

Title: Multi-loop calculations in electroweak physics

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Abstract:

# Precision calculations in electroweak physics

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**University of Pittsburgh**

PI Workshop "Radiative Corrections at the Intensity Frontier of Particle Physics"  
12–14 June 2017

- 1.  $Z$  and  $W$  boson physics**
- 2. Future projections**
- 3. Low-energy electroweak observables**
- 4. Muon anomalous magnetic moment**

You can shoot a goal from behind with enough precision



### W mass

$\mu$  decay in Fermi Model

$\mu^- \rightarrow v_\mu + v_e$

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QED corr.  
(2-loop)

$$\Gamma_\mu = \frac{G_F^2 m_\mu^5}{192\pi^3} F\left(\frac{m_e^2}{m_\mu^2}\right) (1 + \Delta q)$$

Ritbergen, Stuart '98  
Pak, Czarnecki '08

$\mu$  decay in Standard Model

$\mu^- \rightarrow v_\mu + v_e$

$\mu^- \rightarrow v_\mu + v_e$

$\frac{G_F^2}{\sqrt{2}} = \frac{e^2}{8s_W^2 M_W^2} (1 + \Delta r)$

electroweak corrections

### ■ Deconvolution of initial-state QED radiation:

$$\sigma[e^+e^- \rightarrow f\bar{f}] = \mathcal{R}_{\text{ini}}(s, s') \otimes \sigma_{\text{hard}}(s')$$

Kureav, Fadin '85

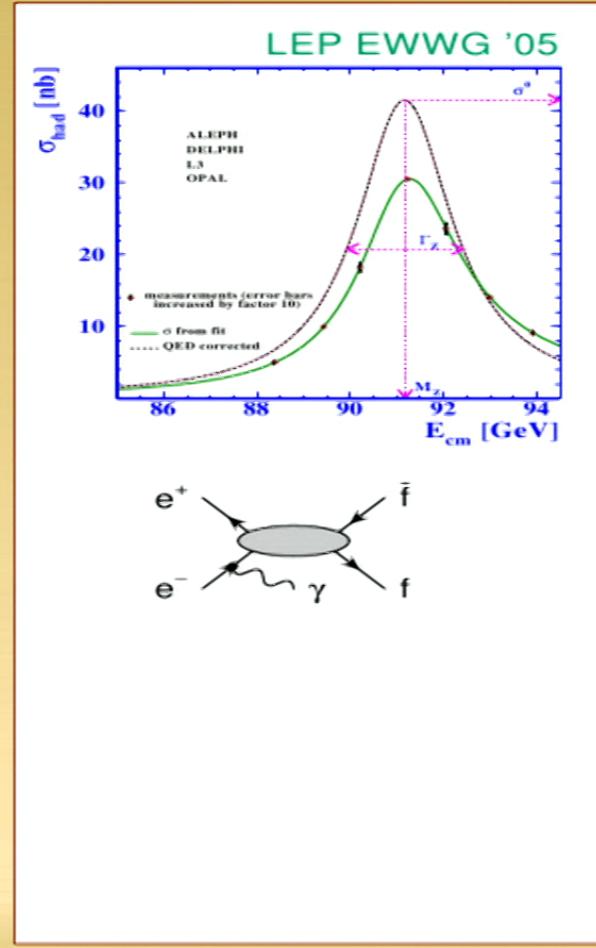
Berends, Burgers, v. Neerven '88

Kniehl, Krawczyk, Kühn, Stuart '88

Beenakker, Berends, v. Neerven '89

Skrzypek '92

Montagna, Nicrosini, Piccinini '97



## Z-pole observables

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- Deconvolution of initial-state QED radiation:

$$\sigma[e^+e^- \rightarrow f\bar{f}] = \mathcal{R}_{\text{ini}}(s, s') \otimes \sigma_{\text{hard}}(s')$$

- Subtraction of  $\gamma$ -exchange,  $\gamma-Z$  interference, box contributions:

$$\sigma_{\text{hard}} = \sigma_Z + \sigma_\gamma + \sigma_{\gamma Z} + \sigma_{\text{box}}$$

- $Z$ -pole contribution:

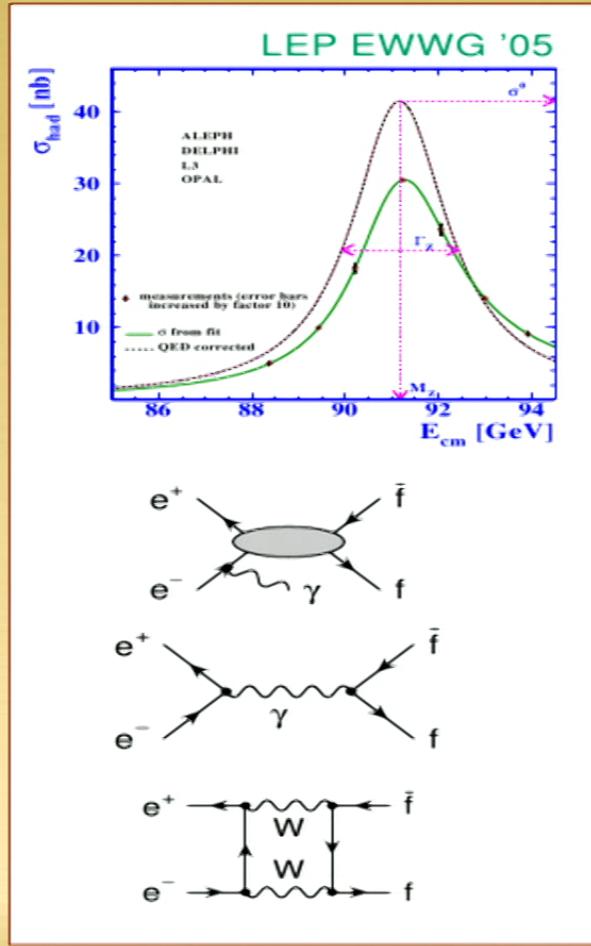
$$\sigma_Z = \frac{R}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} + \sigma_{\text{non-res}}$$

- In experimental analyses:

$$\sigma \sim \frac{1}{(s - M_Z^2)^2 + s^2 \Gamma_Z^2 / M_Z^2}$$

$$\overline{M}_Z = M_Z / \sqrt{1 + \Gamma_Z^2 / M_Z^2} \approx M_Z - 34 \text{ MeV}$$

$$\overline{\Gamma}_Z = \Gamma_Z / \sqrt{1 + \Gamma_Z^2 / M_Z^2} \approx \Gamma_Z - 0.9 \text{ MeV}$$



Effective weak mixing angle:

Z-pole asymmetries:

$$A_{\text{FB}}^f \equiv \frac{\sigma(\theta < \frac{\pi}{2}) - \sigma(\theta > \frac{\pi}{2})}{\sigma(\theta < \frac{\pi}{2}) + \sigma(\theta > \frac{\pi}{2})} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f$$

$$A_{\text{LR}} \equiv \frac{\sigma(\mathcal{P}_e > 0) - \sigma(\mathcal{P}_e < 0)}{\sigma(\mathcal{P}_e > 0) + \sigma(\mathcal{P}_e < 0)} = \mathcal{A}_e$$

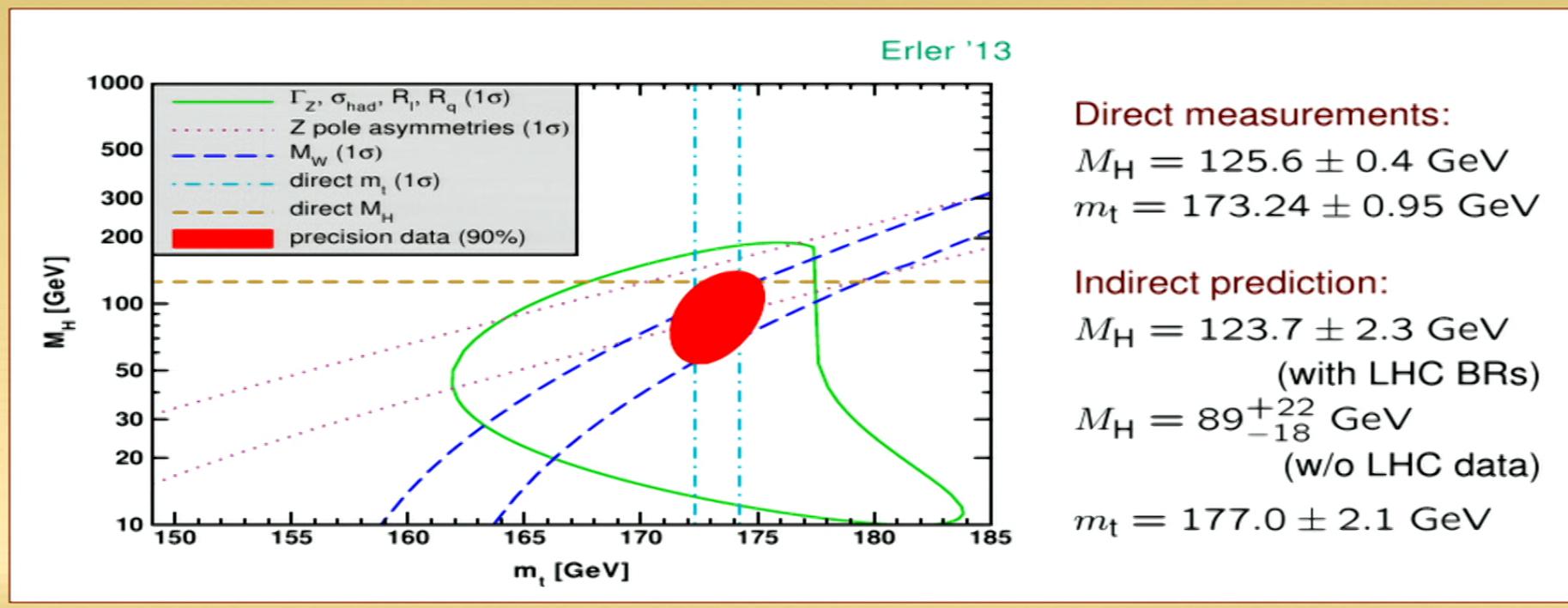
$$\mathcal{A}_f = 2 \frac{g_{Vf}/g_{Af}}{1 + (g_{Vf}/g_{Af})^2} = \frac{1 - 4|Q_f| \sin^2 \theta_{\text{eff}}^f}{1 - 4|Q_f| \sin^2 \theta_{\text{eff}}^f + 8(|Q_f| \sin^2 \theta_{\text{eff}}^f)^2}$$

Most precisely measured for  $f = \ell$  (also  $f = b, c$ )

## Current status of electroweak precision tests

### Standard Model after Higgs discovery:

- Good agreement between measured mass and indirect prediction
- Very good agreement over large number of observables



Effective field theory:  $\mathcal{L} = \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i + \mathcal{O}(\Lambda^{-3}) \quad (\Lambda \gg M_Z)$

$$\mathcal{O}_{\phi 1} = (D_\mu \Phi)^\dagger \Phi \Phi^\dagger (D^\mu \Phi) \quad \alpha \Delta \textcolor{blue}{T} = -\frac{v^2}{2} \frac{c_{\phi 1}}{\Lambda^2}$$

$$\mathcal{O}_{BW} = \Phi^\dagger B_{\mu\nu} W^{\mu\nu} \Phi \quad \alpha \Delta \textcolor{blue}{S} = -e^2 v^2 \frac{c_{BW}}{\Lambda^2}$$

$$\mathcal{O}_{LL}^{(3)e} = (\bar{L}_L^e \sigma^a \gamma_\mu L_L^e)(\bar{L}_L^e \sigma^a \gamma^\mu L_L^e) \quad \Delta G_F = -\sqrt{2} \frac{c_{LL}^{(3)e}}{\Lambda^2}$$

$$\mathcal{O}_R^f = i(\Phi^\dagger \overset{\leftrightarrow}{D}_\mu \Phi)(\bar{f}_R \gamma^\mu f_R) \quad f = e, \mu, \tau, b, lq$$

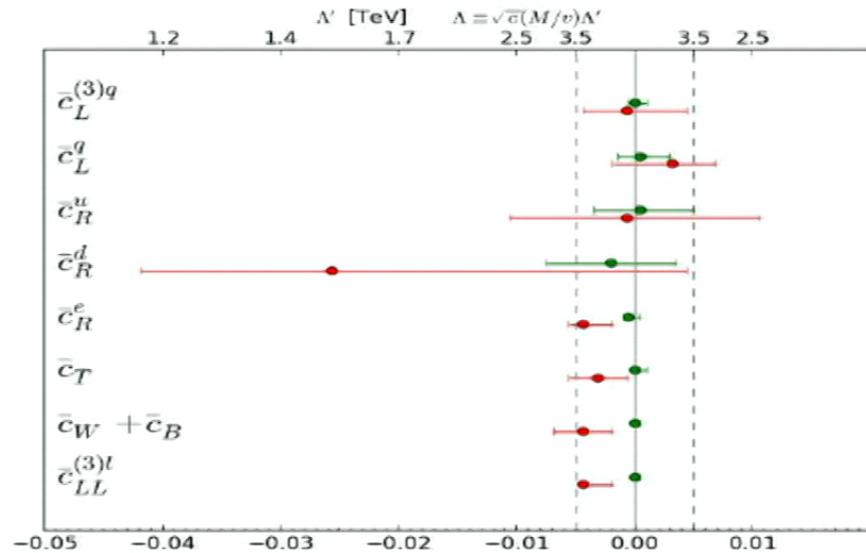
$$\mathcal{O}_L^F = i(\Phi^\dagger \overset{\leftrightarrow}{D}_\mu \Phi)(\bar{F}_L \gamma^\mu F_L) \quad F = \binom{\nu_e}{e}, \binom{\nu_\mu}{\mu}, \binom{\nu_\tau}{\tau}, \binom{u, c}{d, s}, \binom{t}{b}$$

$$\mathcal{O}_L^{(3)F} = i(\Phi^\dagger \overset{\leftrightarrow}{D}_\mu^a \Phi)(\bar{F}_L \sigma_a \gamma^\mu F_L)$$

More operators than EWPOs

→ Some can be constrained by  $W \rightarrow \ell\nu$ , had.,  $e^+ e^- \rightarrow W^+ W^-$

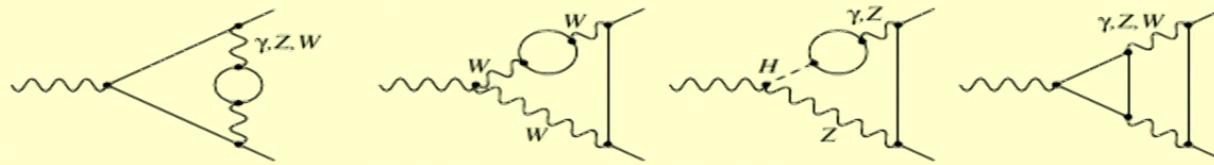
Assuming flavor universality:



Significant correlation/  
degeneracy between  
different operators

Pomaral, Riva '13  
Ellis, Sanz, You '14

Known corrections to  $\Delta r$ ,  $\sin^2 \theta_{\text{eff}}^f$ ,  $g_{Vf}$ ,  $g_{Af}$ :



- Complete NNLO corrections ( $\Delta r$ ,  $\sin^2 \theta_{\text{eff}}^\ell$ ) Freitas, Hollik, Walter, Weiglein '00  
Awramik, Czakon '02; Onishchenko, Veretin '02  
Awramik, Czakon, Freitas, Weiglein '04; Awramik, Czakon, Freitas '06  
Hollik, Meier, Uccirati '05,07; Degrassi, Gambino, Giardino '14
  - “Fermionic” NNLO corrections ( $g_{Vf}$ ,  $g_{Af}$ ) Czarnecki, Kühn '96  
Harlander, Seidensticker, Steinhauser '98  
Freitas '13,14
  - Partial 3/4-loop corrections to  $\rho/T$ -parameter  
 $\mathcal{O}(\alpha_t \alpha_s^2)$ ,  $\mathcal{O}(\alpha_t^2 \alpha_s)$ ,  $\mathcal{O}(\alpha_t \alpha_s^3)$   
Chetyrkin, Kühn, Steinhauser '95  
Faisst, Kühn, Seidensticker, Veretin '03  
Boughezal, Tausk, v. d. Bij '05  
Schröder, Steinhauser '05; Chetyrkin et al. '06  
Boughezal, Czakon '06
- $(\alpha_t \equiv \frac{y_t^2}{4\pi})$

	Experiment	Theory error	Main source
$M_W$	$80.385 \pm 0.015$ MeV	4 MeV	$\alpha^3, \alpha^2\alpha_s$
$\Gamma_Z$	$2495.2 \pm 2.3$ MeV	0.5 MeV	$\alpha_{bos}^2, \alpha^3, \alpha^2\alpha_s, \alpha\alpha_s^2$
$\sigma_{had}^0$	$41540 \pm 37$ pb	6 pb	$\alpha_{bos}^2, \alpha^3, \alpha^2\alpha_s$
$R_b \equiv \Gamma_Z^b/\Gamma_Z^{had}$	$0.21629 \pm 0.00066$	0.00015	$\alpha_{bos}^2, \alpha^3, \alpha^2\alpha_s$
$\sin^2 \theta_{eff}^\ell$	$0.23153 \pm 0.00016$	$4.5 \times 10^{-5}$	$\alpha^3, \alpha^2\alpha_s$

- Theory error estimate is not well defined, ideally  $\Delta_{th} \ll \Delta_{exp}$
- Common methods:
  - Count prefactors ( $\alpha, N_c, N_f, \dots$ )
  - Extrapolation of perturbative series
  - Renormalization scale dependence
  - Renormalization scheme dependence
- Also parametric error from external inputs ( $m_t, m_b, \alpha_s, \Delta\alpha_{had}, \dots$ )

Use of  $\overline{\text{MS}}$  renormalization for  $m_t$  reduces h.o. QCD corrections of  $\mathcal{O}(\alpha_t \alpha_s^n)$ :

loops $(n+1)$	$\Delta\rho_{(n)}^{\overline{\text{MS}}} / \left( \frac{3G_F \overline{m}_t^2}{8\sqrt{2}\pi^2} \right)$	$\Delta\rho_{(n)}^{\text{OS}} / \left( \frac{3G_F m_t^2}{8\sqrt{2}\pi^2} \right)$	
2	$-0.193 \left( \frac{\alpha_s}{\pi} \right)$	$-3.970 \left( \frac{\alpha_s}{\pi} \right)$	Djouadi, Verzegnassi '87 Kniehl '90
3	$-2.860 \left( \frac{\alpha_s}{\pi} \right)^2$	$-14.59 \left( \frac{\alpha_s}{\pi} \right)^2$	Avdeev, Fleischer, et al. '94 Chetyrkin, Kühn, Steinhauser '95
4	$-1.680 \left( \frac{\alpha_s}{\pi} \right)^3$	$-93.15 \left( \frac{\alpha_s}{\pi} \right)^3$	Schröder, Steinhauser '05 Chetyrkin, Faisst, Kühn, et al. '06 Boughezal, Czakon '06

No clear pattern of this kind known for  $\mathcal{O}(\alpha^n)$

→ Only few results available that allow direct comparison  
e.g. Faisst, Kühn, Seidensticker, Veretin '03

- $m_t$ : < 1 GeV precision challenging at hadron colliders (b-jet energy scale, hadronization, color reconnection, MC generator, ...) Erler '14
- $M_W$ : Currently  $\delta M_W = 15$  MeV  
Ultimate LHC goal  $\delta M_W \sim 5 \dots 8$  MeV ?
- $\alpha_s$ :  
Most precise determination using Lattice QCD from  $v$  spectroscopy:  
 $\alpha_s = 0.1184 \pm 0.0006$  HPQCD '10  
But  $e^+e^-$  event shapes and DIS prefer  $\alpha_s \sim 0.114$   
Alekhin, Blümlein, Moch '12; Abbate et al. '11; Gehrmann et al. '13
- $\Delta\alpha_{\text{had}}$ : Current:  $\delta(\Delta\alpha_{\text{had}}) \sim 10^{-4}$   
Improvement to  $\delta(\Delta\alpha_{\text{had}}) \sim 5 \times 10^{-5}$  likely (BES III, Belle II)

## Future projections

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**ILC:** High-energy  $e^+e^-$  linear collider, running at  $\sqrt{s} \approx M_Z$  with  $30 \text{ fb}^{-1}$

**CEPC:** Circular  $e^+e^-$  collider, running at  $\sqrt{s} \approx M_Z$  with  $2 \times 150 \text{ fb}^{-1}$

**FCC-ee:** Circular  $e^+e^-$  collider, running at  $\sqrt{s} \approx M_Z$  with  $2 \times (> 10) \text{ ab}^{-1}$

	Current exp.	ILC	CEPC	FCC-ee	Current perturb.
$M_W [\text{MeV}]$	15	3–4	3	1	4
$\Gamma_Z [\text{MeV}]$	2.3	0.8	0.5	0.1	0.5
$R_b [10^{-5}]$	66	14	17	6	15
$\sin^2 \theta_{\text{eff}}^\ell [10^{-5}]$	16	1	2.3	0.6	4.5

→ Existing theoretical calculations adequate for LEP/SLC/LHC,  
but not ILC/CEPC/FCC-ee!

	ILC	FCC-ee	perturb. error with 3-loop <sup>†</sup>	Param. error ILC*	Param. error FCC-ee**
$M_W$ [MeV]	3–5	$\sim 1$	1	2.6	1
$\Gamma_Z$ [MeV]	$\sim 1$	$\sim 0.1$	$\lesssim 0.2$	0.5	0.06
$R_b$ [ $10^{-5}$ ]	15	$\lesssim 5$	5–10	$< 1$	$< 1$
$\sin^2 \theta_{\text{eff}}^\ell$ [ $10^{-5}$ ]	1.3	0.6	1.5	2	2

<sup>†</sup> **Theory scenario:**  $\mathcal{O}(\alpha\alpha_s^2)$ ,  $\mathcal{O}(N_f\alpha^2\alpha_s)$ ,  $\mathcal{O}(N_f^2\alpha^2\alpha_s)$

( $N_f^n$  = at least  $n$  closed fermion loops)

Parametric inputs:

\* **ILC:**  $\delta m_t = 50$  MeV,  $\delta \alpha_s = 0.001$ ,  $\delta M_Z = 2.1$  MeV

\*\* **FCC-ee:**  $\delta m_t = 50$  MeV,  $\delta \alpha_s = 0.0001$ ,  $\delta M_Z = 0.1$  MeV

also:  $\delta(\Delta\alpha) \sim 5 \times 10^{-5}$

## ■ Subtraction of QED radiation contributions

- Known to  $\mathcal{O}(\alpha^2)$ ,  $\mathcal{O}(\alpha^3 L^3)$  for **ISR**,  
 $\mathcal{O}(\alpha^2)$  for **FSR** and  $\mathcal{O}(\alpha^2 L^2)$  for **A<sub>FB</sub>**

$$(L = \log \frac{s}{m_e^2})$$

Berends, Burgers, v.Neerven '88

Kniehl, Krawczyk, Kühn, Stuart '88

Beenakker, Berends, v.Neerven '89

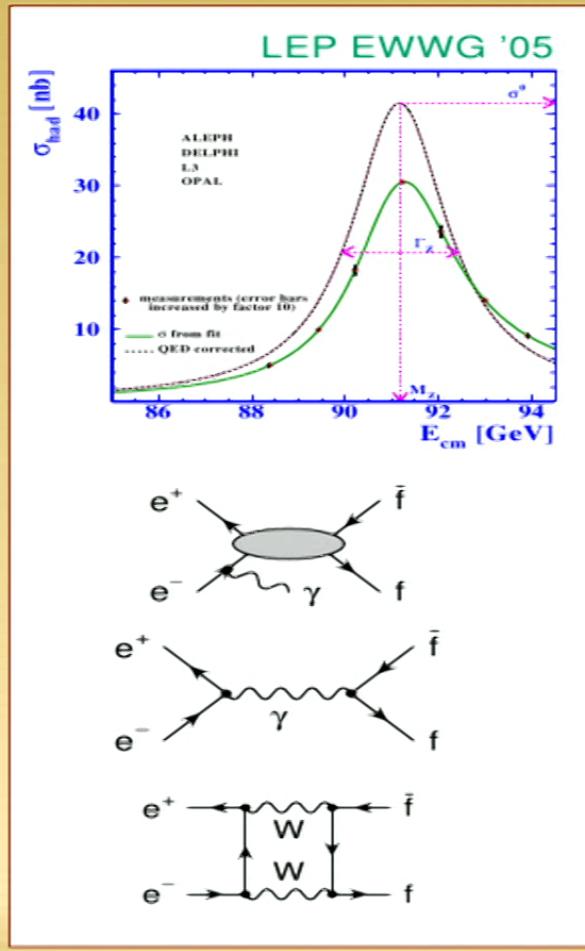
Skrzypek '92; Montagna, Nicrosini, Piccinini '97

- $\mathcal{O}(0.1\%)$  uncertainty on  $\sigma_Z$ ,  $A_{FB}$
- Improvement needed for ILC/CEPC/FCC-ee

## ■ Subtraction of non-resonant $\gamma$ -exchange, $\gamma$ -Z interf., box contributions, Bhabha scattering

see, e.g., Bardin, Grünewald, Passarino '99

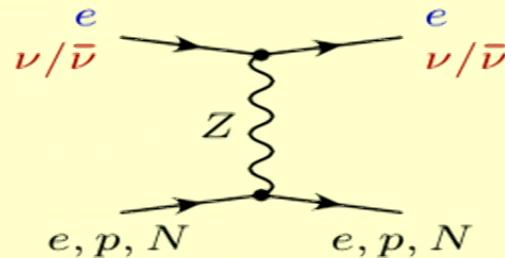
- $\mathcal{O}(0.01\%)$  uncertainty within SM  
(improvements may be needed)
- Sensitivity to some NP beyond EWPO



## Low-energy electroweak observables

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- Polarized  $ee$ ,  $ep$ ,  $ed$  scattering  
( $Q_W(e)$ ,  $Q_W(p)$ , eDIS)  
E158 '05; Qweak '13; JLab Hall A '13
  - $\nu N/\bar{\nu} N$  scattering NuTeV '02
  - Atomic parity violation  
( $Q_W(^{133}\text{Cs})$ ) Wood et al. '97  
Guéna, Lintz, Bouchiat '05
- Test of running  $\overline{\text{MS}}$  weak mixing angle  $\sin^2 \bar{\theta}(\mu)$



$$g_{AV}^{ef} [\bar{e}\gamma^\mu\gamma_5 e] [\bar{f}\gamma_\mu f]$$

$$g_{VA}^{ef} [\bar{e}\gamma^\mu e] [\bar{f}\gamma_\mu\gamma_5 f]$$

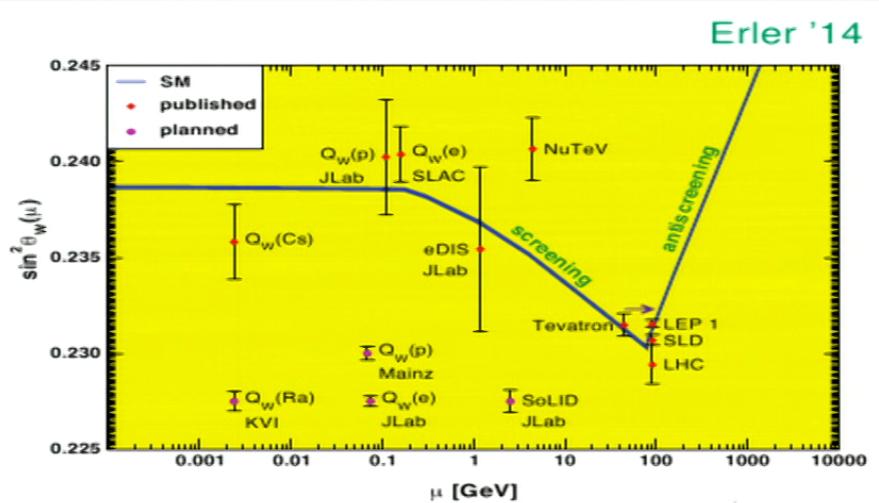
$$g_{AV}^{ef} = \frac{1}{2} - 2|Q_f|\sin^2 \bar{\theta}(\mu)$$

$$g_{VA}^{ef} = \frac{1}{2} - 2\sin^2 \bar{\theta}(\mu)$$

## Low-energy electroweak observables

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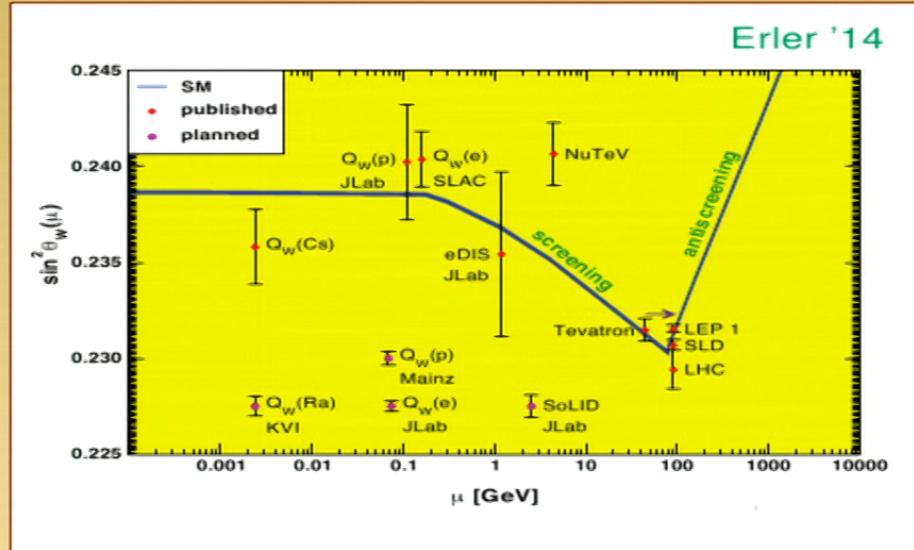
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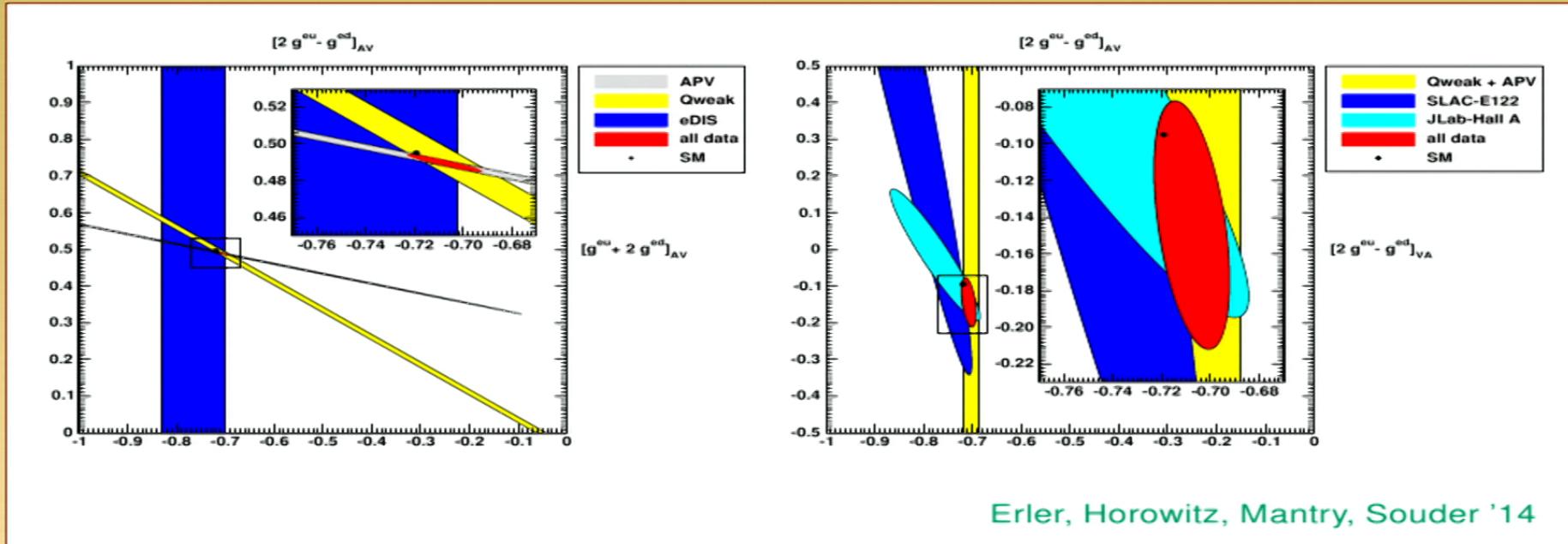
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- Atomic parity violation  
( $Q_W(^{133}\text{Cs})$ ) Wood et al. '97  
Guéna, Lintz, Bouchiat '05
- Future experiments:  
MOLLER ( $ee$ ), P2, SoLID ( $ep$ ),  
Atomic PV in radium



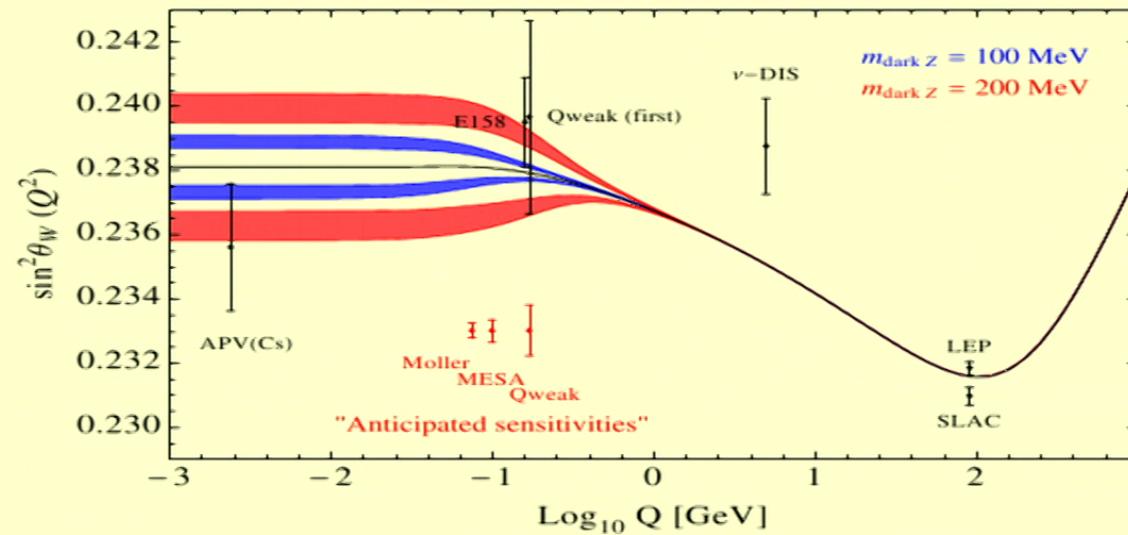
## Independent contact interactions

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New neutral gauge boson with mass  $\mathcal{O}(100 \text{ MeV})$ , which mixes with photon

- Can explain  $g_\mu - 2$  discrepancy
- Low-energy precision experiments have highest sensitivity



Davoudiasl, Lee, Marciano '14

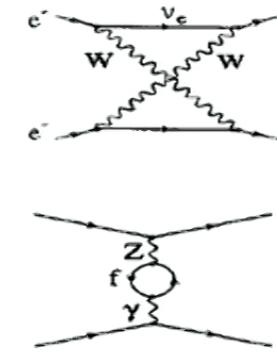
### ■ Other physics cases?

## Electroweak one-loop corrections:

Czarnecki, Marciano '96

Large correction to  $A_{PV} = \frac{d\sigma_L - d\sigma_R}{d\sigma_L + d\sigma_R}$ :

$$\begin{aligned} &\sim 40\% \text{ for } \sin^2 \bar{\theta}(M_Z), \\ &\sim 10\% \text{ for } \sin^2 \bar{\theta}(0) \end{aligned}$$



- Tree-level contribution suppressed by  $1 - 4 \sin^2 \bar{\theta}(0) \sim 0.045$
- Running  $\sin^2 \bar{\theta}(M_Z) \rightarrow \sin^2 \bar{\theta}(0)$ :  
Corrections  $\sim \ln m_f^2/M_Z^2$   
 $\rightarrow \sin^2 \bar{\theta}(\mu)$  shifted by  $\sim 3\%$
- Quark contribution determined by fitting  $m_q$  to  $\alpha(\mu)$

Erler, Ramsey-Musolf '04

## Higher order corrections:

- $\mathcal{O}(\alpha_{QED}^2)$ ,  $\mathcal{O}(\alpha \alpha_S)$  (NLL) and  $\mathcal{O}(\alpha \alpha_S^2)$  (NNLL) effects in running of  $\sin^2 \bar{\theta}(\mu)$

Erler, Ramsey-Musolf '04

Higher order corrections:

- **Genuine weak  $\mathcal{O}(\alpha^2)$  currently unknown**
  - Leading contributions could be not much smaller than target MOLLER exp. uncertainty (2.4% relative)
- Additional QCD corrections of  $\mathcal{O}(\alpha\alpha_s)$  (and NP uncertainties) for  $ep$  scattering  
**Erler, Kurylov, Ramsey-Musolf '03**

Definition of  $\sin^2 \bar{\theta}(\mu)$ :

- $\overline{\text{MS}}$   $\sin^2 \bar{\theta}(\mu)$  is gauge dependent  
(e.g. due to integrating out  $b/t, c/s$  at different thresholds)
- Gauge violation may be restored with pinch technique,  
but cumbersome beyond 1-loop
- More practical: Define  $\sin^2 \bar{\theta}(\mu)$  in Feynman gauge

## Muon anomalous magnetic moment

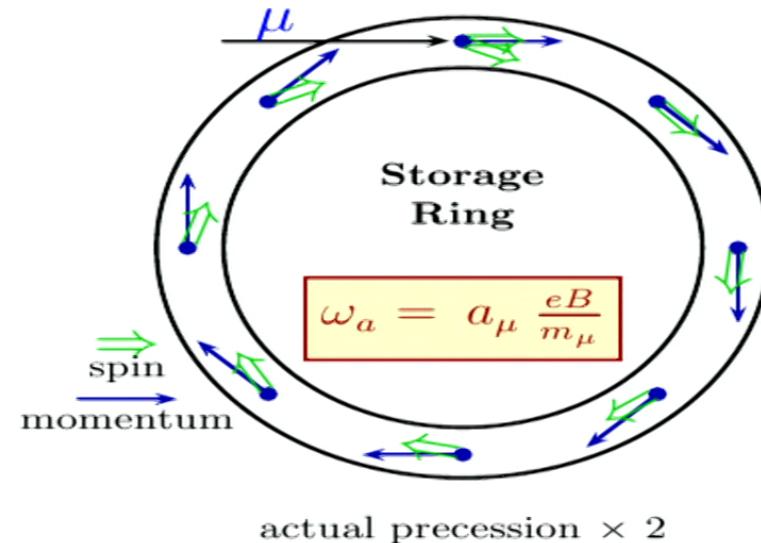
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$$\gamma(q) \quad \mu(p_2)$$
$$\mu(p_1)$$
$$= (-ie) \bar{u}(p_2) \left[ \gamma^\mu F_E(q^2) + i \frac{\sigma^{\mu\nu} q_\nu}{2m_\mu} F_M(q^2) \right] u(p_1)$$

$$a_\mu \equiv \frac{g_\mu - 2}{2} = F_M(0)$$

Measured at NBL g-2 experiment:

$$a_\mu = (11\,659\,208.0 \pm 6.3) \times 10^{-10}$$

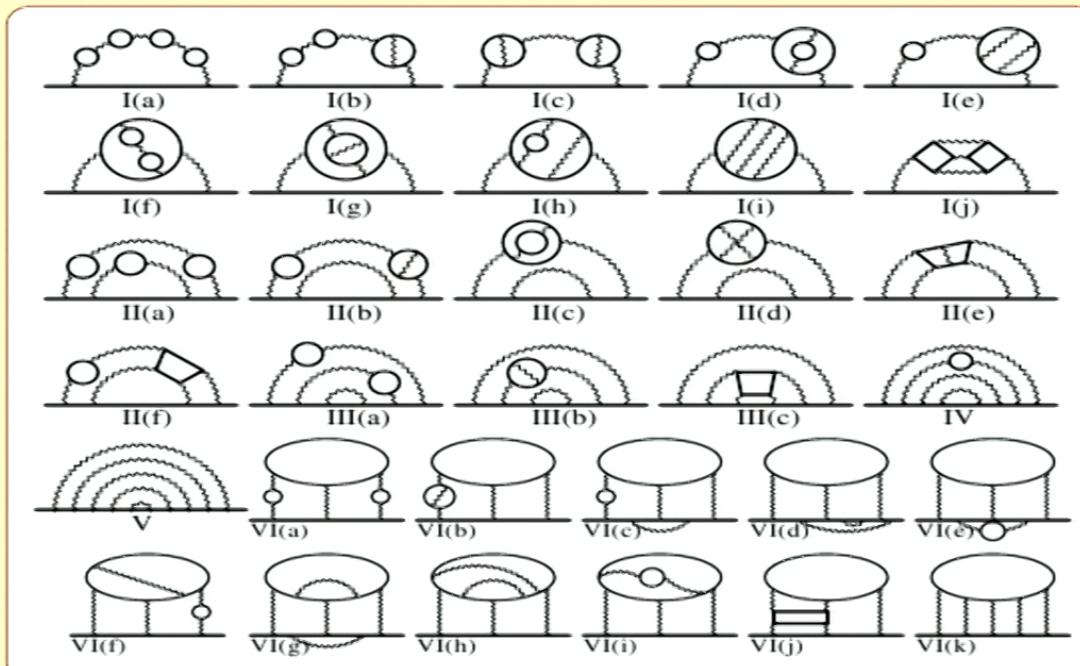


Jegerlehner, Nyfeller '09

## Muon $g-2$ : SM theory prediction

	$a_\mu [10^{-10}]$
QED $\mathcal{O}(\alpha^5)$	$11\ 658\ 471.88 \pm 0.01$

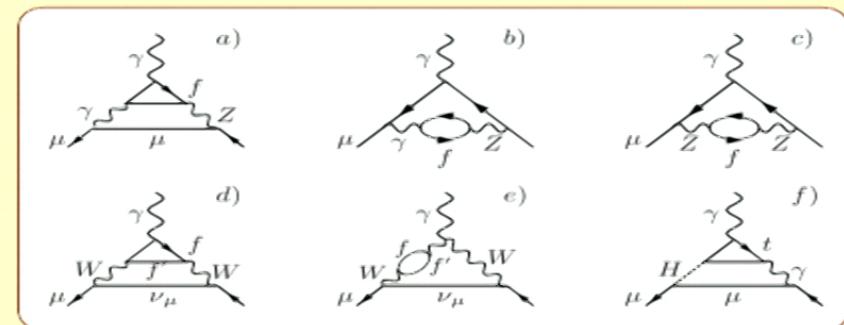
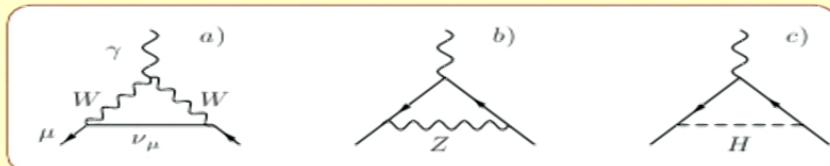
Aoyama, Hayakawa, Kinoshita, Nio '12



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Aoyama, Hayakawa, Kinoshita, Nio '12  
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## Muon $g-2$ : SM theory prediction

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QED $\mathcal{O}(\alpha^5)$	$11\ 658\ 471.88 \pm 0.01$
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LO had. vac. pol.	$687.2 \pm 3.5$
NLO	$-9.93 \pm 0.09$
NNLO	$1.23 \pm 0.01$

Aoyama, Hayakawa, Kinoshita, Nio '12

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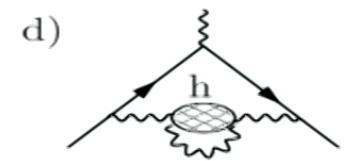
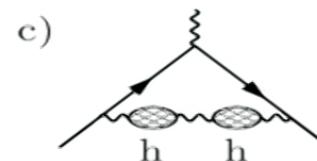
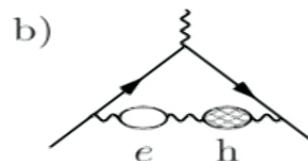
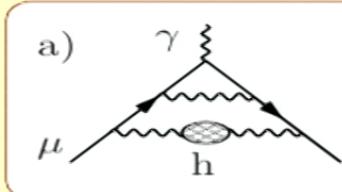
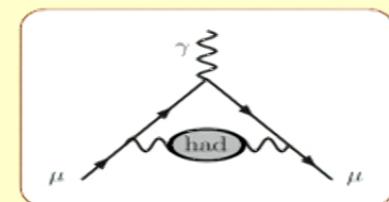
Knecht et al. '02

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Hagiwara et al. '11

Davier, Hoecker, Malaescu, Zhang '11

Jegerlehner '15



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Aoyama, Hayakawa, Kinoshita, Nio '12

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Czarnecki, Marciano, Vainshtain '03

Hagiwara et al. '11

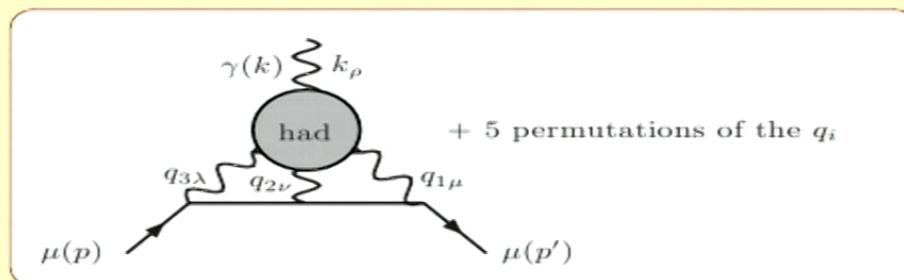
Davier, Hoecker, Malaescu, Zhang '11

Jegerlehner '15

Prades, de Rafael, Vainshtein '09

Nyffeler '09

Erler, Toledo Sanchez '06



## Muon $g-2$ : SM theory prediction

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	$a_\mu [10^{-10}]$
QED $\mathcal{O}(\alpha^5)$	11 658 471.88 $\pm$ 0.01
EW $\mathcal{O}(\alpha^2)$	15.3 $\pm$ 0.2
LO had. vac. pol.	687.2 $\pm$ 3.5
NLO	-9.93 $\pm$ 0.09
NNLO	1.23 $\pm$ 0.01
light-by-light	10.7 $\pm$ 3.2
Total	11 659 176.4 $\pm$ 4.8
Exp	11 659 208.0 $\pm$ 6.3

Aoyama, Hayakawa, Kinoshita, Nio '12

Czarnecki, Krause, Marciano '96

Knecht et al. '02

Czarnecki, Marciano, Vainshtain '03

Hagiwara et al. '11

Davier, Hoecker, Malaescu, Zhang '11

Jegerlehner '15

Prades, de Rafael, Vainshtein '09

Nyffeler '09

Erler, Toledo Sanchez '06

→ > 3 standard deviations!

## Muon $g-2$ : Uncertainties

Difficulties with hadronic contributions:

- Had. vac. pol. from  $e^+e^-$  and  $\tau$  decay data (or lattice<sup>†</sup>)
- Calibration of old  $e^+e^-$  experiments
- $\gamma-\rho$  mixing important for relating  $e^+e^-$  and  $\tau$  data

Jegerlehner, Szafron '11

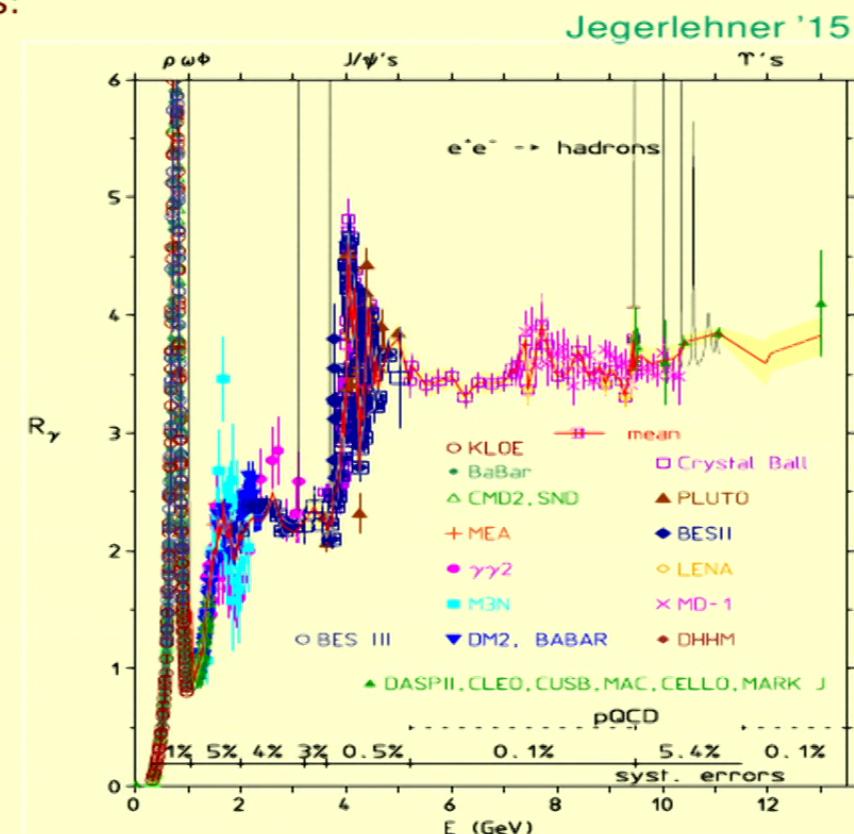
- Light-by-light contribution only from hadron models (or lattice\*)

<sup>†</sup>Blum et al. '15

Chakraborty et al. '16

Della Morte et al. '17

\*Blum et al. '16,17



## Muon $g-2$ : Uncertainties

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Jegerlehner, Szafron '11

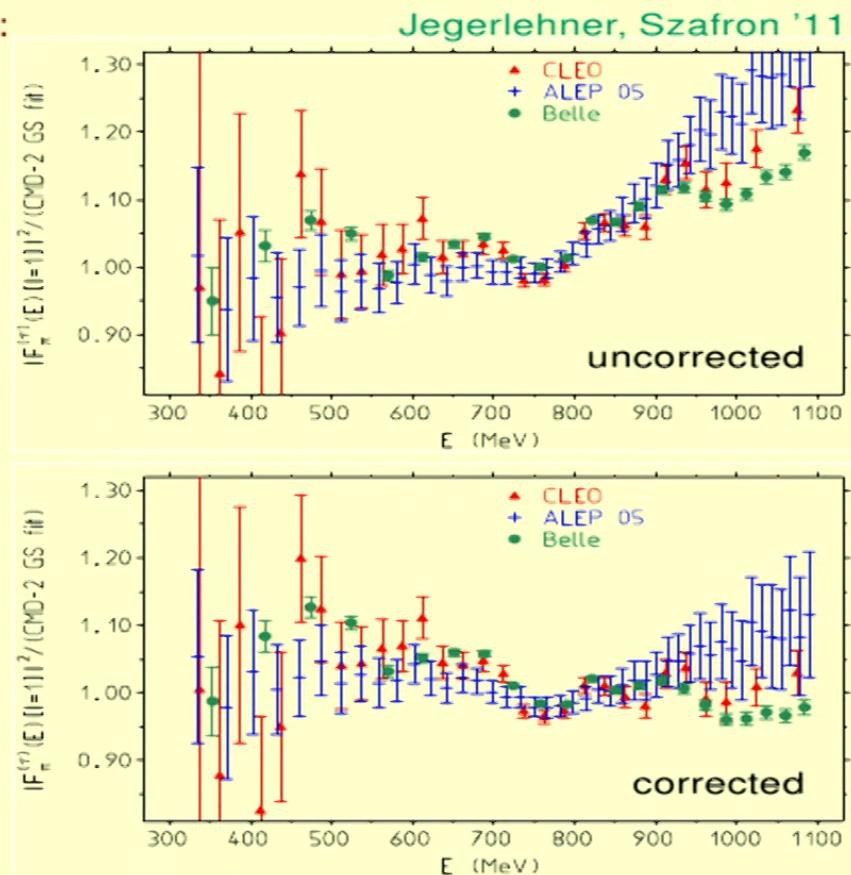
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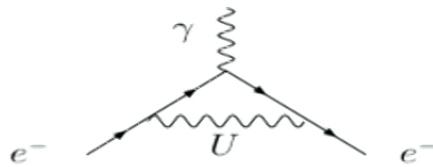


New neutral gauge boson

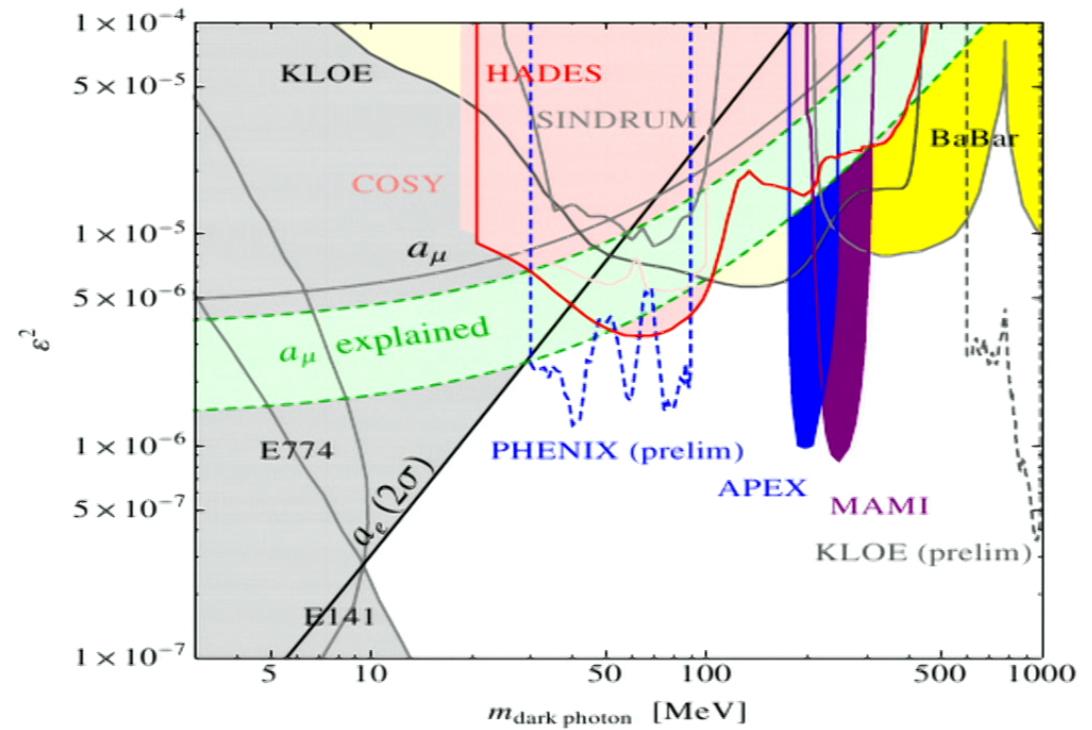
$m_U \sim \mathcal{O}(100 \text{ MeV})$ ,

which mixes with photon

$$\mathcal{L}_{\text{int}} = \frac{\epsilon}{2c_w} B_{\mu\nu} U^{\mu\nu}$$



Gninenko, Krasnikov '01  
 Fayet '07; Pospelov '08  
 Davoudiasl, Lee, Marciano '14



Introduce one or two new fields (spin 0,  $\frac{1}{2}$ , 1; SU(2) singlet, doublet, triplet)



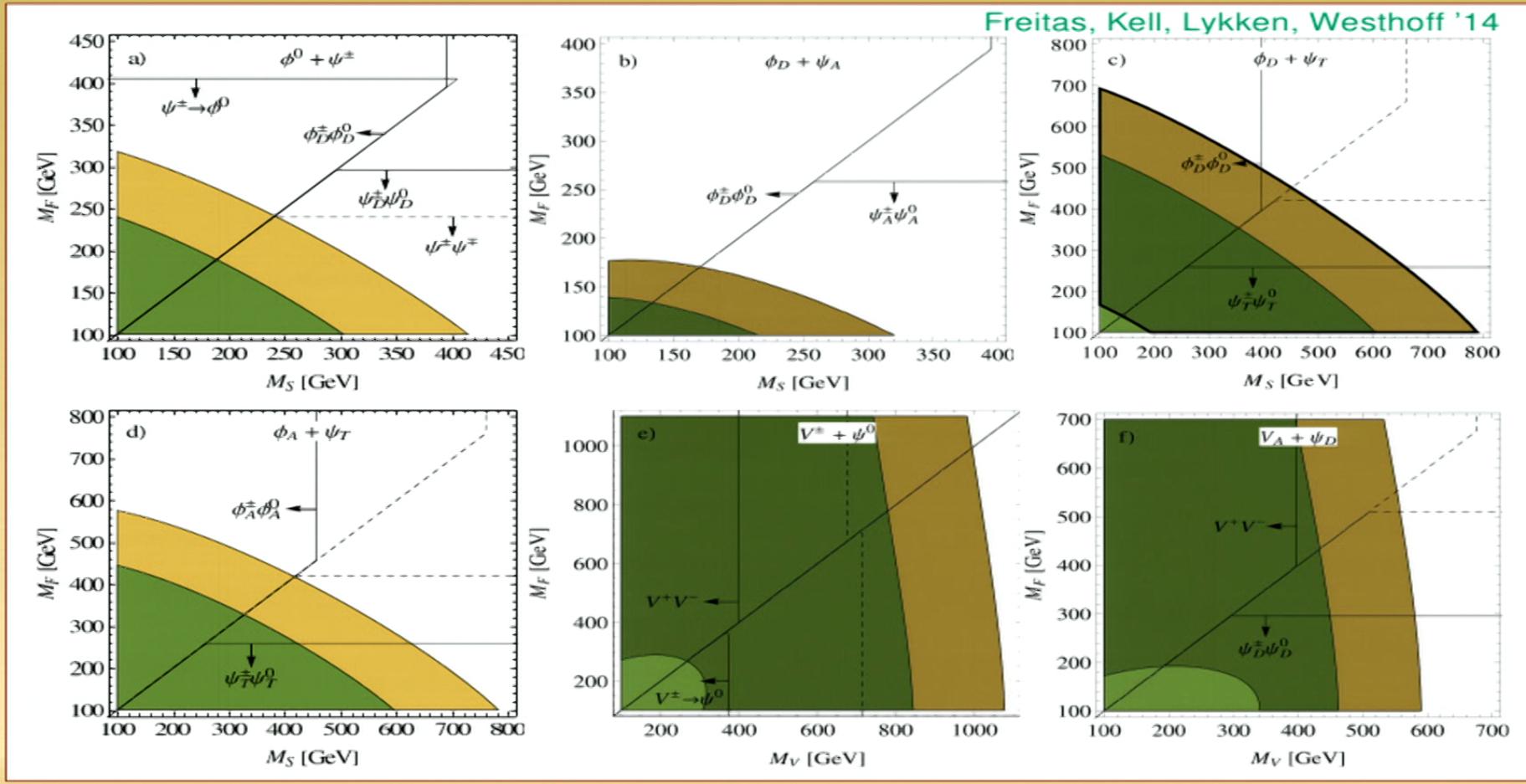
$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (29.3 \pm 8.4) \rightarrow \begin{cases} m_{\text{NP}} \sim \text{few} \times 100 \text{ GeV} \\ g_{\text{NP}} \sim 1 \end{cases}$$

→ Within reach of LHC!

- Identify parameter space that matches  $\Delta a_\mu$  at one-loop
- Compare with constraints from LHC searches

## Two new fields: Allowed parameter space

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## Conclusions

- W/Z precision data may move into the intensity frontier
  - Strong constraints on multi-TeV new physics
  - Interesting constraints on superweak 10–100 GeV-scale new physics?
- Low-energy precision experiments will become competitive with W/Z-pole data
  - Unique probes for light new physics
  - Muon  $g-2$  may already hint toward BSM,  
but hadronic error could be underestimated
- Good control over input parameters  $m_t$ ,  $M_W$ ,  $\alpha_s$  and  $\Delta\alpha_{\text{had}}$  is crucial
  - Influence of theory uncertainties!
- Open questions:
  - Improved higher-order (3-loop) corrections for  $Z$ -pole EWPO
  - Improved higher-order (2-loop) corrections for low-energy EWPO
  - Motivated new physics scenarios at scales  $\Lambda \lesssim \sqrt{s}$   
for future  $Z$ -pole and low-energy precision experiments
  - Parametrization of possible low-scale new physics  
( $\sin^2 \bar{\theta}(\mu)$ , eff. operators, etc.)