

Title: PSI 2017/2018 - Relativistic Quantum Information - Lecture 11

Date: Apr 03, 2018 09:00 AM

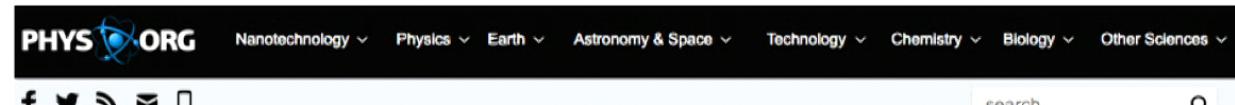
URL: <http://pirsa.org/18040004>

Abstract:

Communication through massless fields

Communication through a massless fields in vacuum

- Information propagates arbitrarily slow even for massless field.
- Recover the message even if the beam is missed.
- Information flow not supported by real quanta (photons) flow.
- Information flow in absence of energy flow.



Home > Physics > Quantum Physics > March 31, 2015

Photon 'afterglow' could transmit information without transmitting energy

March 31, 2015 by Lisa Zyga feature

(Phys.org)—Physicists have theoretically shown that it is possible to transmit information from one location to another without transmitting energy. Instead of using real photons, which always carry energy, the technique uses a small, newly predicted quantum afterglow of virtual photons that do not need to carry energy. Although no energy is transmitted, the receiver must provide the energy needed to detect the incoming signal—similar to the

Antenna states

$$|\Psi_A\rangle = \alpha_A |e_A\rangle + \beta_A |g_A\rangle$$

$$|\Psi_B\rangle = \alpha_B |e_B\rangle + \beta_B |g_B\rangle$$

$$\tilde{F}_A(\vec{x}, \vec{x}') = \int dt \int dz \int dx \int dx' \chi_A(t) \chi_B(z) F_A(\vec{x} - \vec{x}_i) \tilde{F}_B(\vec{x}' - \vec{x}_i) \underbrace{\langle [\phi(t, \vec{x}), \phi(t', \vec{x}')] \rangle}_{\text{State independent}}$$

ONLY NON-ZERO if
- THERE ARE COHERENCES IN THE STATE

Mathematical Methods: Beyond the Strong Huygens Principle

Subtleties in the behaviour of the solutions of certain PDEs:
The strong Huygens principle

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The Green's function of the (massless) wave equation in 3+1D Minkowski space has support only on the light cone. Hence, any disturbances propagate strictly along null geodesics (at the speed of light)

Mathematical Methods: Beyond the Strong Huygens Principle

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The strong Huygens principle

The Green's function of the (massless) wave equation in 3+1D Minkowski space has support only on the light cone. Hence, any disturbances propagate strictly along null geodesics (at the speed of light)

Exploitable when emitters are quantum!

TECHNICAL DETAILS

R. H. Jonsson, E. Martin-Martinez, A. Kempf, Phys. Rev. Lett. 114, 110505 (2015)

A. Blasco, L. J. Garay, M. Martin-Benito, E. Martin-Martinez, Phys. Rev. Lett. 114, 141103 (2015)

A. Blasco, L. J. Garay, M. Martin-Benito, E. Martin-Martinez, Phys. Rev. D 93, 024055 (2016)

P. Simidzija, E. Martin-Martinez, Phys. Rev. D 95, 025002 (2017)

See also:

R. H. Jonsson, J. of Phys. A, 44, 445402 (2016)

STRONG HUYGENS PRINCIPLE

The radiation Green's function (or equivalently the commutator) of a massless field has support only on the light-cone

$$\square G(x, x') = -4\pi\delta_4(x, x') \quad [\Phi(x), \Phi(x')] = \frac{i}{4\pi}G(x, x')$$

→ **Communication** has support only on the **light-cone**

True in 3+1 Flat spacetime

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BEYOND THE STRONG HUYGENS PRINCIPLE

In general: if there is curvature (unless there is conformal invariance)

→ In curved spacetimes, **communication through massless fields** is not confined to the light-cone, but there can be a leakage of information towards the **inside of the light-cone decoupled from energy propagation**.

SPATIALLY FLAT, OPEN FRW SPACETIME 3+1D:

$$ds^2 = a(\eta)^2(-d\eta^2 + dr^2 + r^2 d\Omega^2)$$

η : conformal time
 $a(\eta)$: scale factor
 t : cosmological time,
 $dt = a(\eta)d\eta$
units: $\hbar = c = 1$

This geometry will be generated by:

a **perfect fluid** with a constant density-to-pressure ratio ($p = w\rho$)

→ the **scale factor** evolves as $a \propto \eta^{\alpha+\frac{1}{2}} \propto t^{\frac{2\alpha+1}{2\alpha+3}}$ with $\alpha = \frac{3-3w}{6w+2}$

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A TEST SCALAR FIELD QUANTIZED IN THE BUNCH-DAVIS VACUUM
WILL BE COUPLED TO THE BACKGROUND GEOMETRY.

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TRANSMISSION OF INFORMATION

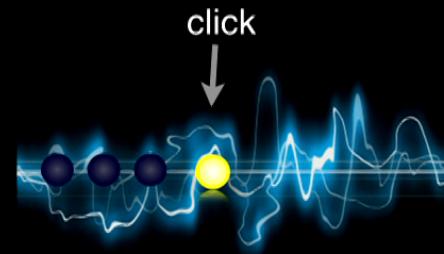
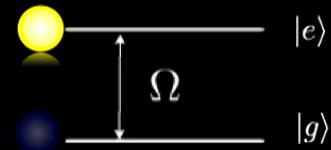
Influence of the presence of A on B → **SIGNALING ESTIMATOR, S**

how much information can be sent? → **CHANNEL CAPACITY, C**

ALICE & BOB's DETECTOR MODEL

Unruh-DeWitt DETECTOR

-Two-level system



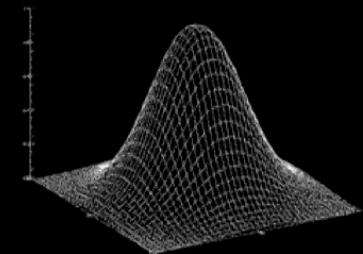
-Energy gap ground-excited states:

$$\Omega$$

-Monopole moment operator:

$$\nu = \{A, B\}$$

-Spatially smeared: $F(\vec{x}, t) = \frac{1}{\sigma^3 \sqrt{\pi^3}} e^{-a(t)^2 \vec{x}^2 / \sigma^2}$



Detectors: $|\psi_\nu\rangle = \alpha_\nu |e_\nu\rangle + \beta_\nu |g_\nu\rangle$

**DETECTOR-FIELD
INTERACTION
HAMILTONIAN**

$$H_{I,\nu} = \lambda_\nu \chi_\nu(t) \mu_\nu(t) \int d^3x \, a(t)^3 F[\mathbf{x} - \mathbf{x}_\nu(t), t] \Phi[\mathbf{x}, \eta(t)]$$

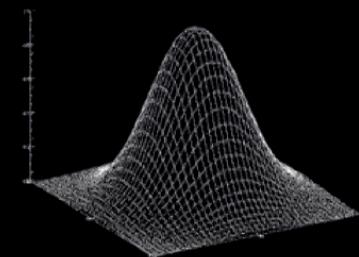
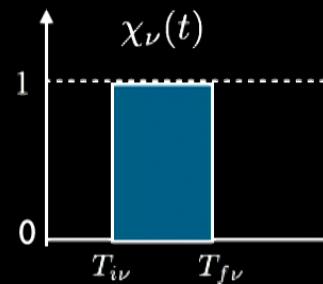
Coupling strength

Monopole moment

Scale factor

Smearing function

Switching function



Total Interaction Hamiltonian:
 $H_I = H_{I,A} + H_{I,B}$

TRANSMISSION OF INFORMATION

Influence of the presence of A on B → **SIGNALING ESTIMATOR, S**

how much information can be sent? → **CHANNEL CAPACITY, C**

TRANSMISSION OF INFORMATION

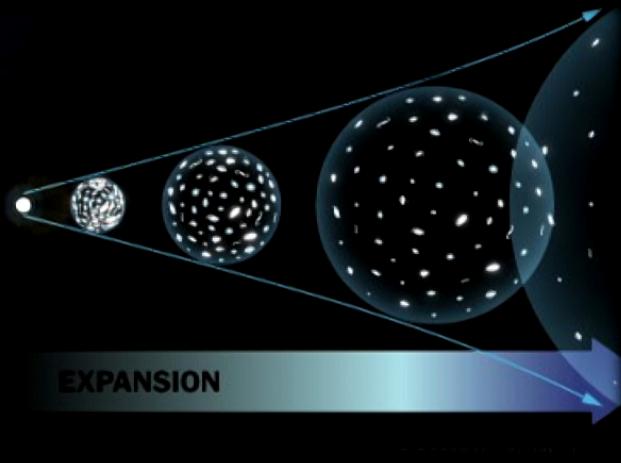
Influence of the presence of A on B

$$\xrightarrow{\hspace{1cm}} \left\{ \begin{array}{l} \text{SIGNALING ESTIMATOR, } \mathbf{S} \\ P_e(t) = |\alpha_B|^2 + P_{vac}(t) + S(t). \end{array} \right.$$

how much information can be sent?

$\xrightarrow{\hspace{1cm}}$ CHANNEL CAPACITY, C

THE **BIG BANG** Setting



BIG BANG CASE, ST. COSMOLOGICAL MODEL: GENERAL RELATIVITY

SCALAR FIELD: COUPLING TO GRAVITY

KLEIN-GORDON EQUATION

$$(\square - m^2 + \xi R)\phi = 0 \quad \square = \frac{1}{\sqrt{|g|}} \partial_\mu \left(\sqrt{|g|} g^{\mu\nu} \partial_\nu \right)$$

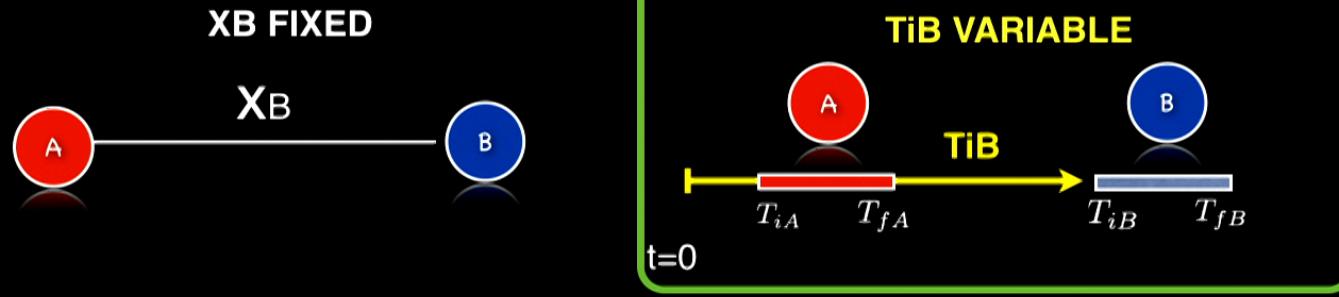
CONFORMAL COUPLING

$$\xi = \frac{1}{6} \quad \text{Yields Conformally Invariant Action}$$

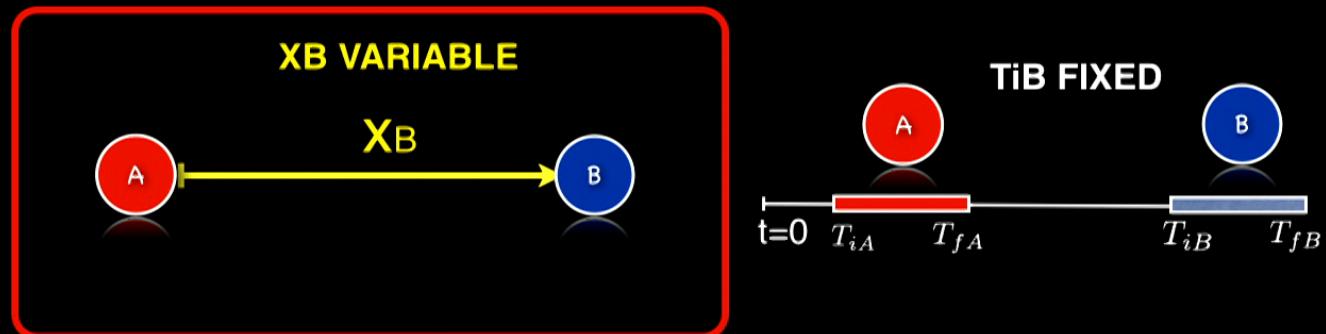
MINIMAL COUPLING

$$\xi = 0 \quad \text{Gives good predictions (Cosmology, etc..)}$$

CASE : Variation of **temporal** separation



CASE: Variation of **spatial** separation



IS INFORMATION
TRANSMITED?

Influence of the presence of A on B


$$\left\{ \begin{array}{l} \text{SIGNALING ESTIMATOR, } \mathbf{S} \\ P_e(t) = |\alpha_B|^2 + P_{vac}(t) + S(t). \end{array} \right.$$

A dashed red box encloses the term $S(t)$, with a red arrow pointing upwards from the text 'Influence of the presence of A on B' towards this term.

**SIGNALING
ESTIMATOR, S**

$$S = \lambda_A \lambda_B S_2 + \mathcal{O}(\lambda_\nu^4)$$

$$\boxed{S_2 = 4 \int a(t)^3 d^3 \mathbf{x} dt \int a(t')^3 d^3 \mathbf{x}' dt' \chi_A(t) \chi_B(t') \text{Re}(\alpha_A^* \beta_A) F(\mathbf{x} - \mathbf{x}_A, t) \\ \times F(\mathbf{x}' - \mathbf{x}_B, t) \text{Re}(\alpha_B^* \beta_B [\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')])}$$

**SIGNALING
ESTIMATOR, S**

CONFORMAL COUPLING

$$S = \lambda_A \lambda_B S_2 + \mathcal{O}(\lambda_\nu^4)$$

$$\begin{aligned} S_2 = 4 \int a(t)^3 d^3 \mathbf{x} dt \int a(t')^3 d^3 \mathbf{x}' dt' & \chi_A(t) \chi_B(t') \operatorname{Re}(\alpha_A^* \beta_A) F(\mathbf{x} - \mathbf{x}_A, t) \\ & \times F(\mathbf{x}' - \mathbf{x}_B, t) \operatorname{Re}(\alpha_B^* \beta_B [\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')]) \end{aligned}$$

$$[\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')] = \frac{i}{4\pi} \left[\frac{\delta(\Delta\eta + |\mathbf{x} - \mathbf{x}'|) - \delta(\Delta\eta - |\mathbf{x} - \mathbf{x}'|)}{a(t)a(t')|\mathbf{x} - \mathbf{x}'|} \right]$$

$$\Delta\eta = \eta(t) - \eta(t')$$

$$|\psi_{0,\nu}\rangle = \alpha_\nu |e_\nu\rangle + \beta_\nu |g_\nu\rangle$$

CHANNEL CAPACITY

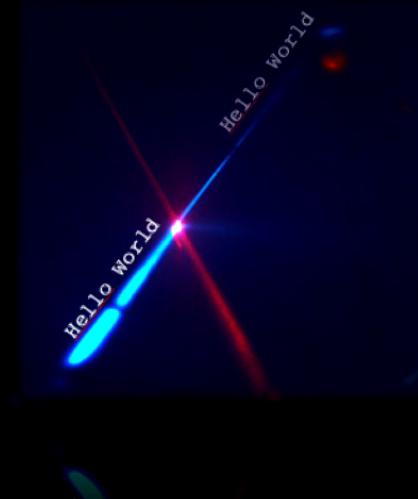
To obtain a lower bound to the channel capacity, we use a simple **COMMUNICATION PROTOCOL**:

- **Alice** encodes “**1**” by coupling her detector A to the field, and “**0**” by not coupling it.
- Later **Bob** switches on B and measures its energy. If B is excited, Bob interprets a “**1**”, and a “**0**” otherwise.

$$C \simeq \lambda_A^2 \lambda_B^2 \frac{2}{\ln 2} \left(\frac{S_2}{4|\alpha_B||\beta_B|} \right)^2 + \mathcal{O}(\lambda_\nu^6)$$

(noisy asymmetric binary channel)

Robert H. Jonsson, Eduardo Martín-Martínez, and Achim Kempf.
Quantum Collect Calling.
Phys. Rev. Lett. 114, 110505 (2015).



CONFORMAL COUPLING

$$[\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')] = \frac{i}{4\pi} \left[\frac{\delta(\Delta\eta + |\mathbf{x} - \mathbf{x}'|) - \delta(\Delta\eta - |\mathbf{x} - \mathbf{x}'|)}{a(t)a(t')|\mathbf{x} - \mathbf{x}'|} \right]$$

support on the
light cone

Decay with Spatial
separation

SIGNALING ESTIMATOR, S

MINIMAL COUPLING

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$$[\phi(\mathbf{x}_A, t_A), \phi(\mathbf{x}_B, t_B)] = i \frac{\theta(\eta(t_B) - \eta(t_A)) - \theta(\eta(t_A) - \eta(t_B))}{(2\pi)^3 |\mathbf{x} - \mathbf{x}'| a(\eta(t_A)) a(\eta(t_B))} \int_0^\infty dk k \sin(k|\mathbf{x} - \mathbf{x}'|) \hat{g}(\eta(t_A), \eta(t_B), k)$$

$$\Delta\eta = \eta(t) - \eta(t')$$

$$|\psi_{0,\nu}\rangle = \alpha_\nu |e_\nu\rangle + \beta_\nu |g_\nu\rangle$$

MINIMAL COUPLING

SIGNALING ESTIMATOR, S

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$$\hat{g}(\eta, \eta', k) = \frac{8\pi}{k} \sqrt{\left| \frac{\eta}{\eta'} \right|} \frac{\operatorname{sgn}(\eta') [J_{\alpha-1/2}(k|\eta|) Y_{\alpha-1/2}(k|\eta'|) - Y_{\alpha-1/2}(k|\eta|) J_{\alpha-1/2}(k|\eta'|)]}{Y_{\alpha-1/2}(k|\eta'|) [J_{\alpha-3/2}(k|\eta'|) - J_{\alpha+1/2}(k|\eta'|)] - J_{\alpha-1/2}(k|\eta'|) [Y_{\alpha-3/2}(k|\eta'|) - Y_{\alpha+1/2}(k|\eta|)]}$$

J_α, Y_α BESSEL FUNCTIONS

SIGNALING ESTIMATOR, S

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J_α Y_α BESSEL FUNCTIONS

MATTER DOMINATED UNIVERSE $\longrightarrow \alpha = 2 \longrightarrow a \propto \eta^2 \propto t^{2/3}$

$$J_{2-1/2}(k|\eta|) = \sqrt{2/\pi} \frac{1}{\sqrt{k|\eta|}} \left[-\cos(k\eta) + \frac{\sin(k\eta)}{k\eta} \right]$$

$$Y_{2-1/2}(k|\eta|) = \sqrt{2/\pi} \frac{\operatorname{sgn}(\eta)}{\sqrt{k|\eta|}} \left[-\sin(k\eta) + \frac{\cos(k\eta)}{k\eta} \right]$$

MINIMAL COUPLING

**SIGNALING
ESTIMATOR, S**

**MATTER DOMINATED
UNIVERSE**

$$\longrightarrow \quad \alpha = 2 \quad \longrightarrow \quad a \propto \eta^2 \propto t^{2/3}$$

$$[\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')] = \frac{i}{4\pi} \left[\frac{\delta(\Delta\eta + |\mathbf{x} - \mathbf{x}'|) - \delta(\Delta\eta - |\mathbf{x} - \mathbf{x}'|)}{a(t)a(t')|\mathbf{x} - \mathbf{x}'|} + \frac{\theta(-\Delta\eta - |\mathbf{x} - \mathbf{x}'|) - \theta(\Delta\eta - |\mathbf{x} - \mathbf{x}'|)}{a(t)a(t')\eta(t)\eta(t')} \right]$$

CONFORMAL COUPLING

$$[\phi(\mathbf{x}, t), \phi(\mathbf{x}', t')] = \frac{i}{4\pi} \left[\frac{\delta(\Delta\eta + |\mathbf{x} - \mathbf{x}'|) - \delta(\Delta\eta - |\mathbf{x} - \mathbf{x}'|)}{a(t)a(t')|\mathbf{x} - \mathbf{x}'|} \right]$$

support on the light cone

SIGNALING ESTIMATOR, S

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VIOLATION OF
STRONG HUYGENS
PRINCIPLE !!!!

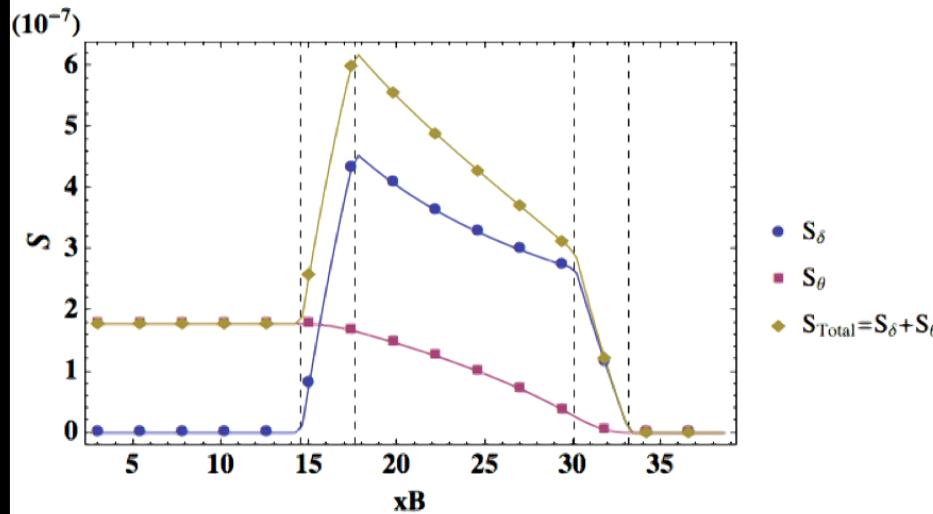
Decay with Spatial separation

Does NOT decay with Spatial separation

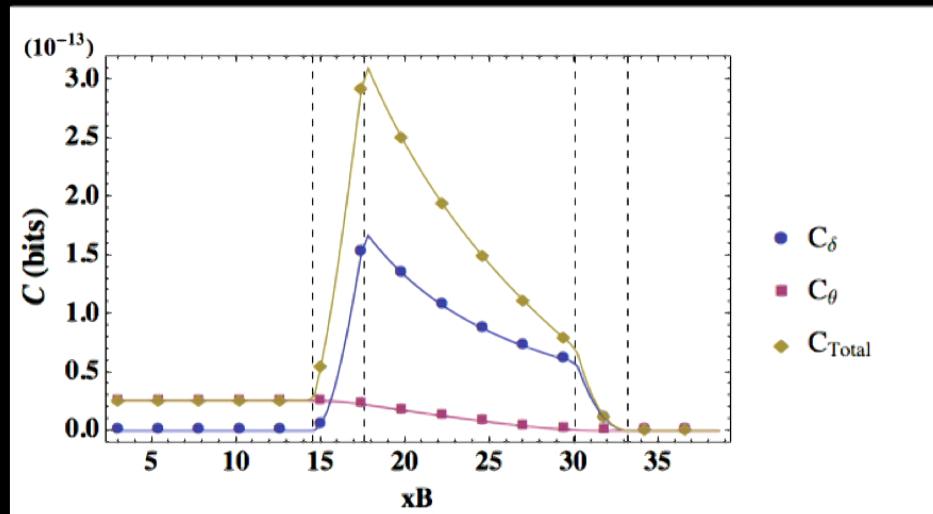
Timelike-leakage

Case:
Variation of
spatial
separation

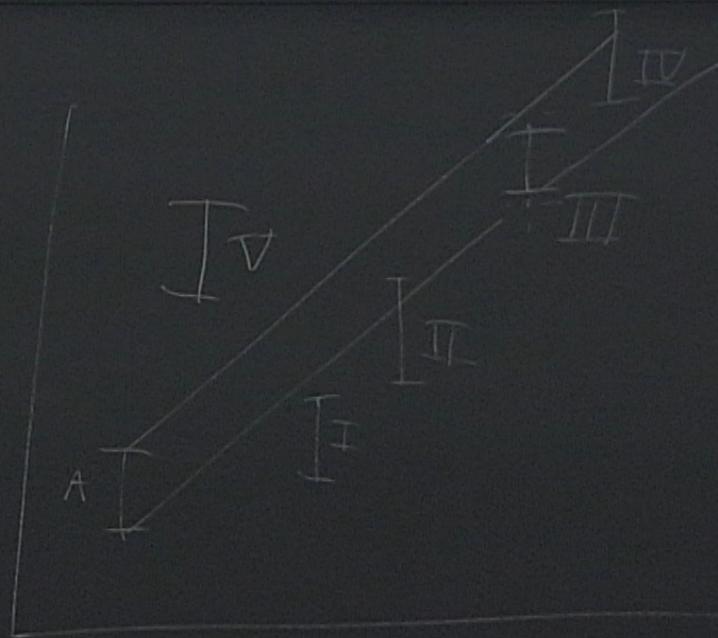
MINIMAL COUPLING



SIGNALING ESTIMATOR,S



CHANNEL CAPACITY

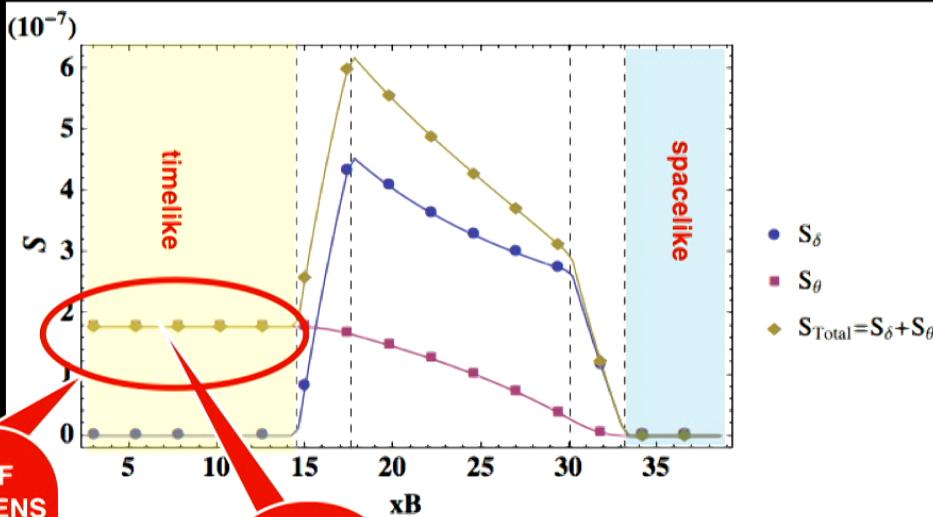


Case:
Variation of
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MINIMAL COUPLING

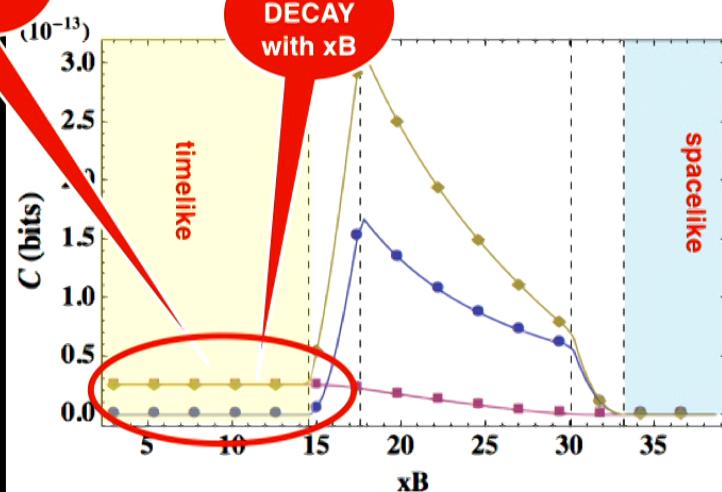
**VIOLATION OF
STRONG HUYGENS
PRINCIPLE !!!!**

**NO
DECAY
with xB**



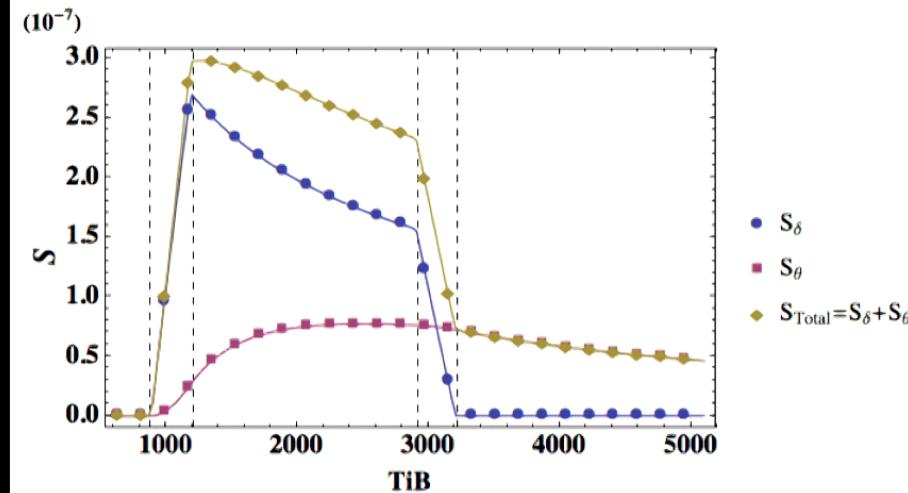
**SIGNALING
ESTIMATORS**

**CHANNEL
CAPACITY**

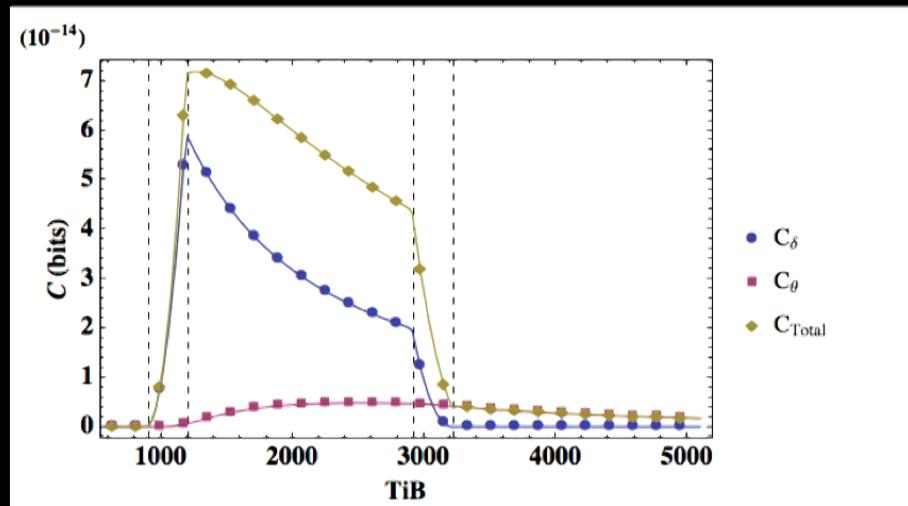


Case:
Variation of
temporal
separation

MINIMAL COUPLING



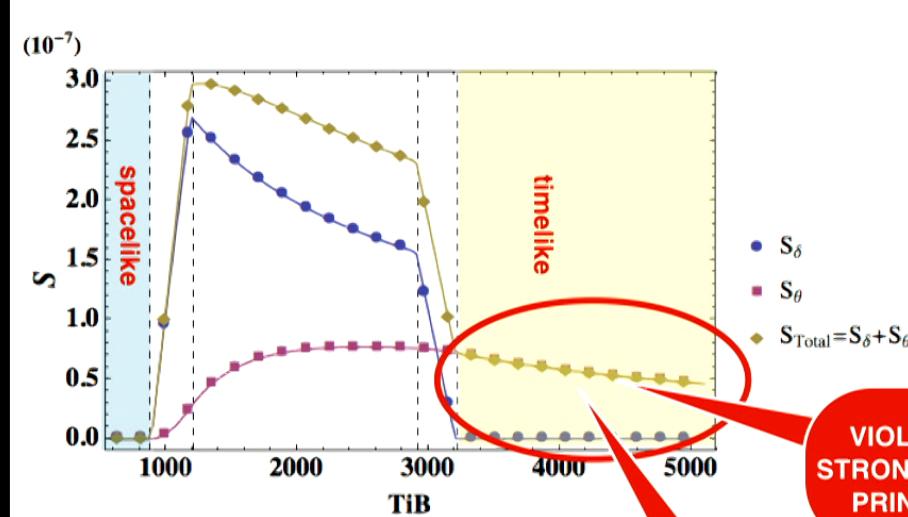
SIGNALING ESTIMATOR,S



CHANNEL CAPACITY

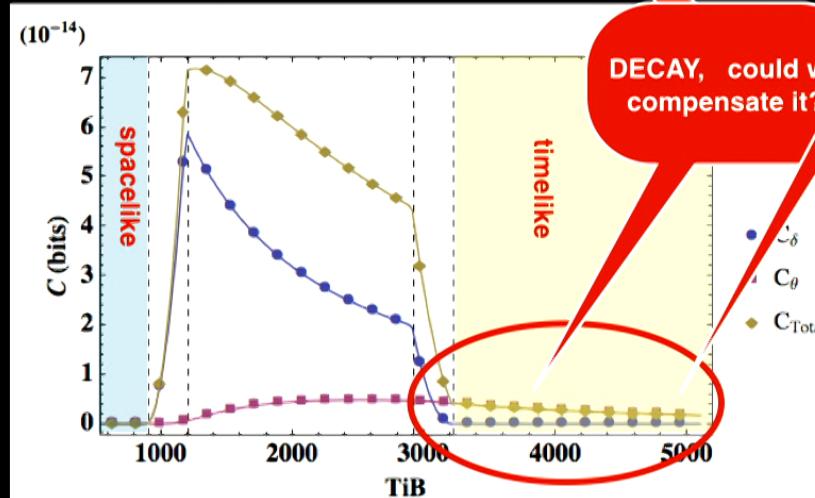
Case:
Variation of
temporal
separation

MINIMAL COUPLING



**SIGNALING
ESTIMATORS**

VIOLATION OF
STRONG HUYGENS
PRINCIPLE !!!!

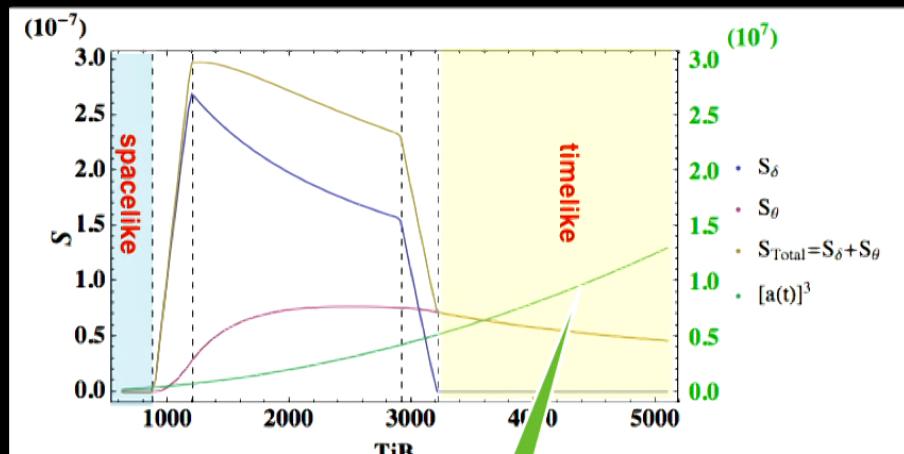


**CHANNEL
CAPACITY**

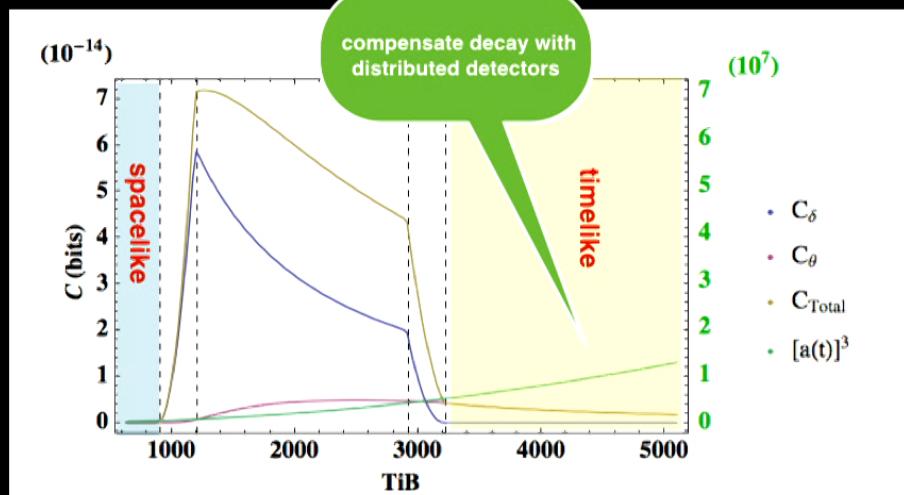
DECAY, could we
compensate it?

Case:
Variation of
temporal
separation

MINIMAL COUPLING



SIGNALING ESTIMATORS



CHANNEL CAPACITY

Exponential Expansion (deSitter): No decay in time!

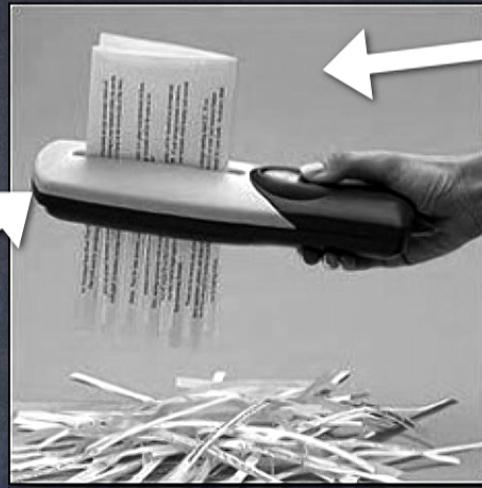
P. Simidzija, E. Martin-Martinez, Phys. Rev. D 95, 025002 (2017)

AND...WHAT HAPPENS in the
case of **QUANTUM BOUNCE**
Setting ?

How much information survives a Cosmological cataclysm!!!!



Cosmological
cataclysm!!!!



information