

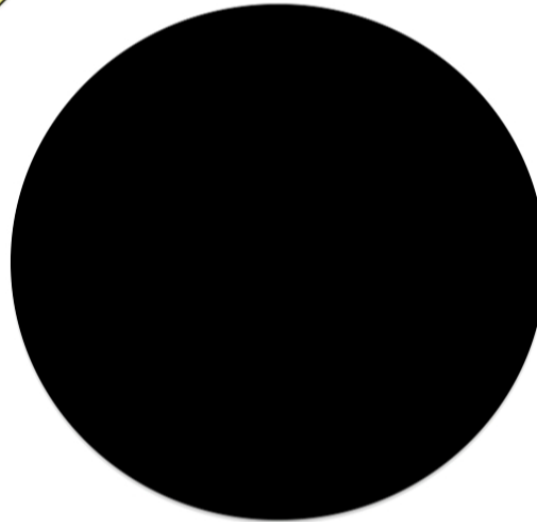
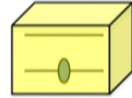
Title: Entanglement harvesting near black holes

Date: Jan 25, 2018 03:00 PM

URL: <http://pirsa.org/18010086>

Abstract: <p>Although entanglement harvesting was first posited over 25 years ago, it is only in recent years that this phenomenon has been the subject of active study. The basic idea of entanglement harvesting is to transfer correlations from the vacuum of some quantum field to a pair of detectors. The result provides a new probe of the structure of spacetime via quantum correlations. I shall describe recent work on some of the first results in harvesting entanglement in curved spacetime, in particular anti de Sitter spacetime and black holes.</p>

Harvesting Entanglement Near Black Holes



Robert B. Mann
L. Henderson R. Hennigar K. Ng A. Smith J. Zhang
E. Martin-Martinez

Entanglement Harvesting

- Extracting correlations from the vacuum

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- Extracting correlations from the vacuum
- Uncorrelated detectors can become correlated after a finite time depending on their
 - Energy gaps
 - Separation
 - State of motion

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- Applications (in principle)
 - Seismology
 - Ranging
 - Quantum Key Distribution
 - Extraction from Atoms

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 - Seismology Brown/Donnelly/Kempf/RBM/Martin-Martinez
NJP16 (2014)105020
 - Ranging Salton/RBM/Menicucci NJP17 (2015) 035001
 - Quantum Key Distribution Ralph/Walk NJP17 (2015) 063008
 - Extraction from Atoms Pozas-Kerstjens /Martin-Martinez
PRD94 (2016) 064074

A Brief History of Entanglement Harvesting

- 1991: Valentini: uncorrelated atoms that are spacelike separated can become correlated via QED vacuum fluctuations Valentini PLA153(1991) 321
- 2003: Reznik rediscovers and quantifies this effect Reznik
FndPhy 33 (2003) 167
- 2009: VerSteeg/Menicucci: investigate non-local correlations between detectors in de Sitter spacetime → first curved-spacetime study

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Ver Steeg/Menicucci PRD 79 (2009) 044027
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Martin-Martinez /Brown/Donnelly PRA88 (2013) 052310

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- 2013: Sustainable Harvesting → entanglement farming
Martin-Martinez /Brown/Donnelly PRA88 (2013) 052310
- 2017: Harvesting outside of black holes
Henderson/Hennigar/RBM/Smith/ Zhang (2018) 1712.10018

Quantum Detectors

Vacuum

$$S = \frac{m_0}{2} \int d\tau \left[(\partial_\tau \mathcal{Q})^2 - \Omega_0^2 \mathcal{Q}^2 \right] - \int d^4x \sqrt{-g} \frac{1}{2} (\nabla \Phi(x))^2 + S_I$$

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Cavity

$$\hat{H} = \Omega_d \hat{a}_d^\dagger \hat{a}_d + \frac{dt}{d\tau} \sum_n \omega_n \hat{a}_n^\dagger \hat{a}_n + H_I$$

Quantum Detectors

S-Y Lin, B.L.Hu PRD73 (2006) 124018

PRD76 (2007) 064008

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interaction

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detector
field
interaction

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E.G. Brown, E. Martin-Martinez, N. Menicucci, RBM PRD87 (2013) 084062

D. Bruschi, A. Lee, I Fuentes J. Phys A46 (2013) 165303

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Provide an operational means of probing the quantum character of spacetime

E.G. Brown, E. Martin-Martinez, N. Menicucci, RBM PRD87 (2013) 084062
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Hot Accelerating Detectors?

$$T = \frac{a}{2\pi} \left(\frac{\hbar}{k_B c} \right)$$

S.A. Fulling PRD7 (1973) 2850 P.C.W.
Davies J Phys A8 (1975) 609
W. G. Unruh PRD14 (1976) 3251

- Unruh effect
 - Geometric Methods + Bogoliubov transformations
 - Eternally accelerating qubit coupled to a quantum field

B. deWitt in *General Relativity: An Einstein Centenary Survey* (CUP 1980)

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- Unruh effect
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 - Eternally accelerating qubit coupled to a quantum field
- Limitations
 - Highly idealized: eternal uniform acceleration, unbounded system, perturbative, model-dependent, ...
- What we would like and need to know
 - Finite time and distance effects (cavities, switching)
 - Boundary conditions
 - Non-perturbative effects; non-equilibrium effects
 - Entanglement, Non-locality of correlations

B. deWitt in *General Relativity: An Einstein Centenary Survey* (CUP 1980)

Detector Response Outside Black Holes

- BTZ Black holes
 - Static and Rotating
- Schwarzschild Black Holes
- Schwarzschild AdS Black Holes
- All for various boundary conditions, detector trajectories

Hodgkinson/Louko PRD86 (2012) 064031

Hodgkinson/Louko/Ottewill
PRD89 (2014) 104002

Ng/ Hodgkinson/Louko/RBM/
Martin-Martinez
PRD90 (2014) 064003

$$H_{\text{int}} = c\chi(\tau)\mu(\tau)\phi(x(\tau))$$

$$P(E) = c^2 \left| \langle 0_d | \mu(0) | E \rangle \right|^2 \mathcal{F}(E)$$

$$\mathcal{F}(E) = \Re \left[\int_{-\infty}^{\infty} du \chi(u) \int_0^{\infty} ds \chi(u-s) e^{-iEs} G^+(u, u-s) \right]$$

$$\frac{d\mathcal{F}}{d\tau}(E; M, \ell, \dots) = \frac{1}{4} + 2\Re \left[\int_0^{\Delta\tau} ds e^{-iEs} G^+(\tau, \tau-s) \right]$$

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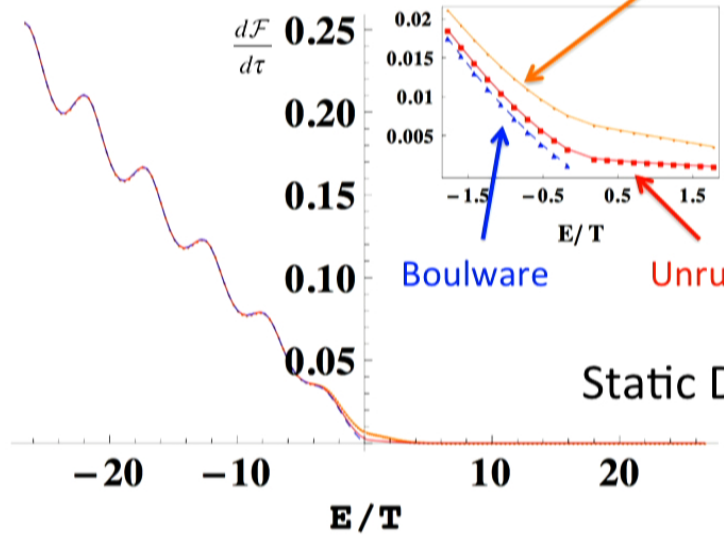
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Detector
Response
Rate

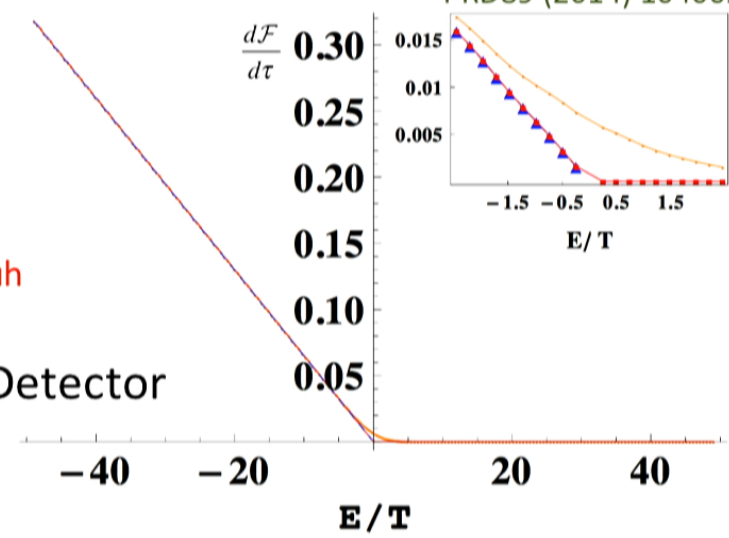


Schwarzschild



(a) $R = 4M$

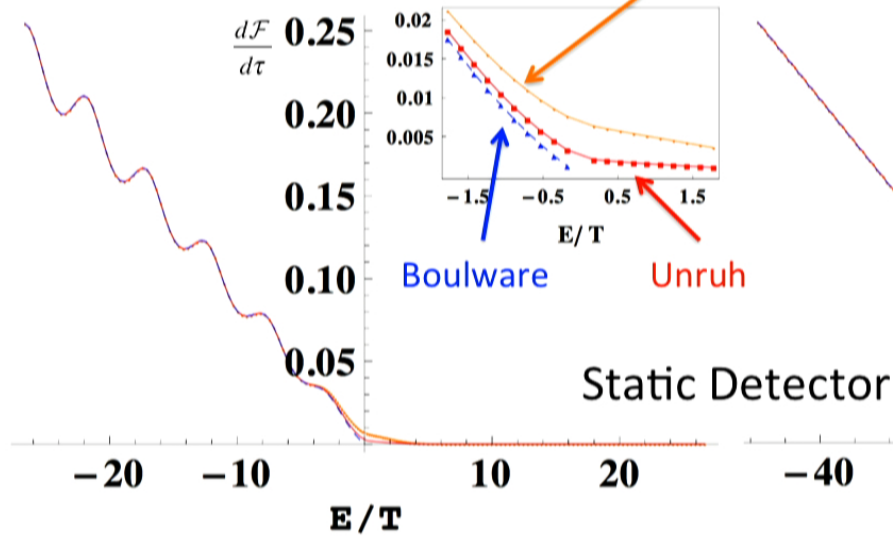
Hartle-Hawking



(b) $R = 40M$

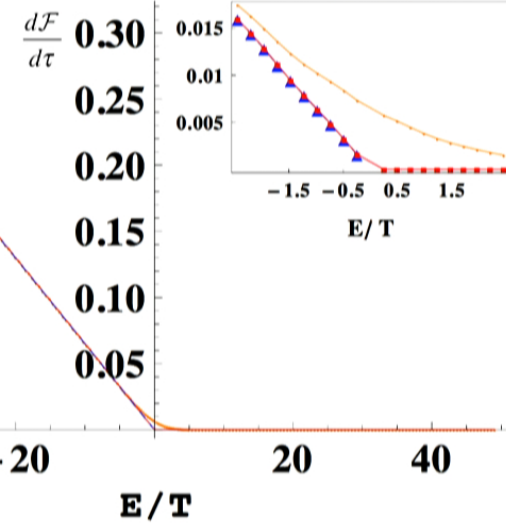
Hodgkinson/Louko/Ottewill PRD89 (2014) 104002

Schwarzschild

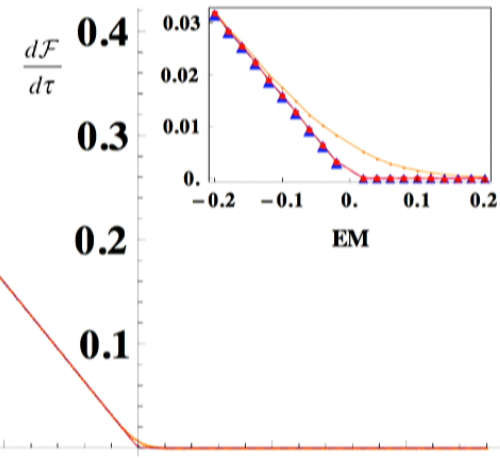
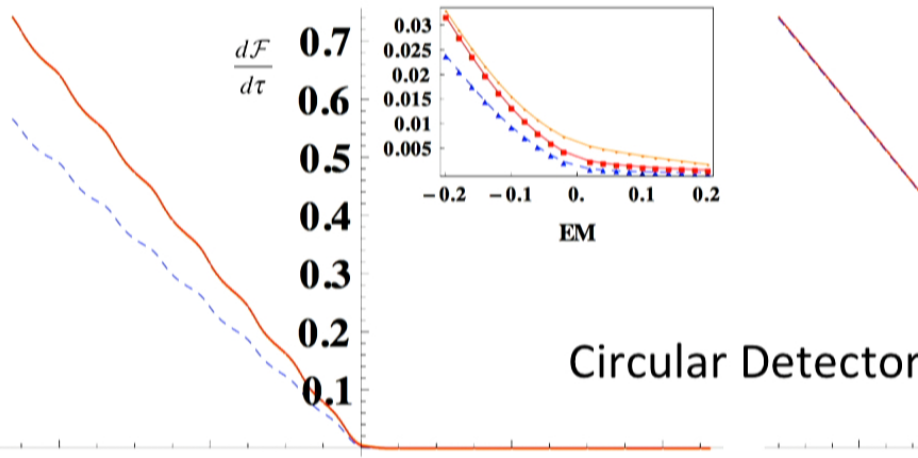


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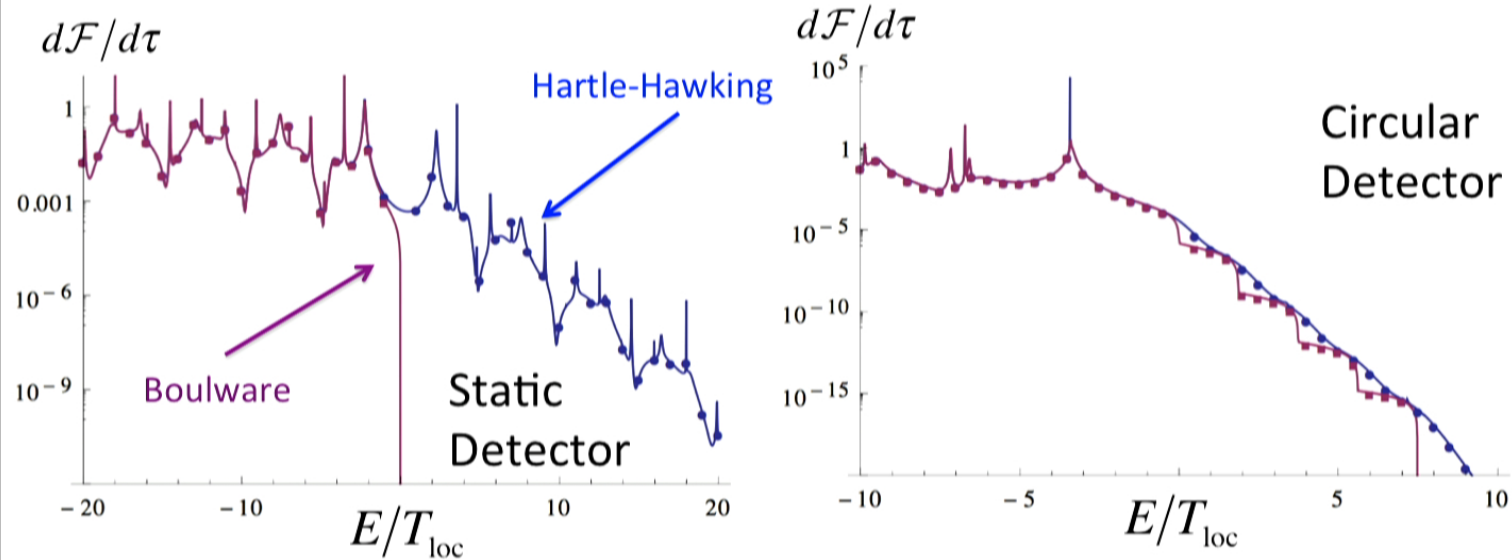


(b) $R = 40M$



Detector Response in Schwarzschild-AdS

Ng/ Hodgkinson/Louko/RBM/Martin-Martinez
PRD90 (2014) 064003



- Spikes due to Quasinormal mode resonances
- Visible only when black hole is much smaller than AdS length
- Peaks become higher and sharper as black hole size decreases

Harvesting in Flat Spacetime

- Single Detectors have sensitivity to spacetime geometry and topology

Harvesting in Flat Spacetime

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- Can more be learned from Detector correlations?
- Flat Spacetime
 - 2 Static Detectors

Pozas-Kerstjens/Martin-Martinez
PRD92 (2015) 064042

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- Can more be learned from Detector correlations?
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 - 2 Static Detectors
 - 2 Accelerating Detectors
 - Detectors in Identified Minkowski Space

Pozas-Kerstjens/Martin-Martinez
PRD92 (2015) 064042

Salton/RBM/Menicucci
NJP17 (2015) 035001

Harvesting Formalism

$$S = -\int d^4x \sqrt{-g} \left[R + \frac{1}{2} \partial_\mu \Phi(x) \partial^\mu \Phi(x) - \xi R \Phi^2(x) \right] \\ + \int d\tau \left\{ \frac{m_0}{2} [(\partial_\tau Q)^2 - \Omega_0^2 Q^2] + \sum_D \lambda_D \int d^4x Q_D(\tau) \Phi(x) \delta^4(x^\mu - z_D^\mu(\tau)) \right\}$$

Harvesting Formalism


$$\begin{aligned}
 S = & -\int d^4x \sqrt{-g} \left[R + \frac{1}{2} \partial_\mu \Phi(x) \partial^\mu \Phi(x) - \xi R \Phi^2(x) \right] \\
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 & \underbrace{\hspace{10em}} \\
 H_{ID}(\tau) = & \chi_D(\tau) \left[e^{i\Omega_D \tau} \sigma_D^+ + e^{-i\Omega_D \tau} \sigma_D^- \right] \Phi[z_D(\tau)]
 \end{aligned}$$

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switcher

$$\chi_D = \exp\left(-\frac{(\tau - \tau_D)^2}{2\sigma_D^2}\right)$$


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switcher

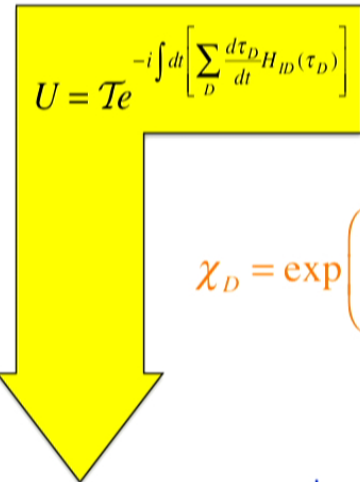
monopole operator

$$\chi_D = \exp\left(-\frac{(\tau - \tau_D)^2}{2\sigma_D^2}\right)$$

$$\sigma_D^+ := |1_D\rangle\langle 0_D| = |e_D\rangle\langle g_D| \\ \sigma_D^- := |0_D\rangle\langle 1_D| = |g_D\rangle\langle e_D|$$

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$$U = \mathcal{T} e^{-i \int d\tau \left[\sum_D \frac{d\tau_D}{dt} H_{ID}(\tau_D) \right]}$$

$$H_{ID}(\tau) = \chi_D(\tau) \left[e^{i\Omega_D \tau} \sigma_D^+ + e^{-i\Omega_D \tau} \sigma_D^- \right] \Phi[z_D(\tau)]$$

switcher

monopole operator

$$\chi_D = \exp\left(-\frac{(\tau - \tau_D)^2}{2\sigma_D^2}\right)$$

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$$\rho_{ij} := \text{Tr}_\Phi(U |\Psi\rangle_i \langle\Psi|_i U^\dagger) = \begin{pmatrix} 1 - P_A - P_B & 0 & 0 & X \\ 0 & P_B & C & 0 \\ 0 & C^* & P_A & 0 \\ X^* & 0 & 0 & 0 \end{pmatrix} + \mathcal{O}(\lambda^4)$$


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$$P_D = \lambda^2 \int_{-\infty}^{\infty} d\tau_D \int_{-\infty}^{\infty} d\tau_{D'} \chi_D(\tau_D) \chi_{D'}(\tau_{D'}) e^{-i\Omega_D(\tau_D - \tau_{D'})} W(x_D(\tau_D), x_{D'}(\tau_{D'})) \quad D = A, B$$

$$C = \lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^{\infty} dt' \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A - \Omega_B \tau_B)} W(x_A(t), x_B(t'))$$

$$X = -\lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^t dt' \left[\frac{d\tau_A}{dt'} \frac{d\tau_B}{dt} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_B \tau_B + \Omega_A \tau_A)} W(x_A(t'), x_B(t)) \right. \\ \left. + \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A + \Omega_B \tau_B)} W(x_B(t'), x_A(t)) \right]$$

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$$W(x, x') := \langle 0 | \phi(x) \phi(x') | 0 \rangle$$

$$\tau_D = \gamma_D t$$

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$$X = -\lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^t dt' \left[\frac{d\tau_A}{dt'} \frac{d\tau_B}{dt} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_B \tau_B + \Omega_A \tau_A)} W(x_A(t'), x_B(t)) \right. \\ \left. + \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A + \Omega_B \tau_B)} W(x_B(t'), x_A(t)) \right]$$

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$$P_D = \lambda^2 \int_{-\infty}^{\infty} d\tau_D \int_{-\infty}^{\infty} d\tau_{D'} \chi_D(\tau_D) \chi_{D'}(\tau_{D'}) e^{-i\Omega_D(\tau_D - \tau_{D'})} W(x_D(\tau_D), x_{D'}(\tau_{D'})) \quad D = A, B \quad \text{Local excitations}$$

$$C = \lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^{\infty} dt' \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A - \Omega_B \tau_B)} W(x_A(t), x_B(t')) \quad \text{Local correlations}$$

$$X = -\lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^t dt' \left[\frac{d\tau_A}{dt'} \frac{d\tau_B}{dt} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_B \tau_B + \Omega_A \tau_A)} W(x_A(t'), x_B(t)) \right. \\ \left. + \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A + \Omega_B \tau_B)} W(x_B(t'), x_A(t)) \right] \quad \text{Non-Local correlations}$$

$$\rho = \begin{pmatrix} 1 - P_A - P_B & 0 & 0 & X \\ 0 & P_B & C & 0 \\ 0 & C^* & P_A & 0 \\ X^* & 0 & 0 & 0 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

$$W(x, x') := \langle 0 | \phi(x) \phi(x') | 0 \rangle$$

$$\tau_D = \gamma_D t$$

$$P_D = \lambda^2 \int_{-\infty}^{\infty} d\tau_D \int_{-\infty}^{\infty} d\tau_{D'} \chi_D(\tau_D) \chi_{D'}(\tau_{D'}) e^{-i\Omega_D(\tau_D - \tau_{D'})} W(x_D(\tau_D), x_{D'}(\tau_{D'})) \quad D = A, B \quad \text{Local excitations}$$

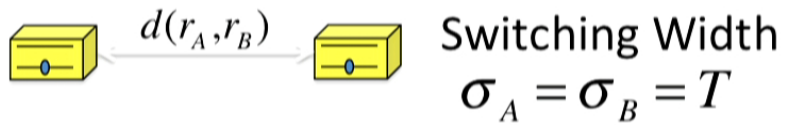
$$C = \lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^{\infty} dt' \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A - \Omega_B \tau_B)} W(x_A(t), x_B(t')) \quad \text{Local correlations}$$

$$X = -\lambda^2 \int_{-\infty}^{\infty} dt \int_{-\infty}^t dt' \left[\frac{d\tau_A}{dt'} \frac{d\tau_B}{dt} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_B \tau_B + \Omega_A \tau_A)} W(x_A(t'), x_B(t)) \right. \\ \left. + \frac{d\tau_A}{dt} \frac{d\tau_B}{dt'} \chi_A(\tau_A) \chi_B(\tau_B) e^{-i(\Omega_A \tau_A + \Omega_B \tau_B)} W(x_B(t'), x_A(t)) \right] \quad \text{Non-Local correlations}$$

Concurrence

$$C = 2\mathcal{N} = \max\{0, |X| - \sqrt{P_A P_B}\} + \mathcal{O}(\lambda^4)$$

Harvesting with Static Detectors



Pozas-Kerstjens/
Martin-Martinez
PRD92 (2015) 064042

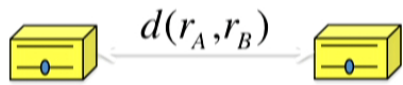
Switching Displacement

$$\tau_A - \tau_B = \Delta$$

Detector Gap

$$\Omega_A = \Omega_B = \Omega$$

Harvesting with Static Detectors



Switching Width
 $\sigma_A = \sigma_B = T$

Pozas-Kerstjens/
 Martin-Martinez
 PRD92 (2015) 064042

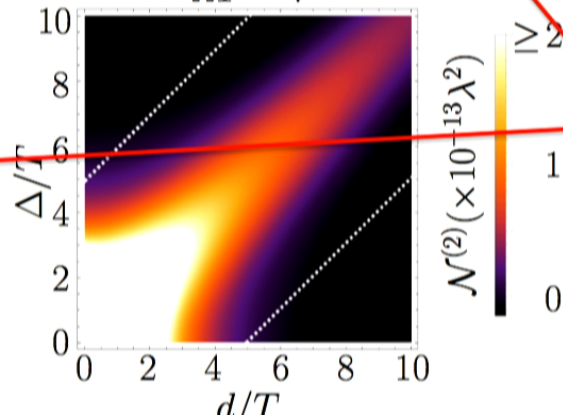
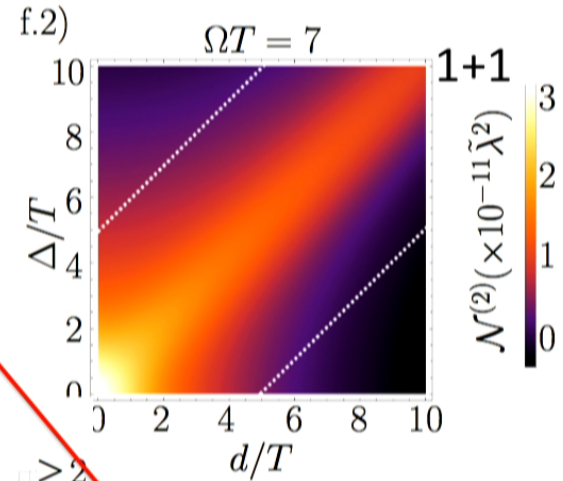
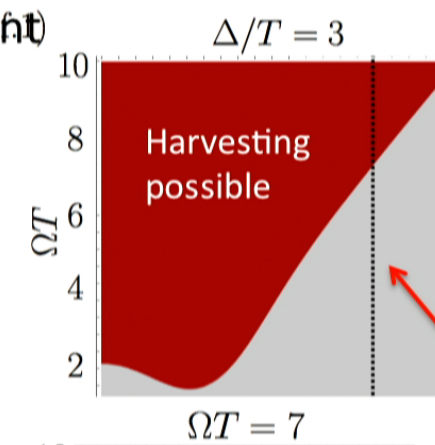
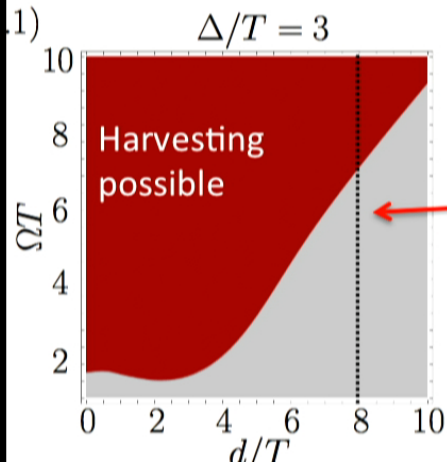
Switching Displacement
 $\tau_A - \tau_B = \Delta$

$$\tau_A - \tau_B = \Delta$$

Detector Gap
 $\Omega_A = \Omega_B = \Omega$

$$\Omega_A = \Omega_B = \Omega$$

3+1



Spacelike separation

General Features

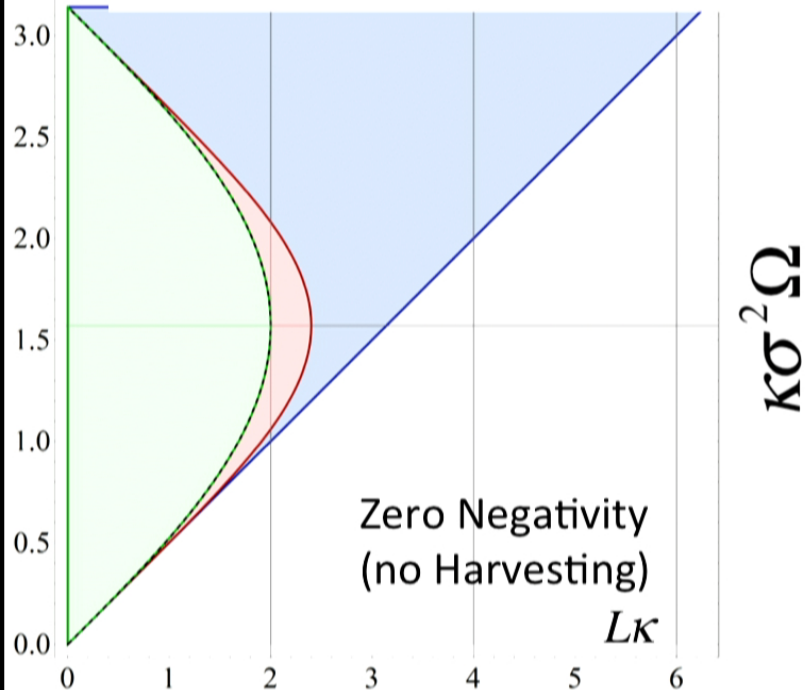
- Entanglement
 - Decreases with increasing separation
 - Increases with increasing gap
 - Weak dependence on spacetime dimension
 - Harvesting Possible at spacelike separation




General Features

- Entanglement
 - Decreases with increasing separation
 - Increases with increasing gap
 - Weak dependence on spacetime dimension
 - Harvesting Possible at spacelike separation
- Other features studied
 - Pointlike vs. finite size
 - Sudden switching vs. Gaussian Switching

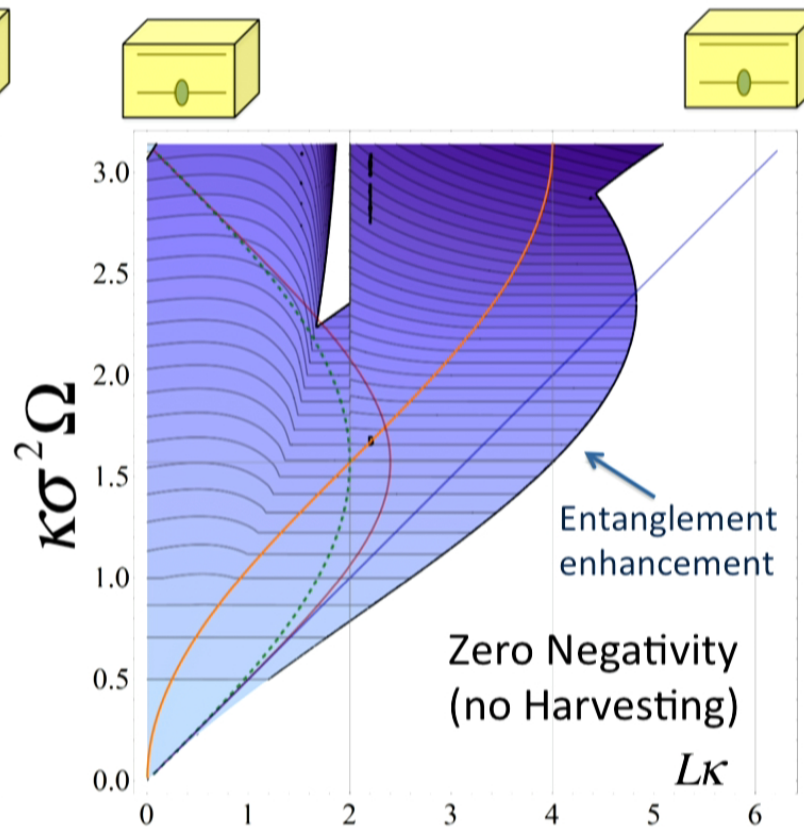
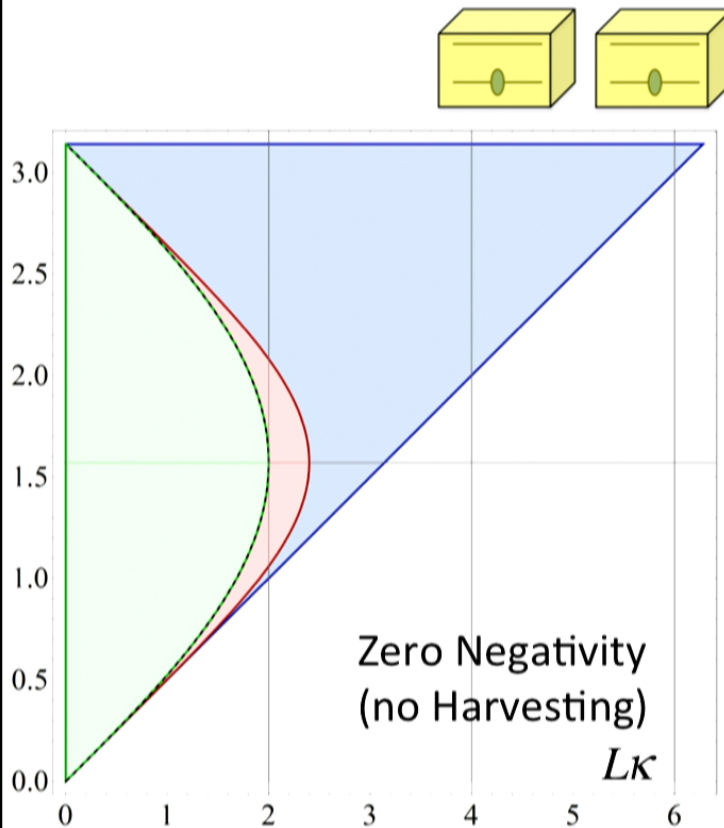


Harvesting with Accelerating Detectors



-  Parallel Acc'n or de Sitter
-  Inertial detectors in thermal Minkowski
-  Inertial detectors in vacuum Minkowski

VerSteeg/Menicucci
PRD79 (2009) 044027
Salton/RBM/Menicucci
NJP17 (2015) 035001

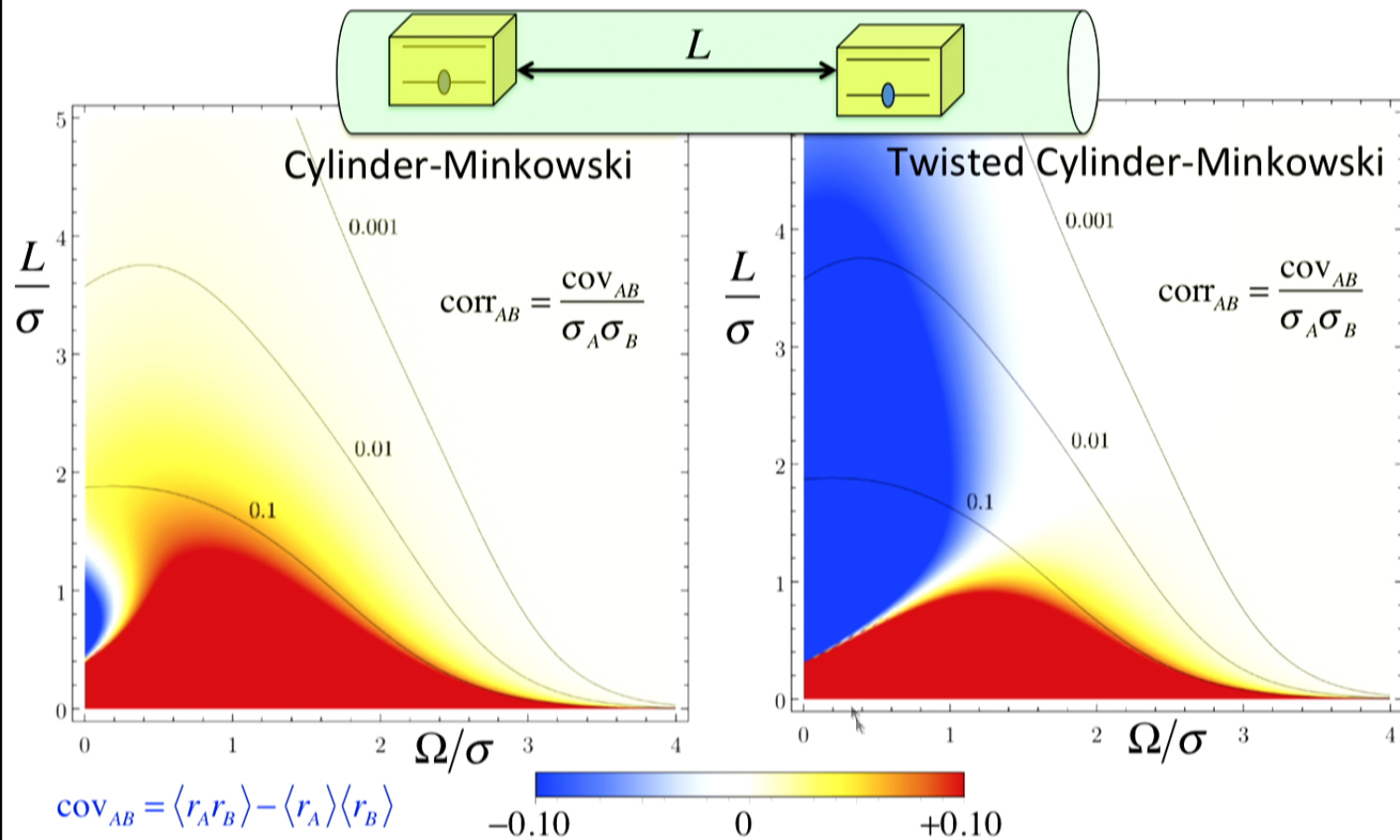


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VerSteeg/Menicucci
PRD79 (2009) 044027

Salton/RBM/Menicucci
NJP17 (2015) 035001

Harvesting as a Probe of Topology



$$\text{cov}_{AB} = \langle r_A r_B \rangle - \langle r_A \rangle \langle r_B \rangle$$

$$\sigma_A^2 = \text{cov}_{AA} \quad r \in \{0, 1\}$$

Martin-Martinez /Smith/Terno PRD93 (2016) 044001

Harvesting in Curved Spacetime

- De Sitter spacetime
 - Correlations distinct from thermal case

Harvesting in Curved Spacetime

- De Sitter spacetime
 - Correlations distinct from thermal case
- Anti de Sitter spacetime
 - Single detector: thermal response above threshold
 - Harvesting: ??????

VerSteeg/Menicucci
PRD79 (2009) 044027

Jennings
CQG 27 (2010) 205005

$$T = \frac{\sqrt{a^2 \ell^2 - 1}}{2\pi \ell}$$



Harvesting in Curved Spacetime

- De Sitter spacetime
 - Correlations distinct from thermal case
- Anti de Sitter spacetime
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 - Harvesting: ???????
- Black Holes
 - Single detector
 - response correlated with BH QNMs
 - sensitive to (hidden) topology
 - Harvesting: ???????

VerSteeg/Menicucci
PRD79 (2009) 044027

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PRD79 (2009) 044027

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Jennings
CQG 27 (2010) 205005

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Ng/Hodgkinson/Louko/
Mann/Martin-Martinez
PRD 90 (2014) 064003

Ng/Mann/Martin-Martinez
PRD 96 (2017) 0850043

- Harvesting: ???????

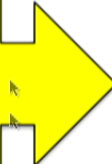
Smith/Mann CQG 31 (2014) 082001

Anti de Sitter Spacetime

$$\sum_{J=1}^{D-1} X_J^2 - T_1^2 - T_2^2 = -\ell^2$$

$$ds^2 = -dT_1^2 - dT_2^2 + \sum_{J=1}^{D-1} dX_J^2$$

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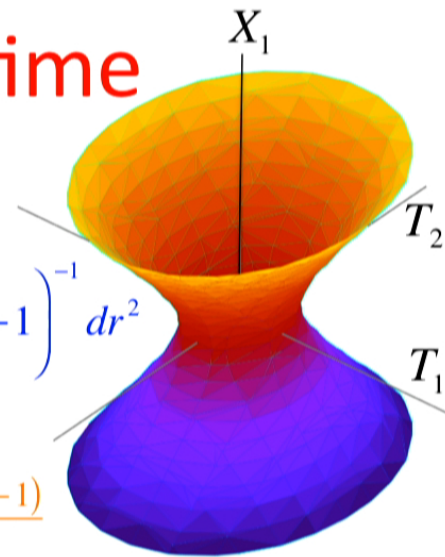


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$$\Lambda = -\frac{(D-2)(D-1)}{2\ell^2}$$



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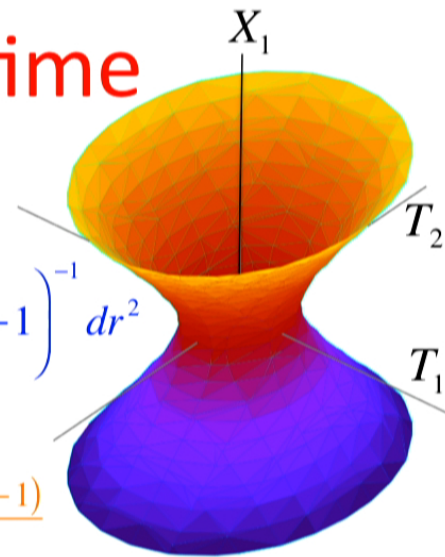
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Hyperboloid in flat spacetime²

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Conformal coupling

$$W_{AdS}^{(\zeta)}(x, x') = \frac{1}{4\pi\ell\sqrt{2}} \left(\frac{1}{\sqrt{\sigma_\epsilon(x, x')}} - \frac{\zeta}{\sqrt{\sigma_\epsilon(x, x') + 2}} \right) \quad 2+1$$

Geodesic length

Anti de Sitter Spacetime

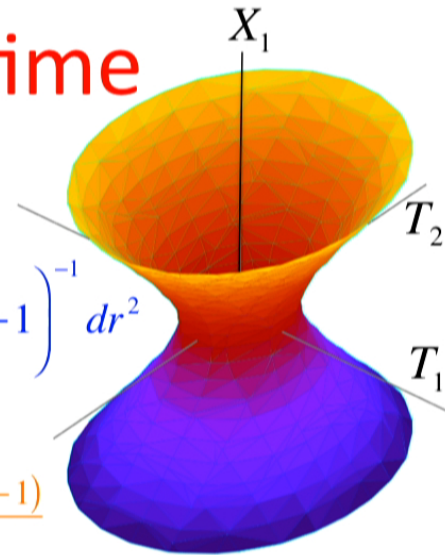
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Geodesic length

$$W_{AdS}^{(\zeta=1)}(x, x') = \sum_{\omega=0}^{\infty} \sum_{lm} \frac{1}{2\omega} e^{-i\omega(t-t')} \varphi_{\omega lm}(x) \bar{\varphi}_{\omega lm}(x') \quad 3+1$$

Sum over modes

$$\Phi_{\omega lm}(t, x) = \frac{1}{\sqrt{2\omega}} e^{-i\omega t} \varphi_{\omega lm}(x)$$

Anti de Sitter Spacetime

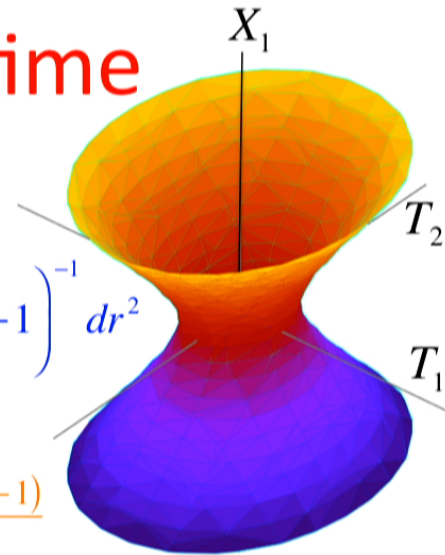
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Geodesic length

$\zeta = 1$ (Dirichlet)

$\zeta = 0$ (Transparent)

$\zeta = -1$ (Neumann)

$$W_{AdS}^{(\zeta=1)}(x, x') = \sum_{\omega=0}^{\infty} \sum_{lm} \frac{1}{2\omega} e^{-i\omega(t-t')} \varphi_{\omega lm}(x) \bar{\varphi}_{\omega lm}(x') \quad 3+1$$

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Harvesting in Anti de Sitter Space

2+1: Henderson/Hennigar/Smith/Zhang/RBM 1712.10018
3+1 Ng/Martin-Martinez/RBM (to appear)



Harvesting in Anti de Sitter Space

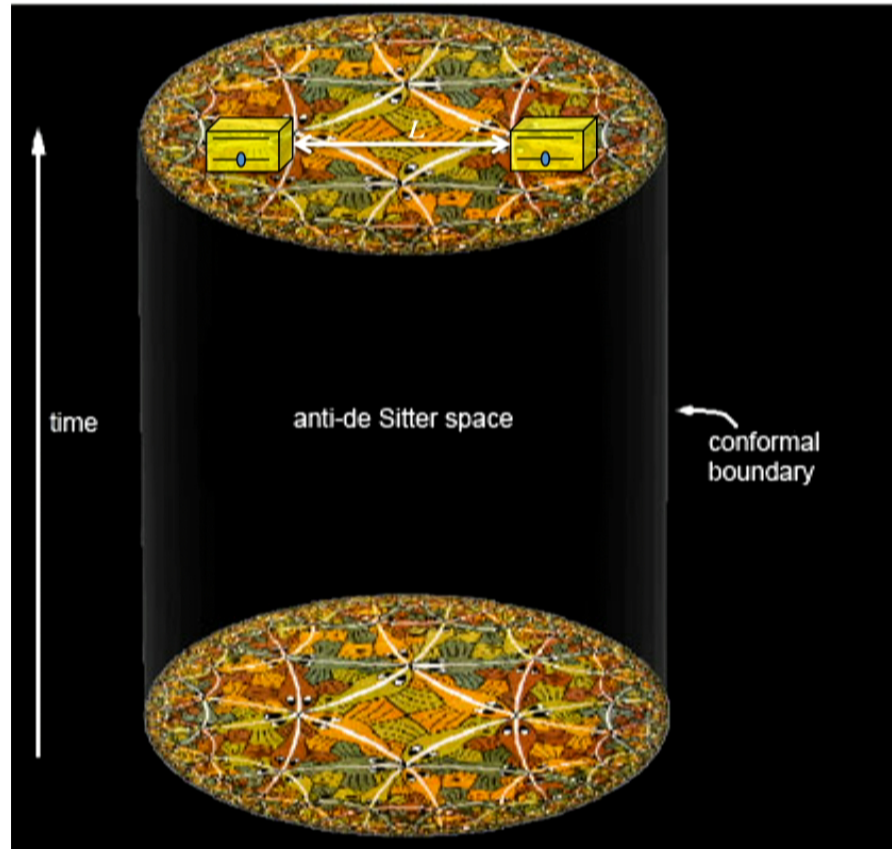
2+1: Henderson/Hennigar/Smith/Zhang/RBM 1712.10018

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2+1: Henderson/Hennigar/Smith/Zhang/RBM 1712.10018
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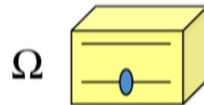
2+1 vs 3+1

	2+1	3+1
Constant Curvature	Yes	Yes
Conformally Flat	Yes	Yes
Conformally Coupled Scalar	Yes	Yes
Wightmann Function	Explicit Function of Geodesic length	Sum over Modes
Huygens Principle	No	Yes
Black Hole	From identifying AdS	Not identifying AdS

Results in 2+1 AdS

Henderson/Hennigar/
Smith/Zhang/RBM
(to appear)

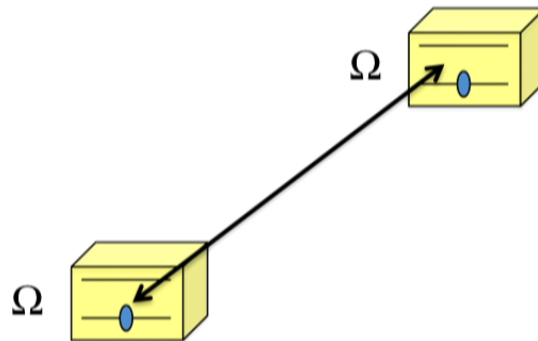
$$ds^2 = -\left(\frac{r^2}{\ell^2} + 1\right) dt^2 + \left(\frac{r^2}{\ell^2} + 1\right)^{-1} dr^2 + r^2 d\phi^2$$



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Smith/Zhang/RBM
(to appear)

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Switching Width

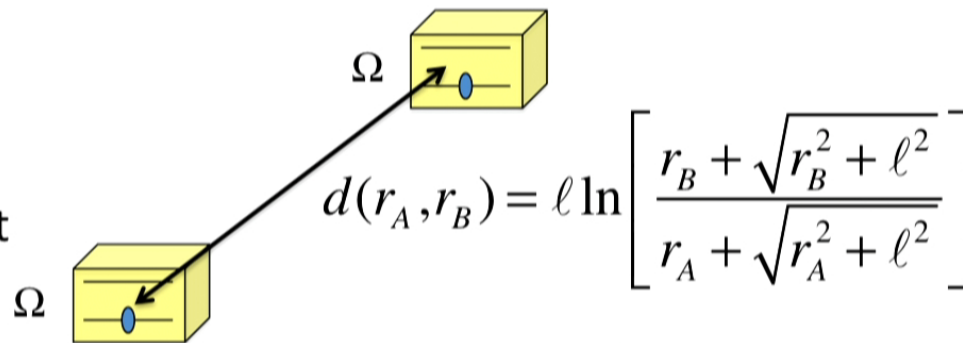
$$\sigma_A = \sigma_B = \sigma$$

Switching Displacement

$$\tau_A = \tau_B = 0$$

Detector Gap

$$\Omega_A = \Omega_B = \Omega$$

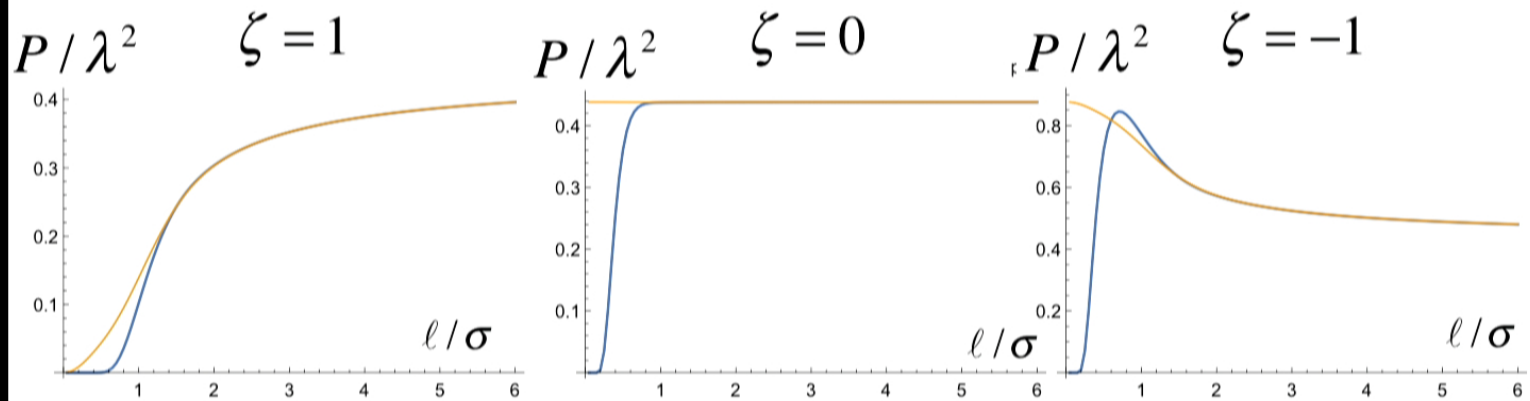


Detector Separation

$$d(0, r_B) / \sigma = 1$$

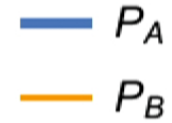
Detector Excitation

— P_A
— P_B

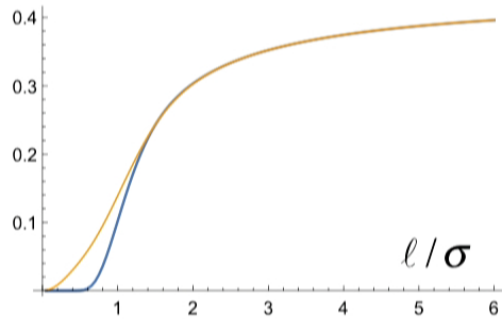


$$d(0, r_B) / \sigma = 1$$

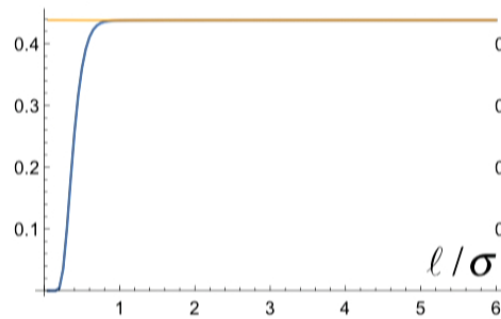
Detector Excitation



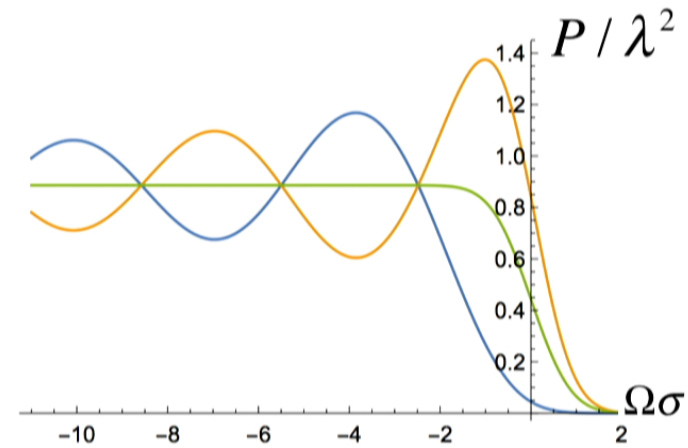
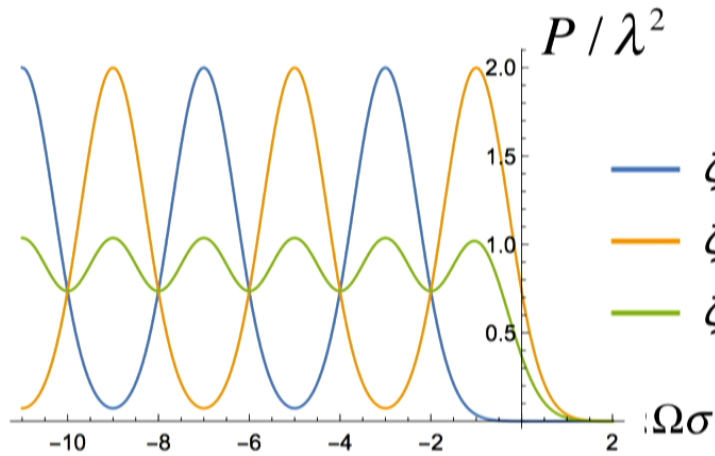
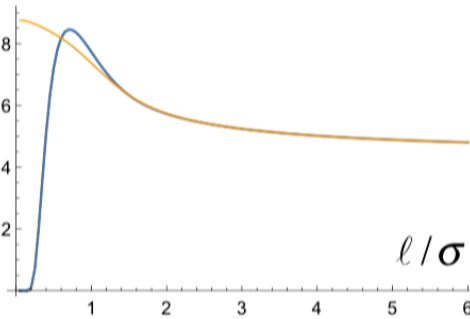
P / λ^2 $\zeta = 1$



P / λ^2 $\zeta = 0$

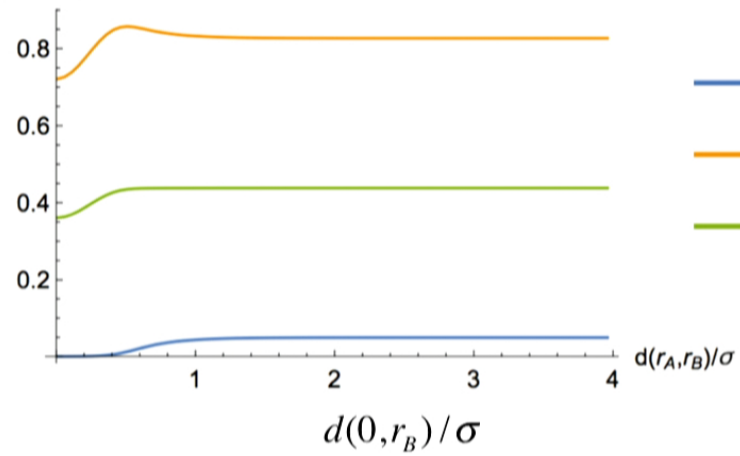


P / λ^2 $\zeta = -1$

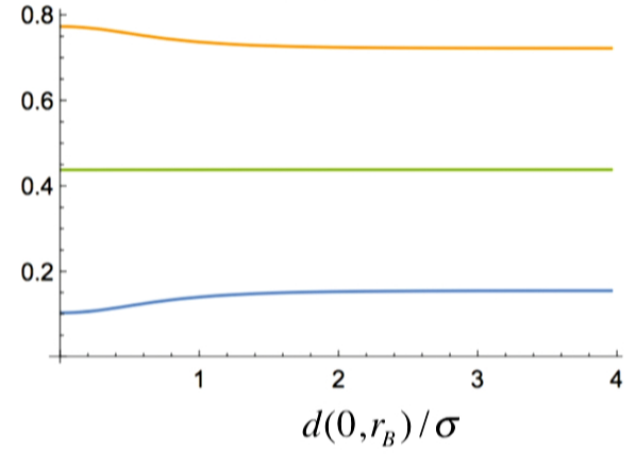


$$\Omega\sigma = 0.01$$

P/λ^2 $\ell/\sigma = 1/2$



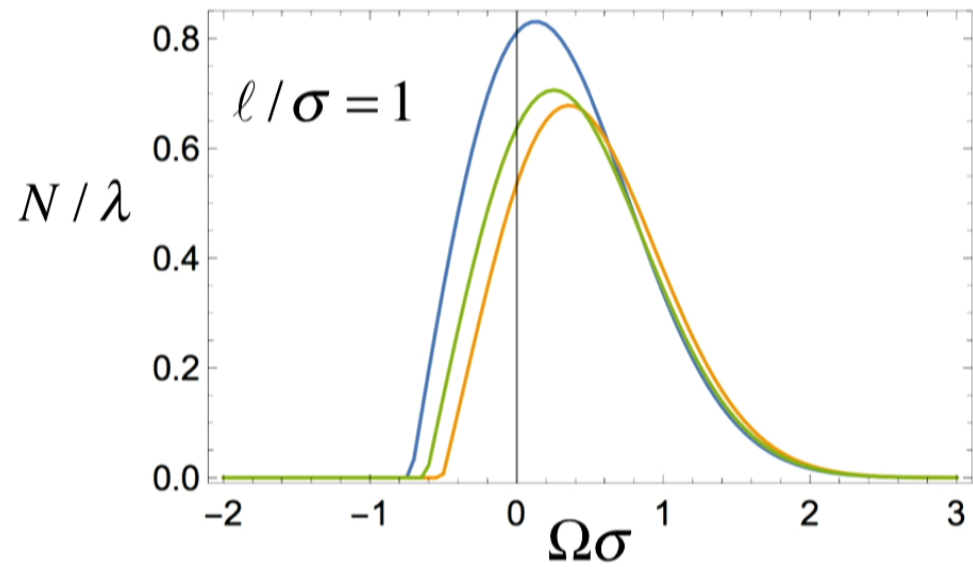
P/λ^2 $\ell/\sigma = 1$



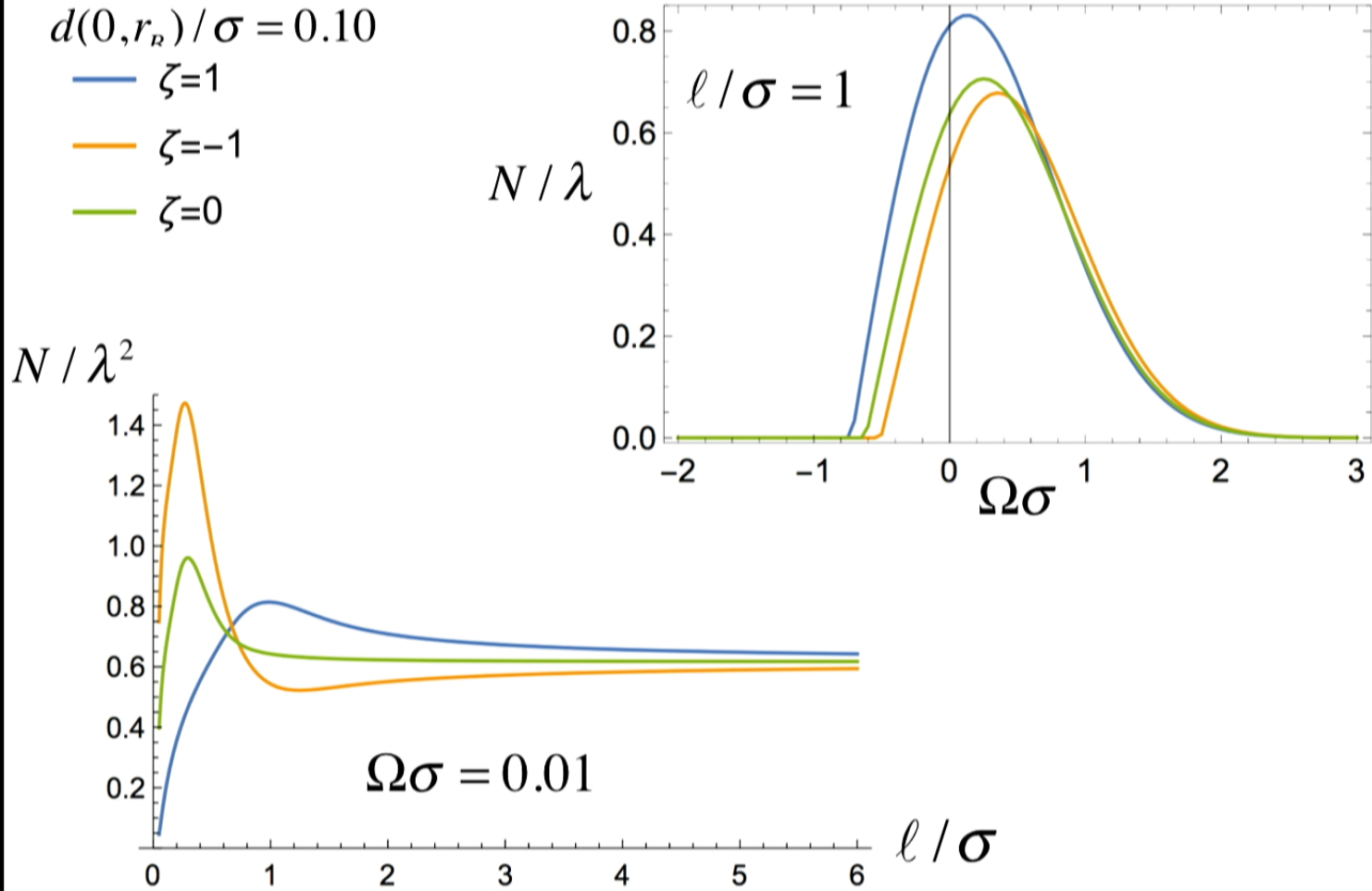
Negativity

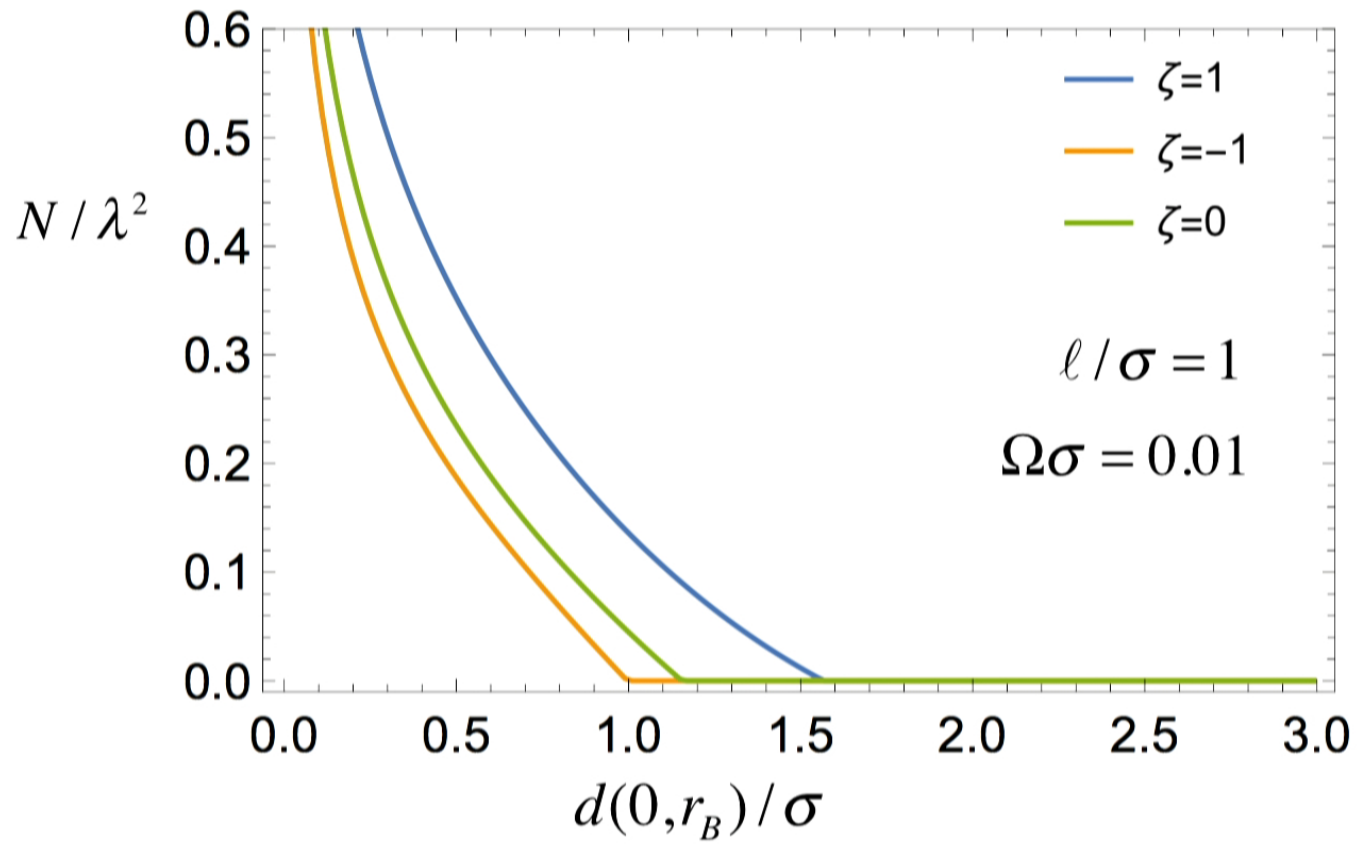
$$d(0, r_r) / \sigma = 0.10$$

- $\zeta=1$
- $\zeta=-1$
- $\zeta=0$

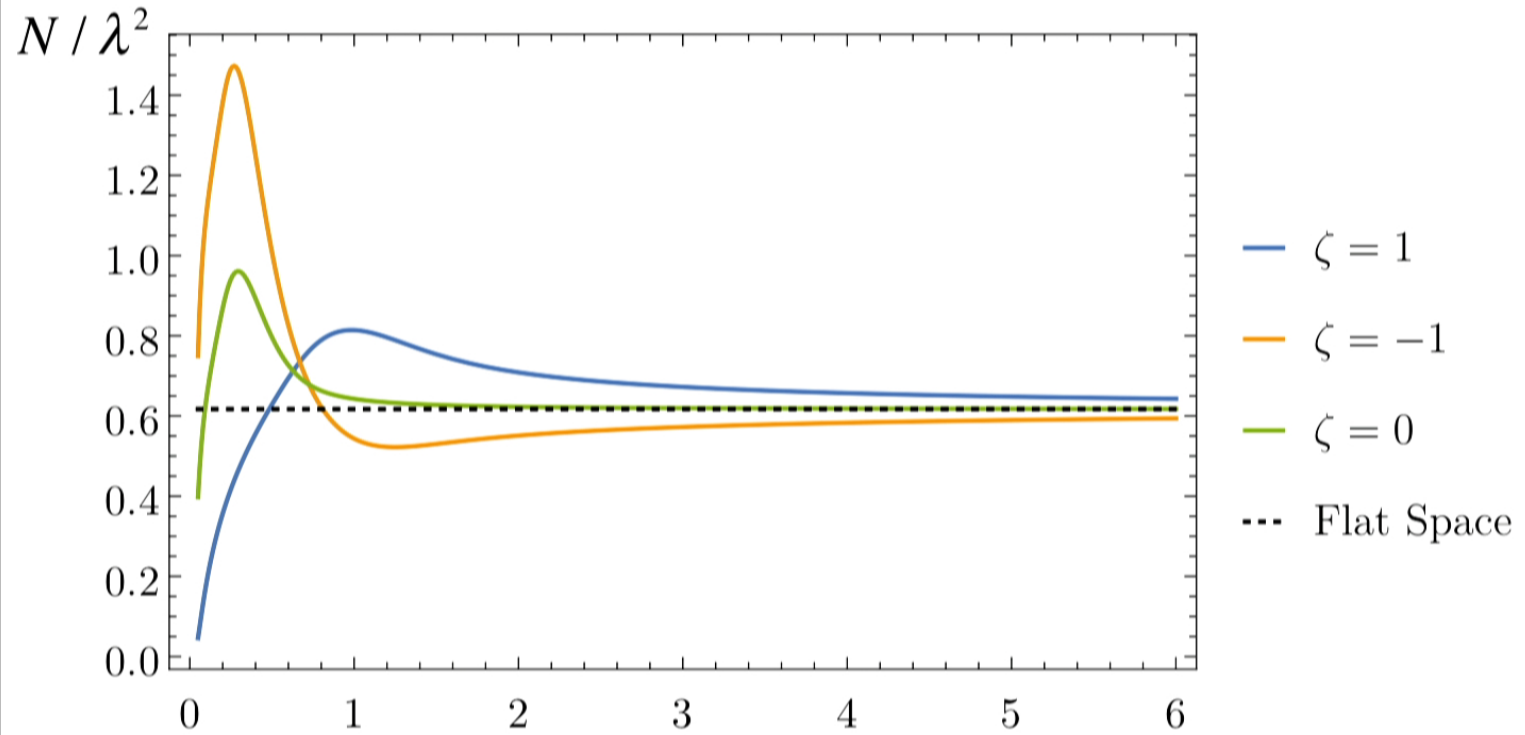


Negativity

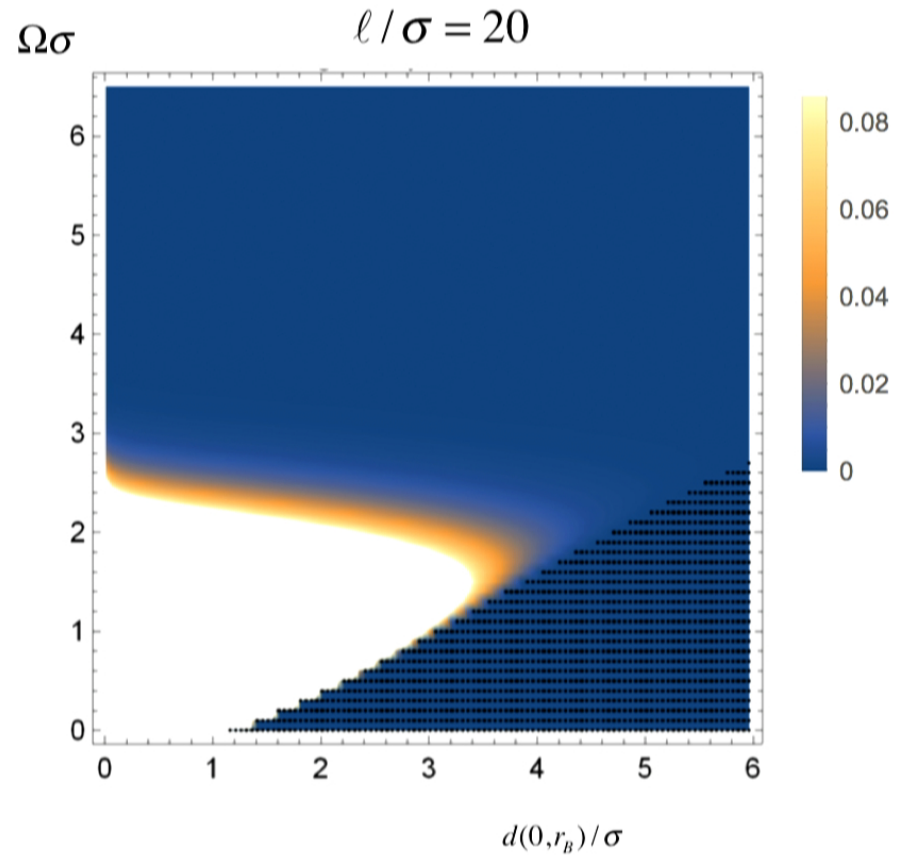




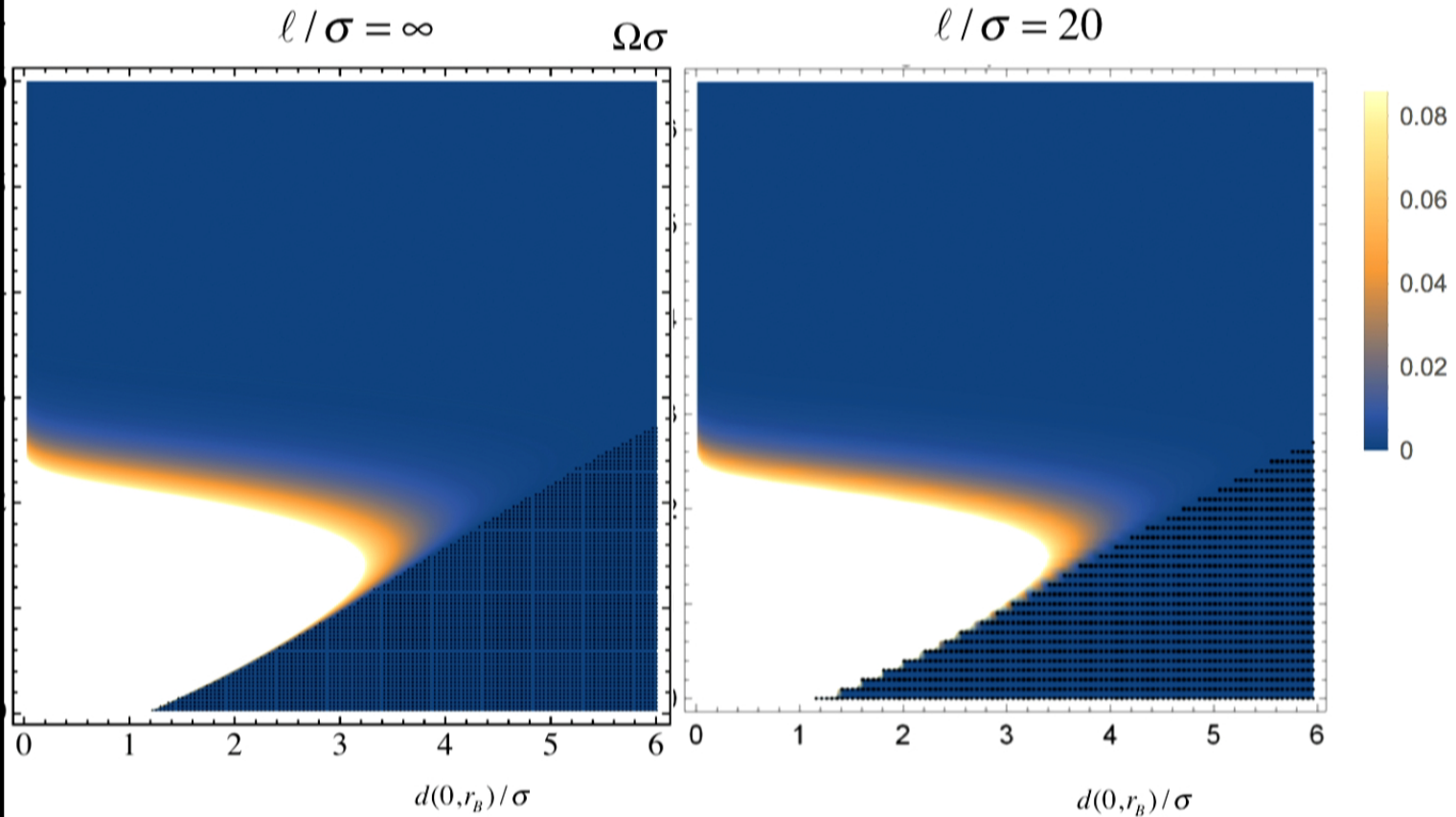
Flat Space Limit



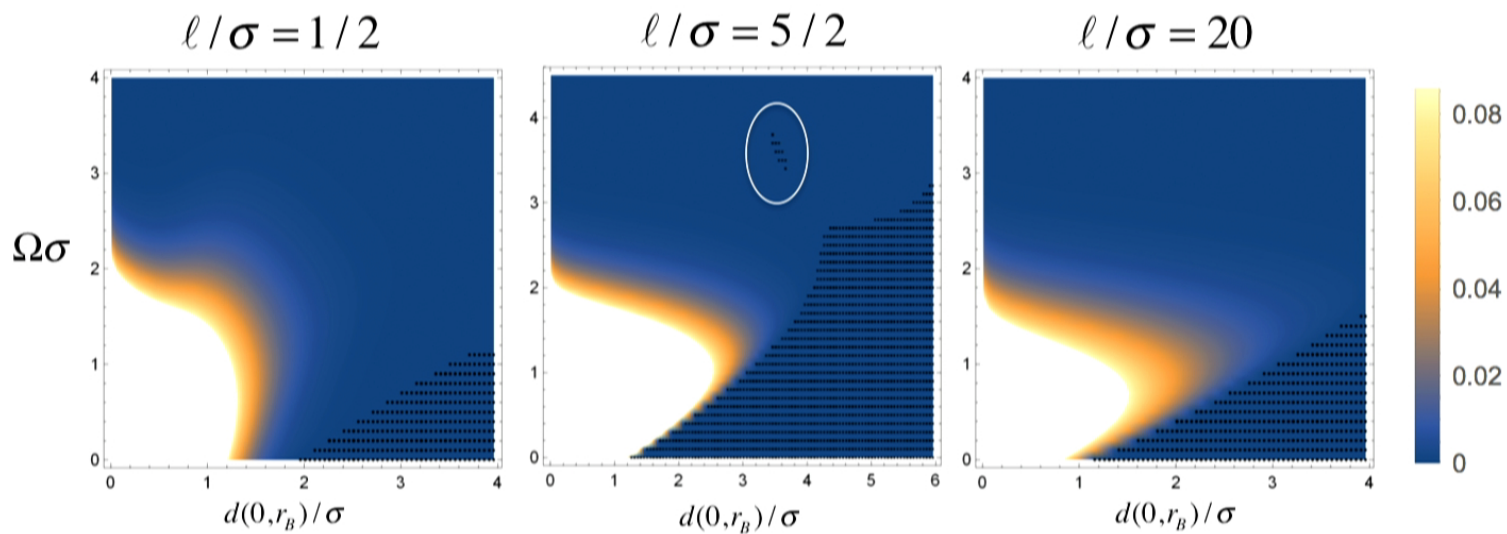
Flat Space Limit



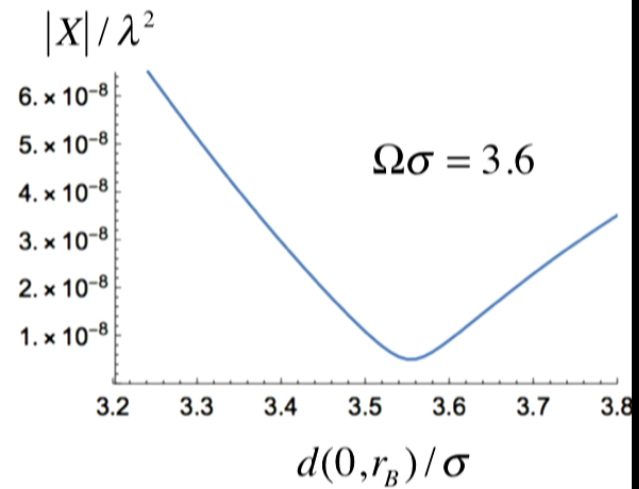
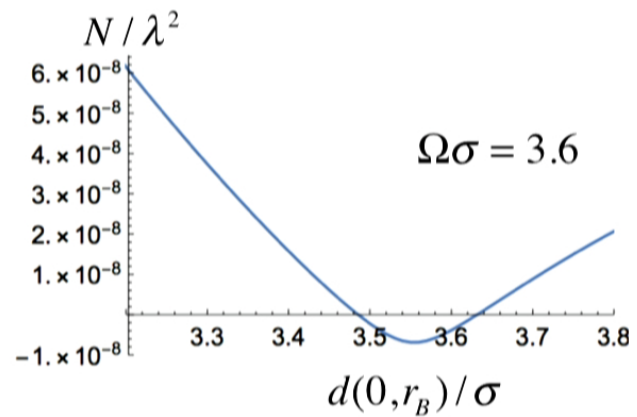
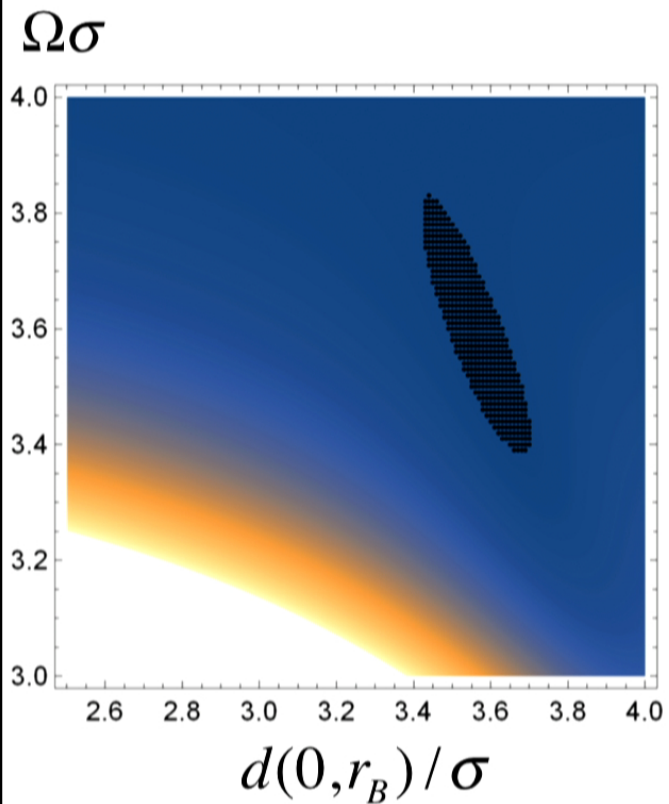
Flat Space Limit



Negativity $\zeta = 1$

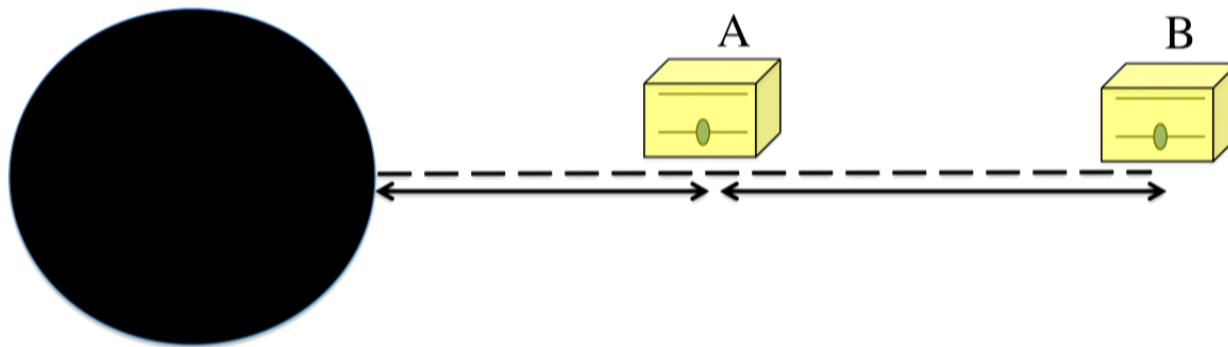


The Dead Zone $\ell/\sigma = 5/2$



Harvesting Near Black Holes

Henderson/Hennigar/Smith/Zhang/RBM
1712.10018

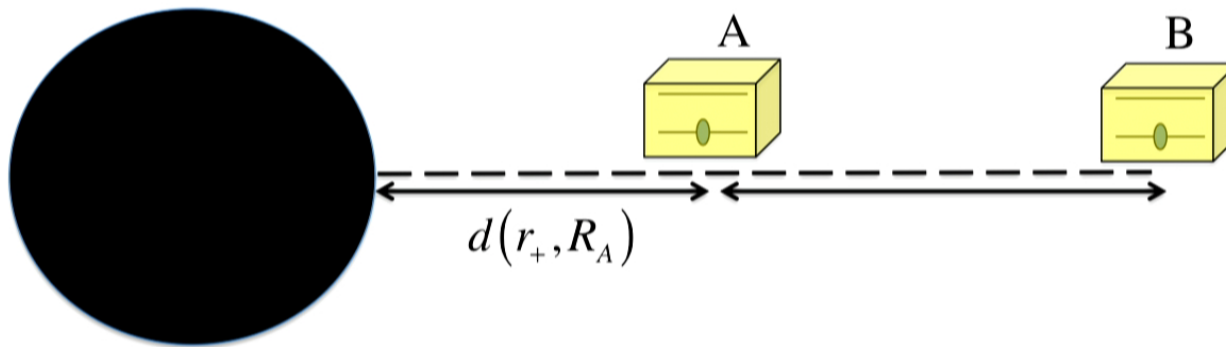


$$ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\phi^2$$

$$f(r) = \left(\frac{r^2}{\ell^2} - M \right)$$

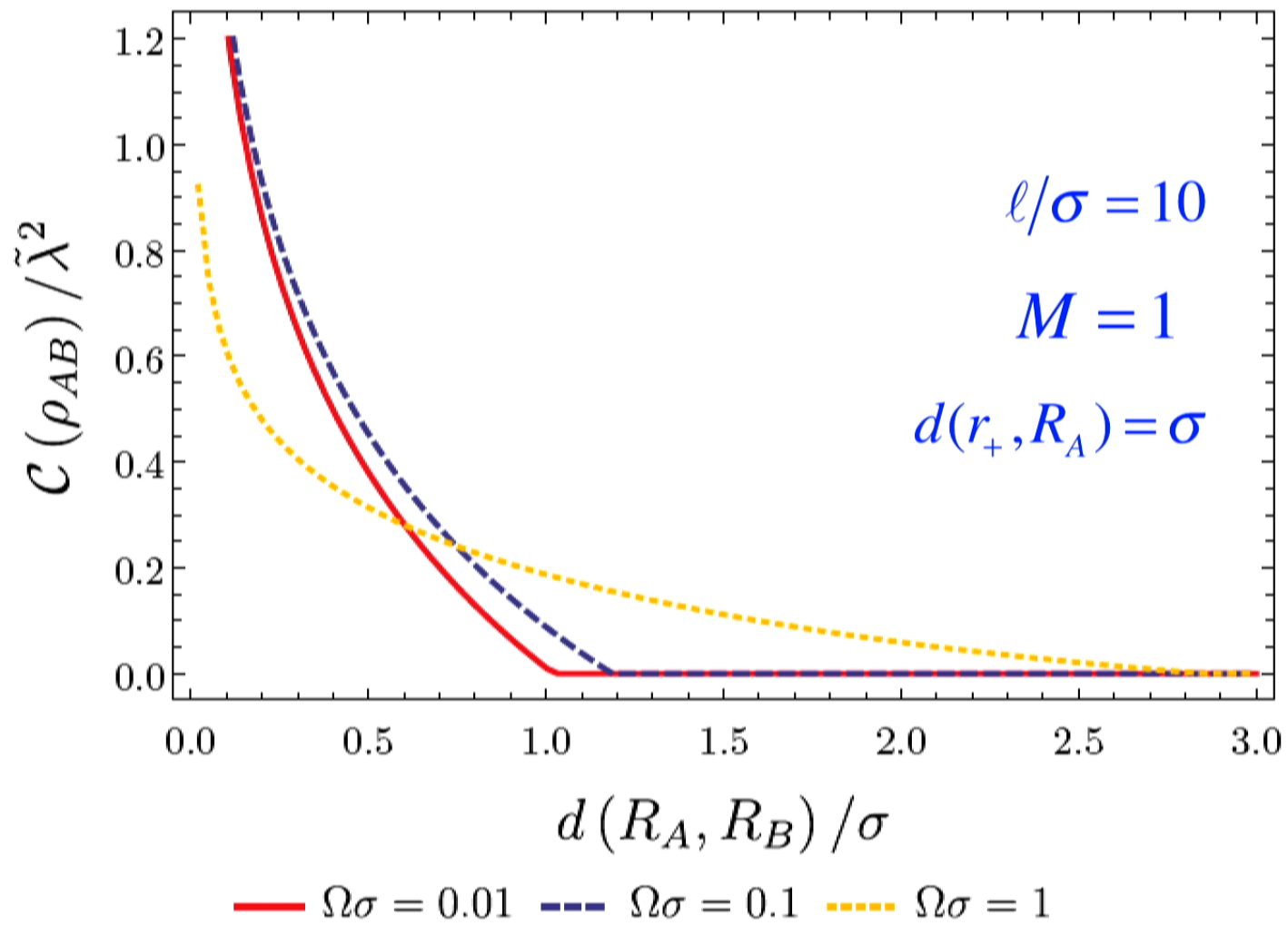
Harvesting Near Black Holes

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1712.10018

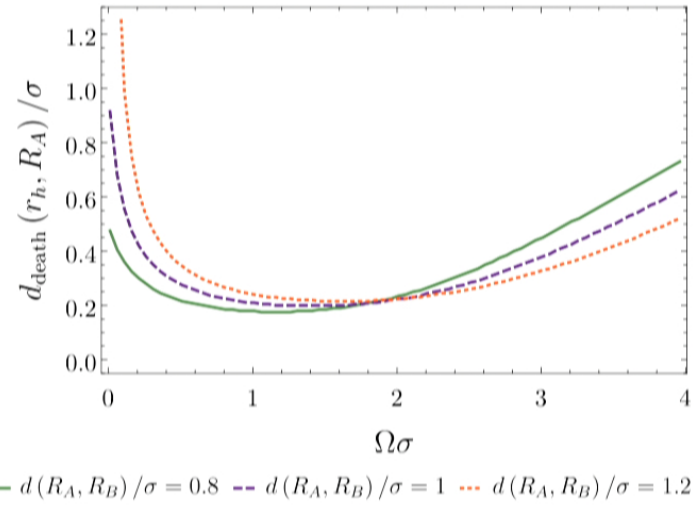
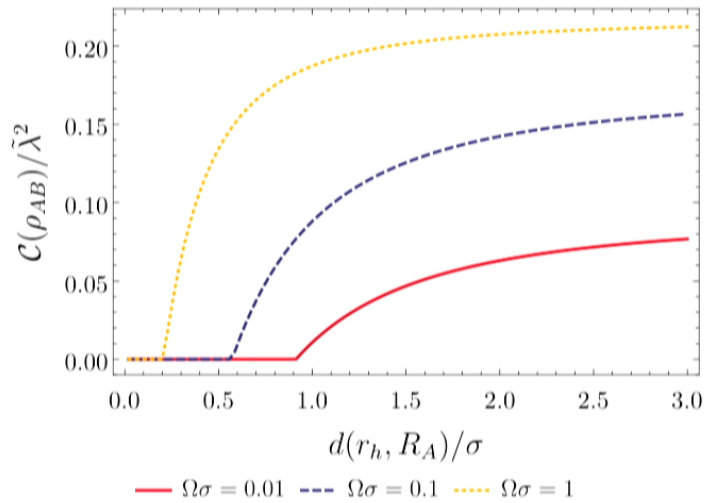


$$ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\phi^2$$

$$f(r) = \left(\frac{r^2}{\ell^2} - M \right)$$

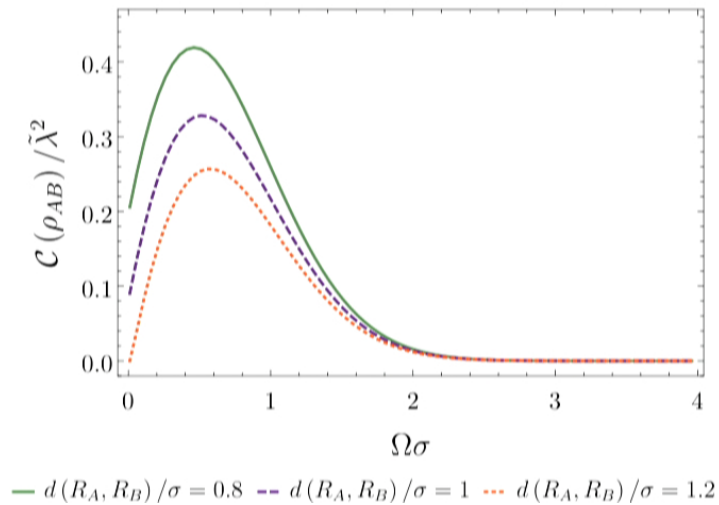


The Death Zone

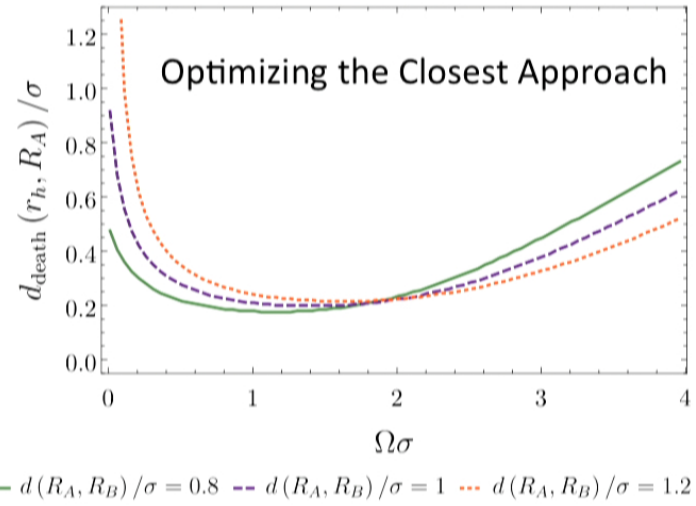
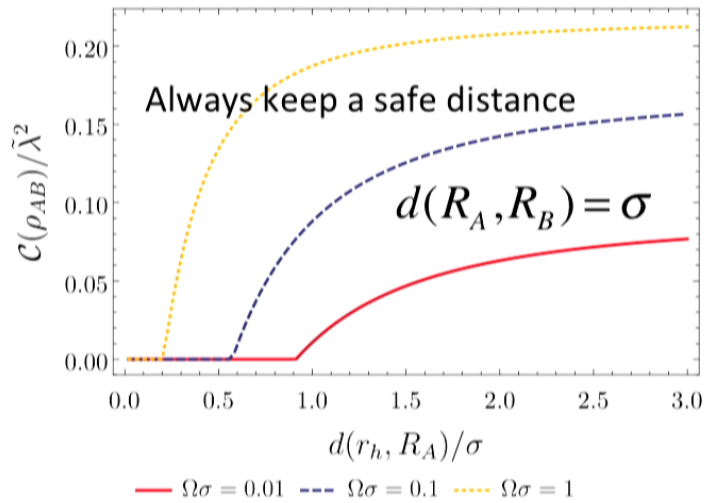


$$\ell/\sigma = 10$$

$$M = 1$$

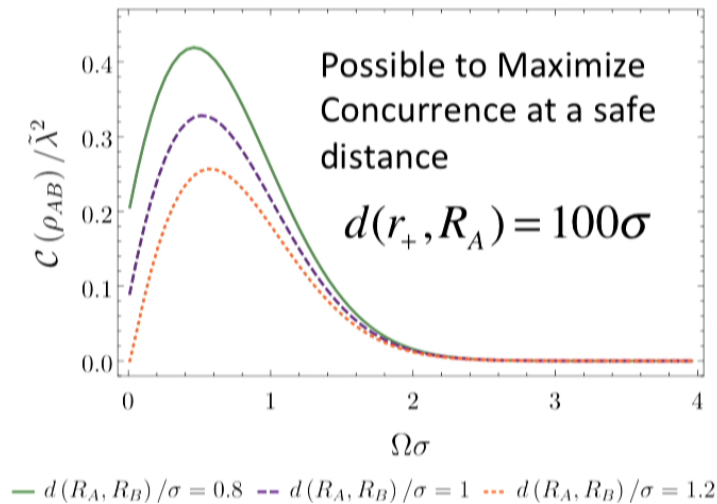


The Death Zone

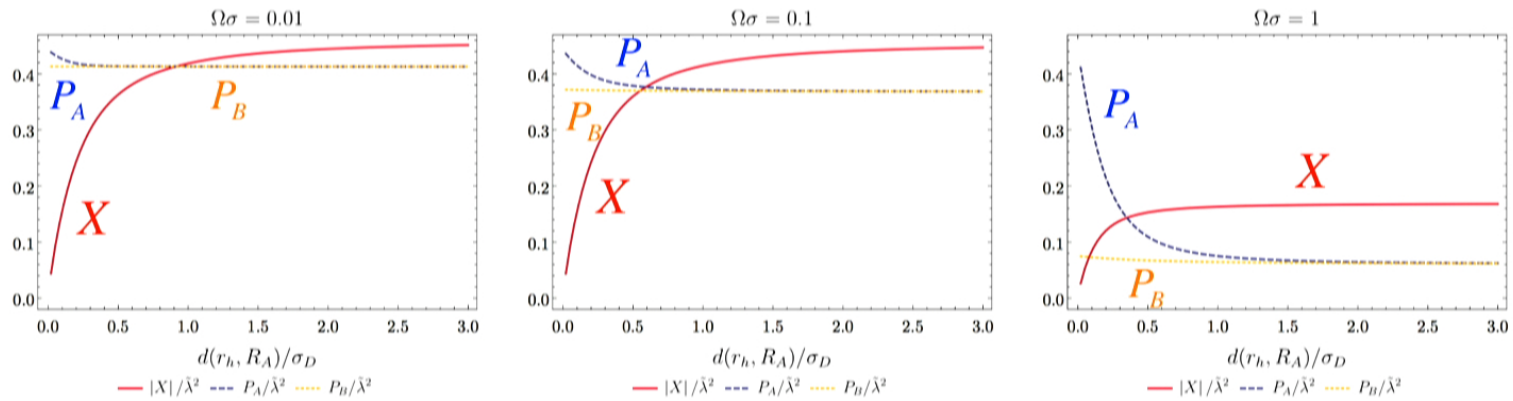


$\ell/\sigma = 10$

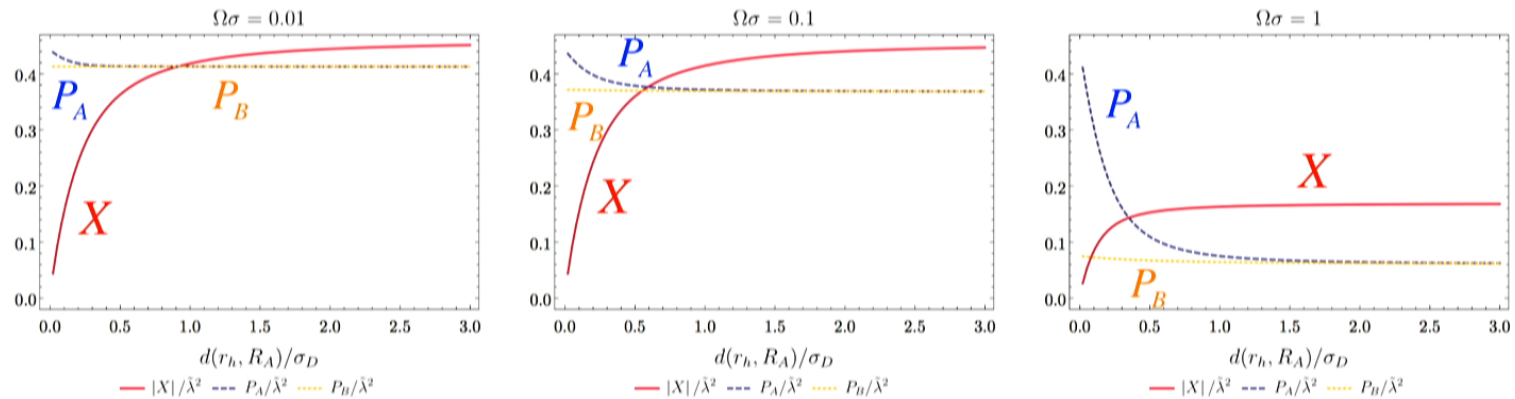
$M = 1$



Entanglement Inhibition

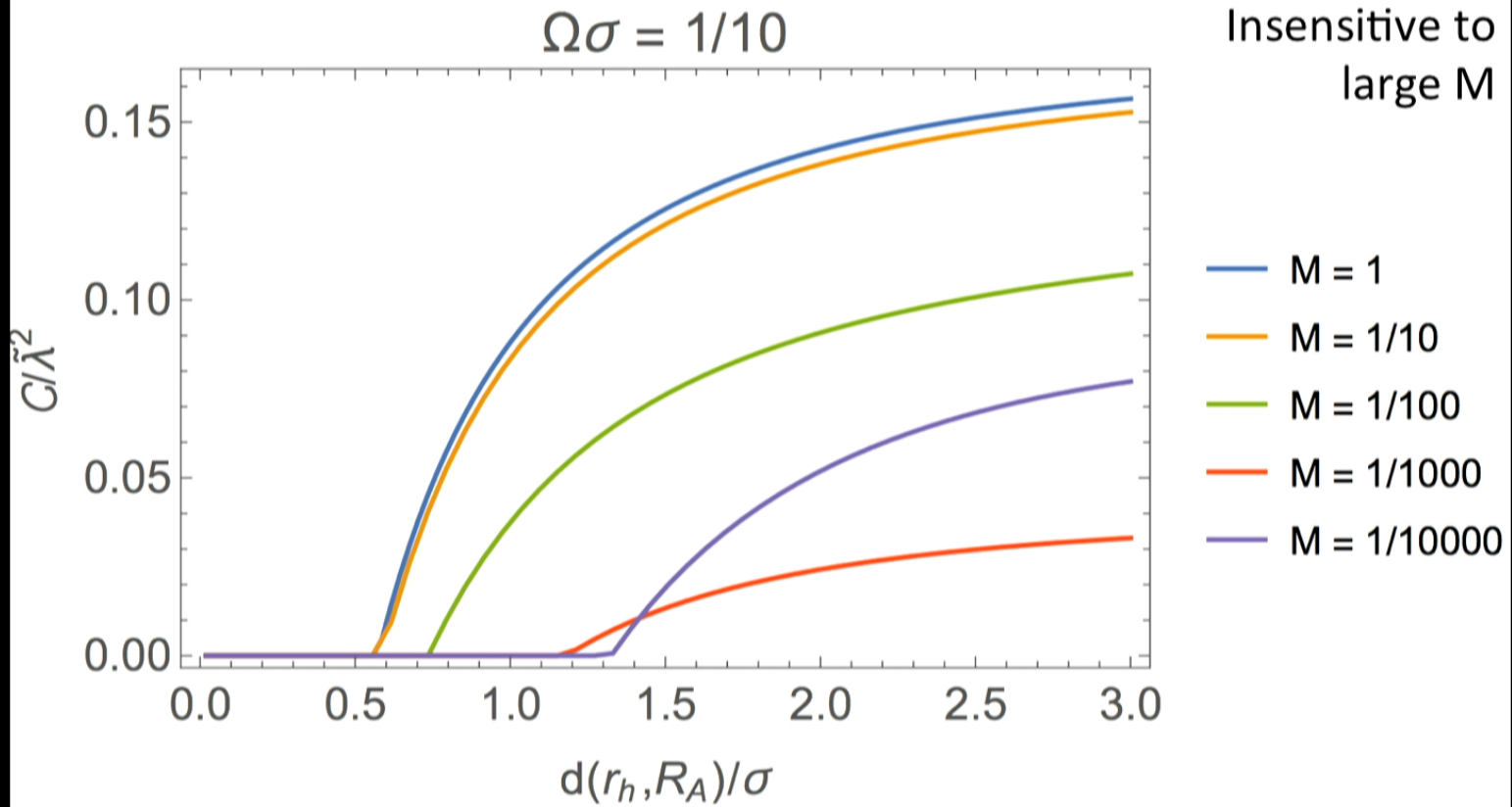


Entanglement Inhibition

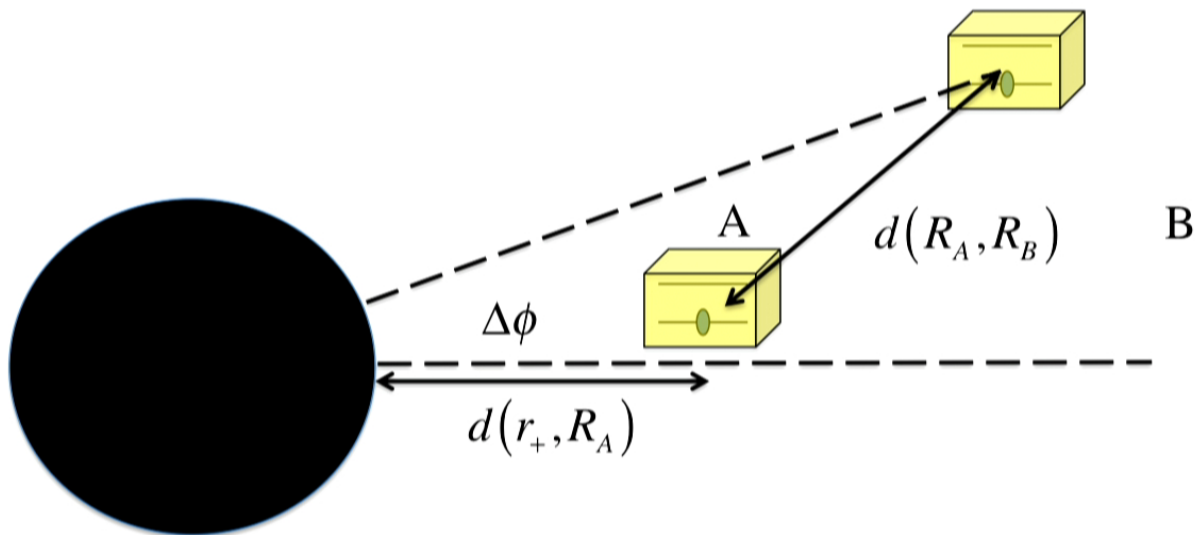


- Competition between increasing local excitations and decreasing non-local correlations
 - Hawking radiation \rightarrow excitation probability rises
 - Redshift effects \rightarrow erode correlations

Mass Dependence



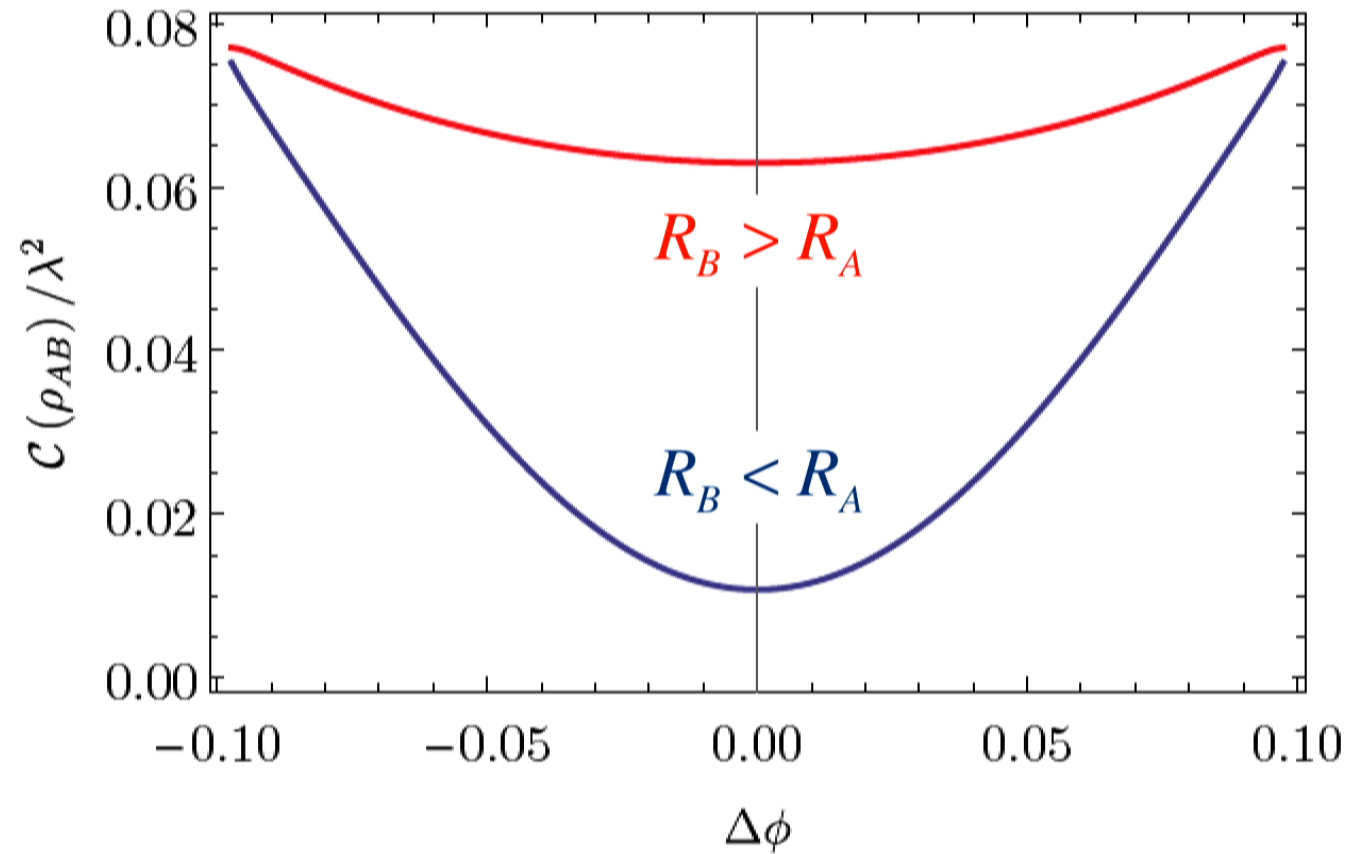
Angular Dependence



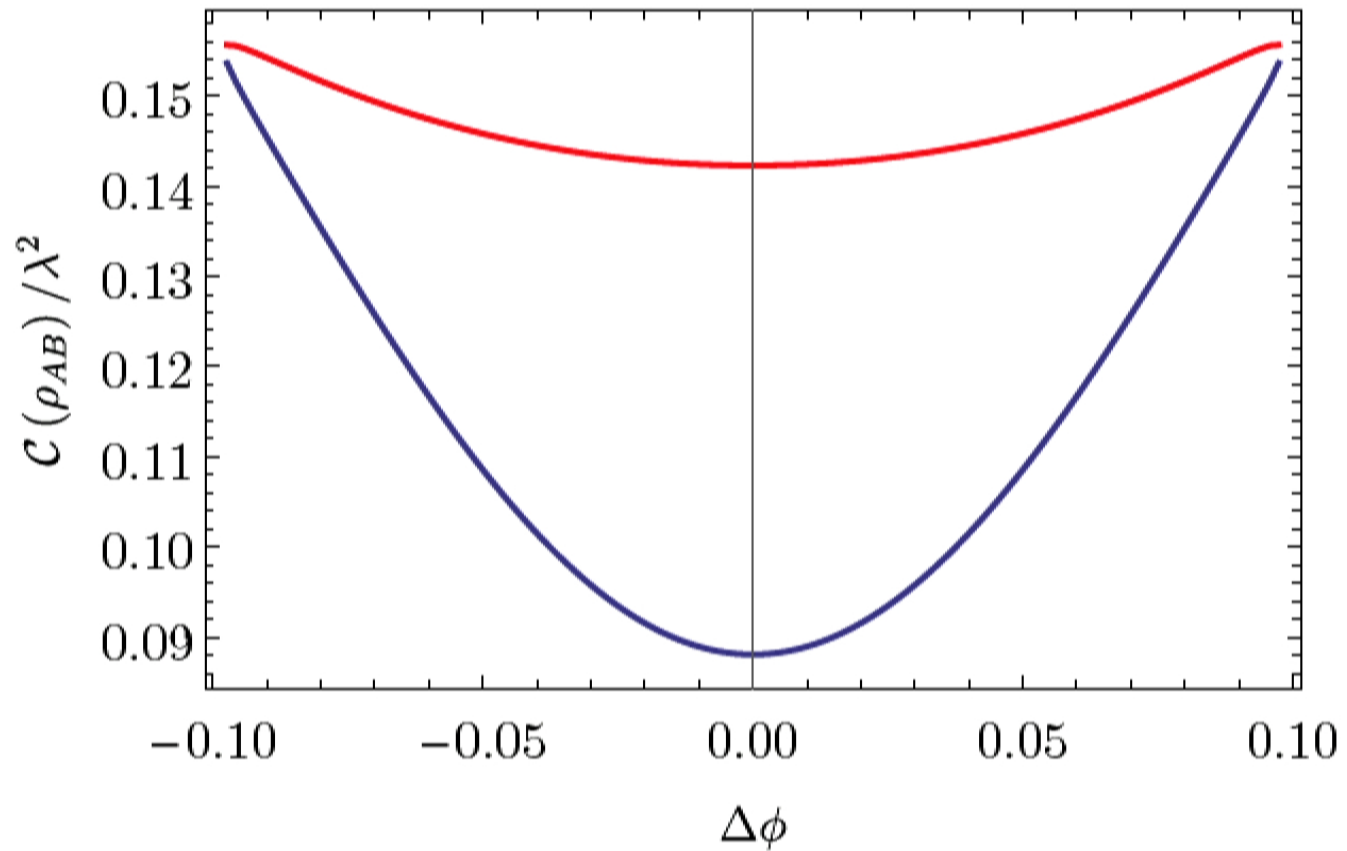
$$ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\phi^2$$

$$f(r) = \left(\frac{r^2}{\ell^2} - M \right)$$

$$\Omega\sigma = 0.01 \quad M = 1 \quad \ell = 10\sigma \quad d(r_+, R_A) = \sigma \quad d(R_A, R_B) = \sigma$$



$$\Omega\sigma = 0.1 \quad M = 1 \quad \ell = 10\sigma \quad d(r_+, R_A) = \sigma \quad d(R_A, R_B) = \sigma$$



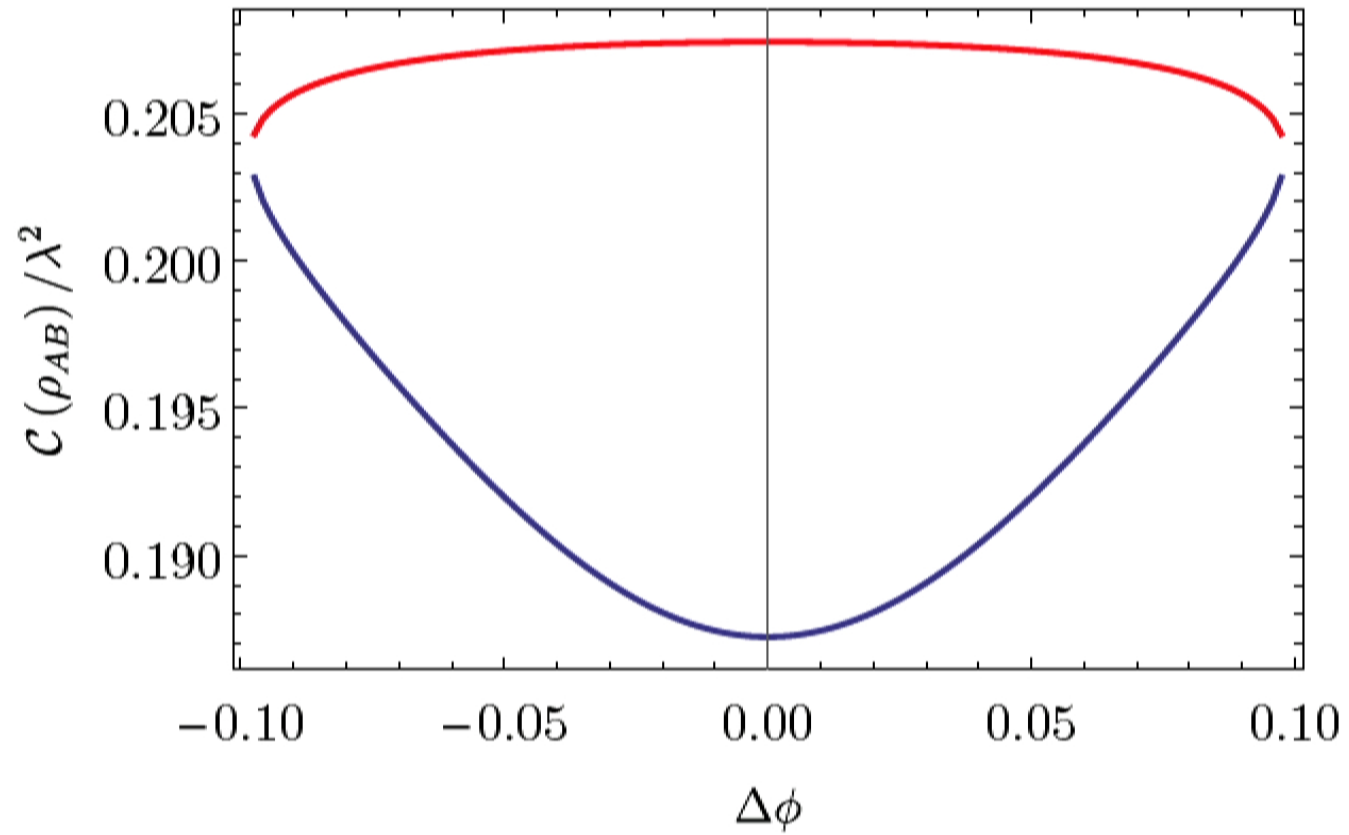
$$\Omega\sigma = 1.0$$

$$M = 1$$

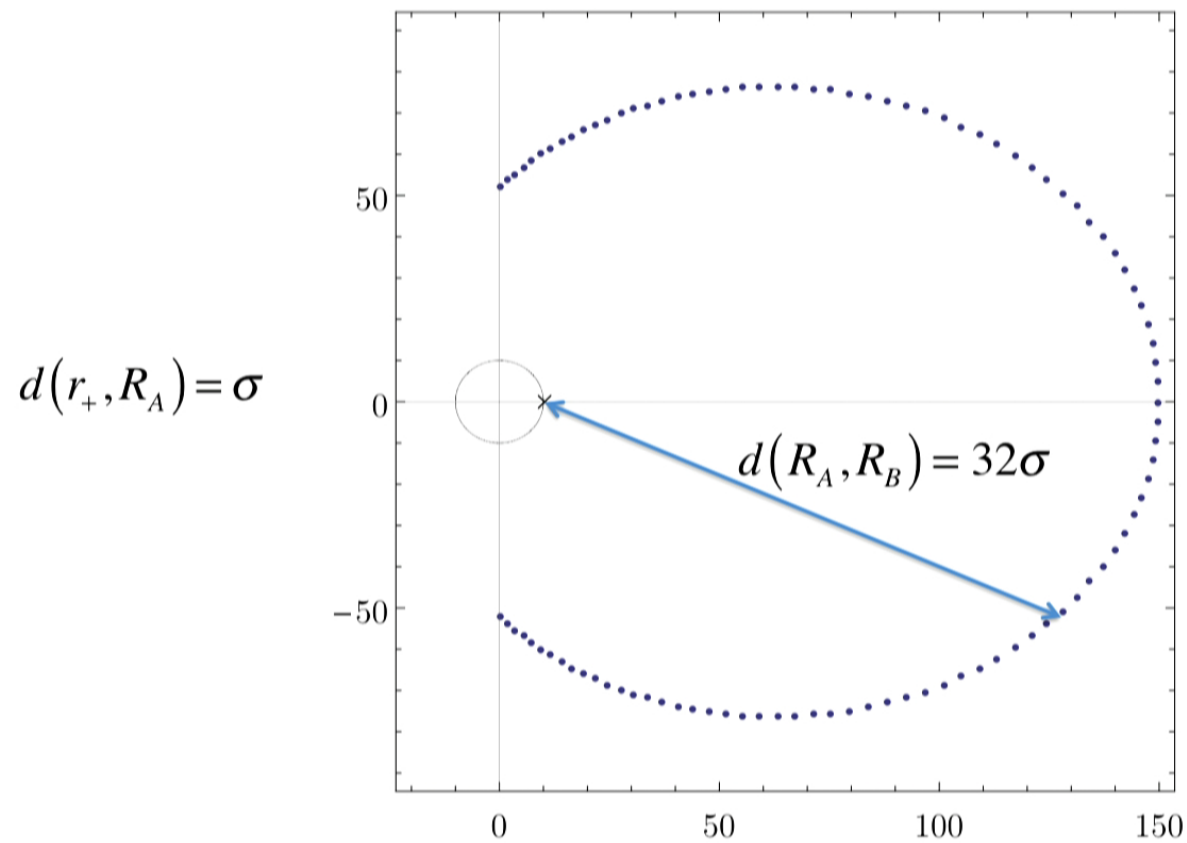
$$\ell = 10\sigma$$

$$d(r_+, R_A) = \sigma$$

$$d(R_A, R_B) = \sigma$$



Encompassing the Hole

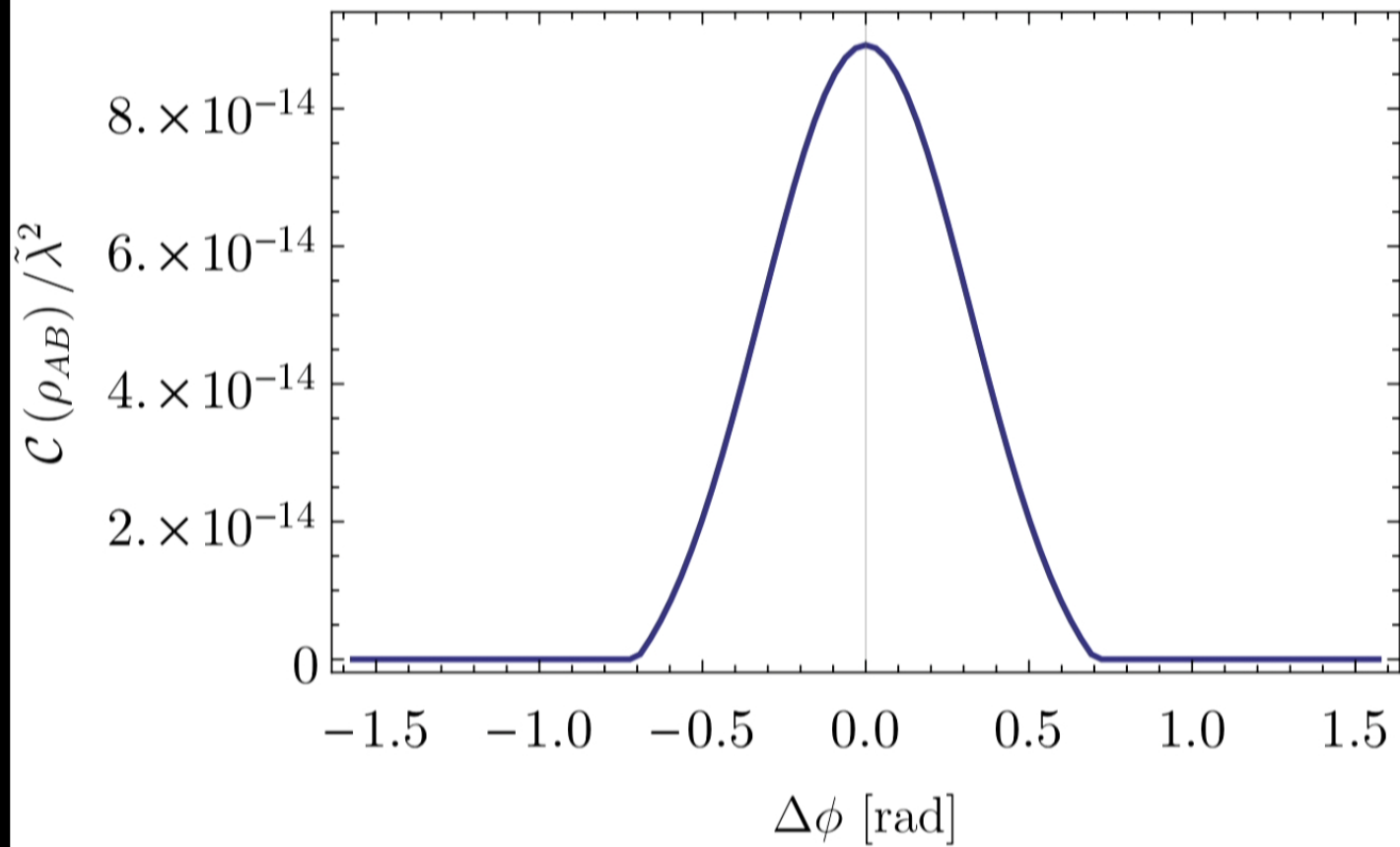


$$\Omega\sigma = 5.5$$

$$M = 1$$

$$\ell = 10\sigma$$

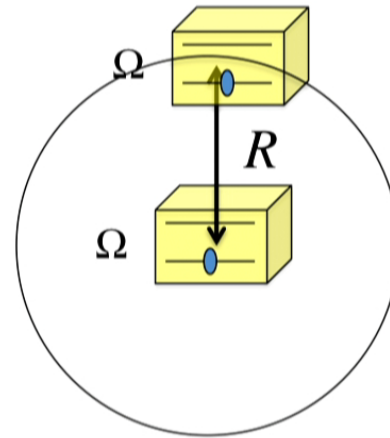
$$d(r_+, R_A) = \sigma \quad d(R_A, R_B) = 32\sigma$$



Results in 3+1 AdS

Ng/Mann/
Martin-Martinez
(to appear)

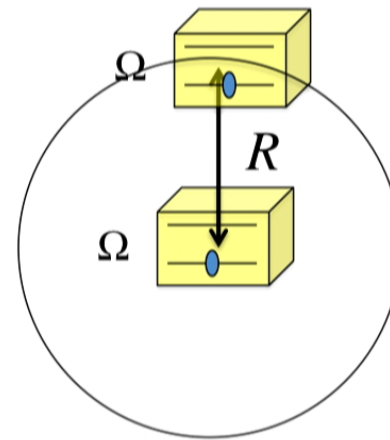
$$ds^2 = -\left(\frac{r^2}{\ell^2} + 1\right) dt^2 + \left(\frac{r^2}{\ell^2} + 1\right)^{-1} dr^2 + r^2 (d\theta^2 + \sin^2 \theta d\phi^2)$$



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$$\begin{aligned} r &= R \\ \theta &= \pi / 2 \\ t &= \tau \\ \phi &= \tau / \ell \end{aligned}$$

Geodesic circular orbit: redshift and angular velocity are completely independent of radius

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Switching Displacement

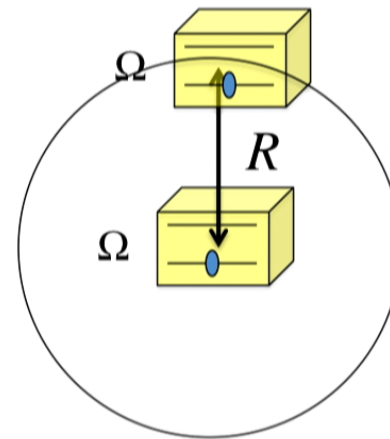
$$\tau_A = 0 \quad \tau_B = \Delta\tau$$

Switching Width

$$\sigma_A = \sigma_B = \sigma$$

Detector Gaps

$$\Omega_A = \Omega_B = \Omega$$



$$r = R$$

$$\theta = \pi / 2$$

$$t = \tau$$

$$\phi = \tau / \ell$$

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Switching Displacement

$$\tau_A = 0 \quad \tau_B = \Delta\tau$$

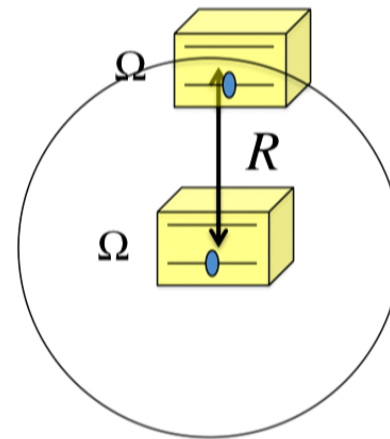
Switching Width

$$\sigma_A = \sigma_B = \sigma$$

Detector Gaps

$$\Omega_A = \Omega_B = \Omega$$

Calibrated wrt
coordinate
time



$$r = R$$

$$\theta = \pi / 2$$

$$t = \tau$$

$$\phi = \tau / \ell$$

Geodesic circular orbit: redshift and angular velocity are completely independent of radius

Correlation Relations

For Spacelike Separated Detectors

For any
detector
motion!

$$X = -\frac{1}{2} [C_{BA}(-\Omega_B, \Omega_A) + C_{AB}(-\Omega_A, \Omega_B)]$$

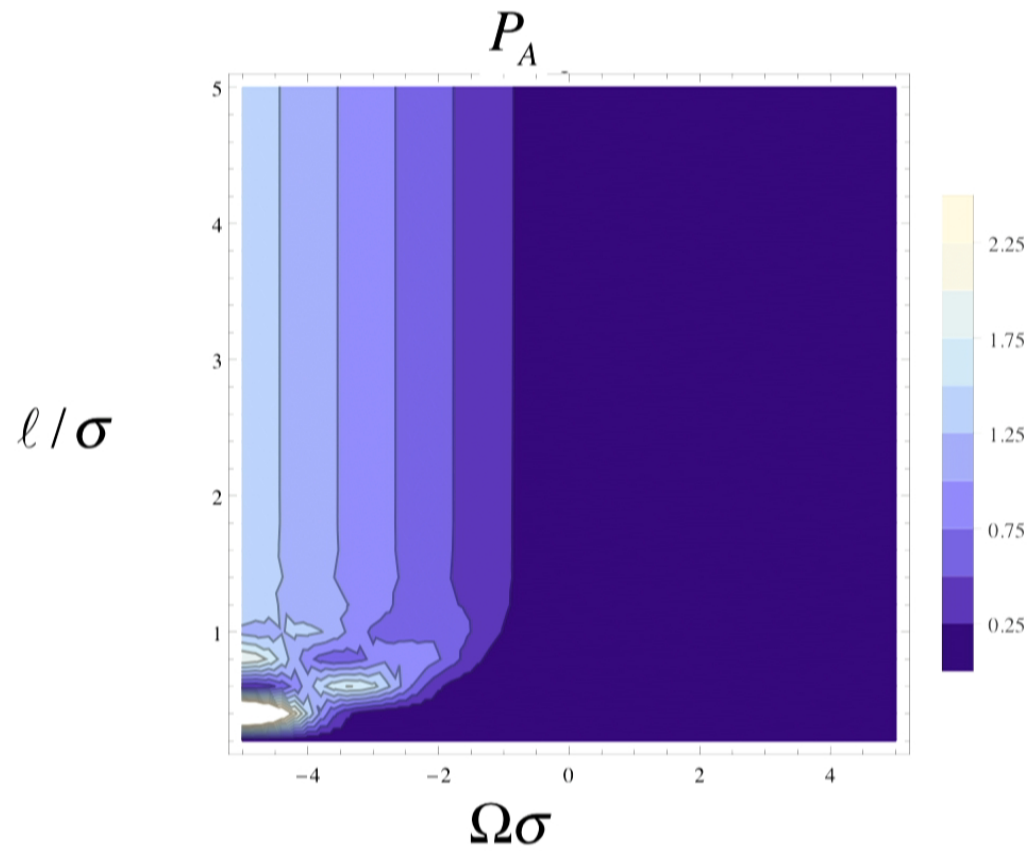
Non-local Correlations

Local Correlations

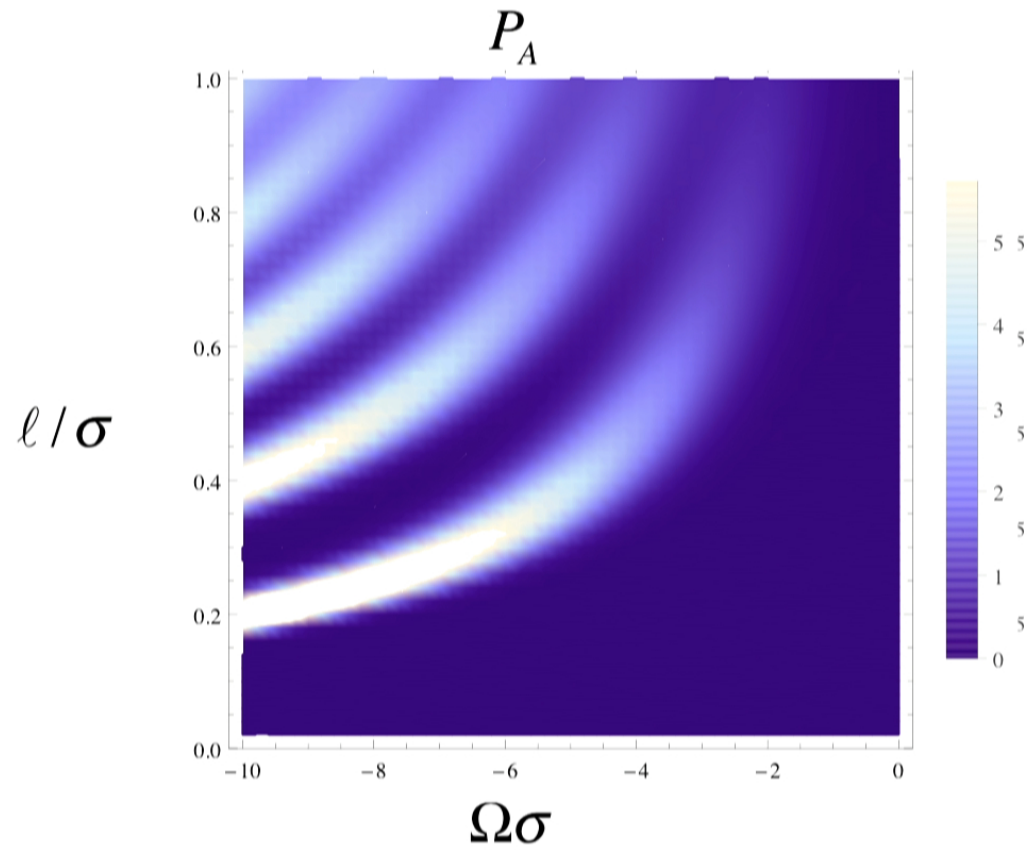
$$C_{AB} = \lambda^2 \sum_n \frac{\pi}{2n+2} \varphi_{2n+2}(x_B) \varphi_{2n+2}(x_A) \hat{\chi}_B^*(2n+2+\Omega_B) \hat{\chi}_A(2n+2+\Omega_A)$$

$$X = \lambda^2 \sum_n \frac{\pi}{2n+2} \varphi_{2n+2}(x_B) \varphi_{2n+2}(x_A) \hat{\chi}_B^*(2n+2+\Omega_B) \hat{\chi}_A(2n+2+\Omega_A)$$

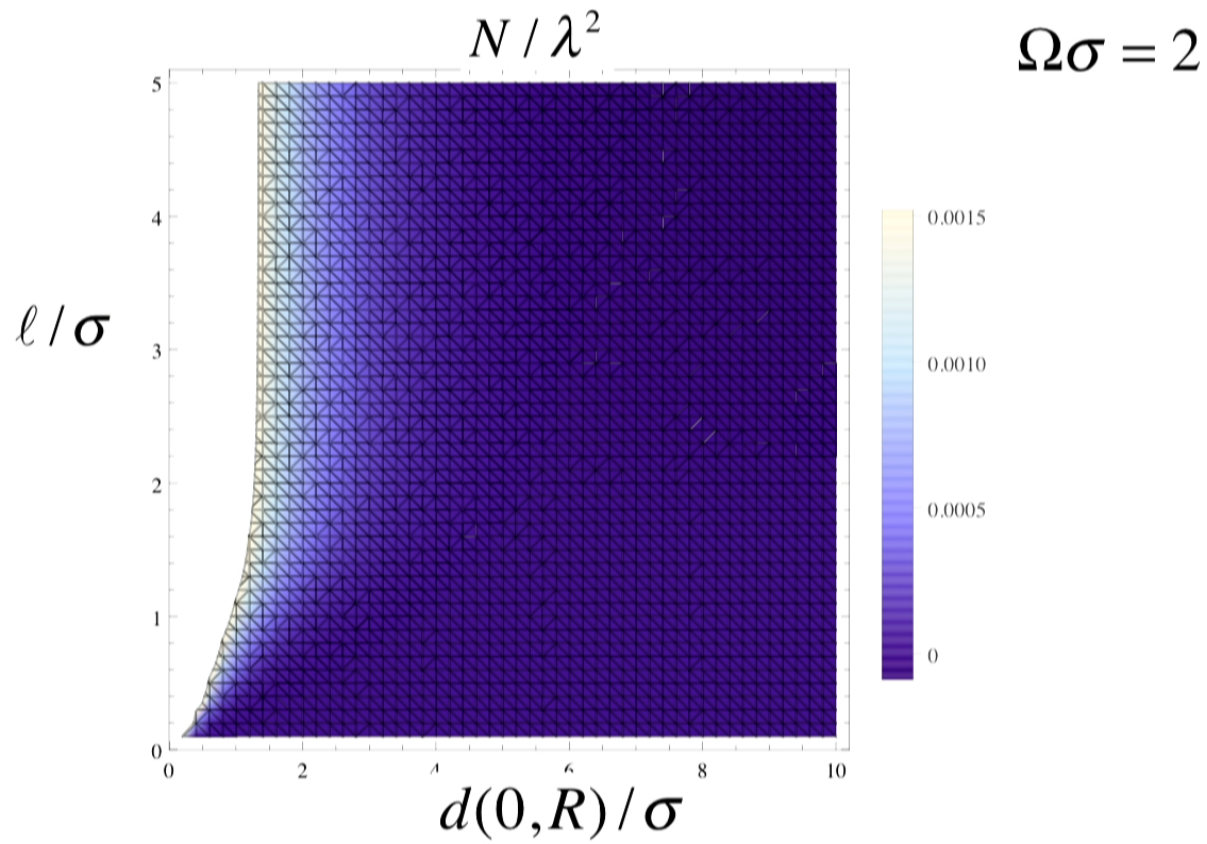
Detector Excitation



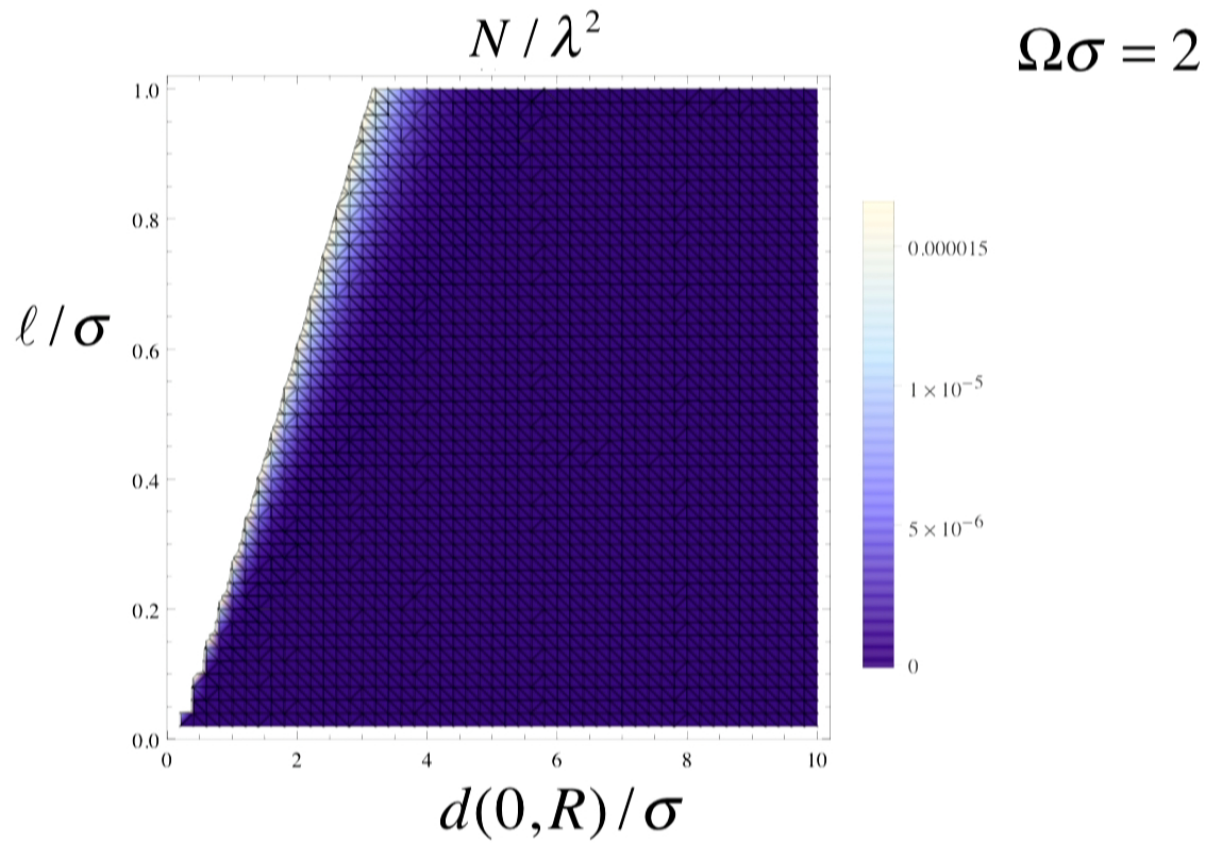
Detector Excitation



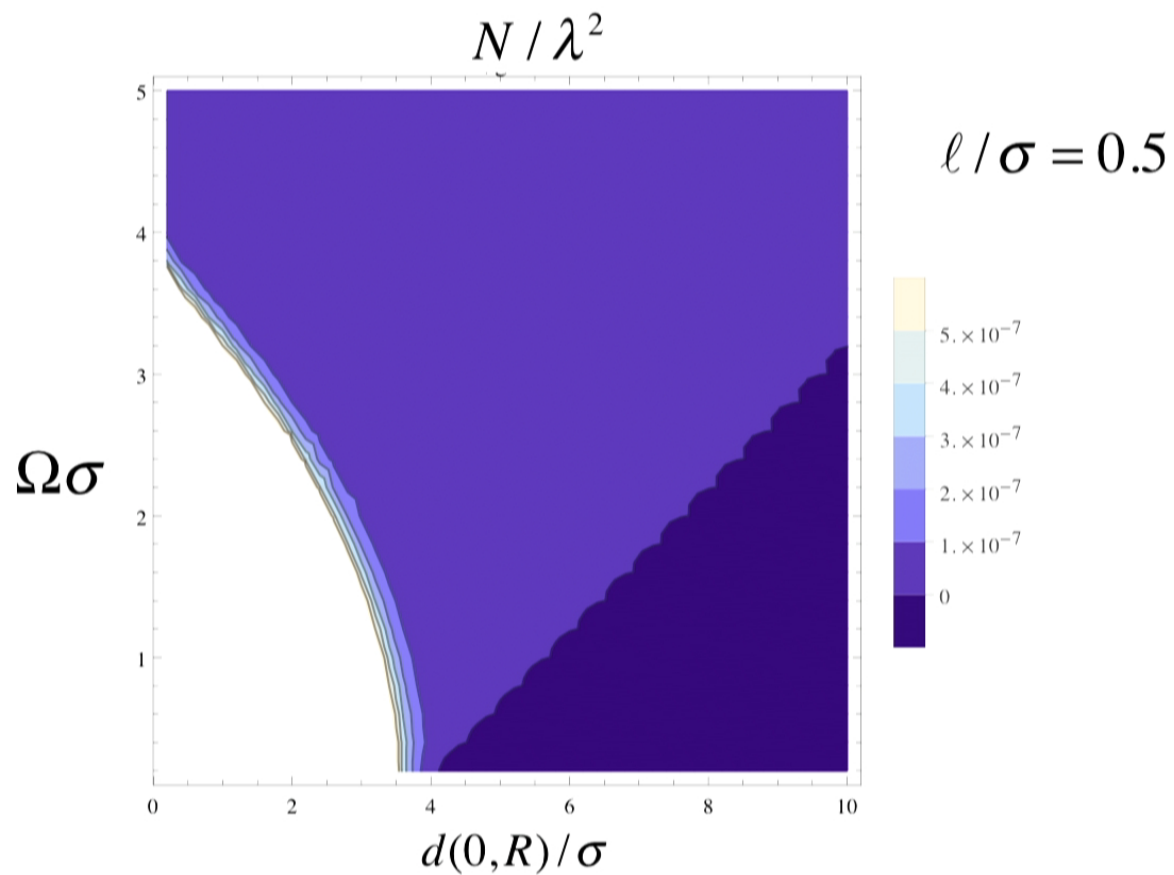
Negativity



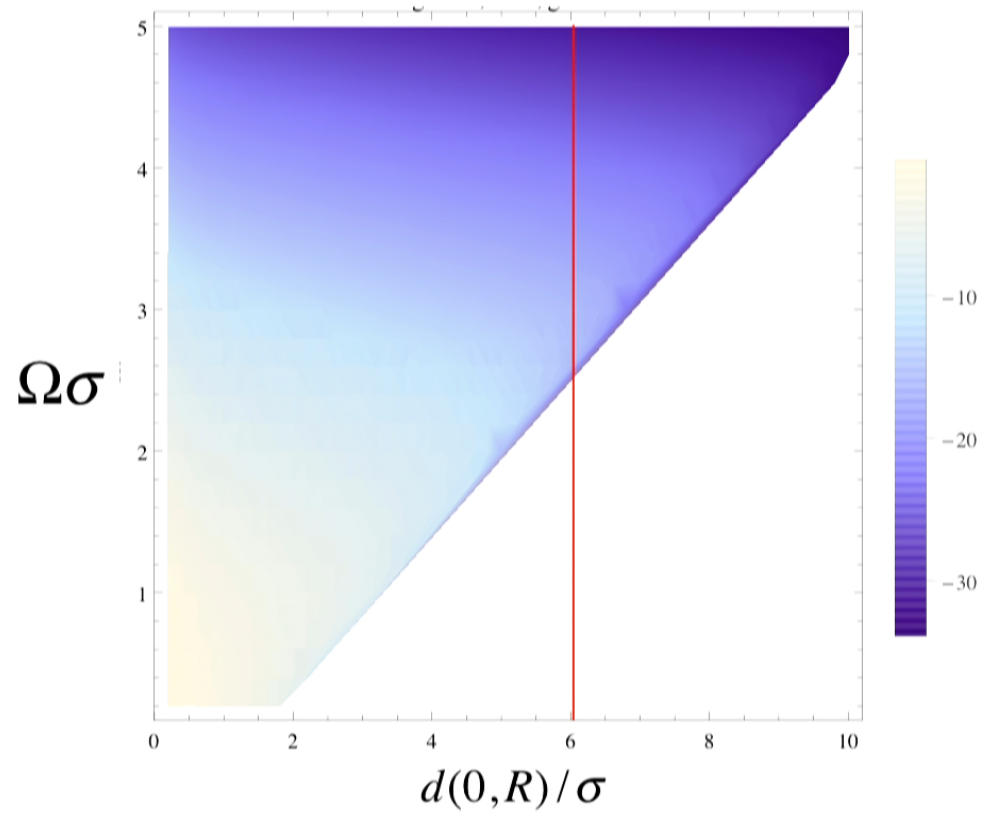
Negativity



Gap Dependence

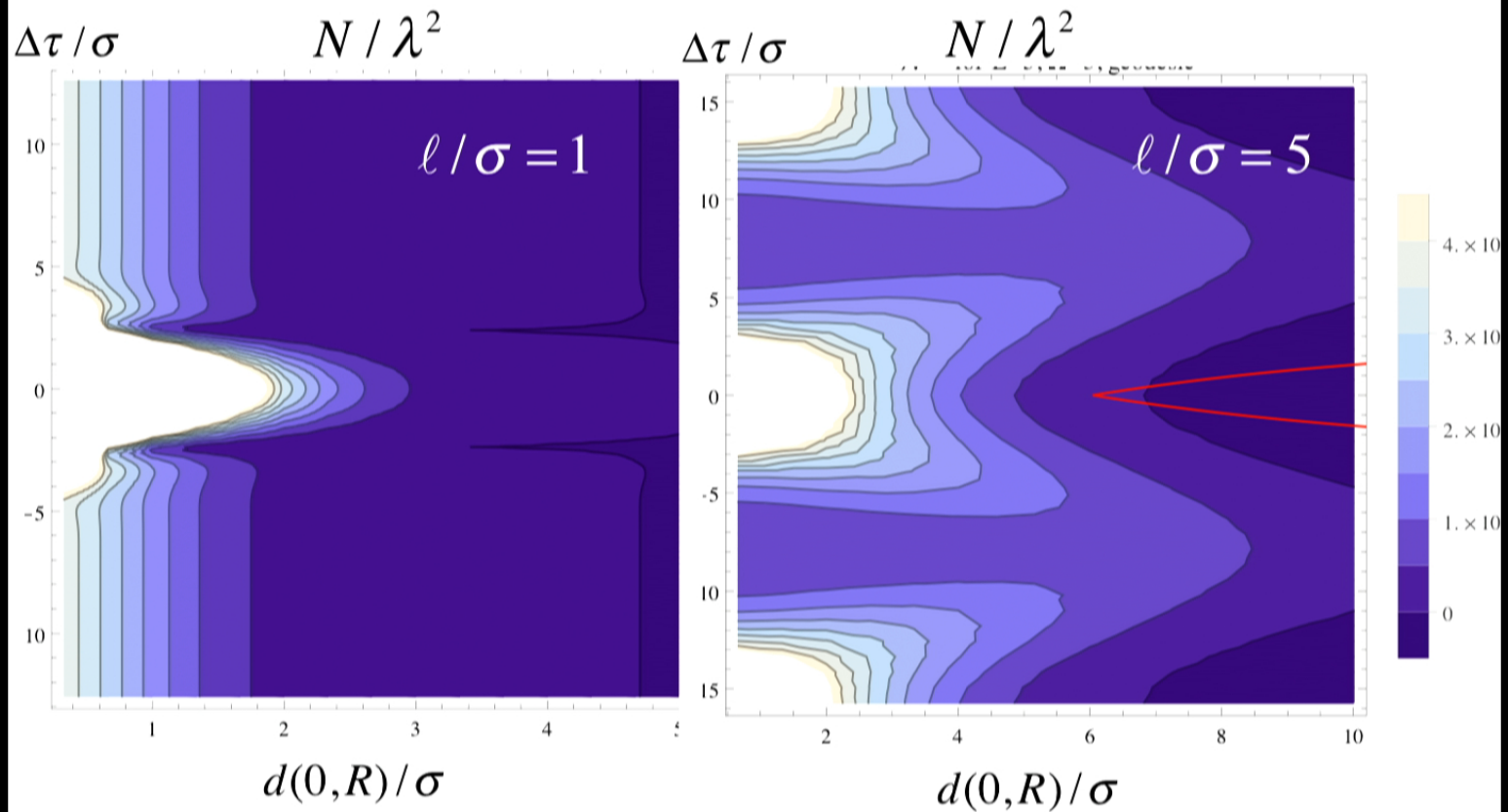


Gap Dependence

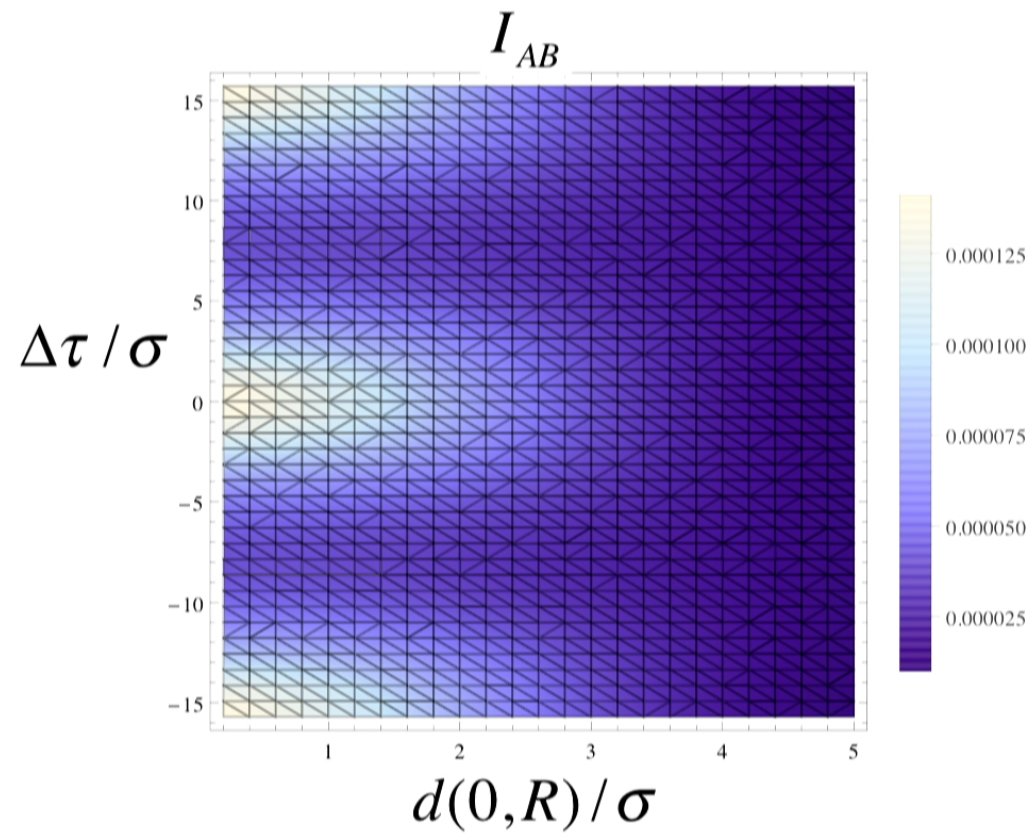


Time-Shift Dependence

$$\Omega\sigma = 3$$



Mutual Information



Summary

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 - New operational means of probing the vacuum structure of spacetime

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- Black Holes Inhibit Entanglement
 - Competition between enhanced local excitations and redshift erosion of non-local correlations