

Title: NMR signature of charge order in high Tc cuprates revisited

Date: May 25, 2017 11:00 AM

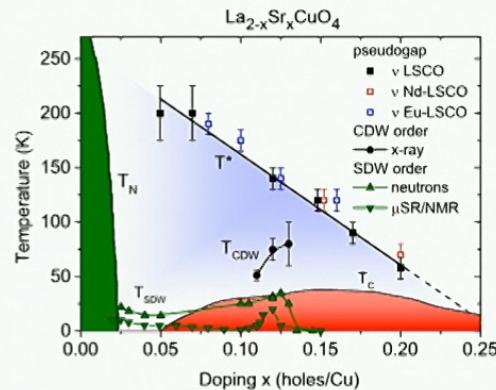
URL: <http://pirsa.org/17050084>

Abstract: In 1999, A. W. Hunt et al. discovered that all the NMR anomalies detected at the charge density wave (CDW) order transition $T_{\text{charge}} \sim 60$ K of nearly non-superconducting $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ are shared by superconducting $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$ ($T_c \sim 30$ K) [1]. The unexpected finding inevitably led us to conclude that charge order must exist even in the superconducting $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, sending a shockwave in the high-Tc community [2]. Subsequent search of charge order peaks based on scattering techniques, however, failed to detect additional evidence for charge order until very recently. In view of the recent confirmation of charge order in many superconducting cuprates by X-ray diffraction techniques, we revisit the old problem of charge order using newer NMR techniques that have become available in recent years.

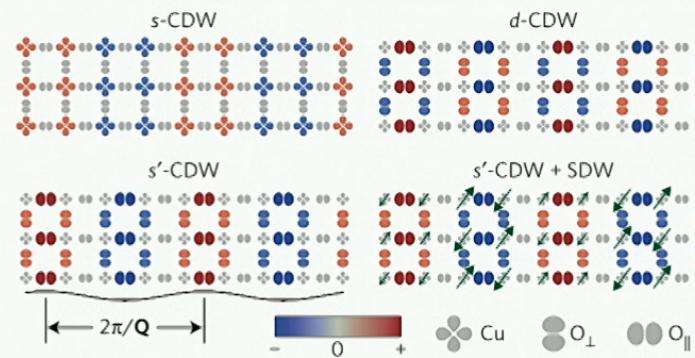
NMR signature of charge order in high T_c cuprates revisited
--- ^{63}Cu and ^{139}La NMR study of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ ($T_c \sim 31\text{K}$, $T_{\text{charge}} \sim 80\text{K}$)
using a modern 21st century NMR spectrometer

Takashi Imai
McMaster University and CIFAR

T. Imai, M. Fujita, W. He, Y.S. Lee et al., in preparation.
A.W. Hunt, P.M. Singer, T.Imai et al., PRL **82** (1999) 4300; PRB **64** (2001) 134524.



Phase diagram by
Croft et al. PRB **89** (2014) 224513

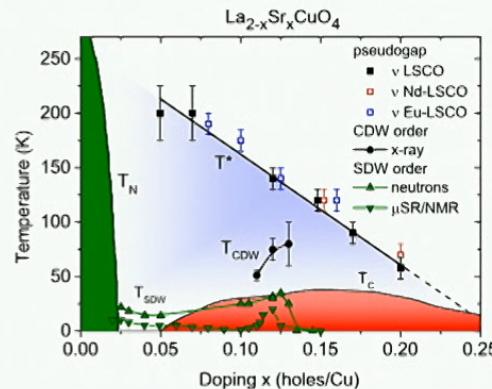


Charge density pattern examined by
Achkar, Hawthorn et al. Nat. Mat. **15** (2014) 616

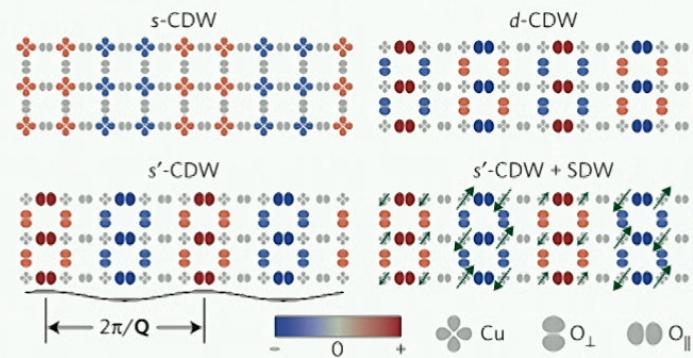
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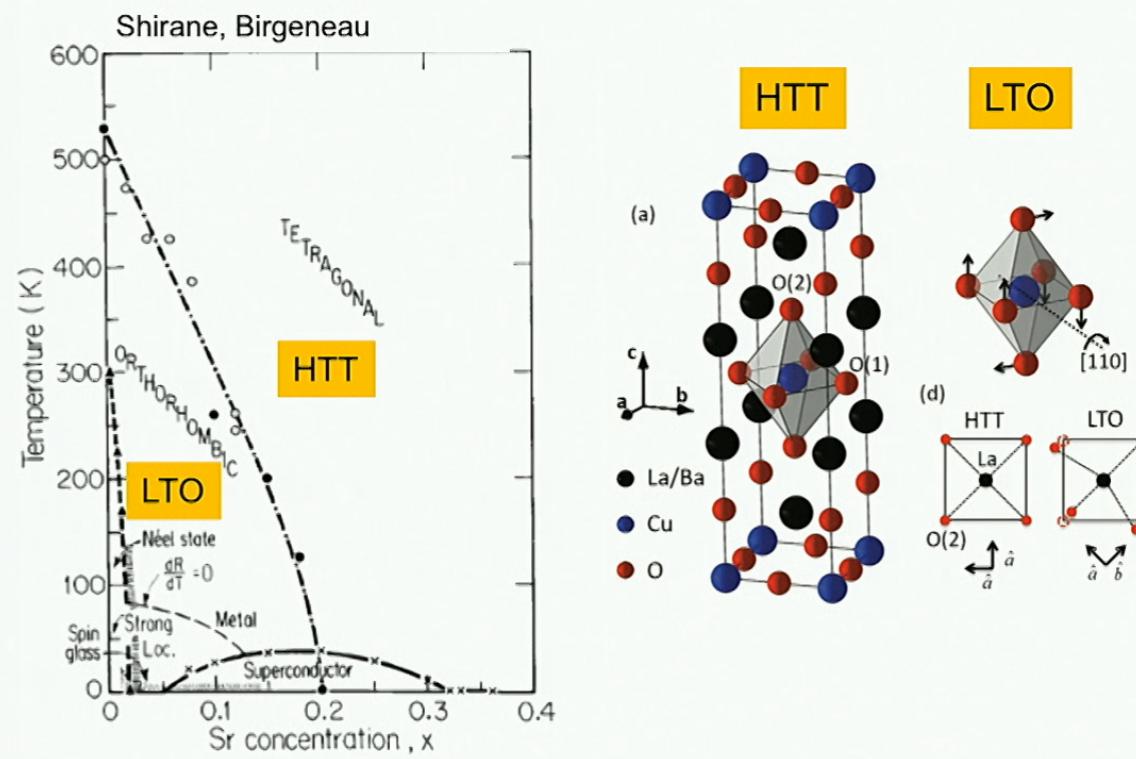


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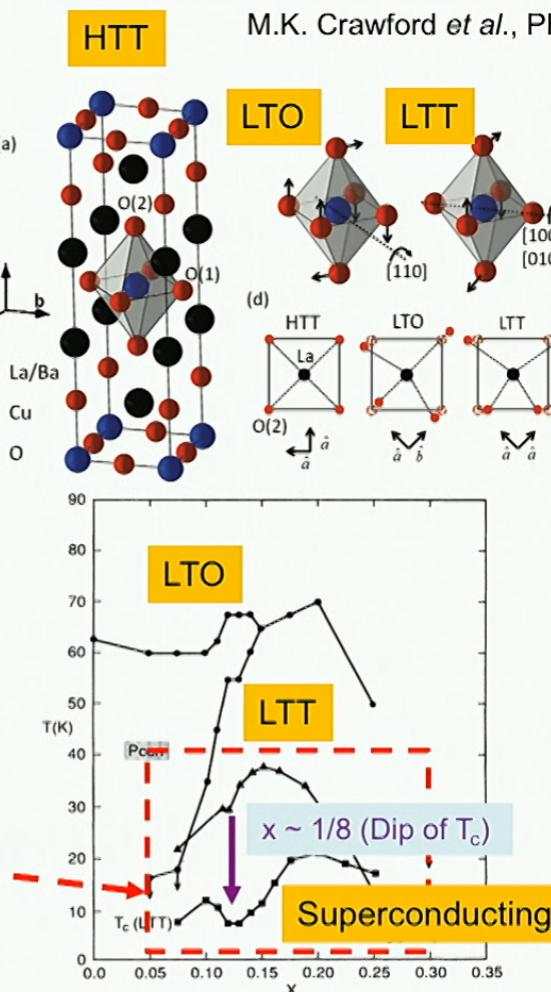
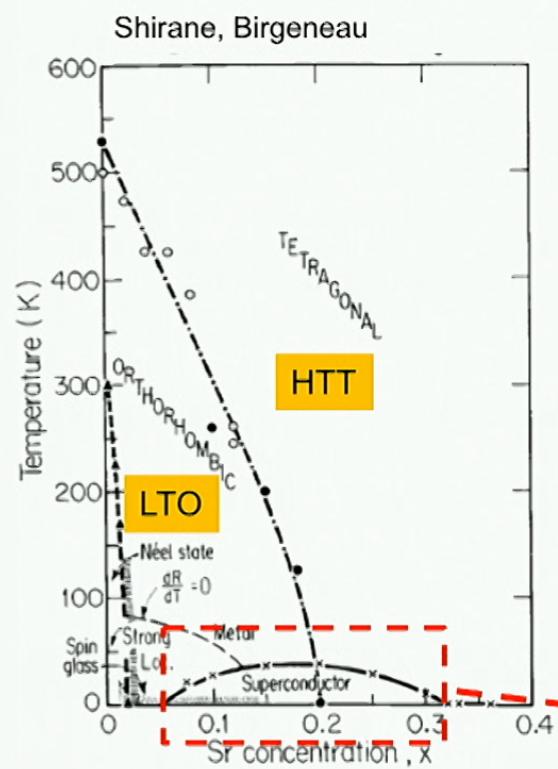
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“Original” phase diagram of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ high T_c cuprates in the early 1990’s

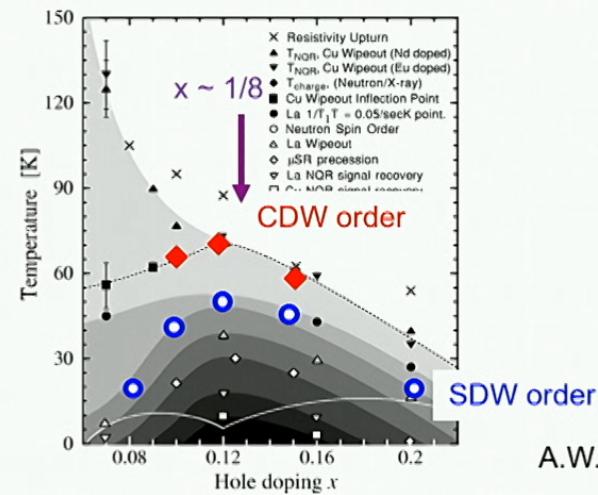
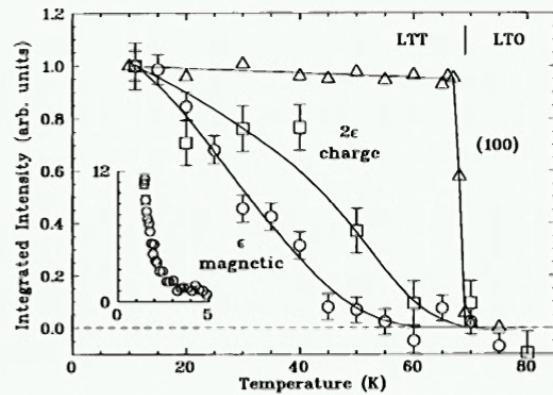


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“1/8 anomaly” : Nd³⁺ substitution into La³⁺ sites of La_{2-x}Sr_xCuO₄ stabilizes the LTT structure and suppresses T_c around x ~ 1/8

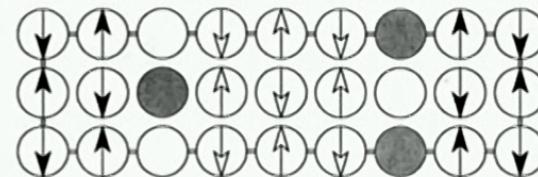


The 1/8 anomaly in the phase diagram of $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ high T_c cuprates arises from Charge and Spin Density Wave Orders



J. Tranquada *et al.*, Nature **375** (1995) 561

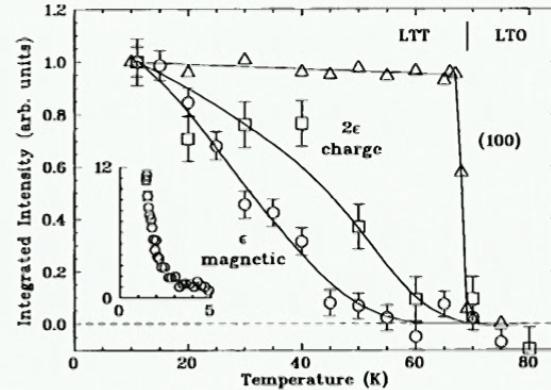
(Note: the SDW order was first discovered for the 1/8 phase of $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$ by G. Luke *et al.*, Physica C **185-189** (1991) 1175).



4

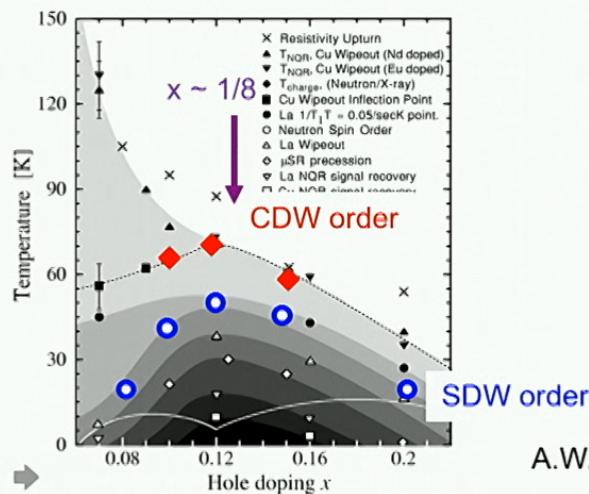
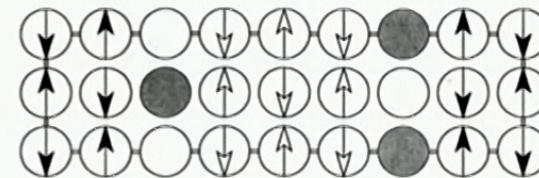
A.W. Hunt, T.I. *et al.*, PRB **64** (2001) 134524

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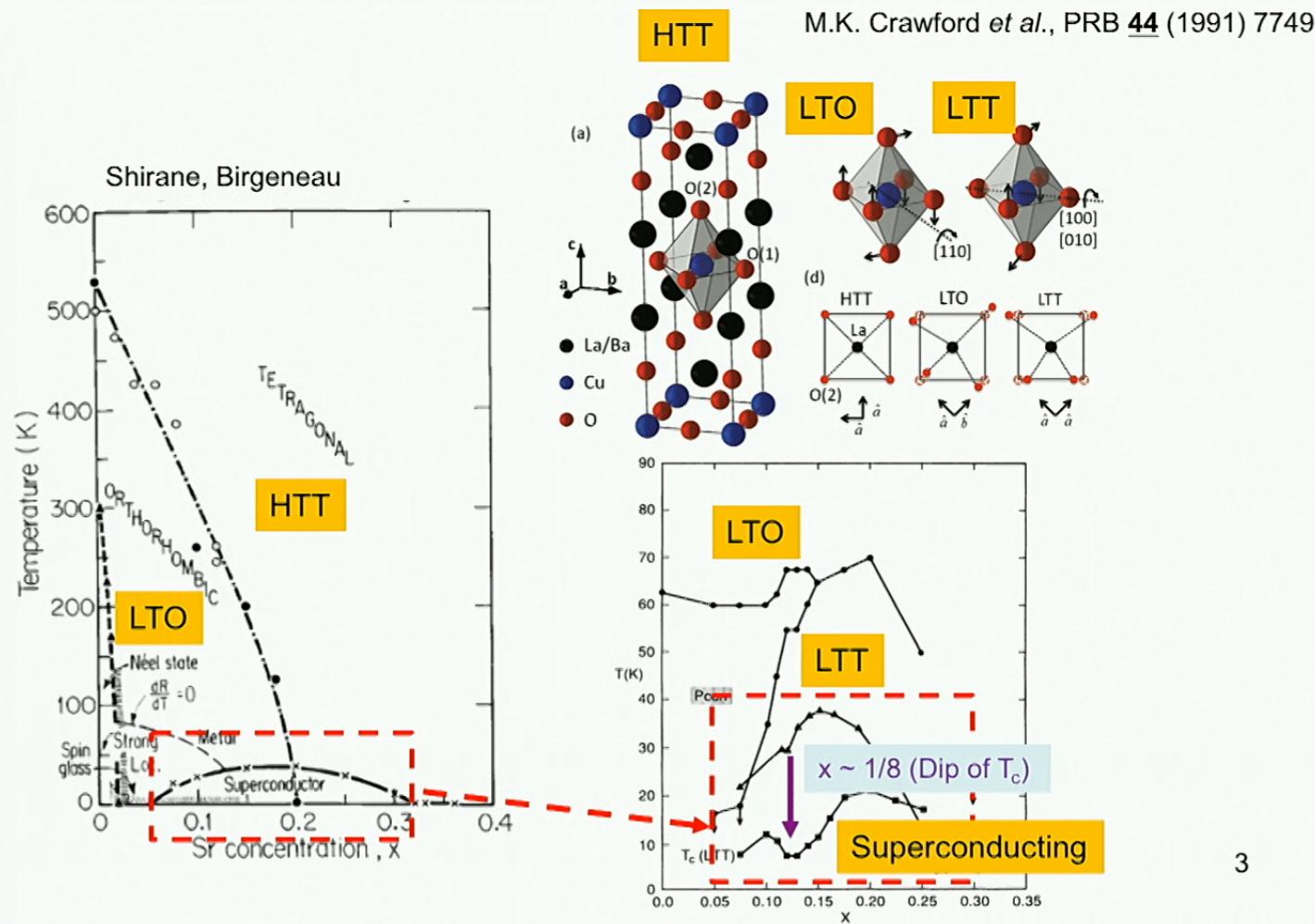
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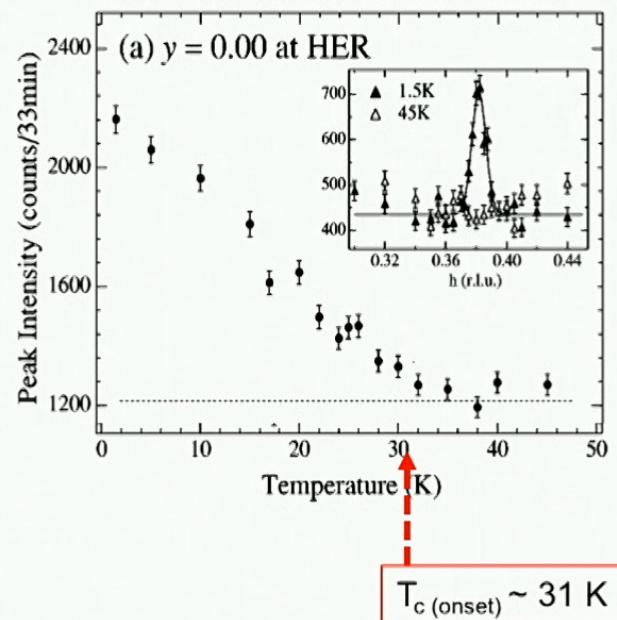
“1/8 anomaly” : Nd³⁺ substitution into La³⁺ sites of La_{2-x}Sr_xCuO₄ stabilizes the LTT structure and suppresses T_c around x ~ 1/8



July 1998: it turned out that the SDW anomaly for $x \sim 1/8$ exists even in superconducting $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$ with the LTO structure (without the LTT structural phase transition)

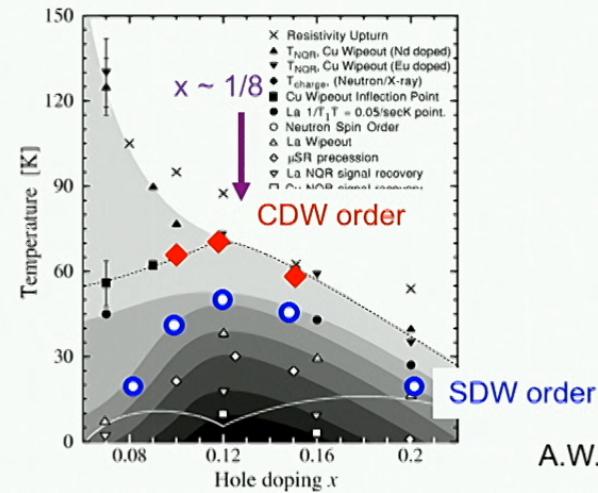
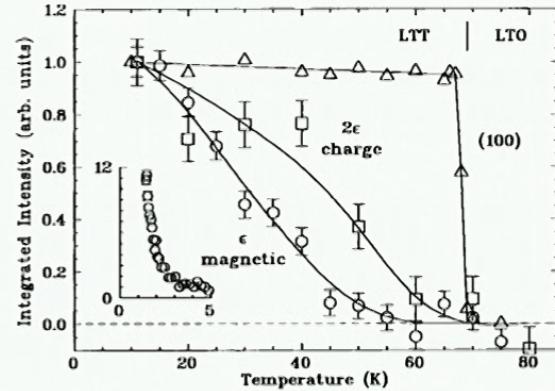
Magnetic Bragg peak intensity in $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$

Kimura et al., PRB **59** (1999) 6517



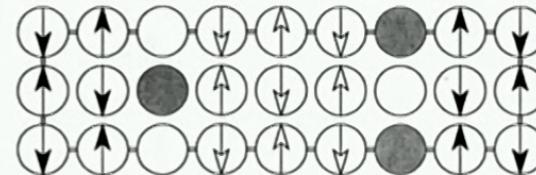
Does superconducting $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$ also undergo a CDW order?

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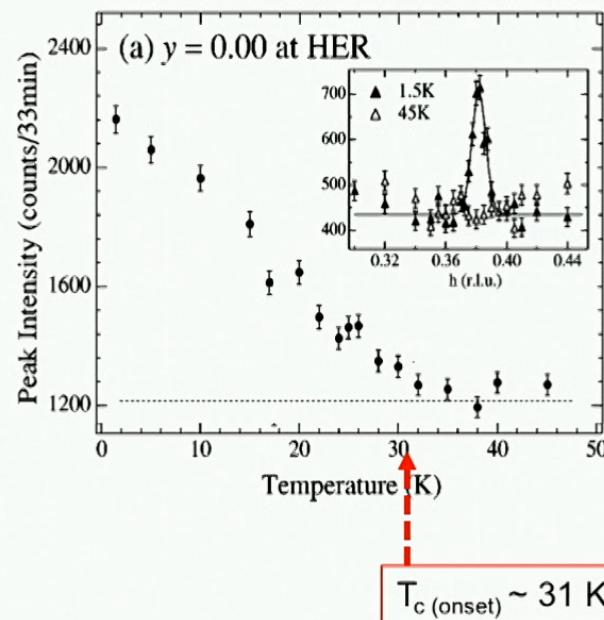
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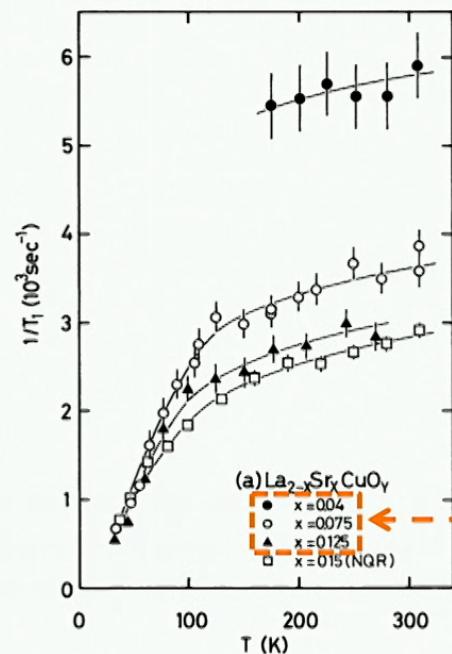
From the late 1980's, we knew that ^{63}Cu NMR signals in LSCO ($x \sim 1/8$) begin to lose its intensity below about 50 K. We didn't know why. Is it related to charge order?!

Journal of The Physical Society of Japan
Vol. 59, No. 11, November, 1990, pp. 3846-3849

LETTERS

^{63}Cu NMR Study of Spin Dynamics
in $\text{La}_{2-x}(\text{Sr}, \text{Ba})_x\text{CuO}_y$ ($0.04 \leq x \leq 0.16$, $3.99 \leq y \leq 4.03$)

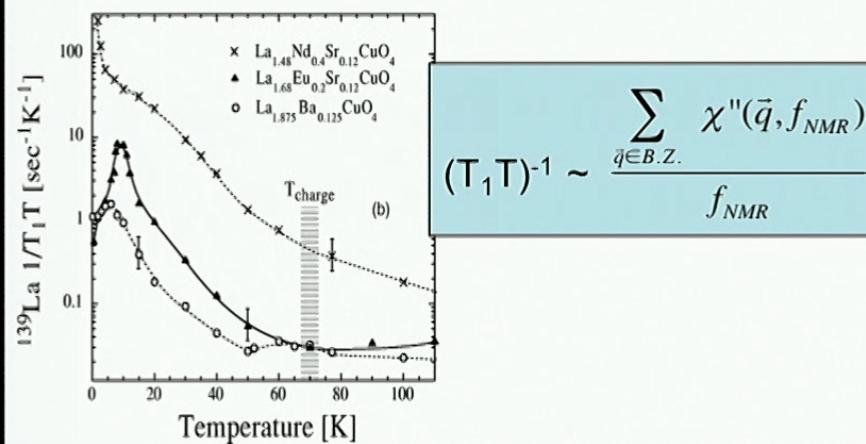
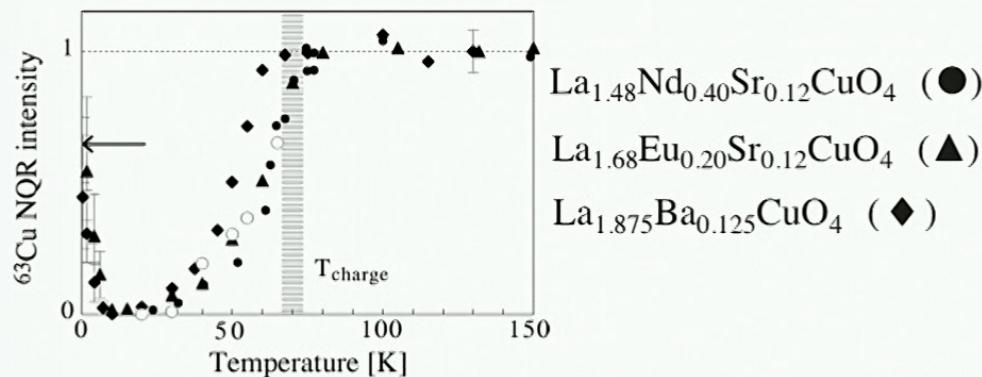
Takashi IMAI, Kazuyoshi YOSHIMURA,[†] Takashi UEMURA,[†]
Hiroshi YASUOKA and Koji KOSUGE[†]



"New data" of 1990 didn't even show results at lower temperatures, because paramagnetic ^{63}Cu NMR signals disappear, a mystery at that time.

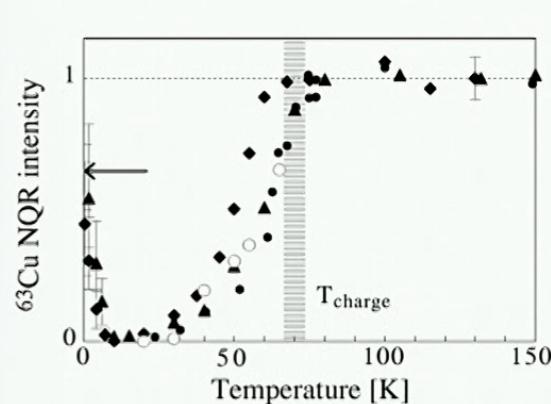
Confirmation: $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ indeed shows analogous ^{63}Cu NMR signal intensity anomaly exactly at the CDW order temperature, $T_{\text{charge}} \sim 65$ K, accompanied by enhanced spin fluctuations

A.W. Hunt, T.I. et al., PRB **64** (2001) 134524

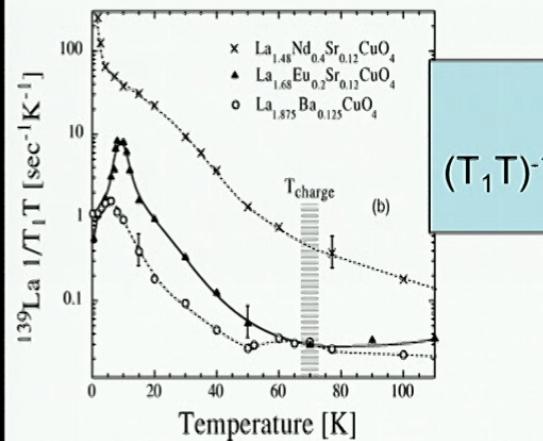
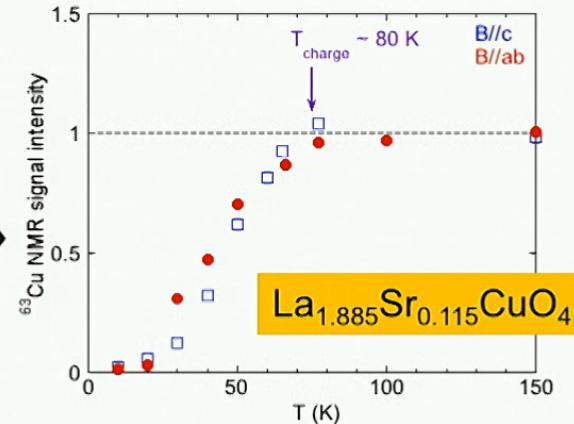


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$\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$
 $\text{La}_{1.68}\text{Eu}_{0.20}\text{Sr}_{0.12}\text{CuO}_4$
 $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$ (◆)



^{63}Cu single crystal NMR data of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ shows analogous anomalies below as high as $T_{\text{charge}} \sim 80$ K!!

T. Imai and K. Hirota
 Unpublished data first presented at Aspen Winter Conference on Quantum Critical Phenomena in January 1999.
 $(T_{\text{charge}} \sim 80$ K seemed too high, as there is no LTT transition)

^{63}Cu NQR Measurement of Stripe Order Parameter in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

A. W. Hunt, P. M. Singer, K. R. Thurber, and T. Imai

Department of Physics and Center for Materials Science and Engineering, MIT, Cambridge, Massachusetts 02139

(Received 4 January 1999)

We demonstrate that one can measure the charge-stripe order parameter in the hole-doped CuO₂ planes of La_{1.875}Ba_{0.125}CuO₄, La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄, and La_{1.68}Eu_{0.2}Sr_{0.12}CuO₄ utilizing the wipeout effects of ^{63}Cu nuclear quadrupole resonance. Application of the same approach to La_{2-x}Sr_xCuO₄ reveals the presence of similar stripe order for the entire underdoped superconducting regime $\frac{1}{16} \lesssim x \lesssim \frac{1}{8}$. [S0031-9007(99)09198-X]

The primary conclusion: La_{1.88}Sr_{0.12}CuO₄ (as well as La_{1.68}Eu_{0.2}Sr_{0.12}CuO₄, La_{1.88}Ba_{0.12}CuO₄, and La₂CuO_{4+y}) undergoes charge order at a comparable temperature as La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄
Highlighted in Science magazine in 1999 & cited over 200 times to date
A big problem..... Nobody else could confirm charge order for years

^{63}Cu NQR Measurement of Stripe Order Parameter in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

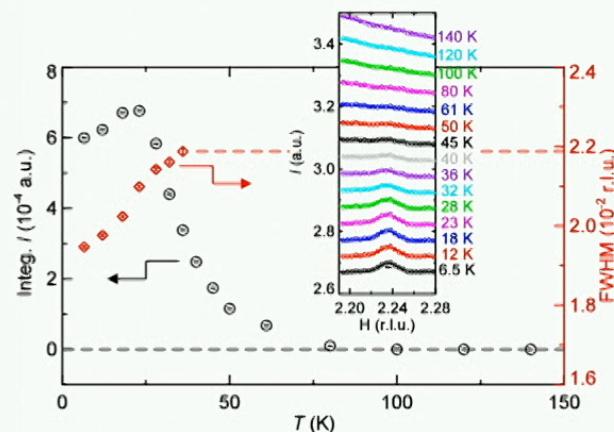
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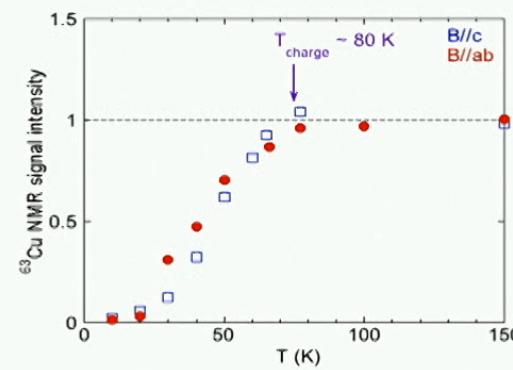
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We demonstrate that one can measure the charge-stripe order parameter in the hole-doped CuO_2 planes of $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$, $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$, and $\text{La}_{1.68}\text{Eu}_{0.2}\text{Sr}_{0.12}\text{CuO}_4$ utilizing the wipeout effects of ^{63}Cu nuclear quadrupole resonance. Application of the same approach to $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ reveals the presence of similar stripe order for the entire underdoped superconducting regime $\frac{1}{16} \leq x \leq \frac{1}{8}$. [S0031-9007(99)09198-X]

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A big problem..... Nobody else could confirm charge order **for years until recently**



W. He, Y.S. Lee, M. Fujita et al. (Stanford/Tohoku 2017)
 Also see Croft (PRB 2014) & Thumpy (PRB 2014)

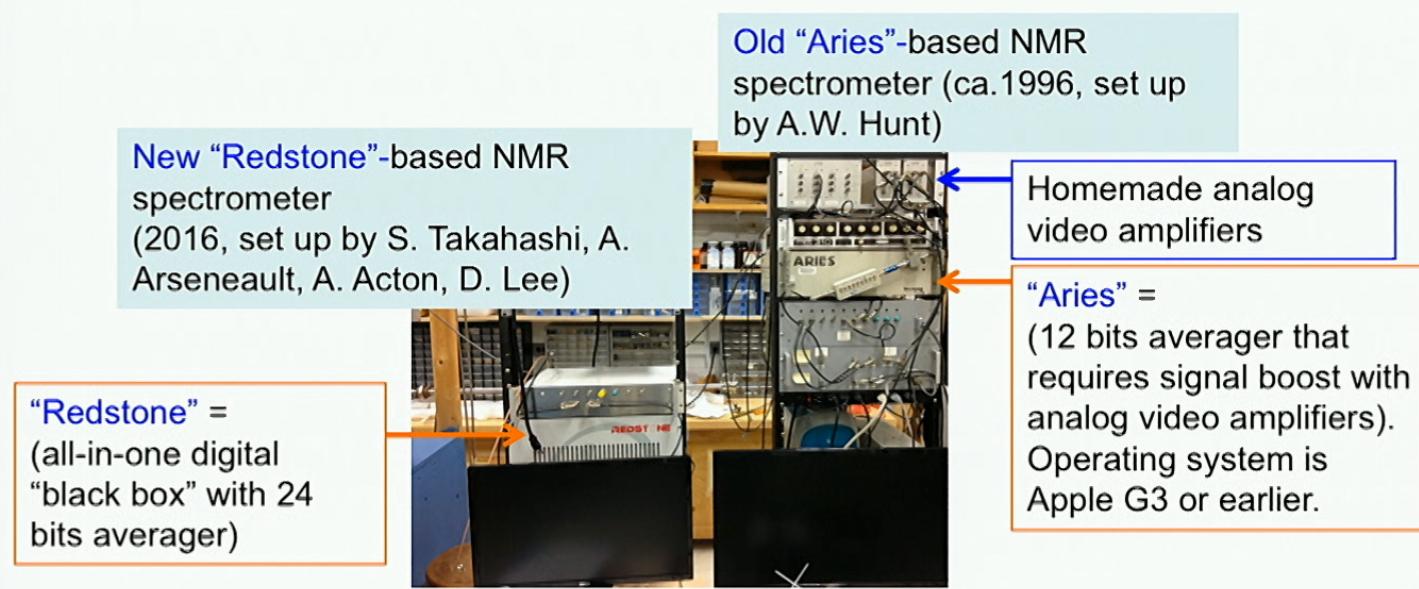


T. Imai and K. Hirota (1999)

10

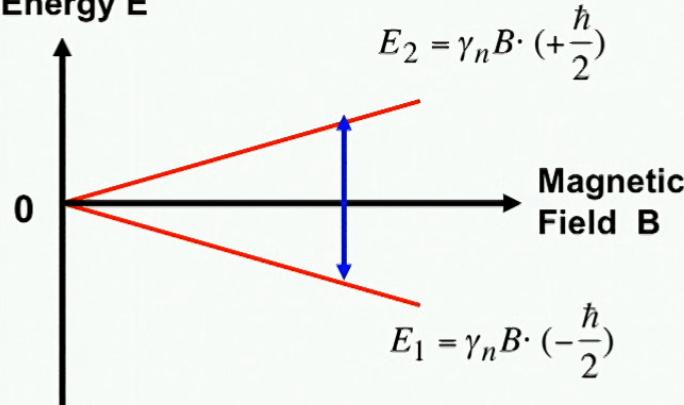
We have been finally vindicated(!!) and charge order exists even in superconducting $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$ etc. (although new comers don't even know the raging battle in ~1999).

But a question remains: why did charge order led to those NMR anomalies?
Let's revisit using modern NMR techniques.



Zeeman interaction (for nuclear spin $I = 1/2$) and “magnetic resonance”

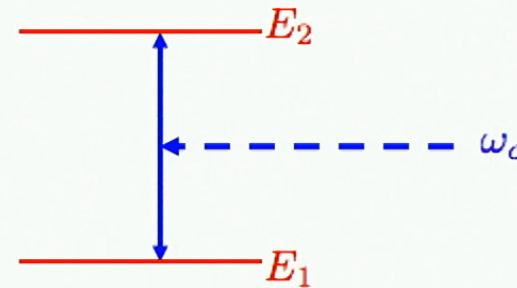
**Zeeman
Energy E**



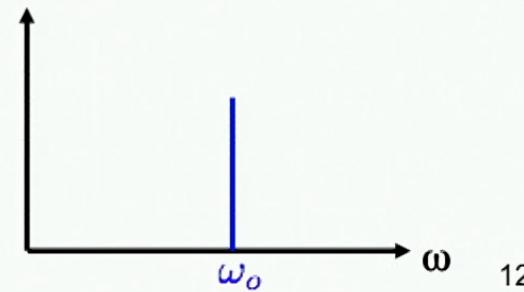
Photons with frequency

$$\omega_o = \frac{E_2 - E_1}{\hbar} = \gamma_n B$$

may be absorbed by nuclear spins,
where γ_n is the nuclear
gyromagnetic ratio.

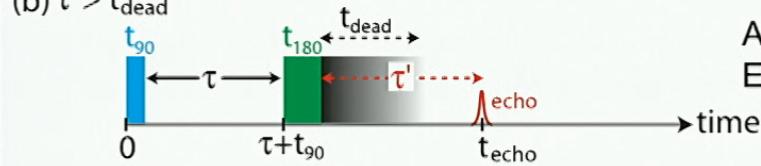


Absorption intensity (“NMR Spectrum”)



How do we detect NMR spin-echo signals?

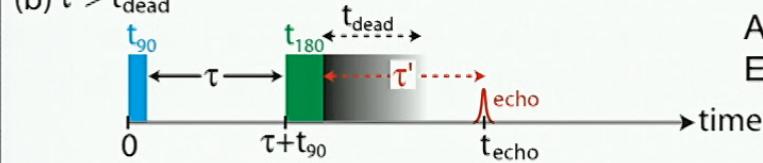
(b) $\tau' > t_{\text{dead}}$



Apply 90 & 180 degree RF pulses, separated by τ .
Echo appears $\tau' = \tau + t_{180}/\pi$ after we turn off 180.

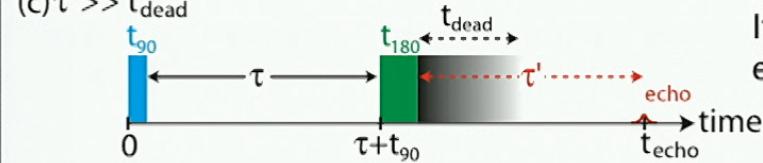
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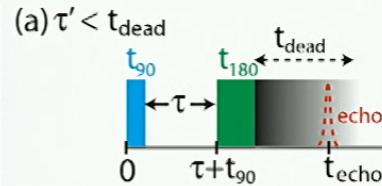
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(c) $\tau' \gg t_{\text{dead}}$

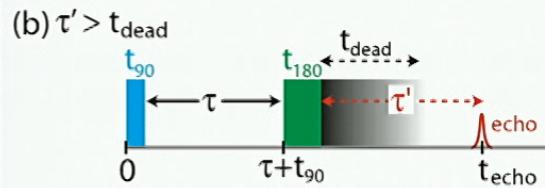


If $\tau' \gg T_2$ (the transverse relaxation time), the echo becomes small.

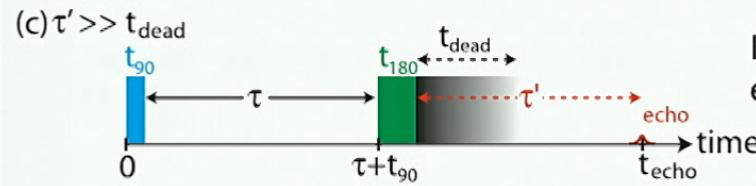
How do we detect NMR spin-echo signals?



τ' must be longer than the spectrometer dead-time, $t_{\text{dead}} \sim 2\mu\text{s}$, to observe the echo.



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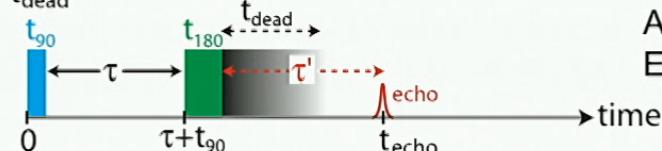
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(a) $\tau' < t_{\text{dead}}$



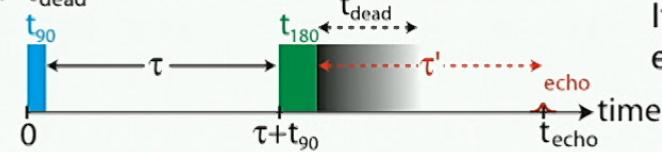
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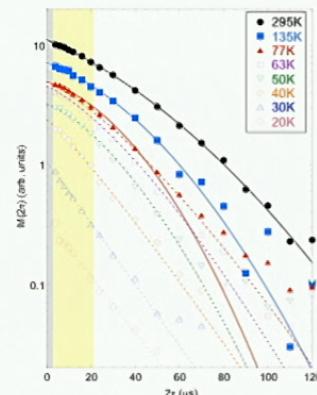
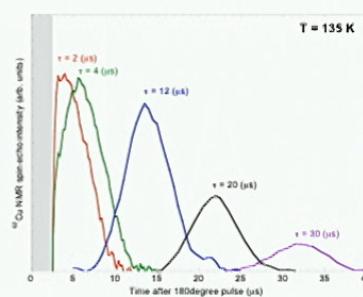


Apply 90 & 180 degree RF pulses, separated by τ . Echo appears $\tau' = \tau + t_{180}/\pi$ after we turn off 180.

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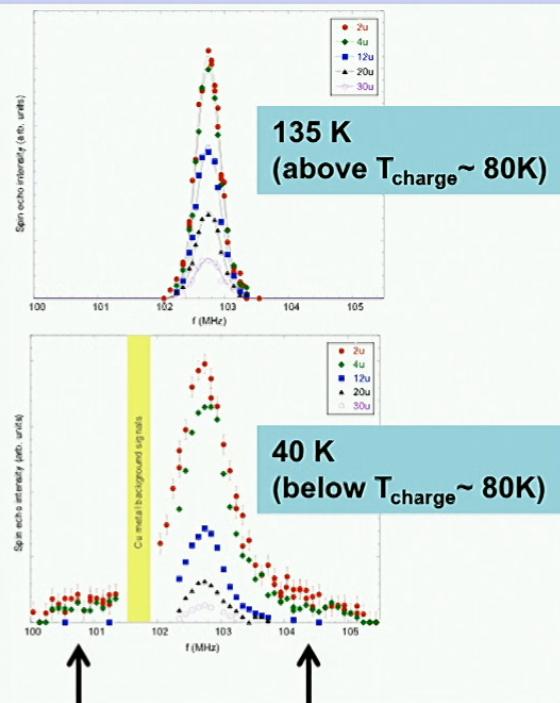


$t_{\text{dead}} \sim 12\text{ }\mu\text{s}$ for Aries (1999)

$t_{\text{dead}} \sim 2\text{ }\mu\text{s}$ for Redstone (2017)

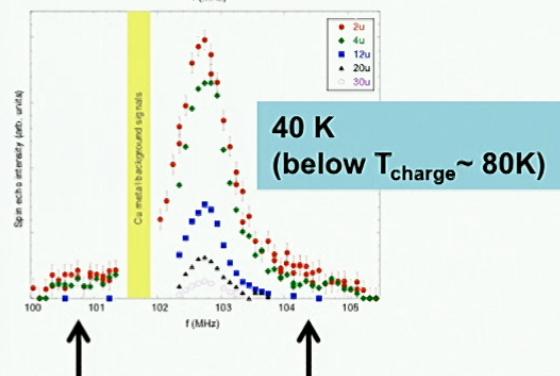
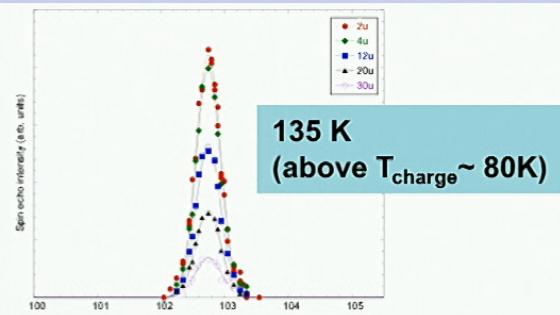
We can detect fast phenomena with newer NMR spectrometers

^{63}Cu NMR lineshapes of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ single crystal (9T || c-axis)

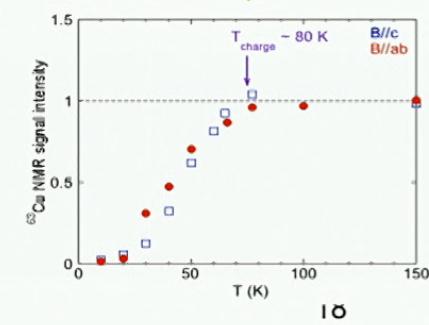
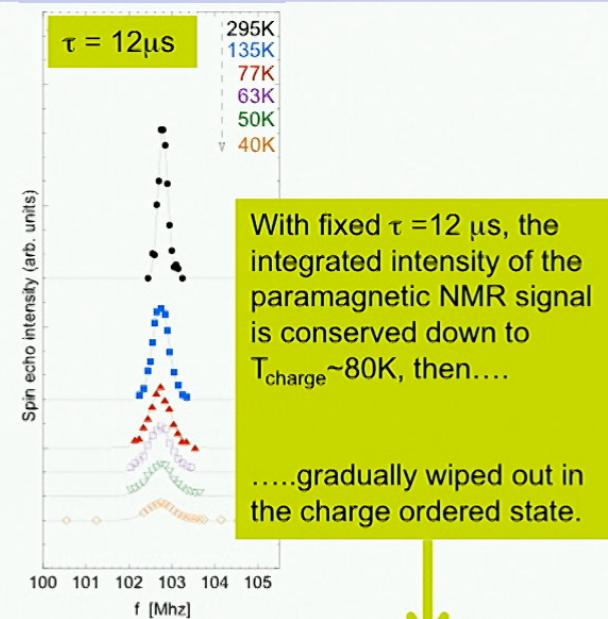


New, broad wings appear in the charge ordered state below $T_{\text{charge}} = 80\text{K}$ if we use very short $\tau = 2$ or $4 \mu\text{s}$. Our old NMR spectrometers used in the 1990's had analog video-amplifiers with $t_{\text{dead}} \sim 12 \mu\text{s}$, and we were unable to detect these very fast signals.

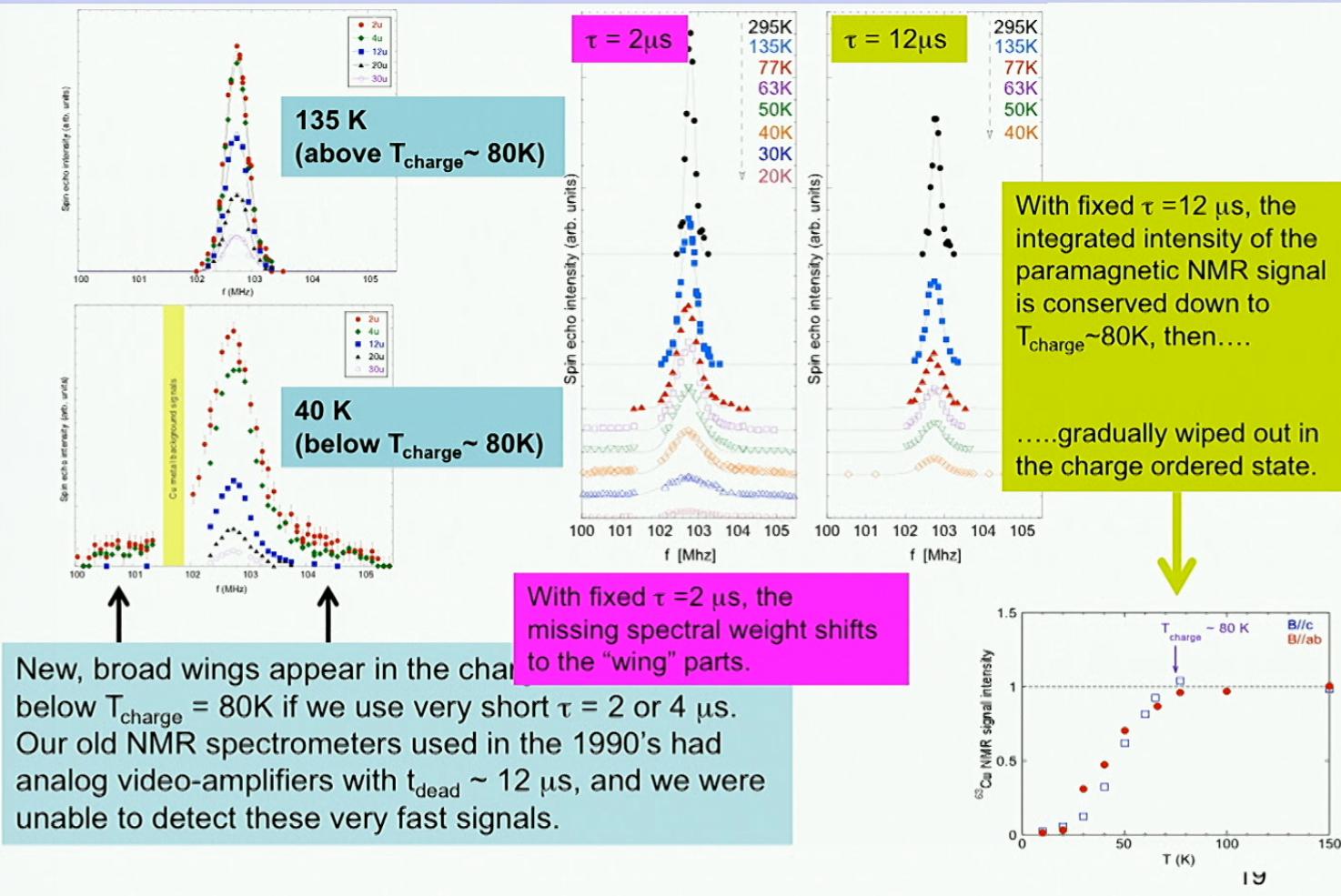
^{63}Cu NMR lineshapes of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ single crystal (9T || c-axis)



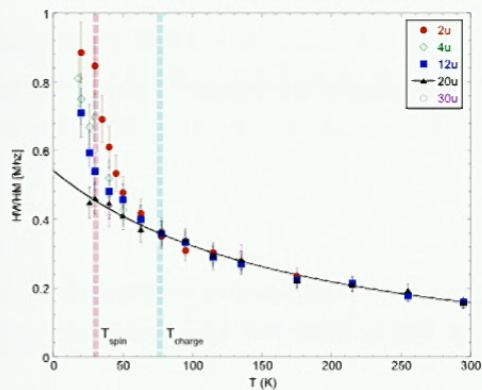
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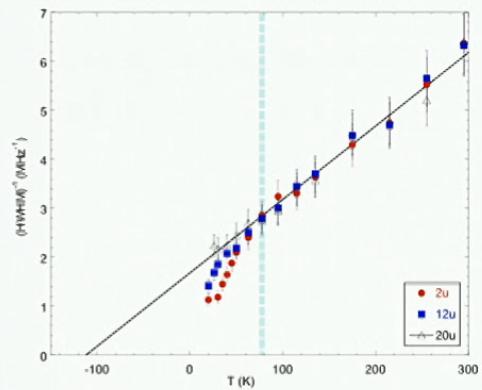
Other ^{63}Cu NMR anomalies below $T_{\text{charge}} \sim 80$ K:
 Real part of the dynamic spin susceptibility $\chi'(\mathbf{q})$ measured with the linewidth



^{63}Cu NMR linewidth with the $B_{\text{ext}} \parallel c$ -axis geometry is broadened by the “*indirect nuclear spin-spin coupling*” effects (originally proposed in the context of NMR by Ruderman-Kittel).

$$(\text{HWHM}) \sim \sum_{\vec{q} \in B.Z.} \chi'(\vec{q})$$

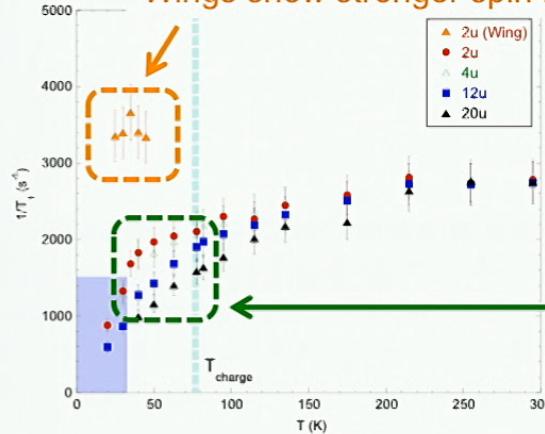
Magnetic correlations gradually grow following an A.F. Curie-Weiss law down to $T_{\text{charge}} \sim 80$ K, a common observation for Cuprates.



Then suddenly begins to diverge at T_{charge} toward the spin ordering temperature, $T_{\text{spin}} \sim 30$ K.

Other ^{63}Cu NMR anomalies below $T_{\text{charge}} \sim 80$ K:
 Imaginary part of the dynamic spin susceptibility $\chi''(\vec{q}, f_{\text{NMR}})$ measured with T_1

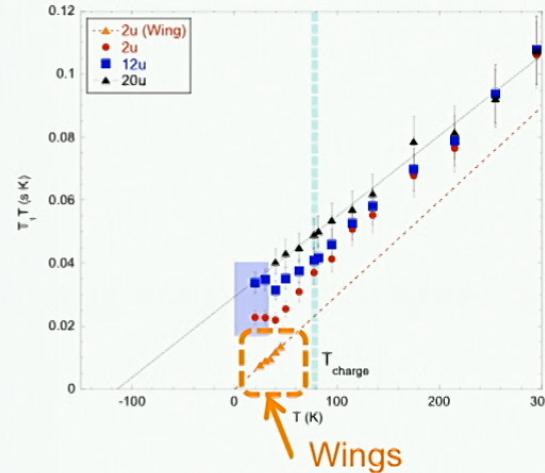
Wings show stronger spin fluctuations



$$1/T_1 \sim \sum_{\vec{q} \in \text{B.Z.}} S(\vec{q}, f_{\text{NMR}}) \quad [\text{spin fluctuations at NMR frequency } f_{\text{NMR}}]$$

Gradually diminishing center peak represents “normally behaving segments of CuO_2 planes.” Its $1/T_1$ is very similar to that in optimally superconducting phase.

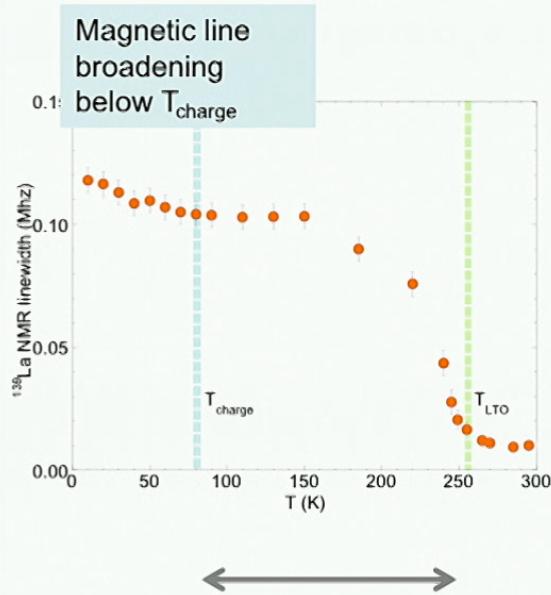
Note: CuO_2 planes become inhomogeneous below T_{charge} ; some segments of CuO_2 planes are not affected by charge order down to ~ 30 K.



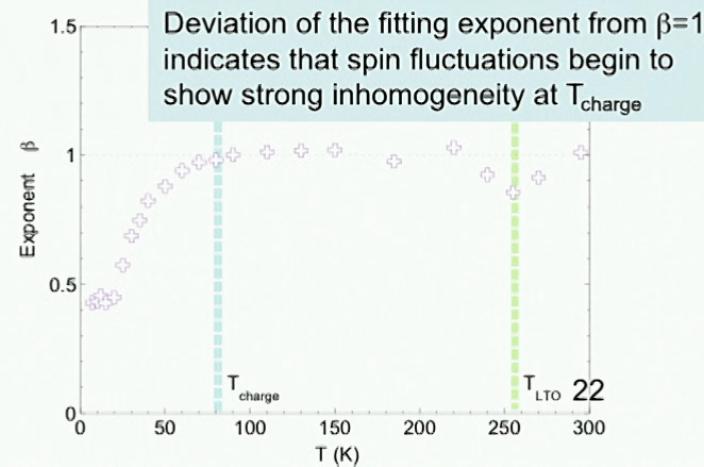
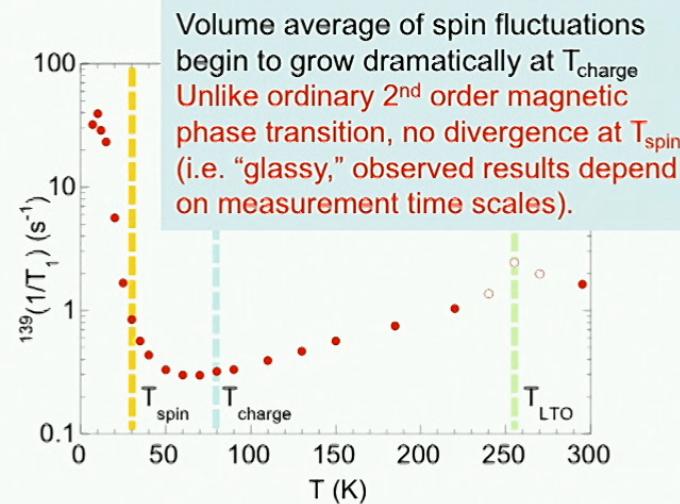
$$(T_1 T)^{-1} \sim \frac{\sum_{\vec{q} \in \text{B.Z.}} \chi''(\vec{q}, f_{\text{NMR}})}{f_{\text{NMR}}}$$

obeys a similar C.W. law as (HWHM) above T_{charge} .

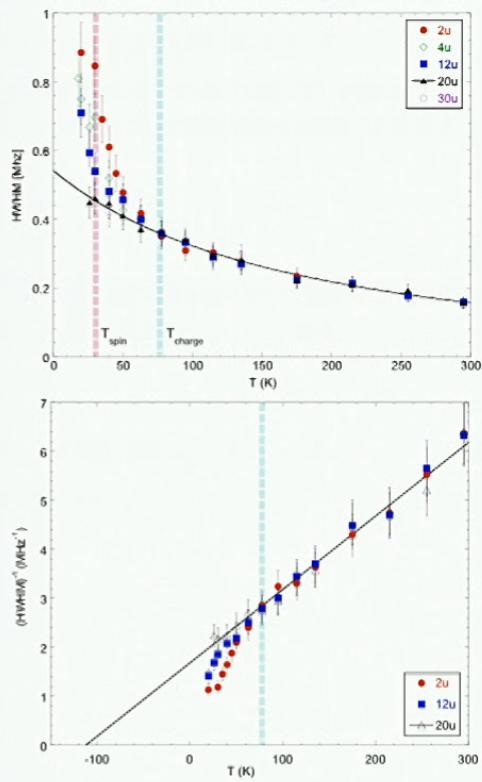
^{139}La NMR anomalies below $T_{\text{charge}} \sim 80$ K:
Real (linewidth) and imaginary part (T_1) of the dynamic spin susceptibility



Broadening due to nuclear quadrupole effects caused by tilting of CuO_6 octahedra below T_{LTO}



Other ^{63}Cu NMR anomalies below $T_{\text{charge}} \sim 80$ K:
 Real part of the dynamic spin susceptibility $\chi'(\mathbf{q})$ measured with the linewidth



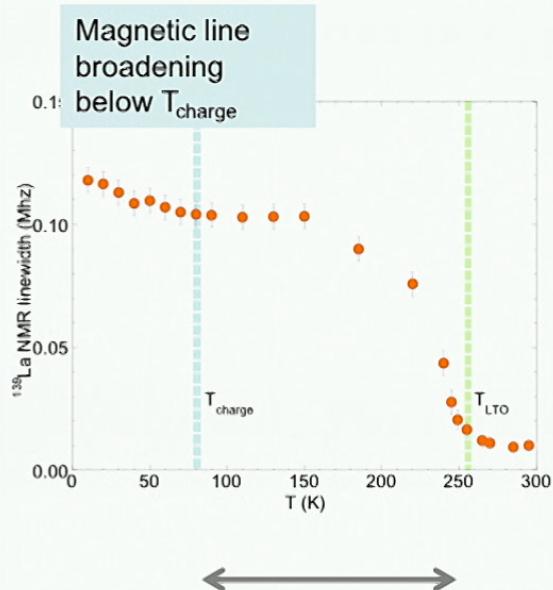
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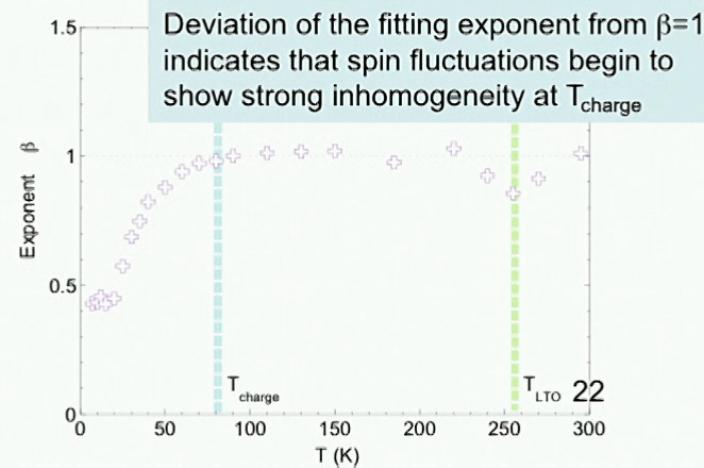
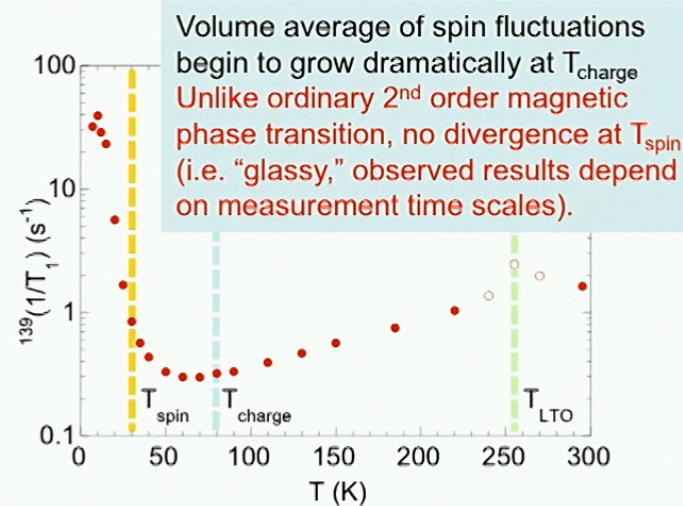
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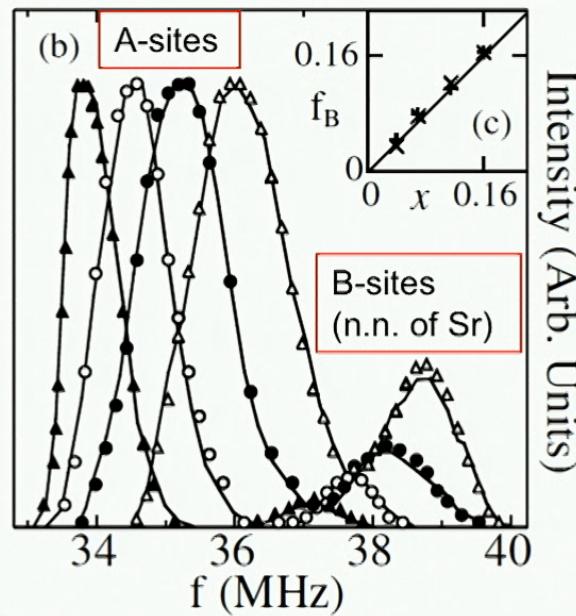


Broadening due to nuclear quadrupole effects caused by tilting of CuO_6 octahedra below T_{LTO}



How much does charge density modulate below T_{charge} ? ---- Small !

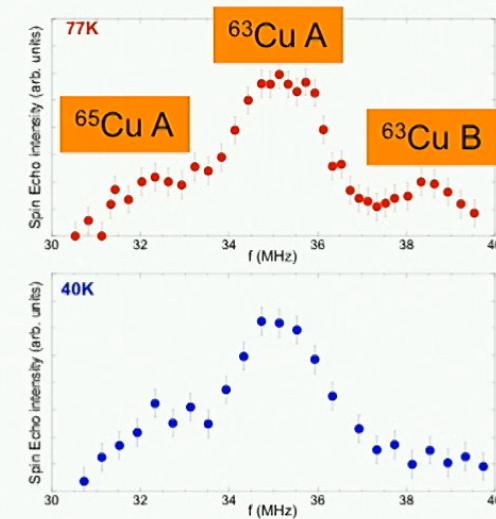
^{63}Cu NQR lineshapes for ^{63}Cu isotope enriched powders with $x = 4\%, 7\%, 11\%, 16\%$



^{63}Cu NQR frequency is sensitive to the hole concentration and its distribution

Singer, Hunt, T.I., PRL 88 (2001) 047602

$^{63,65}\text{Cu}$ NQR lineshapes for $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ single crystal measured with $\tau = 4 \mu\text{s}$



Practically no changes in $^{63,65}\text{Cu}$ NQR lineshapes below T_{charge}

Summary

- 1999 NMR discovery of charge order signatures in superconducting $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ etc. finally verified by recent X-ray scattering experiments.
- Local probe study based on NMR shows that charge order makes the CuO_2 planes inhomogeneous both in time and space, and turns on strong magnetic correlations that affect growing fraction of the CuO_2 planes below T_{charge} .
Note: some fraction of CuO_2 planes remain unaffected by charge order even at $T \ll T_{\text{charge}}$. That is why the first generation NMR study overlooked charge order anomaly in the late 1980's.
- NMR is highly sensitive to charge order in $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ owing to strong magnetism in charge ordered segments of CuO_2 planes
- Modulation of charge density in $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ appears very small (hence it took years to detect it by modern diffraction techniques).