

Title: Uber-Gravity and H0 tension

Date: Aug 29, 2017 11:00 AM

URL: <http://pirsa.org/17080076>

Abstract: Recently, the idea of taking ensemble average over gravity models has been introduced. Based on this idea, we study the ensemble average over (effectively) all the gravity models dubbing the name uber-gravity which is a fixed point in the model space. The uber-gravity has interesting universal properties, independent from the choice of basis: i) it mimics Einstein-Hilbert gravity for high-curvature regime, ii) it predicts stronger gravitational force for an intermediate-curvature regime, iii) surprisingly, for low-curvature regime, i.e. $R < R_0$ where R is Ricci scalar and R_0 is a given scale, the Lagrangian vanishes automatically and iii) there is a sharp transition between low- and intermediate-curvature regimes at $R=R_0$. Finally, we will study the cosmology of this model and argue it can reduce to a cosmology model named "either Lambda or CDM" which is even simpler than standard LCDM. This model can address H0 tension and is distinguishable from LCDM in its prediction for the perturbations.



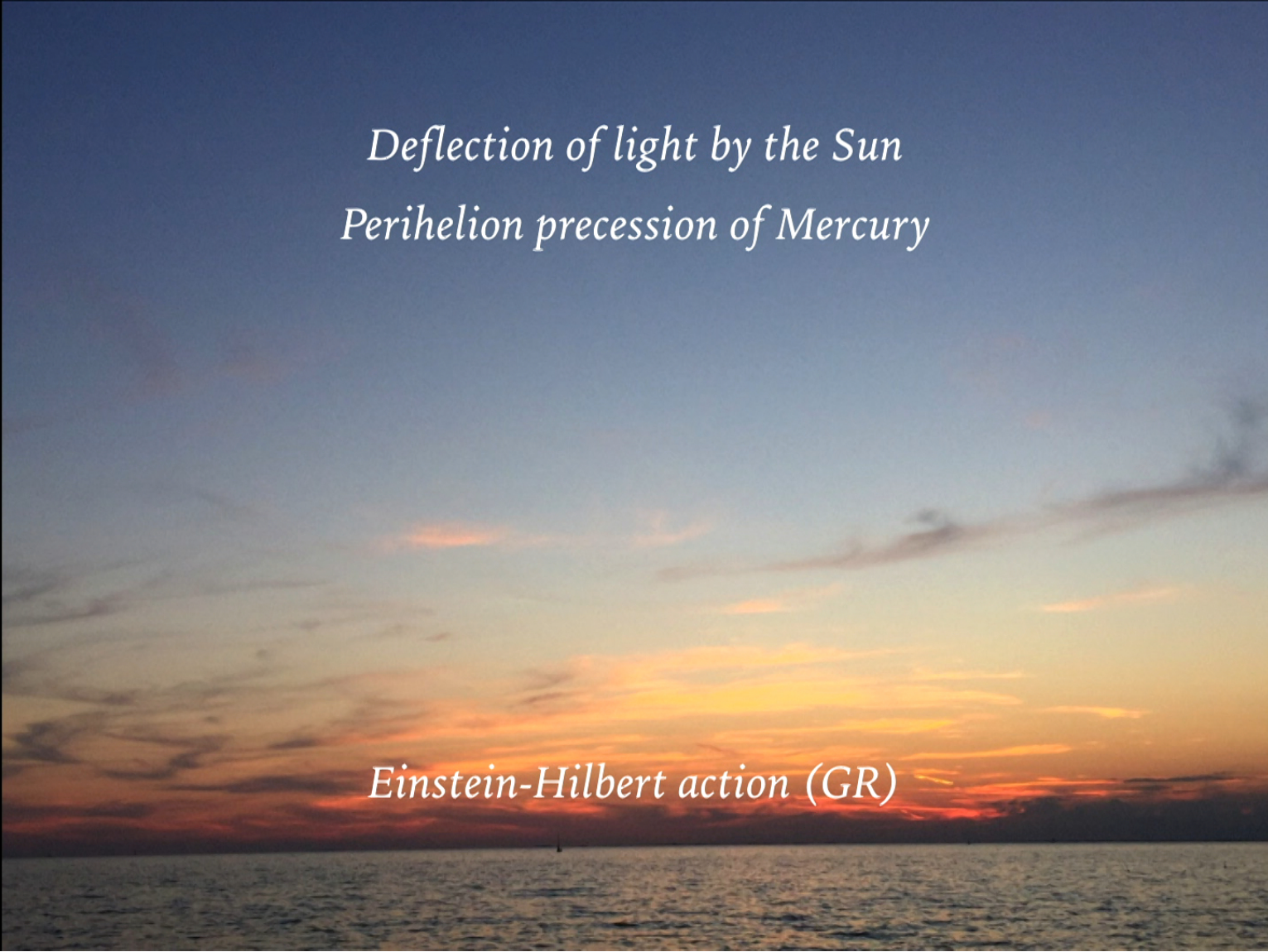
UBER-GRAVITY AND H_0 PROBLEM

Nima Khosravi

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29 August 2017 — Perimeter Institute



A photograph of a sunset over the ocean. The sky is a mix of blue, orange, and yellow, with some clouds. The water is dark blue with small waves. A small boat is visible on the horizon. The text is overlaid on the image.

Deflection of light by the Sun
Perihelion precession of Mercury


Einstein-Hilbert action (GR)



Late-time acceleration

GR cannot explain it?

so we modify GR by adding a cosmological constant

A photograph of a sunset over the ocean. The sky is a mix of blue, orange, and yellow, with some clouds. The ocean is dark blue with small waves. A small boat is visible on the horizon. The text "Lambda and CDM" is centered in the image.

Lambda and CDM

? H_0 tension

? σ_8 tension

? void phenomenon

? missing satellite problem

Lambda and CDM

? the cosmological constant problem

? why GR should govern gravity force

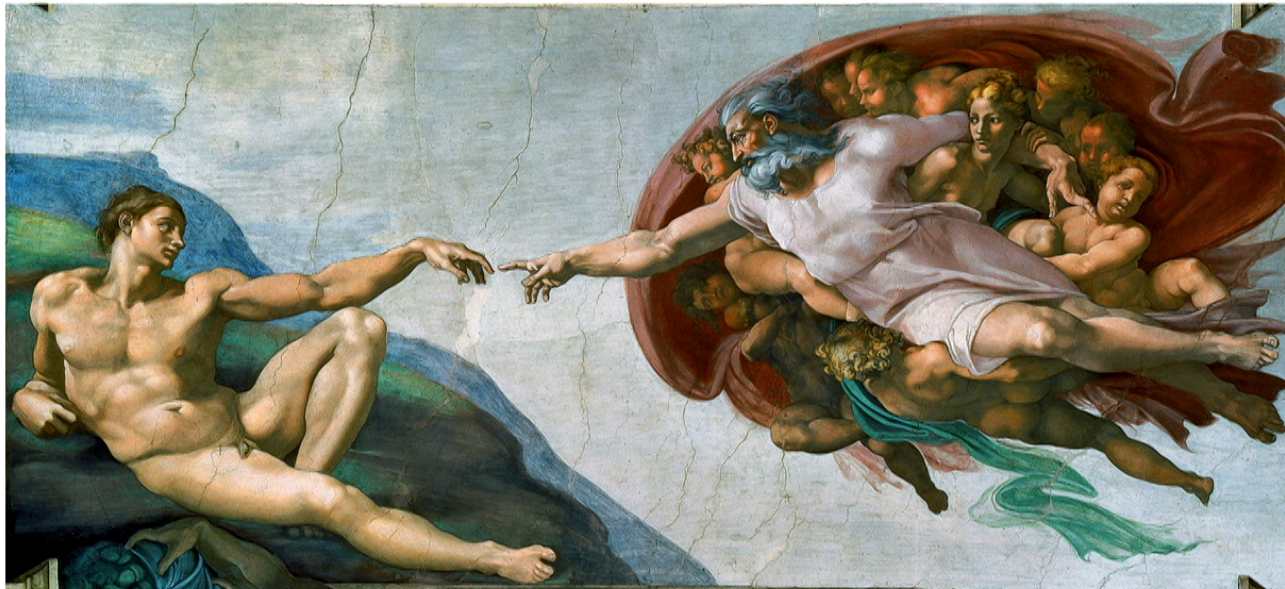
ENSEMBLE AVERAGE THEORY OF GRAVITY

► A. Einstein:

“What really interests me is whether God had any choice in the creation of the World”

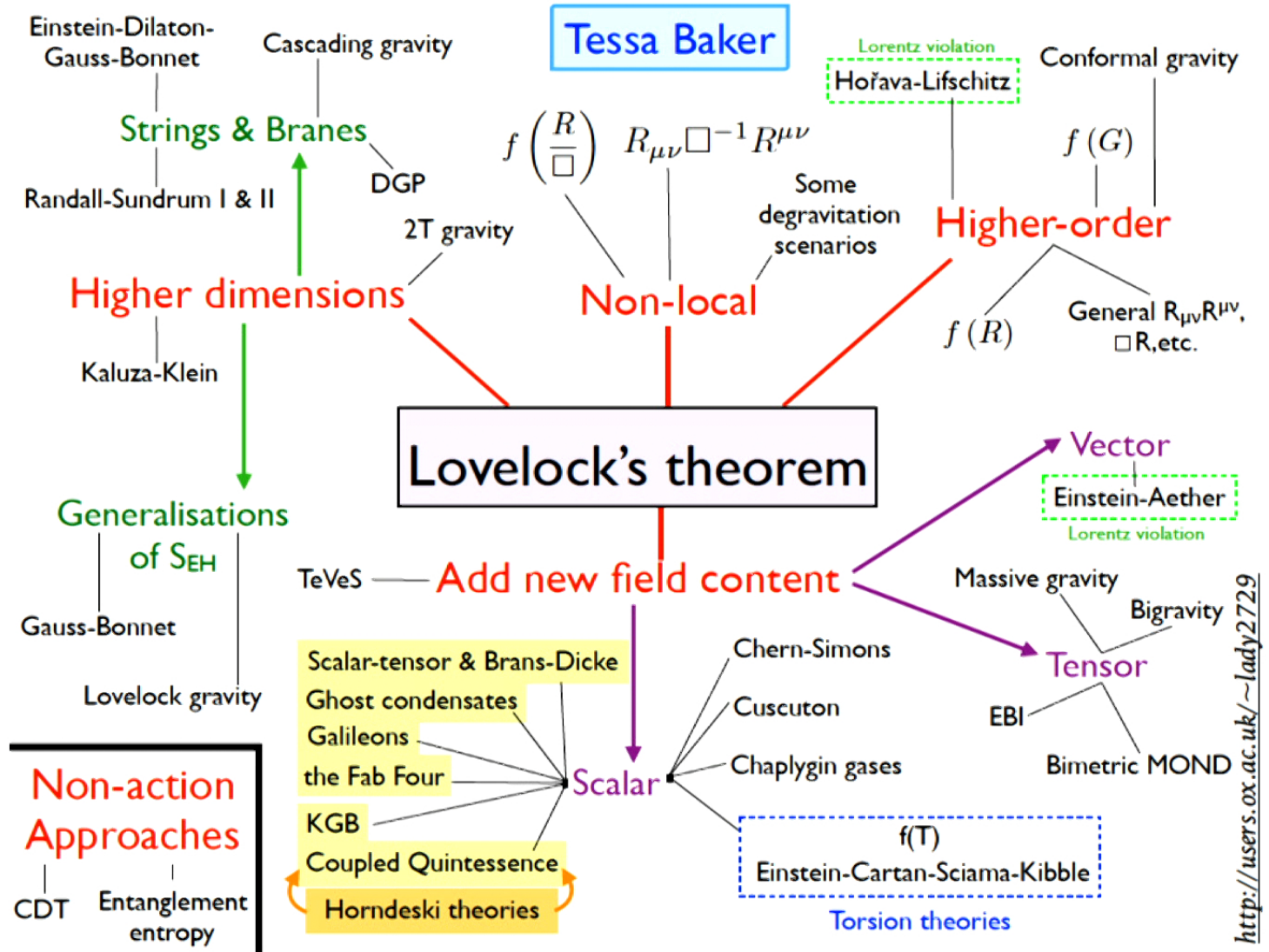
— THE FIRST DAY: IT WAS ASKED FOR A THEORY!

the creation of Adam, Michelangelo:



A. Einstein:

“What really interests me is whether God had any choice in the creation of the World”



— EUREKA: THE ANSWER IS “AVERAGING”!

death of Socrates, David:



ENSEMBLE AVERAGE THEORY OF GRAVITY

- ▶ let's recall Einstein quote:
“What really interests me is whether God had any choice in the creation of the World”

- ▶ what is your answer to his question?
 - no! → why not? why GR is unique?
 - yes! → how can we check this “yes”?
 - it is not a well-defined question! → see you at break!

ENSEMBLE AVERAGE THEORY OF GRAVITY

- what is my answer to his question?
 - my answer to this question is “yes” and “no” both!
 - “yes”: all the theoretically consistent models have been used in the creation of the World!
 - “no”: at the end there is just a “unique model” which is the “ensemble average” of all the theoretically possible models!
- based on PRD 94 (2016) 124035, arXiv:1606.01887
- for a very similar idea see also: N. Arkani-Hamed et al., PRL 117 (2016) 251801, arXiv:1607.06821

ENSEMBLE AVERAGE THEORY OF GRAVITY

\mathcal{M}

the space of all the (consistent) models for gravity!

- ▶ we take average over all the models
- ▶ to do this we need to assigned to each model a probability

$$\mathcal{M} = \sum_i p_i \mathcal{M}_i = \frac{1}{\sum_j e^{-S_j}} \times \sum_i e^{-S_i} \mathcal{M}_i$$

ENSEMBLE AVERAGE THEORY OF GRAVITY

- ▶ an example: higher order gravity
- ▶ in 4-dimension we have Ricci scalar and Gauss-Bonnet term

$$\mathcal{L} = \sqrt{-g} \left[\frac{M^2 R e^{-\beta M^2 R}}{e^{-\beta M^2 R} + e^{-\beta \alpha G}} + \frac{\alpha G e^{-\beta \alpha G}}{e^{-\beta M^2 R} + e^{-\beta \alpha G}} \right]$$

Ricci scalar

Gauss-Bonnet term

temperature of model space??

$$f(R, G)$$

$$f_{RR} f_{GG} - f_{RG}^2 = 0$$

$$\begin{cases} f(R) + G \\ f(G) + R \end{cases}$$

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UBER-GRAVITY

- ▶ based on “Uber-Gravity and the CPP”, arXiv:1703.02052
- ▶ a generalization of EAT-of-Gravity for all analytical functions of $f(\mathbb{R})$. so we have

$$\mathbb{M} = \{R^n \mid \forall n \in \mathbb{N}\}$$

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$$\mathbb{M} = \{R^n \mid \forall n \in \mathbb{N}\}$$

$$\mathcal{L} = \left(\sum_{n=1}^{\infty} \bar{R}^n e^{-\beta \bar{R}^n} \right) / \left(\sum_{n=1}^{\infty} e^{-\beta \bar{R}^n} \right)$$

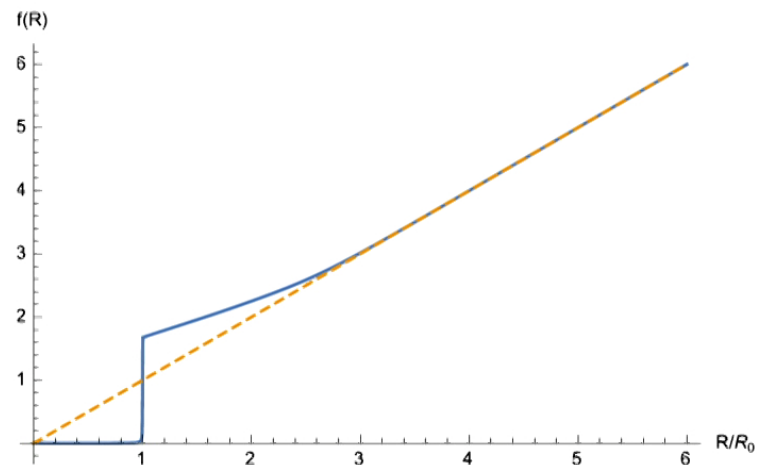
$$f(R, G) \quad \bar{R} \equiv \frac{P}{R} \quad \left\{ \begin{array}{l} f_{1R} \text{ \& } f_{1RR} > 0 \\ R > R_0 \end{array} \right.$$

$$f_{1RR} f_{2GG} - f_{1RG}^2 = 0$$

$$\left\{ \begin{array}{l} f(R) + G \\ f(G) + R \end{array} \right.$$

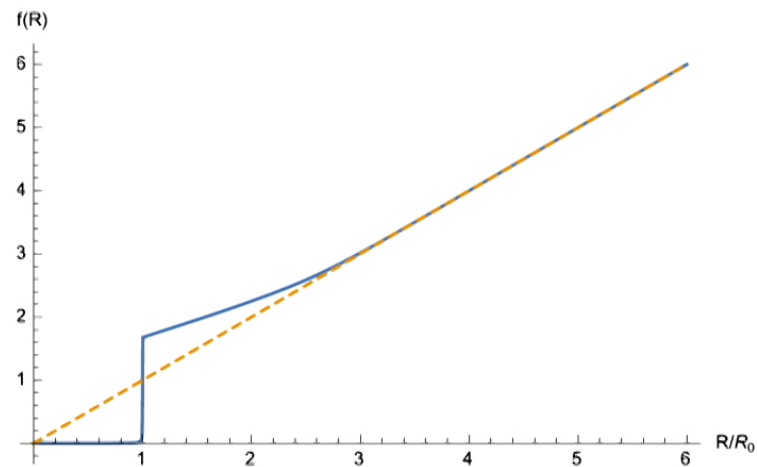
UBER-GRAVITY: UNIVERSAL PROPERTIES

- ▶ for high-curvature regime it reduces to GR
- ▶ for intermediate-curvature regime it predicts stronger gravity than GR
- ▶ it is vanishing for low-curvature regime ($R < R_0$)
- ▶ there is a sharp transition at R_0



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UBER-GRAVITY: A SIMPLIFIED MODEL

$$f(R) = \begin{cases} \bar{R}^n & R \leq R_0 \\ \bar{R} + e^{-(\bar{R}-0.7)} & R_0 < R \end{cases}$$

we focus on low-curvature regime. we have

$$(n - 2)\bar{R}^n + 3n R_0^{-1} \square \bar{R}^{n-1} = \kappa^2 T$$

and for $R = \text{const.}$ we have

$$\frac{R}{R_0} = \left(\frac{\kappa^2 T}{n - 2} \right)^{\frac{1}{n}}$$

which means for $n \rightarrow \infty$ results in $R \rightarrow R_0$!!

this means there is no need to fine-tuning since this model is not sensitive to vacuum energy.

? H_0 tension

? σ_8 tension

? void phenomenon

? missing satellite problem

Uber-Gravity

LAMBDA XOR CDM MODEL:

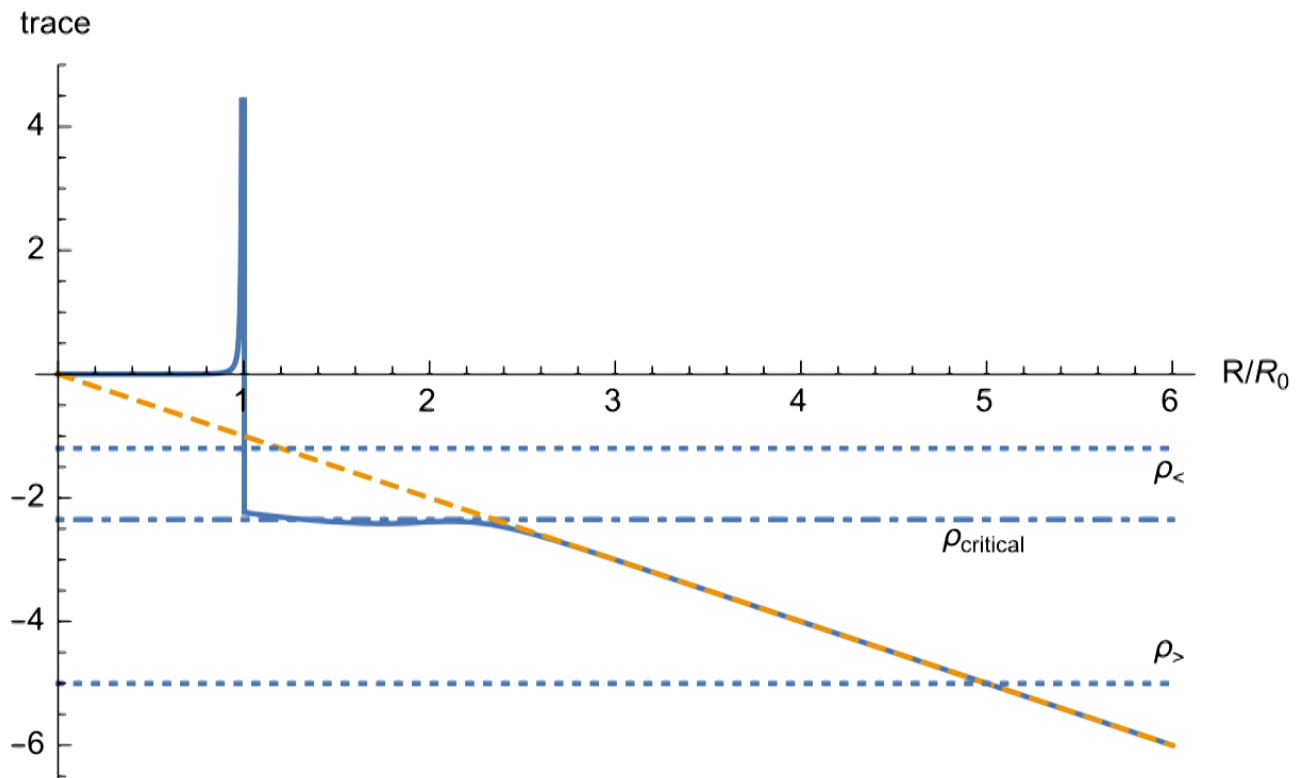
note: this part has been done in collaboration with

Shant Baghram

Sharif University of Technology, Tehran, Iran



UBER-GRAVITY: FULL MODEL



LAMBDA XOR CDM MODEL:

- based on uber-gravity model we suggest the following cosmological model:

$$\text{Gravity} = \begin{cases} \text{de Sitter} & \rho < \rho_{critical} \\ \text{GR} + \text{CDM} & \rho > \rho_{critical} \end{cases}$$

which is dubbed as “either Lambda or CDM”:

$\Lambda \oplus$ CDM MODEL

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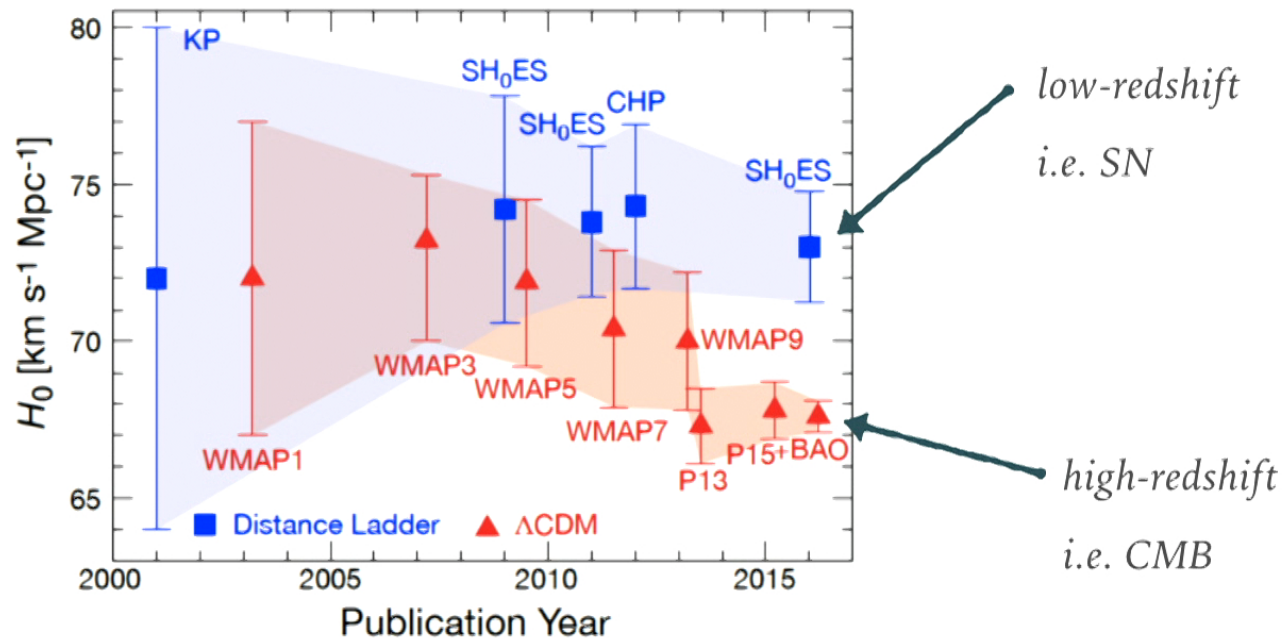
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LAMBDA XOR CDM MODEL: BACKGROUND

The Hubble Constant



NORDITA July 27, 2017

Rachael L. Beaton

Freedman 2017
Beaton et al. 2016

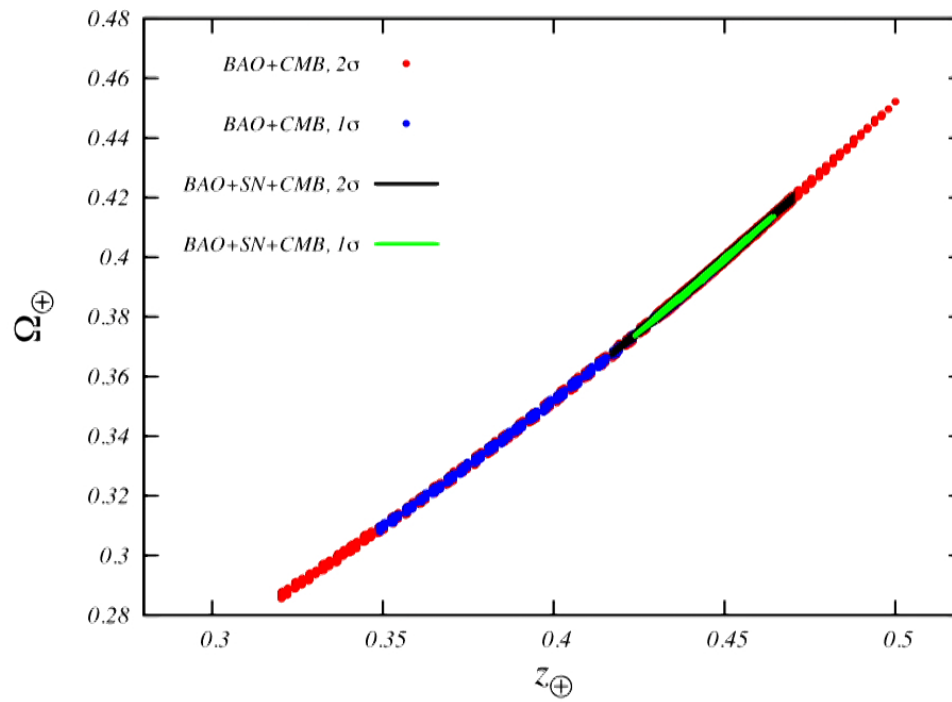
LAMBDA XOR CDM MODEL: BACKGROUND

$$E^2(z) \equiv \left(\frac{H(z)}{H_0^{low}} \right)^2 = \begin{cases} 1 & z < z_{\oplus} \\ \Omega_{m,\oplus} \left(\frac{1+z}{1+z_{\oplus}} \right)^3 & z > z_{\oplus} \end{cases}$$

$$\chi(z) = \frac{c}{H_0^{low}} \left[\int_0^{z_{\oplus}} dz + \int_{z_{\oplus}}^z \frac{dz}{\left(\Omega_{m,\oplus} \left(\frac{1+z}{1+z_{\oplus}} \right)^3 \right)^{1/2}} \right]$$

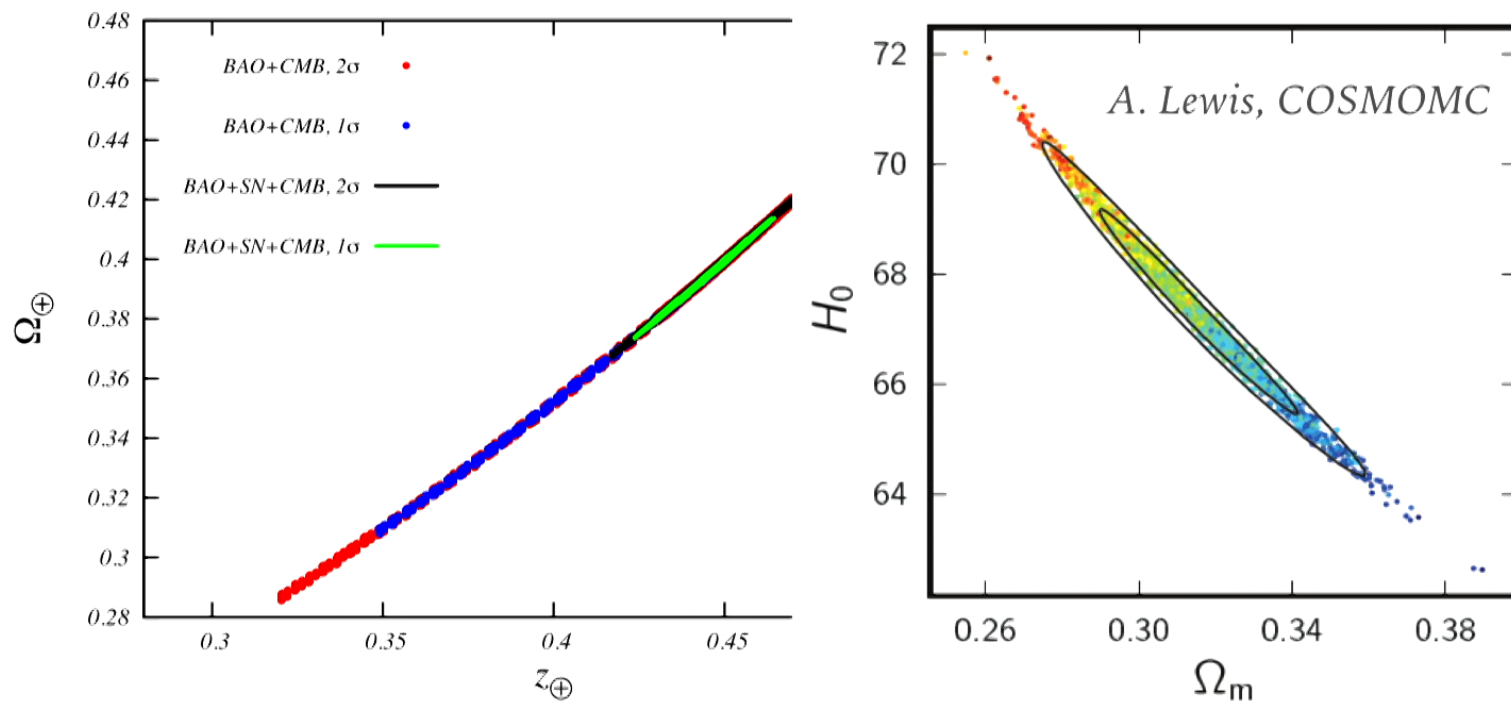
LAMBDA XOR CDM MODEL: BACKGROUND

by fitting $L_{xor}CDM$ with background data including SN, BAO and 1st CMB peak



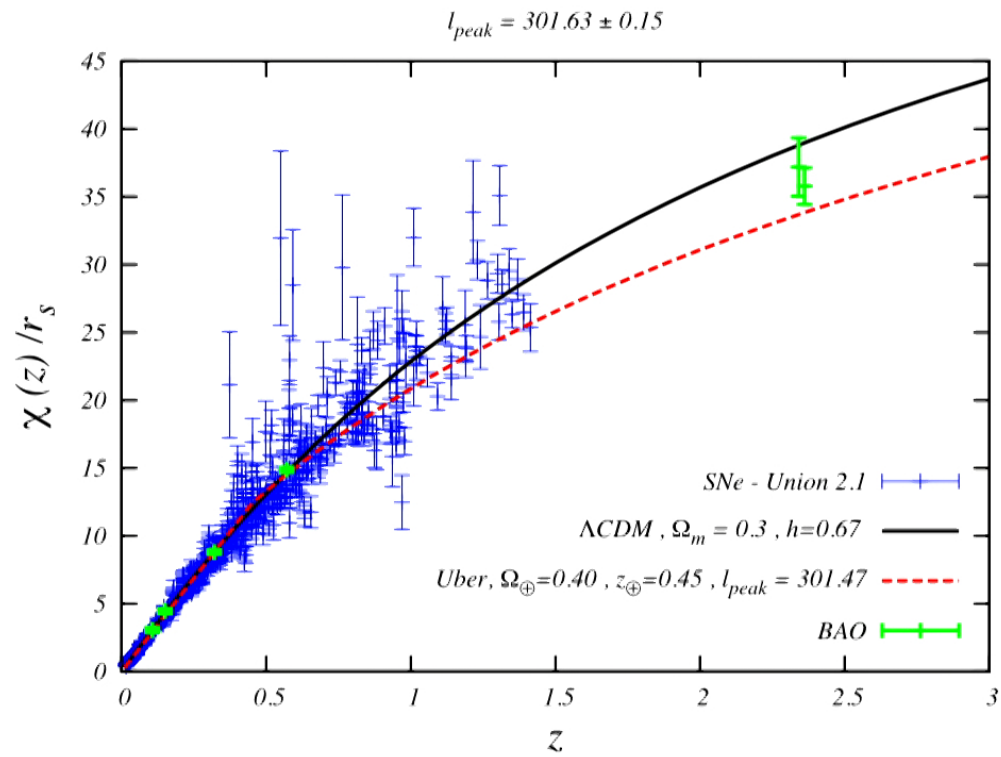
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LAMBDA XOR CDM MODEL: BACKGROUND

- ▶ flat LxorCDM has 3 free parameters Ω_m , H_0 and $z_{\text{transition}}$ which are related to R_0 and β in original uber-gravity model!
- ▶ we fixed $H_0 = 73$ km/sec/Mpc reported by Riess et al.
- ▶ we minimize χ^2 for z_t and Ω_m
- ▶ χ^2 is comparable with number of data points!

- ▶ LxorCDM automatically solves H_0 problem which was not obvious at the first look!

✓ H_0 tension

? void phenomenon

? σ_8 tension

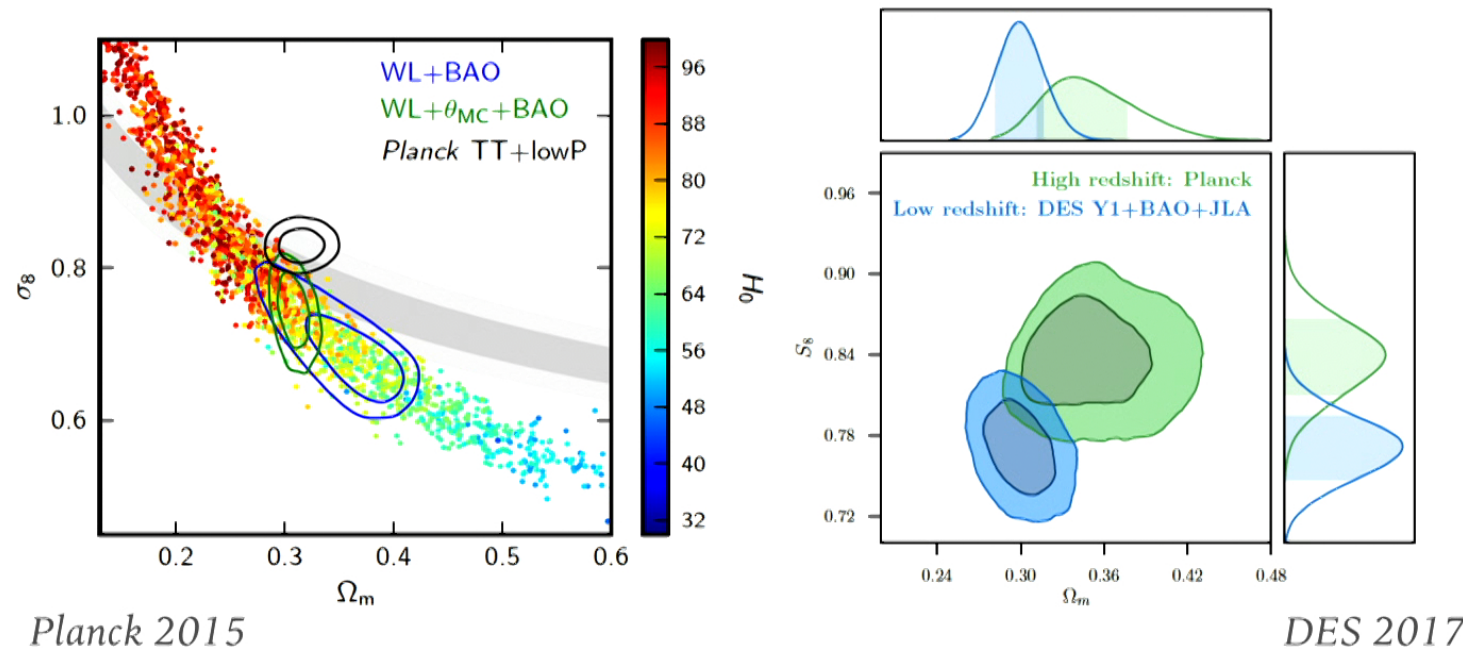
? missing satellite problem

Λ CDM (*background analysis*)
(Uber-Gravity)

LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

► σ_8 problem:

“Cosmic map reveals a not-so-lumpy Universe”, Nature on DES!



LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

in perturbation theory we need to find the redshift where the “total density” touches the critical density:

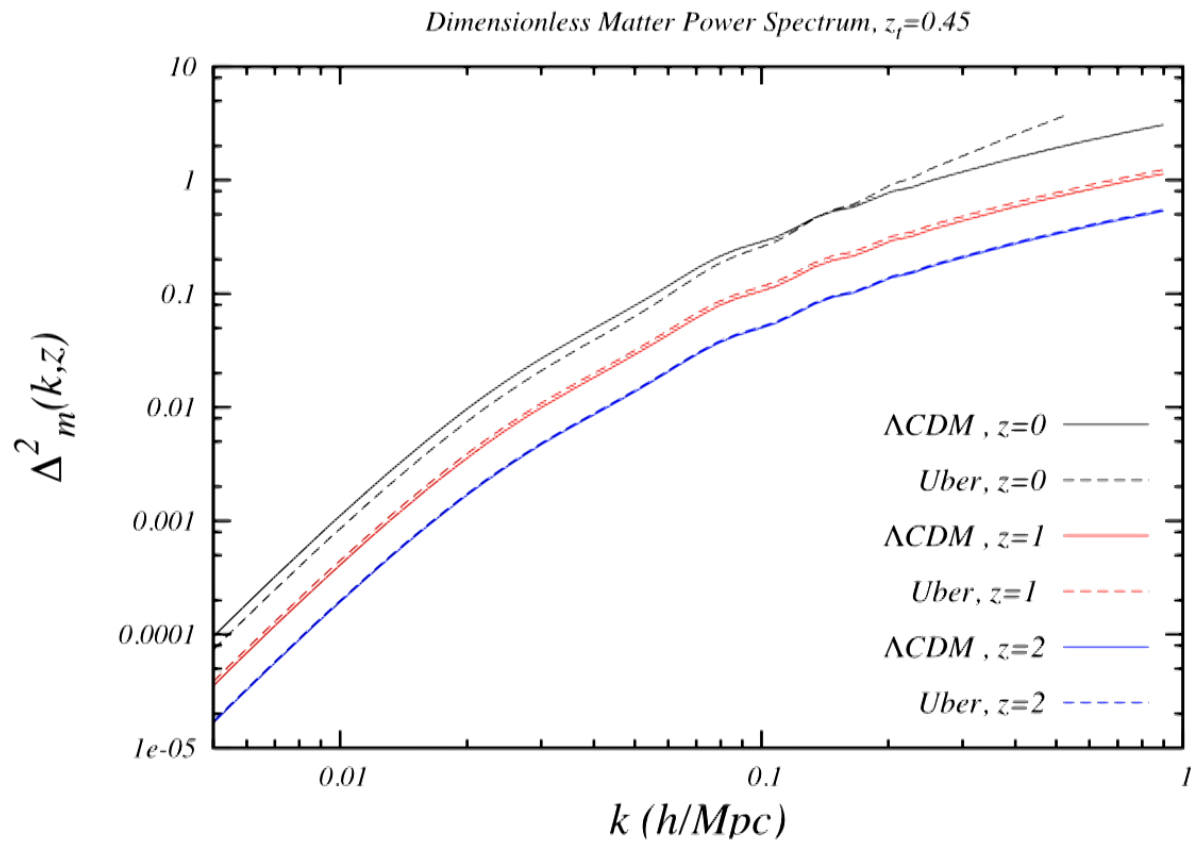
$$\bar{\rho}(z) \left[1 + \delta(k, z) \right] = \rho_{critical}$$

which is equivalent to:

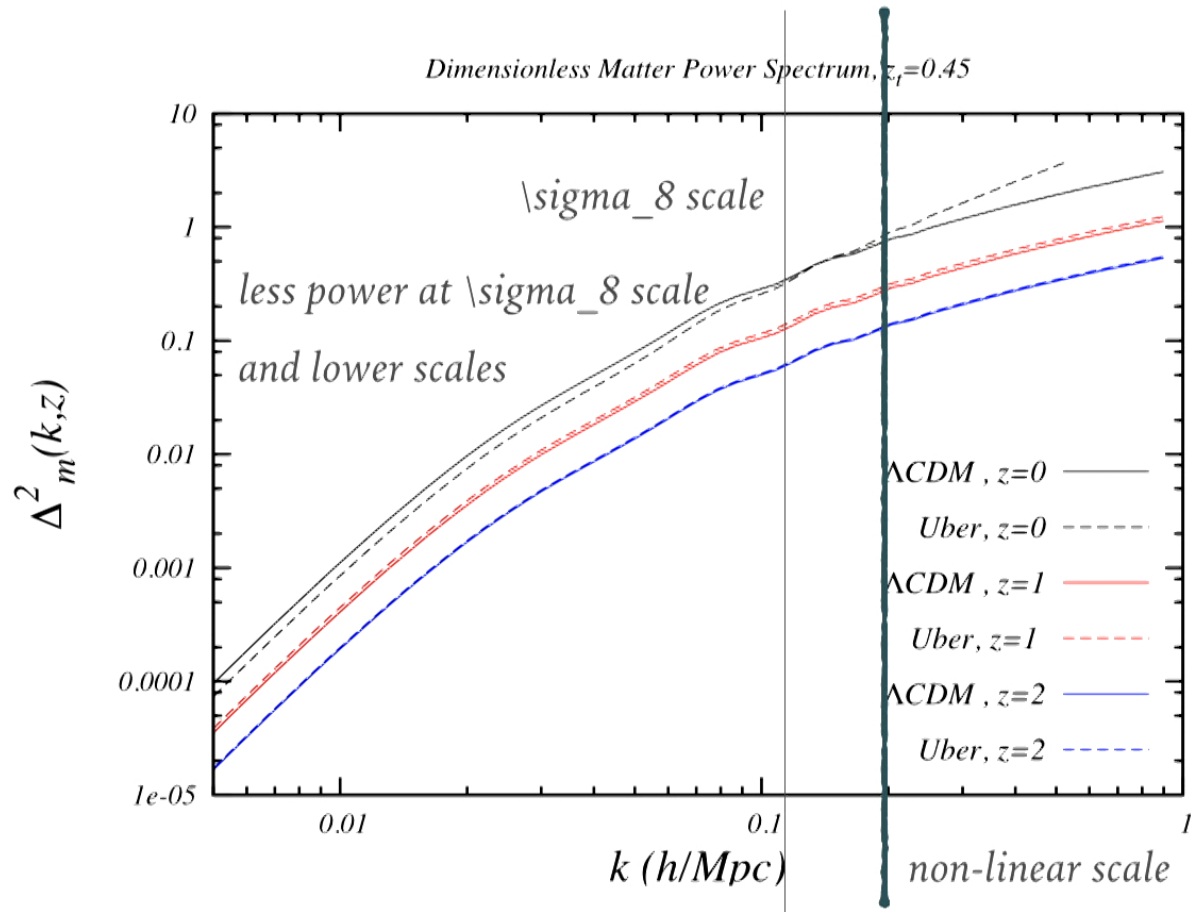
$$X^3 + A(k) X^2 = X_{\oplus}^3$$

for $X=1+z$ in deep CDM era!

LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS



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Λ xor CDM

(background, linear perturbation and non-linear analysis)

(Uber-Gravity)

? a fundamental way to define probabilities

Lambda and CDM (vanilla)

vs.

Lambda xor CDM (chocolate)



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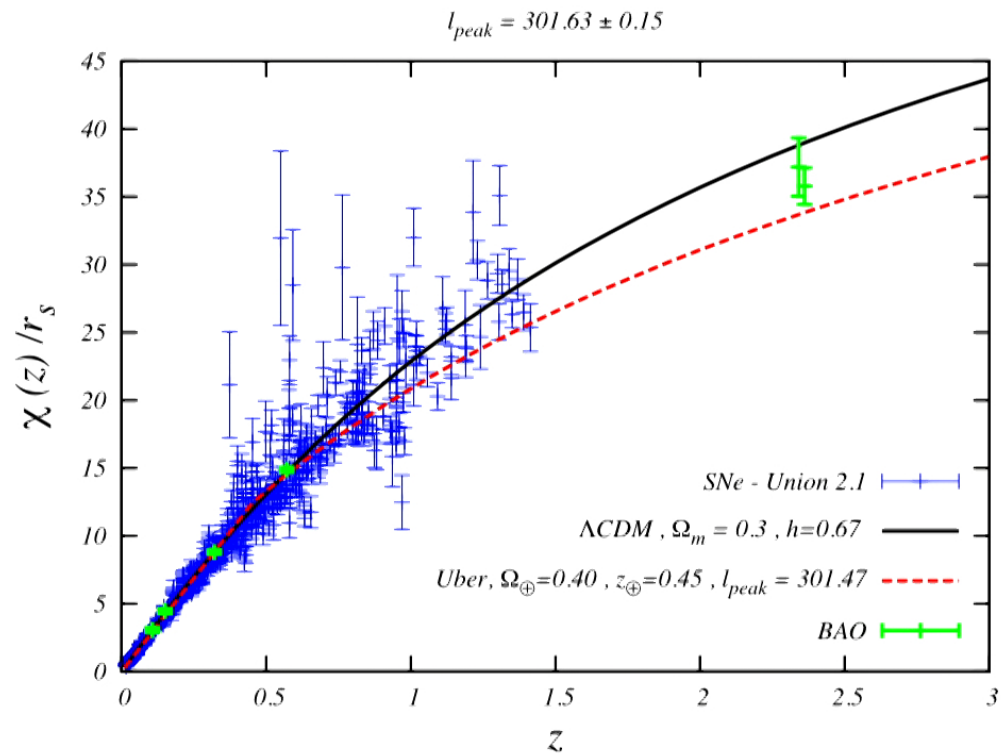
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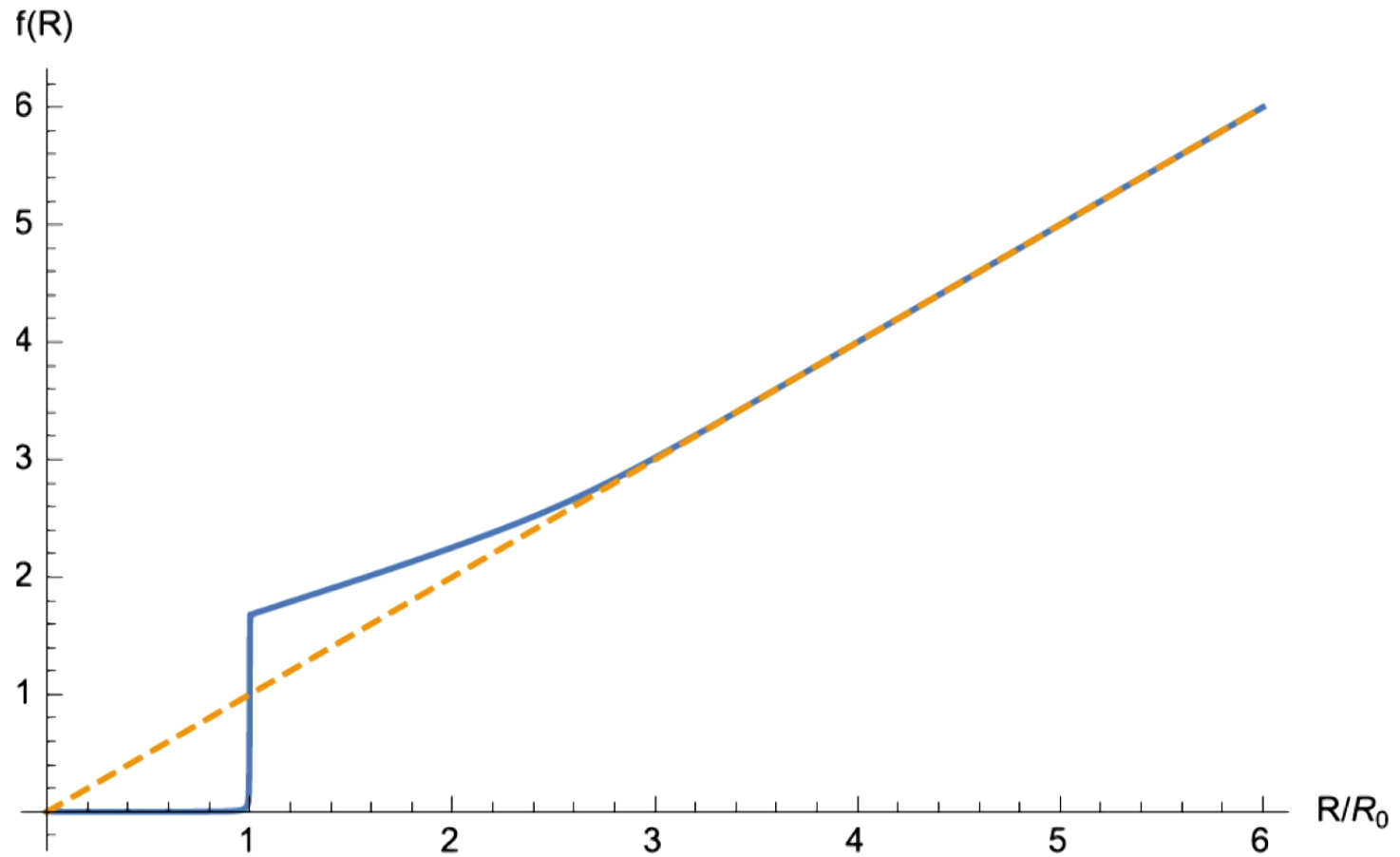
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