

Title: LTS dc-SQUID sensors for precision measurements in metrology and fundamental physics

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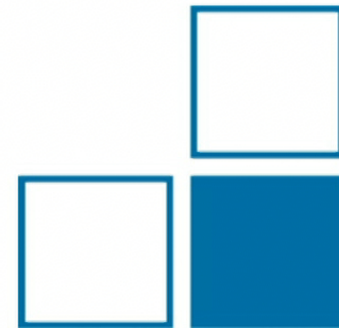
Abstract:



Physikalisch-Technische Bundesanstalt
Braunschweig und Berlin
Nationales Metrologieinstitut

LTS dc-SQUID sensors for precision measurements in metrology and fundamental physics

Jörn Beyer PTB Berlin



PTB Working Group 7.21 Cryosensors



LTS dc-SQUID sensors

- components, operation, parameters
- circuit and design aspects: *signal coupling, SQUID cascades*
SQUID arrays, flux trapping
- noise: excess magnetic flux noise at low temperatures

Sensors examples

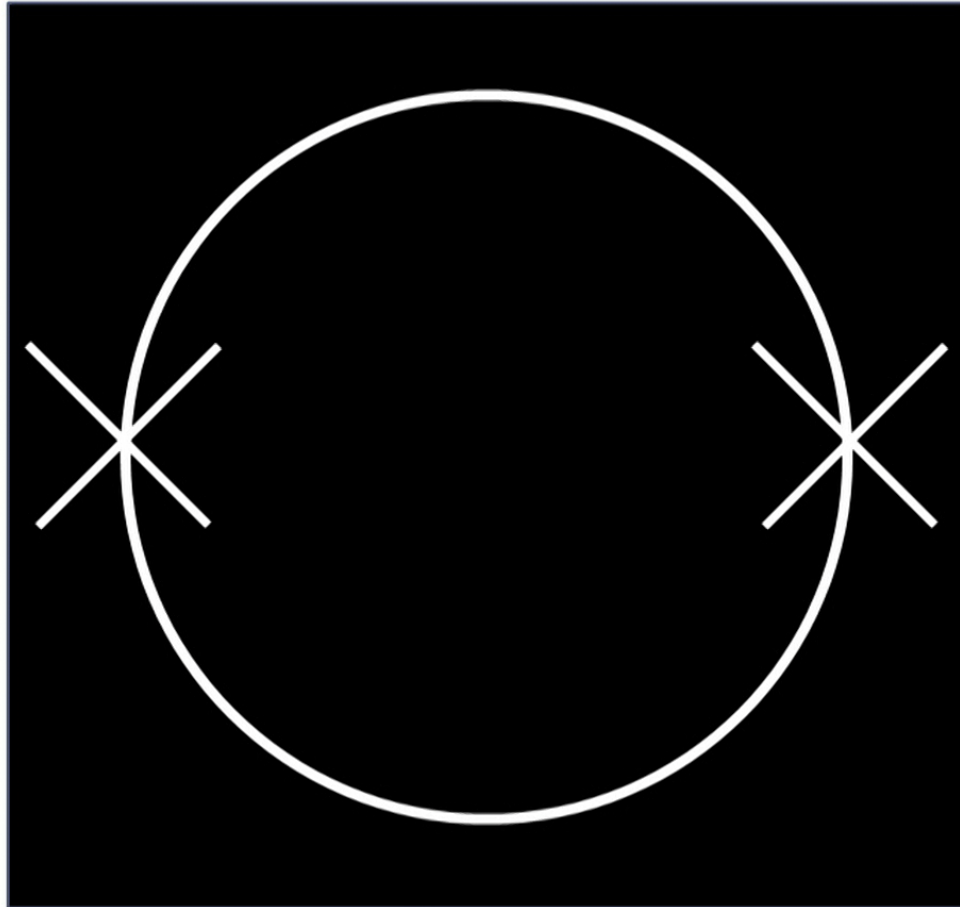
SQUID readout of TES optical photon counter for ALPS

SQUID sensors for wire-wound magnetometers

differential SQUID signal booster



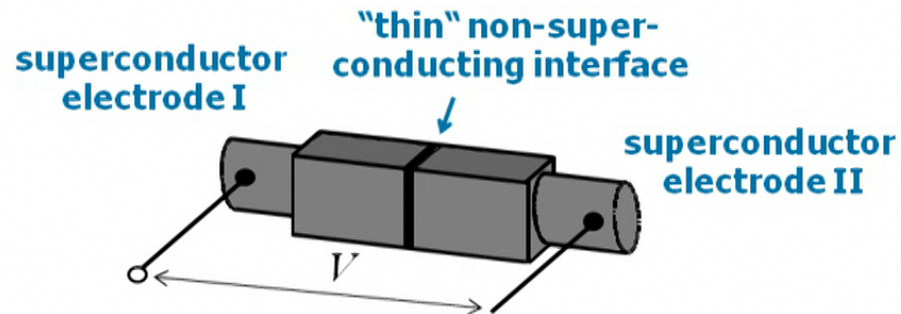
A dc-SQUID – 1 loop, 2 JJs



Superconductive tunneling



- What happens at a superconductor/superconductor contact?

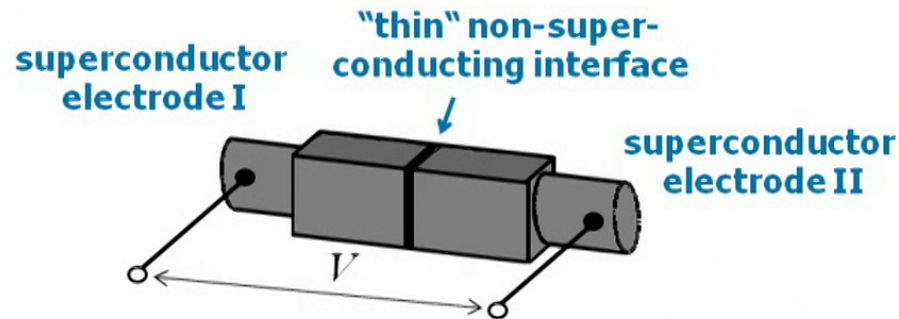


Brian D.
Josephson, 1962
*Possible new effects
in superconductive
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Phys. Lett. 1, 251

Superconductive tunneling



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- supercurrent I_c , $V = 0$
- mag. field dependence $I_c(B)$
- $V \neq 0 \Rightarrow$ ac current I_{ac} , $f_{ac} \propto V$

→ dc Josephson effect

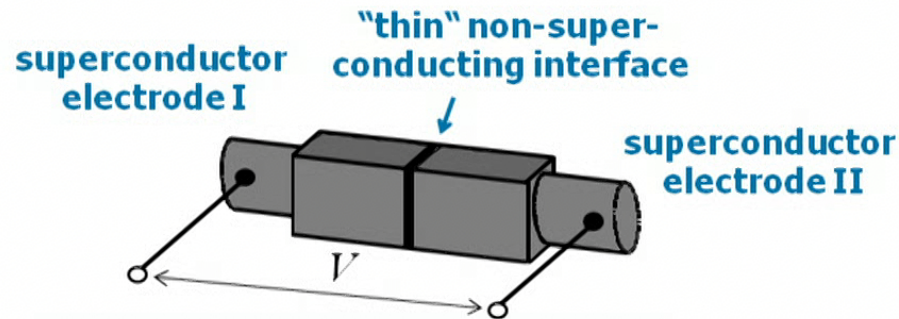
→ current-phase relation, $I_C = I_{Cmax} \sin(\phi)$

→ ac Josephson effect, $K_{J-90} = 483.597.. \text{ MHz}/\mu\text{V}$

Superconductive tunneling



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Josephson junction – JJ

- configuration of *weakly* coupled superconductors across non-superconductor
- insulator, normal metal, structurally modified superconductor, magnetic material, ...

Superconductive tunneling

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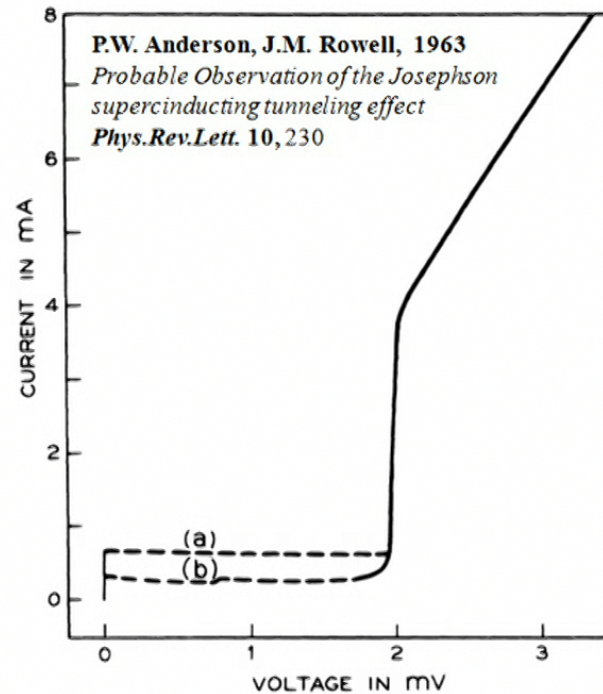


FIG. 1. Current-voltage characteristic for a tin-tin oxide-lead tunnel structure at $\sim 1.5^\circ\text{K}$, (a) for a field of 6×10^{-3} gauss and (b) for a field 0.4 gauss.

Superconductive tunneling

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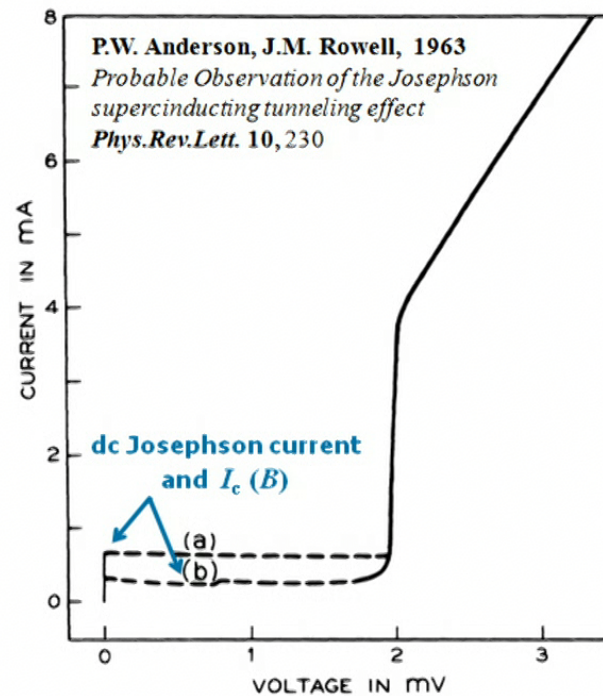


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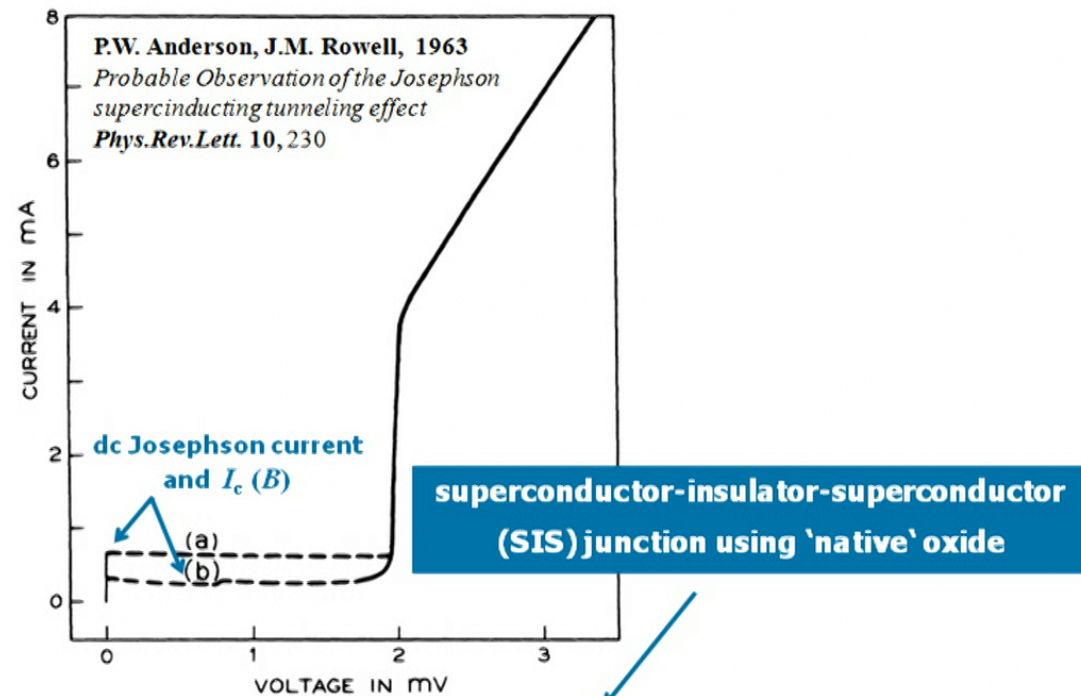
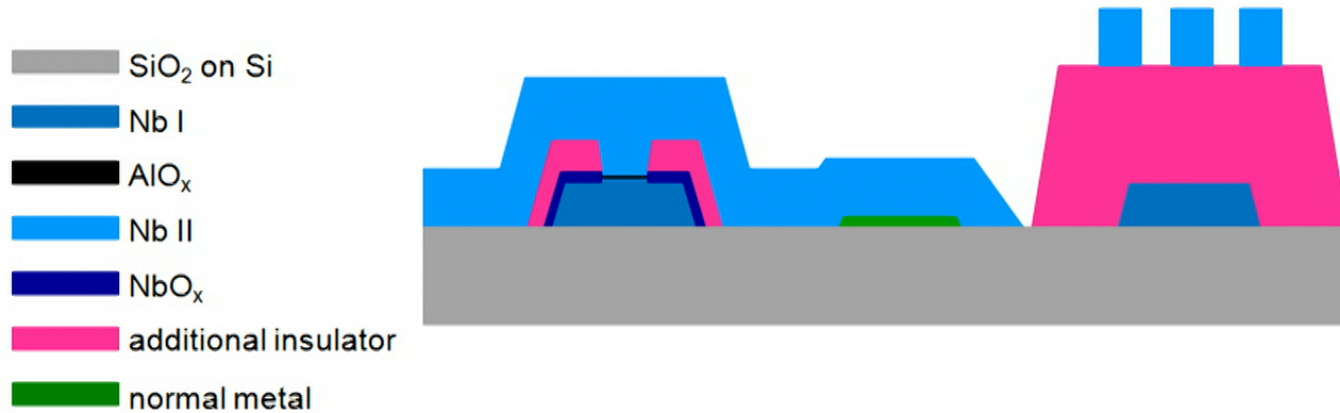


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JJs for superconducting devices



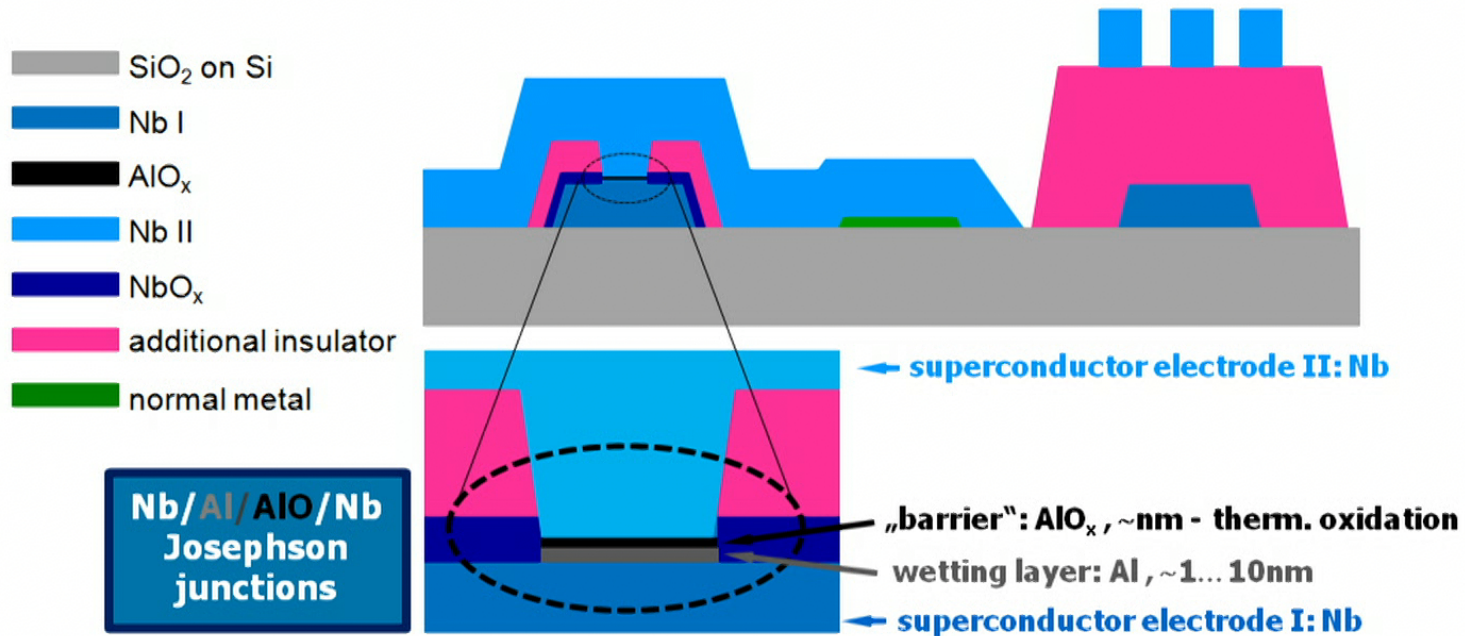
- Refractory metal SIS junctions – thin film process (PTB)



JJs for superconducting devices



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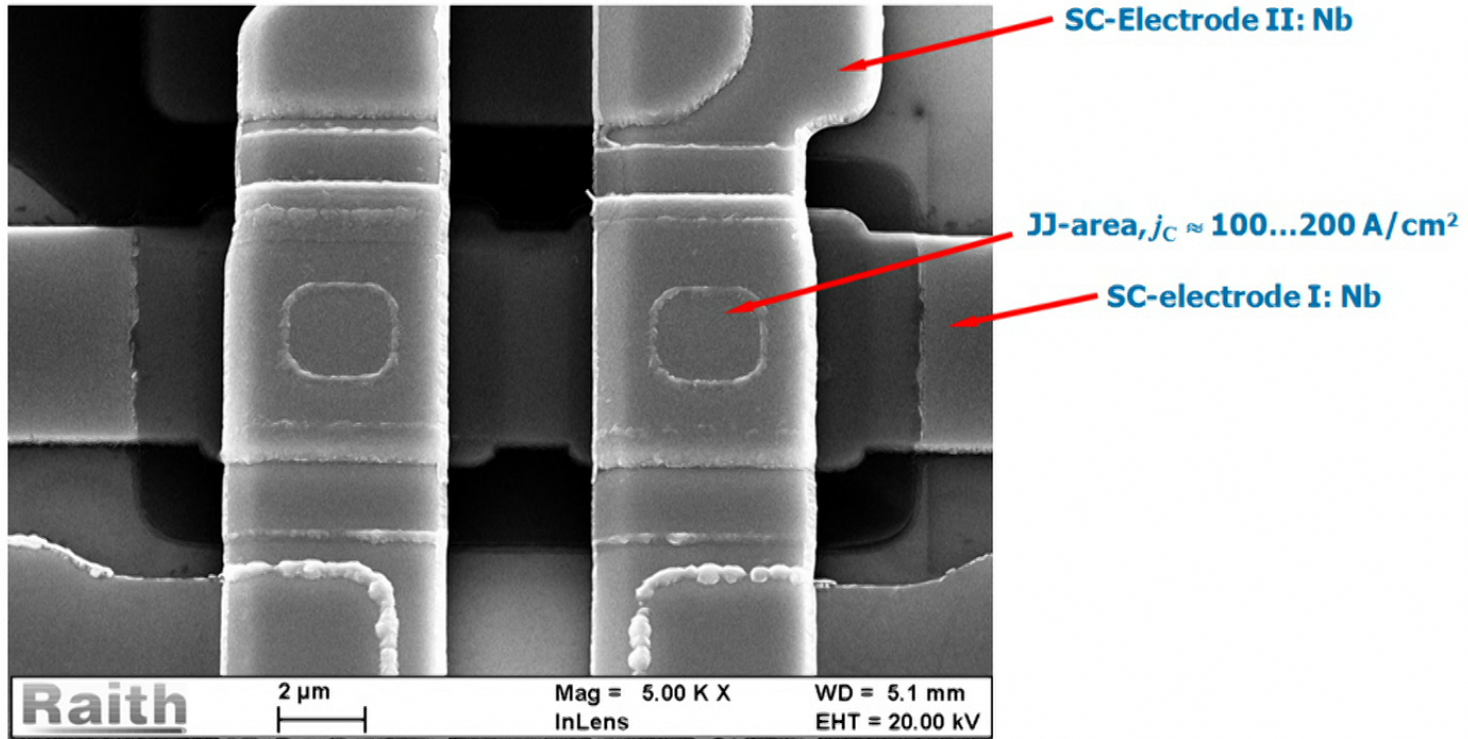


M. Gurvitch et al., 1983
*High quality refractory Josephson tunnel junctions
utilizing thin aluminium layers*
Appl. Phys. Lett. 42, 472

LTS dc-SQUID sensors

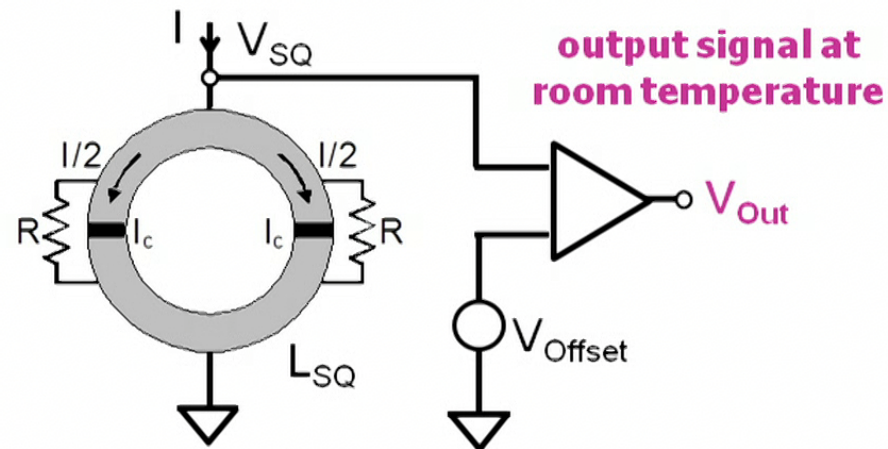


- Example: PTB SQUID fab process, UV contact lithography, min. feature size $\approx 2\mu\text{m}$



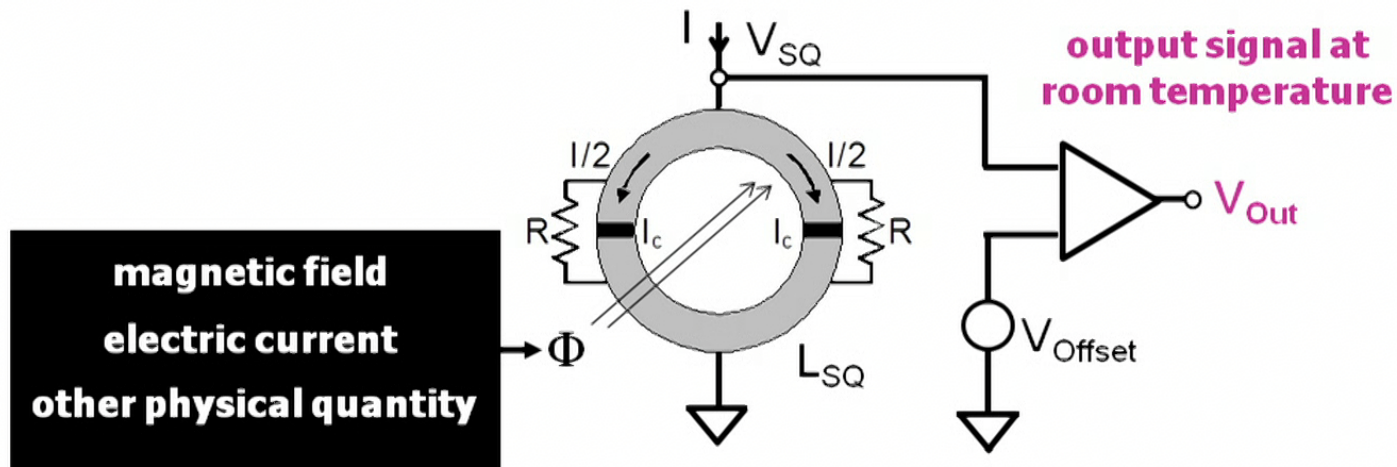
dc-SQUID sensors

- **superconductor ring interrupted by two Josephson junctions**
 - JJs: regions of weakened superconductivity with a critical current I_c
 - JJs resistively shunted with ohmic resistor R
- **sensor of magnetic flux Φ through the SQUID ring of inductance L_{SQ}**



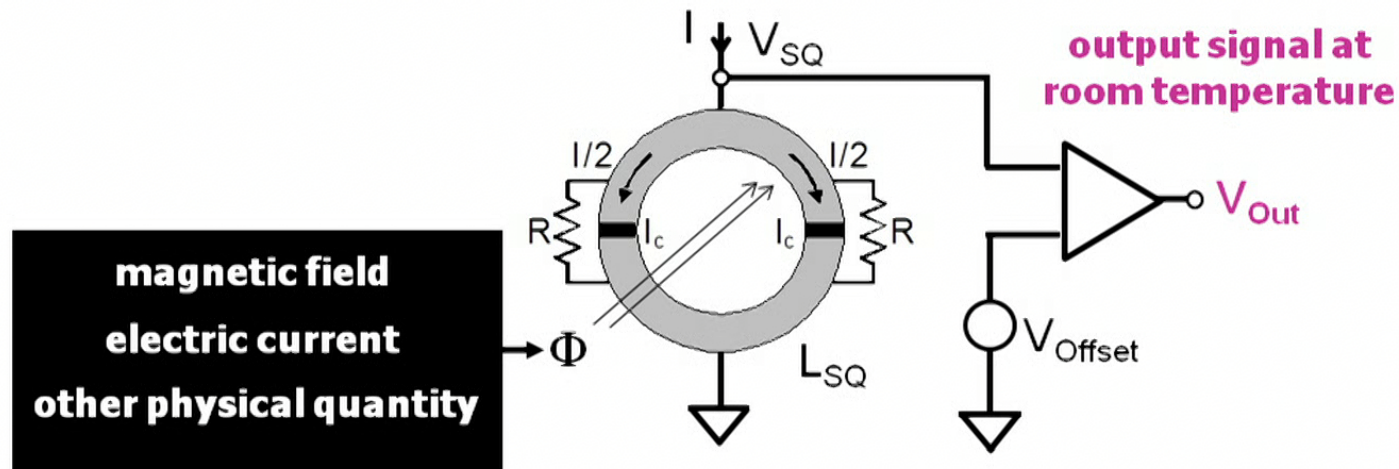
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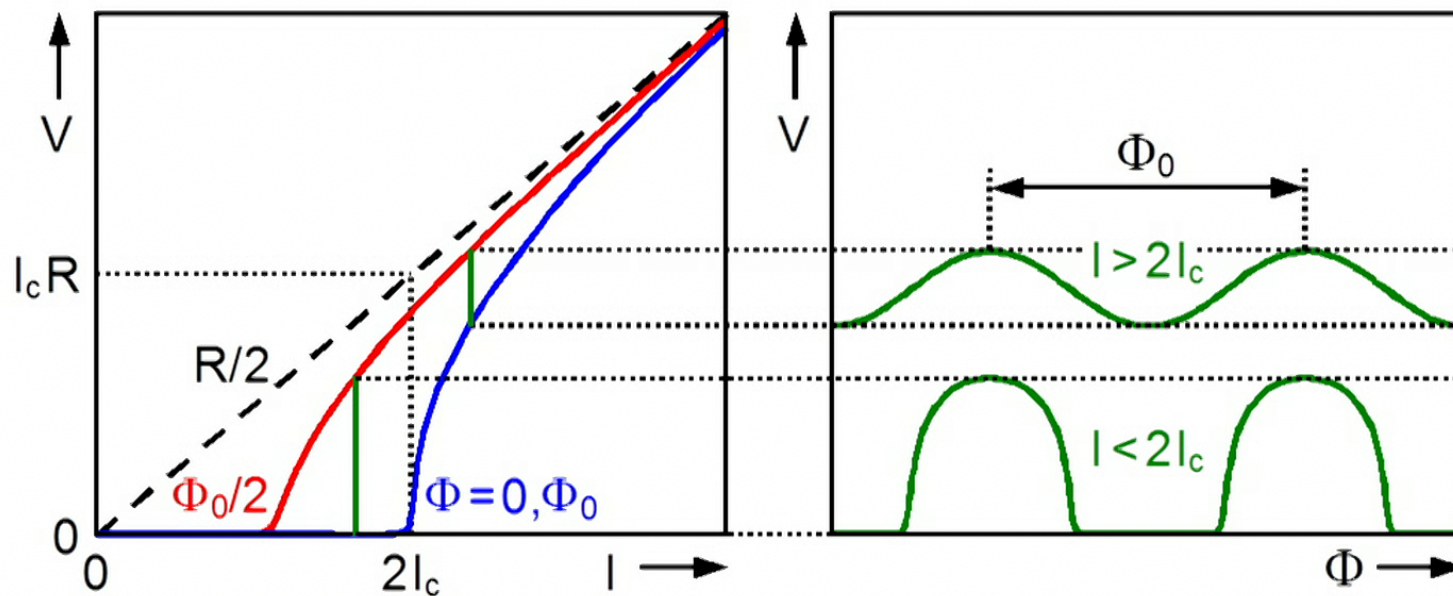
magnetic flux quantization
superconductor ring $T < T_c$
 $\Rightarrow \Phi_{ring} = n \times \frac{h}{2e} = n \times \Phi_0$
 $n = 0, 1, 2, 3, \dots$

Josephson tunneling
SQUID critical current
 $\Rightarrow I_{C,SQ}(\Phi) \propto |\cos(\pi\Phi/\Phi_0)|$

dc-SQUID sensors

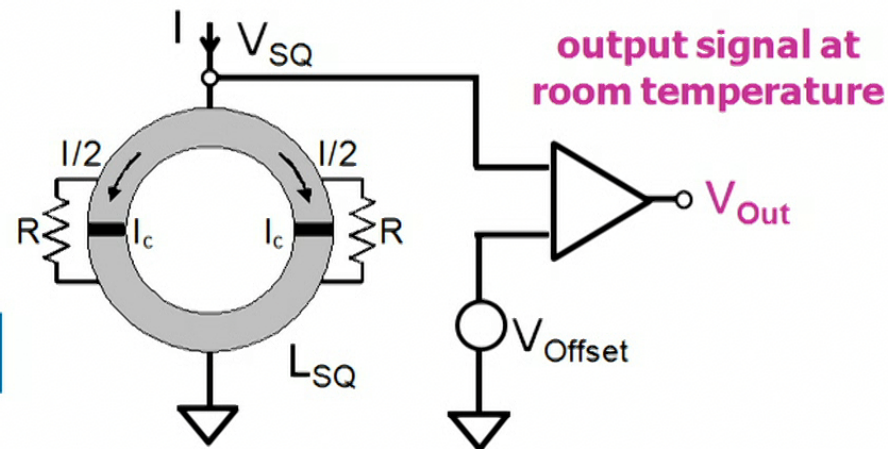


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dc-SQUID sensors

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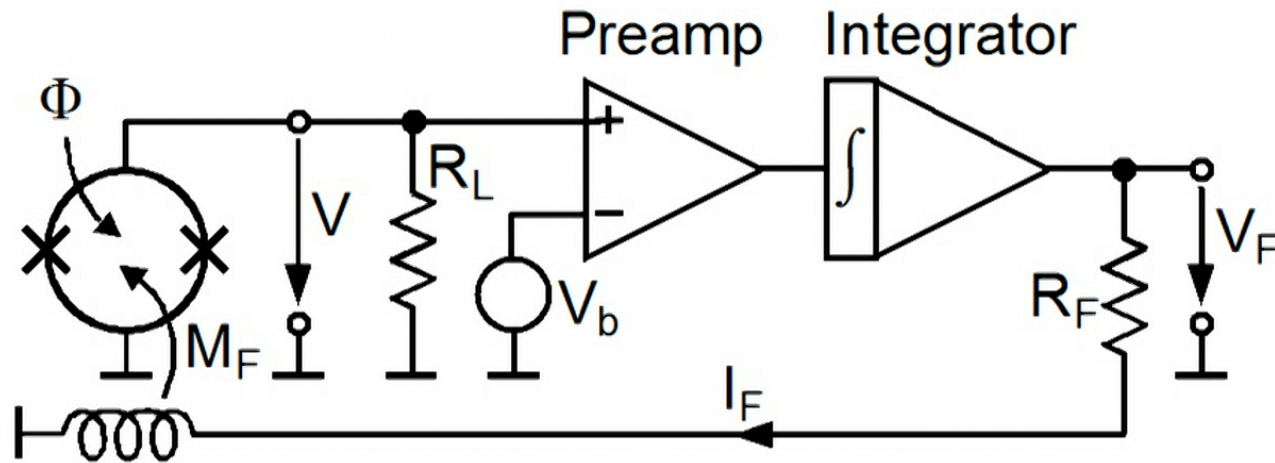
How *fast* is a dc-SQUID?

$$\tau \approx L_{SQ}/2R$$

$$L_{SQ} \approx 100 \text{ pH}, R \approx 10 \text{ } \Omega \\ \rightarrow \approx 5 \text{ ps}$$

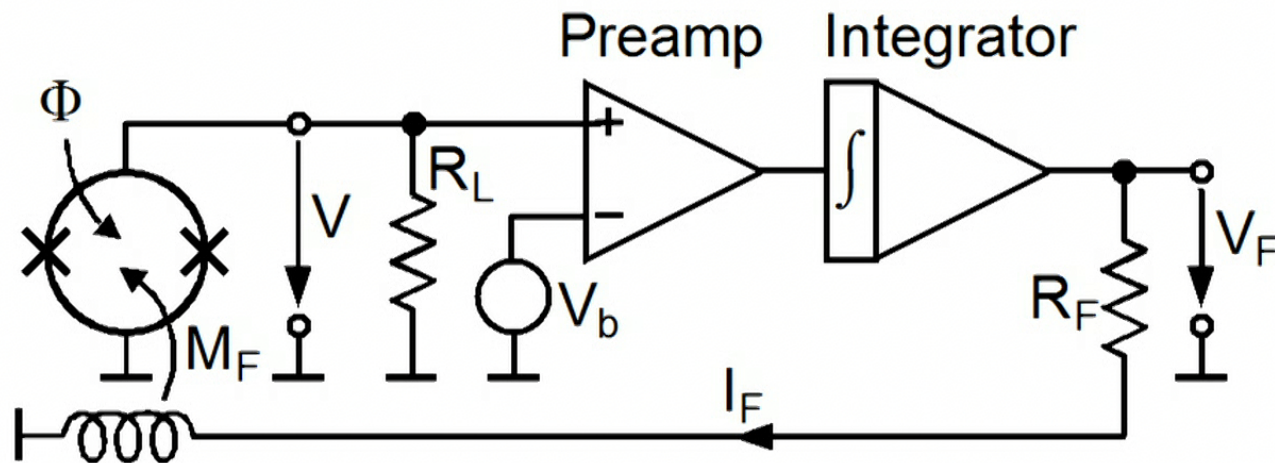
dc-SQUID sensors

- **almost always:** operation in negative feedback („Flux-Locked Loop“)



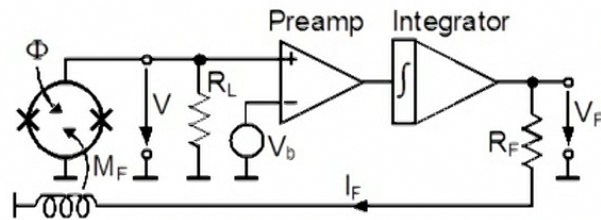
dc-SQUID sensors

- **almost always:** operation in negative feedback („**Flux-Locked Loop**“)



- FLL transfer coefficient $\partial V_F / \partial \Phi = -M_F / R_F$
- flux changes $\ll 1\Phi_0$ can be measured
- no relevant noise degradation, **but BW limitation**

FLL dynamics - ideal



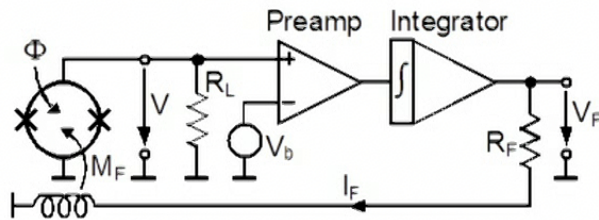
- **FLL bandwidth f_{3dB}**

What is the maximum output signal frequency?

- **System slew rate $\partial\Phi_F / \partial t$**

how fast can the feedback signal change?

FLL dynamics - ideal

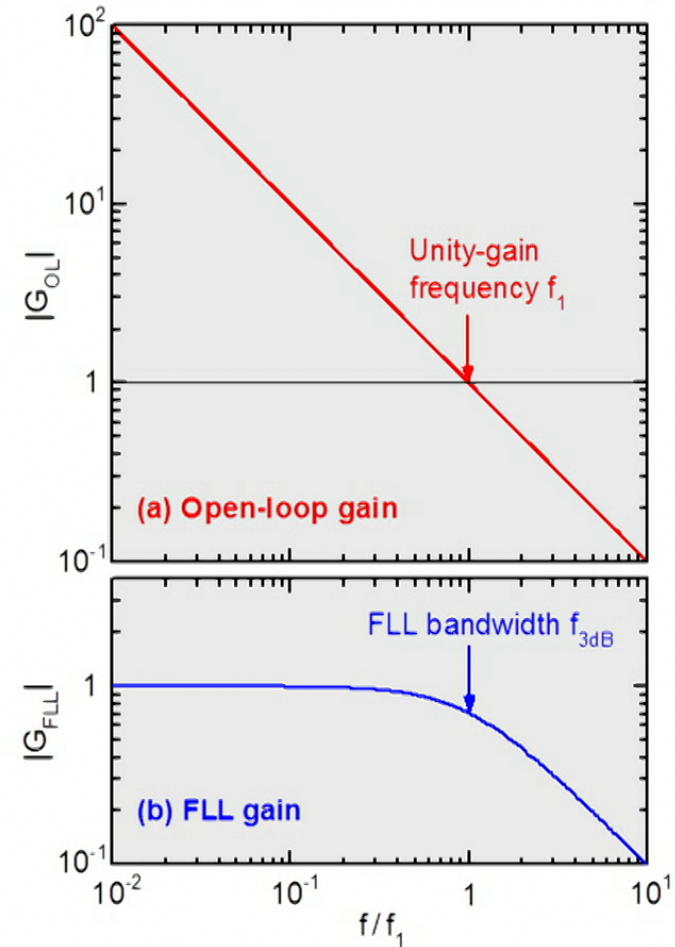


- **FLL bandwidth f_{3dB}**

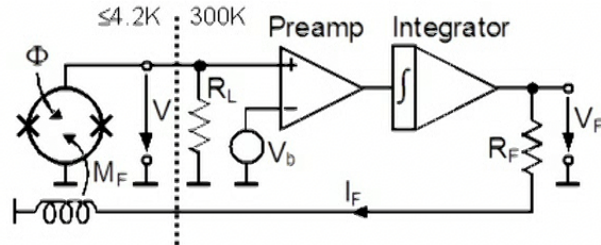
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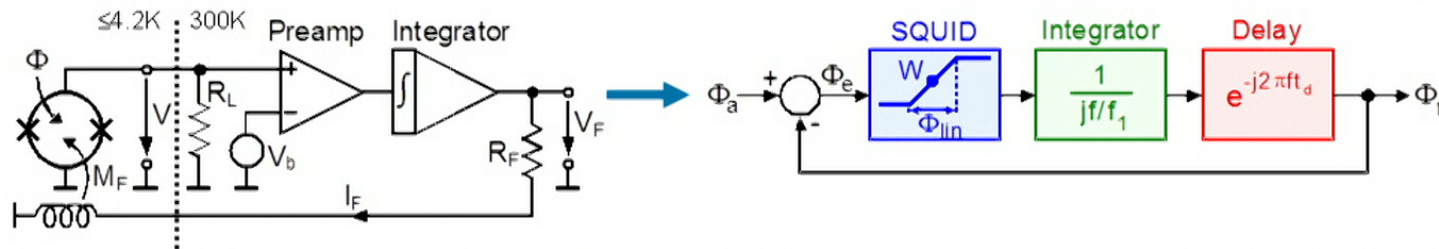


FLL dynamics – delay limit



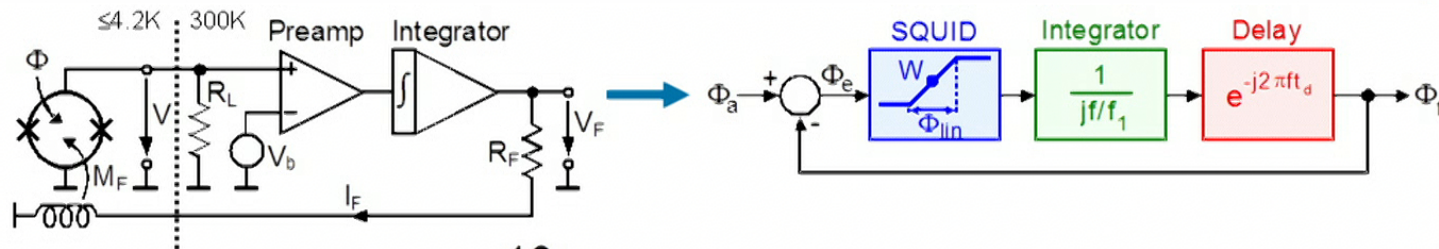
- 1m cable $\rightarrow t_d \approx 10$ ns

FLL dynamics – delay limit

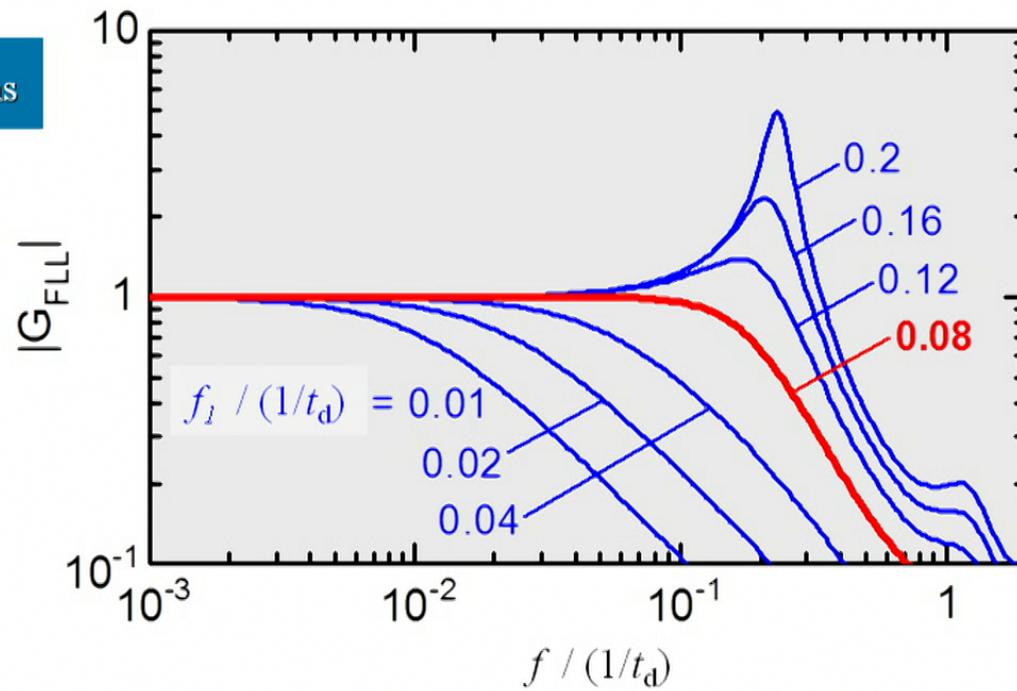


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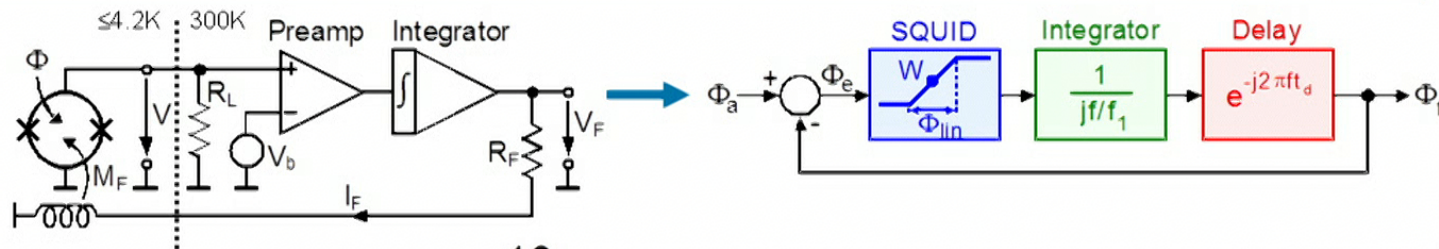
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FLL dynamics – delay limit



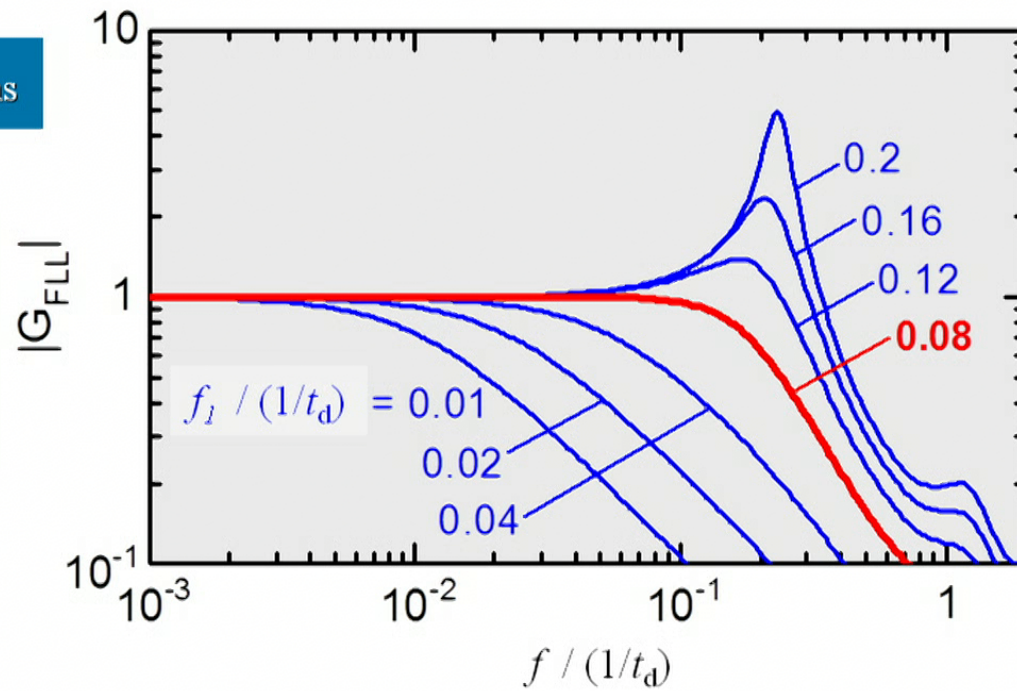
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$$f_1 = 0.08 / t_d$$

$$\approx 8 \text{ MHz}$$

$$f_{3dB} = 2.25 f_1$$

$$\approx 18 \text{ MHz}$$



SQUID sensor types



SQUID sensor types



- *Magnetometer*

SQUID sensor types



- *Magnetometer*

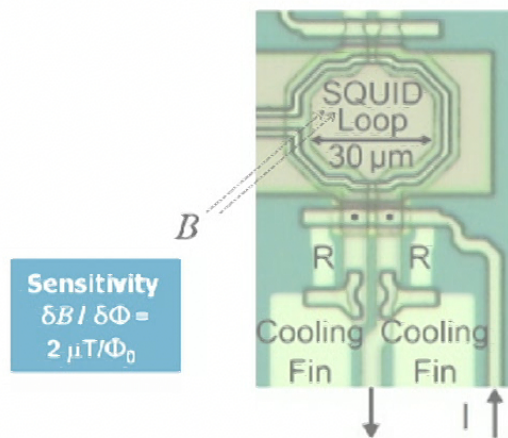
Measurand: magnetic flux density B

SQUID sensor types

- **Magnetometer**

Measurand: magnetic flux density B

Signal coupling: "direct"



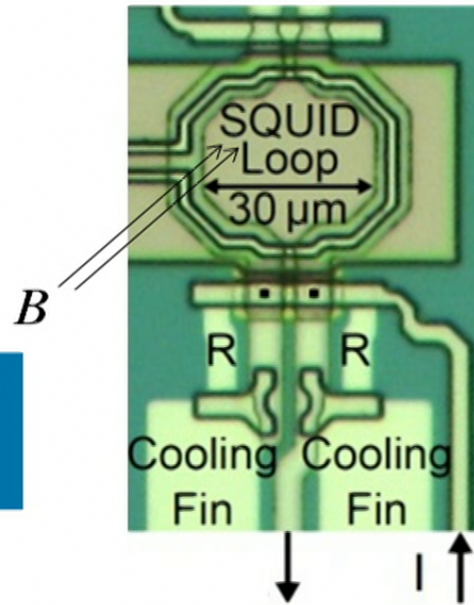
SQUID sensor types

- **Magnetometer**

Measurand: magnetic flux density B

Signal coupling:

“direct”



Sensitivity
 $\delta B / \delta \Phi = 2 \mu T / \Phi_0$

SQUID sensor types

- **Magnetometer**

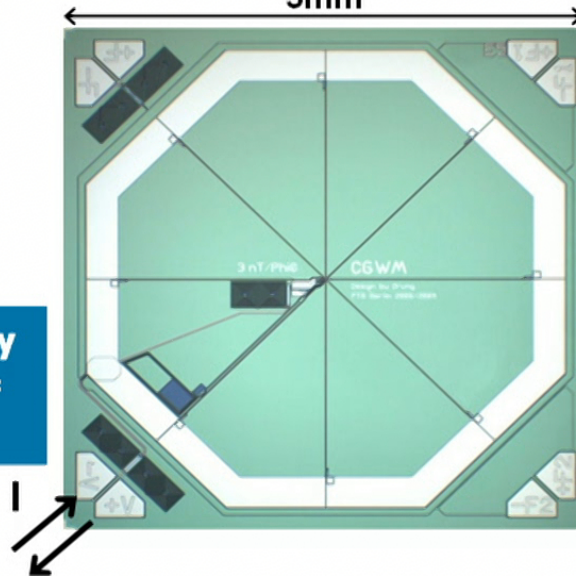
Measurand: magnetic flux density B

Signal coupling:

"direct"

3mm

Sensitivity
 $\delta B / \delta \Phi =$
 $3 \text{ nT}/\Phi_0$



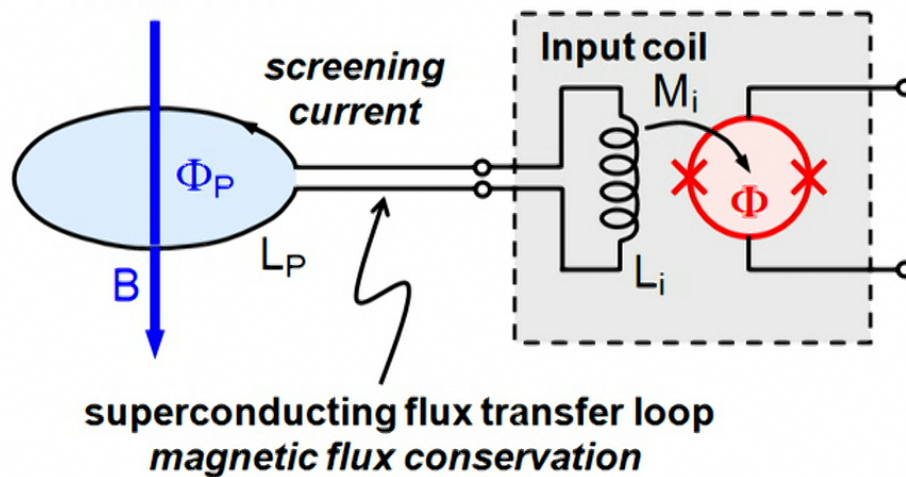
SQUID sensor types

- **Magnetometer**

Measurand: magnetic flux density B

Signal coupling: via pick-up coil
(often superconducting wire)

Pickup coil



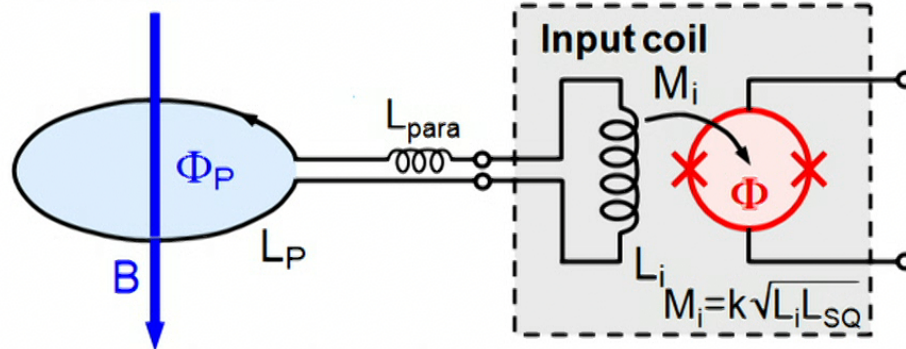
SQUID sensor types

- **Magnetometer**

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Pickup coil



- **optimal signal coupling:**

$$\partial\Phi_{SQ} = \frac{1}{2} \frac{k \sqrt{L_{SQ}}}{\sqrt{L_P}} \partial\Phi_P$$

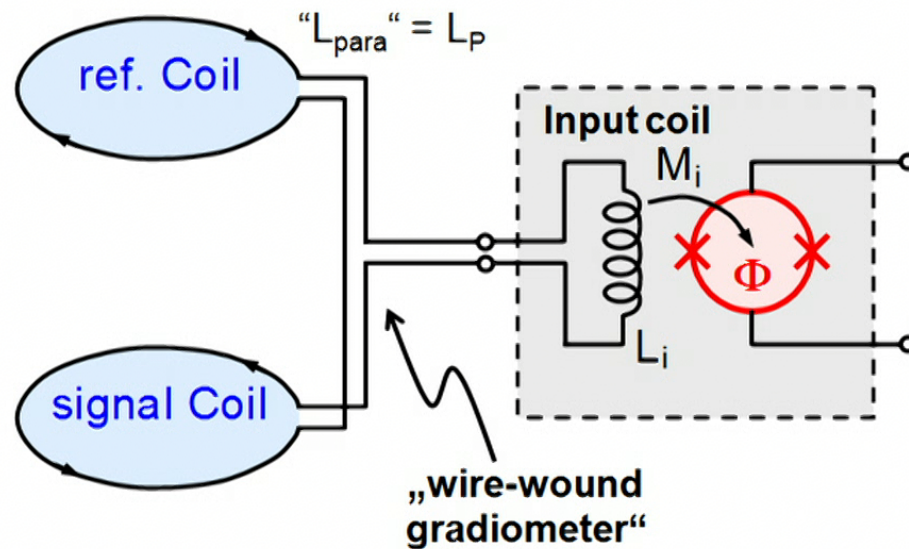
$$L_P = L_i, k \rightarrow 1$$
$$L_{para} = 0$$

SQUID sensor types

- *Magnetometer*

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Signal coupling: via pick-up coil
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SQUID sensor types

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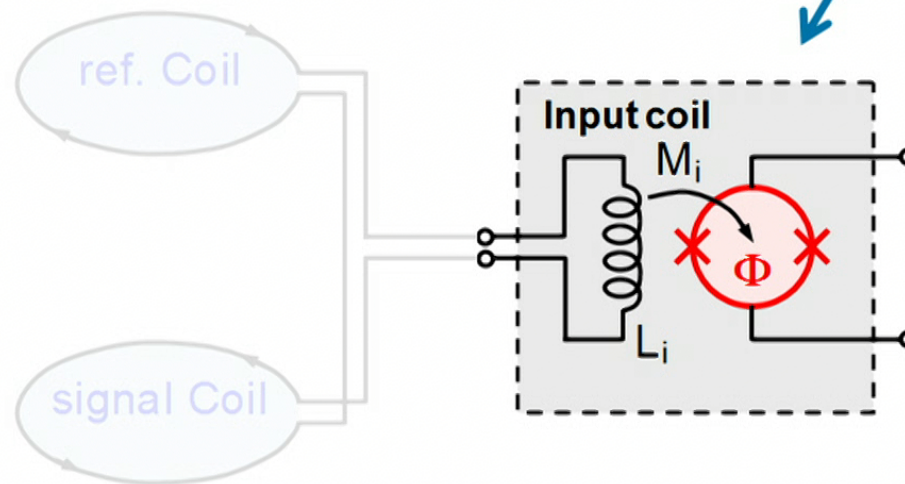
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- **Current sensor**

electric current I

via input coil L_i



SQUID sensor types



• Magnetometer

Measurand: magnetic flux density B

Signal coupling: via pick-up coil
or direct

Sensitivity parameter:

$$[A_{\text{eff}}^{-1}] = \text{T}/\Phi_0$$

• Current sensor

electric current I

via input coil L_i

$$[\delta I / \delta \Phi_{\text{Sq}}] = \text{A}/\Phi_0$$

Sensor noise parameter:

mag. flux density noise

$$[\sqrt{S_B}] = \text{T}/\sqrt{\text{Hz}}$$

current noise density

$$[\sqrt{S_I}] = \text{A}/\sqrt{\text{Hz}}$$

SQUID sensor types



• Magnetometer

• Current sensor

Measurand: magnetic flux density B

electric current I

**Signal
coupling:**

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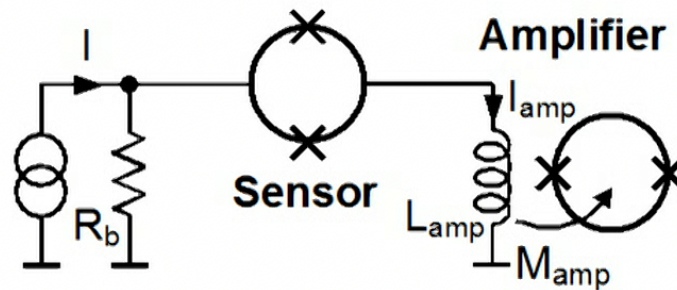
**coupled
energy
sensitivity
[ε] = h**

$$\varepsilon = \frac{1}{2} (A_{\text{eff}}^2 / L_{\text{Sq}}) S_B$$

$$\varepsilon = \frac{1}{2} L_i S_I$$

SQUID cascades

- Voltage-biased front-end SQUID read out by following SQUID stage(s)



advantage

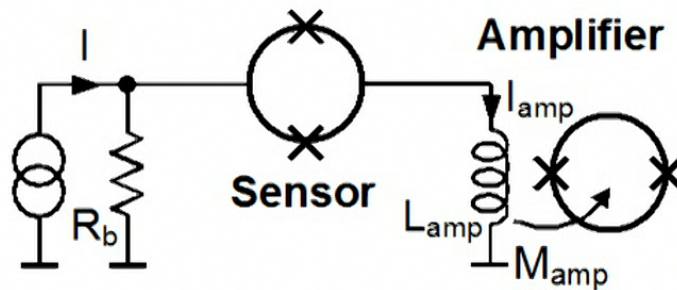
- reduce noise contribution from room temperature electronics

disadvantage

- more complex wiring and response curve
- higher dissipation power and heat load

SQUID cascades

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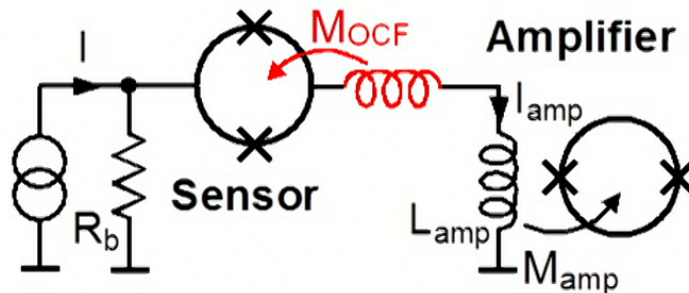
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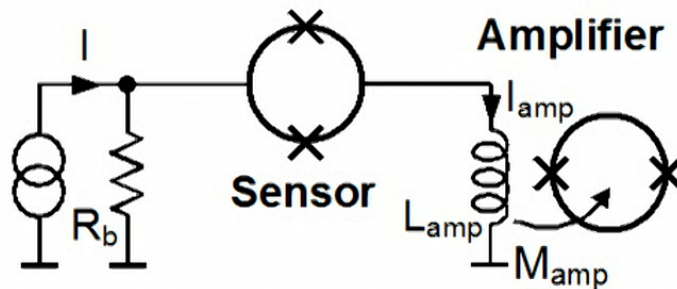
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- sensor SQUID output current fed back to sensor SQUID



SQUID cascades

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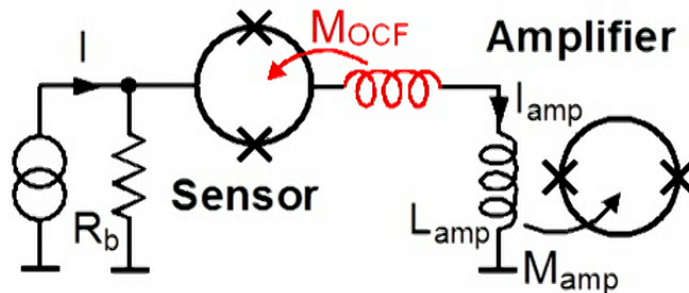
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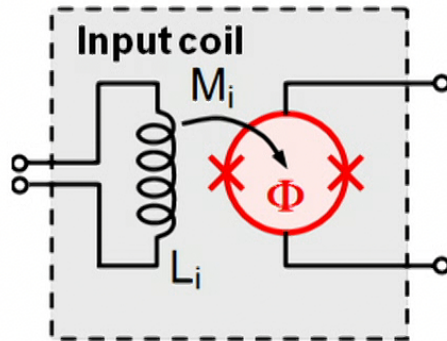
advantage

- increases sensor-to-amp flux gain
- reduces noise contribution of amp to sensor

disadvantage

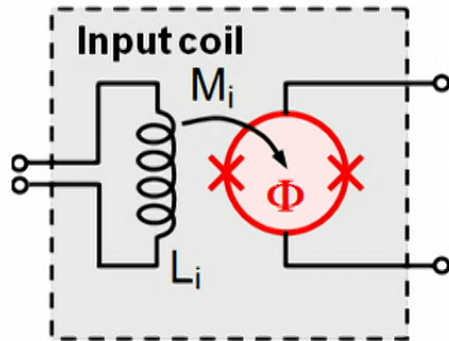
- SQ1 dynamic range is somewhat reduced

Current sensor input coupling

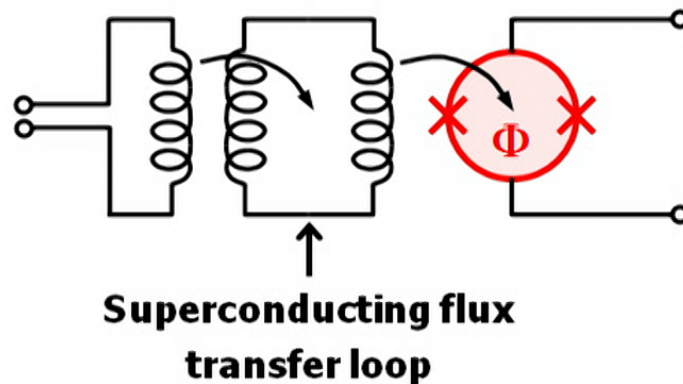


- **required L_i determined by source of signal current to be measured**
 - minimal L_i of order of SQUID inductance $\approx 10\text{pH} \dots 1\text{nH}$
- **when larger input inductances required**
→ (1) **double transformer input**

Current sensor input coupling

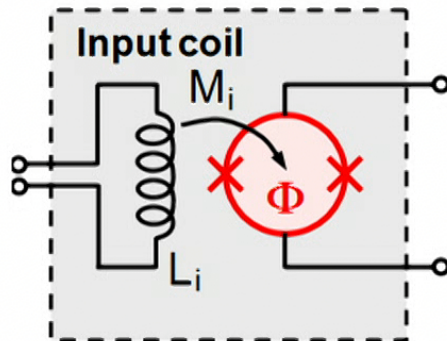


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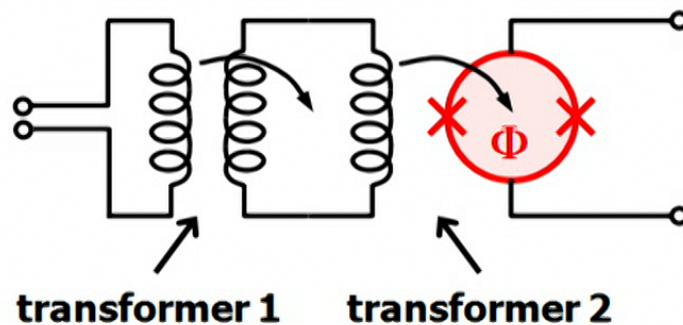


- susceptible to magnetic interference
- affects L_i and S_I
- parasitic resonances can occur
→ **more complex sensor design**

Current sensor input coupling



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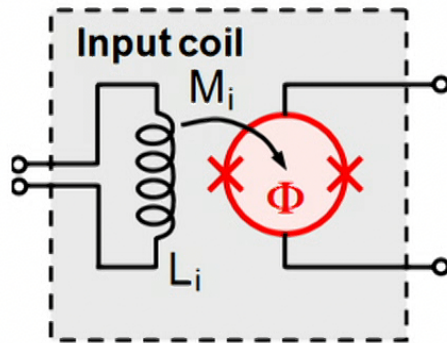


transformer 1 transformer 2

→ current sensor with
"double-transformer input"

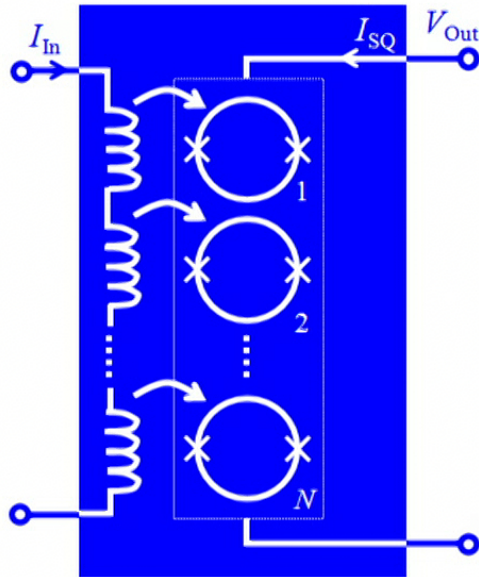
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Input coupling



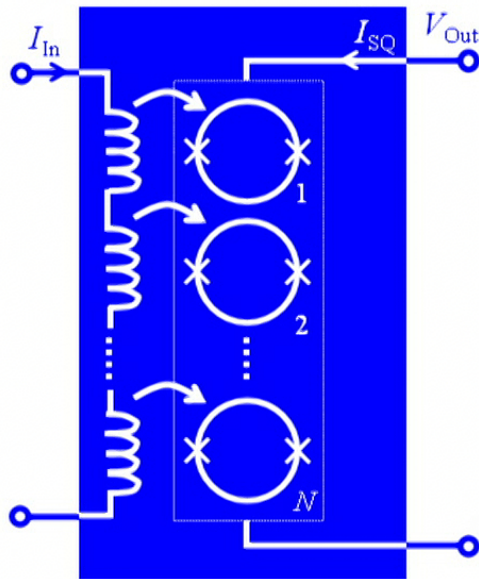
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- **when larger input inductances required**
 - (2) SQUID arrays with serial input

Input coupling



- **required L_i determined by source of signal current to be measured**
 - minimal L_i of order of SQUID inductance $\sim 10\text{pH} \dots 1\text{nH}$
- **when larger input inductances required**
 - (2) SQUID arrays with serial input

SQUID arrays

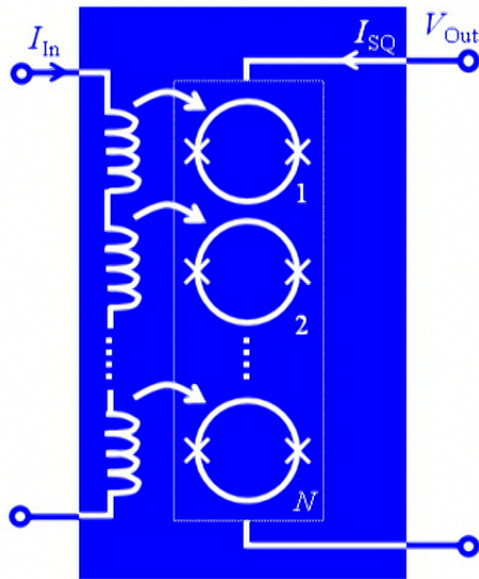


- **input coils of array elements all in series**

→ signal correlated, but intrinsic noise of array elements uncorrelated

Single SQUID	N SQUID series array	N SQUID parallel array
ϵ_c	ϵ_c	ϵ_c
S_I	S_I / N	S_I / N
D	$\sqrt{N} \times D$	$\sqrt{N} \times D$

SQUID arrays



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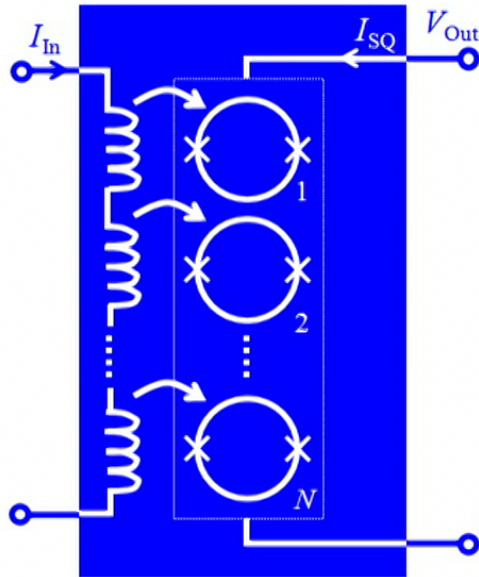
Single SQUID	N SQUID series array	N SQUID parallel array
ϵ_c	ϵ_c	ϵ_c
S_I	S_I / N	S_I / N
D	$\sqrt{N \times D}$	$\sqrt{N \times D}$

- **series, parallel or serial/parallel arrays**

→ flexible dimensioning of array output & transimpedance

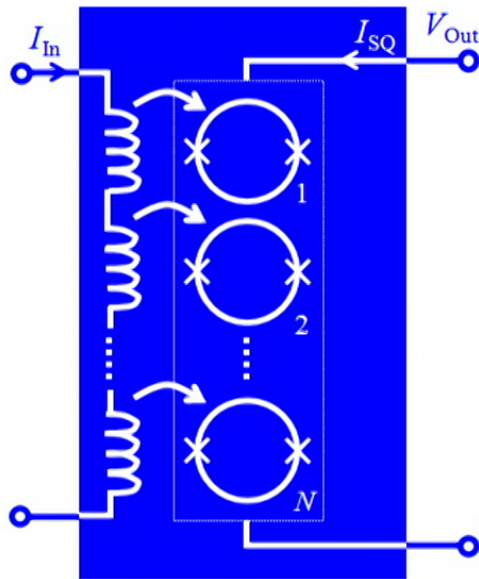
Single SQUID	N SQUID series array	N SQUID parallel array
R_{dyn}	$N \times R_{\text{dyn}}$	R_{dyn} / N
R_{trans}	$\approx N \times R_{\text{trans}}$	$\approx R_{\text{trans}} / N$
P_{Diss}	$N \times P_{\text{diss}}$	$N \times P_{\text{Diss}}$

SQUID arrays – flux trapping



- *single-SQUID-like* array behavior requires identical flux (offsets) in each array element

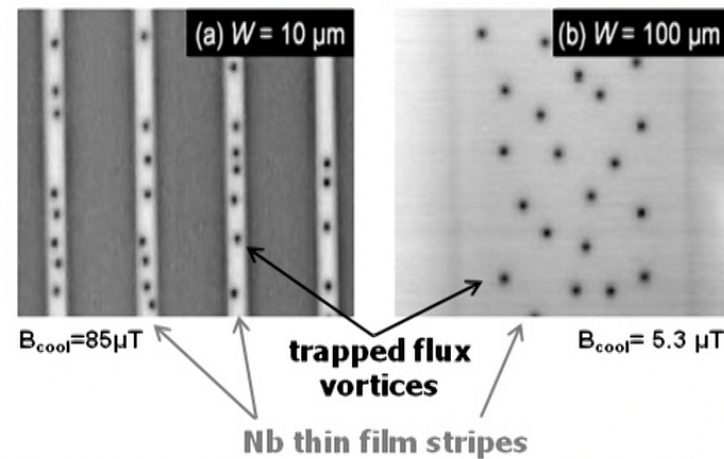
SQUID arrays – flux trapping



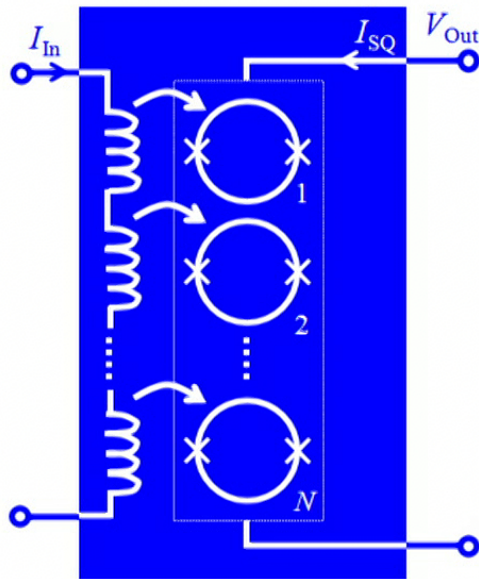
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Cooling in or exposure to 'large' magnetic fields of type-2 superconductor Nb

from G. Stan, et. al., Phys. Rev. Lett. 92, 097003 (2004)



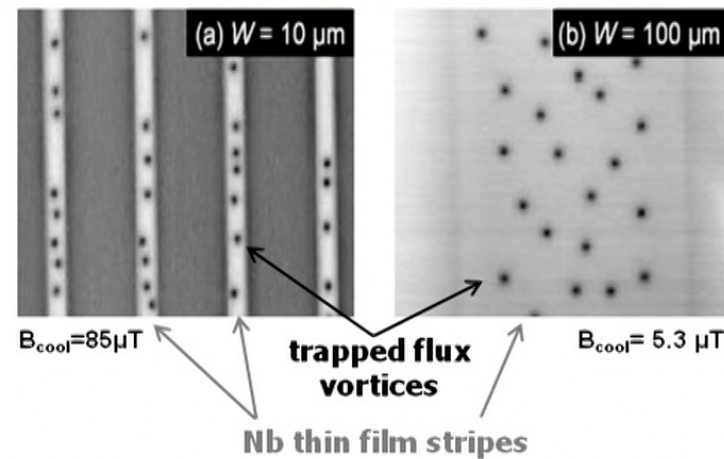
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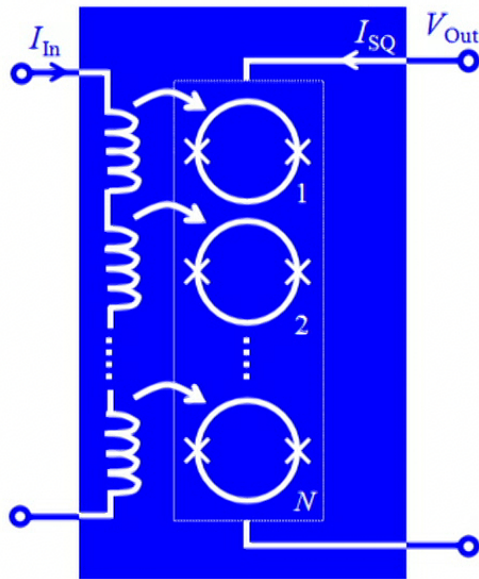
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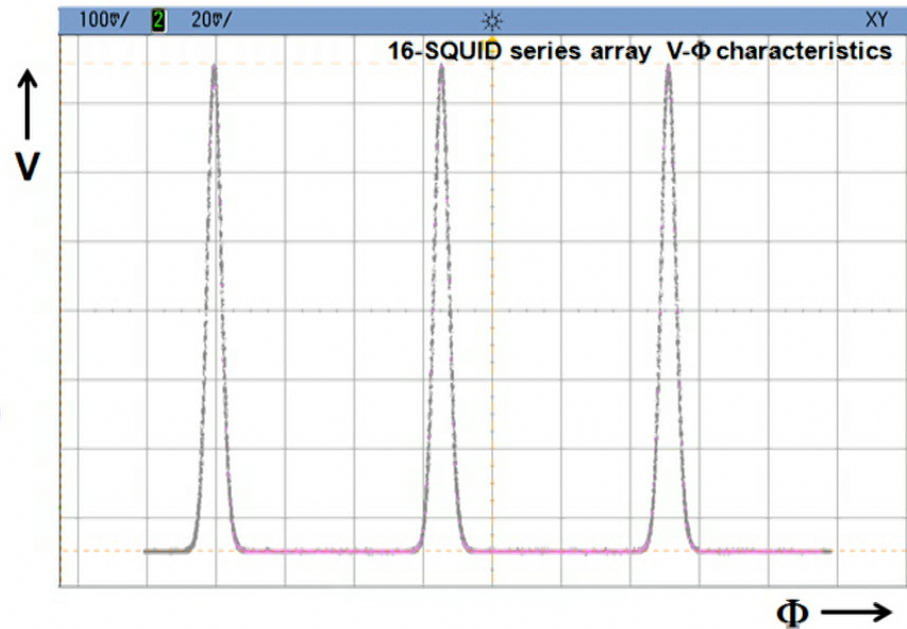
- cooling field w/o trapped flux:

$$B_{fc} \approx \Phi_0 / W^2$$

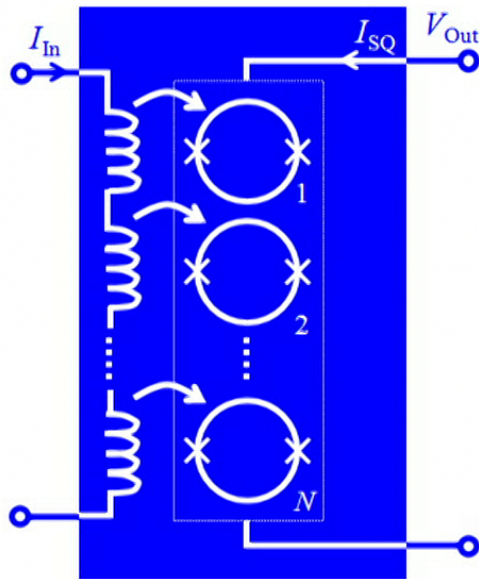
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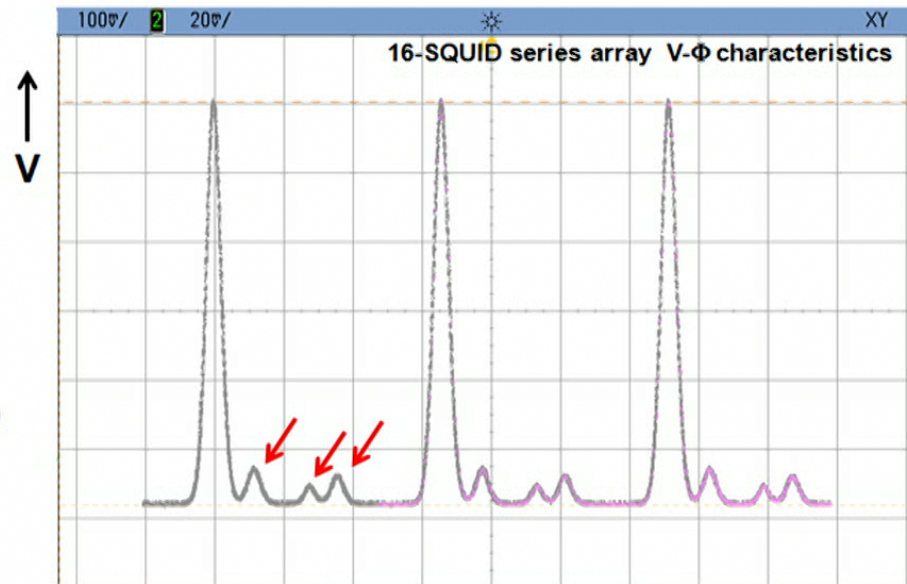
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SQUID arrays – flux trapping



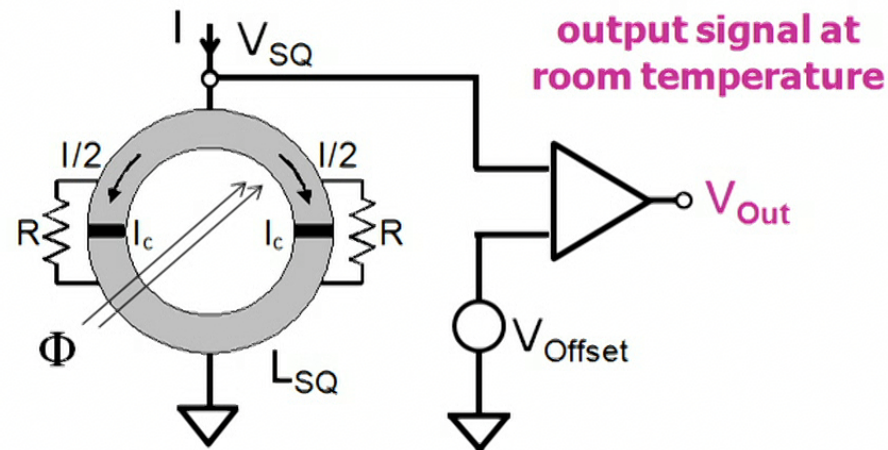
- *single-SQUID-like* array behavior requires identical flux (offsets) in each array element



- ⇒ random flux offsets in array elements
- ⇒ degraded SQUID array performance
- ⇒ also, noise from vortex motion

Magnetic flux noise

- sensor of magnetic flux Φ through the SQUID ring



$$\Rightarrow \varepsilon_{\text{theor}} \equiv \frac{S_{\Phi}}{2L_{SQ}} \approx \frac{2(1 + \beta_L) \Phi_0 k_B T}{I_c R}$$

$$\beta_L = 2I_c L_{SQ} / \Phi_0 \approx 1$$

for optimum LTS-SQUID noise

Chesca B, Kleiner R and Koelle D 2004, *SQUID Theory* in *The SQUID Handbook* ed J Clarke and A I Braginski (Weinheim: Wiley)

Magnetic flux noise

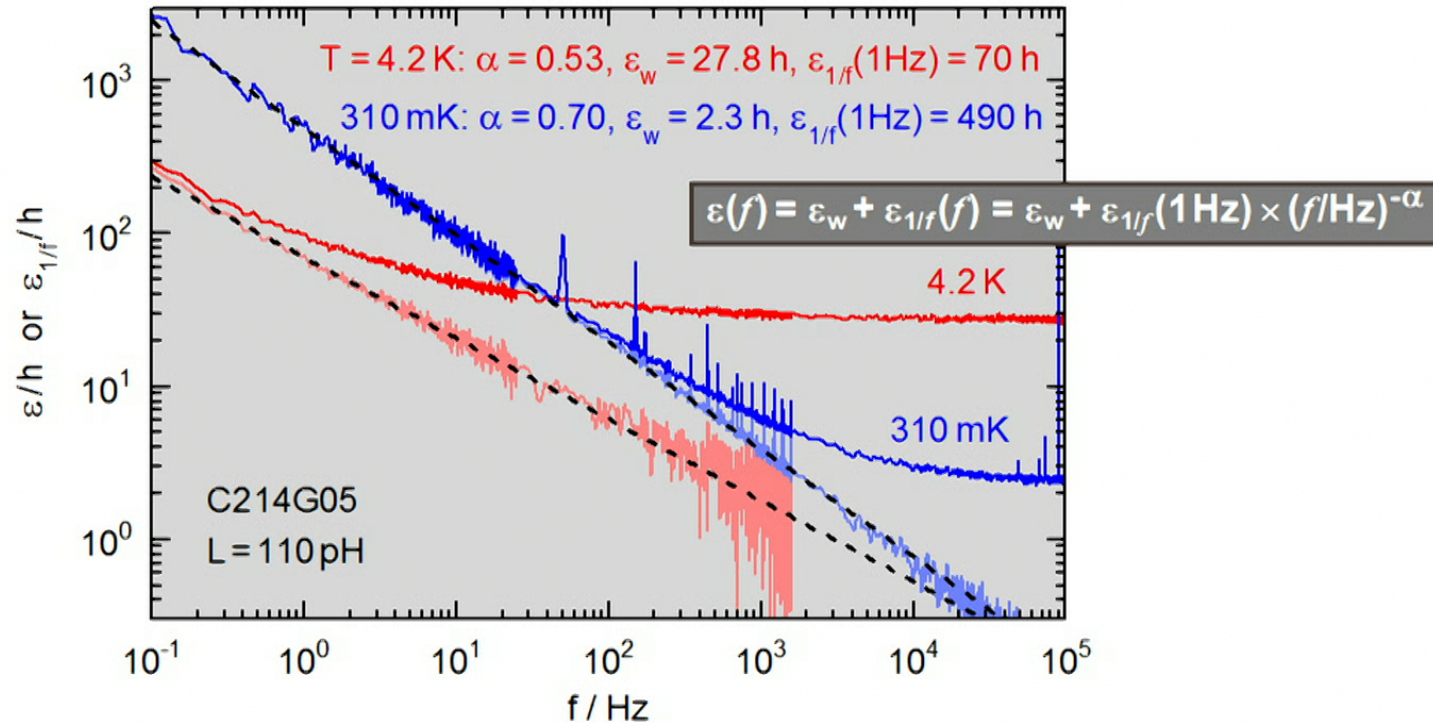
- *cool down your SQUID sensor to lowest possible T_{Op}*



Magnetic flux noise



- increase in "real" excess magnetic flux noise upon cooling, while white noise decreases with lowering temperature T_{Op}

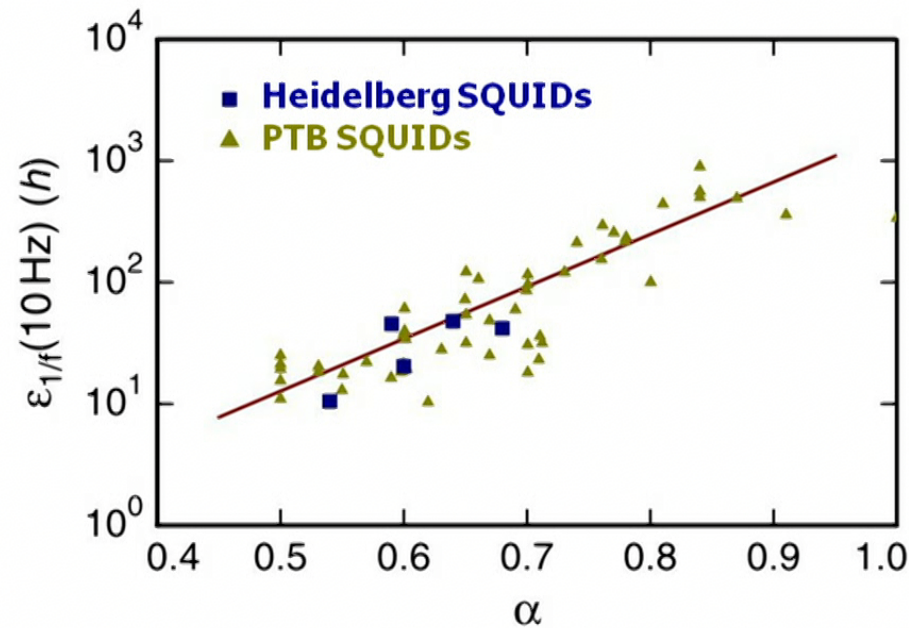


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Supercond. Sci. Technol. **28** (2015) 045008 S. Kempf et al. U Heidelberg

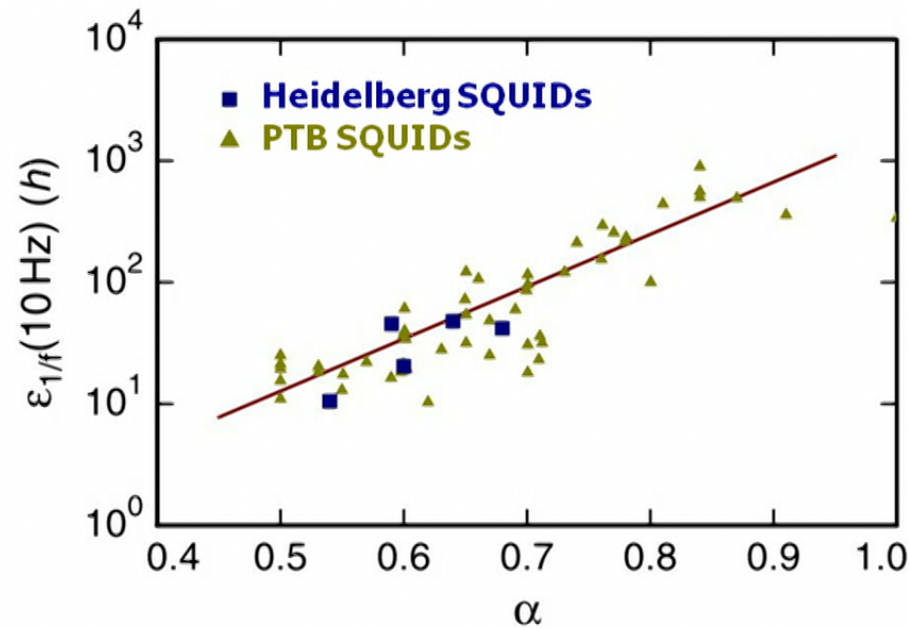


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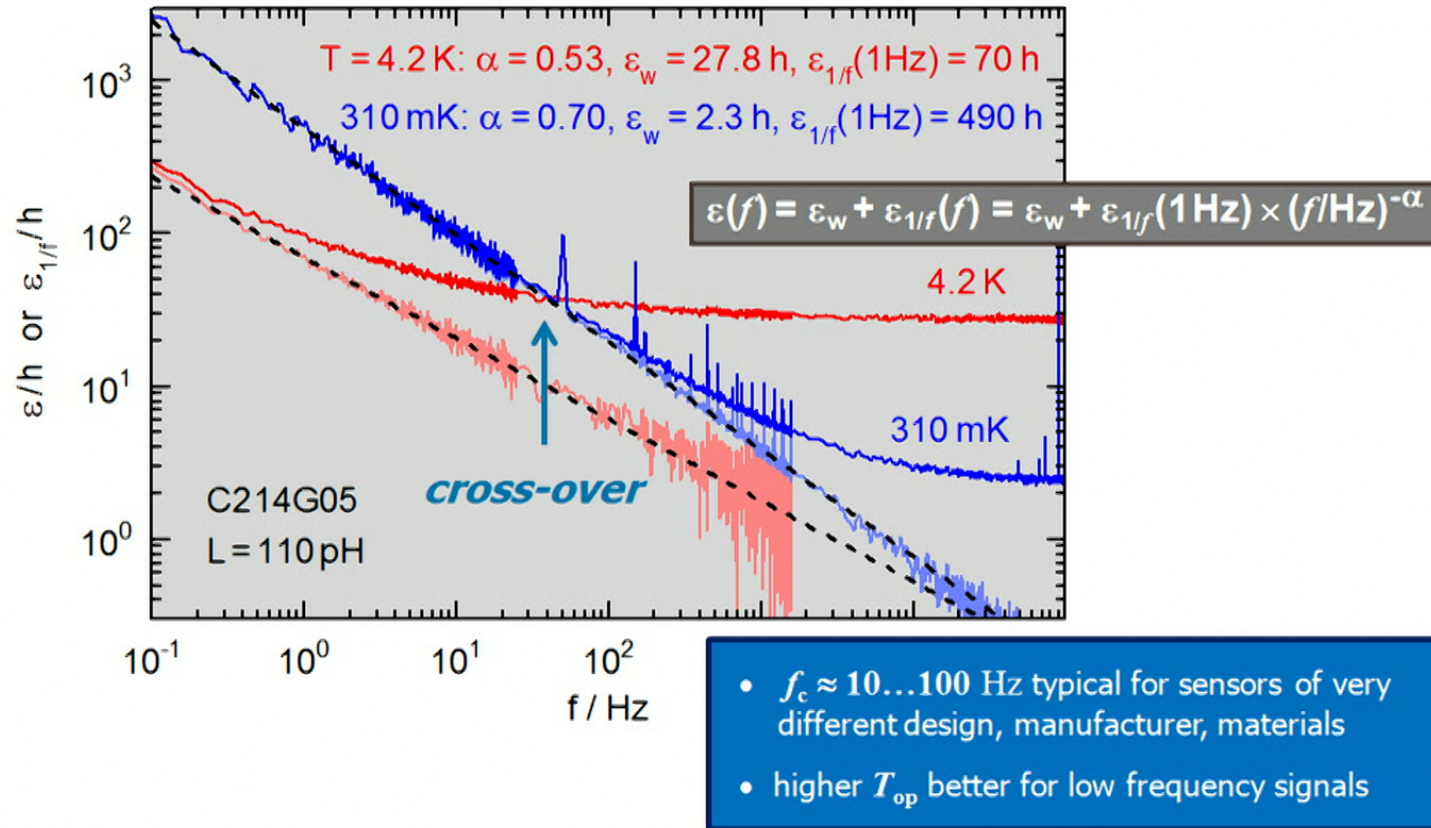


- random reversal of surface spin impurities: ? *danglings bonds, adsorbed O_2 , nuclear spins, metal-induced gap states, ...*

Magnetic flux noise



- increase in "real" excess magnetic flux noise upon cooling, while white noise decreases with lowering temperature T_{op}



SQUID sensor examples

SQUID sensors for TES readout

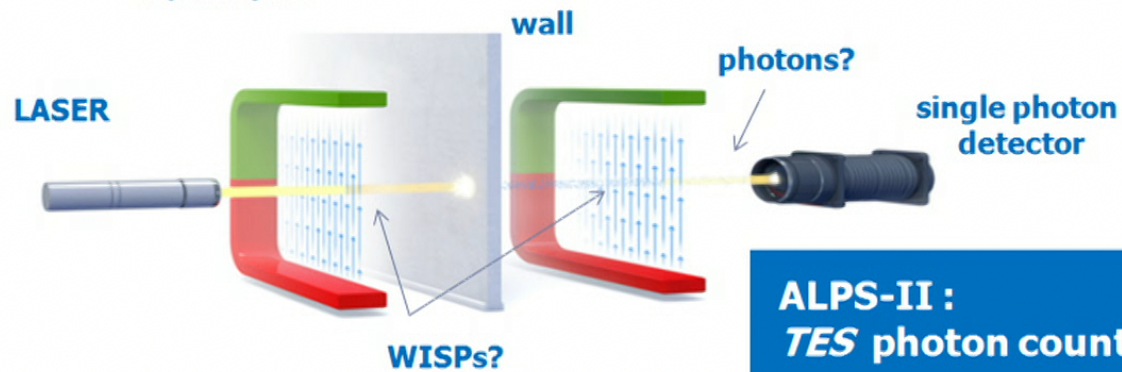


ALPS

Any Light Particle Search

alps.desy.de

Light-shining-through-a-wall experiment



ALPS-II :
***TES* photon counter @ 1064nm**

SQUID sensors for TES readout

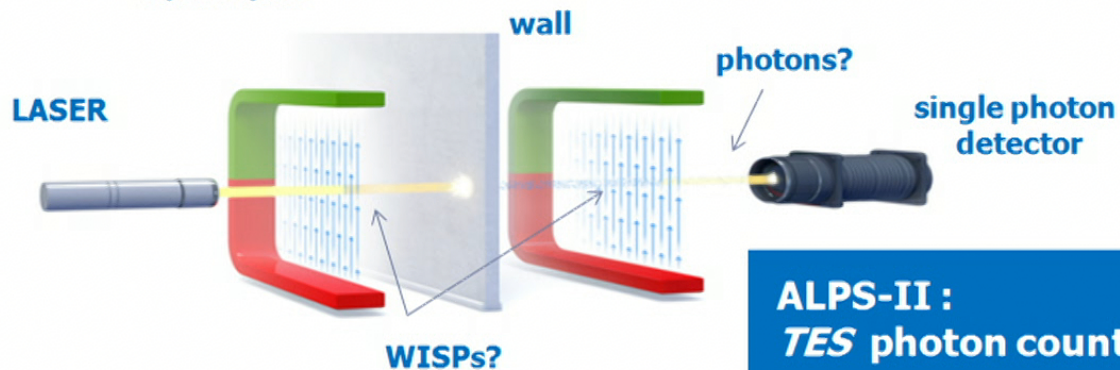


ALPS

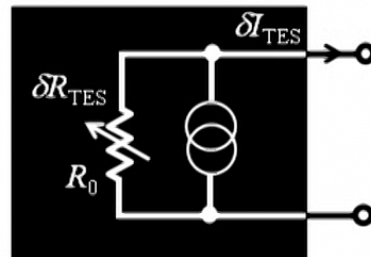
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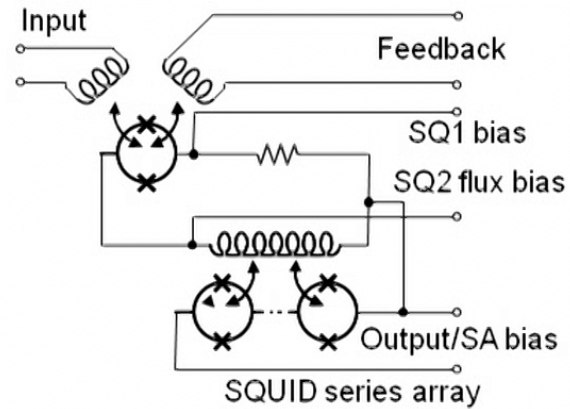


ALPS-II :
TES photon counter @ 1064nm



R_0	$\approx 1 \Omega$
I_0	$\approx 100 \mu A$
δI_{TES}	$\approx 100 nA$
τ	$\approx 0.1 \dots 1 \mu s$
T_{Bath}	$\approx 100 mK$
$\sqrt{S_{I,TES}}$	$\approx 5 pA/\sqrt{Hz}$

SQUID sensors for TES readout

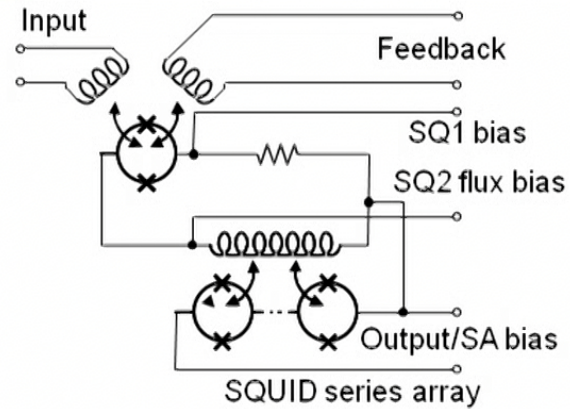


• 2-stage SQUID current sensor

- front-end SQ1 read out by 14-SQUID series array
- single-SQUID-like flux-response
- mK operation ok , magnetically robust
- integrated TES bias resistors & rf-filtered connections
- $L_{In} \approx 2\text{ nH}$, input/feedback inductively decoupled

$$\sqrt{S_I} < 2 \text{ pA}/\sqrt{\text{Hz}} @ 0.1 \text{ K} , P_{\text{Diss}} \approx 3 \text{ nW}$$

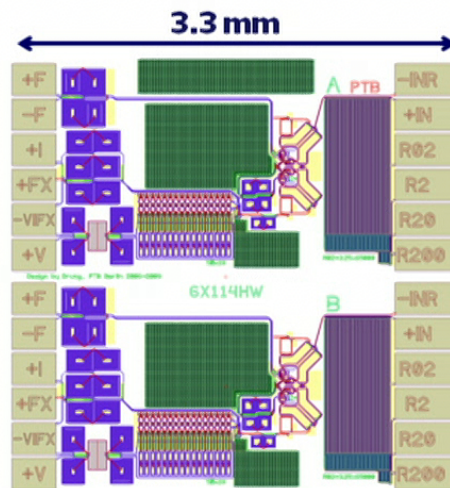
SQUID sensors for TES readout



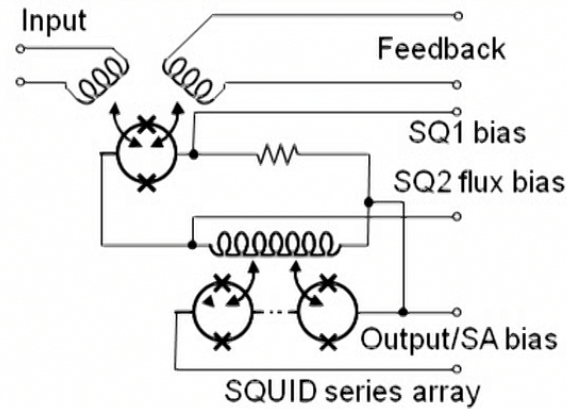
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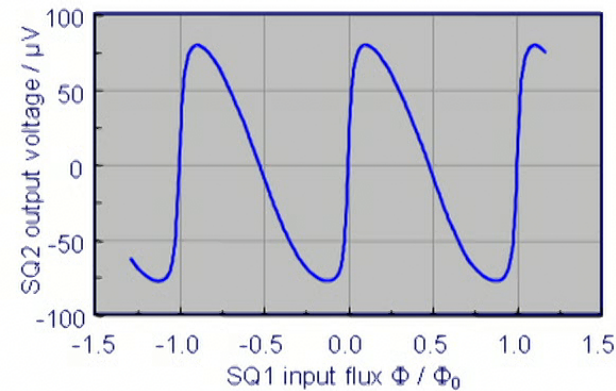
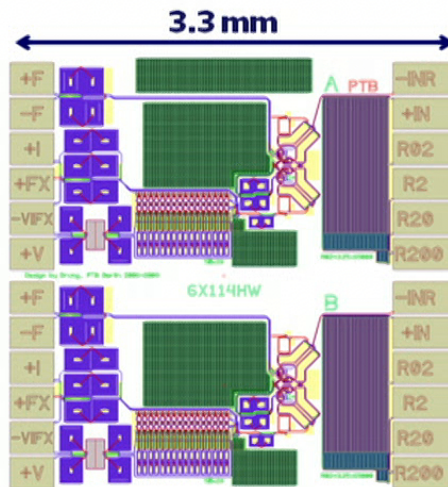
SQUID sensors for TES readout



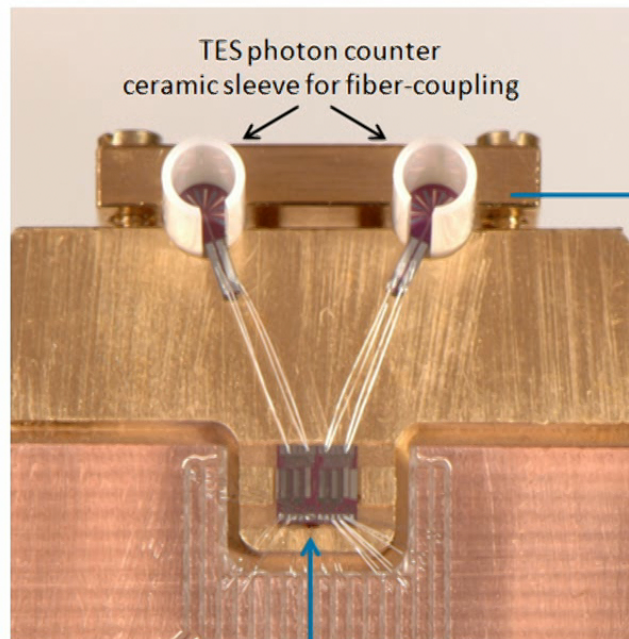
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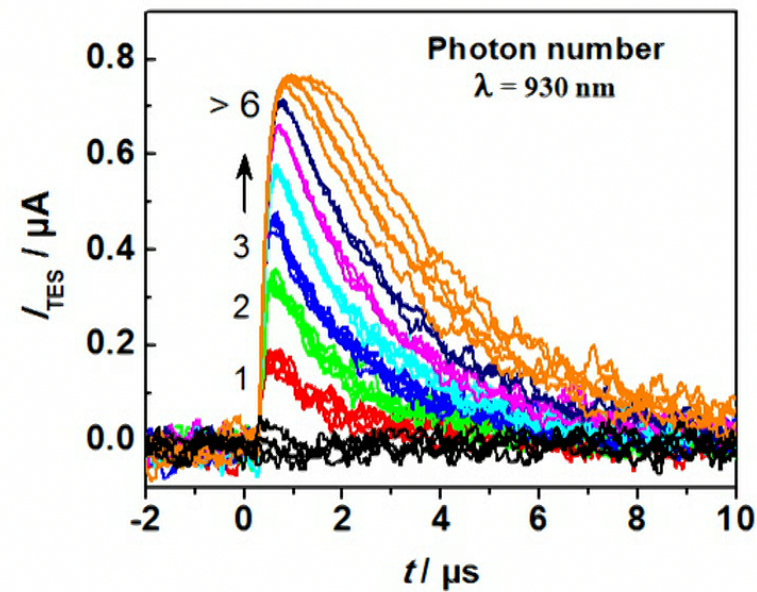
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SQUID sensors for TES readout



X114HW current sensor
chip size 3 mm × 3 mm



SQUID sensors for pick-up coils



- **common configuration: superconducting wire-wound pick-up coil**
- e. g. biomagnetism, susceptometry, NMR/NQR
- $L_p \approx 0.1 \dots 1 \mu\text{H}$

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PHYSICAL REVIEW X 4, 021030 (2014)

Proposal for a Cosmic Axion Spin Precession Experiment (CASPER)

Dmitry Budker,^{1,5} Peter W. Graham,² Micah Ledbetter,³ Surjeet Rajendran,² and Alexander O. Sushkov⁴

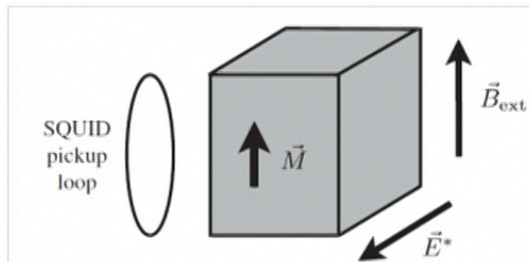


FIG. 1. Geometry of the experiment. The applied magnetic field $\vec{B}_{\text{ext}}$ is colinear with the sample magnetization $\vec{M}$. The effective electric field in the crystal $\vec{E}^*$ is perpendicular to $\vec{B}_{\text{ext}}$. The SQUID pickup loop is arranged to measure the transverse magnetization of the sample.

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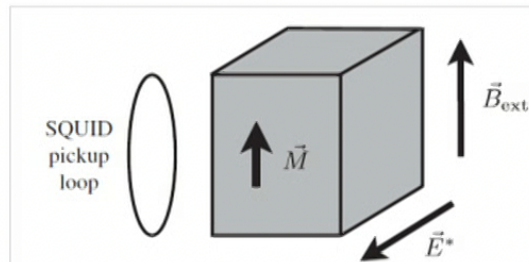
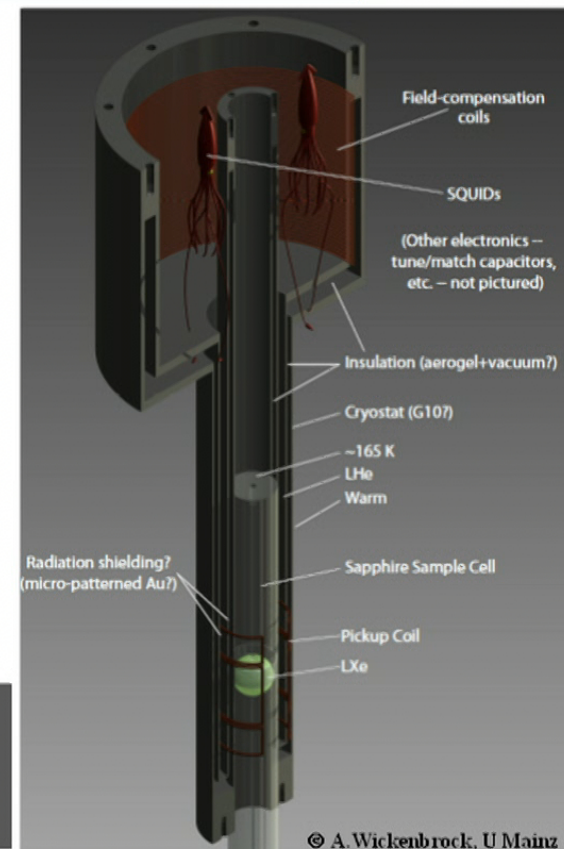


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Xe-129:

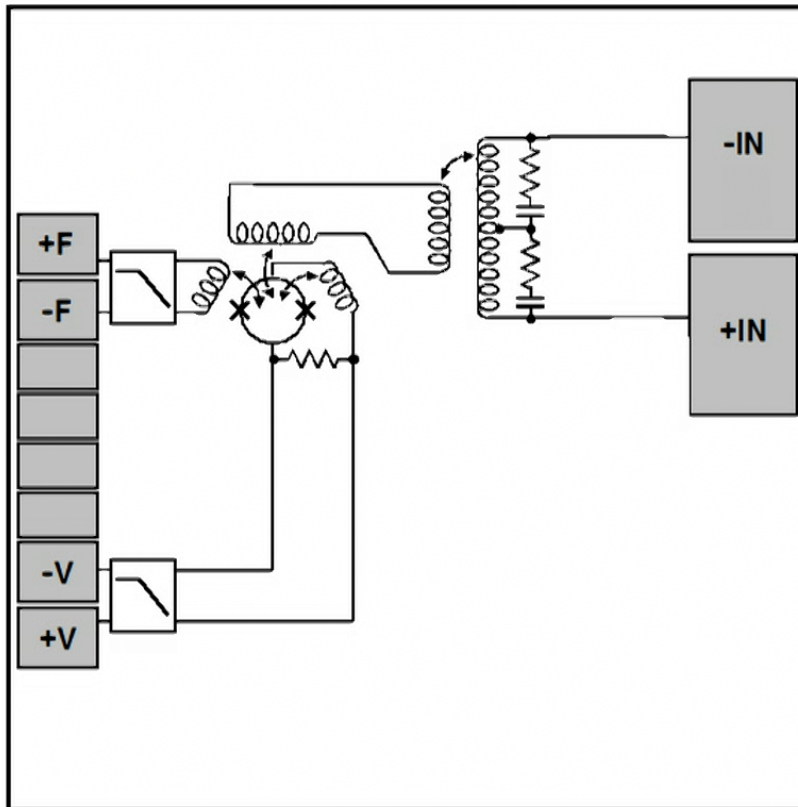
$$B_{\text{ext,max}} = 10 \text{ T} \dots 20 \text{ T}$$

$$f_{\text{sig,max}} = 118 \text{ MHz} \dots 236 \text{ MHz}$$



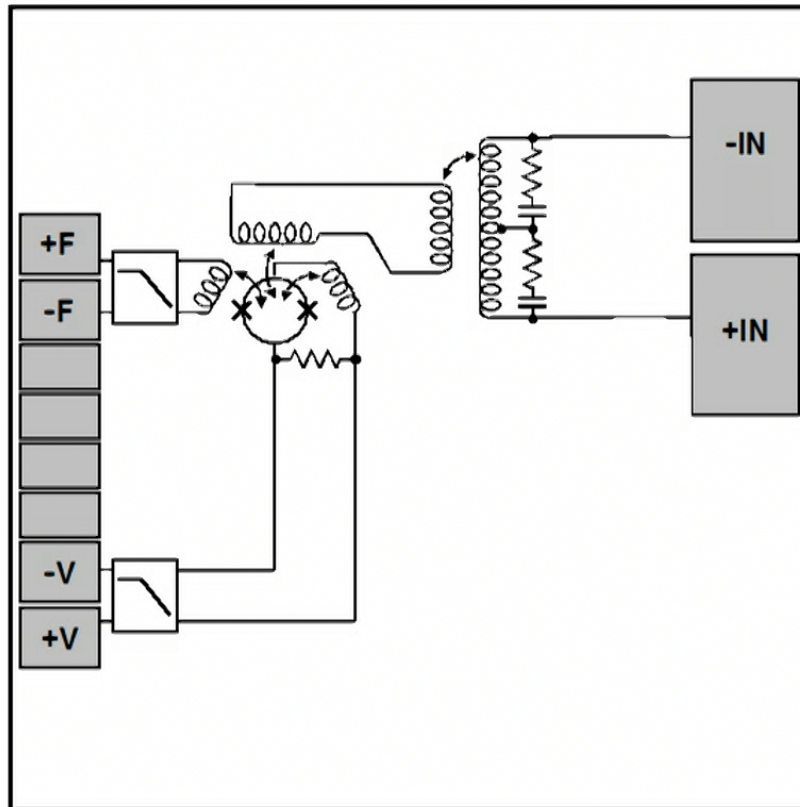
© A. Wickenbrock, U Mainz

SQUID sensors for $L_p \approx 0.1 \dots 1 \mu\text{H}$



- single-SQUID current sensors with double transformer input
- different input inductances L_i
- developed for LHe operation

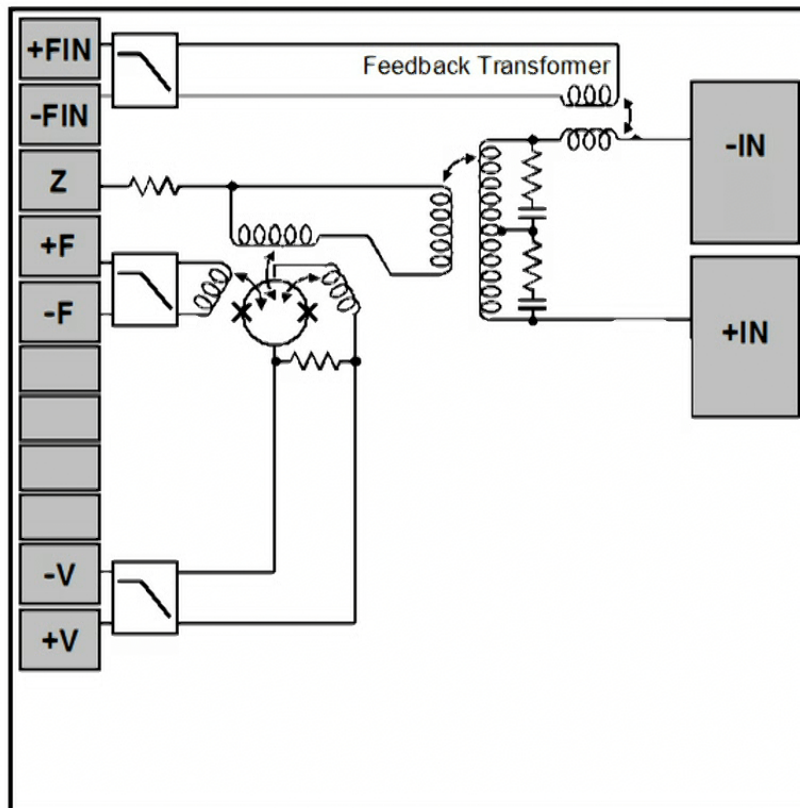
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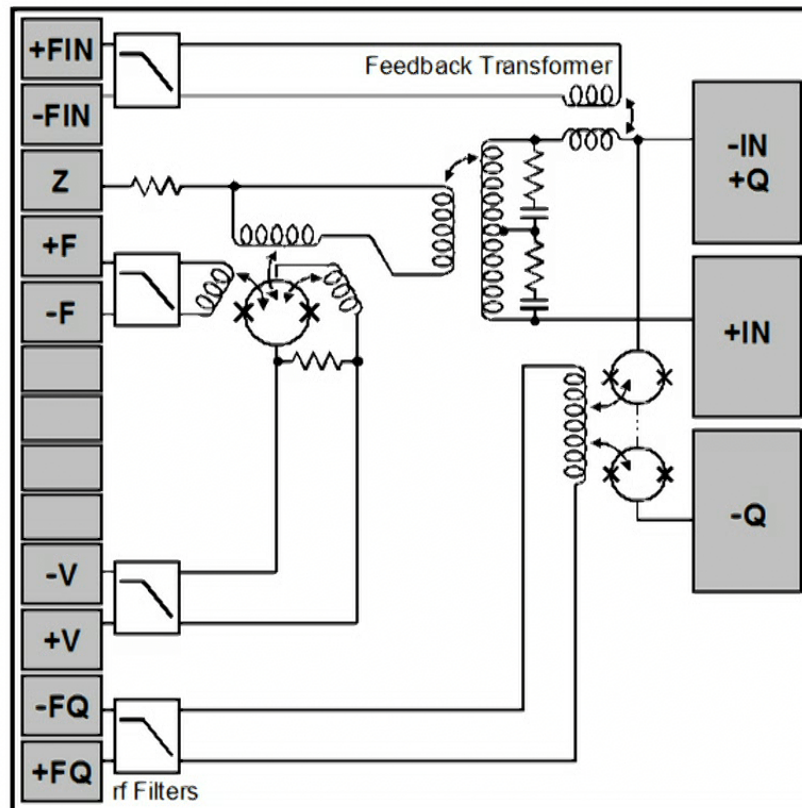
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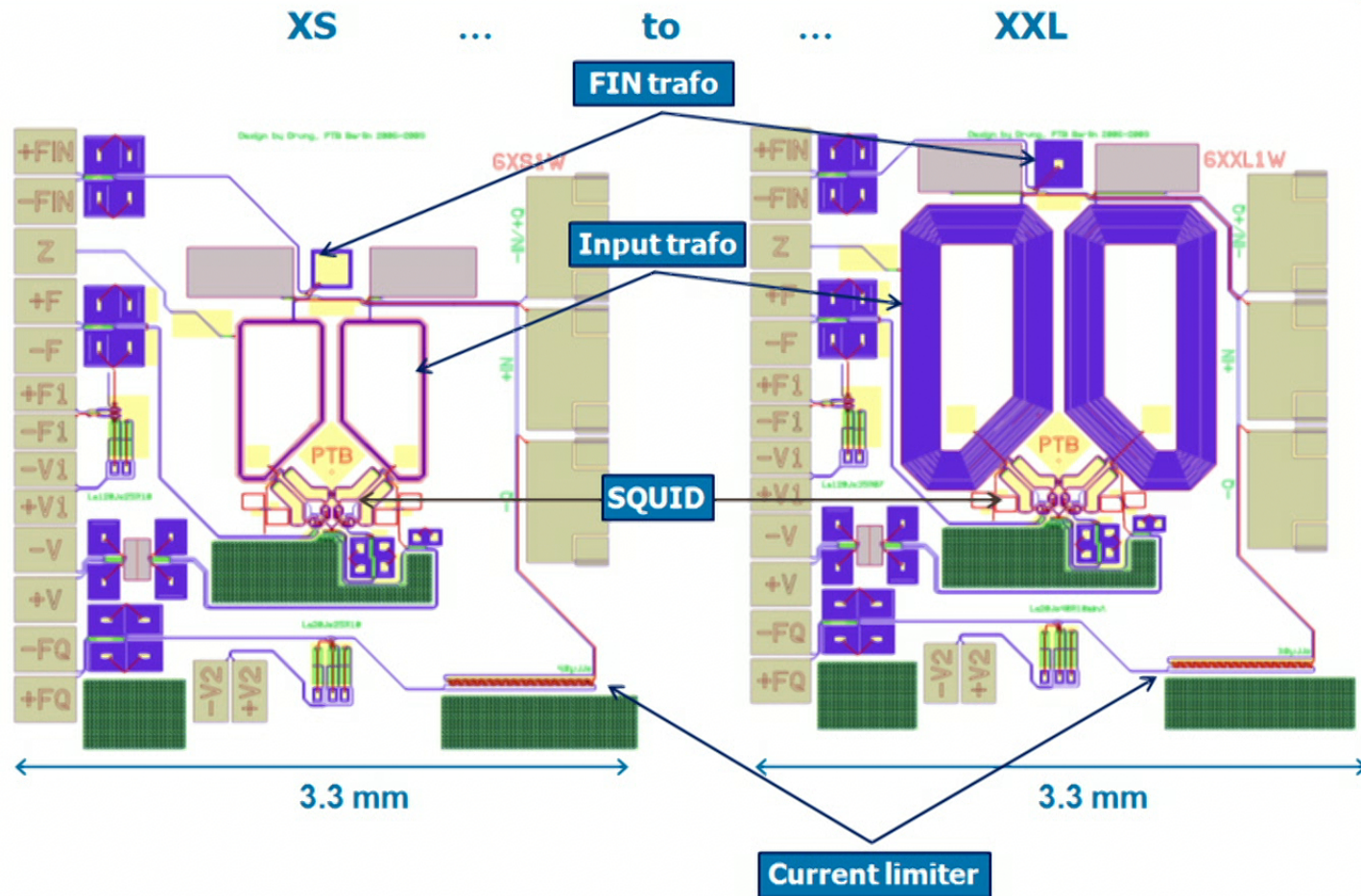
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 - „feedback-into-input“
 - input current limiter

SQUID sensors for $L_p \approx 0.1 \dots 1 \mu\text{H}$



SQUID sensors for $L_p \approx 0.1 \dots 1 \mu\text{H}$



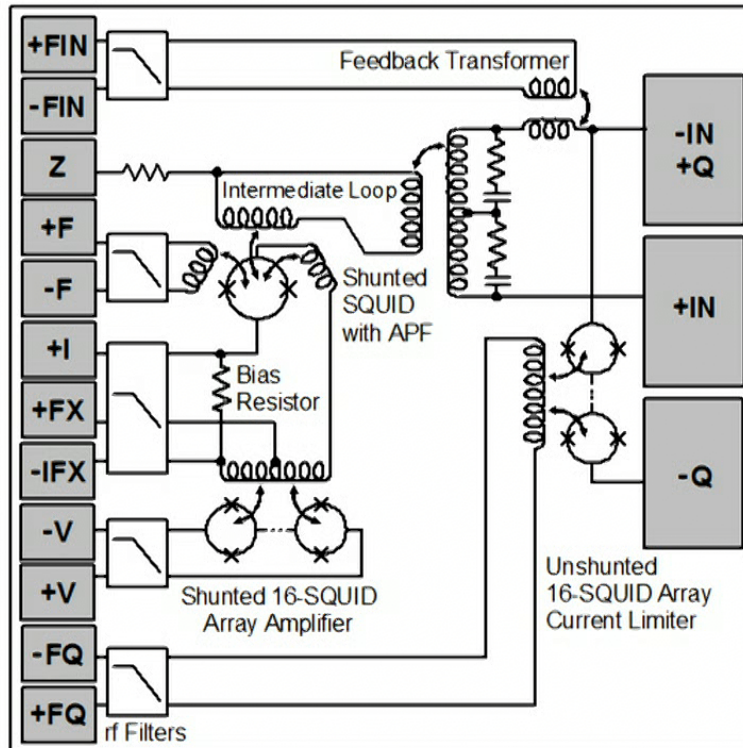
size	L_i / nH	$\delta I / \delta \Phi / \mu\text{A} / \Phi_0$	$\sqrt{S_I} / \text{pA} / \sqrt{\text{Hz}}$	$\epsilon_c / \hbar$	$\sqrt{S_B} / \text{fT} / \sqrt{\text{Hz}}$
XS	27	2.3	2.8	900	6.6
S	65	1.3	1.6		1.9
M	150	0.8	1	700	0.6
L	400	0.5	0.6		0.6
XL	1000	0.3	0.4		0.06
XXL	1800	0.23	0.3		0.03

typical white noise at 4.2K



ideally matched magnetometer
($N_P = 1, L_P = L_i, L_{\text{para}} = 0$)

SQUID sensors for <1K



Integrated 2-stage SQUID cascade

- **Sensor:** single SQUID, 2nd order grad
- **Amplifier:** SQUID series array, $N = 16$

Why?

- **1-stage:** - RT electronics noise contribution
- does not scale w/ T

- **Input and additional features same as for their 1-stage cousins**



SQUID sensors for <1K



size	L_1 / nH	$\delta I / \delta \Phi / \mu\text{A}/\Phi_0$	$\sqrt{S_I} / \text{fA}/\sqrt{\text{Hz}}$	$\epsilon_c / \hbar$
XS	27	2.3	620	50
S	65	1.3	400	
M	150	0.8	240	40
L	400	0.5	150	
XL	1000	0.3	100	
XXL	1800	0.23	70	

typical white noise at 0.3K

SQUID sensors for <1K



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$\approx 3 \times \epsilon_{\text{theor}}$

typical white noise at 0.3K

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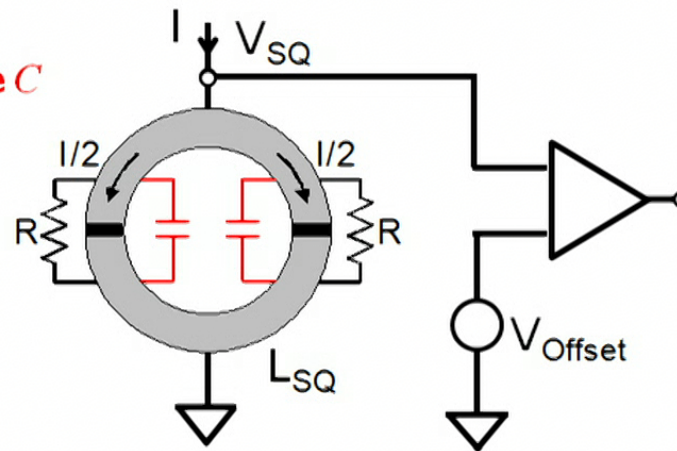
typical white noise at 0.3K

How to get to the theroretical limit ?

Magnetic flux noise

- sensor of magnetic flux Φ through the SQUID ring

parasitic JJ capacitance C



$$\Rightarrow \varepsilon_{\text{theor}} \equiv \frac{S_{\Phi}}{2L_{SQ}} \approx \frac{2(1 + \beta_L) \Phi_0 k_B T}{I_C R}$$

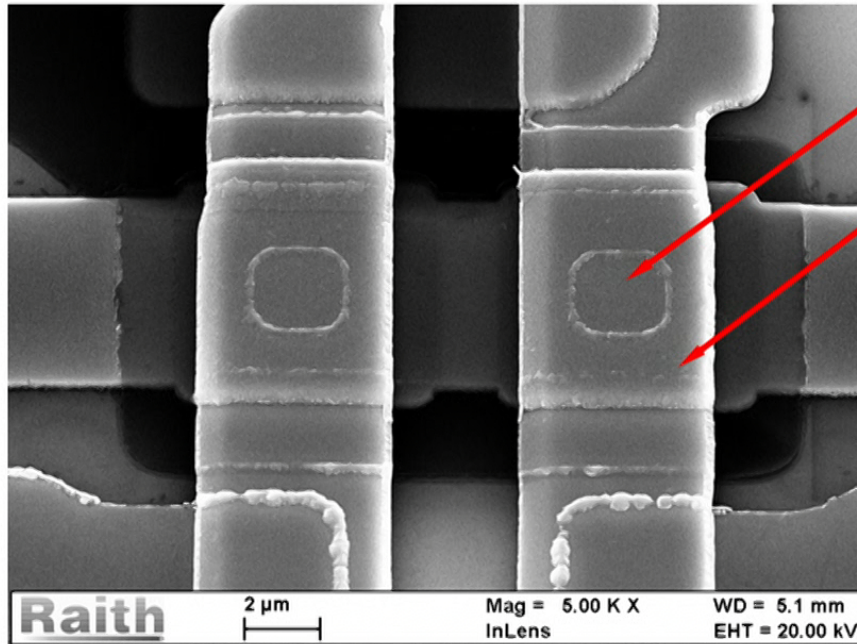
$$\beta_L = 2I_C L_{SQ} / \Phi_0 \approx 1$$

for optimum LTS-SQUID noise

LTS dc-SQUID sensors



- Example: PTB SQUID fab process, UV contact lithography, minimum feature size 2 μ m



JJ area:
ca. 5...6 μm^2

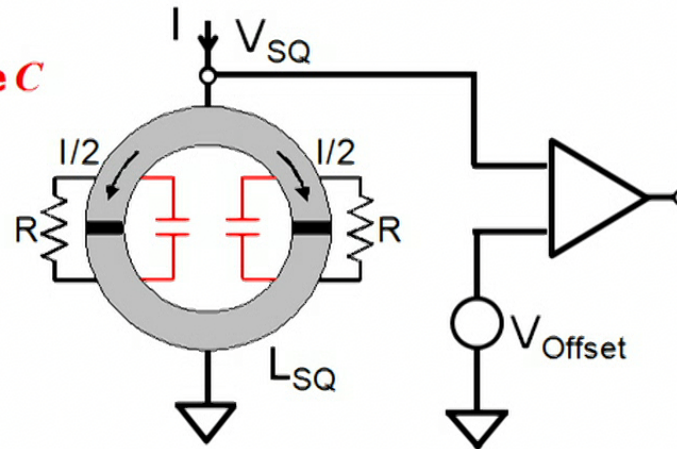
overlap area:
ca. 25...30 μm^2

$$C_{JJ*} = C_{JJ} + C_{\text{overlap}} \\ \approx 0.2\text{pF} + 0.2\text{pF}$$

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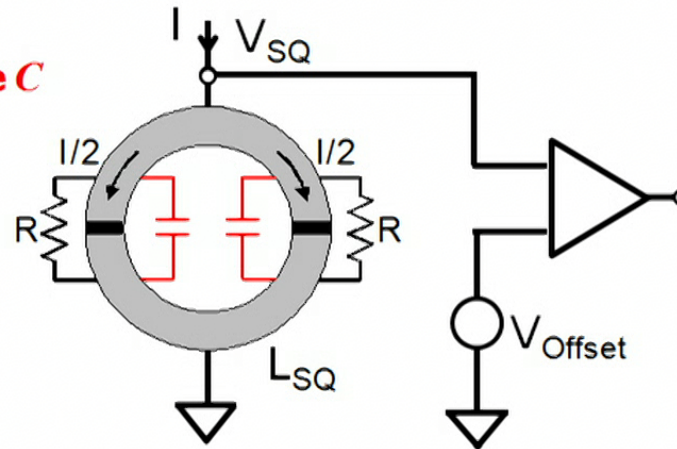
JJ damping requirement:

$$R^2 C < \Phi_0 / 2\pi I_C$$

Magnetic flux noise

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JJ damping requirement:

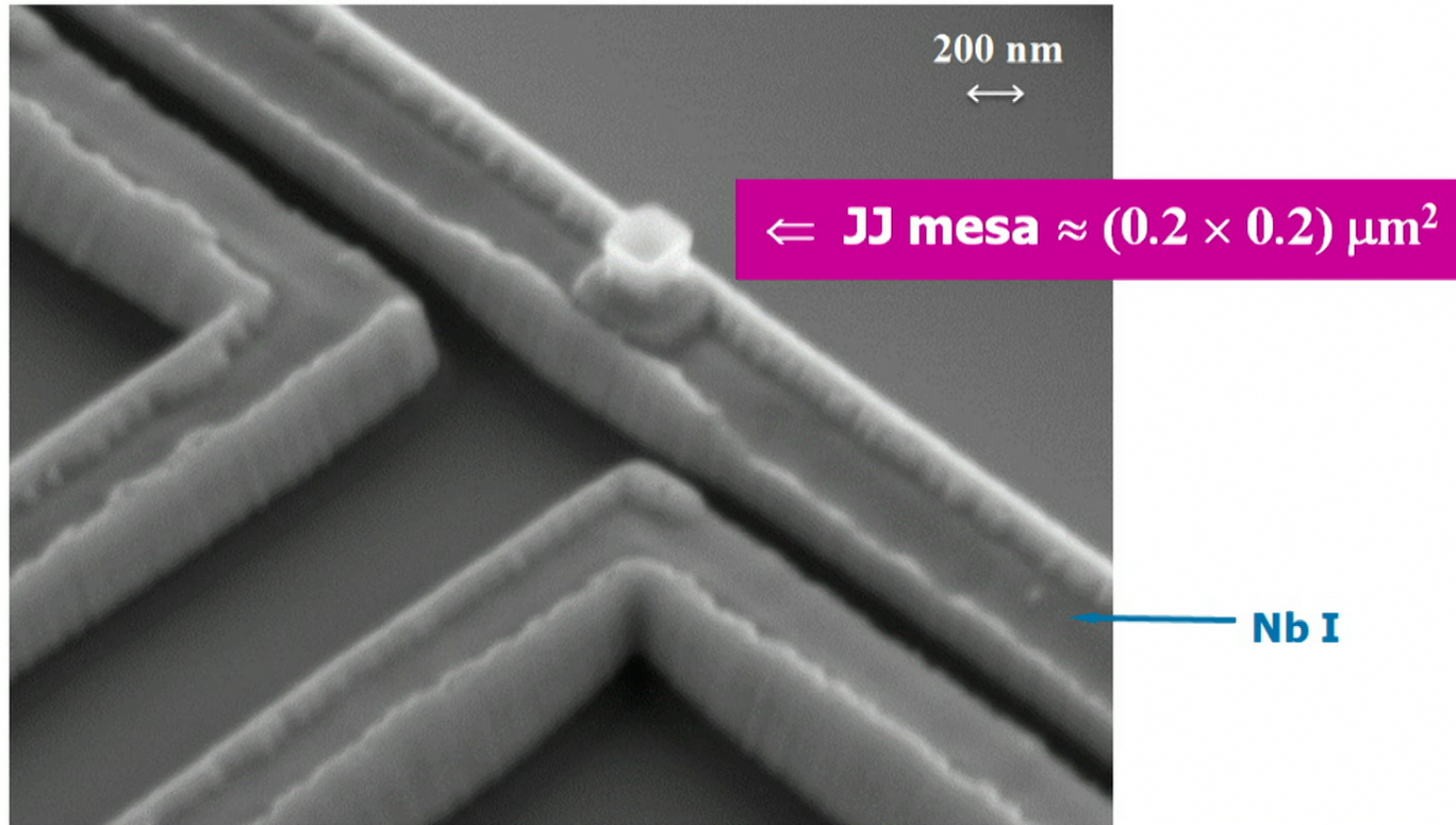
$$R^2 C < \Phi_0 / 2\pi I_C$$

$\Rightarrow$ reduce JJ size

Sub- μm JJs for SQUID sensors



- **electron beam lithography** + chemo-mechanical polishing, reactive ion etching



Sub- μm JJs for SQUID sensors



- **electron beam lithography** + chemo-mechanical polishing, reactive ion etching

- **EBL-JJ process currently in development: $(0.8 \times 0.8) \mu\text{m}^2$**

size	L_i / nH	$\delta I / \delta \Phi / \mu\text{A}/\Phi_0$
XS	27	2.3
S	65	1.3
M	150	0.8
L	400	0.5
XL	1000	0.3
XXL	1800	0.23

$\varepsilon_c / \hbar$
<20
<15

expected at 0.3K

Electromagnetic Interference - EMI

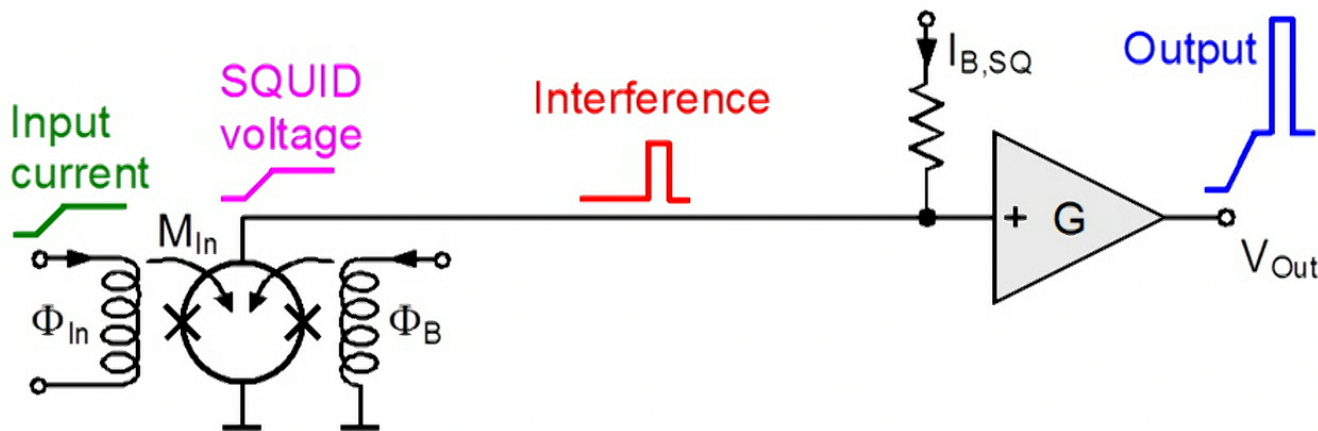


- **common problem in SQUID setups: EMI**
- via SQUID sensor → magnetic shielding
- interference along readout wiring: optimal shielding may not be possible

Electromagnetic Interference - EMI

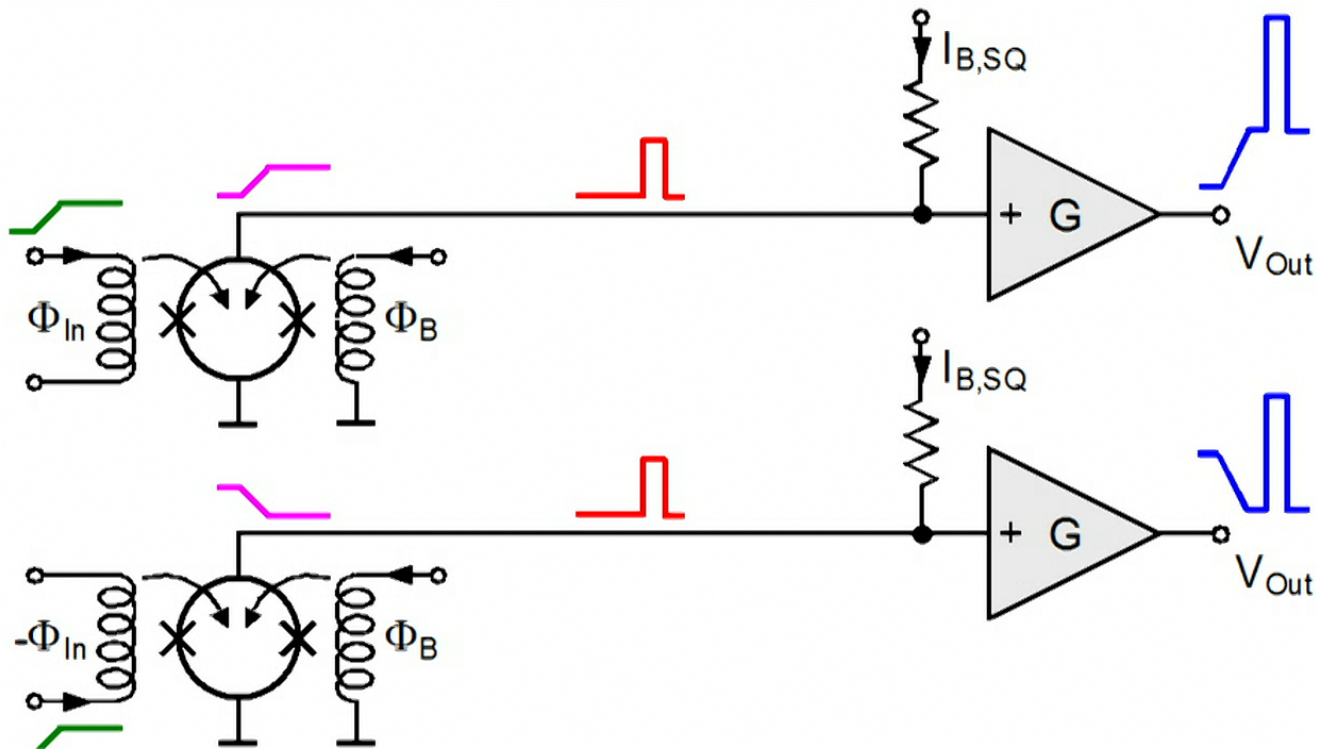


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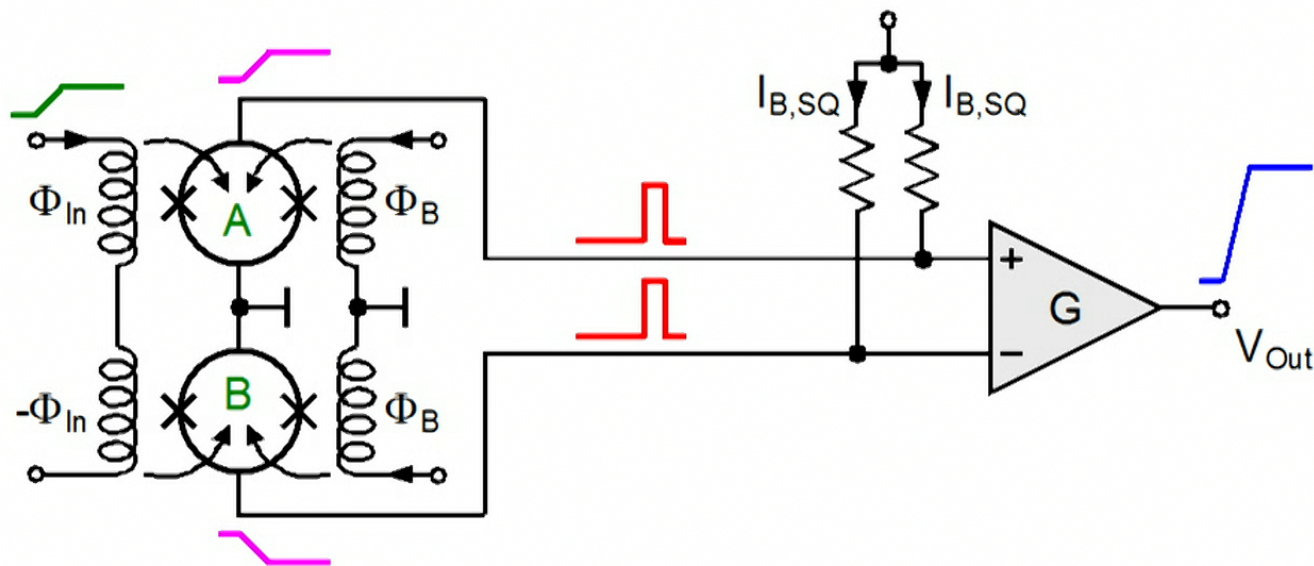
SQUID sensor w/ differential output

- two identical SQUID sensors, but inverted input polarity



SQUID sensor w/ differential output

- two identical SQUID sensors, but inverted input polarity
- combine both sensors, read out with differential amp

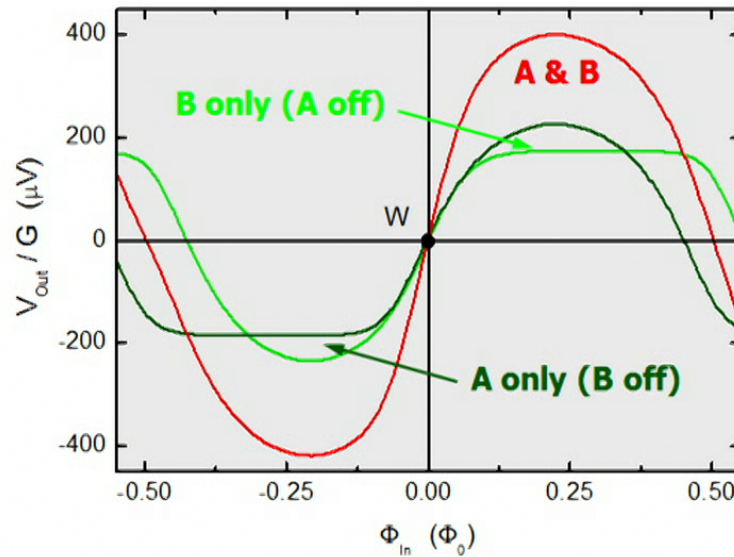


diffSQUID - demo

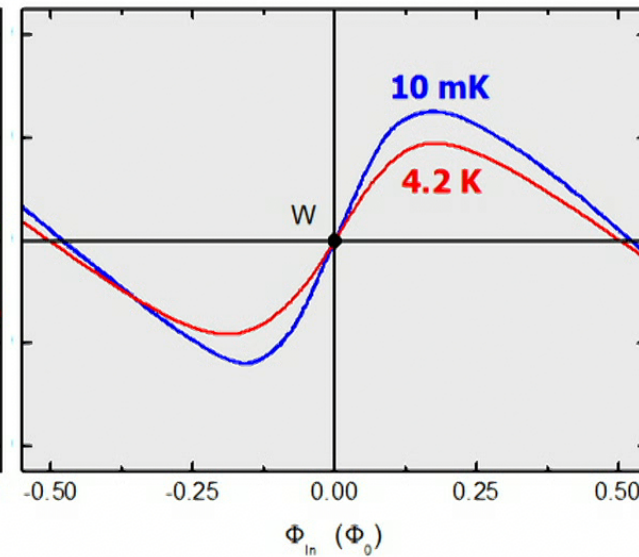


- two identical SQUID sensors, but inverted input polarity
- combine both sensors, read out with differential amp

two 16-SQUID series arrays A and B
unloaded, 4.2 K



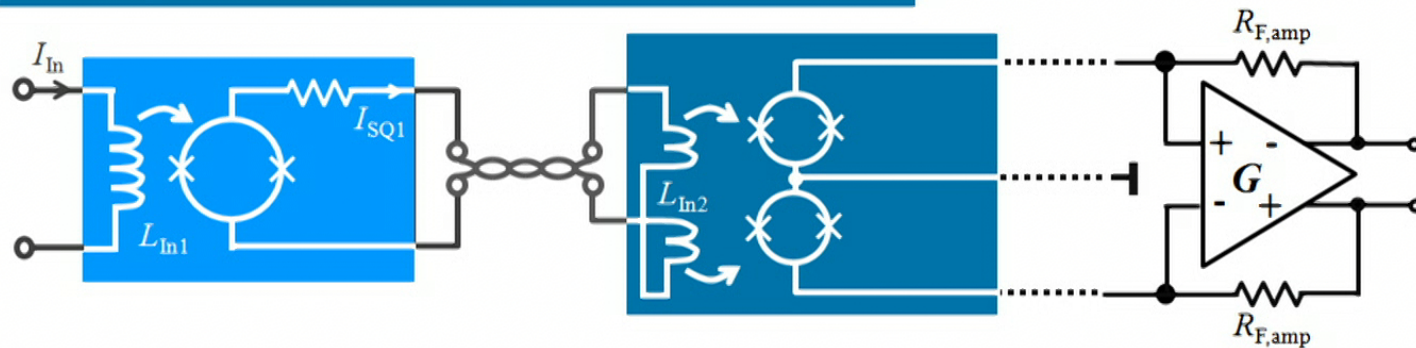
two 16-SQUID series arrays wired as diffSQUID
 $2 \times 50 \Omega$ load



diffSQUID – signal booster



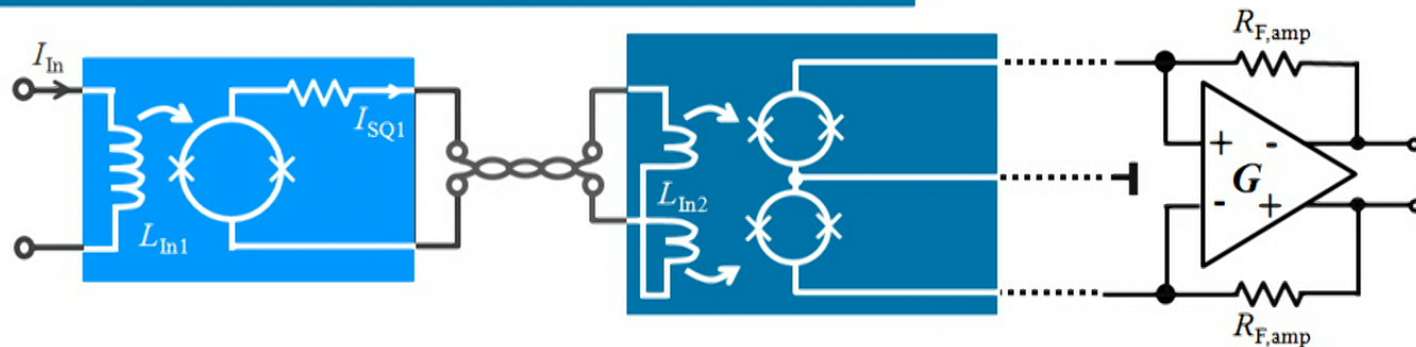
- diffSQUID for amplifier stage in SQUID cascades



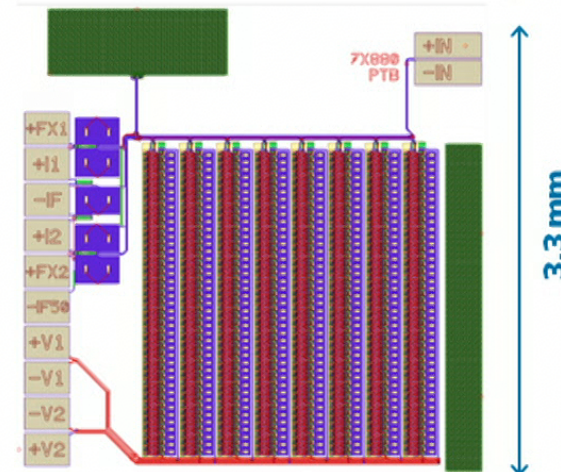
diffSQUID – signal booster



- diffSQUID for amplifier stage in SQUID cascades



- **serial-parallel SQUID array**
two halves: 80-S $\times$ 4-P (1280 JJs)
- **total input inductance** $L_i = 40$ nH
- **dynamic resistance** $R_{\text{dyn}} \approx 120$ Ω
- **dissipation** $P_{\text{diss}} \approx 200$ nW
- **output: 3 mV_{p-p}** into 2×50 Ω load



Summary



- **LTS dc-SQUID sensors 50 years after their invention**
 - *reliable cryoelectronic circuits based on thin-film technology*
 - *very versatile and sensitive devices for various precision measurements*
- **PTB SQUID sensors**
 - *multi-purpose Nb-Al/AlO-Nb-based SQUID current sensors*
single SQUIDs and integrated 2-stage SQUID cascades
 - *for 4.2 K and below ; $\epsilon < 50 \hbar$ @ 300mK*
 - *highly sensitive magnetometers*