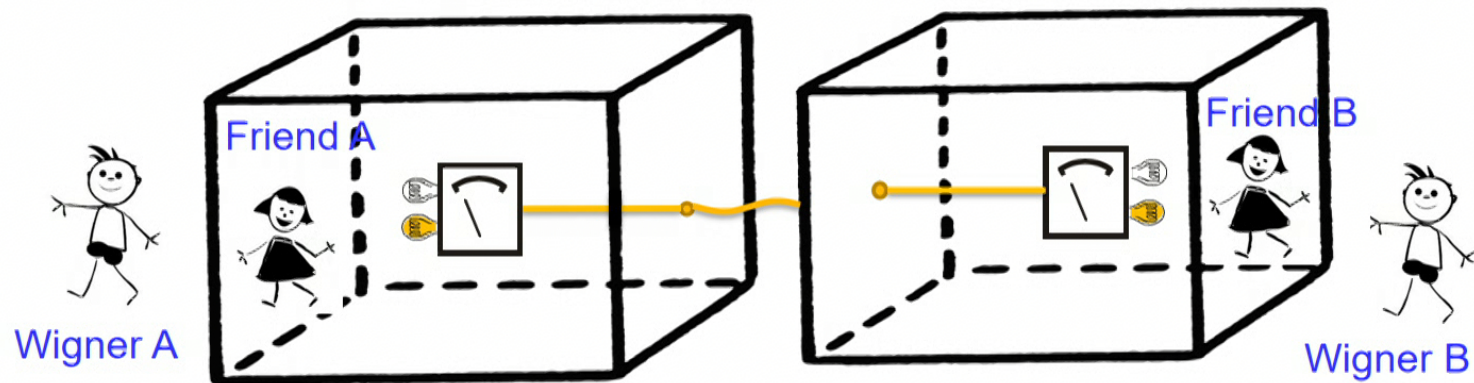
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„Observation of the x-spin“: **W's fact**

$$A_2 = A_x = |A \text{ "up"}\rangle \langle A \text{ "down"}| + |A \text{ "down"}\rangle \langle A \text{ "up"}|$$

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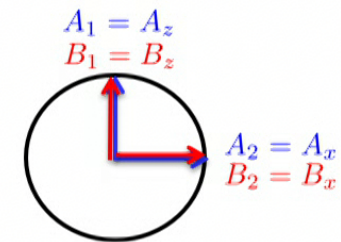


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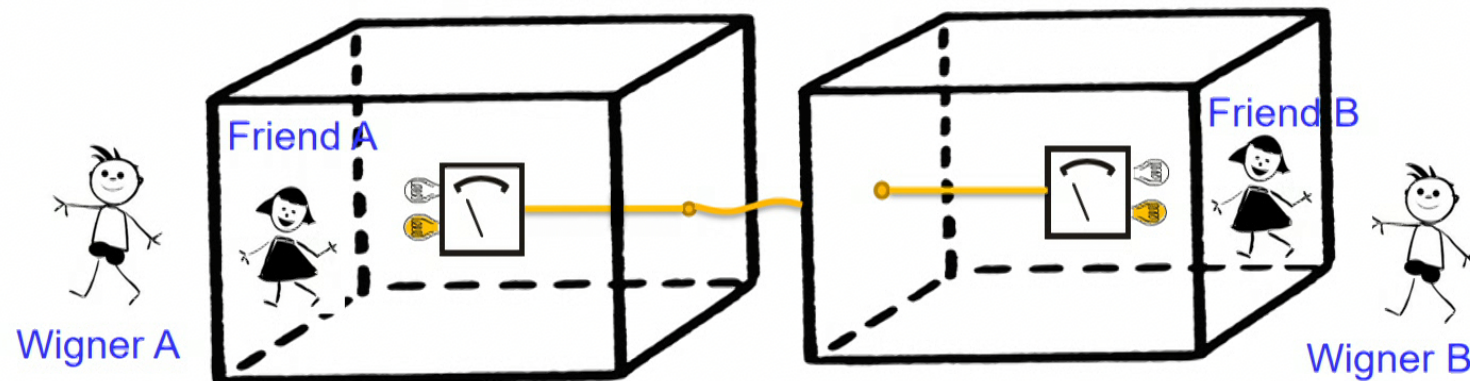
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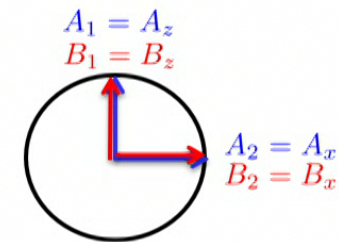


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$$|\langle A_1 B_1 \rangle + \langle A_1 B_2 \rangle + \langle A_2 B_1 \rangle - \langle A_2 B_2 \rangle| \leq 2 \quad \text{LHV}$$

$$2\sqrt{2} \quad \text{QM}$$



# The no-go theorem

1. **Universal validity of quantum theory**: The quantum predictions hold even if the measured system is large enough to contain itself an experimenter.
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4. **“Freedom of Choice”**: The choices of measurements are statistically independent of the rest of the experiment.

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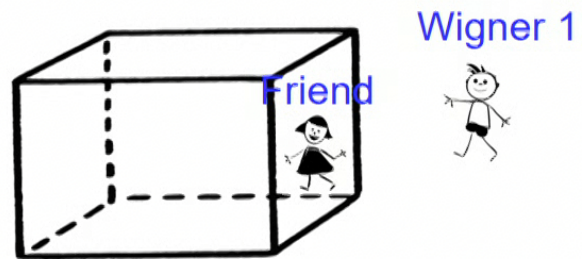
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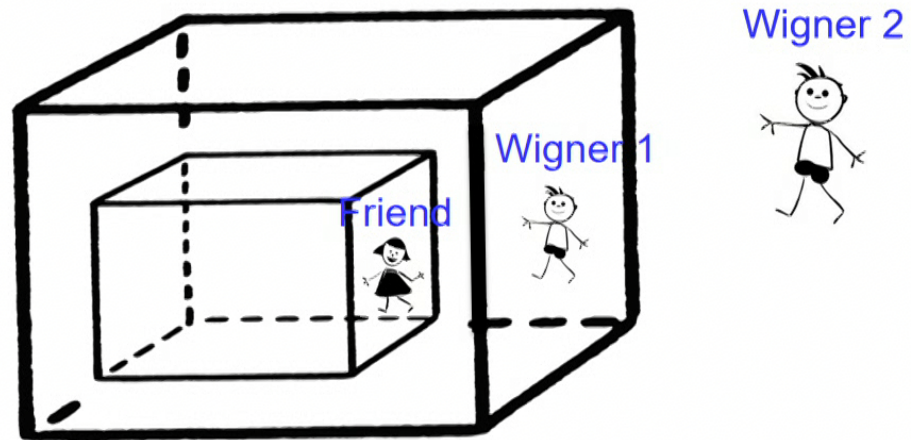
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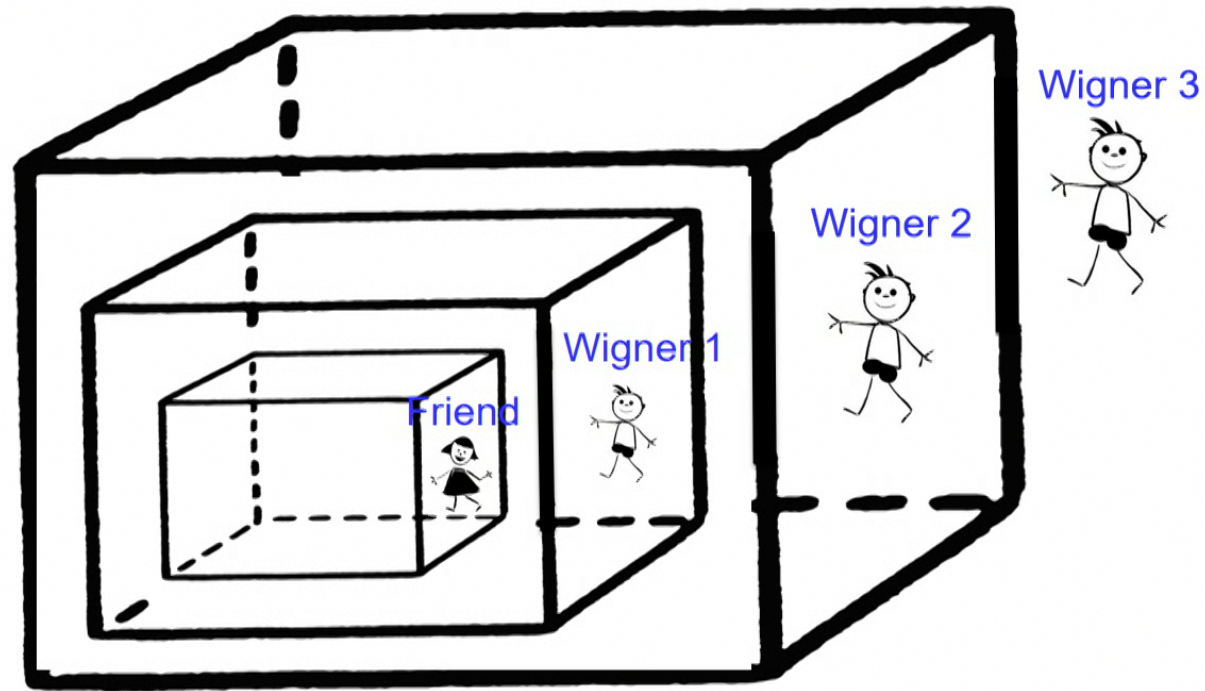


Wigner's facts fundamental? After all, he has superb instruments.

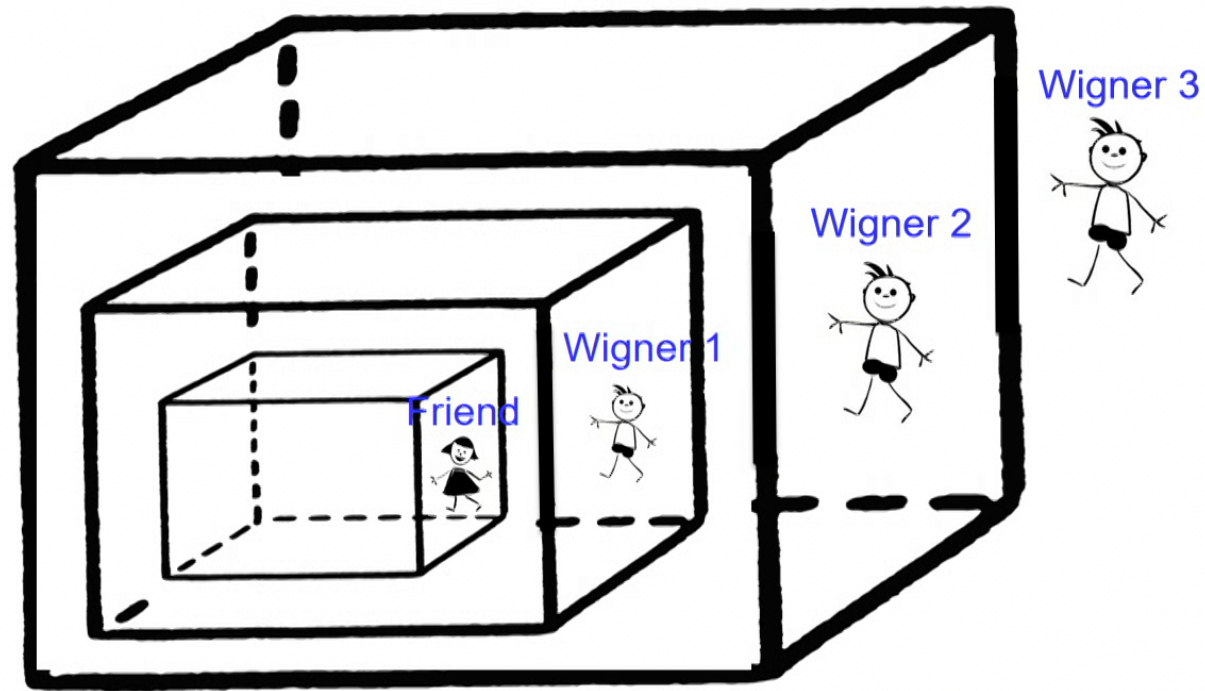




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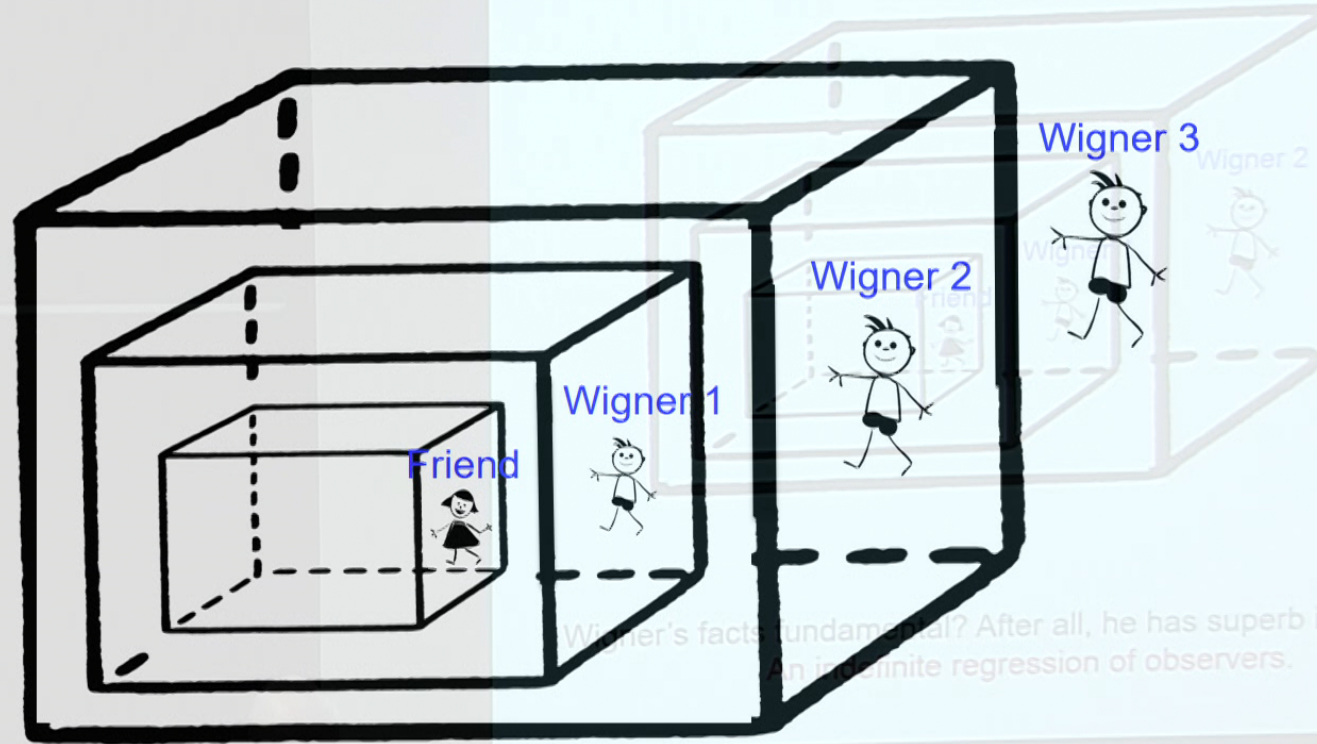


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**An indefinite regression of observers.**

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Another way out: *There are no “facts of the world” per se, but only relative to observers.*

Copenhagen (a version of it) , QBism, Relational int.

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# Part 2

# Frauchiger & Renner paper

arXiv:1604.07422

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“Single-world interpretations of quantum theory cannot be self-consistent.”



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The argument combines a set of statements  $S_1$ ,  $S_2$ ,  $S_3$  and  $S_4$  that involve different observers  $F_1$ ,  $F_2$ , A and W and can be drawn on the basis of theory T:

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**$S_1$ :** If  $F_1$  sees  $r = t$ , then W sees  $w \neq ok$ .

**$S_2$ :** If  $F_2$  sees  $z = +$ , then  $F_1$  sees  $r = t$ .

**$S_3$ :** If A sees  $x = ok$ , then  $F_2$  sees  $z = +$ .

**$S_4$ :** W sees  $w = ok$  and is told by A that  $x = ok$ .



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**SC** enables a “collapse others’ knowledge into one’s own”\*:

*“ $W$  knows that  $A$  knows that  $F_2$  knows that  $F_1$  knows that  $w \neq ok$ ”  
 $\Rightarrow$  “ $W$  knows that  $w \neq ok$ ”*

\*R. Renner, private communication



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$[P \wedge (P \Rightarrow Q) \wedge (Q \Rightarrow R) \wedge (R \Rightarrow S)] \Rightarrow S$ , which is in a contradiction with the directly observed:  $\neg S$ : “W sees  $w = ok$ ”

# Frauchiger & Renner paper

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**SC is also not satisfied in the theory of relativity:** Every inertial observer claims that her/his clock ticks slower than that of a moving partner.



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The statements **have only meaning with respect to the specific, observer-dependent, measurement procedure** defining “simultaneity”.

Similarly, the quantum states referring to outcomes of different observers in a Wigner-friend type of experiment have only meaning with respect to observers’ specific experimental arrangements, in agreement with Bohr’s idea of contextuality.



# Frauchiger & Renner paper

arXiv:1604.07422

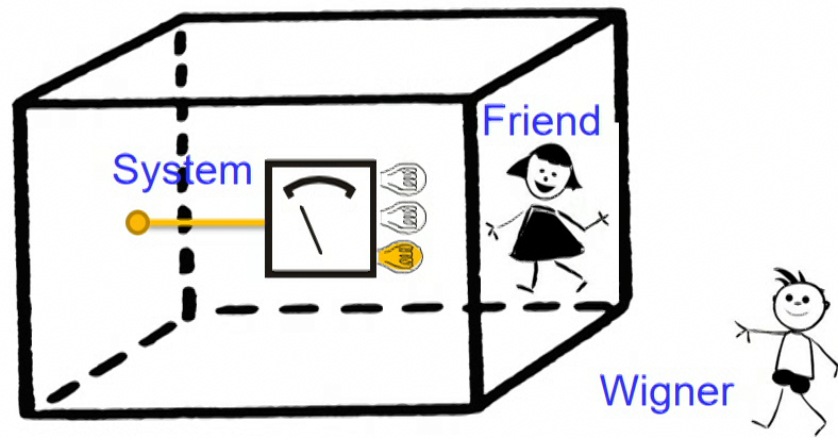
**Conceptual value:** The result points to the necessity to differentiate between ones' knowledge about direct observations and ones' knowledge about others' knowledge that is compatible with physical theories.

Important for **development of Bayesian inference** in situations as in the Wigner-friend experiment.

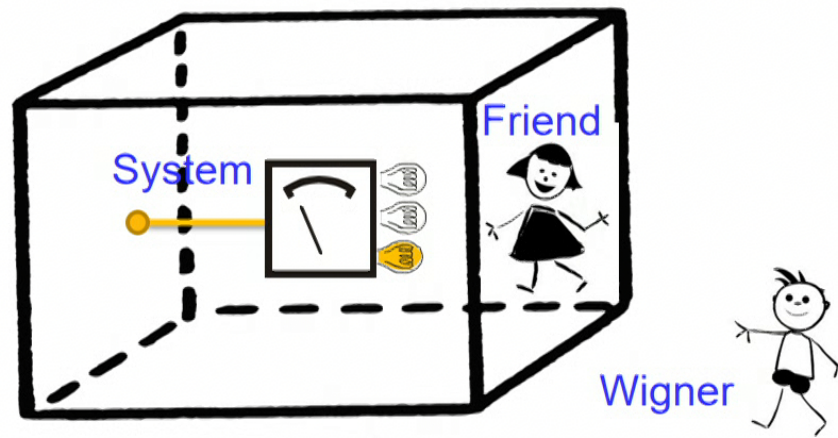
# Part 3



F can find out if she is in a superposition



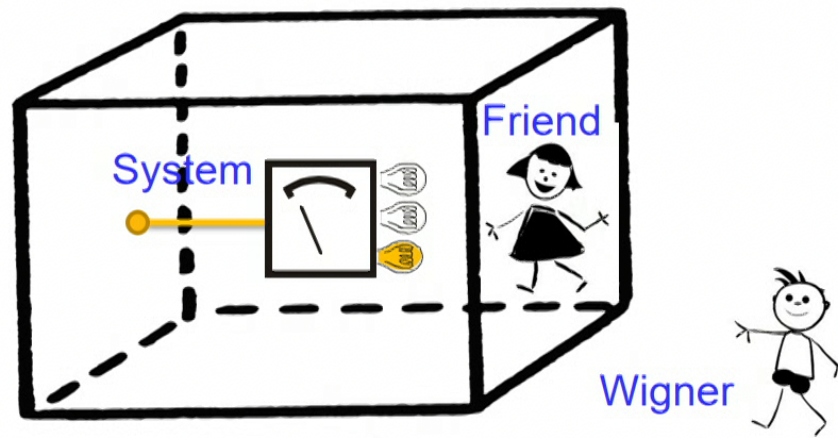
F can find out if she is in a superposition



$$|\psi\rangle = \frac{1}{\sqrt{d}} \sum_{i=1}^d |i\rangle_S |\text{see } "i"\rangle_F, \quad d \rightarrow \infty$$



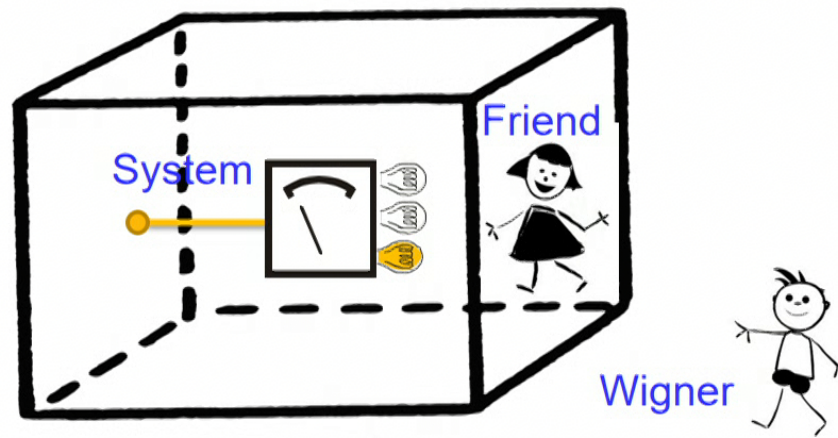
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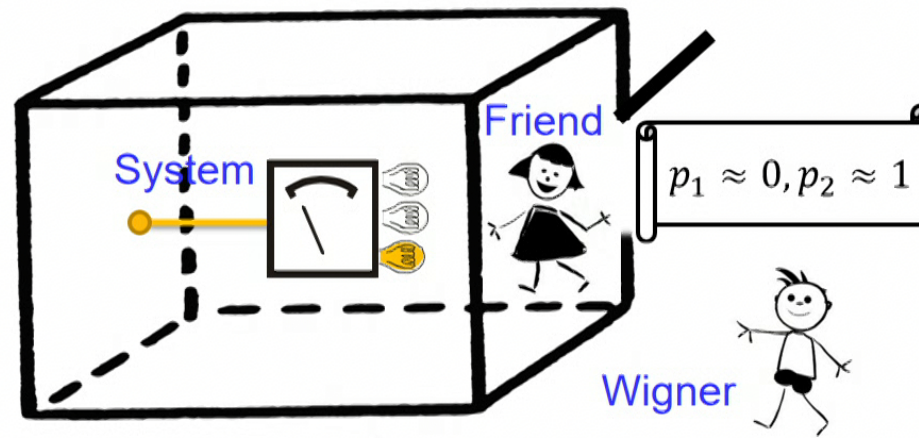


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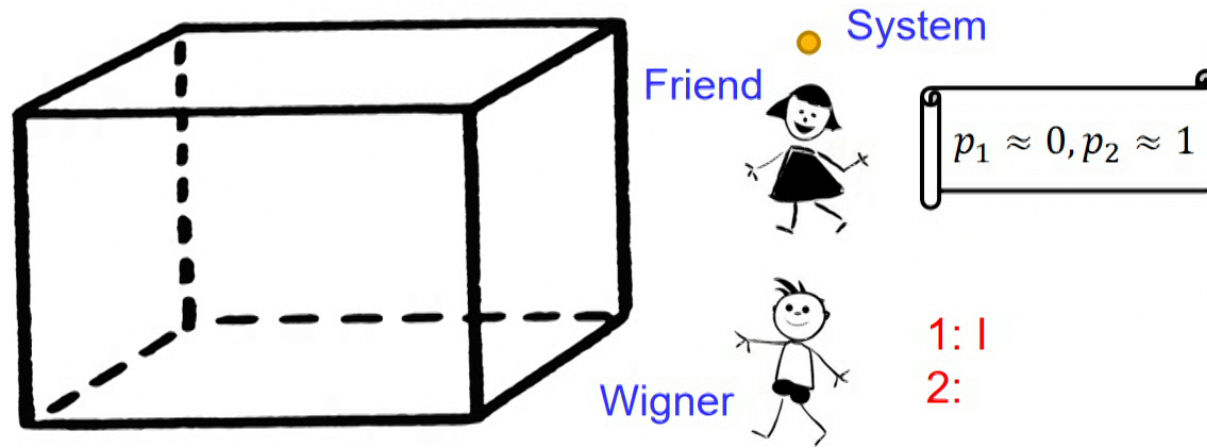
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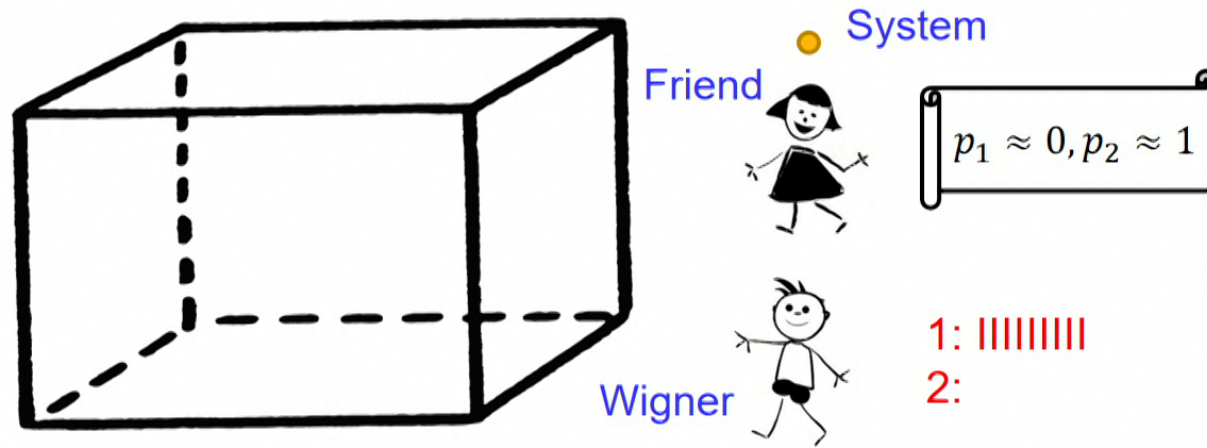


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In both cases there is an element of dissatisfaction as regarding to how an observer should practice QT.



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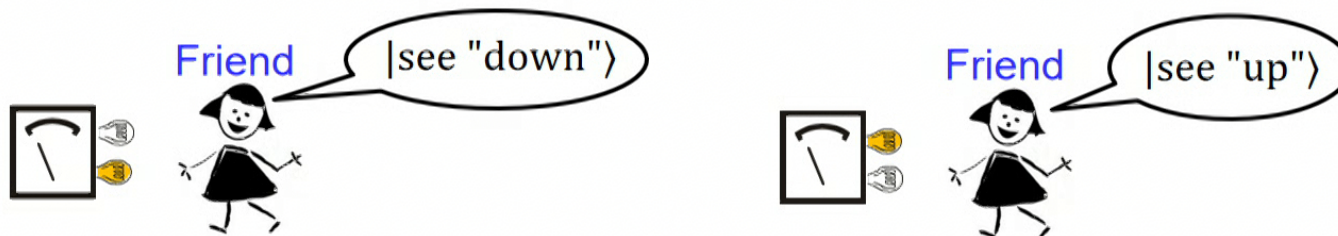
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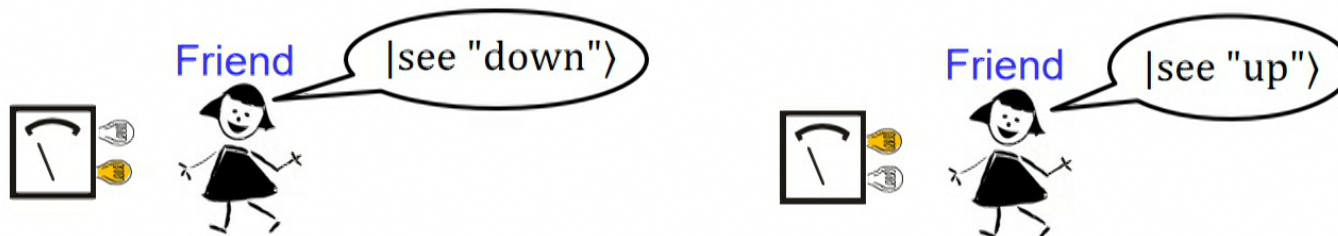
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„Problems“ arise if the predictions are about outcomes involving the “Schrödinger-cat states”,

$$\frac{1}{\sqrt{2}}(|\text{see "up"}\rangle_F + e^{i\Phi}|\text{see "down"}\rangle_F)$$





# Conclusions

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Č.B., arXiv:1507.05255, arXiv:1804.00749

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- „**Self-consistency**“ of Rauchiger-Renner might be too restrictive requirement on a physical theory.
- „Standard“ (textbook) quantum theory seems not to be appropriate for making predictions involving observers' memories (see V. Baumann, S. Worf, arXiv:1710.07212)

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