

Title: Asymptotic safety of gravity and matter

Date: Nov 23, 2017 02:30 PM

URL: <http://pirsa.org/17110042>

Abstract:

Compatibility of asymptotic safety with UV-completions of matter theories may constrain the underlying microscopic dynamics of quantum gravity. Within truncated RG-flows, a weak-gravity bound originates from the loss of quantum scale-invariance in the matter system. Further constraints could arise when linking Planck-scale to electroweak-scale dynamics. Within the constrained region, gravitationally induced scale-invariance could UV-complete the Standard Model, and moreover explain free parameters such as fermion masses and gauge couplings.

Asymptotic safety of gravity and matter

Aaron Held

Institut für Theoretische Physik, Universität Heidelberg



1711.02949 (Astrid Eichhorn, AH & Christof Wetterich)
1707.01107, to appear in PLB (Astrid Eichhorn & AH)
PRD 96 (2017), 086025 (Astrid Eichhorn & AH)
PRD 94 (2016), 104027 (Astrid Eichhorn, AH & Jan M Pawłowski)



Quantum Gravity Seminar, Perimeter Institute for Theoretical Physics
November 23rd 2017



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

classical General Relativity

$$\underbrace{G_{\mu\nu}} = 8\pi G_N \underbrace{T_{\mu\nu}}$$

spacetime
tells matter how to move

&

matter
tells spacetime how to curve

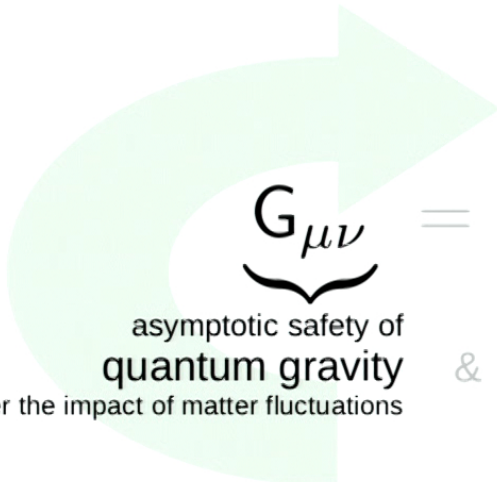
? quantum General Relativity ?

$$\underbrace{G_{\mu\nu}} = \underbrace{8\pi G_N T_{\mu\nu}}$$

asymptotic safety of
quantum gravity
under the impact of matter fluctuations

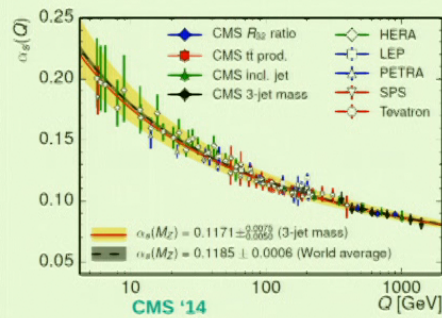
&

asymptotic safety of
matter
induced by spacetime fluctuations


$$\underbrace{G_{\mu\nu}}_{\substack{\text{asymptotic safety of} \\ \text{quantum gravity} \\ \text{under the impact of matter fluctuations}}} = \underbrace{8\pi G_N T_{\mu\nu}}_{\substack{\text{asymptotic safety of} \\ \text{matter} \\ \text{induced by spacetime fluctuations}}} \quad \&$$

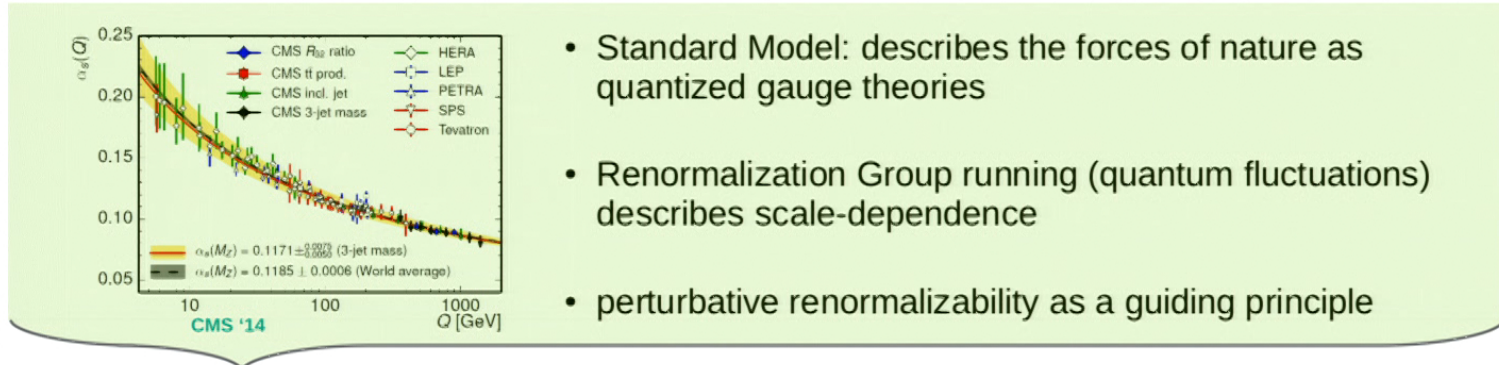
1. Asymptotic safety and gravity

Scales in fundamental physics

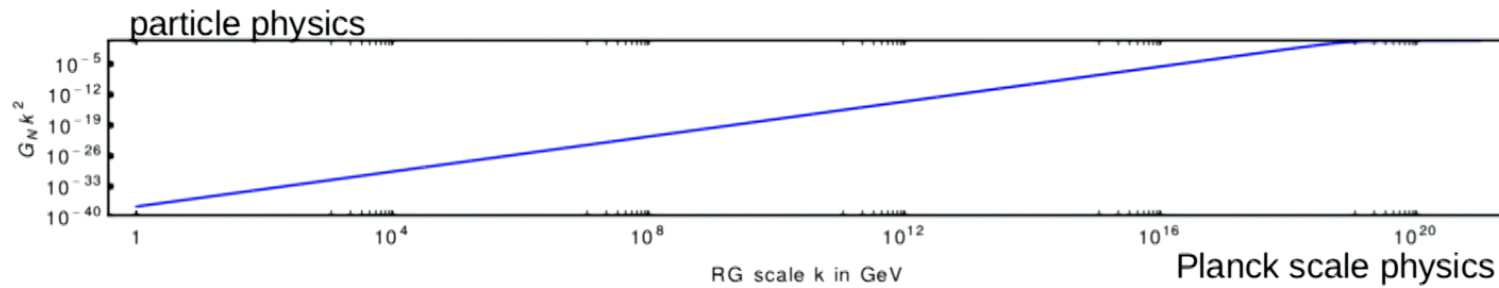


- Standard Model: describes the forces of nature as quantized gauge theories
- Renormalization Group running (quantum fluctuations) describes scale-dependence
- perturbative renormalizability as a guiding principle

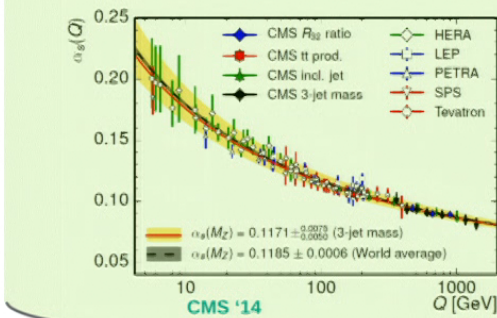
Scales in fundamental physics



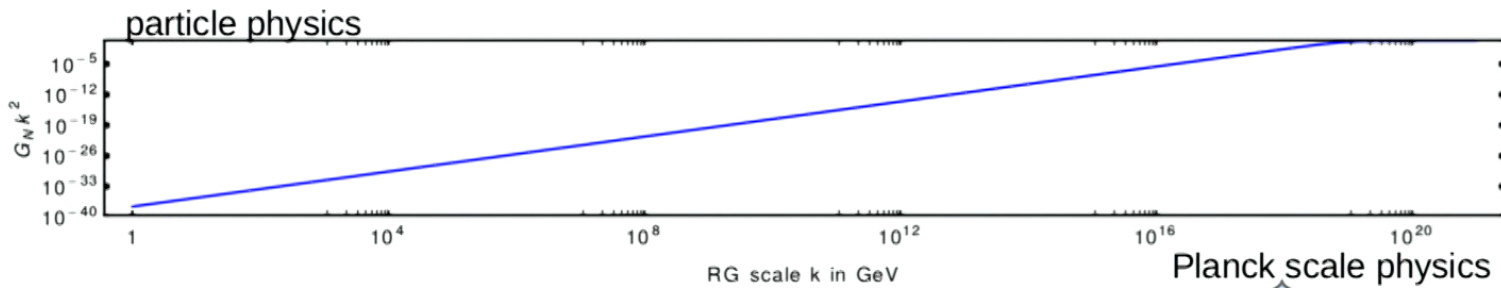
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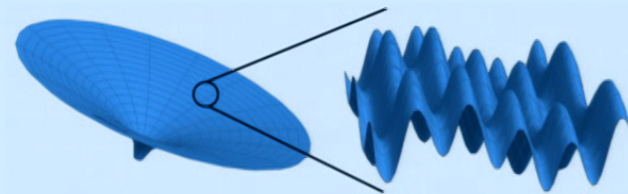


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- crucial at scales where Newton constant $\bar{G}_N \sim 1$
- task: quantized description of spacetime
- perturbatively non-renormalizable $[\bar{G}_N] = -2$

G. 't Hooft and M. J. G. Veltman, '74
S. Deser and P. van Nieuwenhuizen, '74
M. H. Goroff and A. Sagnotti, '81



2

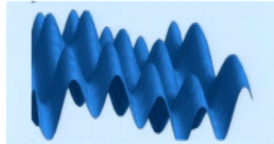
Quantum field theory of the metric

- To Do:
- General relativity is a **perturbatively non-renormalizable** quantum field theory.
 - Can it still be quantized as a **non-perturbatively renormalizable** quantum field theory, by weighing classical scaling against quantum fluctuations?

$$[\bar{G}_N] = -2$$

Canonical dimension

&



Quantum fluctuations

=

**quantum
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path-integral for gravity
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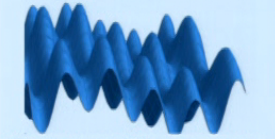
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quantum fluctuations generate
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infinite dimensional
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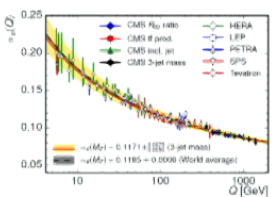
path-integral for gravity

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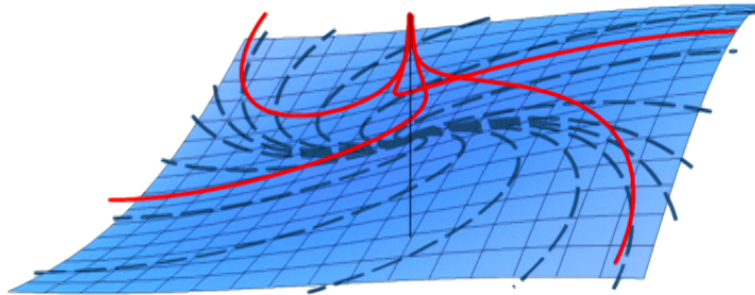
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Asymptotic freedom: perturbative renormalizability as a guiding principle

Asymptotic safety conjecture

Weinberg '76

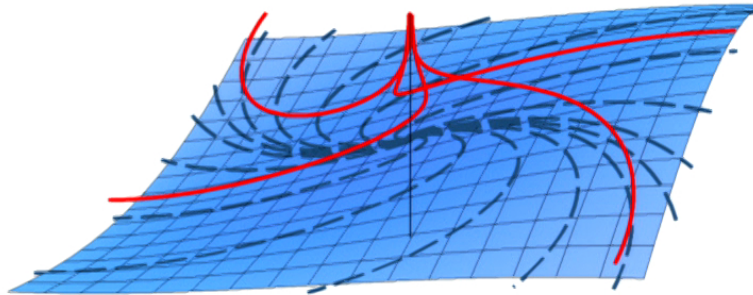


- existence of a UV fixed point for metric field theory (**fundamental theory**)

$$\beta_{\lambda_i} = 0 \quad \forall \lambda_i$$

Asymptotic safety conjecture

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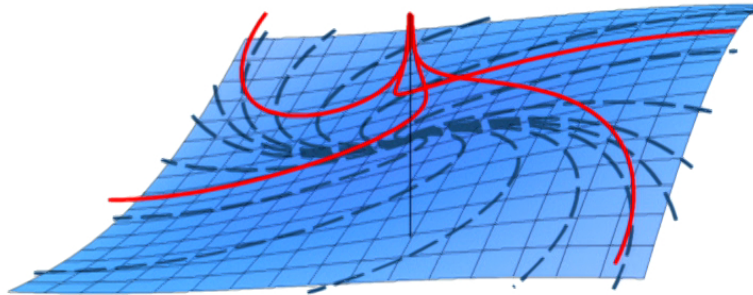
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$$\theta_k = - \left[\text{ev} \left(\frac{\partial \beta_{\lambda_i}}{\partial \lambda_j} \right) \right]_k > 0$$

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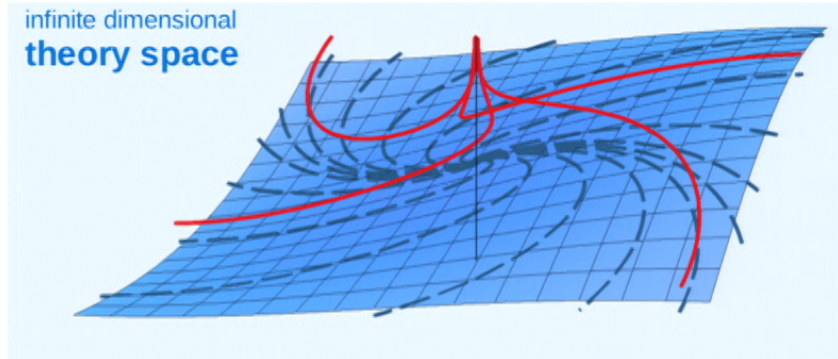
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infinite dimensional theory space

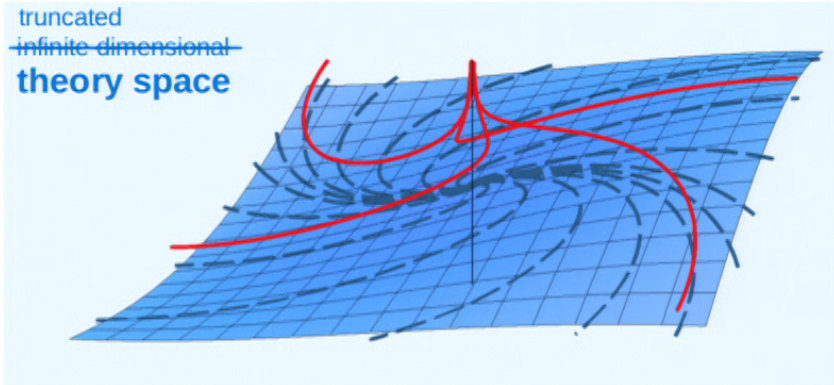
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4

Asymptotic safety conjecture

Weinberg '76

truncated
~~infinite dimensional~~
theory space



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Search for fixed points by use of **truncations** of the functional Renormalization Group

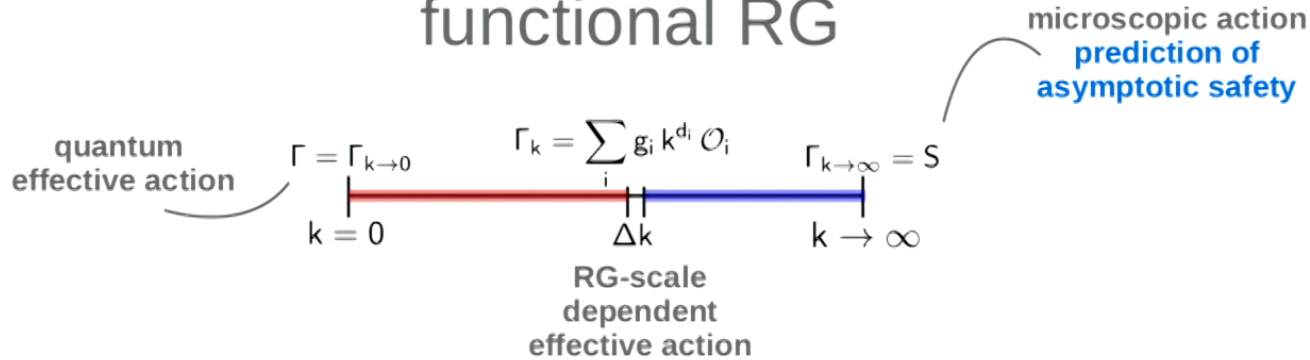
Wetterich '93

truncated ~~infinite dimensional~~ theory space

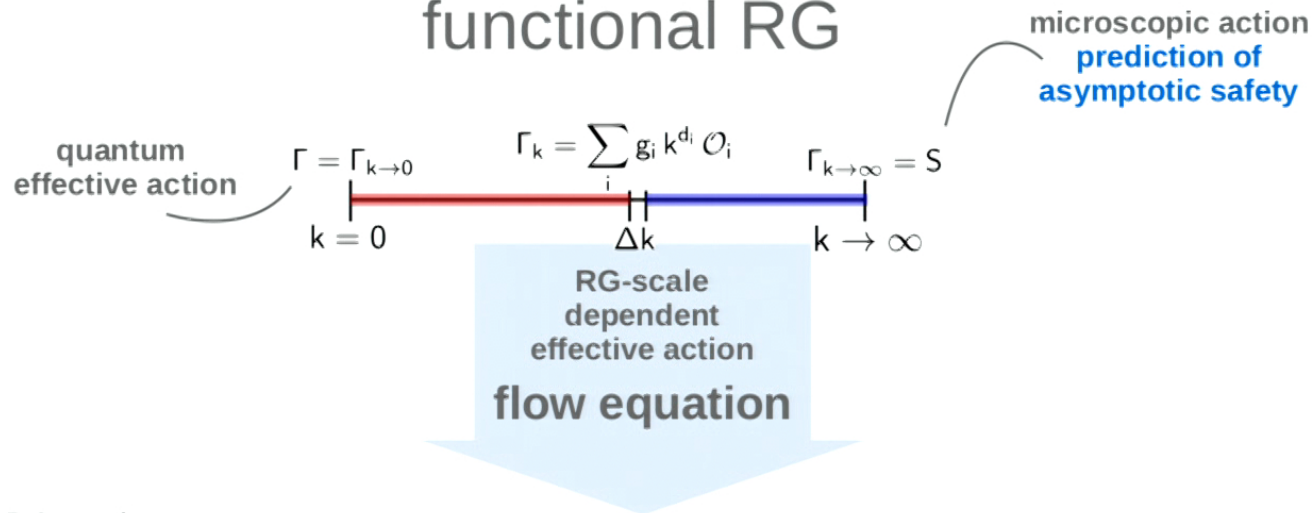
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functional RG



functional RG

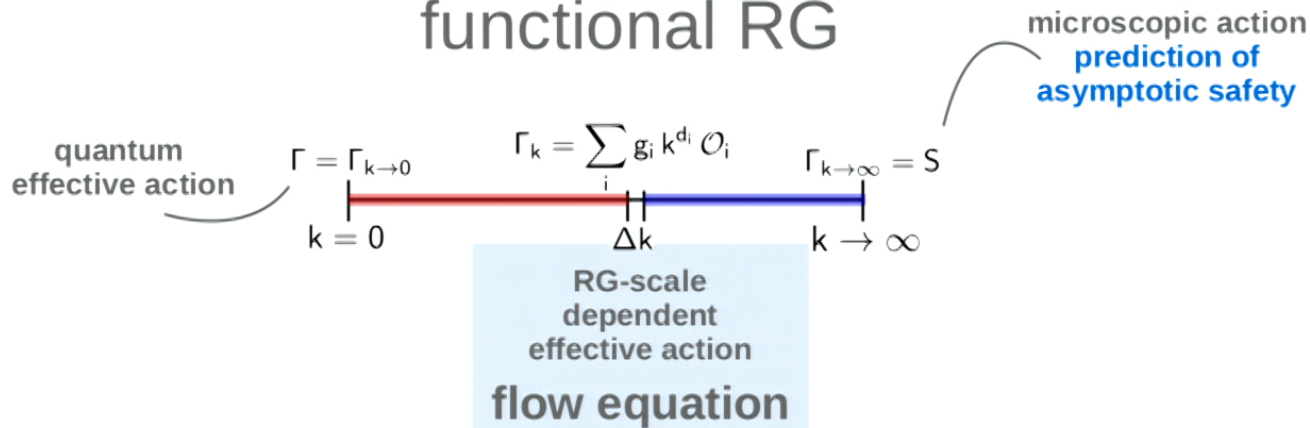


RG-scale dependent effective action

$$k \partial_k \Gamma_k = \frac{1}{2} \text{Tr} \left(\Gamma_k^{(2)}[\Phi] + R_k \right)^{-1} k \partial_k R_k$$

Wetterich '93

functional RG



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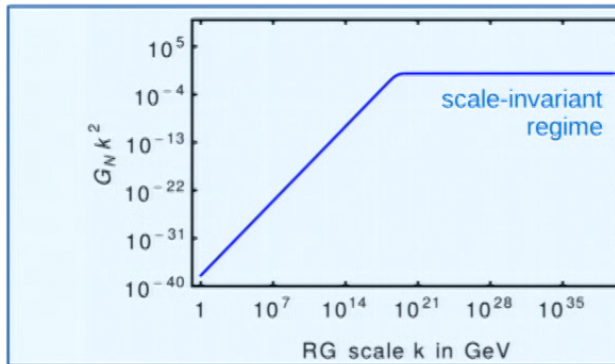
allows for projections on beta functions

$$k \partial_k \Gamma_k = \sum_i (\beta_i + d_i g_i) k^{d_i} \mathcal{O}_i \xrightarrow{\text{projection}} \beta_i$$

Asymptotic safety: truncations

Weinberg '76
Reuter '96

1-dimensional
truncation



$$S_{\text{trunc.}} = -\frac{1}{16\pi\bar{G}_N} \int d^4x \sqrt{g} R$$

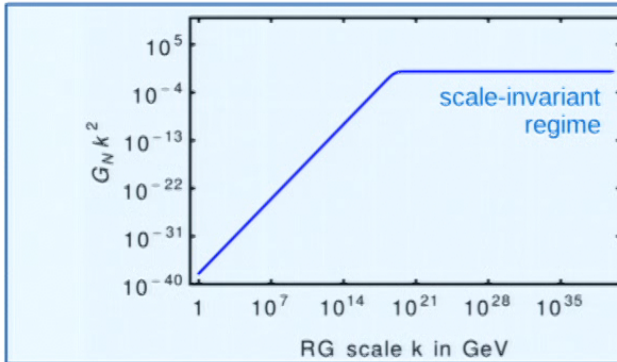
$$\beta_{G_N} = \underbrace{2}_{\text{dimensional}} G_N - \underbrace{\frac{23}{3\pi}}_{\text{quantum}} G_N^2 + \dots \quad \text{Codello, Percacci, Rahmede '08}$$

work with dimensionless couplings $G_N = \bar{G}_N k^2$

Asymptotic safety: truncations

Weinberg '76
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1-dimensional
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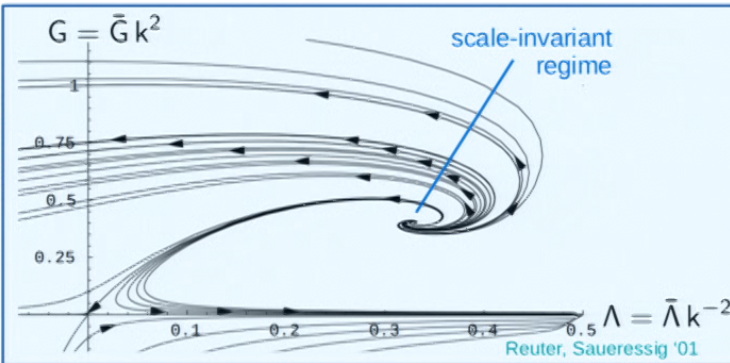


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2-dimensional
truncation

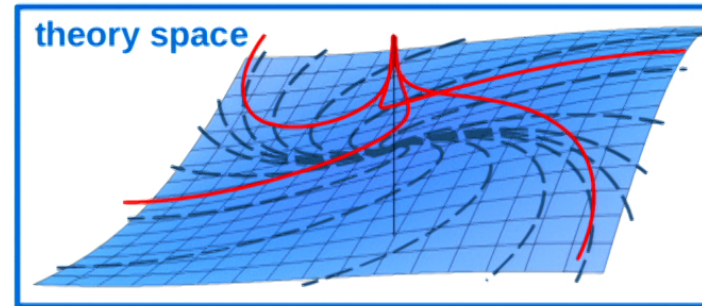


$$S_{\text{trunc.}} = -\frac{1}{16\pi\bar{G}} \int d^4x \sqrt{g} [R - 2\bar{\Lambda}]$$

two UV-attractive directions

Asymptotic safety: truncations

Weinberg '76
Reuter '96



$$f(R)$$

⋮

$$\lambda_4 R^4$$

$$\lambda_3 R^3$$

$$\sigma_k C_{\mu\nu}^{\rho\sigma} C_{\rho\sigma}^{\kappa\lambda} C_{\kappa\lambda}^{\mu\nu} + \text{more}$$

$$\lambda_2 R^2$$

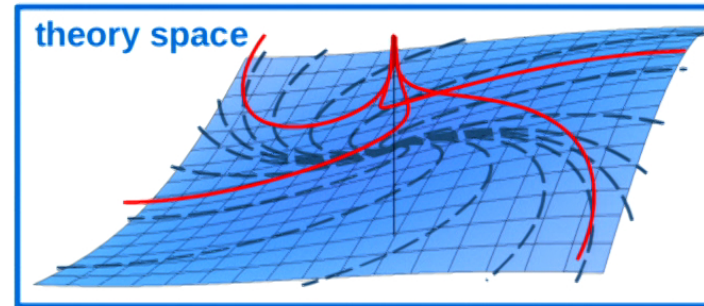
$$b R_{\mu\nu} R^{\mu\nu}$$

$$\frac{R}{G_N} \wedge \frac{G_N}{G_N}$$

Reuter '96
D. Becker and M. Reuter '14, 1404.4537
T. Denz, J. M. Pawłowski and M. Reichert '16, 1612.07315
B. Knorr '17, 1710.07055
J. Biemans, A. Platania, F. Saueressig '16, 1609.04813
B. Knorr, S. Lippoldt '17, 1707.01397

Asymptotic safety: truncations

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Reuter, Lauscher '02,
0205062

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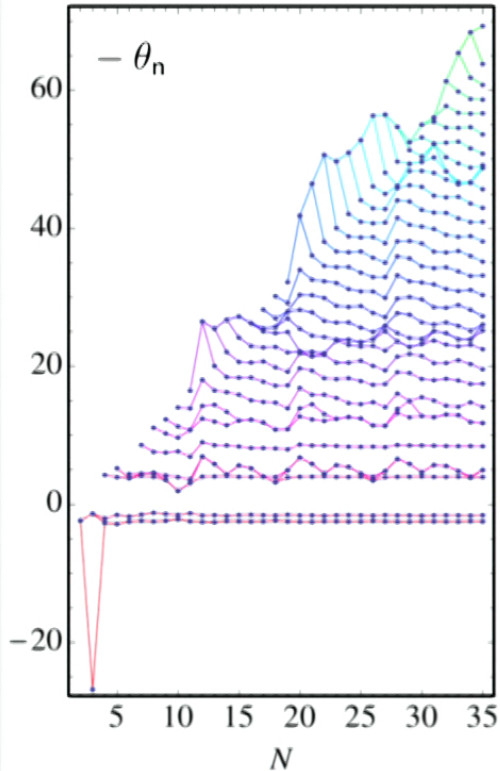
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D. Benedetti, P. F. Machado and F. Saueressig '09, 0901.2984
N. Christiansen '16, 1612.06223

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Asymptotic safety: truncations

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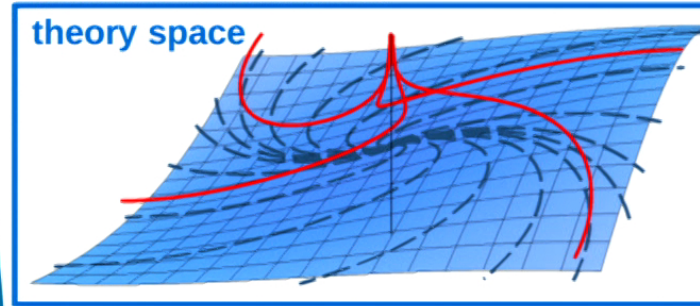


K. Falls, D. F. Litim, K. Nikolakopoulos and C. Rahmede '14, 1410.4815

Codello, Percacci, Rahmede '07, '08
Machado, Saueressig '07
K. Falls, D. F. Litim, K. Nikolakopoulos and C. Rahmede '13, 1301.4191
...

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Reuter, Lauscher '02, 0205062



H. Gies, B. Knorr, S. Lippoldt and F. Saueressig '16, 1601.01800

$$\sigma_k C_{\mu\nu}^{\rho\sigma} C_{\rho\sigma}^{\kappa\lambda} C_{\kappa\lambda}^{\mu\nu}$$

+ more

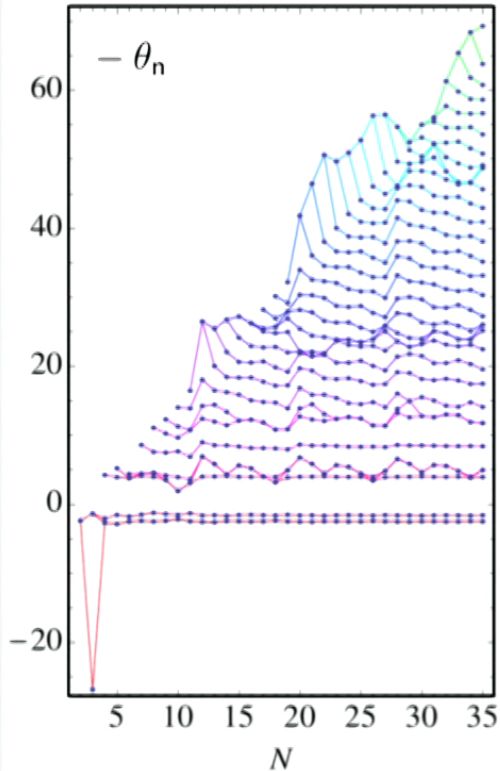
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Asymptotic safety: truncations

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Reuter, Lauscher '02, 0205062

observe powerful guiding principle

near-canonical scaling
& apparent convergence

H. Gies, B. Knorr, S. Lippoldt and F. Saueressig '16, 1601.01800

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Asymptotic safety: truncations

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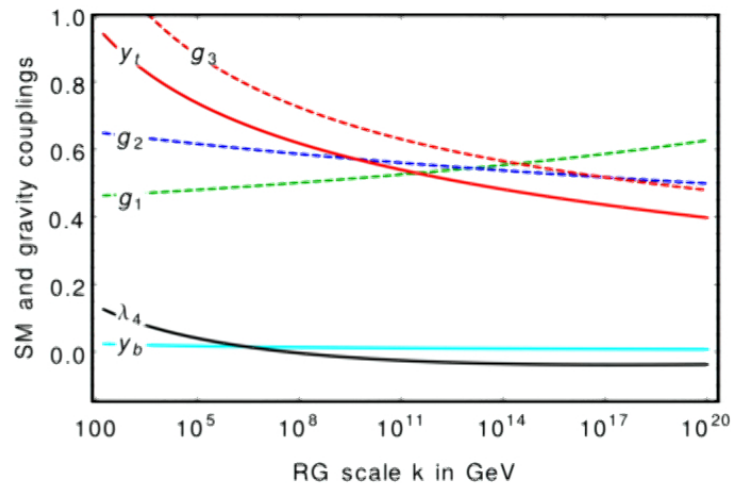
2. Asymptotic safety and matter

Asymptotic safety from a SM perspective

RG equations $\beta_c^{\text{SM}} \sim (d-4)c \pm \# c^3 + \text{h.o.} \quad \forall c \in \{g_1, g_2, g_3, y_t, y_b\}$

marginal canonical dimension

Quantum fluctuations



cf., Buttazzo et al. '13, 1307.3536

Standard Model
as an effective field theory could be
valid up to the Planck scale

Asymptotic safety from a SM perspective

RG equations

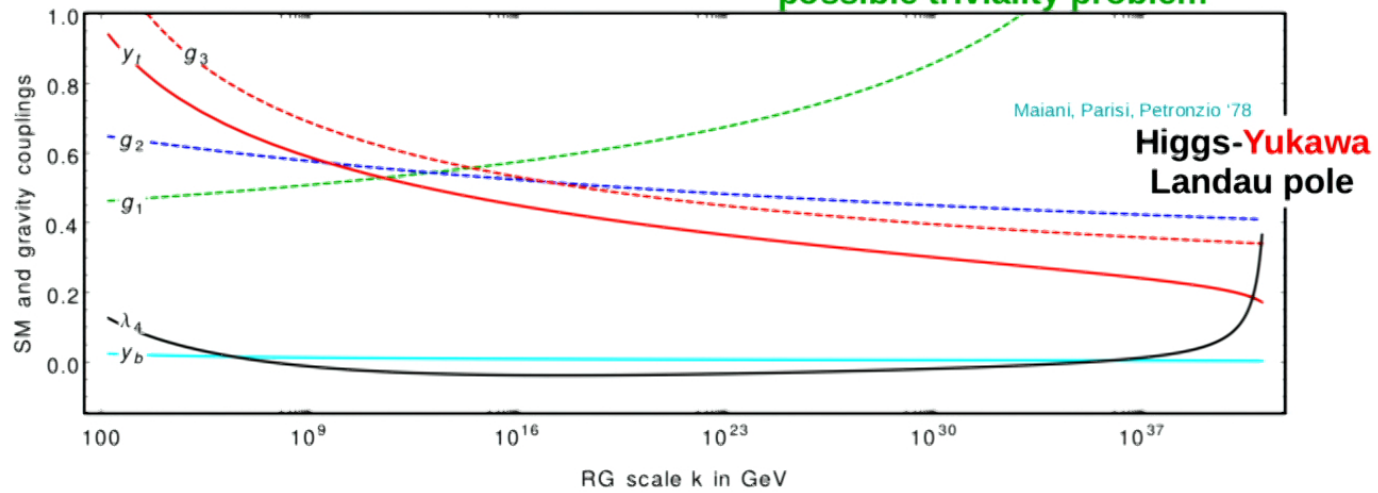
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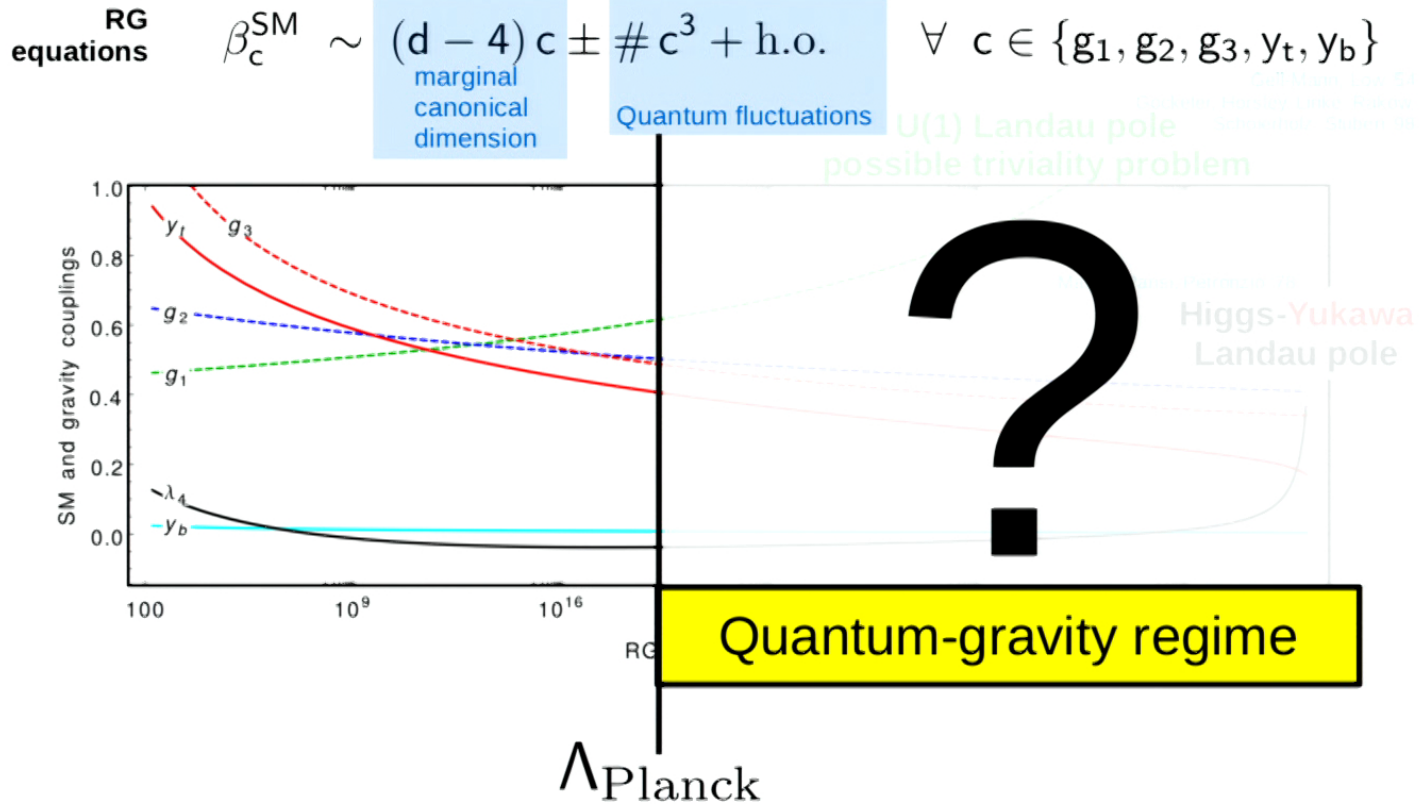
Quantum fluctuations

U(1) Landau pole
possible triviality problem

Gell-Mann, Low '54
Gockeler, Horsley, Linke, Rakow, Schoierholz, Stuben '98
...



Asymptotic safety from a SM perspective

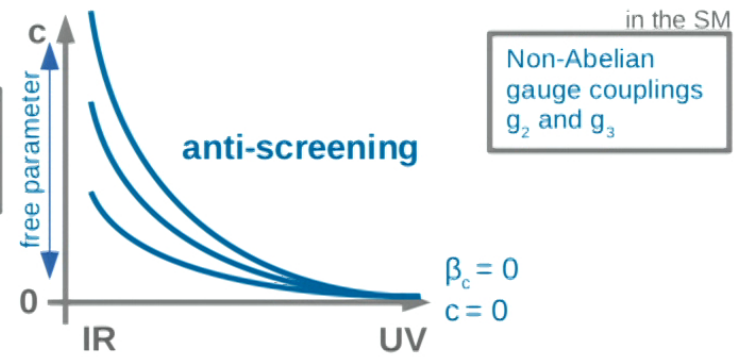


Asymptotic freedom

Scale invariance at a **Gaussian** fixed point ensures a **free** (perturbatively renormalizable) UV theory. **No predictive** power.

$$\beta_c^{\text{SM}} \sim -\# c^3 + \text{h.o.}$$

anti-screening
quantum fluctuations

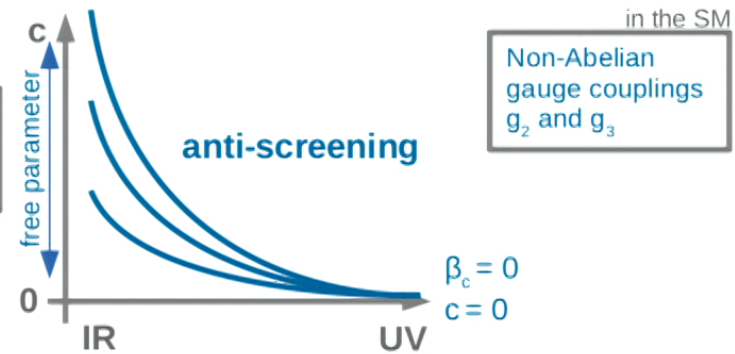


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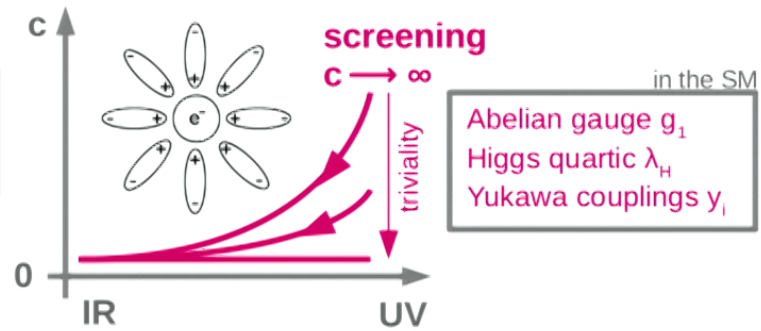


Triviality

Landau divergence at finite scales indicates a **triviality problem**.
 UV-scaling **predicts vanishing coupling**.

$$\beta_c^{\text{SM}} \sim +\# c^3 + \text{h.o.}$$

screening
quantum fluctuations

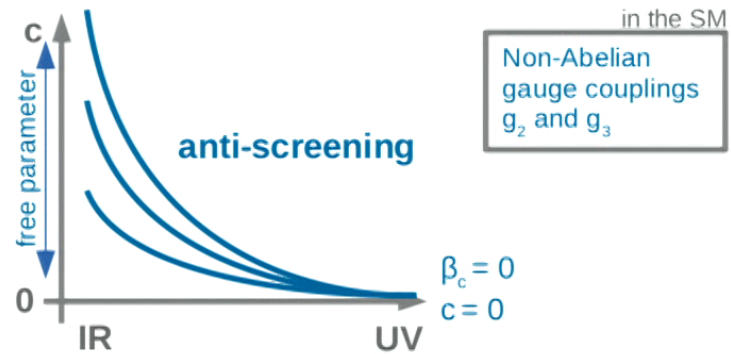


Asymptotic freedom

Scale invariance at a **Gaussian** fixed point ensures a **free** (perturbatively renormalizable) UV theory.
No predictive power.

$$\beta_c^{\text{SM}} \sim -\# c^3 + \text{h.o.}$$

anti-screening
quantum fluctuations

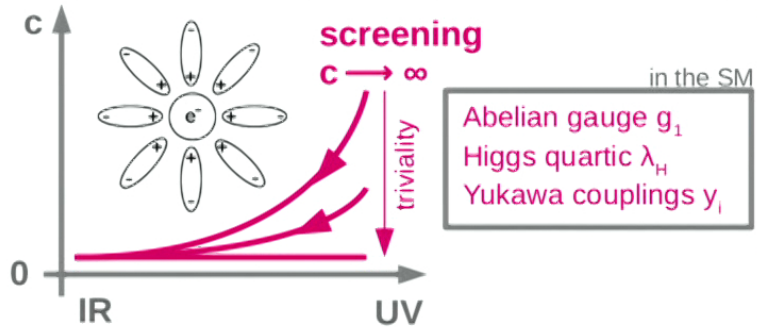


Triviality

Landau divergence at finite scales indicates a **triviality problem**.
 UV-scaling **predicts vanishing coupling**.

$$\beta_c^{\text{SM}} \sim +\# c^3 + \text{h.o.}$$

screening
quantum fluctuations

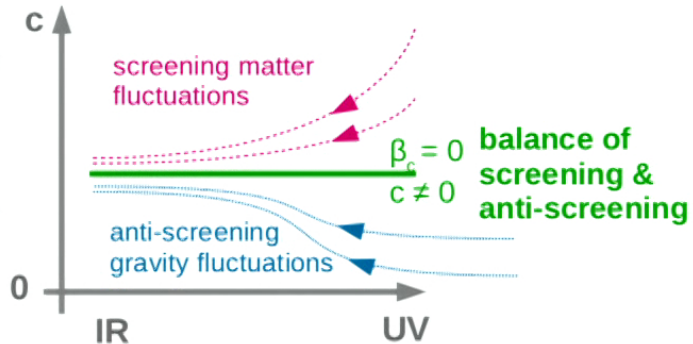


Asymptotic safety

Scale invariance at a **non-Gaussian** fixed point ensures a **safe** (non-perturbatively renormalizable) UV theory.
 Fundamental QFT **predicts finite coupling**.

$$\beta_c^{\text{SM}} \sim -f_c c + \# c^3 + \text{h.o.}$$

quantum gravity anti-screening Standard Model quantum fluctuations



The diagram features the Einstein field equations $G_{\mu\nu} = 8\pi G_N T_{\mu\nu}$ centered on a white background. A large green arrow on the left points from the text below towards the $G_{\mu\nu}$ term. A large blue arrow on the right points from the text below towards the $T_{\mu\nu}$ term. The text below each term is underlined with a curly brace.

$$G_{\mu\nu} = 8\pi G_N T_{\mu\nu}$$

asymptotic safety of
spacetime & asymptotic safety of
under the impact of matter fluctuations matter
induced by spacetime fluctuations

... adding matter to gravity ...

$$G_{\mu\nu} = 8\pi G_N T_{\mu\nu}$$

asymptotic safety of spacetime
under the impact of matter fluctuations

&

asymptotic safety of matter
induced by spacetime fluctuations

... adding matter to gravity ...

3. Asymptotic safety of gravity and matter

Gravitational induction

$$S_{\psi \text{kin}} = i \int d^4x \sqrt{\det(g)} (\bar{\psi} \gamma^\mu \nabla_\mu \psi)$$



$$S_{\phi \text{kin}} = \frac{1}{2} \int d^4x \sqrt{\det(g)} (g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi)$$



Gravitational induction

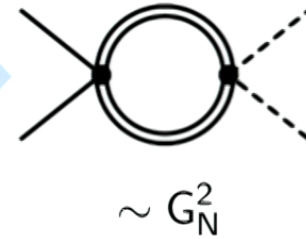
$$S_{\psi \text{kin}} = i \int d^4x \sqrt{\det(g)} (\bar{\psi} \gamma^\mu \nabla_\mu \psi)$$



Gies, Eichhorn '11, 1104.5366
Eichhorn '12, 1204.0965

gravitational
induction

$$S_{\phi \text{kin}} = \frac{1}{2} \int d^4x \sqrt{\det(g)} (g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi)$$



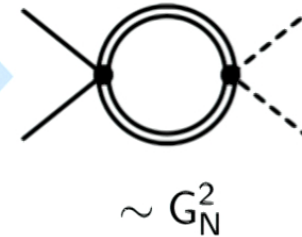
Gravitational induction

$$S_{\psi \text{ kin}} = i \int d^4x \sqrt{\det(g)} (\bar{\psi} \gamma^\mu \nabla_\mu \psi)$$



Gies, Eichhorn '11, 1104.5366
Eichhorn '12, 1204.0965

gravitational
induction



$$S_{\phi \text{ kin}} = \frac{1}{2} \int d^4x \sqrt{\det(g)} (g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi)$$



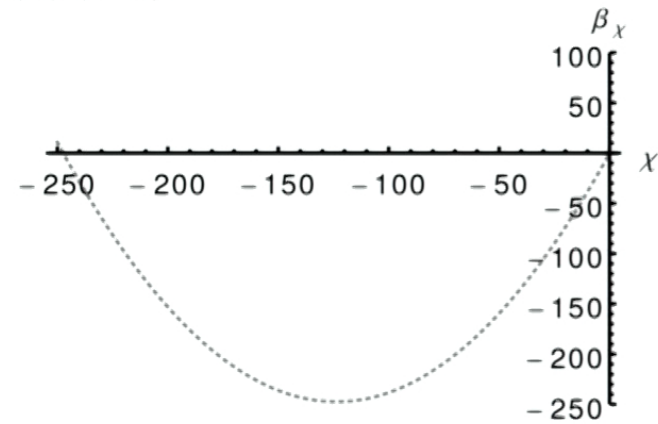
Eichhorn, Held '17, 1705.02342

gravity induces all matter interactions invariant under the
maximal global symmetries
of the matter kinetic terms

$$i\chi \int d^4x \sqrt{g} \left[(\bar{\psi} \gamma^\mu \nabla_\nu \psi - (\nabla_\nu \bar{\psi}) \gamma^\mu \psi) (\partial_\mu \phi \partial^\nu \phi) \right. \\ \left. + (\bar{\psi} \gamma^\mu \nabla_\mu \psi - (\nabla_\mu \bar{\psi}) \gamma^\mu \psi) (\partial_\nu \phi \partial^\nu \phi) \right]$$

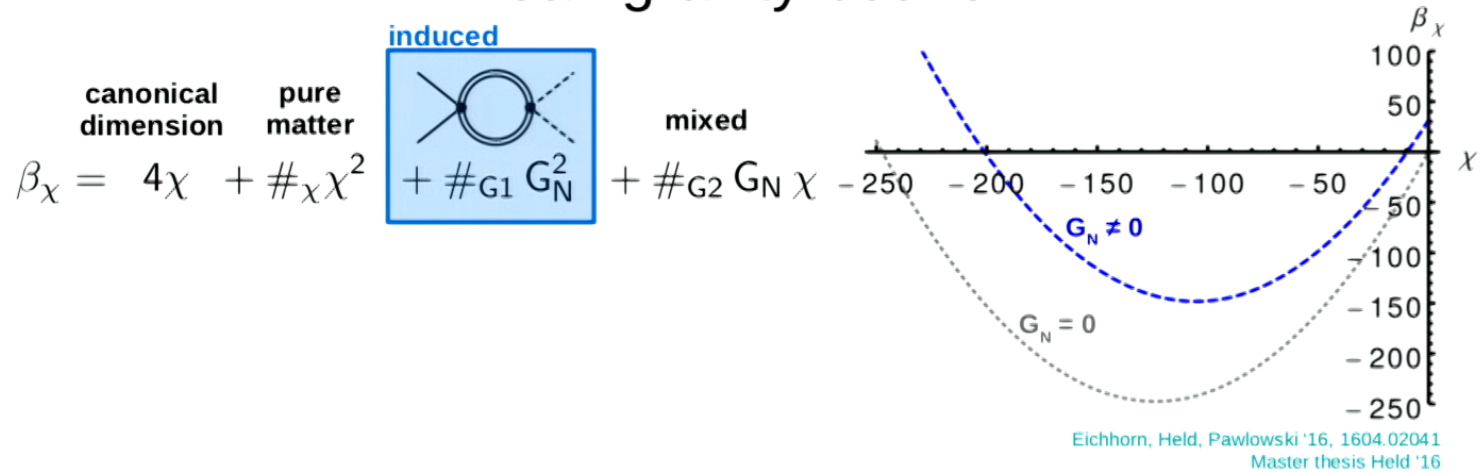
Weak gravity bound

canonical dimension	pure matter
$\beta_\chi = 4\chi$	$+ \#_\chi \chi^2$



Eichhorn, Held, Pawłowski '16, 1604.02041
Master thesis Held '16

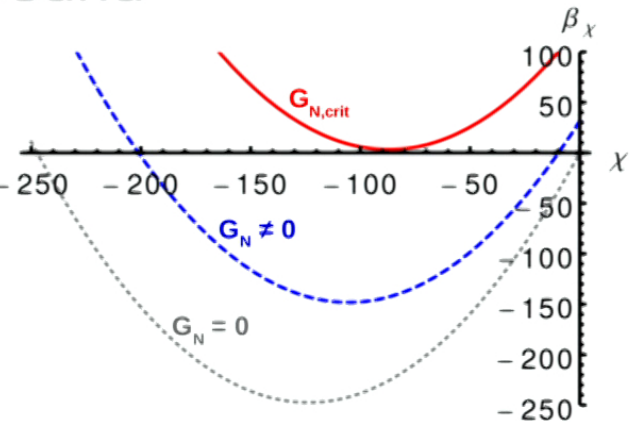
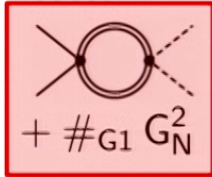
Weak gravity bound



Weak gravity bound

$$\beta_\chi = 4\chi + \#_\chi \chi^2 + \#_{G1} G_N^2 + \#_{G2} G_N \chi$$

canonical dimension
pure matter
induced
mixed

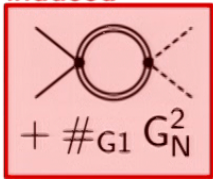


within truncations

Weak gravity bound:
 Too strong gravity triggers **new divergences** in the **matter sector**

Eichhorn, Held, Pawłowski '16, 1604.02041
 Master thesis Held '16

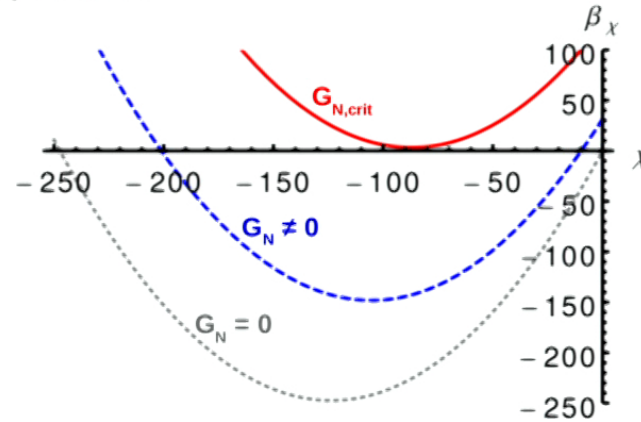
Weak gravity bound

canonical dimension $\beta_\chi = 4\chi + \#\chi\chi^2$ + pure matter $+ \#_{G1} G_N^2$ + induced  + mixed $+ \#_{G2} G_N \chi$

within truncations

Weak gravity bound:

Too strong gravity triggers new divergences in the matter sector



Eichhorn, Held, Pawłowski '16, 1604.02041
Master thesis Held '16

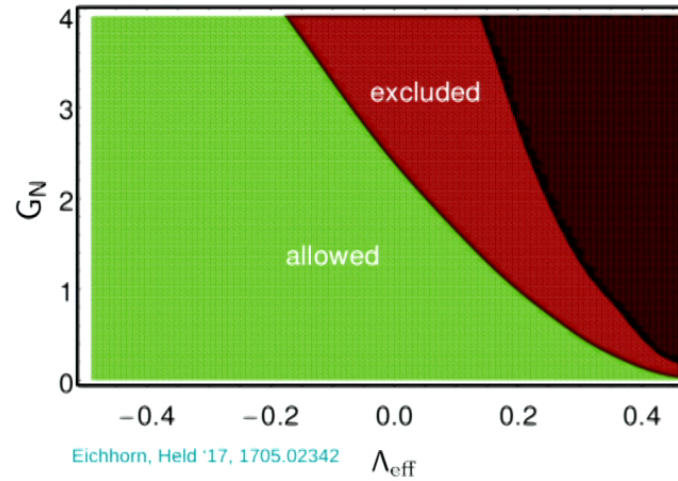
spin-2 mode

$$\left(\Gamma_{k,TT}^{(2)}\right)^{-1} = \frac{32\pi G_N}{p^2 - 2\Lambda}$$

Newton coupling

microscopic cosmological constant

- a large (and negative) **cosmological constant** (and higher curvature couplings) work like an **effective mass**




Eichhorn, Held '17, 1705.02342

Λ_{eff}

Weak gravity bound

$$\beta_\chi = 4\chi + \#_\chi \chi^2 + \#_{G1} G_N^2 + \#_{G2} G_N \chi$$

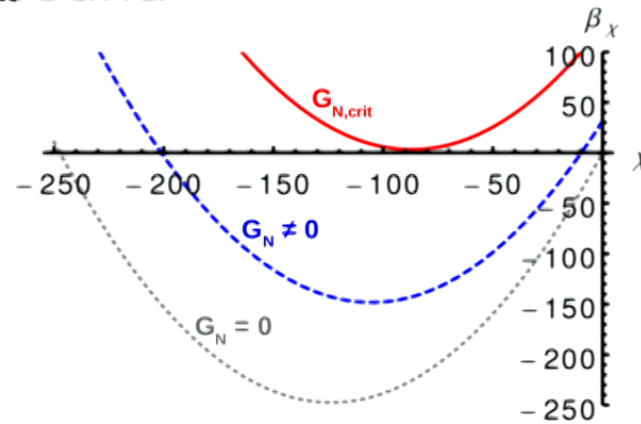
canonical dimension pure matter **induced** mixed



within truncations

Weak gravity bound:

Too strong gravity triggers **new divergences** in the **matter sector**



Eichhorn, Held, Pawłowski '16, 1604.02041
Master thesis Held '16

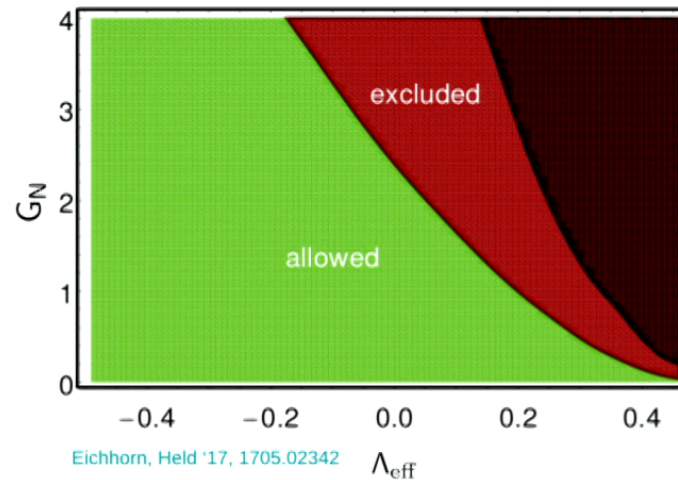
spin-2 mode

$$\left(\Gamma_{k,TT}^{(2)}\right)^{-1} = \frac{32\pi G_N}{p^2 - 2\Lambda}$$

Newton coupling microscopic cosmological constant

- a large (and negative) **cosmological constant** (and higher curvature couplings) work like an **effective mass**
- remaining question: does adding matter effectively weaken or strengthen gravity?

P. Dona, A. Eichhorn, R. Percacci '13, 1311.2898
 J. Meibohm, J. Pawłowski, M. Reichert '15, 1510.07018
 J. Biemans, A. Platania, F. Saueressig '17, 1702.06539



Eichhorn, Held '17, 1705.02342

Asymptotic safety of gauge couplings

Asymptotic safety of gauge couplings

$$\beta_\alpha = (\mathcal{N} - \mathcal{N}_c) \frac{\alpha^2}{4\pi} - f_\alpha(G_N, \Lambda) \alpha$$

gauge & matter
fluctuations:
screening

quantum gravity:
anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$

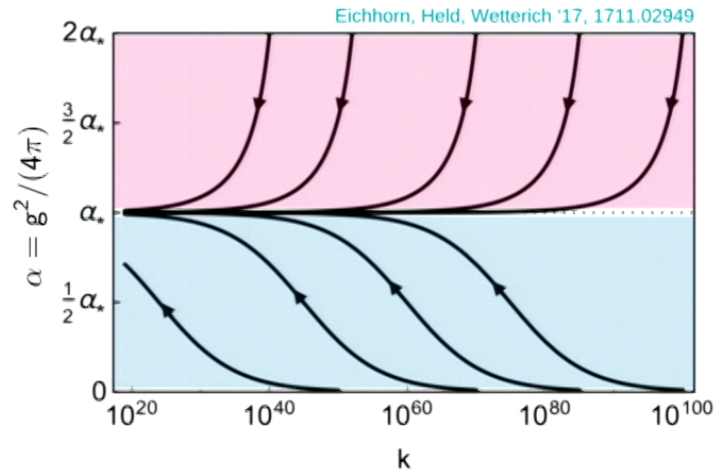
Daum, Harst, Reuter '10, JHEP 084
Harst, Reuter '11, JHEP 119
Folkerts, Litim, Pawłowski '12, Phys.Lett.B 709
Christiansen, Eichhorn '17, Phys.Lett.B 770
Christiansen, Litim, Pawłowski, Reichert '17, 1710.04669
Eichhorn, Versteegen '17, 1709.07252

Asymptotic safety of gauge couplings

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gauge & matter fluctuations: screening
quantum gravity: anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$



Asymptotic safety of gauge couplings

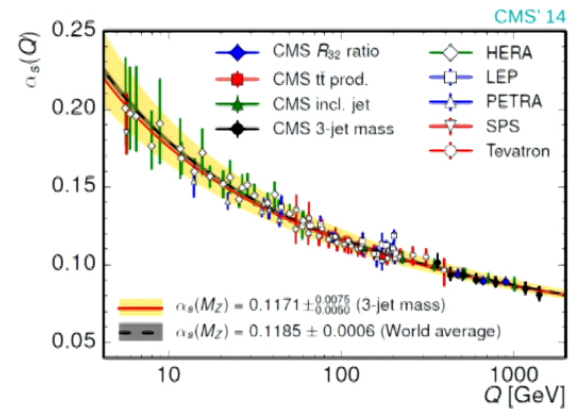
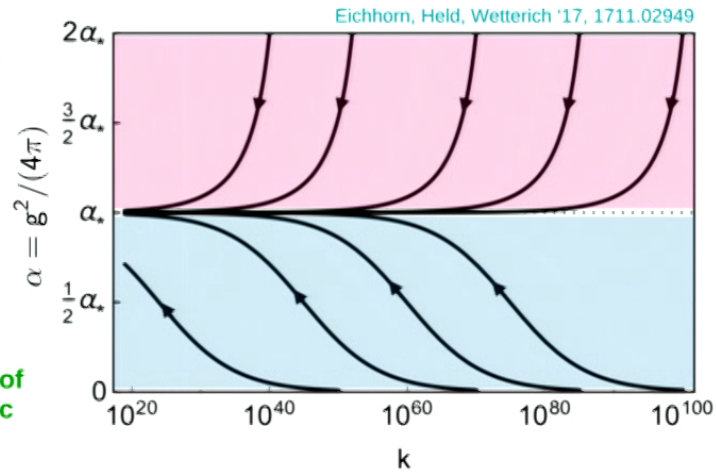
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gauge & matter fluctuations: screening
quantum gravity: anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$

viability of the Standard Model

$\mathcal{N} - \mathcal{N}_c = -14$ for SU(3) with SM-matter

speed-up of asymptotic freedom


Asymptotic safety of gauge couplings

$$\beta_\alpha = (\mathcal{N} - \mathcal{N}_c) \frac{\alpha^2}{4\pi} - f_\alpha(G_N, \Lambda) \alpha$$

gauge & matter fluctuations: screening

quantum gravity: anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$

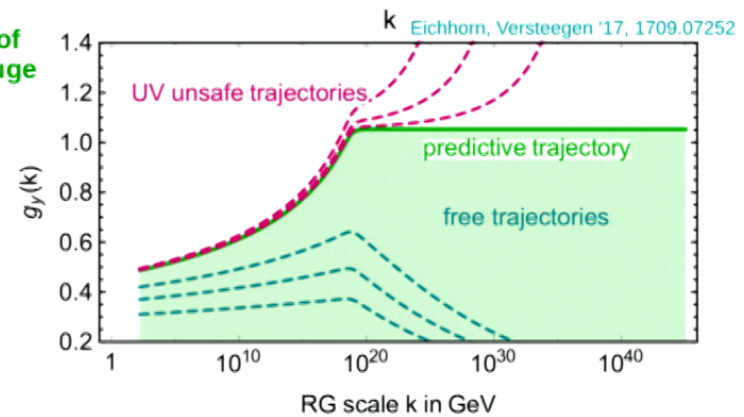
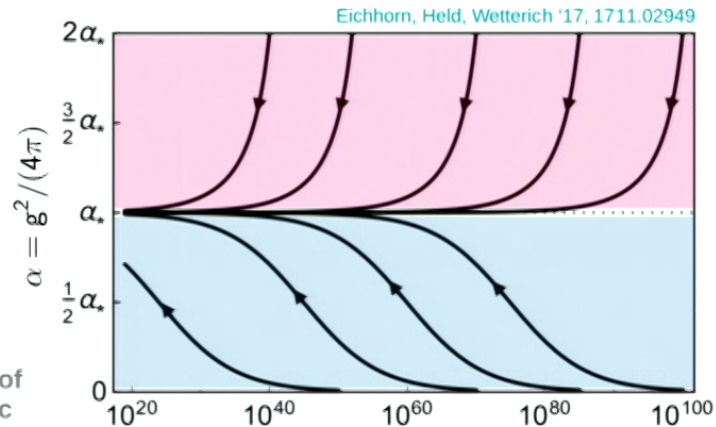
viability of the Standard Model

$$\mathcal{N} - \mathcal{N}_c = -14 \text{ for SU(3) with SM-matter}$$

speed-up of asymptotic freedom

$$\mathcal{N} - \mathcal{N}_c = \frac{41}{5} \text{ for U(1) with SM-matter}$$

prediction of abelian gauge coupling



Asymptotic safety of gauge couplings

$$\beta_\alpha = (\mathcal{N} - \mathcal{N}_c) \frac{\alpha^2}{4\pi} - f_\alpha(G_N, \Lambda) \alpha$$

gauge & matter fluctuations: screening
quantum gravity: anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$

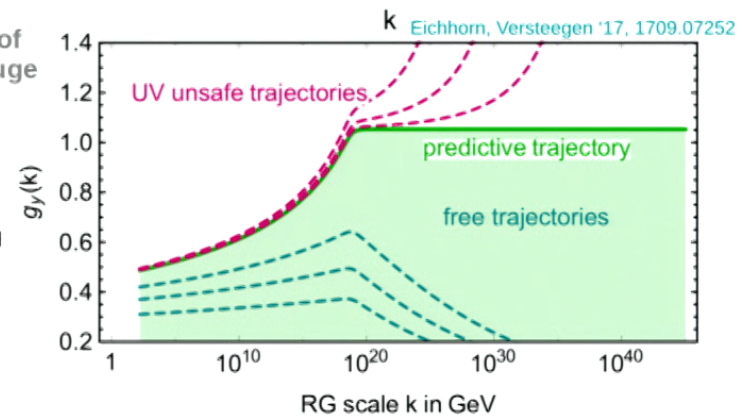
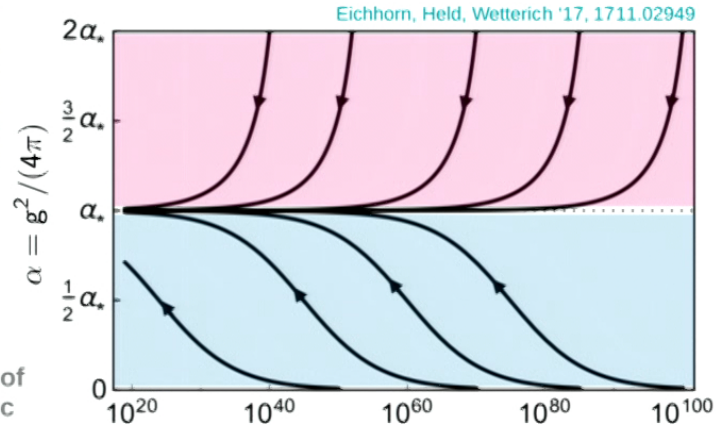
viability of the Standard Model

$\mathcal{N} - \mathcal{N}_c = -14$ for SU(3) with SM-matter	speed-up of asymptotic freedom
$\mathcal{N} - \mathcal{N}_c = \frac{41}{5}$ for U(1) with SM-matter	prediction of abelian gauge coupling

GUT-gravity model building

$$\mathcal{N} - \mathcal{N}_c = \mathcal{N} - 50 \quad \text{for SO}(10) \text{ with three } \mathbf{16}_F \text{ and } \mathbf{10}_H$$

$$\Rightarrow \alpha_{EM} = \alpha_{EM}(\mathcal{N}, f_\alpha)$$



Asymptotic safety of gauge couplings

$$\beta_\alpha = (\mathcal{N} - \mathcal{N}_c) \frac{\alpha^2}{4\pi} - f_\alpha(G_N, \Lambda) \alpha$$

gauge & matter fluctuations: screening
quantum gravity: anti-screening < 0

$$\Rightarrow \alpha_* = \frac{4\pi G_N f_\alpha}{\mathcal{N} - \mathcal{N}_c}$$

viability of the Standard Model

$\mathcal{N} - \mathcal{N}_c = -14$ for SU(3) with SM-matter	speed-up of asymptotic freedom
$\mathcal{N} - \mathcal{N}_c = \frac{41}{5}$ for U(1) with SM-matter	prediction of abelian gauge coupling

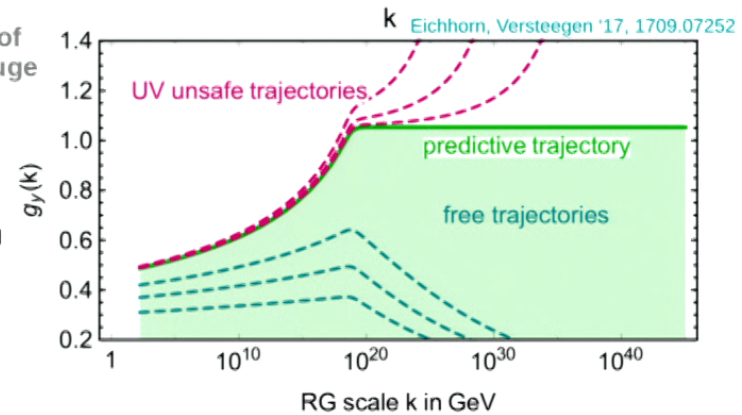
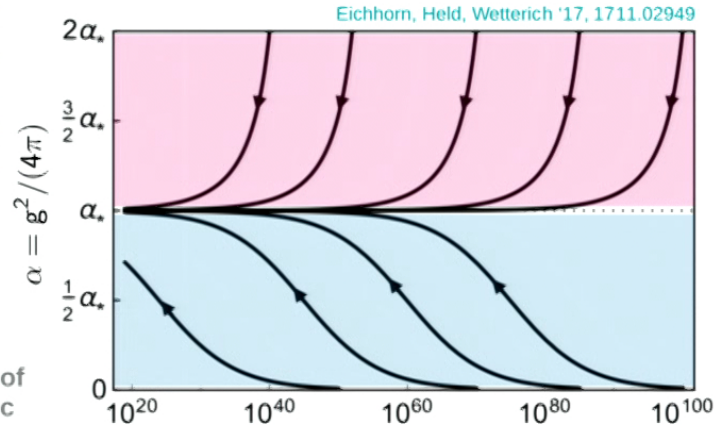
GUT-gravity model building

$$\mathcal{N} - \mathcal{N}_c = \mathcal{N} - 50 \quad \text{for SO(10) with three } \mathbf{16}_F \text{ and } \mathbf{10}_H$$

$$\Rightarrow \alpha_{EM} = \alpha_{EM}(\mathcal{N}, f_\alpha)$$

asymptotic safety offers a mechanism

fixes α_{EM} in terms of quantum gravity (f_α) and matter content (\mathcal{N})



Asymptotic safety of Yukawa couplings

UV-complete SM: triviality problem

SM exhibits **Landau poles in marginally irrelevant** couplings:

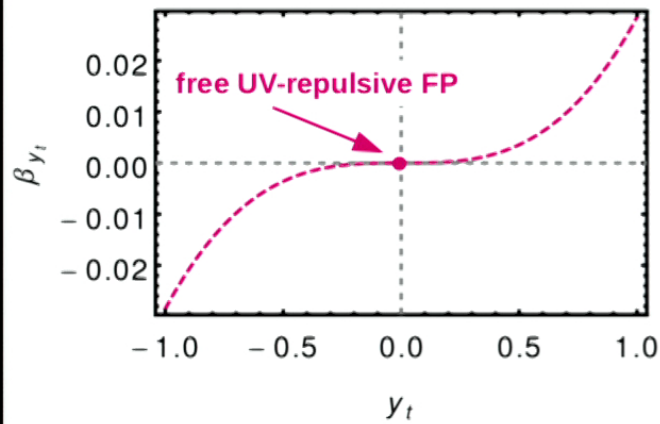
g_1, λ_4, y_t

Gell-Mann, Low '54
Maiani, Parisi, Petronzio '78
...

$$\beta_{y_t} = \frac{9}{32\pi^2} y_t^3 + (\text{SM-terms})$$

beta-function

running of the coupling



UV-complete SM: triviality problem

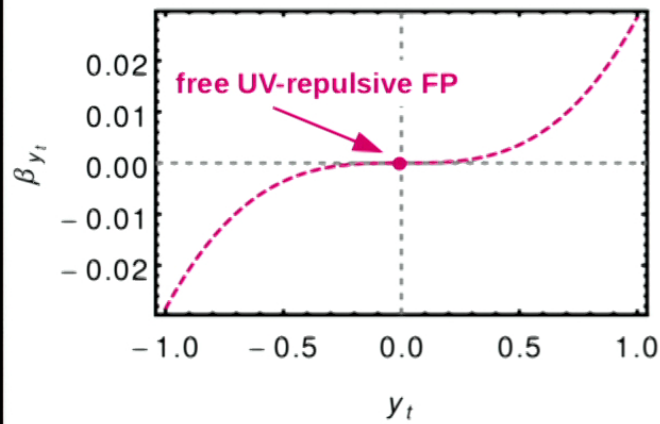
SM exhibits **Landau poles in marginally irrelevant** couplings:

g_1, λ_4, y_t

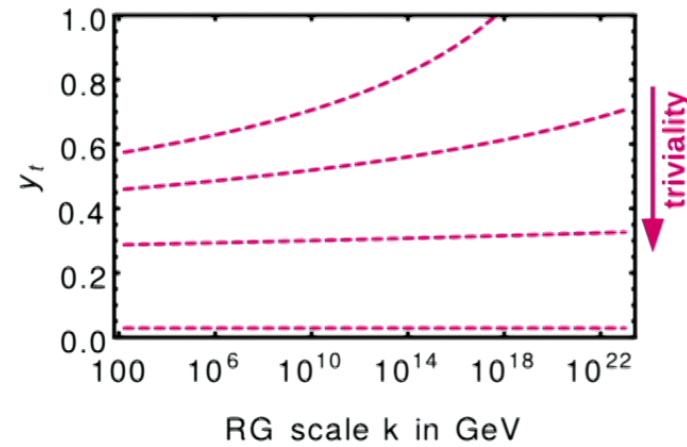
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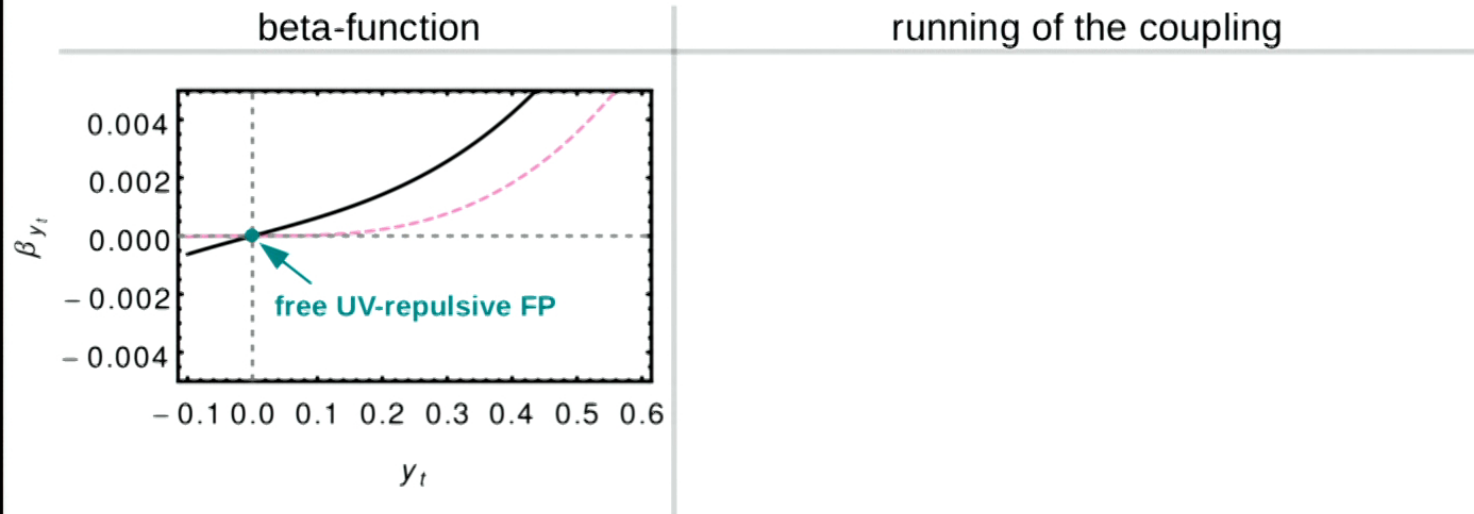


UV-complete SM: predicting the top

$$\beta_{y_t} = \frac{9}{32\pi^2} y_t^3 + G_N y_t f_y(\Lambda) + (\text{SM-terms})$$

$$f_y(\Lambda) > 0$$

screening gravity fluctuations



UV-complete SM: predicting the top

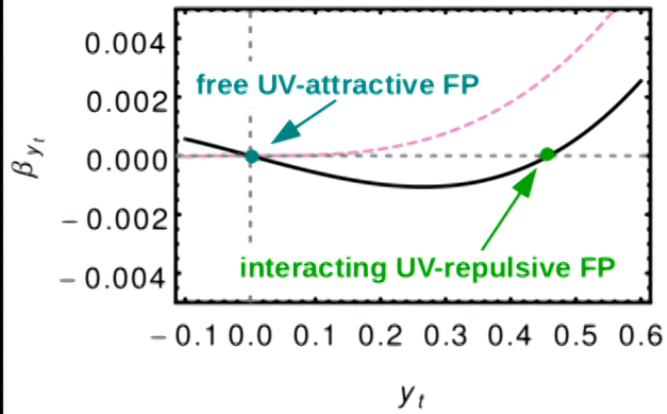
$$\beta_{y_t} = \frac{9}{32\pi^2} y_t^3 + G_N y_t f_y(\Lambda) + (\text{SM-terms})$$

quantum gravity

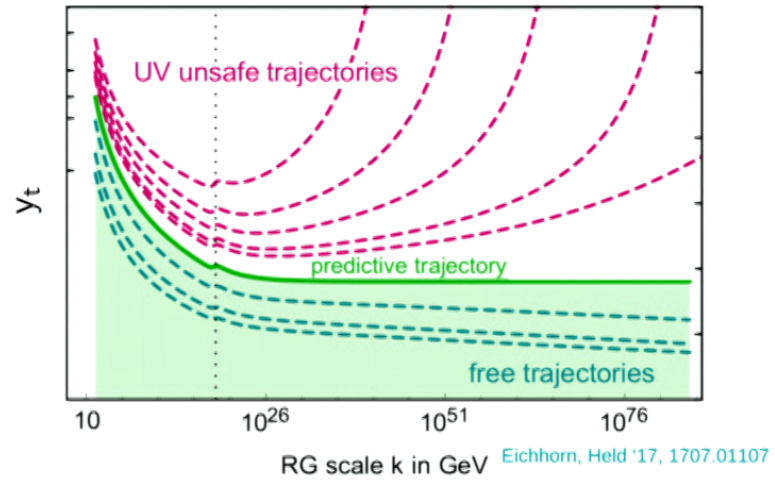
$$f_y(\Lambda) < 0$$

balance of
screening matter and
anti-screening gravity fluctuations

beta-function



running of the coupling



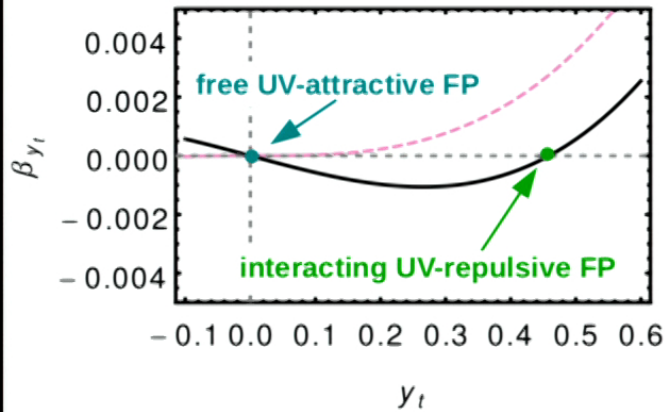
RG scale k in GeV Eichhorn, Held '17, 1707.01107

UV-complete SM: predicting the top

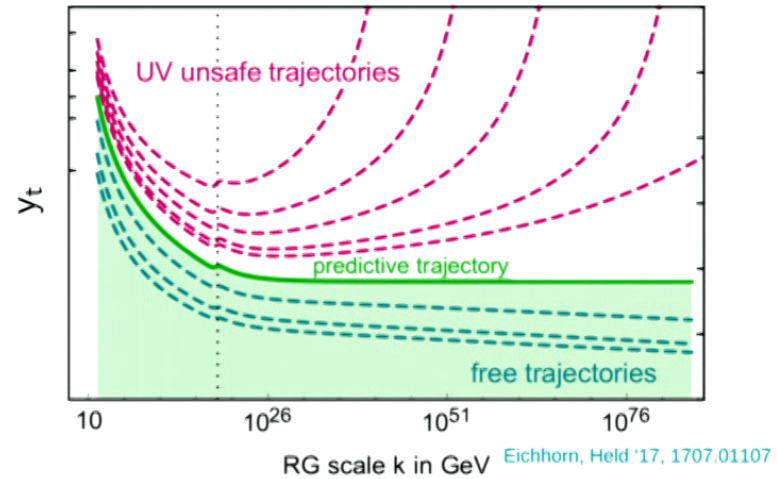
$$\beta_{y_t} = \frac{9}{32\pi^2} y_t^3 + \underbrace{G_N y_t f_y(\Lambda)}_{\text{quantum gravity}} + (\text{SM-terms})$$

$f_y(\Lambda) < 0$
 balance of
 screening matter and
 anti-screening gravity fluctuations

beta-function



running of the coupling



➔ **free fixed point:** accommodates $M_t < M_{t,crit}$

UV-complete SM: constraining quantum gravity

$$y_t^* = \frac{\sqrt{32}\pi}{3} \sqrt{-G_N f_y(\Lambda)}$$

$$\text{with: } f_y(\Lambda) = \frac{96 + \Lambda(-235 + \Lambda(103 + 56\Lambda))}{12\pi(3 + 2\Lambda(-5 + 4\Lambda))^2}$$

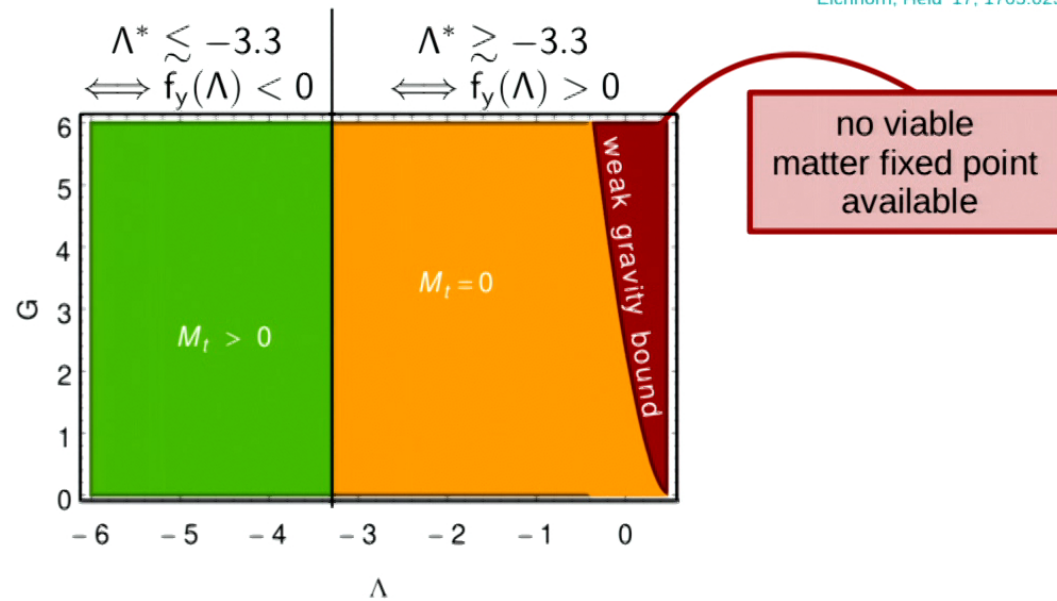
Eichhorn, Held '17, 1705.02342

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Eichhorn, Held '17, 1705.02342

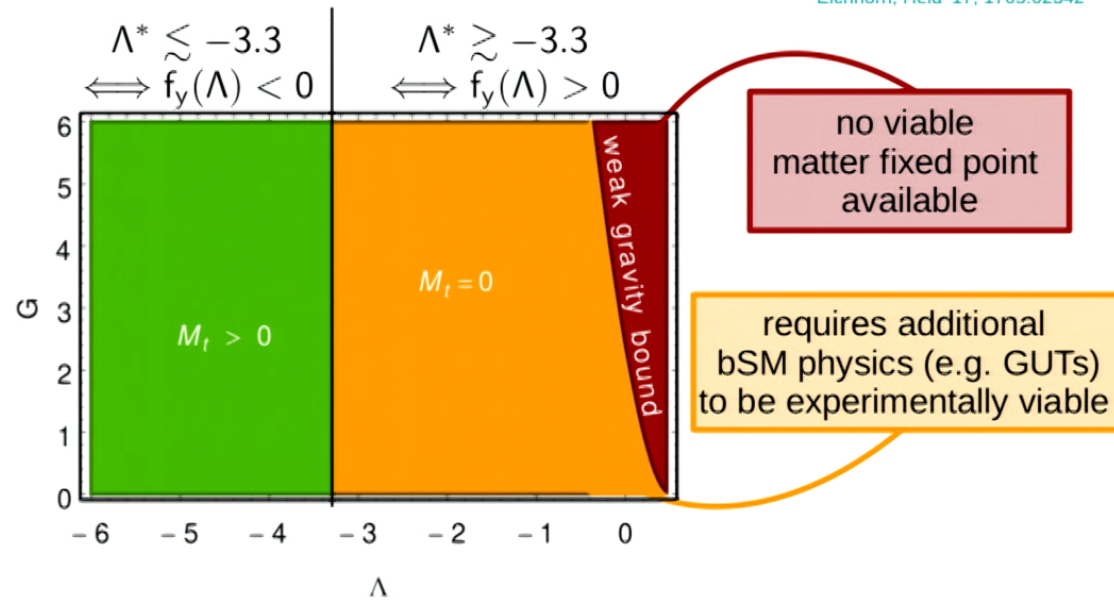


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Eichhorn, Held '17, 1705.02342

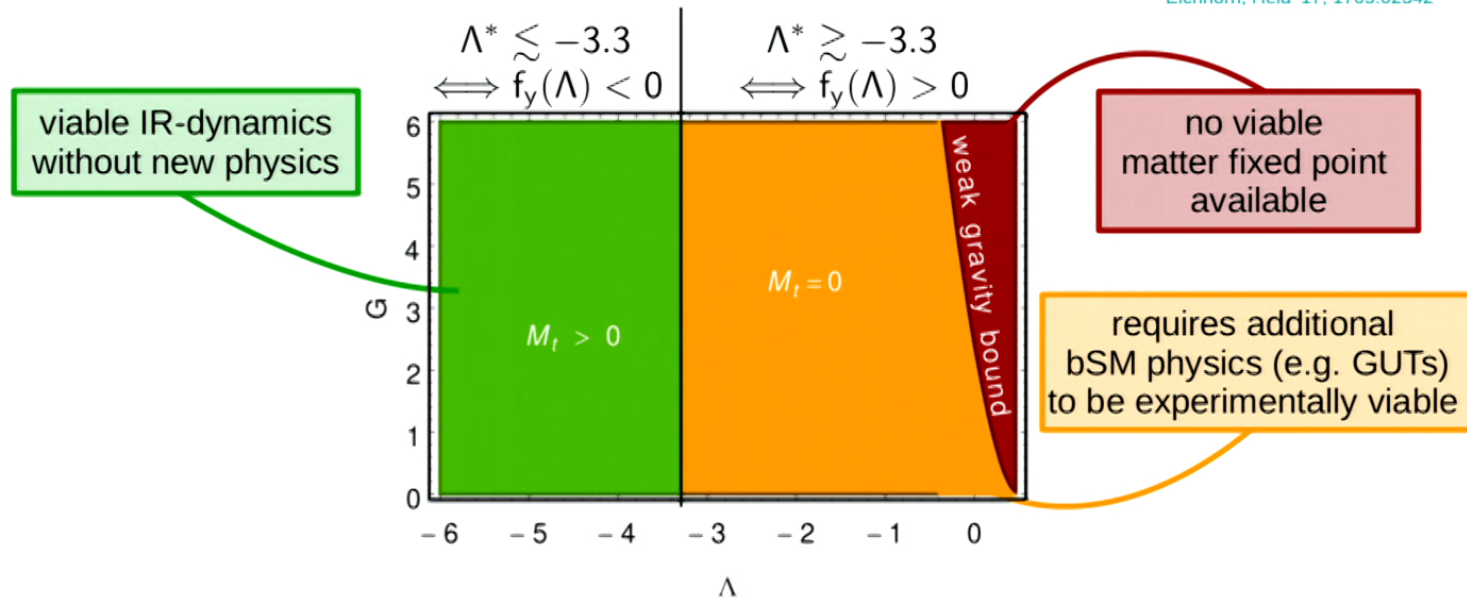


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Eichhorn, Held '17, 1705.02342

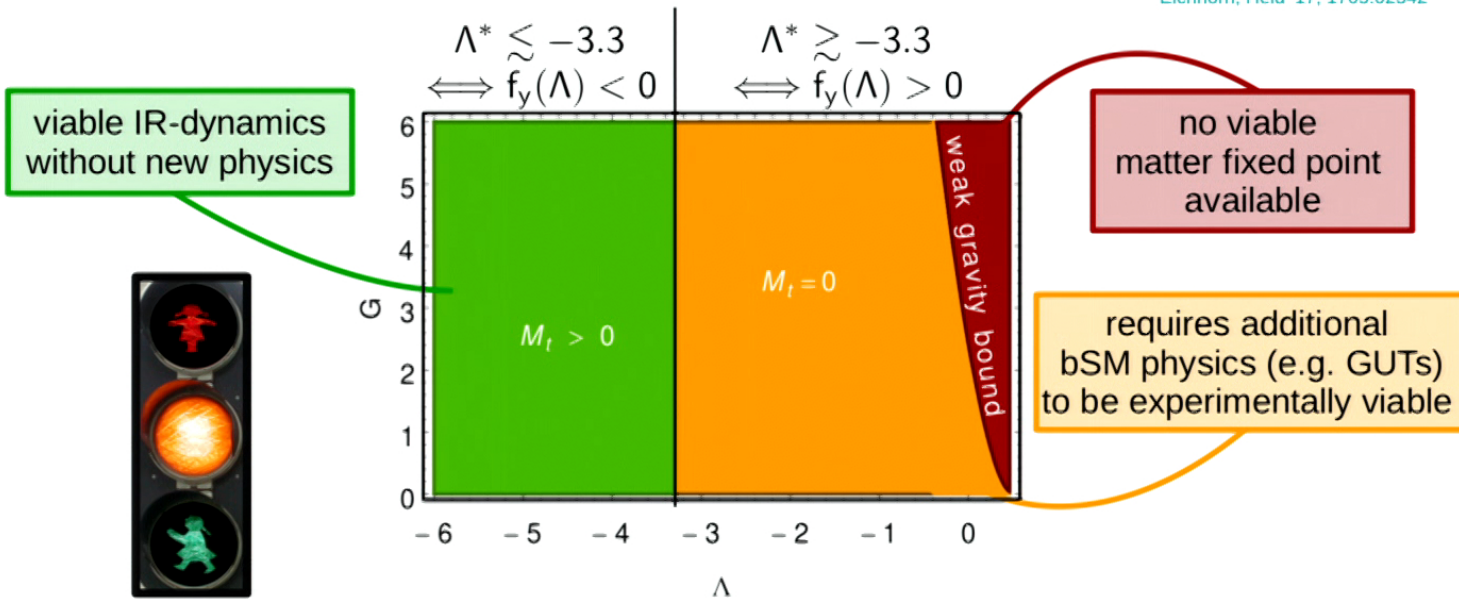


UV-complete SM: constraining quantum gravity

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Eichhorn, Held '17, 1705.02342



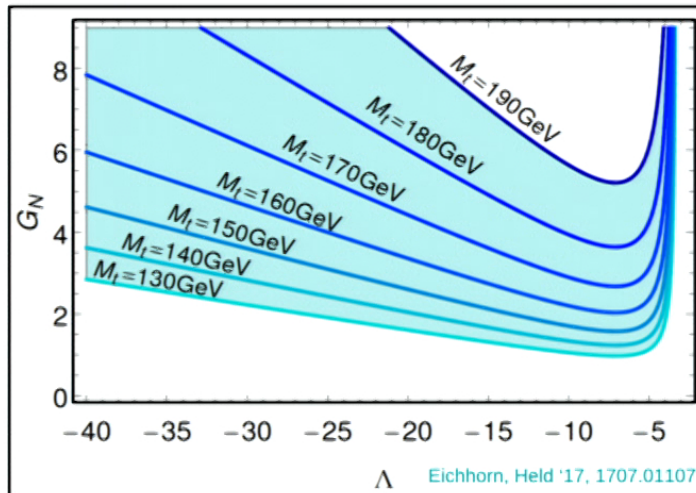
observation of **matter at accessible energy scales** imposes constraints on the **gravitational dynamics at transplanckian scales**

Top mass from asymptotic safety

$$y_t^* = \frac{\sqrt{32\pi}}{3} \sqrt{-G_N f_y(\Lambda)}$$

$$\text{with: } f_y(\Lambda) = \frac{96 + \Lambda(-235 + \Lambda(103 + 56\Lambda))}{12\pi(3 + 2\Lambda(-5 + 4\Lambda))^2}$$

Eichhorn, Held '17, 1705.02342



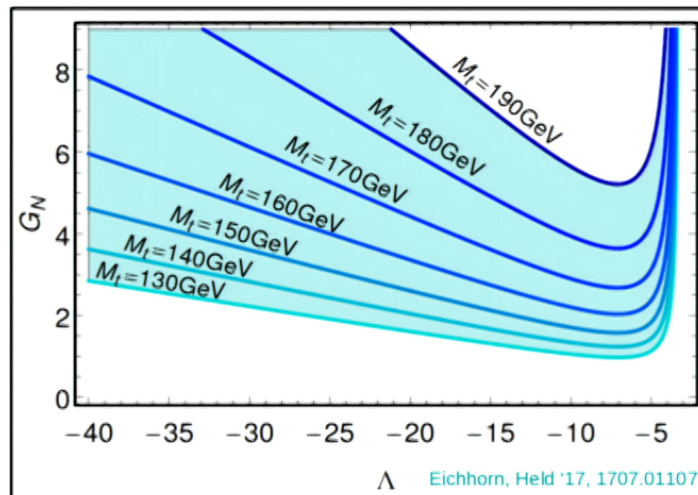
Top mass from asymptotic safety

$$G_N^* = \frac{12\pi}{46 - N_W - N_S + 4N_V}$$

$$\Lambda^* = \frac{3}{4} \left(\frac{2 - 2N_W + N_S + 2N_V}{31 - N_W - N_S + 4N_V} \right)$$

simplified form:
Donà, Eichhorn, Percacci '13, 1311.2898

fermionic matter content of the SM
could shift gravity into the **viable regime**



Top mass from asymptotic safety

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simplified form:
Donà, Eichhorn, Percacci '13, 1311.2898

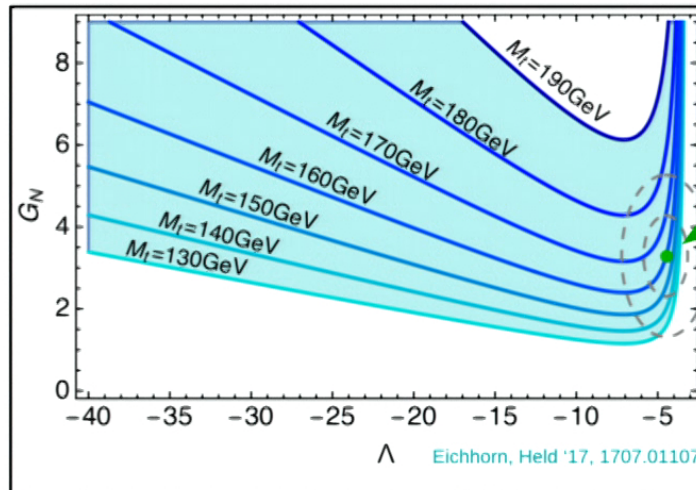
$N_W = 45$: Weyl fermions

$N_S = 4$: scalars

$N_V = 12$: gauge fields

fermionic matter content of the SM
could shift gravity into the **viable regime**

$$\Rightarrow G_N^* = 3.3, \Lambda^* = -4.5$$



predicts a top pole mass of $M_{t, \text{pole}} \approx 170 \text{ GeV}$

within truncations

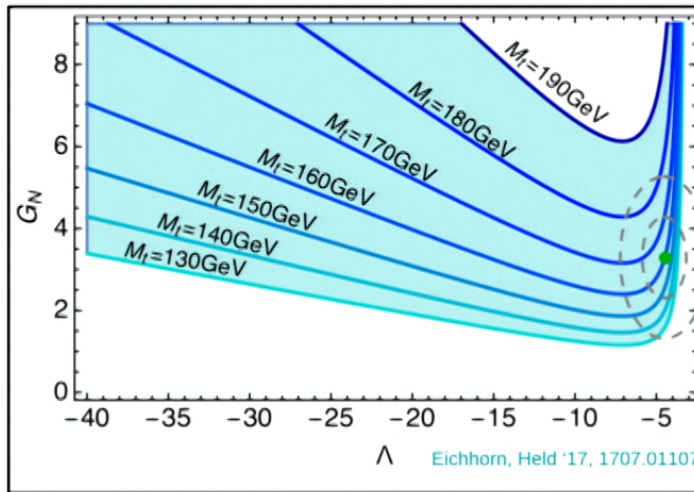
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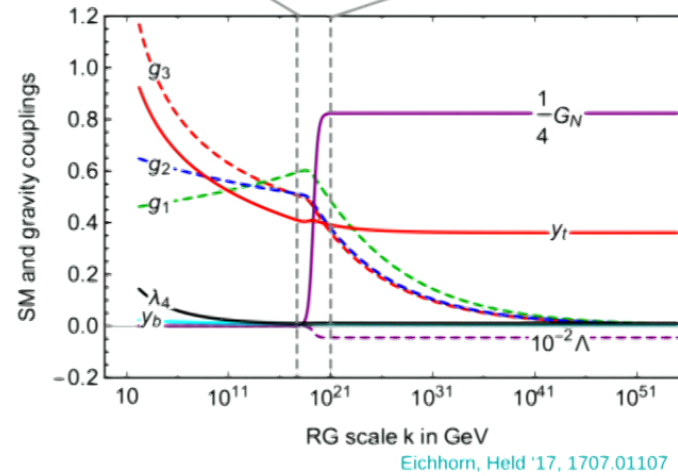
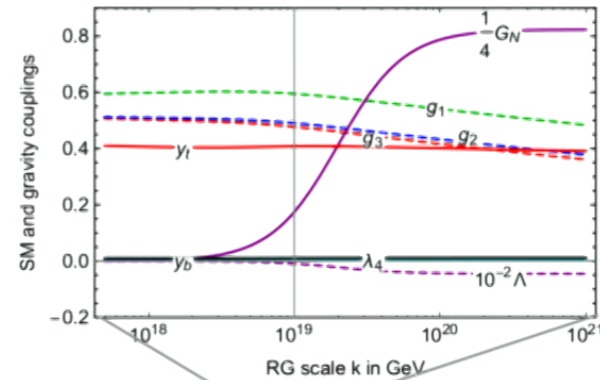
simplified form:
Donà, Eichhorn, Percacci '13, 1311.2898

fermionic matter content of the SM
could shift gravity into the **viable regime**



predicts a top pole mass of $M_{t, \text{pole}} \approx 170 \text{ GeV}$

within truncations



Outlook:
Asymptotic safety of gauge-Yukawa theories

U(1)-hypercharge breaks exchange symmetry $y_t \leftrightarrow y_b$

$$\beta_{y_t}^{\text{SM}} = \frac{y_t}{16\pi^2} \left(\frac{3y_b^2}{2} + \frac{9y_t^2}{2} - 3g_Y^2 (Y_Q^2 + Y_b^2) \right) - y_t G_N f_y(\Lambda)$$

$$\beta_{y_b}^{\text{SM}} = \frac{y_b}{16\pi^2} \left(\frac{9y_b^2}{2} + \frac{3y_t^2}{2} - 3g_Y^2 (Y_Q^2 + Y_t^2) \right) - y_b G_N f_y(\Lambda)$$

U(1) explicitly breaks exchange symmetry
matter fluctuations gauge fluctuations quantum gravity fluctuations

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- an asymptotically safe U(1) can establish a mass hierarchy in terms of electric charges Q_b and Q_t

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U(1) explicitly breaks exchange symmetry
matter fluctuations gauge fluctuations quantum gravity fluctuations

- an asymptotically safe U(1) can establish a mass hierarchy in terms of electric charges Q_b and Q_t
- In SM: $Q_t=2/3$, $Q_b=-1/3$

$$0 \simeq y_b^{2*} = y_t^{2*} - [Q_t^2 - Q_b^2] g_Y^{2*}$$

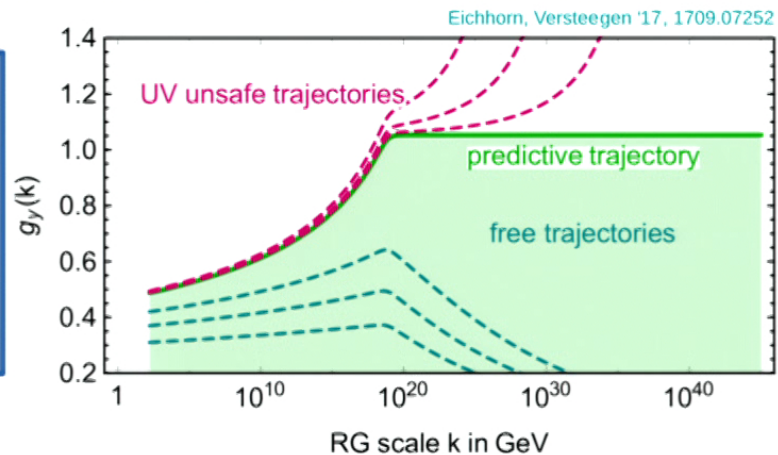
$$\Rightarrow \frac{y_t^{2*}}{g_Y^{2*}} \simeq \frac{1}{3} \quad \text{guarantees a large hierarchy}$$

recall:

$$\beta_{g_Y} = \frac{g_Y^3}{16\pi^2} \frac{41}{10} - g_Y f_g(G, \Lambda, \dots)$$

gauge fluctuations quantum gravity fluctuations

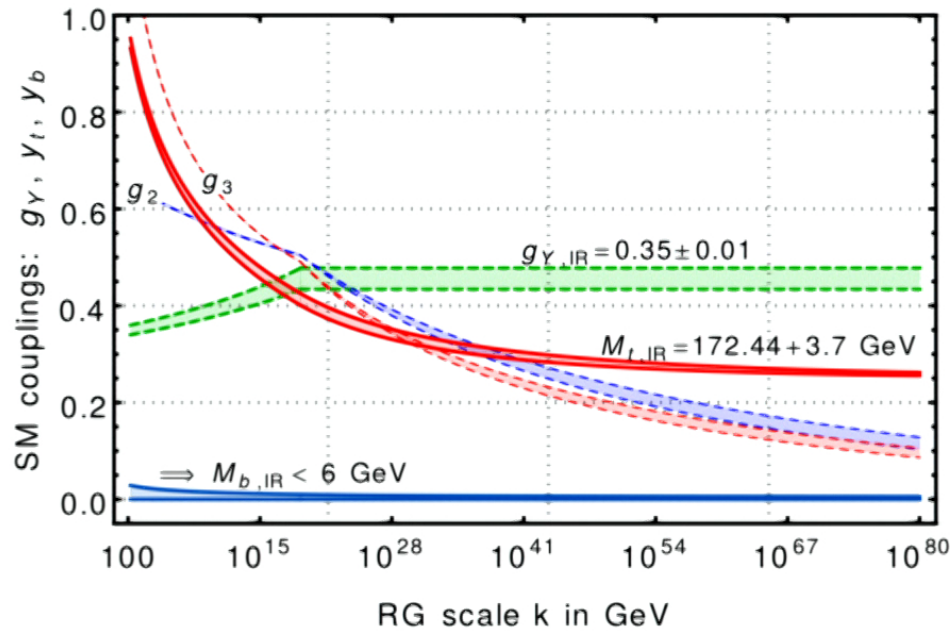
Daum, Harst, Reuter '10, JHEP 084
 Harst, Reuter '11, JHEP 119
 Folkerts, Litim, Pawłowski '12, Phys.Lett.B 709
 Christiansen, Eichhorn '17, Phys.Lett.B 770
 Christiansen, Litim, Pawłowski, Reichert '17, 1710.04669
 Eichhorn, Versteegen '17, 1709.07252





Outlook: hypercharges and mass-hierarchy

$$\left. \begin{aligned}
 \beta_{y_t} &= \frac{y_t}{32\pi^2} \left(9y_t^2 + 3y_b^2 - \frac{17}{10}g_Y^2 \right) + G_N y_t f_y(\Lambda) + (\text{SM-terms}) \\
 \beta_{y_b} &= \frac{y_b}{32\pi^2} \left(9y_b^2 + 3y_t^2 - \frac{1}{2}g_Y^2 \right) + G_N y_b f_y(\Lambda) + (\text{SM-terms}) \\
 \beta_{g_Y} &= \frac{g_Y^3}{16\pi^2} \frac{41}{10} - G_N g_Y f_g(\Lambda)
 \end{aligned} \right\} \begin{array}{l} f_g(g_Y, \text{IR}) \\ f_y(M_t, \text{IR}) \end{array} \text{ fixed}$$



Eichhorn, Held, in prep.



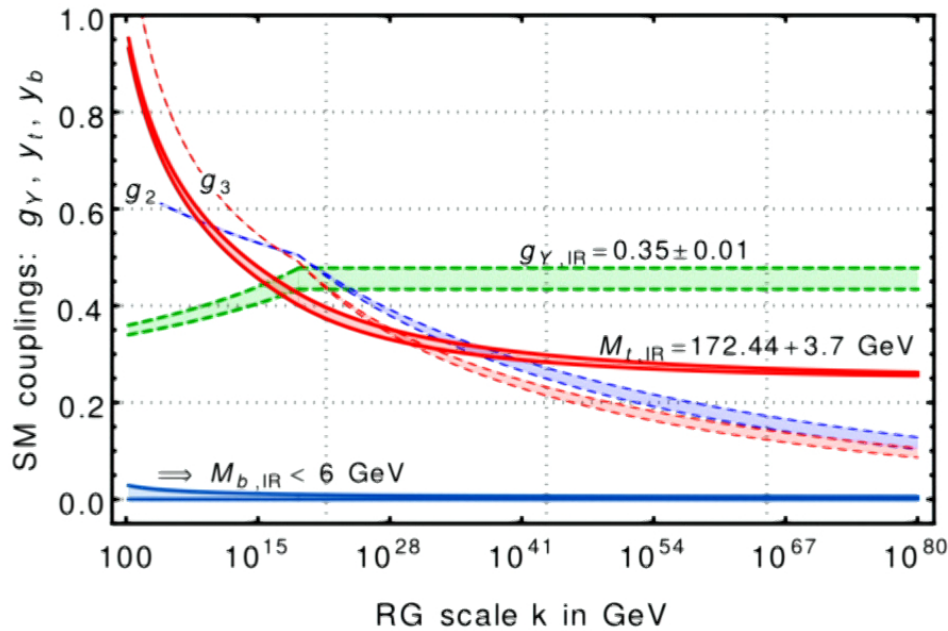
Outlook: hypercharges and mass-hierarchy

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$f_g(g_Y, \text{IR})$
 $f_y(M_t, \text{IR})$ fixed

recall

$\frac{y_t^{2*}}{g_Y^{2*}} \simeq \frac{1}{3}$ guarantees a large hierarchy



$g_Y^{2*} \simeq 3y_t^{2*}$

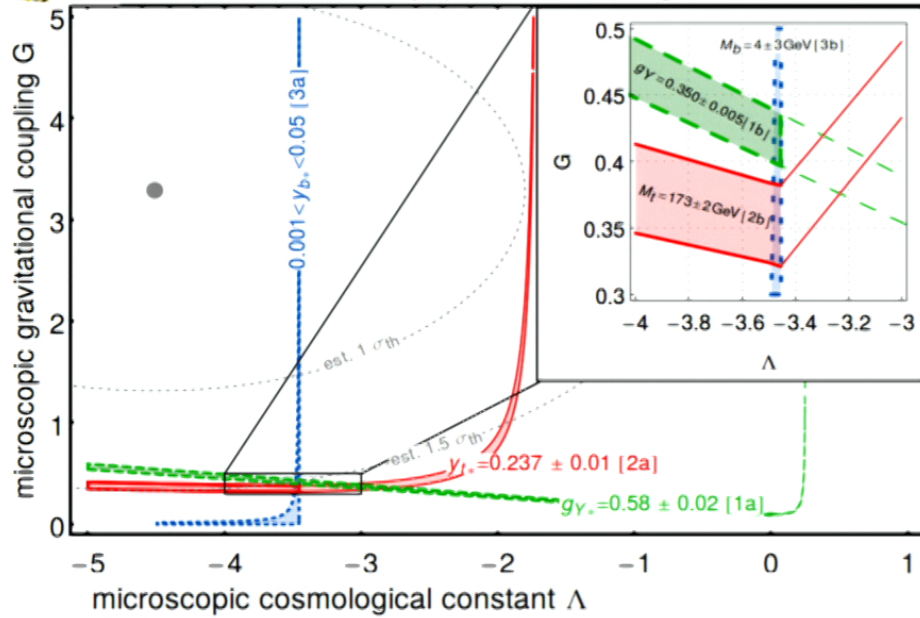
in the gravitating Standard Model

A gravitating Standard Model could also predict a significant top-bottom mass-difference

Eichhorn, Held, in prep.



Outlook: hypercharges and mass-hierarchy



Theory:

[1a] Eichhorn, Held,
1707.01107 (2017)

[2a] Eichhorn, Versteegen,
1709.07252 (2017)

[3a] Eichhorn, Held,
in prep. (2017)

Experiment:

[1b] $g_{Y,exp} = 0.3497$
Buttazzo et. Al. (2013)

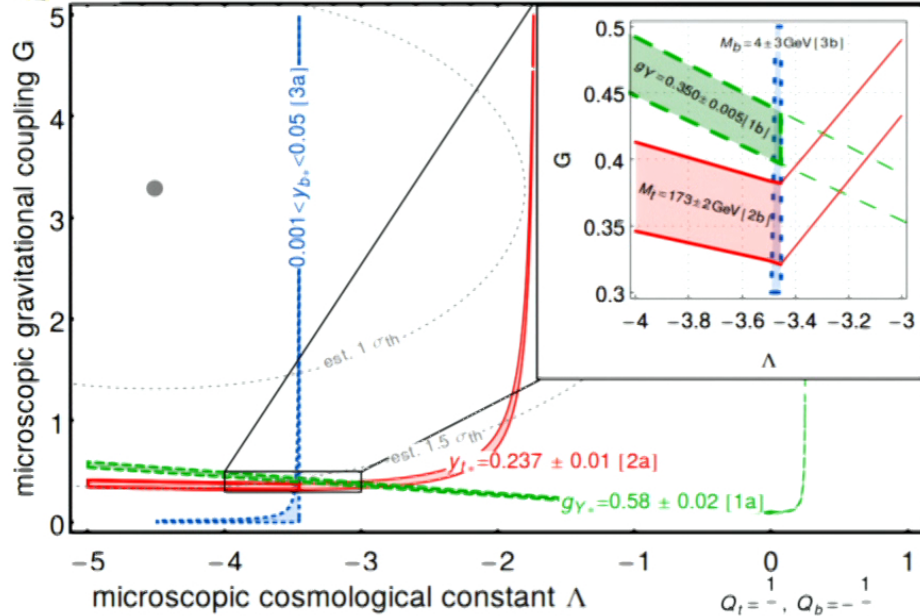
[2b] $M_{t,exp} = 172.35 \pm 0.64$
CMS, Phys.Rev. D93 (2016)

[3b] $M_{b,exp} = 4.18 \pm 0.03$
PDG, Phys.Rev. D86 (2012)

Eichhorn, Held, in prep.



Outlook: hypercharges and mass-hierarchy



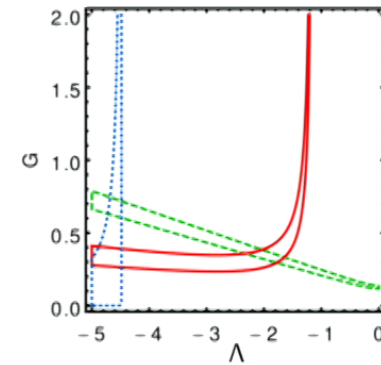
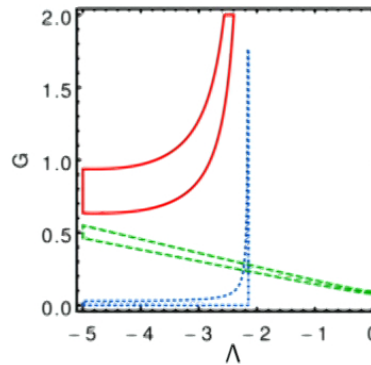
- Theory:
- [1a] Eichhorn, Held, 1707.01107 (2017)
 - [2a] Eichhorn, Versteegen, 1709.07252 (2017)
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PDG, Phys.Rev. D86 (2012)

Eichhorn, Held, in prep.

$$\Rightarrow \left(g_Y^*, y_t^*, y_b^* \right) (G_N, \Lambda)$$

only works for electric charges of the SM

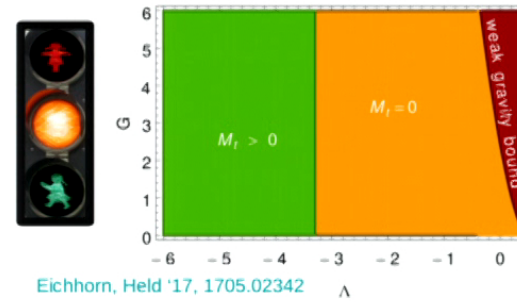
$$Q_t = \frac{2}{3}, Q_b = -\frac{1}{3}$$



21

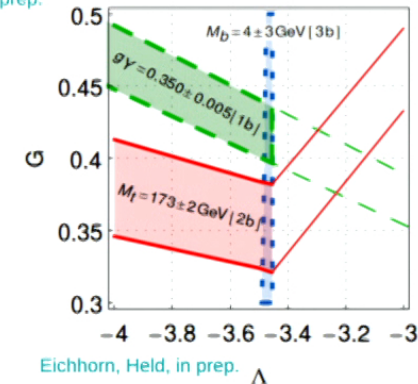
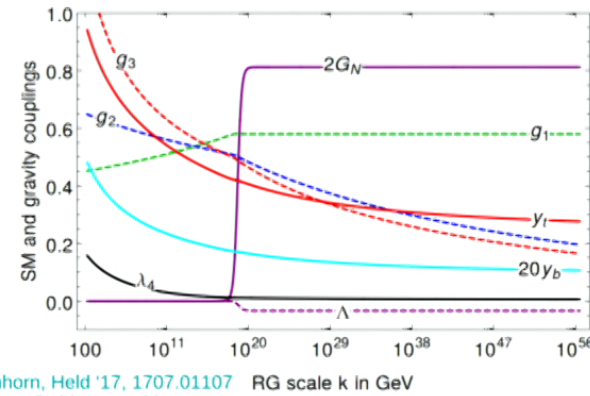
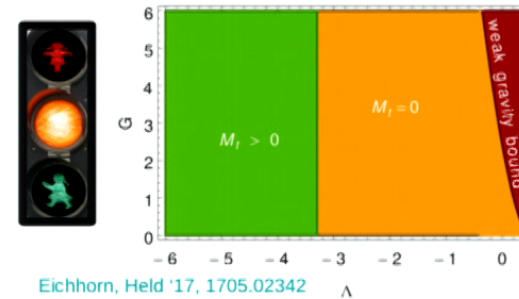
Conclusions

- viability of matter-gravity systems constrains quantum gravity:
weak-gravity bound



Conclusions

- viability of matter-gravity systems constrains quantum gravity: **weak-gravity bound**
- asymptotically safe quantum gravity could **UV-complete the Standard Model** (or GUTs)
- **higher predictive power** than the Standard Model (~~fewer 19~~ free parameters)
 g_1, M_t, M_b



Conclusions

- viability of matter-gravity systems constrains quantum gravity:

weak-gravity bound

- asymptotically safe quantum gravity could **UV-complete the Standard Model** (or GUTs)

- higher predictive power** than the Standard Model

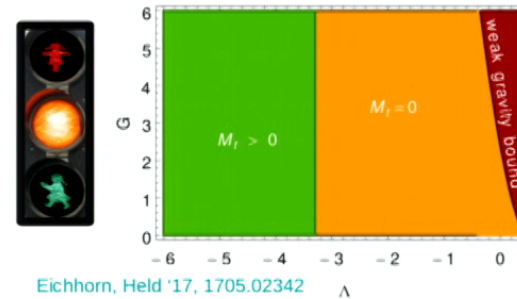
(**fewer** ~~10~~ free parameters)

g_1, M_t, M_b

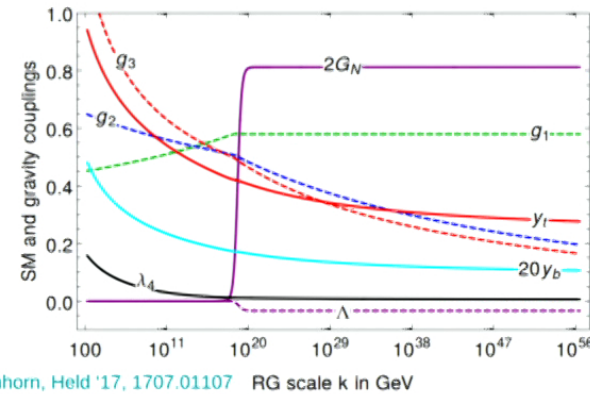
- convergence** of FP values for microscopic gravity couplings **needs to be studied in the future**



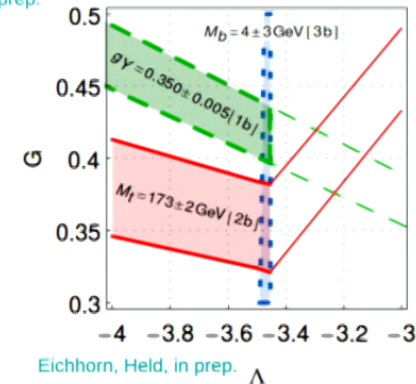
– Thank you for your attention. –



Eichhorn, Held '17, 1705.02342



Eichhorn, Held '17, 1707.01107
Eichhorn, Held, in prep.



Eichhorn, Held, in prep.