

Title: Accelerating an axionic dark matter search with quantum technology

Date: Aug 23, 2017 09:30 AM

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Abstract:

## Outline (and summary)

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axion dark matter search: a microwave measurement problem

HAYSTAC search operates at the quantum limit

accelerating axion search with squeezing  
2.5 times faster than quantum limit possible today  
10-fold speed up with technical progress

accelerating axion search with photon counting  
10,000-fold speed up might be possible



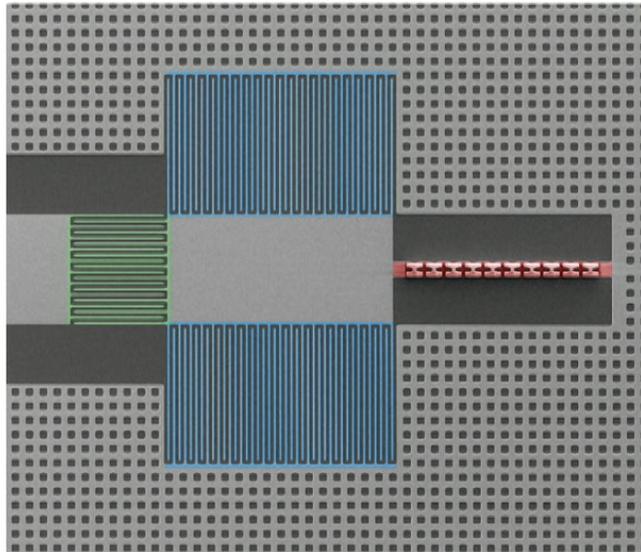


# Accelerating axion dark matter searches with quantum information technology

Haystac 

## JILA, U. of Colorado

Konrad Lehnert  
Maxime Malnou  
Daniel Palken



## Yale (Haystac)

Benjamin Brubaker  
Ling Zhong  
Kelly Backes  
Steve Lamoreaux

## UC Berkeley

Maria Simanovskaia  
Saad Al Kenany  
Samantha Lewis  
Jaben Root  
Nicholas Rapidis  
Isabella Urdinaran  
Karl van Bibber

## Yale (Theory)

Steve M. Girvin  
Huaixiu Zheng  
Matti Silveri,  
R. T. Brierley,  
Konrad Lehnert (YQI visitor)

YQI

arXiv:1607.02529



NIST



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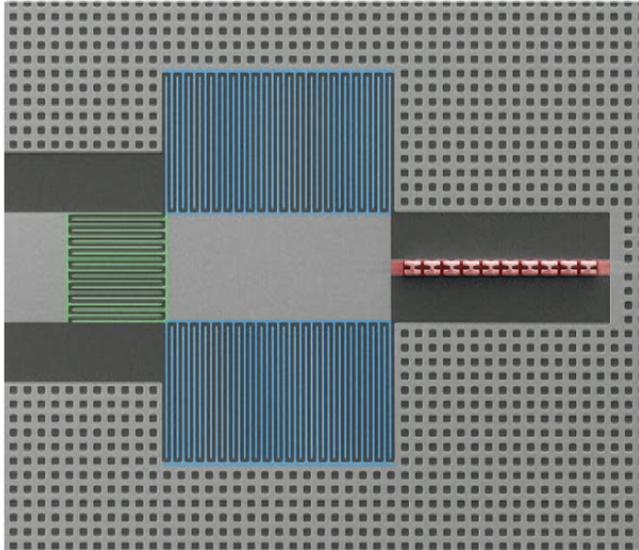
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# Axion dark matter search

# Hypothetical axion: a light particle that is cold and dense enough to contribute to dark matter

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mechanism to resolve strong-CP problem (Peccei and Quinn)

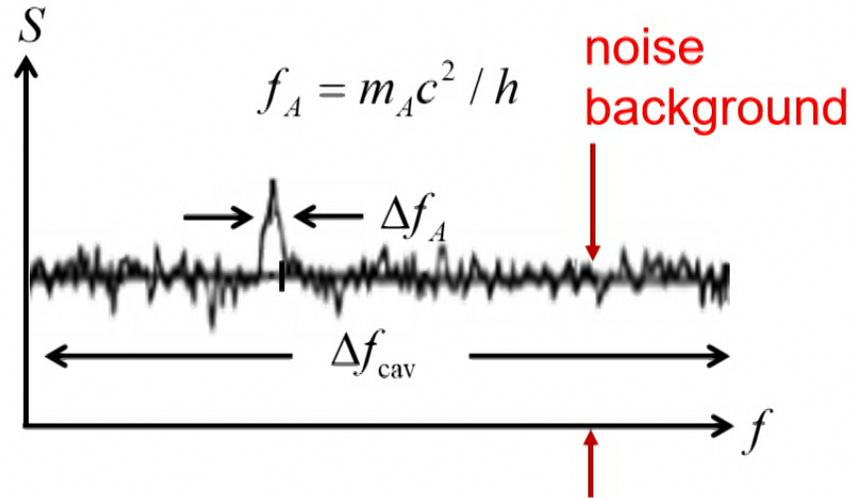
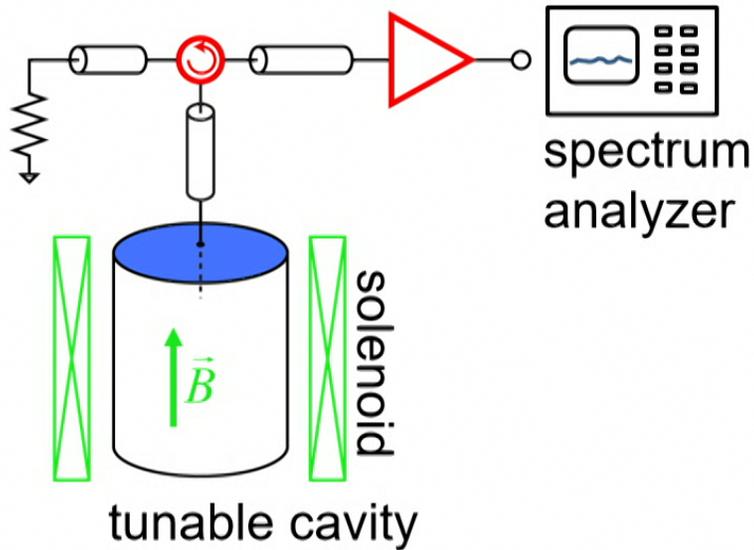
associated particle (axion) is dark matter candidate

mass approximately  $2 \mu\text{eV} < m_a c^2 < 2000 \mu\text{eV}$

as a frequency  $500 \text{ MHz} < m_a c^2 / h < 500 \text{ GHz}$



# Scan narrowband cavity to search for resonant axion to photon conversion (Sikivie 1983)



tune -> wait and integrate -> tune

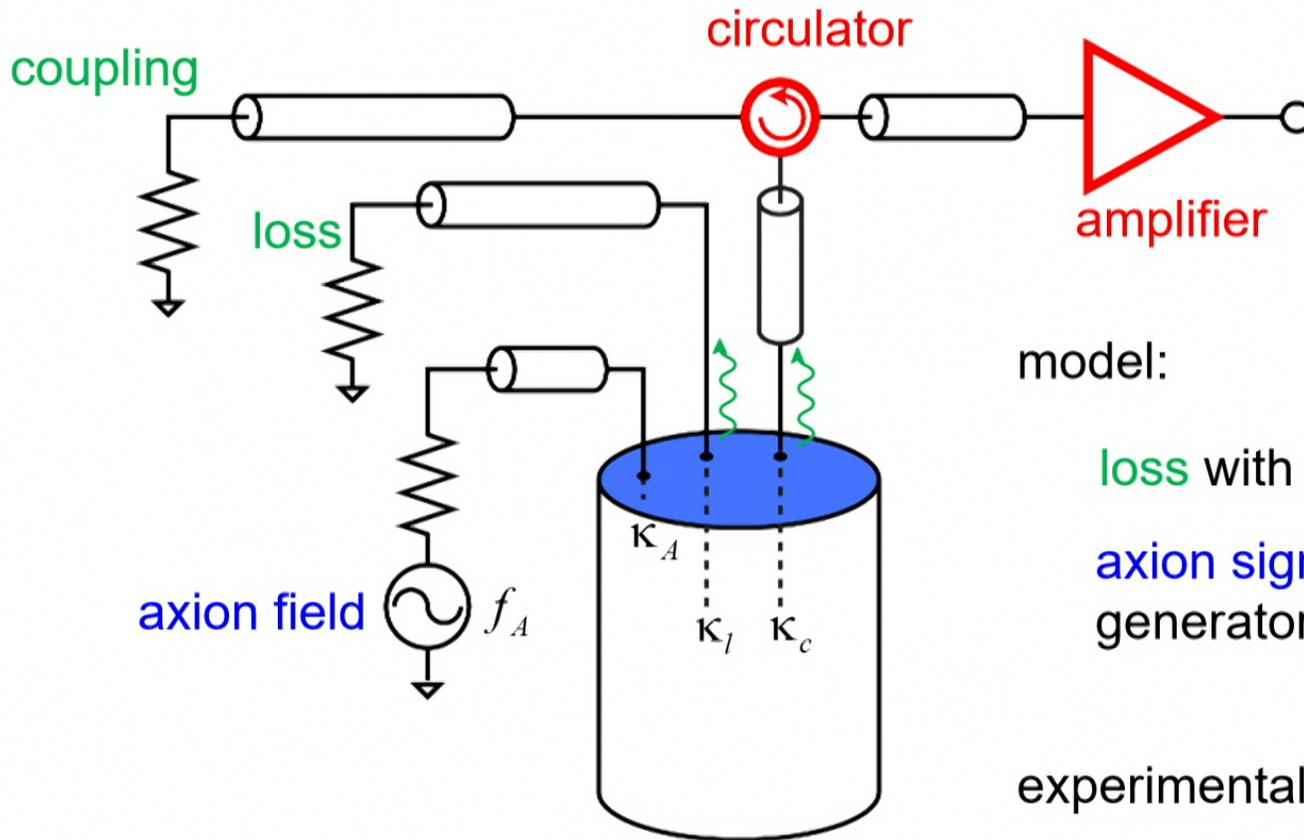
axion line narrower than cavity

$$\frac{f_A}{\Delta f_A} \approx 10^6 \quad \frac{f_{cav}}{\Delta f_{cav}} \approx 10^4$$

---

# Noise in an axion haloscope

# Signal and noise can be modeled as a microwave network



model:

loss with fictitious port

axion signal with weakly coupled generator  $\kappa_A \ll \kappa_l$

experimental constraints today

$$\kappa_A \ll 2\pi\Delta f_A \ll \kappa_l$$

# Microwave frequency fluctuations form the background for axion detection

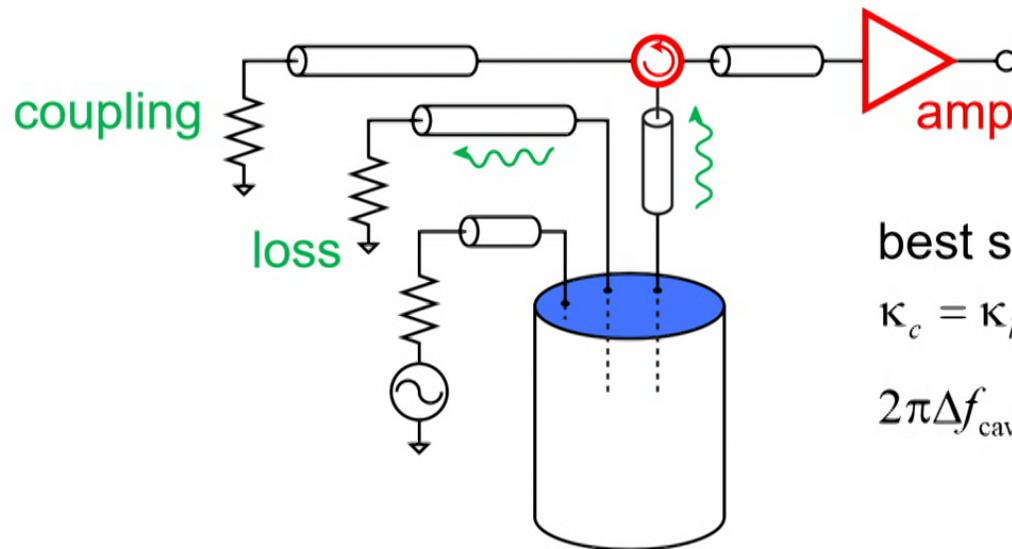
noise sources:

amplifier noise

cavity dissipation

$$S_{\text{amp}} = hf (N_{\text{add}})$$

$$S_d = hf \left( \frac{1}{\exp(hf / k_B T) - 1} + \frac{1}{2} \right) = hf \left( N_T + \frac{1}{2} \right)$$



best sensitivity:

$$\kappa_c = \kappa_l$$

$$2\pi\Delta f_{\text{cav}} = \kappa_c + \kappa_l$$

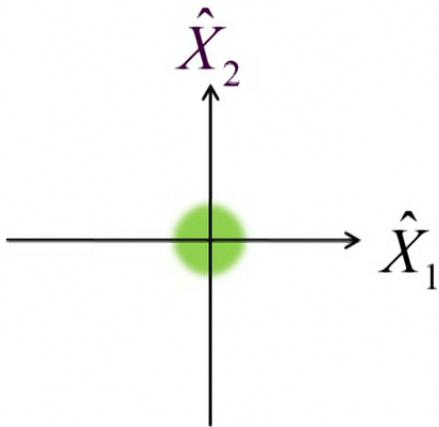
# Cool axion cavity to reach quantum limit

$$k_B T \ll \hbar \omega_{\text{cav}} \Rightarrow S_d = \hbar \omega_{\text{cav}} \left( \frac{1}{2} \right)$$

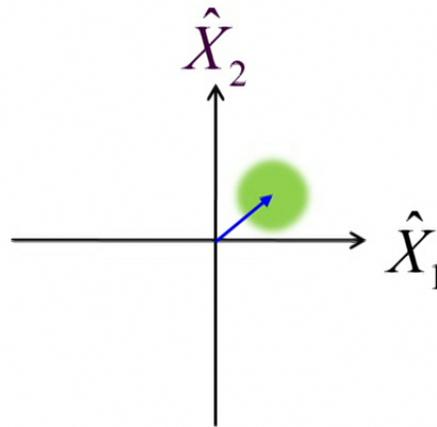
amplifiers measure cavity quadratures  $X_1$  and  $X_2$

$$\hat{H}_{\text{cav}} = \frac{\hbar f}{2} (\hat{X}_1^2 + \hat{X}_2^2)$$

$$[\hat{X}_1, \hat{X}_2] = i \Rightarrow \Delta X_1 \Delta X_2 \geq \frac{1}{2}$$



vacuum state



axion displaced state



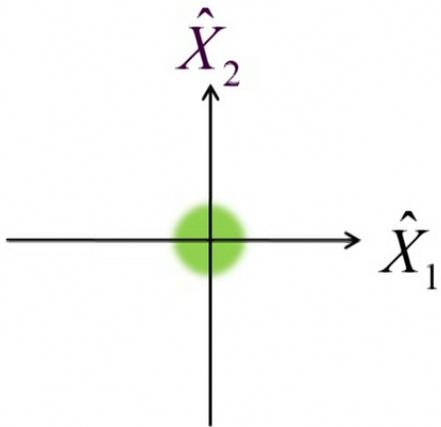
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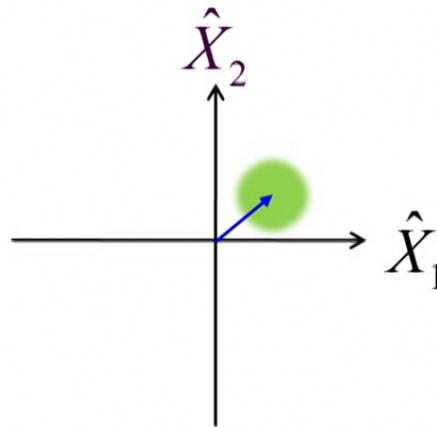
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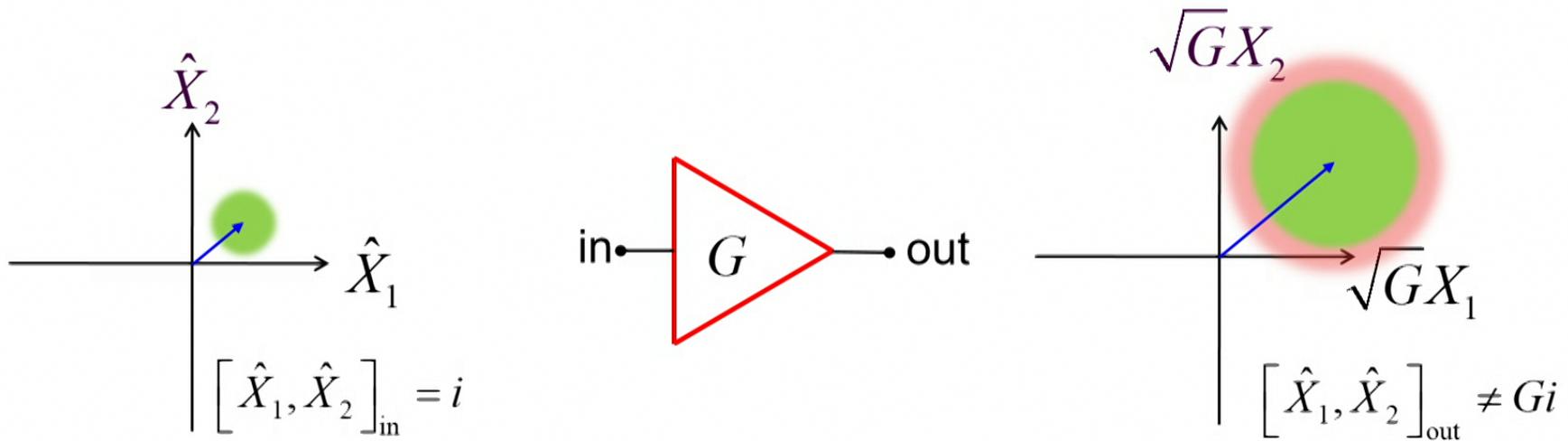


vacuum state



axion displaced state

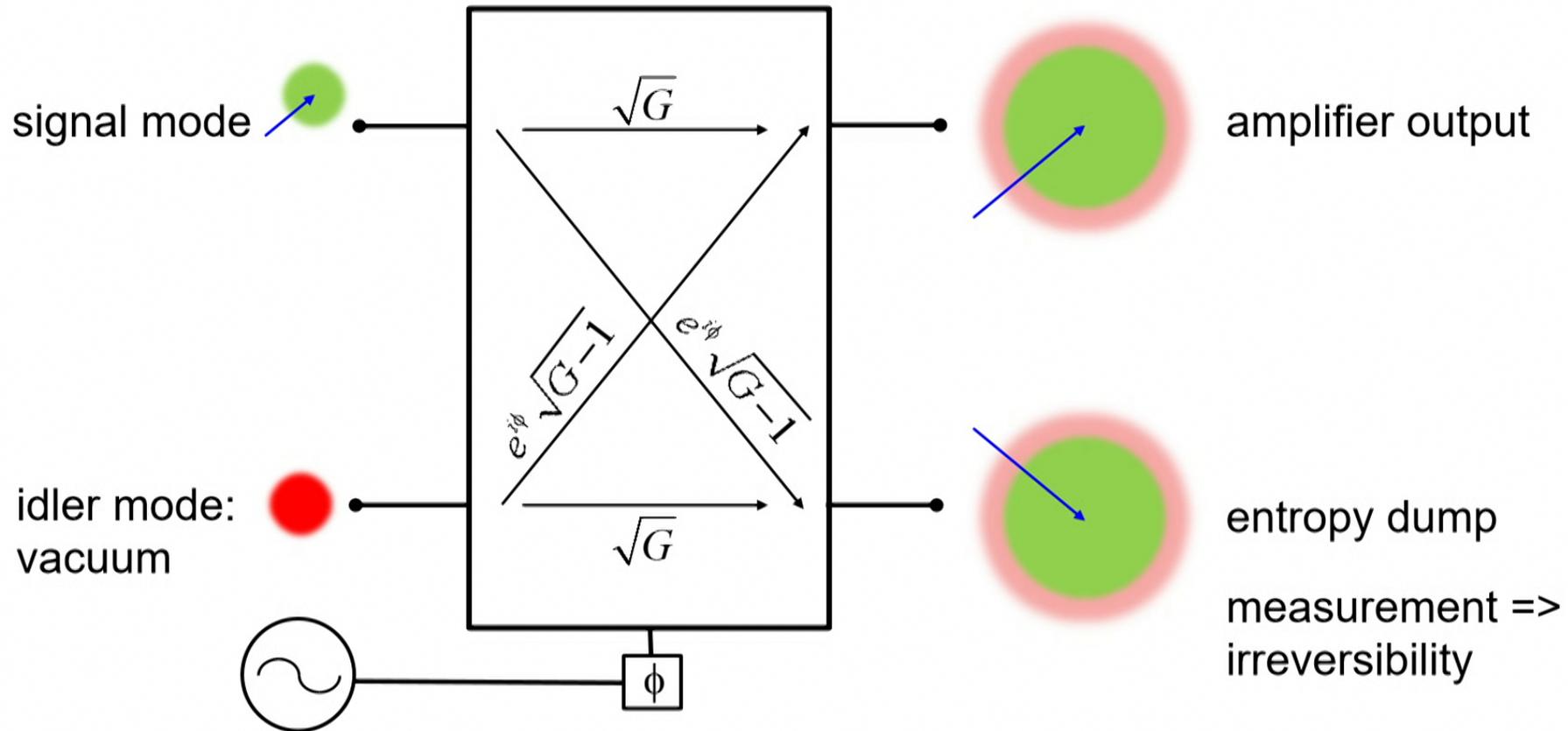
# Quantum limited amplifiers add half a photon of noise



phase space volume not conserved => added noise

$$N_{\text{add}} \geq \frac{1}{2}$$

# Josephson parametric amplifiers reach the quantum limit



R. Movshovich, B. Yurke *et al.* *Phys. Rev. Lett.* **65**, 1419–1422 (1990).  
M.A. Castellanos-Beltran, KWL, *et al.*, *Nature Physics* **4**, 929 - 931 (2008).  
N. Bergeal, M. Devoret *et al.*, *Nature* **465**, 64–68 (2010).

# Axion dark matter search at the quantum limit

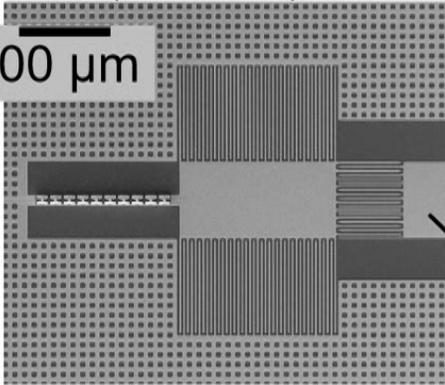


Haloscope At Yale Sensitive To Axion Coupling

# Overview of the experiment and its integration

JPA (tunable)

100  $\mu\text{m}$



microwave cavity  
(tunable)



$^3\text{He}/^4\text{He}$   
dilution  
refrigerator  
 $T = 126 \text{ mK}$



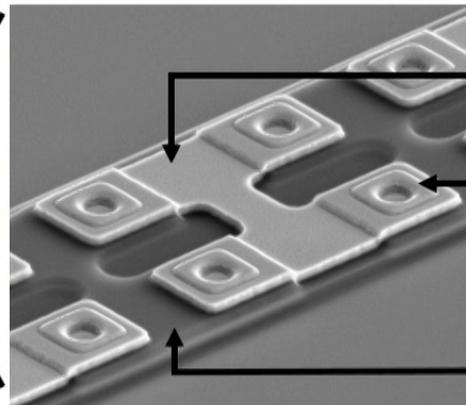
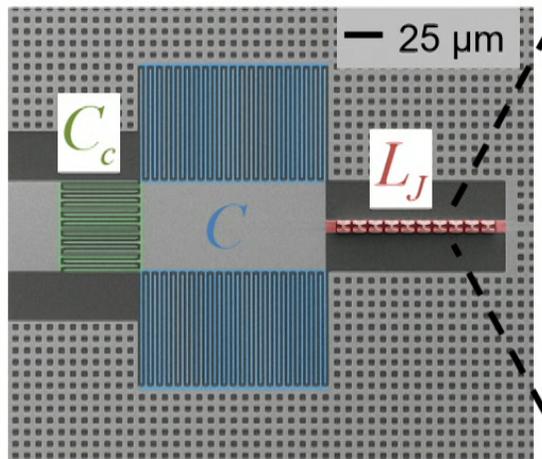
magnet : 9.4 T, 10 L



located at Yale's Wright laboratory  
Steve Lamoreaux's group

# The JPA contains a flux tunable, dissipationless, and nonlinear resonant circuit

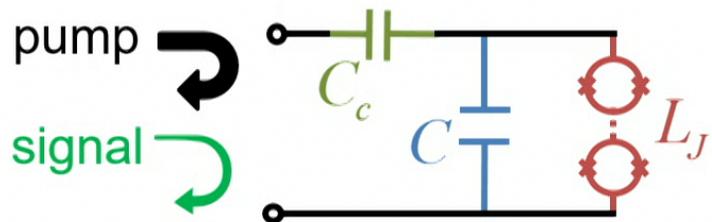
SQUID array



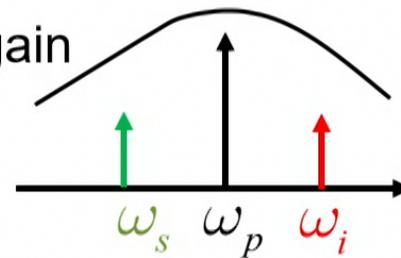
SQUID  
two junction loop:

$$\text{⊗} L_J(I^2, \Phi)$$

nonlinear tunable  
inductor



JPA gain

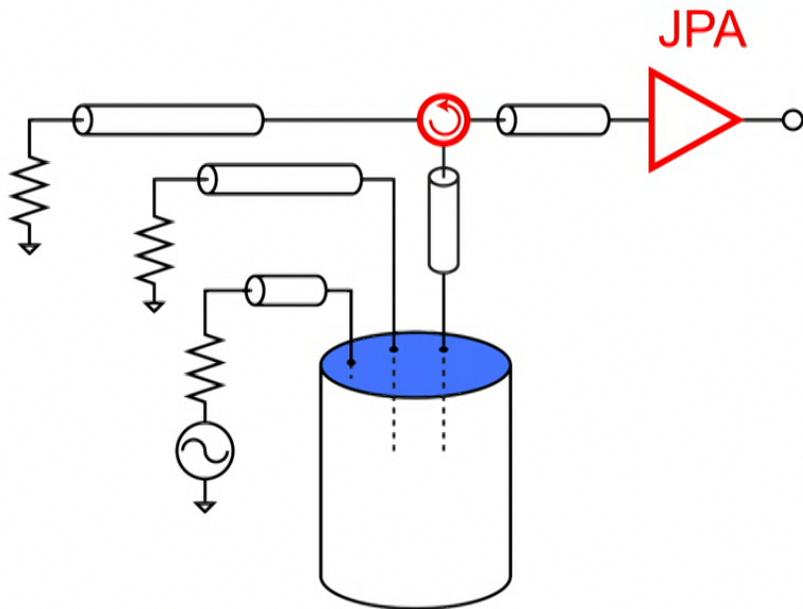


4 photon process

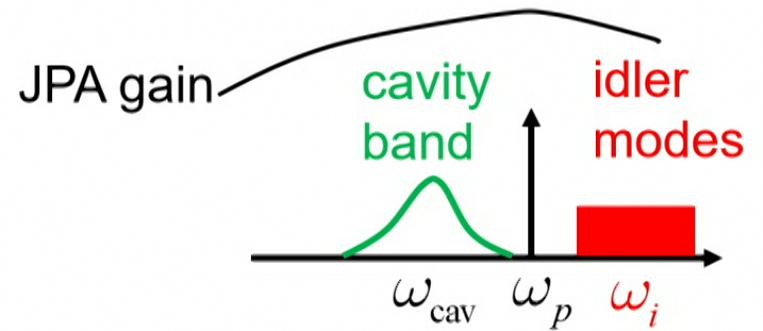
$$2\omega_p = \omega_s + \omega_i$$



# Reaching the quantum limit with a JPA: phase insensitive operation



phase insensitive:  
cavity detuned from pump

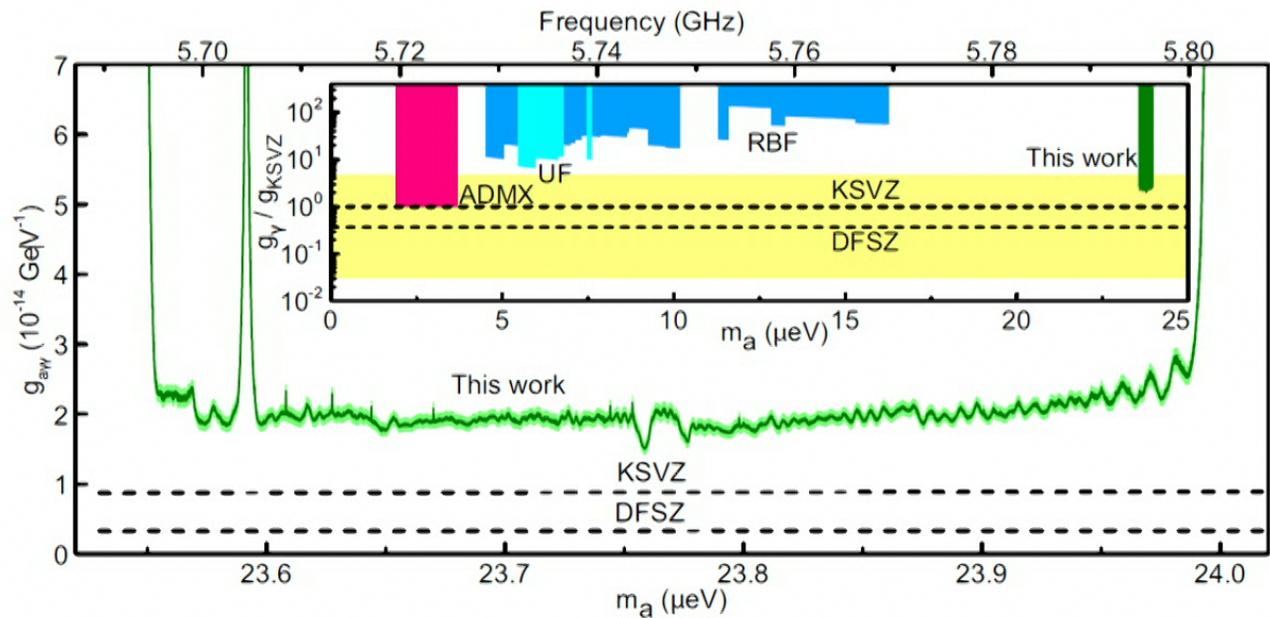


Al Kenany et al. *Nucl. Instr.* **854**, 11-24 (2017)

# First near-quantum limited haloscope data

added noise: 0.63 photons

1.5 months data: 100 MHz scanned (no axion)



Brubaker et al. *Phys. Rev. Lett.* **118**, 061302 (2017)

since publication:

200 MHz scanned

operation at quantum limit

upgrade in progress

# Josephson parametric amplifiers overcome quantum noise

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Idealization: prepare cavity in eigenstate of  $X_I$ , wait, noiselessly measure  $X_I$

JPA's prepare approximate eigenstates of  $X_I$  (squeezed states),  
and measure  $X_I$  noiselessly

Squeezed state receiver increases scan rate, not ultimate sensitivity

# Quantum noise limits axion search rate

$X_1$  and  $X_2$  don't commute with **Hamiltonian** or **each other**

$$S_d \rightarrow \frac{hf}{2} \quad S_{\text{amp}} \rightarrow \frac{hf}{2}$$



noise variance: 1 quantum (photon)

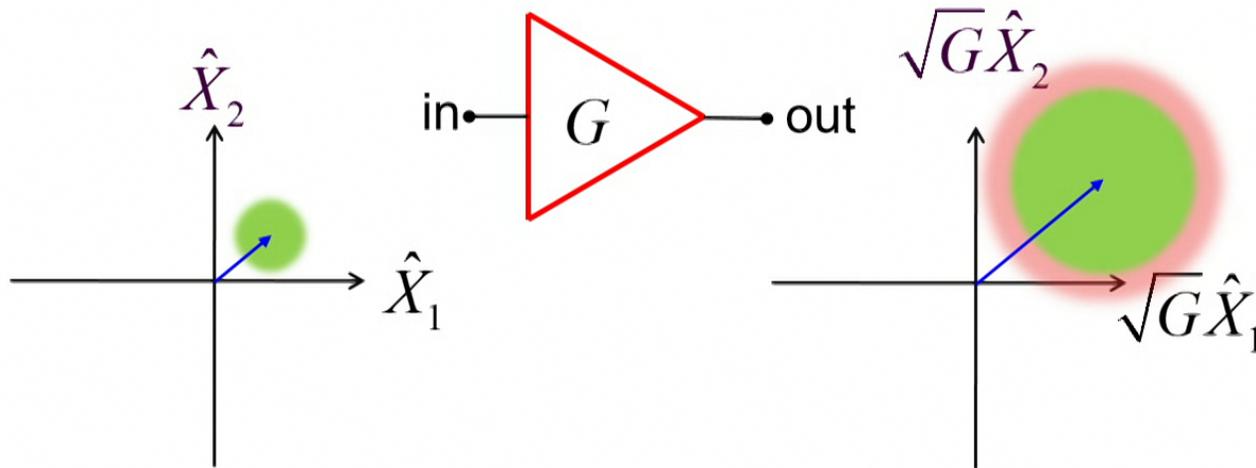


axion energy:  $10^{-3} - 10^{-4}$  photon

resolve signal in  $10^6 - 10^8$  averages

$$\frac{\delta S}{S} = \frac{1}{\sqrt{\Delta f_a \tau}} \quad \begin{array}{l} \tau \sim 3 \text{ minutes: each cavity resonance} \\ \sim \text{years: one octave} \end{array}$$

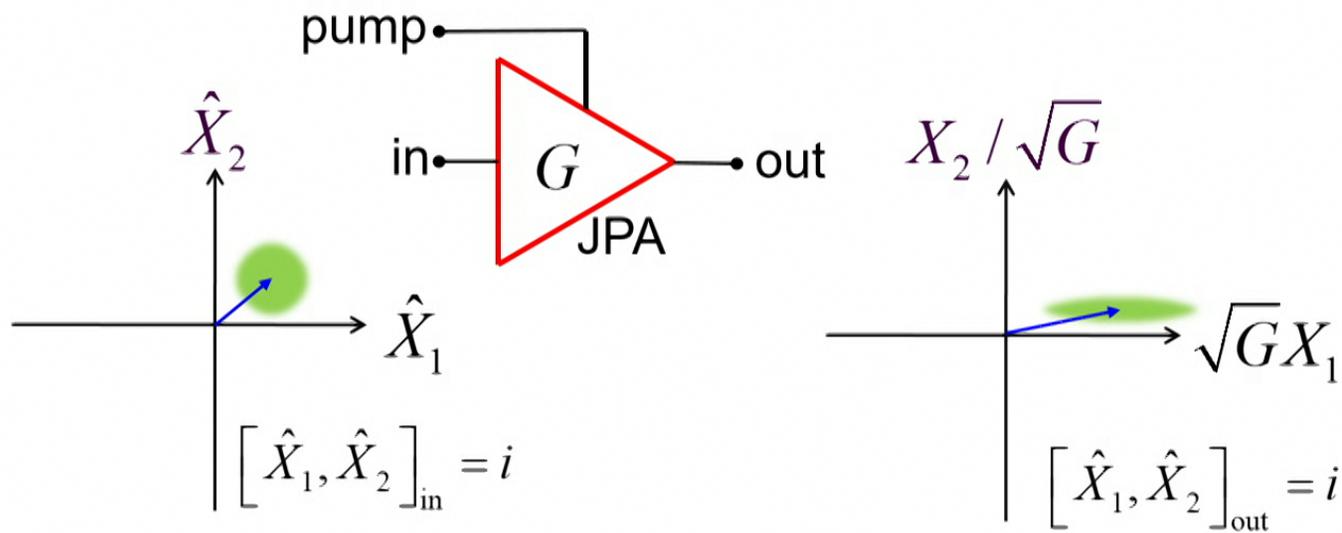
# Linear, phase-insensitive amplifiers must add noise



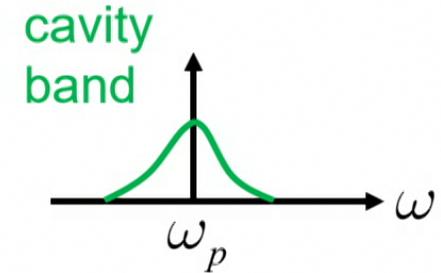
phase space volume not conserved => added noise

$$N_{\text{add}} \geq \frac{1}{2}$$

# Phase sensitive amplifier measures one quadrature noiselessly



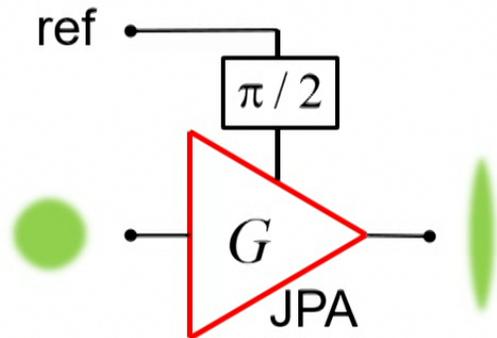
phase sensitive mode:  
pump resonant with cavity



phase space volume conserved  $\leq$  no added noise

$$N_{\text{add}} \geq 0$$

# Ideal JPA noiselessly transforms vacuum state into squeezed state



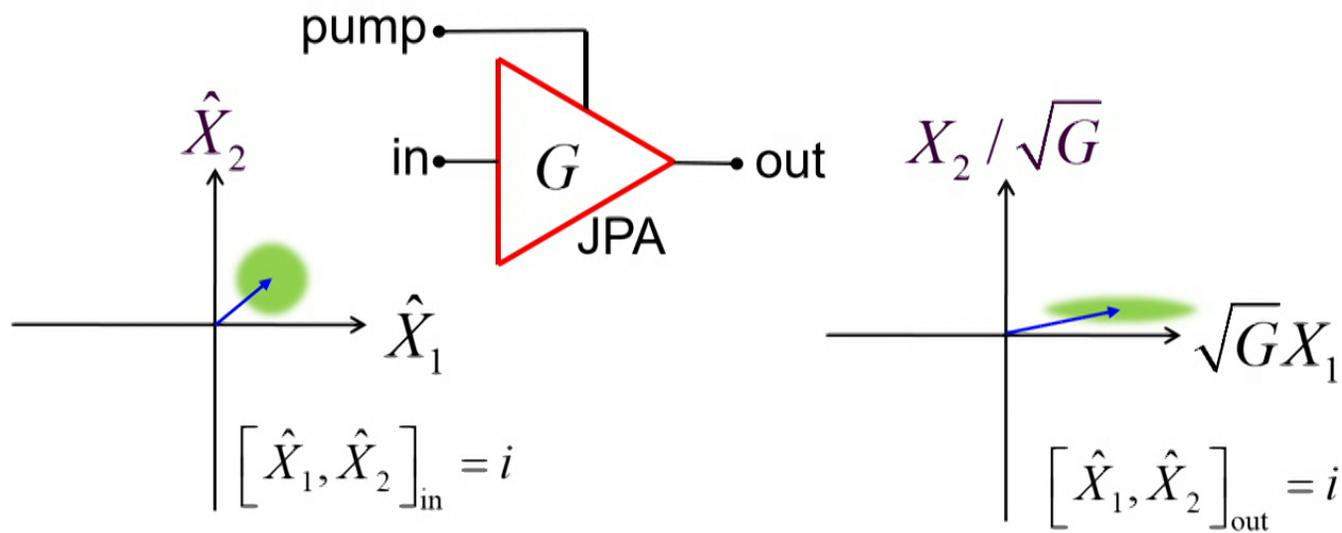
$$\text{var}(\hat{X}_2) = \frac{G}{2}$$

$$\text{var}(\hat{X}_1) = \frac{1}{2G}$$

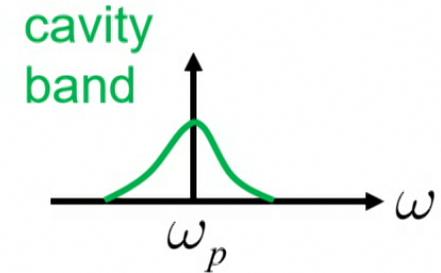
squeezed quadrature: quantum noise suppressed

use JPA to prepare cavity in squeezed state

# Phase sensitive amplifier measures one quadrature noiselessly



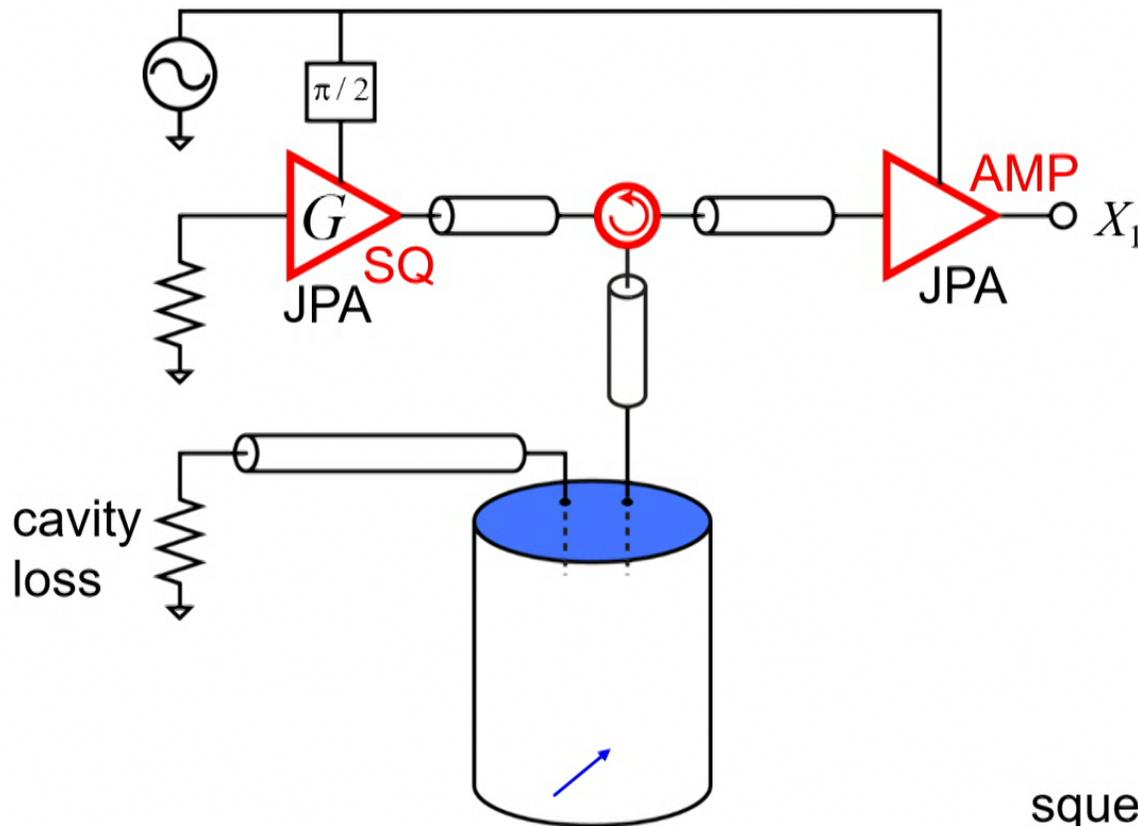
phase sensitive mode:  
pump resonant with cavity



phase space volume conserved  $\leq$  no added noise

$$N_{\text{add}} \geq 0$$

# Squeezing does not improve on-resonance and critically coupled sensitivity



axion signal at amplifier

$$\text{sig} \propto \frac{2\sqrt{\kappa_c \kappa_A}}{\kappa_c + \kappa_l - i\Delta}$$

$$\Delta = \omega_{\text{cav}} - \omega_A$$

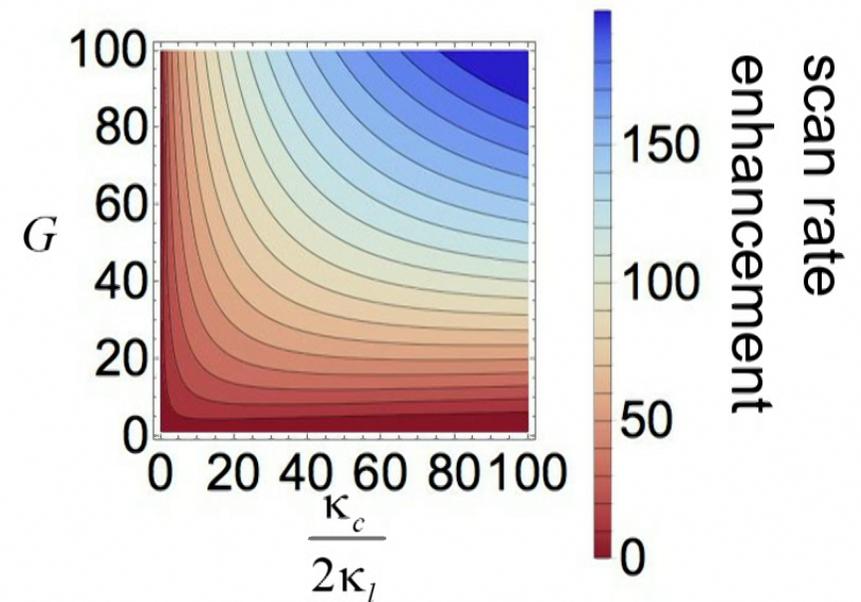
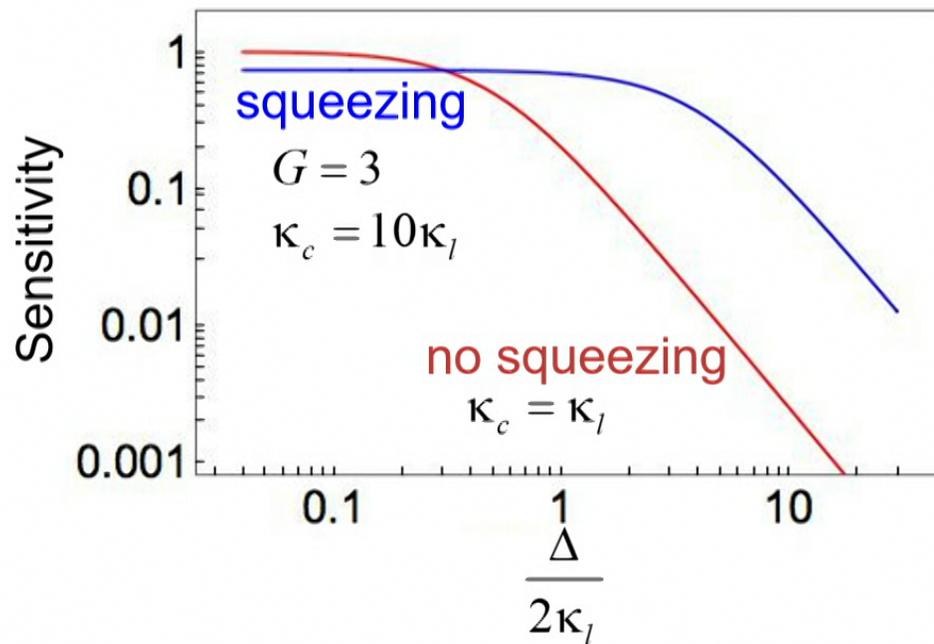
maximum: critical coupling on resonance

$$\kappa_c = \kappa_l \quad \text{sig} \propto \sqrt{\frac{\kappa_A}{\kappa_l}}$$

$$\Delta = 0$$

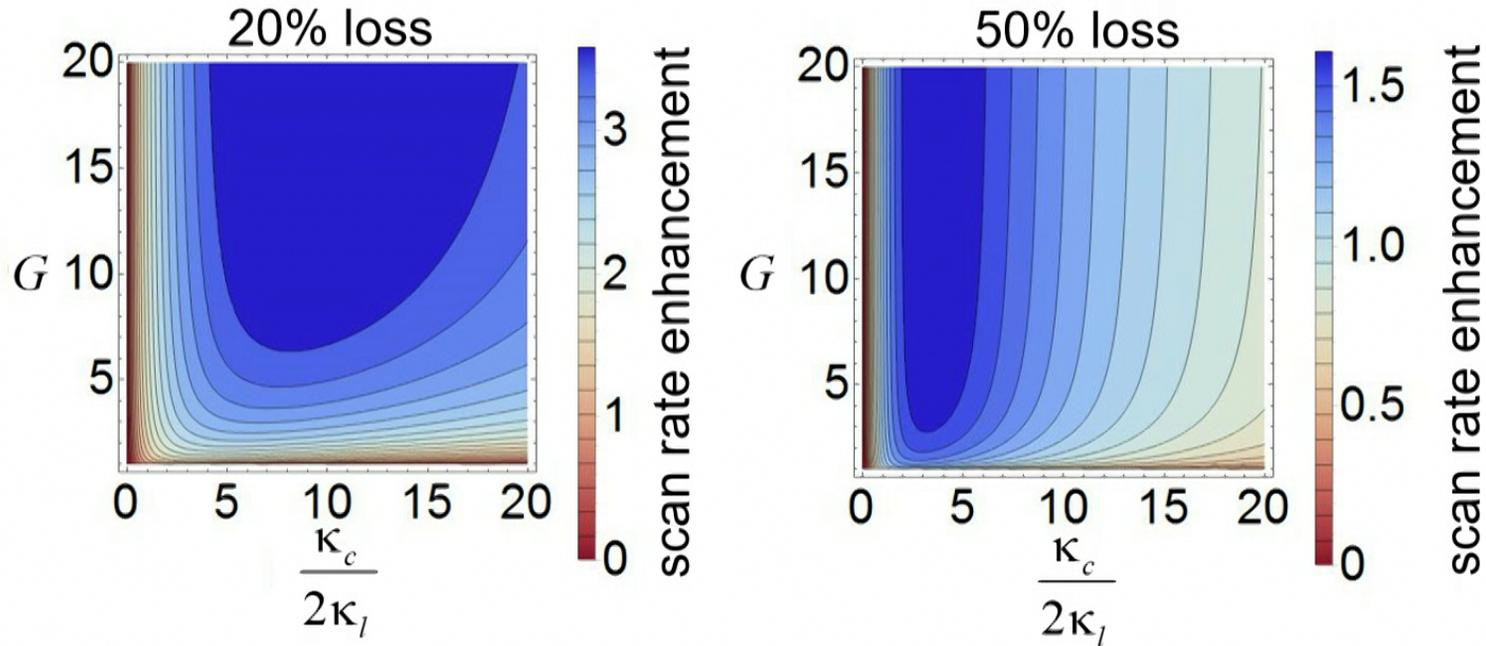
squeezed state absorbed in cavity

# Scan rate enhancement, perfect efficiency



slight reduction in sensitivity  
much larger bandwidth

# Propagation loss reduces benefit of squeezing

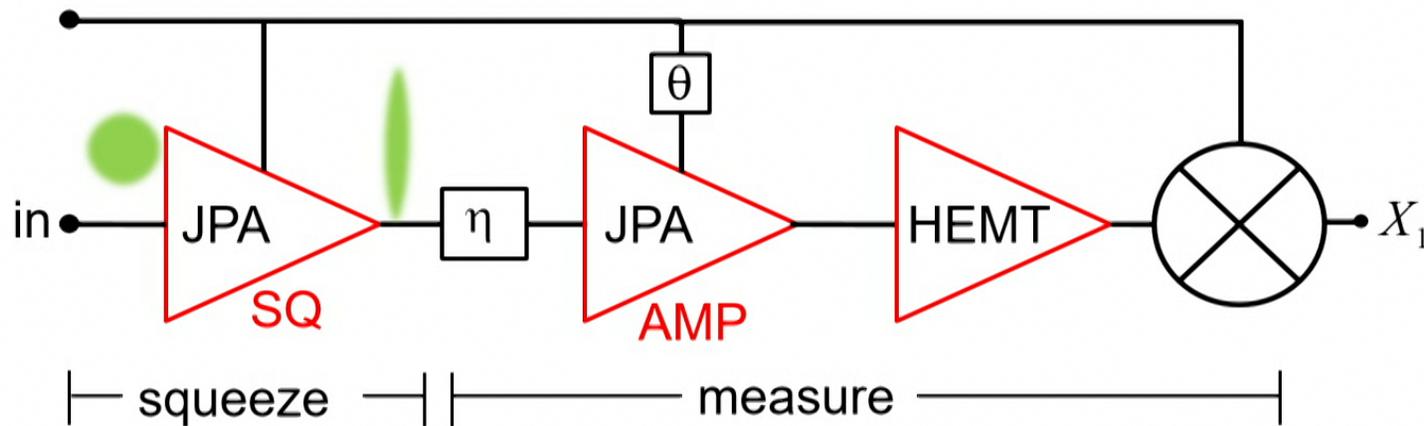


20% loss: scan rate x 3.5

50% loss: scan rate x 1.5

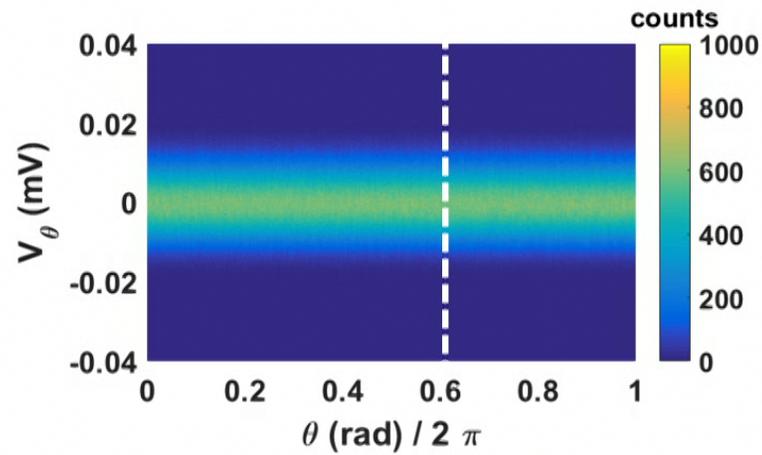
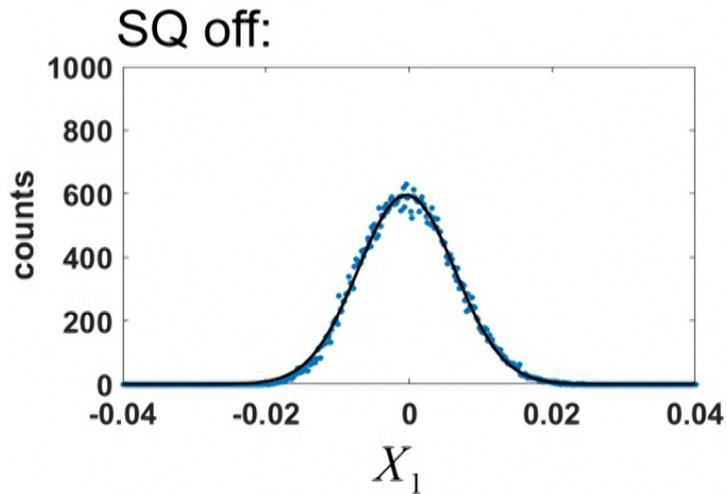
# Demonstration of squeezing and determination of loss: second JPA analyzes squeezed state created by first

pump (phase reference)



phase  $\theta$  chooses measured quadrature  
relative to squeezed quadrature

# Vacuum fluctuations are squeezed



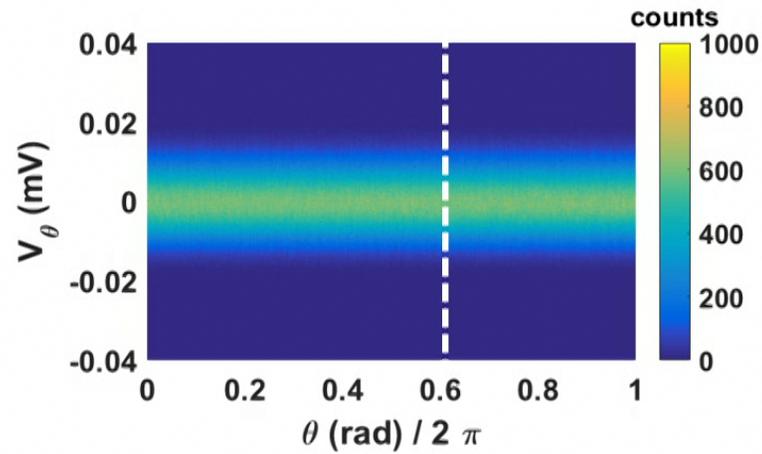
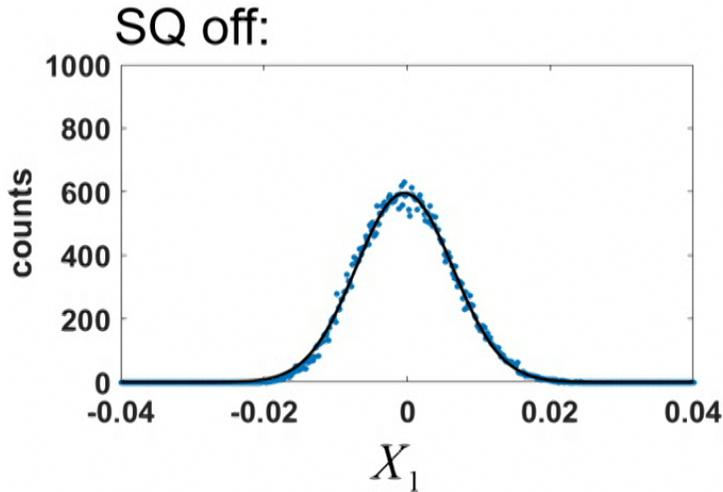
best performance

40% loss:  
scan rate x 2.5

next: deploy in  
HAYSTAC

F. Mallet, KWL et al.,  
PRL **106**, 220502 (2011).

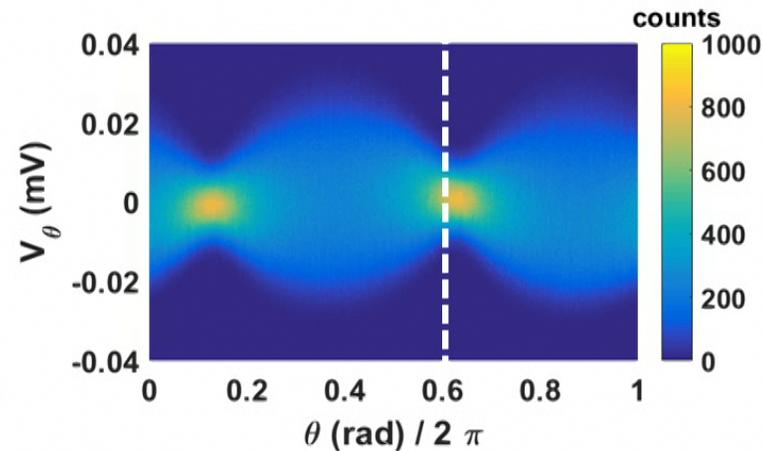
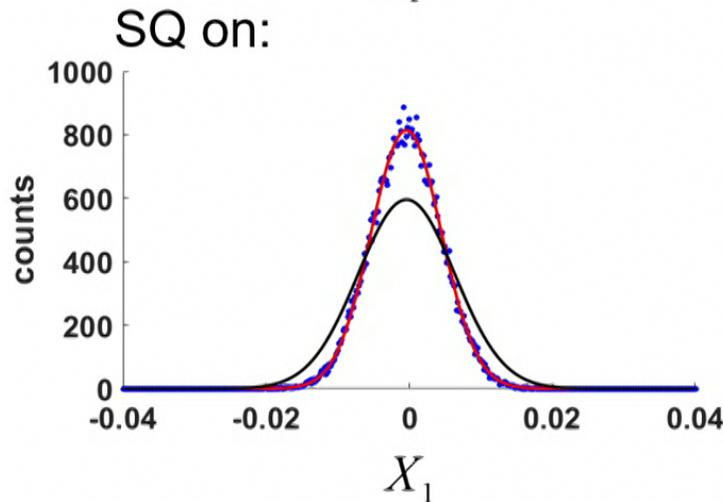
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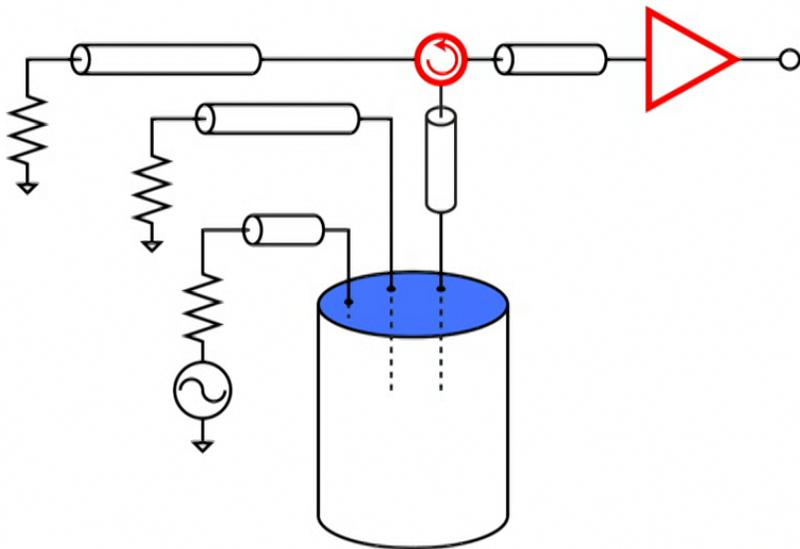
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# Both axion quadratures can be measured without quantum noise

32



axion field:

large amplitude coherent state  
weakly coupled

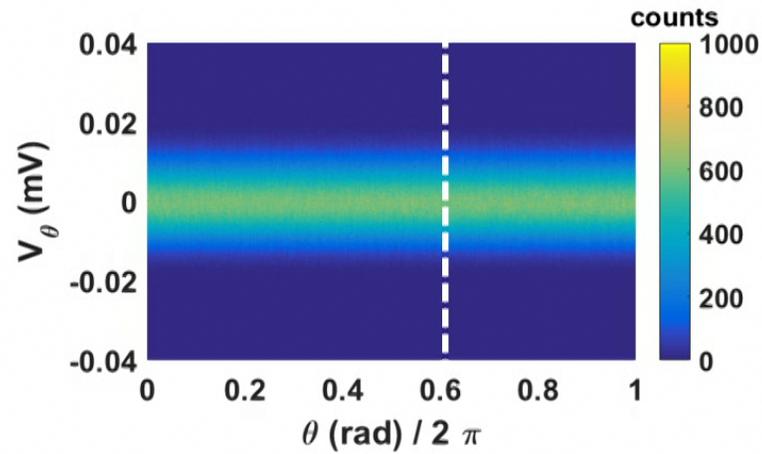
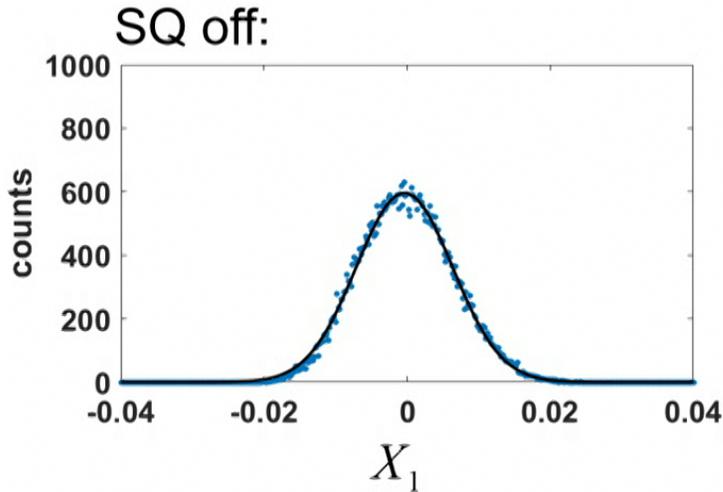
$$\hat{A} = \alpha + \delta\hat{A} \quad \kappa_A \ll \kappa_I$$

axion appears in Hamiltonian as a parameter

$$\hat{H}_{\text{cav}} \approx \hbar\omega_{\text{cav}} (\hat{X}_1^2 + \hat{X}_2^2) + \sqrt{\kappa_A} \text{Re}(\alpha) \hat{X}_1 + \sqrt{\kappa_A} \text{Im}(\alpha) \hat{X}_2$$

commutation relations don't limit knowledge of  $\alpha$

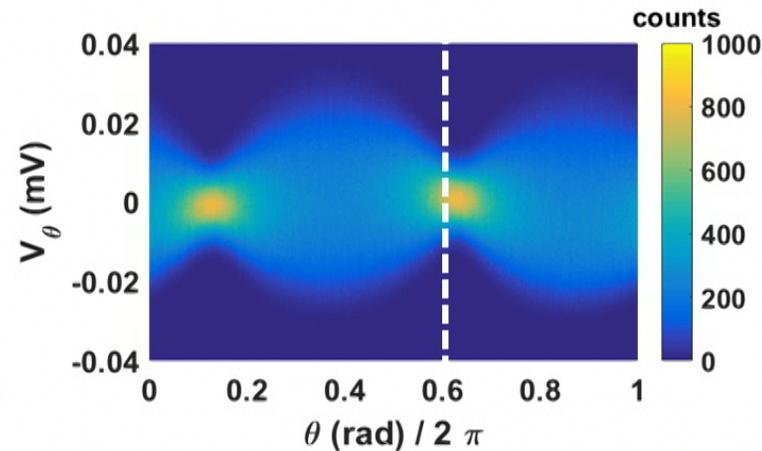
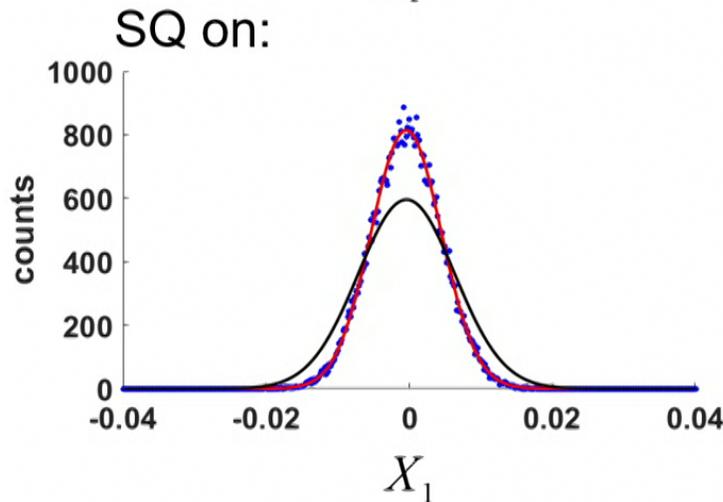
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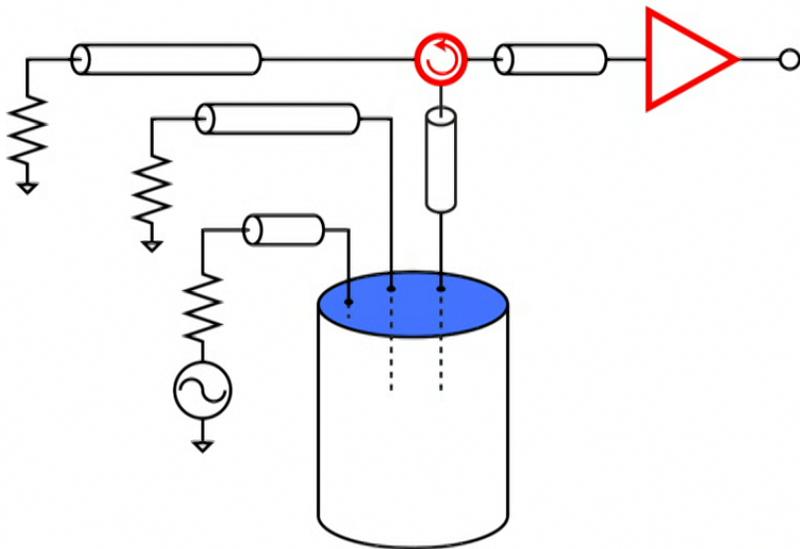
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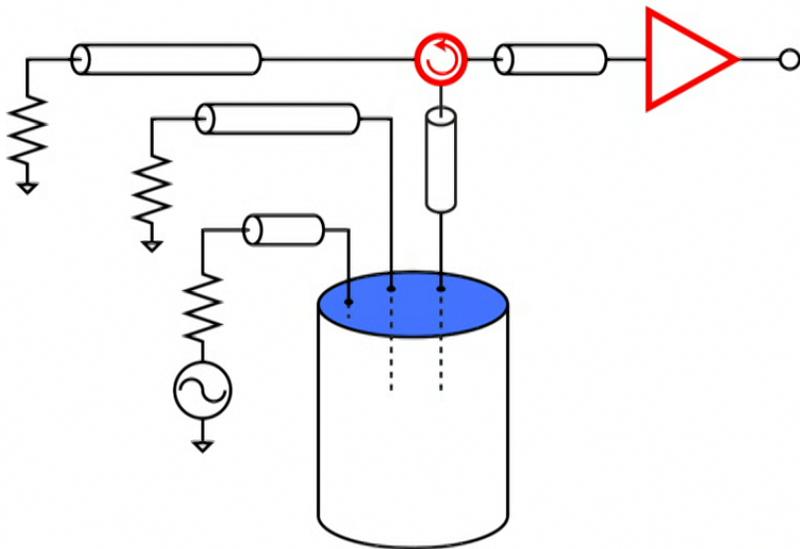
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commutation relations don't limit knowledge of  $\alpha$

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commutation relations don't limit knowledge of  $\alpha$



parameter estimation problem: no quantum policeman...

arXiv:1607.02529

# Circumventing the quantum limit with CQED photon counting

# Circuit quantum electrodynamical devices enable microwave photon counting in an axion experiment

Key idea: to a photon counter, vacuum is noiseless\*  
much less sensitive to transmission loss than squeezed state receiver

CQED devices efficiently detect microwave photons without destroying them (QND)

CQED: superconducting quantum bit + microwave cavities  
invented by Robert Schoelkopf and Michel Devoret

QND measurements => measure same photon many times => vanishing dark counts

\*Matsuki, S., and K. Yamamoto, 1991, *Phys. Lett. B* **263**, 523 (1991). [Carrack concept]  
S. K. Lamoreaux, K. A. van Bibber, KWL, G. Carosi *Phys. Rev. D* **88**, 035020 (2013).



axion hypothesis

$$\hat{H}_{\text{cav}} = \hbar\omega_{\text{cav}} \left( \hat{X}_1^2 + \hat{X}_2^2 \right) + \sqrt{\kappa_A} \text{Re}(\alpha) \hat{X}_1 + \sqrt{\kappa_A} \text{Im}(\alpha) \hat{X}_2$$

$$\hat{H}_{\text{cav}} = \hbar\omega_{\text{cav}} \left( a^\dagger a + \frac{1}{2} \right) + \sqrt{\kappa_A} \text{Re}(\alpha) \hat{X}_1 + \sqrt{\kappa_A} \text{Im}(\alpha) \hat{X}_2$$

null hypothesis

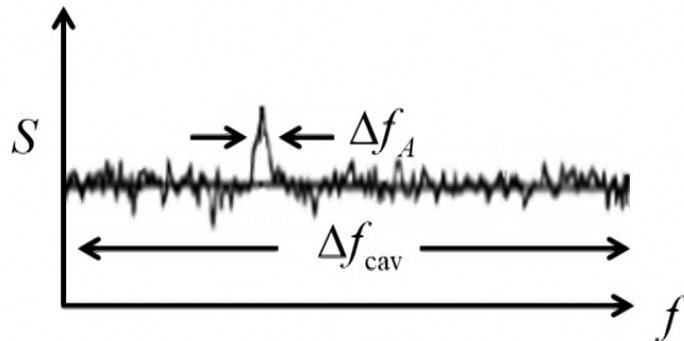
$$\hat{H}_{\text{cav}} = \hbar\omega_{\text{cav}} \left( a^\dagger a + \frac{1}{2} \right)$$

idealized notion

prepare cavity in ground state, wait, measure photon number

$N \neq 0 \Rightarrow$  axion

# Comparison between quantum limited amplifiers and photon counters



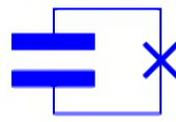
$$\frac{\text{counter scan rate}}{\text{amplifier scan rate}} \approx \frac{\Delta f_A}{\Delta f_{\text{cav}}} \frac{1}{N_T + n_{\text{dark}}}$$

linear amplifier resolves many possible axion lines simultaneously  $\frac{\Delta f_{\text{cav}}}{\Delta f_A} \sim 10 \rightarrow 100$

noise of photon counters: thermal back ground and dark count probability

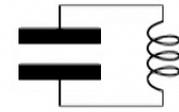
prefer photon counter when  $N_T + n_{\text{dark}} < 1\%$

# Transmon qubit: a strongly nonlinear LC circuit

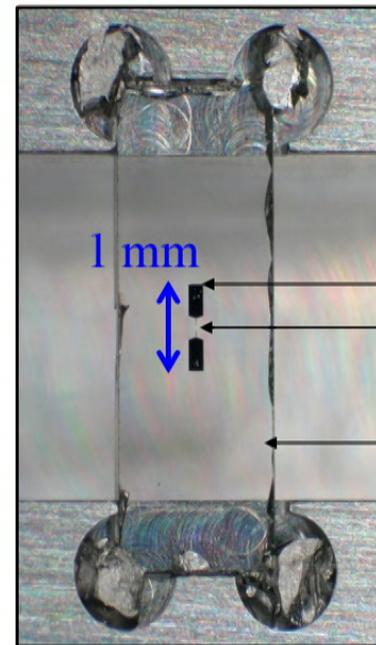
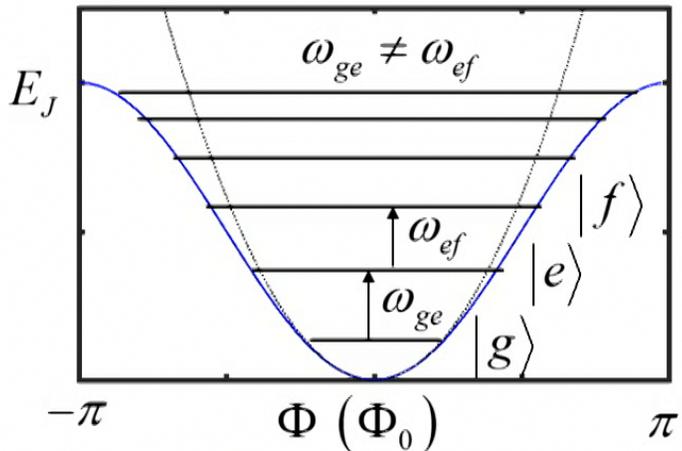


$$\hat{H} = \frac{E_J}{2} \left( 1 - \cos \left( 2\pi \frac{\hat{\Phi}}{\Phi_0} \right) \right) + \frac{\hat{Q}^2}{2C}$$

$$\hat{H} = \frac{\hat{\Phi}^2}{2L} + \frac{\hat{Q}^2}{2C}$$



$$\omega_{ge} \sim 5 - 10 \text{ GHz}$$



aluminum paddle  
Josephson junction  
sapphire chip

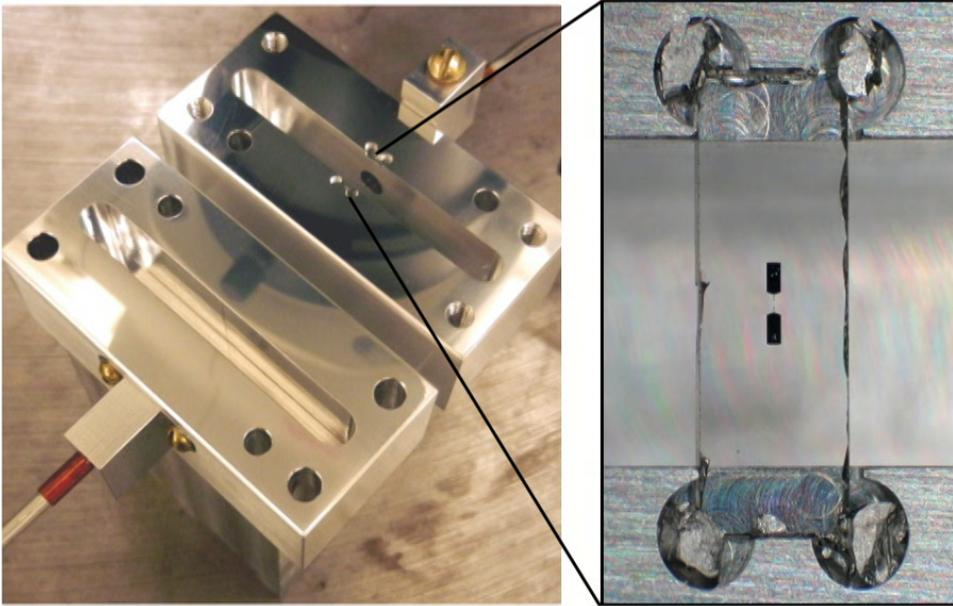
pseudo-spin-1/2

$$|g\rangle = |\downarrow\rangle$$

$$\hat{H} = \frac{\omega_{ge}}{2} \hat{\sigma}^z$$

$$|e\rangle = |\uparrow\rangle$$

# CQED: transmon qubit in a microwave cavity



$$g = \frac{\vec{d} \cdot \vec{E}_{\text{rms}}}{\hbar}$$

$$|\vec{d}| = 2e \times 1 \text{ nm} \approx 10^7 \text{ Debye!}$$

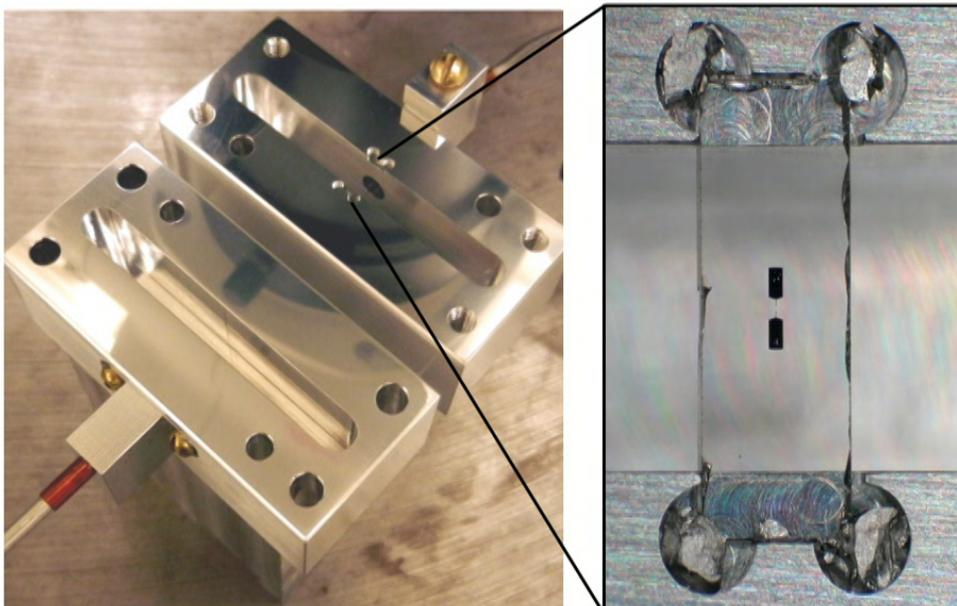
$$g \approx 2\pi \times 100 \text{ MHz}$$

$$\hat{V}_{\text{dipole}} = g \hat{\sigma}_x (\hat{a}^\dagger + \hat{a}) \quad \text{spin flip}$$

huge dipole moment: strong coupling

Hanhee Paik et al., *Phys. Rev. Lett.* **107**, 240501 (2011).

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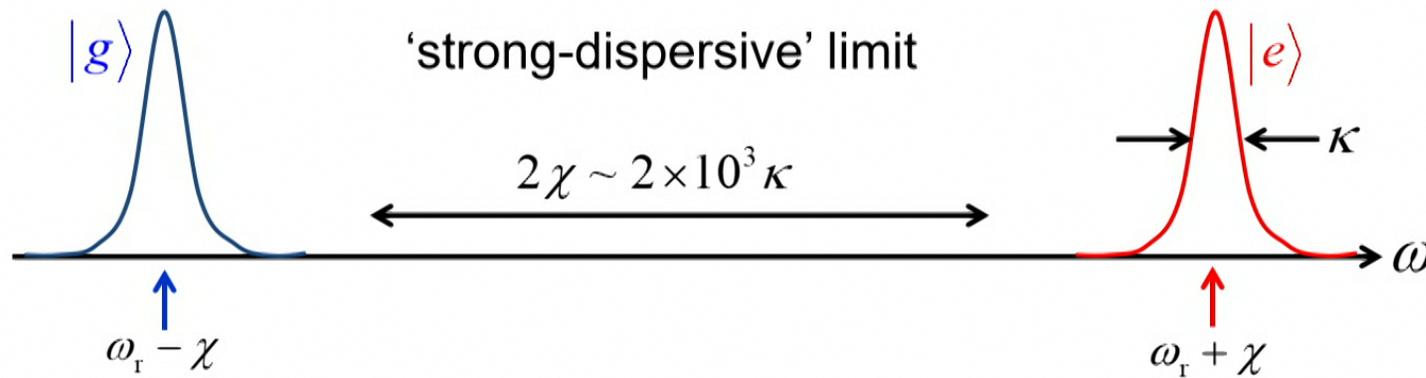
# Strong dispersive regime: cavity measures qubit state

$$|\omega_r - \omega_q| \gg g$$

$$\hat{H} = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q}{2} \hat{\sigma}^z + \chi \hat{\sigma}^z \hat{a}^\dagger \hat{a}$$

cavity      qubit      dispersive coupling

$$\text{cavity frequency} = \omega_r + \chi \hat{\sigma}^z$$



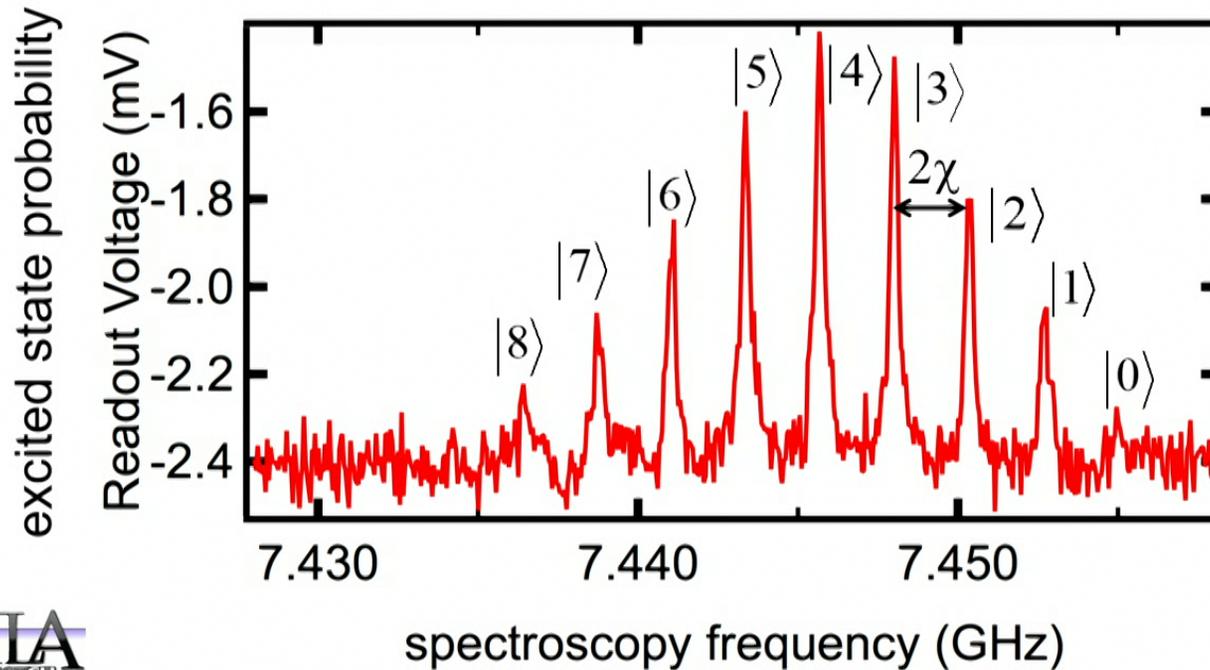
qubit readout: 300 ns, 99% fidelity, QND

R. Vijay et al., *Phys. Rev. Lett.* **106**, 110502 (2011).

# Strong dispersive regime: qubit measures cavity state

$$|\omega_r - \omega_q| \gg g \quad \hat{H} = \omega_r \hat{a}^\dagger \hat{a} + \frac{\omega_q + 2\chi \hat{a}^\dagger \hat{a}}{2} \hat{\sigma}^z$$

qubit frequency depends on cavity photon number



spectrally resolve  
cavity photon number

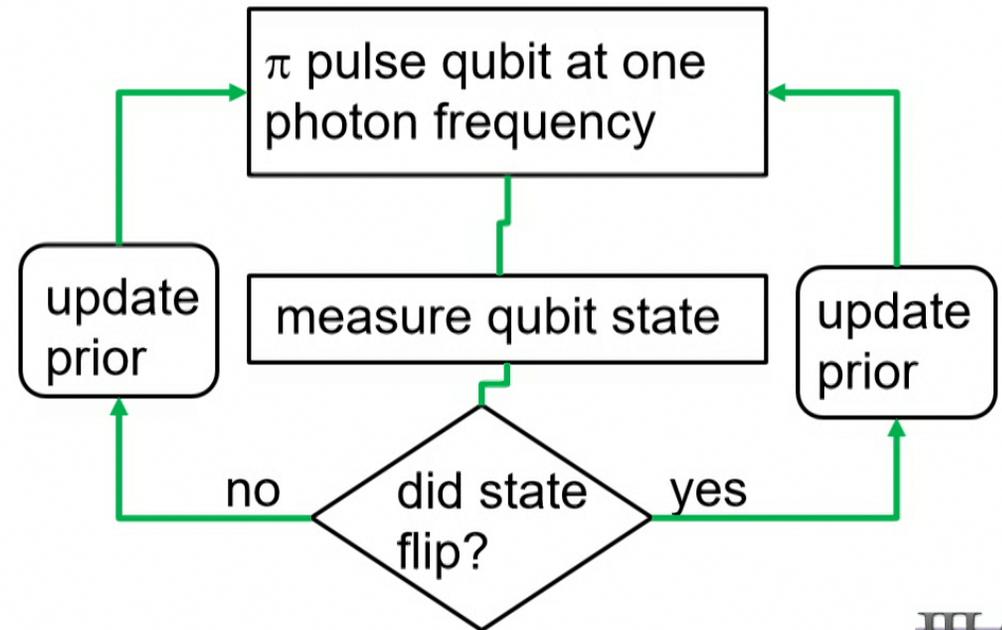
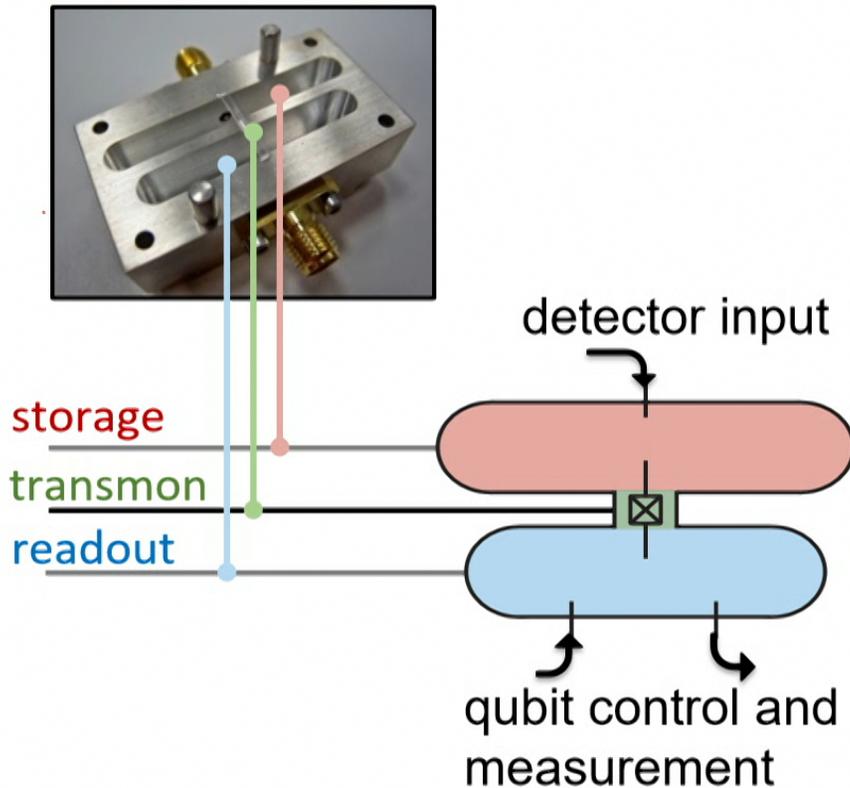
micro-“waves” are particles!

D. I. Schuster *et al.*, *Nature* **445**, 515-518 (2007).

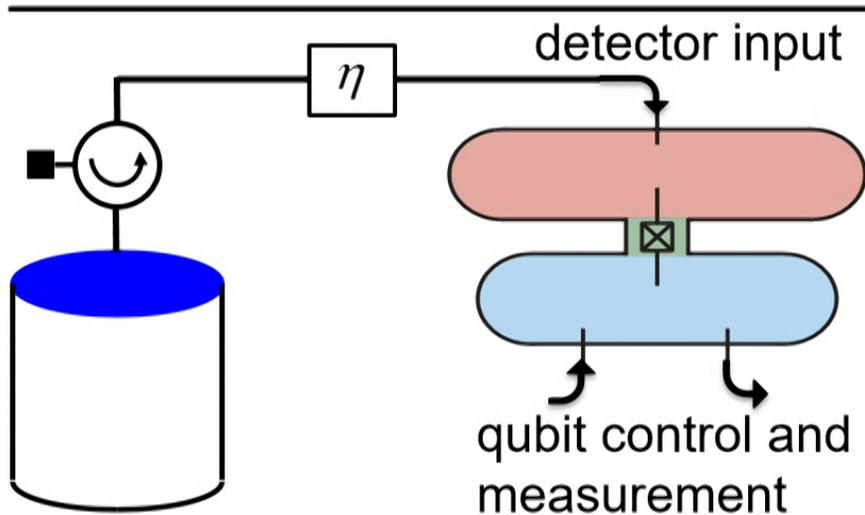
# Two-cavity one-qubit device is a QND photon counter

measurement time  $\ll$  storage cavity lifetime

QND photon counting with Bayesian filter



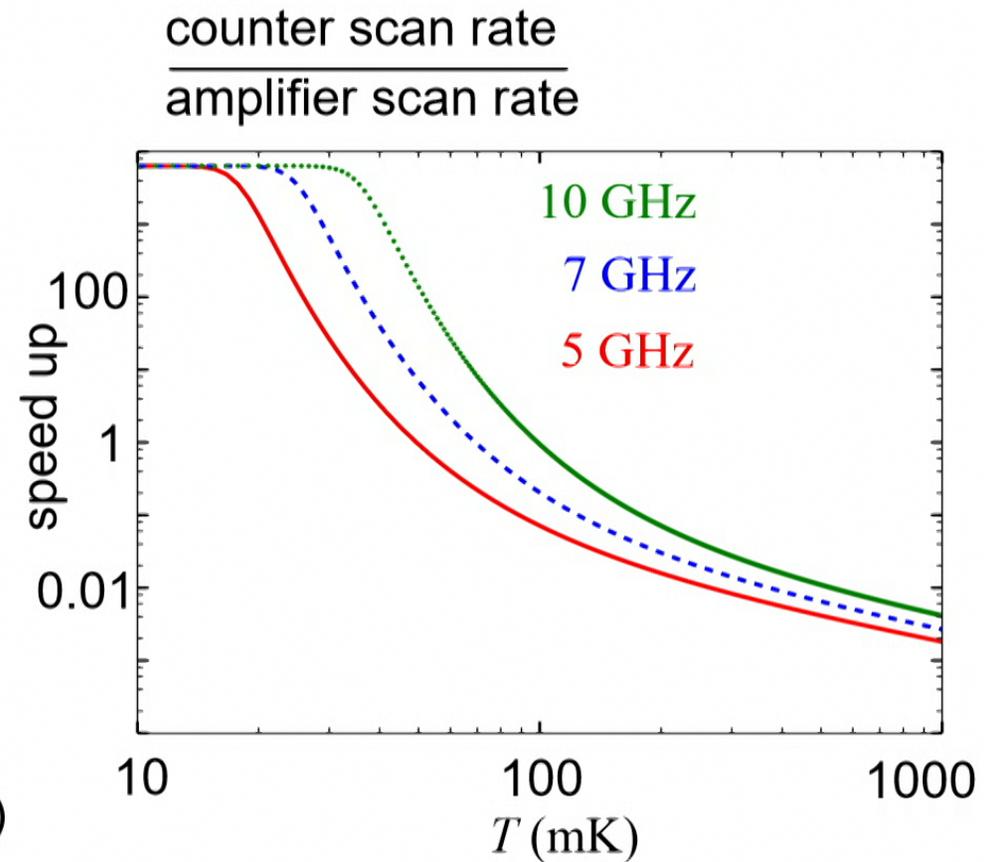
# QND photon measurement suppresses dark counts



intrinsic error “dark counts”  $n_{\text{dark}} = 10^{-2}$

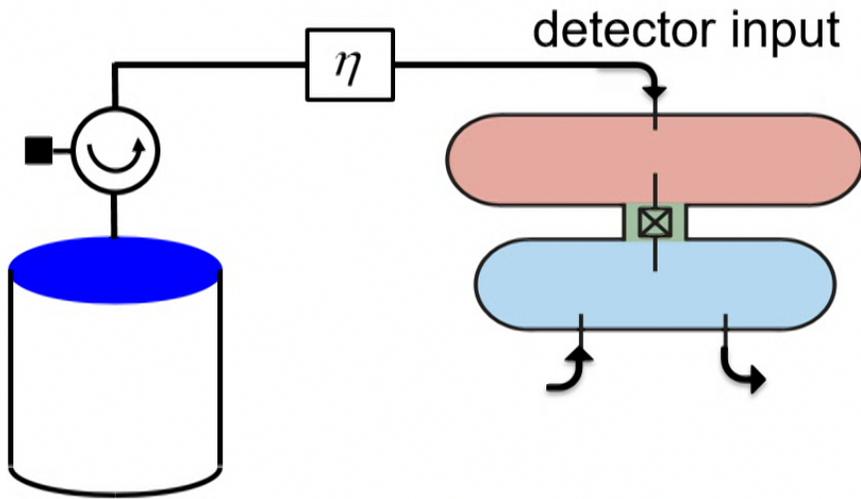
detect same photon 3 times  $n_{\text{dark}}^3 \approx 10^{-6}$

no extra noise from loss (c.f. squeezing)



PERIMETER  INSTITUTE FOR THEORETICAL PHYSICS

# Progress required to implement photon counting receiver in an axion haloscope



tunable CQED photon counter

cooling E+M environment to  $T = 20$  mK

$$N_T = 10^{-6} @ 20 \text{ mK}$$

discriminating background photons from signal

compatibility with large magnet

# Conclusions and acknowledgements

cavity haloscope searches operate at the quantum limit  
 quantum noise in axion search can be overcome  
 possible today: 2.5-fold speed up with squeezing  
 future: potential to speed up 10,000 - fold  
 quantum noise evading concepts already demonstrated



## JILA JPAs and axions

Maxime Malnou

Dan Palken

Manuel Castellanos-Beltran

Francois Mallet

Mehmet Anil

Will Kindel

Hsiang-Shen Ku

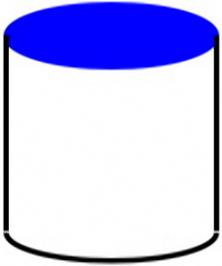


HEISING - SIMONS  
FOUNDATION

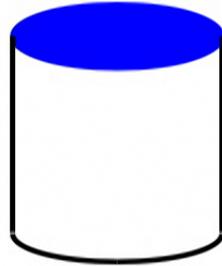


# EPR observables of two cavities commute

---



$$[\hat{X}_1, \hat{X}_2] = i$$



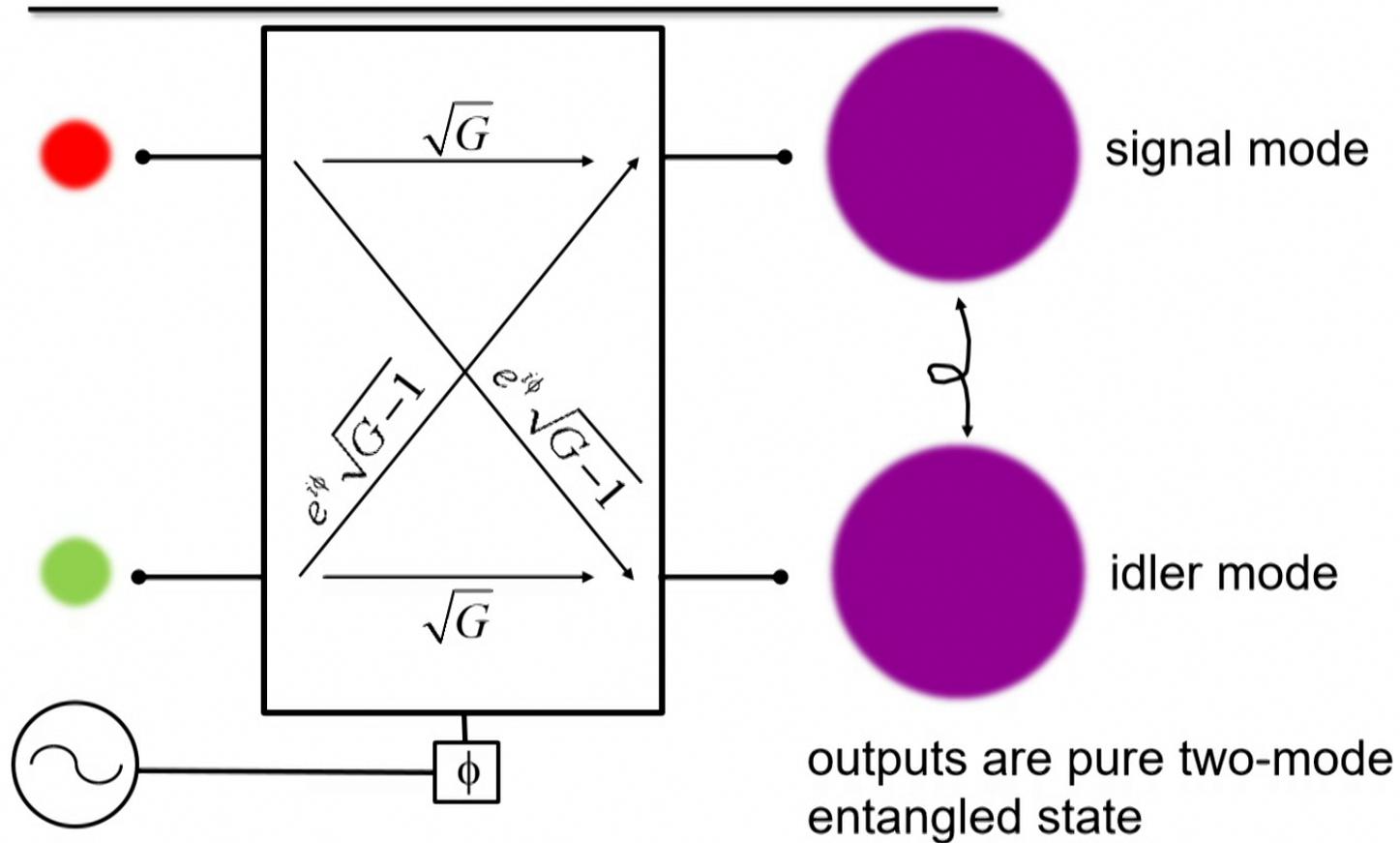
$$[\hat{Y}_1, \hat{Y}_2] = i$$

$$\hat{Q} = \hat{X}_1 + \hat{Y}_1; \hat{P} = \hat{X}_2 - \hat{Y}_2$$

$$[\hat{Q}, \hat{P}] = 0$$

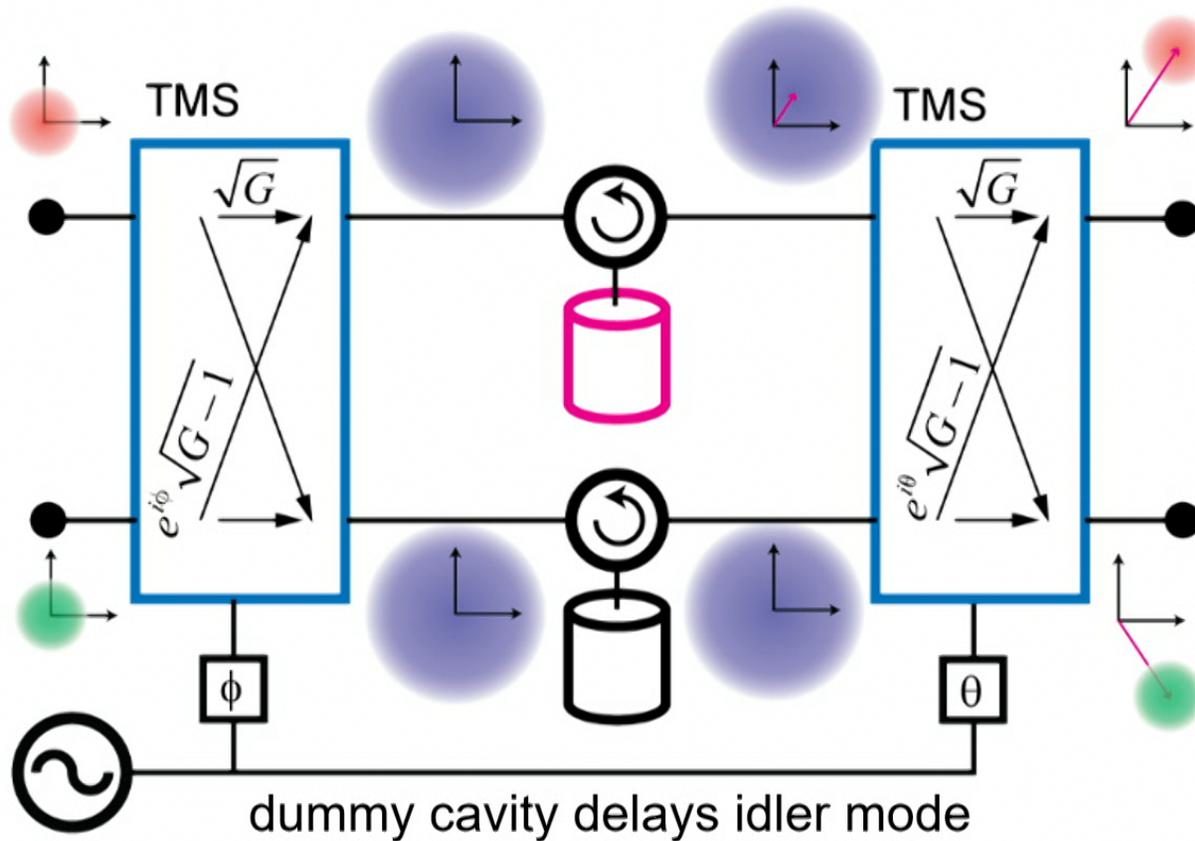
measure both  $Q$  and  $P$   
without added noise

# Two-mode squeezer prepares simultaneous eigenstates of EPR observables



N. Bergeal, M. Devoret *et al.*, Nature **465**,64–68  
 E. Flurin, B. Huard *et al.*, Phys. Rev. Lett. **109**, 183901

# Concept for noiseless measurement of both quadratures



B. Yurke and J. S. Denker, *Phys. Rev. A* **29**, 1419

# Circumventing the quantum limit with CQED photon counting