

Title: Microscopic structure of quantum black holes

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URL: <http://pirsa.org/18020092>

Abstract: <p>If a black hole horizon has its microscopic structure as is conjectured by the candidates of quantum gravity, the dispersion relation of gravitational waves (GWs) near the horizon may be drastically modified since its wavelength can be comparable to the size of the microscopic structure because of its infinite gravitational blue-shift near the horizon.&nbsp; We investigate ringdown-GWs from a perturbed black hole with such a modified dispersion relation and found that the change of modified dispersion relation near the horizon would lead to the partial reflection of infalling GWs at the horizon and echo-signals may appear in the late-time of ringdown-GWs. This implies that the echoes can be a supporting evidence of the existence of microscopic degrees of freedom on black hole horizons.</p>

Cosmology and Gravitation seminar @ Perimeter Institute, February 6th, 2018

# Microscopic structure of quantum black holes

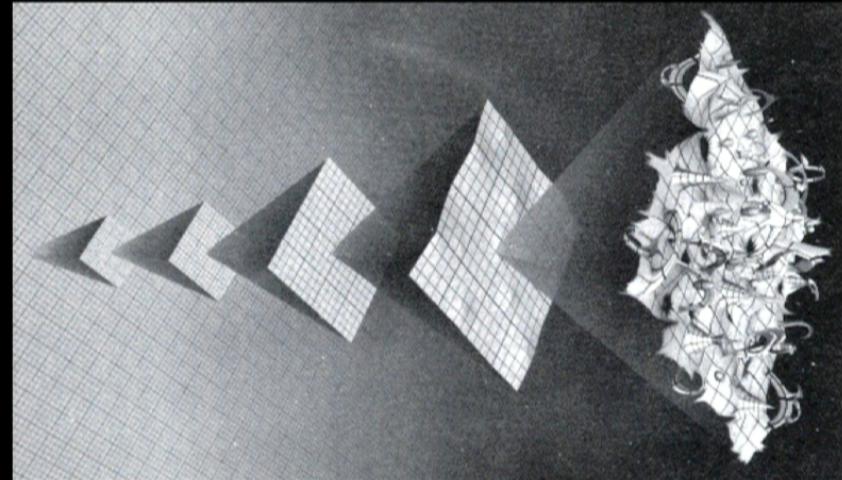
Naritaka Oshita

University of Tokyo, Research Center for the Early Universe



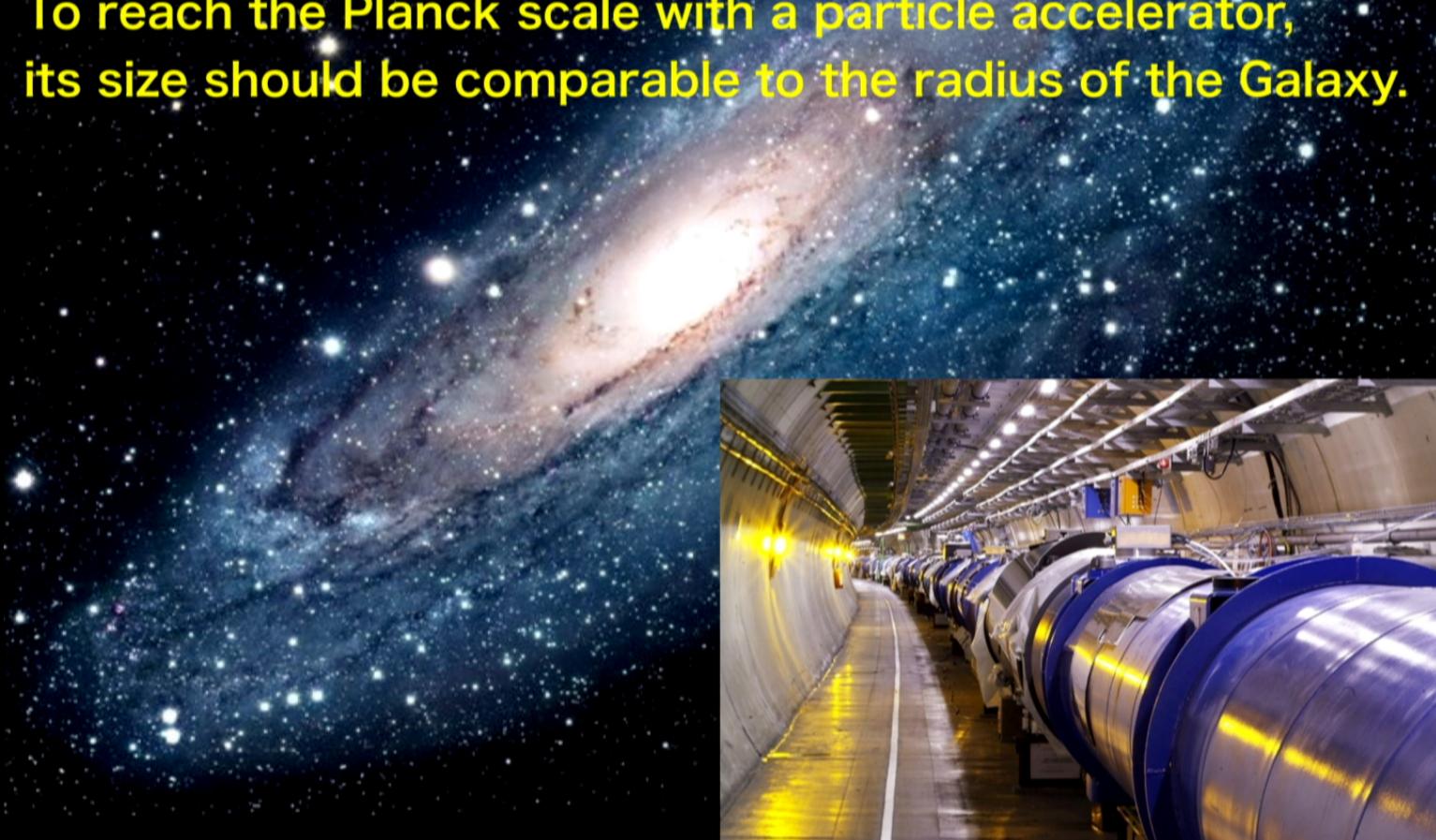
artwork by Kaća Bradonjić

- There seems to be an operational limitation in measuring lengths smaller than the Planck length  $\ell_{\text{Pl}}$ .
- superstring theories and the spin network formalism might have ingredients to describe the microscopic structure of spacetime.

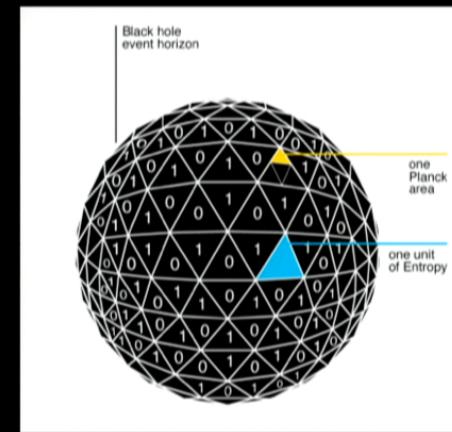
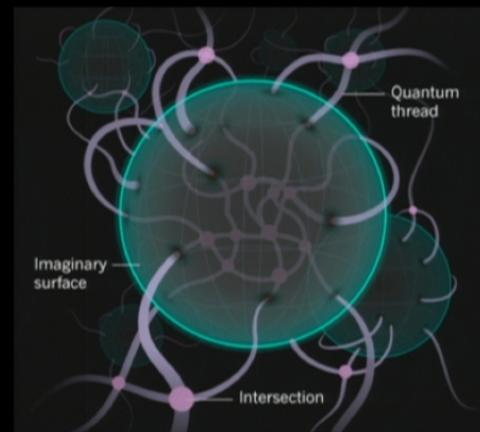
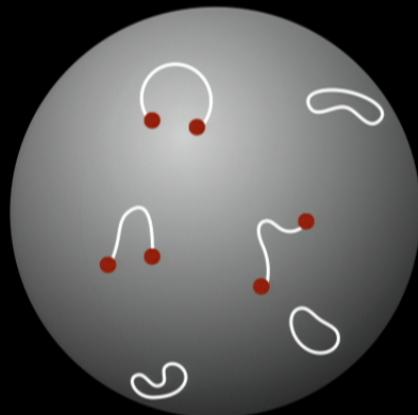


# How can we access the Planck scale?

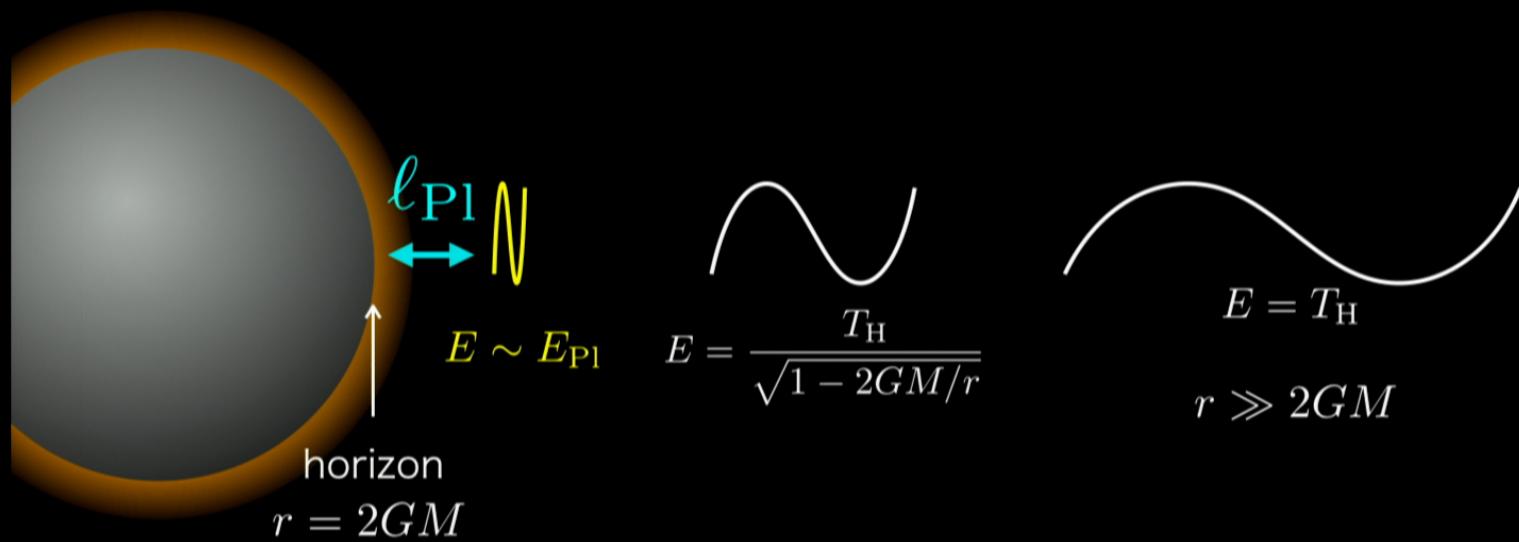
To reach the Planck scale with a particle accelerator,  
its size should be comparable to the radius of the Galaxy.



- Bekenstein entropy (generalized second law of thermodynamics)  
→ black hole may be complicated
- Hawking radiation (black holes may possess their temperatures)  
→ black hole may be thermodynamical
- superstring theory gives the Bekenstein entropy and Hawking temperature

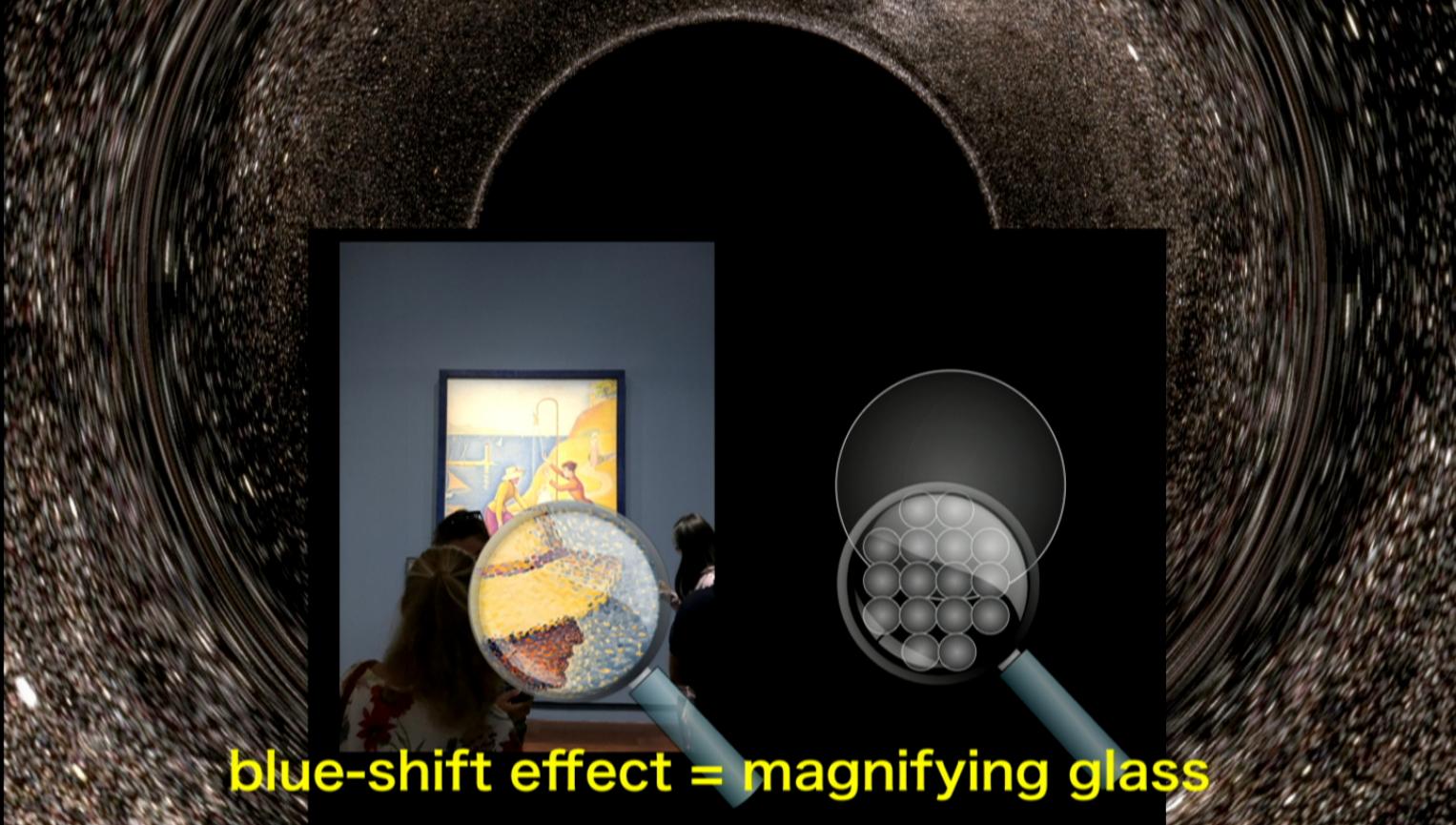


# Trans-Planckian problem on blackholes

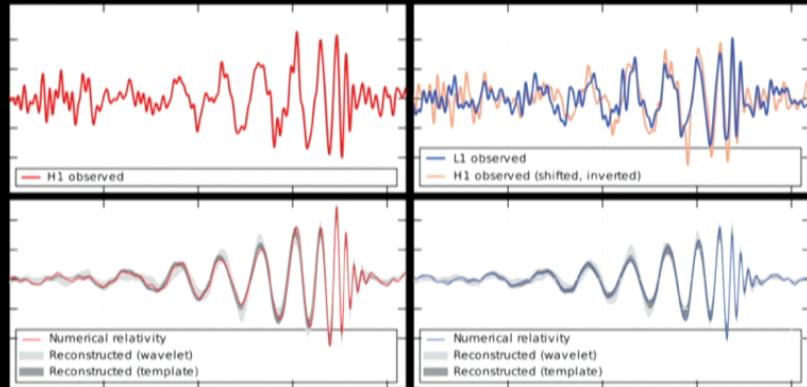


physics beyond Planck scale!

The gravitational blue-shift effect  
may allow us to reach the Planck scale !



# Gravitational waves from a binary black hole



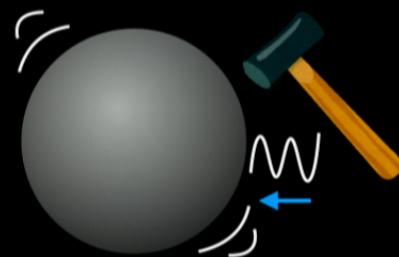
GW150914  
(the first detection of GWs by LIGO)

- consist of specific modes (Quasi-Normal Modes)
- QNMs determined only by its mass and angular momentum

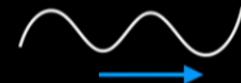


**ringdown is useful to test a BH**

# Quasi-Normal Modes



$$\phi(t, r^*)$$



Regge-Wheeler equation

$$\left[ \frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial r^{*2}} + V(r) \right] \phi(t, r^*) = 0 \longrightarrow \left[ \frac{\partial^2}{\partial r^{*2}} + (\omega^2 - V(r)) \right] \phi_\omega(r^*) = 0$$

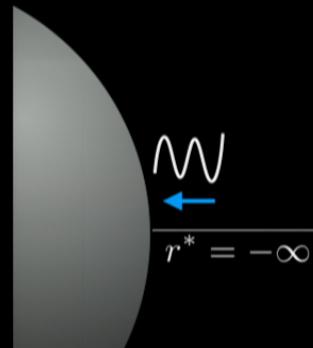
$$r^* = r + 2GM \ln \left( \frac{r}{2GM} - 1 \right)$$

$$V(r) = \left( 1 - \frac{2GM}{r} \right) \left( \frac{\ell(\ell+1)}{r^2} - \frac{6GM}{r^3} \right)$$

$$\boxed{\phi(t, r^*) = \int d\omega \phi_\omega(r^*) e^{-i\omega t}}$$

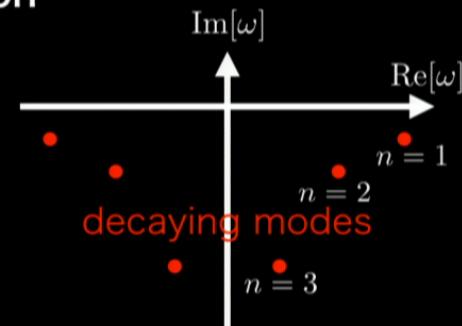
$$\propto e^{\text{Im}[\omega]t}$$

looking for  $\omega$  satisfying this boundary condition



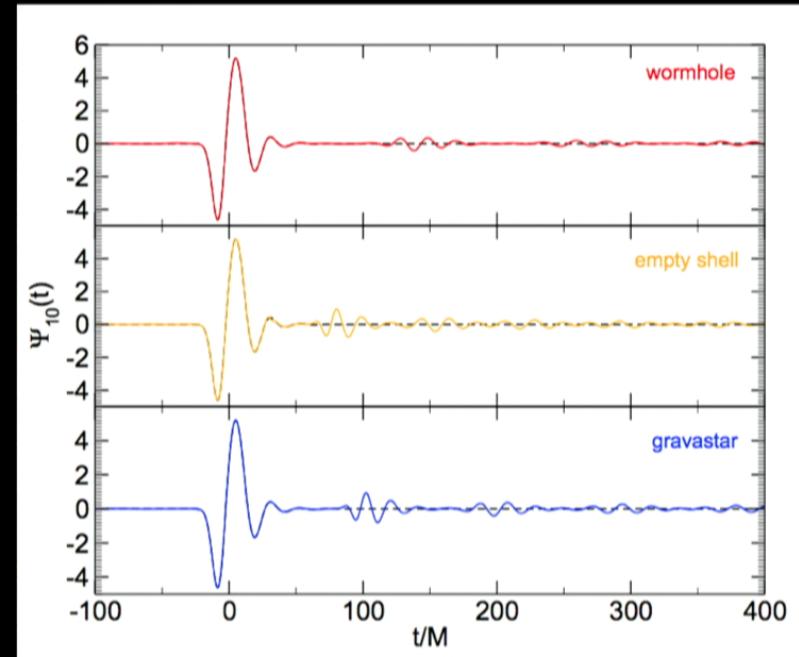
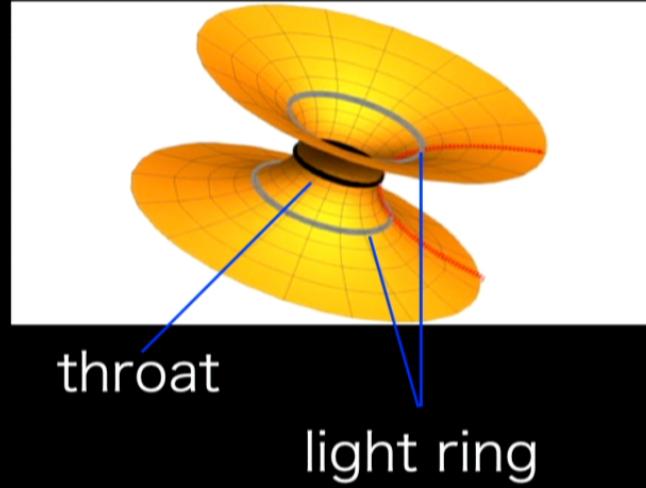
$$V(r^*)$$

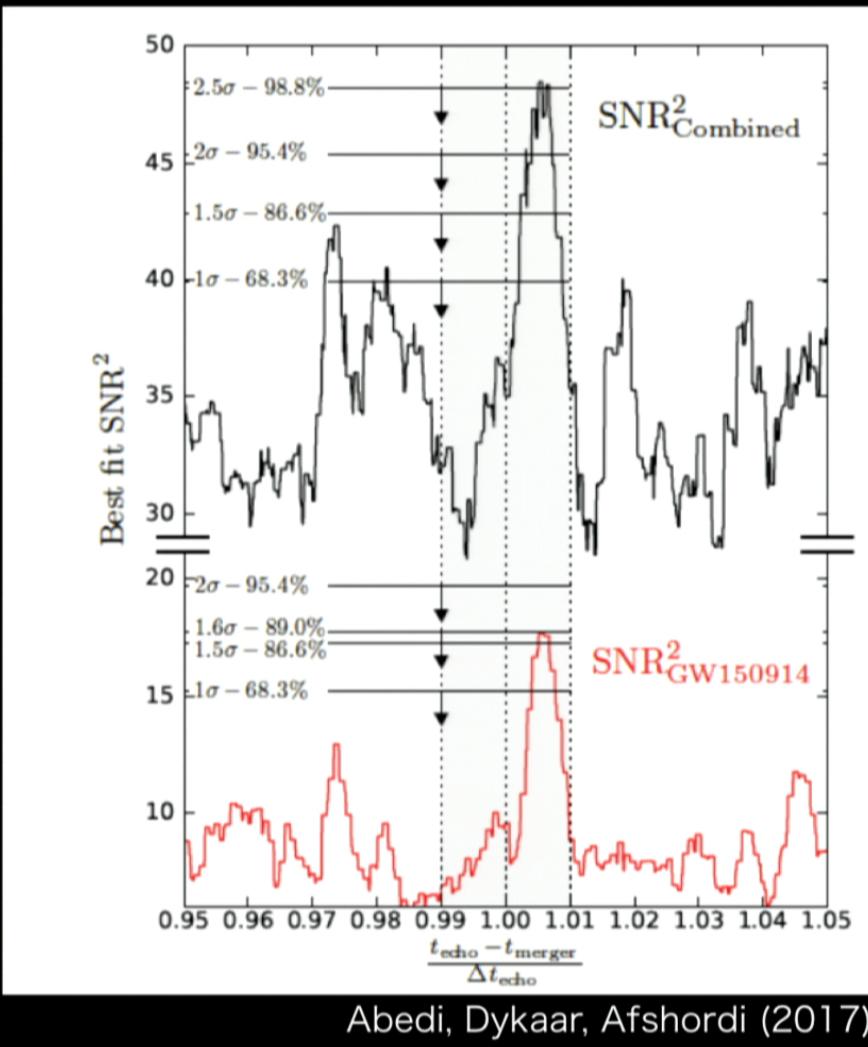
$$r^* = +\infty$$



# Blackholes? Exotic Compact Objects?

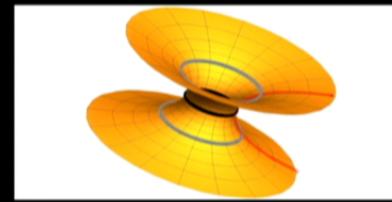
Cardoso et al. (2016)





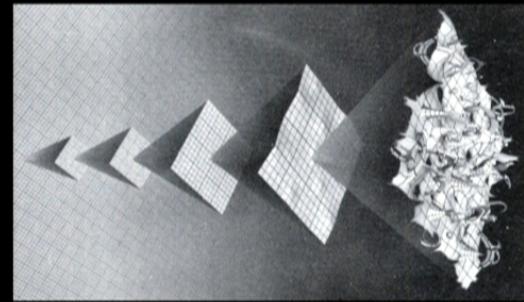
echo!

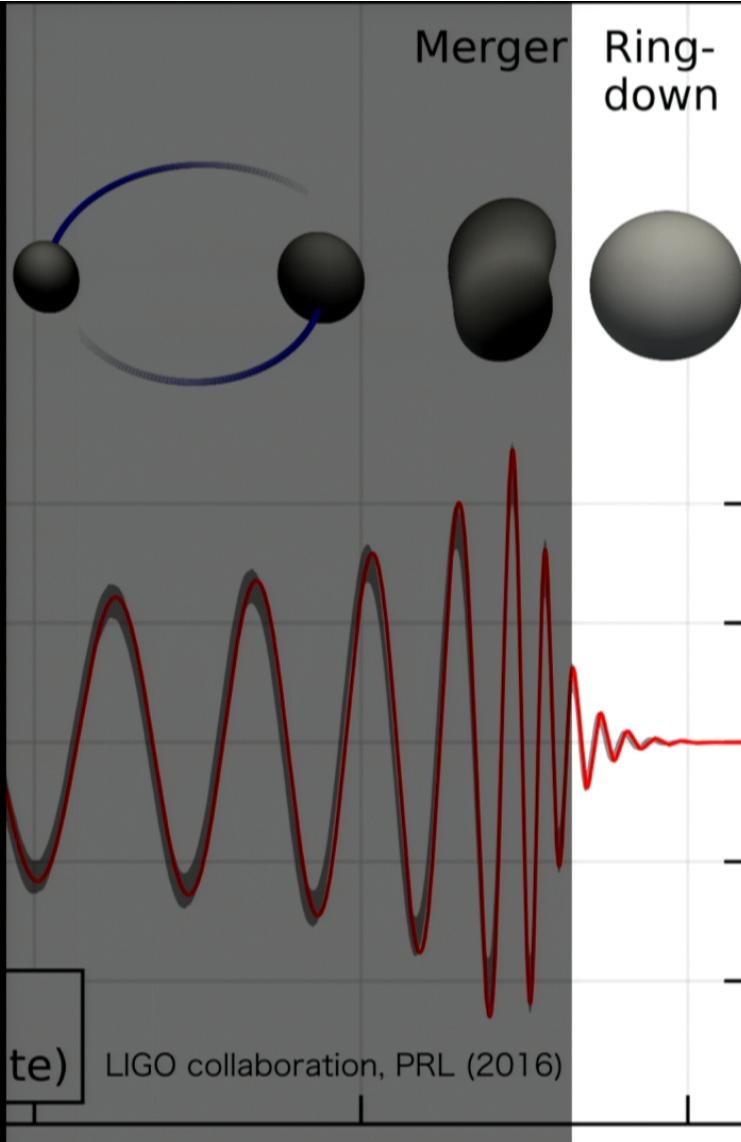
ECOs?



or

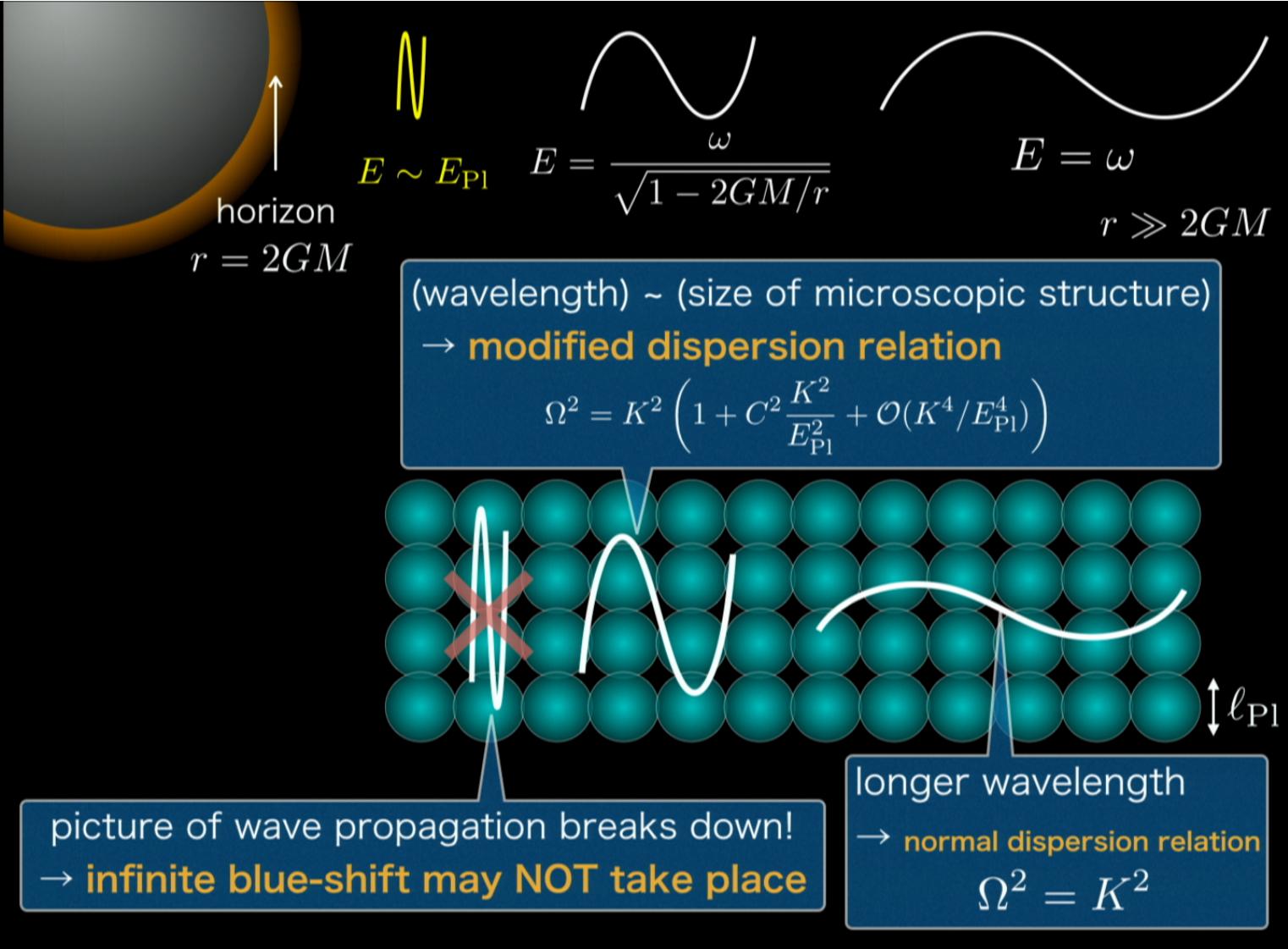
microscopic structure  
of spacetime ?





Is it possible to test  
the candidates of  
**quantum gravity**  
with **ringdown** ??

(e.g., loop quantum gravity  
Horava-Lifshitz gravity,  
causal dynamical triangulation)

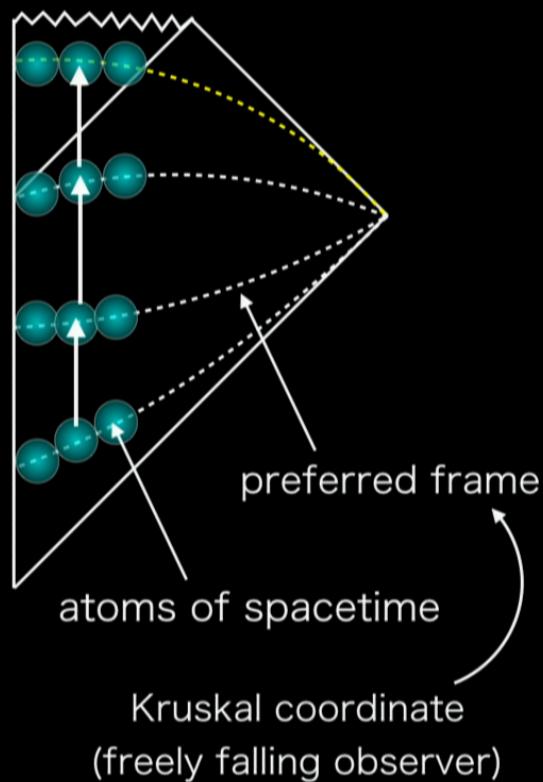


space has a special length (Planck length)

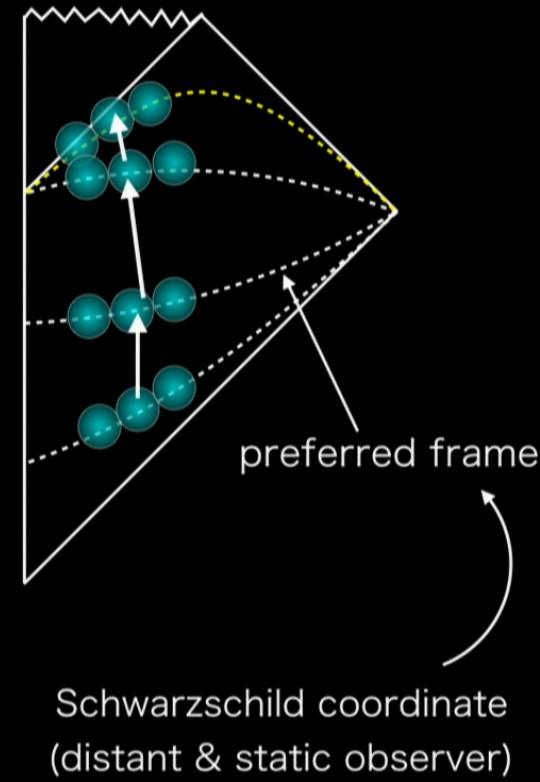


Lorentz symmetry is broken → preferred frame may exist

### infalling atoms



### atoms stuck at horizon

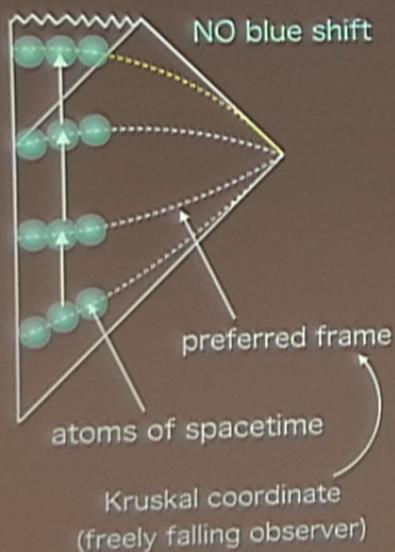


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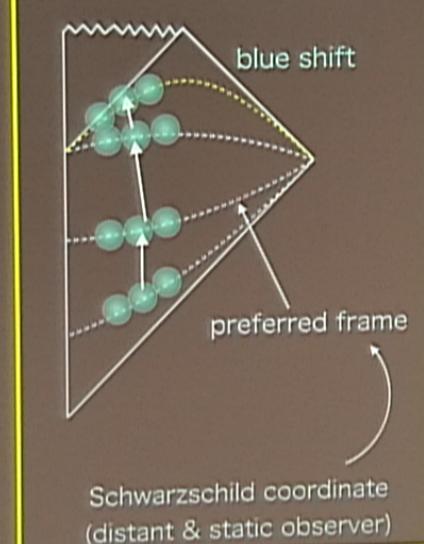


Lorentz symmetry is broken → preferred frame may exist

infalling atoms



atoms stuck at horizon



# model

dispersion relation

$$\Omega^2 = K^2 \left( 1 + C^2 \frac{K^2}{E_{\text{Pl}}^2} \right)$$

e.g.

$C^2 > 0$  Horava-Lifshitz gravity

$C^2 = -\frac{4\pi}{3}$  Padmanabhan (1998)

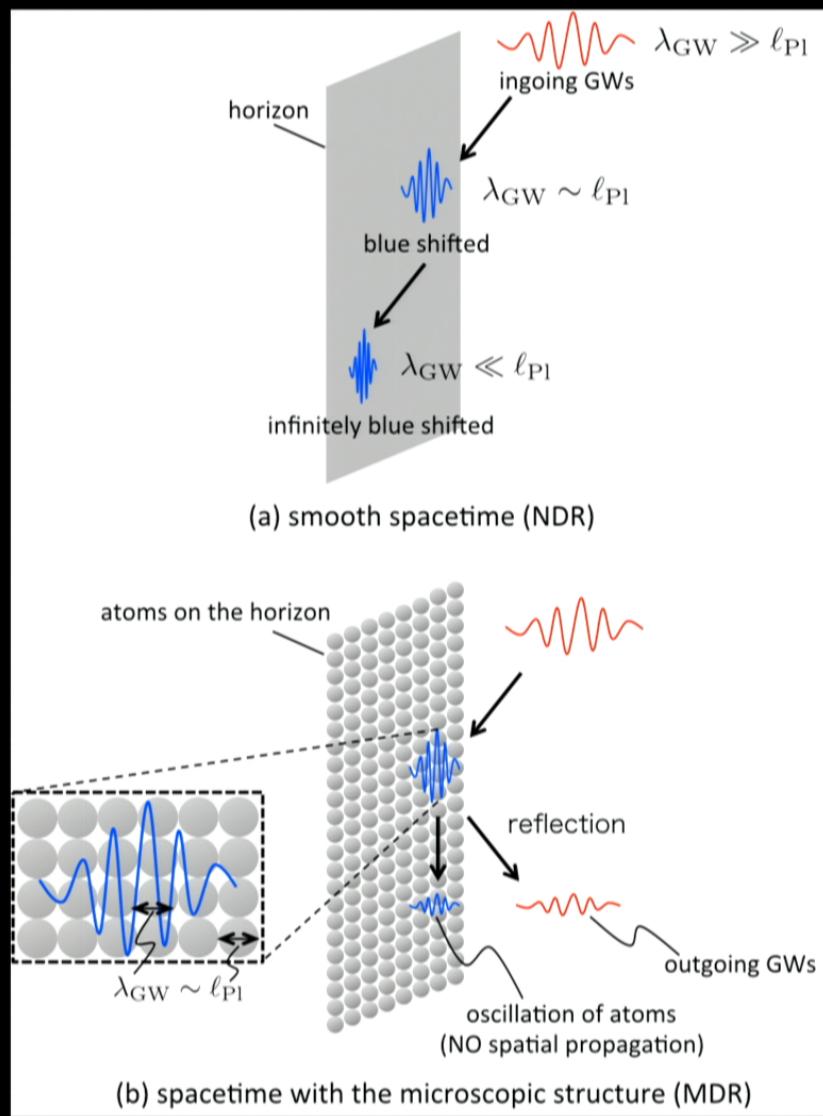
$$ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\Omega^2 \quad f(r) \equiv 1 - \frac{2GM}{r}$$

e.g. Horava-Lifshitz gravity

$$f(r) = 1 - \alpha r^{(2\lambda \pm \sqrt{6\lambda - 2})/(\lambda - 1)} \quad 1/3 < \lambda < 1$$

reduce to the Schwarzschild spacetime with  $\lambda \rightarrow 1/3$

$\alpha$ : arbitrary constant



$$\Omega^2 = K^2 \left( 1 + C^2 \frac{K^2}{M_{\text{Pl}}^2} \right)$$

size of microstructure  
 $|C|/M_{\text{Pl}} = |C|\ell_{\text{Pl}}$

$$-K^2 \rightarrow \nabla = g^{ij} \partial_i \partial_j$$

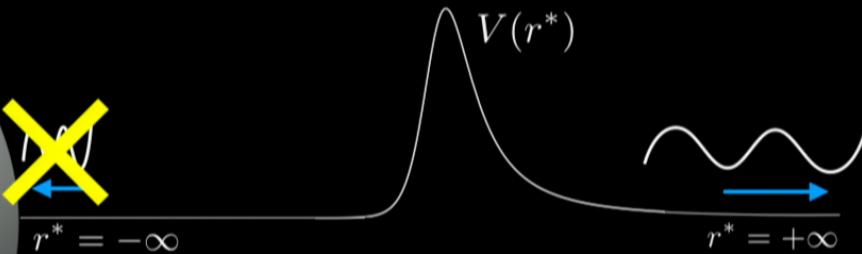
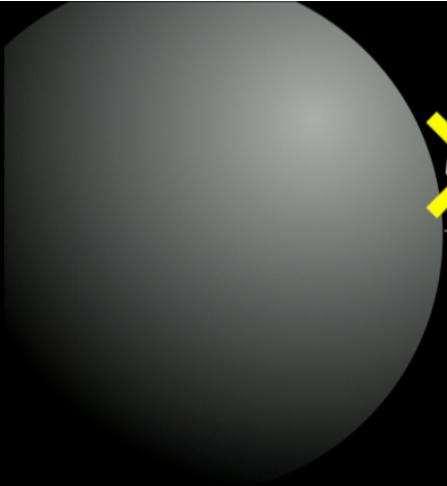
$$1 - \frac{C^2 M_{\text{Pl}}^{-2}}{1 - r_g/r} \partial_{r^*}^2 - C^2 \left( \frac{\ell_{\text{Pl}}}{r} \right)^2 \left( \partial_\theta^2 + \frac{1}{\sin^2 \theta} \partial_\varphi^2 \right) \ll 1$$

$$\ell_{\text{Pl}} \ll 2GM < r$$

$$\Omega^2 = g^{00} \omega^2 = \frac{\omega^2}{1 - 2GM/r}$$

modified-Regge-Wheeler Eq.

$$\left[ -\frac{C^2 M_{\text{Pl}}^{-2}}{1 - r_g/r} \partial_{r^*}^4 + \partial_{r^*}^2 + (\omega^2 - V(r)) \right] \tilde{\psi}(\omega, r^*) = 0$$



$$\left[ -\frac{C^2 M_{\text{Pl}}^{-2}}{1 - r_g/r} \partial_{r^*}^4 + \partial_{r^*}^2 + (\omega^2 - V(r)) \right] \tilde{\psi}(\omega, r^*) = 0$$

impossible to impose ingoing modes at horizon

## What is the new guiding principle ?

(boundary condition)

minimum size of space

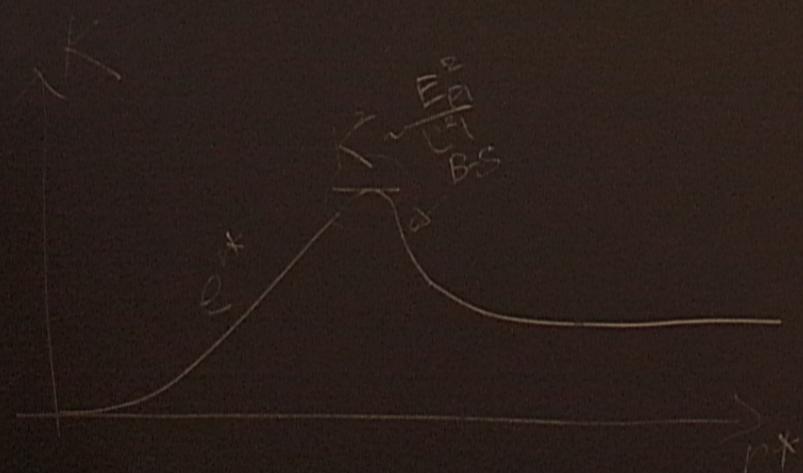
upper bound for wavenumber

$$\delta L \gtrsim |C| \ell_{\text{Pl}}$$



$$K \lesssim E_{\text{Pl}}/|C|$$





# Solving the modified RW equation

$$\left[ -\frac{C^2}{M_{\text{Pl}}^2} \frac{1}{1 - r_g/r} \partial_{r^*}^4 + \partial_{r^*}^2 + \omega^2 - V(r) \right] \tilde{\psi}(\omega, r^*) = 0 \quad \tilde{\psi}(\omega, r^*) = \sum_{n=0}^3 C_n \phi_n$$

  $r^* \rightarrow -\infty$

$$\left[ -\frac{C^2 e^{-r^*/r_g}}{M_{\text{Pl}}^2} \partial_{r^*}^4 + \partial_{r^*}^2 + \omega^2 - V(r) \right] \tilde{\psi}(\omega, r^*) = 0$$

solution

$$\phi_n(\omega, r^*) = \left( \frac{r^*}{r_g} \right)^n + \epsilon(r^*) f_n(r^*, r_g \omega) + \mathcal{O}(\epsilon^2) \quad n = 0, 1, 2, 3$$

**power law**  $\epsilon(r^*) = e^{r^*/r_g} \frac{r_g^2}{e C^2 \ell_{\text{Pl}}^2} \quad |\epsilon(r^*)| < 1$

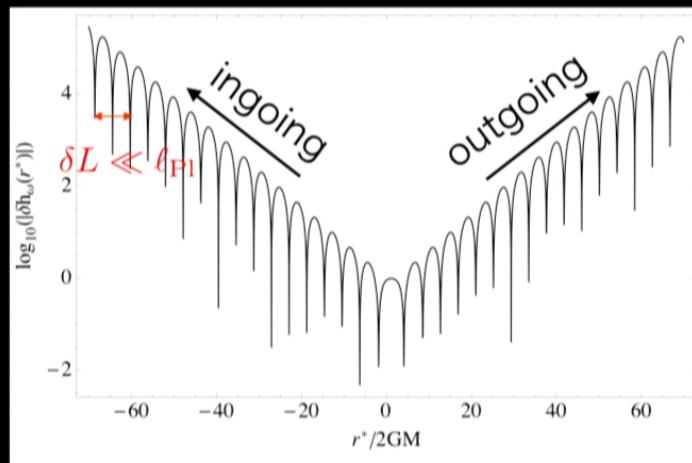
$f_n$  : quartic function of  $r^*$

substitute boundary condition  $K \lesssim E_{\text{Pl}}/|C|$

$$K \sim \phi_n^{-1} \partial_L \phi_n \simeq e^{-r^*/2r_g} \phi_n^{-1} \partial_{r^*} \phi_n \simeq$$

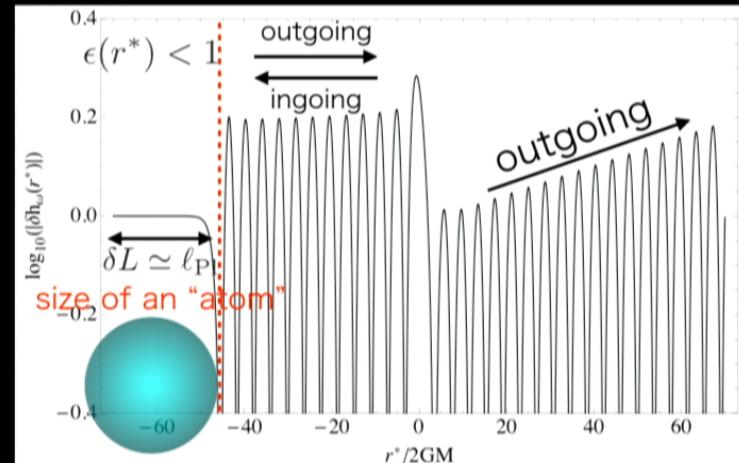
$$\phi_n(\omega, r^*) = \left(\frac{r^*}{r_g}\right)^n + \epsilon(r^*) f_n(r^*, r_g \omega) + \mathcal{O}(\epsilon^2)$$

$$\epsilon(r^*) = e^{r^*/r_g} \frac{r_g^2}{e C^2 \ell_{\text{Pl}}^2} \quad |\epsilon(r^*)| < 1$$

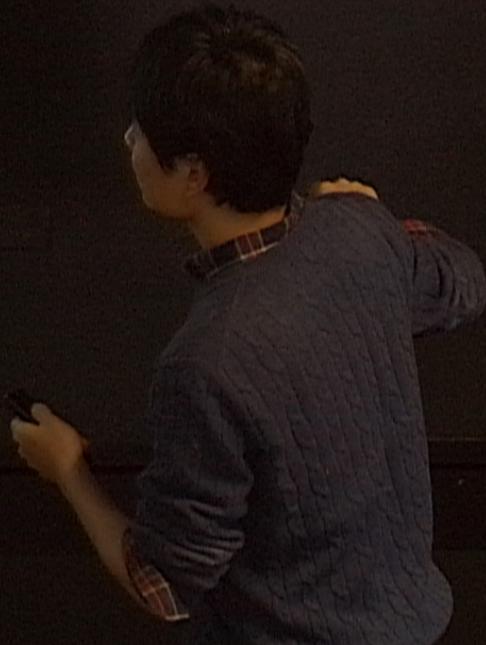
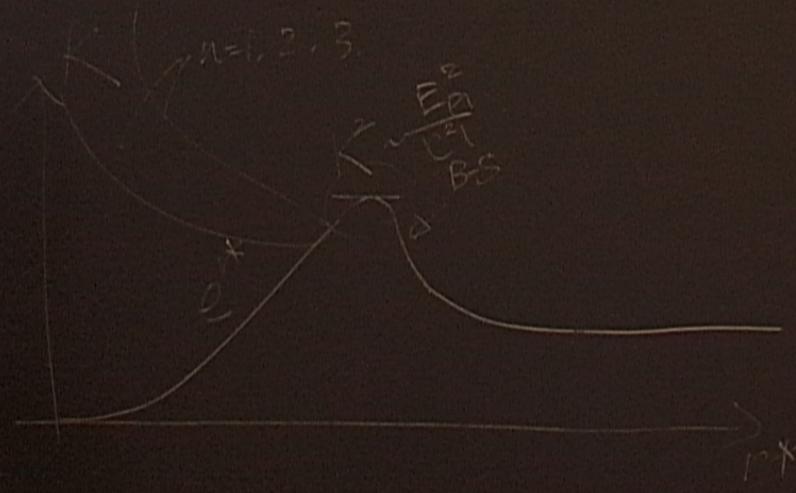


$$\lim_{r^* \rightarrow -\infty} \tilde{\psi} = e^{-i\omega r^*}, \quad \lim_{r^* \rightarrow \infty} \tilde{\psi} = e^{+i\omega r^*}$$

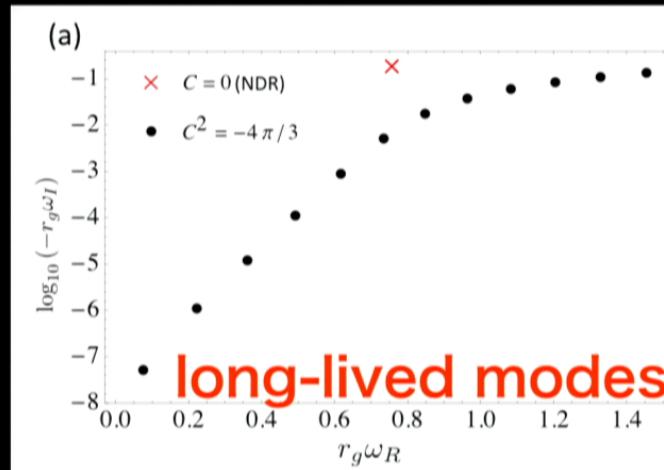
$$\begin{cases} e^{-r^*/2r_g}/r^* & n = 1, 2, 3 \\ \text{divergence} & \\ e^{+r^*/2r_g}/r_g & n = 0 \\ \text{suppressed} & \end{cases}$$



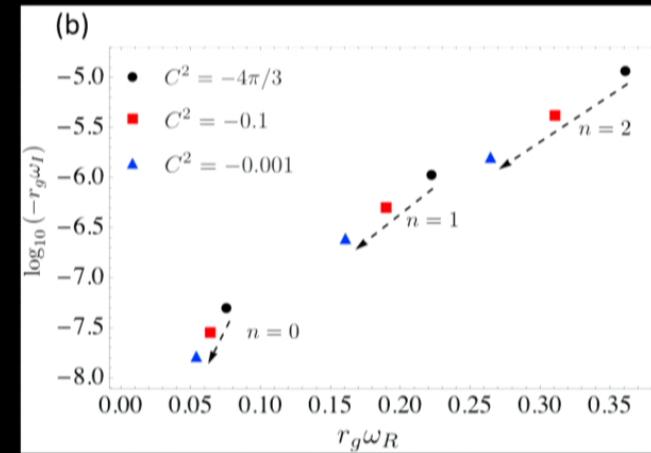
$$\lim_{r^* \rightarrow -\infty} \tilde{\psi} = \text{const.}, \quad \lim_{r^* \rightarrow \infty} \tilde{\psi} = e^{+i\omega r^*}$$

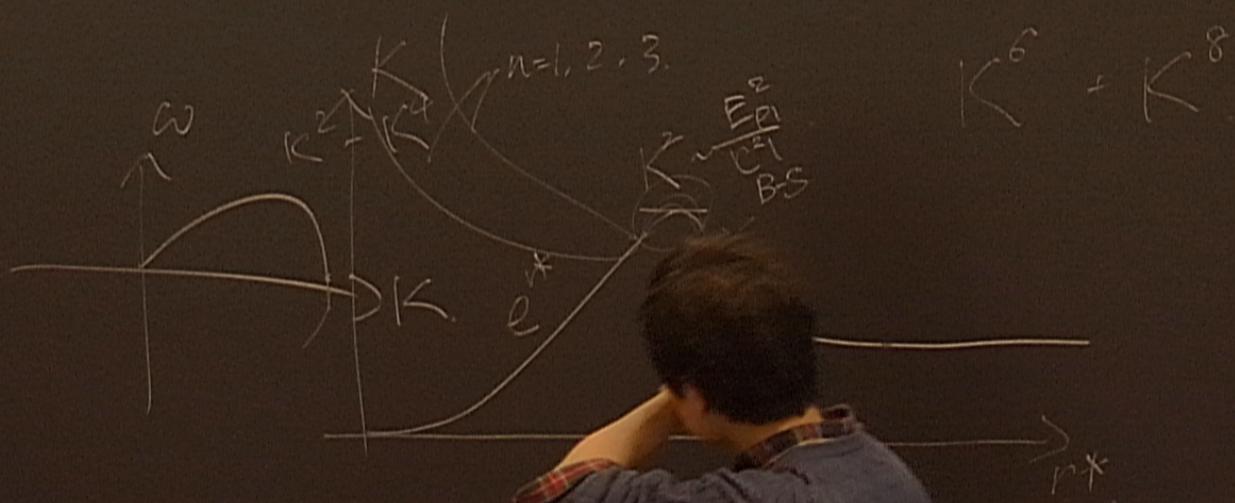


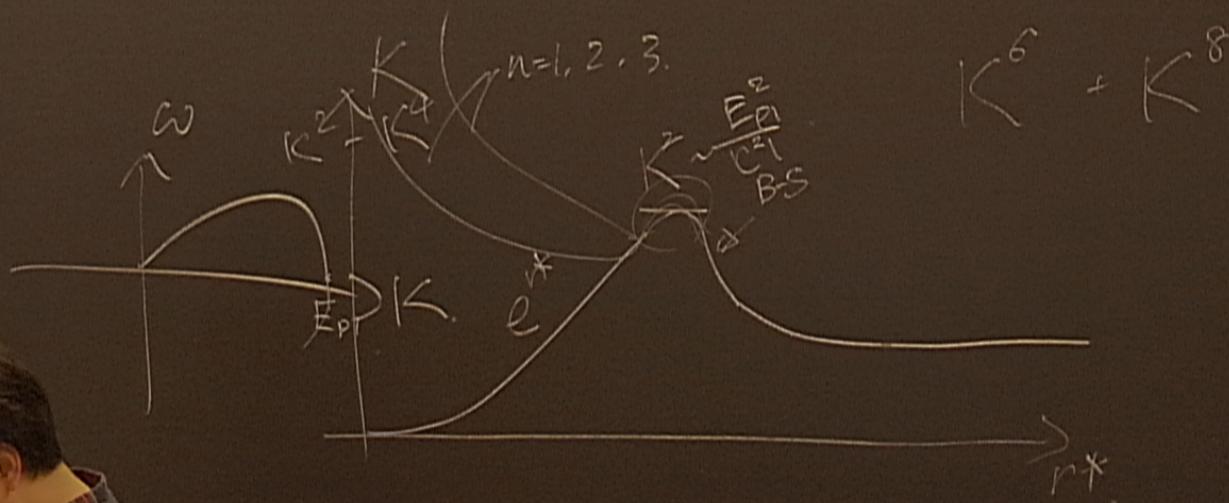
# QNMs with modified DRs



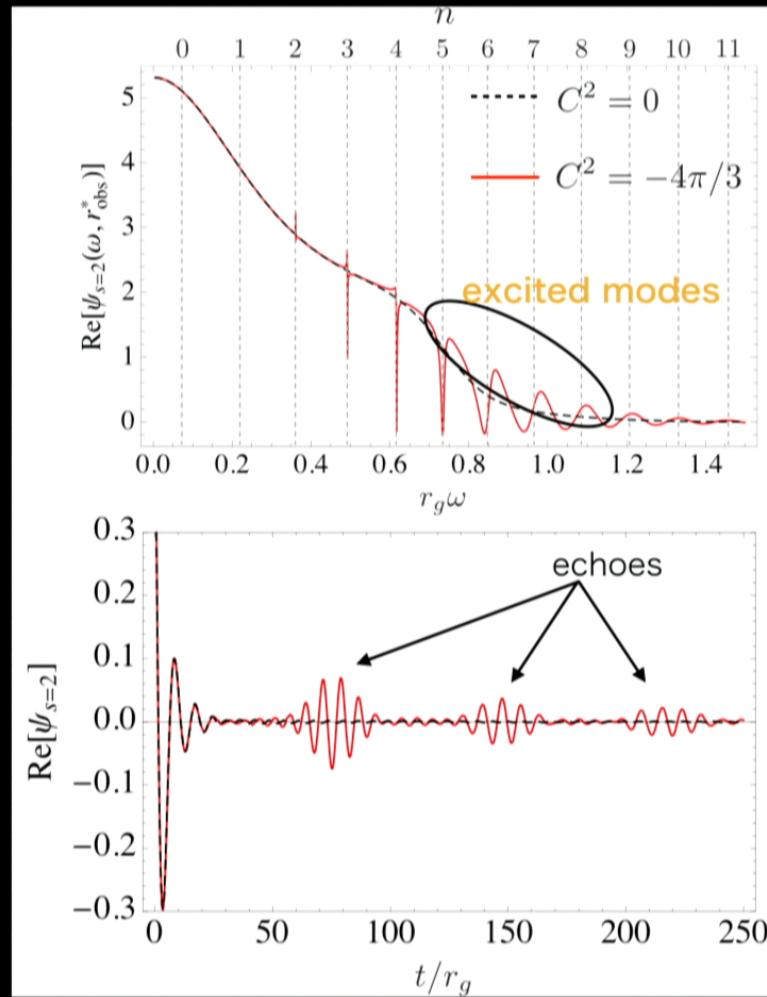
smaller microstructure  
↔  
more long-lived QNMs



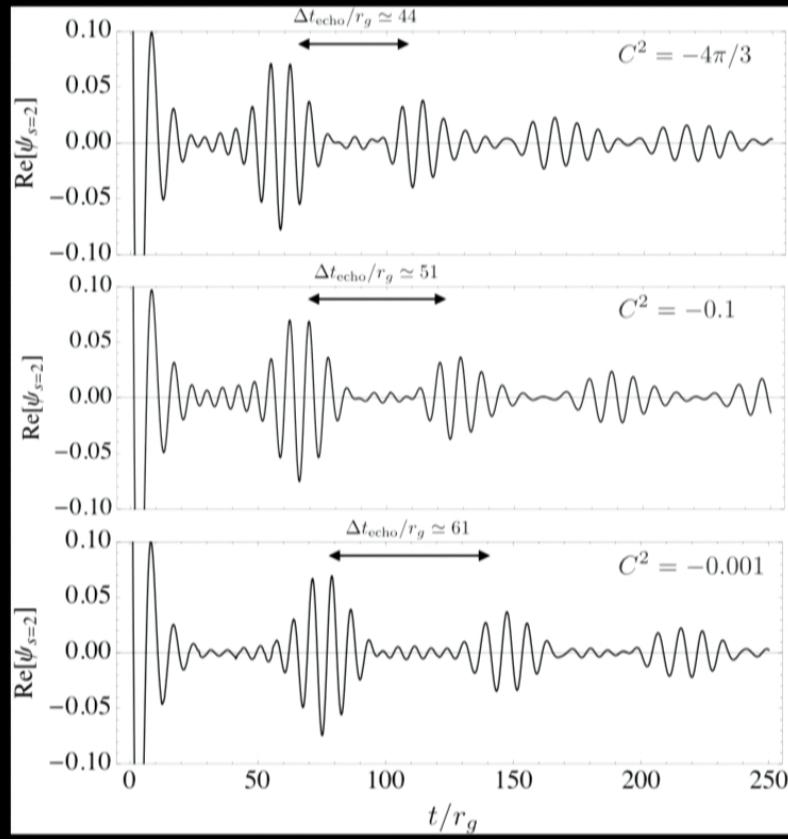




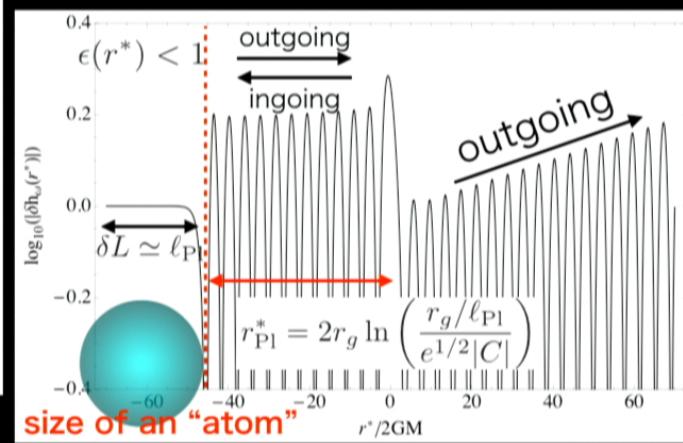
# Supporting evidence of atoms of spacetime - echoes from a black hole -



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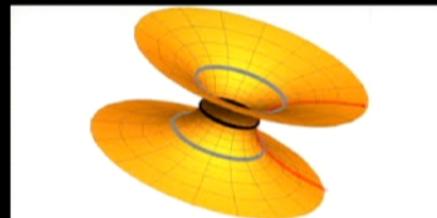


$$\Delta t_{\text{echo}} \equiv 4r_g \ln \left( \frac{r_g/\ell_{\text{Pl}}}{e^{1/2}|C|} \right)$$



# Probing atoms of spacetime with BH ringdowns

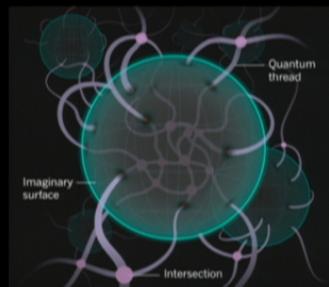
**Previous works** show that a ECHO-signal can be a probe of the **Exotic Compact Objects (ECOs)** which imitate black holes.  
e.g. wormhole, gravaster, mirror, firewall etc



Cardoso et al. PRL (2016)

**Our work** implies that the non-trivial dispersion relation of quantum gravity can be testable with ringdown GWs.

e.g. **loop quantum gravity, Horava-Lifshitz Gravity** etc



non-trivial dispersion relation

# Summary & Conclusions



- Planckian scale appears near a horizon.
- We can model the microscopic structure of spacetime by modifying its dispersion relation
- NO ingoing modes (NO oscillatory solution) near the horizon → boundary condition changed there
- Then, quantum gravity can be testable with ringdown-GWs from a black hole.

