

Title: Baryogenesis from L-violating Higgs doublet decay

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Abstract: <p>In the framework of the ordinary seesaw model with right-handed neutrinos (and nothing else) we show that the total lepton number violating decay of the Higgs doublet into a right-handed neutrino and a standard model lepton can successfully account for the baryon asymmetry of the Universe. This is possible thanks to thermal effects shortly before the sphalerons decouple.</p>

# Baryogenesis from L-violating Higgs doublet decay

Thomas Hambye  
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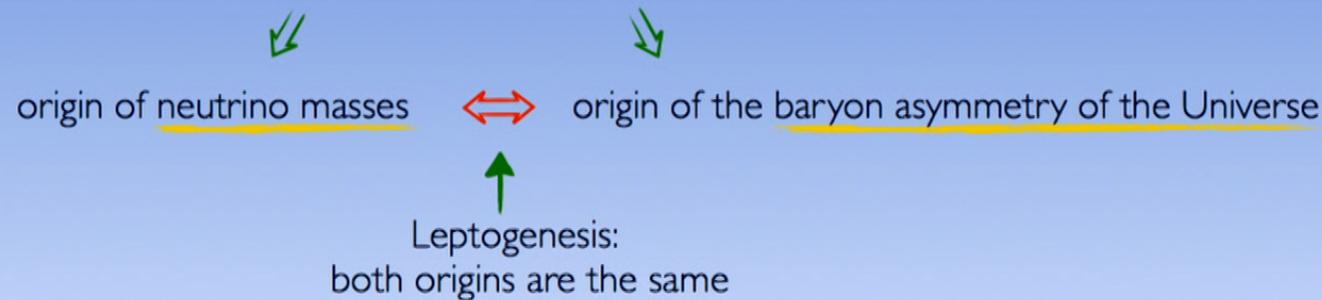
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Work in collaboration with Daniele Teresi (ULB): arXiv:1606.00017 (PRL 2016)  
arXiv:1705.00016

Perimeter Institute, 09/05/2017

## Leptogenesis motivation

Two fundamental questions beyond the Standard Model



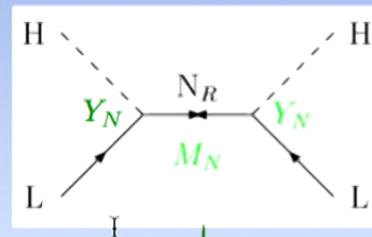
+ <sup>I</sup> a series of numerical coincidences which makes it particularly effective

## The 3 seesaw models

Fermion singlets:  
(type-I seesaw)

$$N_{R_i}$$

$$\mathcal{L} \ni -Y_{N_i j} \bar{N}_i L_j H - \frac{m_{N_i}}{2} \bar{N}_i^c N_i + h.c.$$



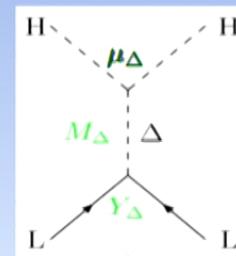
$$m_\nu = Y_N^T \frac{1}{M_N} Y_N v^2$$

Minkowski; Gellman, Ramon, Slansky;  
Yanagida; Glashow; Mohapatra, Senjanovic

Scalar triplet:  
(type-II seesaw)

$$\Delta \equiv (\Delta^{++}, \Delta^+, \Delta^0)$$

$$\mathcal{L} \ni -Y_\Delta \Delta L_i L_j - \mu_\Delta \Delta H H + h.c.$$



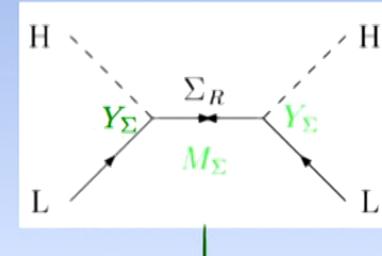
$$m_\nu = Y_\Delta^T \frac{\mu_\Delta}{M_\Delta^2} v^2$$

Magg, Wetterich; Lazarides, Shafi;  
Mohapatra, Senjanovic; Schechter, Valle

Fermion triplets:  
(type-III seesaw)

$$\Sigma_i \equiv (\Sigma_i^+, \Sigma_i^0, \Sigma_i^-)$$

$$\mathcal{L} \ni -Y_{\Sigma_i j} \bar{\Sigma}_i L_j H - \frac{m_{\Sigma_i}}{2} \bar{\Sigma}_i^c \Sigma_i + h.c.$$



$$m_\nu = Y_\Sigma^T \frac{1}{M_\Sigma} Y_\Sigma v^2$$

Foot, Lew, He, Joshi; Ma; Ma, Roy; T.H., Lin, Notari,  
Papucci, Strumia; Bajc, Nemevsek,  
Senjanovic; Dorsner, Fileviez-Perez;....

for example with  $Y_N \sim 1$ ,  $m_\nu \sim 0.1$  eV requires  $M_N \sim 10^{15}$  GeV  
with  $Y_N \sim 10^{-6}$ ,  $m_\nu \sim 0.1$  eV requires  $M_N \sim$  TeV

# The 3 leptogenesis ingredients

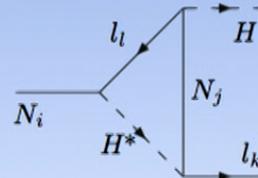
first in type-I

- I) The CP-asymmetry (averaged  $\Delta L$  produced per  $N_i$  decay)

$$\epsilon_{N_i} = \sum_k \frac{\Gamma(N_i \rightarrow L_k H) - \Gamma(N_i \rightarrow \bar{L}_k H^*)}{\Gamma_{N_i}^{\text{TOT}}}$$

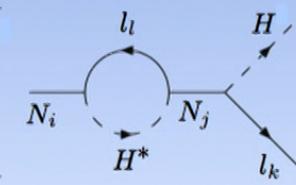
⇒ CP-violation from 2 one-loop diagrams:

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vertex diagram

Fukugida, Yanagida '86



self-energy diagram

Liu, Segré '93; Flanz et al '94;  
Covi, Roulet, Vissani '94, Pilaftsis '97

$$\Rightarrow \epsilon_{N_i} = \frac{1}{8\pi} \sum_j \frac{\sum_{jl} \text{Im}[Y_{Nik} Y_{Nkj}^\dagger Y_{Nil} Y_{Nlj}^\dagger] M_{Nj}}{\sum_k |Y_{Nik}|^2} \frac{M_{Nj}}{M_{Ni}} \cdot \left[ 1 - \left( 1 + \frac{M_{Nj}^2}{M_{Ni}^2} \right) \log \left( 1 + \frac{M_{Ni}^2}{M_{Nj}^2} \right) + \frac{M_{Ni}^2 (M_{Ni}^2 - M_{Nj}^2)}{(M_{Ni}^2 - M_{Nj}^2)^2 + \Gamma_{Nj}^2 M_{Ni}^2} \right]$$

$$\Rightarrow Y_L \equiv \frac{n_L}{s} = \epsilon_{N_i} \cdot \frac{n_{N_i}}{s} \Big|_{T >> M_{N_i}}$$

# The 3 leptogenesis ingredients

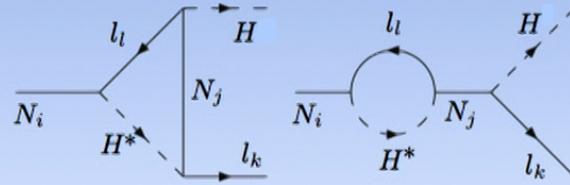
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## The 3 leptogenesis ingredients

- 2) The efficiency  $\eta$ :  $\frac{n_L}{s} = \varepsilon_{N_i} \cdot \frac{n_{N_i}}{s} \Big|_{T >> M_{N_i}} \cdot \eta$ 
  - $\eta \sim 1 \leftarrow$  out-of-equilibrium
  - $\eta \ll 1 \leftarrow$  N decays partly in thermal equil. and/or washout of L asym.

can be obtained integrating the Boltzmann equations:

$$\begin{aligned} \frac{s}{z} \frac{dY_N}{dz} &= \left(1 - \frac{Y_N}{Y_N^{EQ}}\right) \cdot \frac{\gamma_D}{H(T = M_N)} \\ \frac{s}{z} \frac{dY_{\bar{l}}}{dz} &= \varepsilon_N \cdot \left(\frac{Y_N}{Y_N^{EQ}} - 1\right) \cdot \frac{\gamma_D}{H(T = M_N)} - 2 \frac{Y_L}{Y_l^{EQ}} \cdot \frac{\gamma_{\Delta L=2}}{H(T = M_N)} \end{aligned}$$

$$\begin{aligned} Y_N &= n_N/s \\ Y_L &= (n_l - n_{\bar{l}})/s \\ z &\equiv \frac{M_N}{T} \\ \frac{\gamma_D}{H(T = M_N)} &\equiv \frac{\Gamma_N^{\text{TOT}}}{H(T = M_N)} \frac{K_1(z)}{K_2(z)} n_N^{EQ}(z) \end{aligned}$$

each decay produces a  $\Delta L = \varepsilon_N$

each inverse decay produces a  $\Delta L = -\varepsilon_N$

if more  $l$  than  $\bar{l}$ : more  $l H \rightarrow N \rightarrow \bar{l} H^*$  processes than  $\bar{l} H^* \rightarrow N \rightarrow l H$

⇒ main condition to avoid an efficiency suppression:  $\underline{\Gamma_N^{\text{TOT}} < H(T = M_N)}$

## The 3 leptogenesis ingredients

- 3) The L to B conversion from SM sphalerons:

→ above the EW scale B+L violating but B-L conserving

SM sphalerons are in thermal equilibrium

$$T_{Decoupl.}^{Sphal.} \sim 140 \text{ GeV}$$

⇒ put B+L to  $\sim 0$  but conserving B-L:

$$\left. \begin{array}{lcl} (B+L)_{Fin} & \sim & 0 \\ (B-L)_{Fin} & = & (B-L)_{In} \\ B_{In} & = & 0 \end{array} \right\} \Rightarrow B_{Fin} \sim -L_{Fin} \sim -\frac{L_{In}}{2}$$



$$\frac{n_B}{s} = -\frac{28}{79} \frac{n_L}{s} = -\frac{28}{79} \eta \epsilon_{N_i} \frac{n_{N_i}}{s} \Big|_{T>>M_{N_i}}$$



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$$\frac{n_B}{s} = (8.82 \pm 0.23) \cdot 10^{-11}$$

WMAP  
Planck

## High scale leptogenesis (briefly)

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$$\hookrightarrow m_N \gg v_{EW}$$

## Two intriguing numerical coincidences

- The seesaw state mass (slight) coincidence:

- for a hierarchical spectrum of  $N_i$ :  $\varepsilon_{N_1} \leq M_{N_1} \frac{3}{8\pi} \frac{1}{v^2} \sqrt{\Delta m_{atm}^2}$

$$M_{N_1} \ll M_{N_{2,3}}$$



.... Davidson, Ibarra '02, ....

$$M_{N_1} \gtrsim 4 \cdot 10^8 \text{ GeV}$$



this scale is determined by the totally independent value  
of  $n_B/s$ , fits well with seesaw expectations

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a much larger value of  $n_B/s$  and/or much  
smaller neutrino mass scale would fit much less

## Two intriguing numerical coincidences

- The neutrino mass scale value versus electroweak and Planck scales coincidence

in full generality:  $\Gamma_{N_1}/H(T = M_{N_1}) \geq m_\nu^{\text{Min}}/10^{-3} \text{ eV}$

$$\downarrow \quad \downarrow \quad \downarrow$$
$$\propto |Y_{N_{1i}}|^2 M_{N1} \quad \propto M_{N1}^2 \quad \propto \frac{Y_{N_{1i}}^2}{M_{N1}}$$

..., Buchmuller, Di Bari, Plumacher, 96-2003, ...

given the  $m_\nu^{\text{Min}} < 2.2 \text{ eV}$  direct bound or the  $m_\nu^{\text{Min}} \lesssim 0.2 \text{ eV}$  cosmology bound

the washout from inverse decays is naturally limited

$\Gamma_{N_1}/H(T = M_{N_1}) \leq 1$   
is not much violated

I real coincidence because  $10^{-3} \text{ eV}$  scale is determined by  
independent e-w scale and Planck scale

$$10^{-3} \text{ eV} \simeq 17 \cdot 8\pi \cdot v^2/M_{\text{Planck}}$$

for example  $m_\nu \sim \text{KeV}$  would have given quite large washout

## Flavor effects in leptogenesis

so far all results were obtained by just counting the number of lepton created and destroyed independently of whether the lepton is of  $e$ ,  $\mu$  or  $\tau$  type  
a single Boltzmann equation for total lepton number

justified for  $T \gtrsim 10^{12}$  GeV:  $e^-$ ,  $\mu^-$ ,  $\tau^-$  indistinguishable in the thermal bath

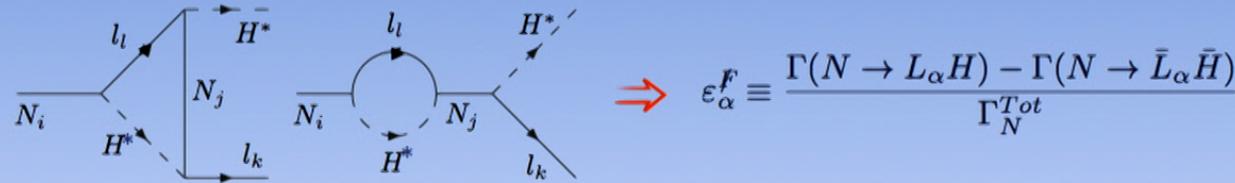
 same gauge interactions       SM charged Yukawa interactions out of equil.

→ the  $N_1$  which couples to a single  $\tilde{l} \propto Y_{N_1e} e + Y_{N_1\mu} \mu + Y_{N_1\tau} \tau$  flavour combination creates leptons in this combination which remains coherent afterwards

→ one has just to count the number of  $\tilde{l}$  created and destroyed → a single Boltzmann equation!

## Flavor Leptogenesis: new flavor breaking L conserving CP asymmetries

↳ L conserving (pure flavor) asymmetries



gives no contribution in one-flavor approx:  $\sum_k \varepsilon_{N_k}^F = 0$

but has in reality a non-zero contribution: if  $\varepsilon_{\tau}^F = -\varepsilon_{e+\mu}^F \neq 0$

I

can be not  
washed out      can be largely  
washed out      ↳ a net L asym.  
remains

↳ generically subleading because suppressed by a  $\frac{m_{N_1}^2}{m_{N_{2,3}}^2}$  factor

except in setups with approximate lepton number violation where it can give the dominant contribution and lead to successful leptogenesis

↳ "Purely flavored leptogenesis"

(not so easy to cook in type-I but possible)

Aristizabal Sierra, Losada, Nardi '08  
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Gonzalez-Garcia, Racker, Rius '09

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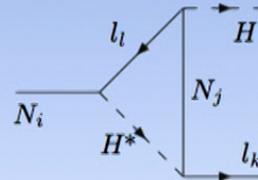
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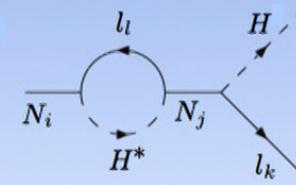
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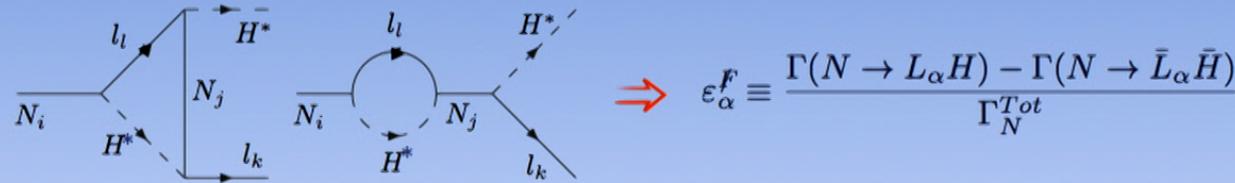
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## Low scale leptogenesis

$$\hookrightarrow m_N \gtrsim v_{EW}$$

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## Going below the high scale lower bound on $m_N$

below  $m_N > 4 \cdot 10^8 \text{ GeV} ???$

- ↪ in order to be able to produce the  $N$   $T_{reh.} \lesssim 10^{8-9} \text{ GeV}$
- ↪ not to be in tension with gravitino upper bound on reheating  $T$
- ↪ in order not to be in tension with naturalness

$$\delta m_h^2 \simeq \frac{1}{2\pi} \frac{m_\nu m_N^3}{v^2} \quad \Rightarrow \quad m_N < 3 \cdot 10^7 \text{ GeV} \cdot \left( \frac{v}{246 \text{ GeV}} \right)^{2/3}$$

$\delta m_H^2 < 1 \text{ TeV}^2$

⇒ to lift up the naturalness problem:

- regularize the radiative corrections: Susy, .... but gravitino problem
- to reduce the effective electroweak vev entering neutrino masses
- to consider a quasi-degenerate  $m_N$  spectrum

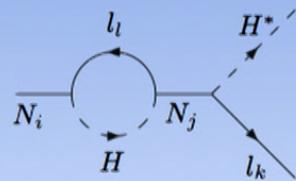
## Going to lower $m_N$ : resonance from quasi-degenerate spectrum

Covi, Roulet, Vissani '96'  
Flanz, Paschos, Sarkar '96'

for a quasi-degenerate spectrum of  $N_i$  instead: resonance occurs:

$$M_{N_1} \sim M_{N_2}$$

$$\varepsilon_{CP} = \frac{\text{Im}[(Y_N Y_N^\dagger)_{12}^2]}{(Y_N Y_N^\dagger)_{11}(Y_N Y_N^\dagger)_{22}} \cdot \frac{2 \Delta m_N \Gamma_N}{4(\Delta m_N)^2 + \Gamma_N^2}$$



- ↪  $\varepsilon_{N_1}$  not bounded by value of  $M_{N_1}$  or  $m_\nu$
- ↪  $M_{N_1}$  bounded from below only by sphaleron decoupling scale and  $m_h$
- ↪  $M_{N_1} \sim \text{TeV}$  perfectly possible

Pilaftsis '97; '99; Pilaftsis, Underwood '05; ...;  
Dev, Millington, Pilaftsis, Teresi '14

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a precise treatment of the resonant case requires inclusion of a series of extra effects, in particular quantum Boltzmann equations

takes into account memory effects, off-shell effects, finite density effects, flavor oscillations, decoherence

Buchmüller, Fredenhagen '00  
De Simone, Riotto '07  
Cirigliano, Isidori, Masina, Riotto, '08  
Anisimov, Buchmüller, Drewes, Mendizabal '08  
Garny, Hohenegger, Kartavtsev, Lindner '09  
Garny, Hohenegger, Kartavtsev, '11  
Garbrecht, Herranen '11  
Cirigliano, Lee, Ramsey-Musolf, Tulin '13,  
Bhupal Dev, Millington, Pilaftsis, Teresi '14, '15

.....

also relevant for weak washout regime  $\left. \frac{\Gamma_N}{H} \right|_{T=M_N} \ll 1$

## Testing low scale leptogenesis at colliders?

by producing low scale seesaw states at colliders?

- type-I: very difficult:

Yukawa couplings are expected far too small to allow  $N$  production

$$Y_N \sim 10^{-6} \text{ for } M_N \sim 1 \text{ TeV}$$

in special cases larger  $Y_N$  are allowed,

Dev, Millington, Pilaftsis, Teresi '14

allowing  $N$  production + observable charged lepton flavor violation

$$\mu \rightarrow e\gamma$$

$$\mu \rightarrow eee$$

$$R_{\mu \rightarrow e}^{Al}, \dots$$

production mechanisms other than Yukawa

- type-II and type-III: Drell-Yan pair production mechanisms

problem: production interactions tend to thermalize the seesaw state  $\rightarrow$  leptogenesis suppressions!

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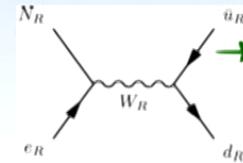
$\hookrightarrow$  SM gauge interact, for type-II and III:  $m_{\Delta, \Sigma} > 1.6 \text{ TeV}$

too large for LHC

$\hookrightarrow$   $N$  production via  $Z'$ : similar bounds as for type-II/III

see Plumacher et al,  
Frère et al, Babu et al  
Fileviez-Perez et al, ...

$\hookrightarrow$   $N$  production via  $W_R$ : much more dramatic thermalization effect!



involves only one heavy external state instead of two

$\Rightarrow$  only one Boltzm. suppression power instead of 2  
scattering is never slower than the decay  $\Rightarrow m_{W_R} \gtrsim 18 \text{ TeV}$

Frère, TH,  
Vertongen '07

Dev, Lee, Mohapatra '14, '15

$\hookrightarrow$  L-violating signal observation at LHC would lead to lower bound on washout

## Very low scale leptogenesis

$$\hookrightarrow m_N \sim \text{GeV} < v_{EW}$$

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## Leptogenesis from L-violating decay: relevant scales for low $m_N$

$$T_{Sphaler.} \sim 135 \text{ GeV}$$

very low scale leptogenesis:  $T_{Sphaler.} > m_H >> m_{N,L}$

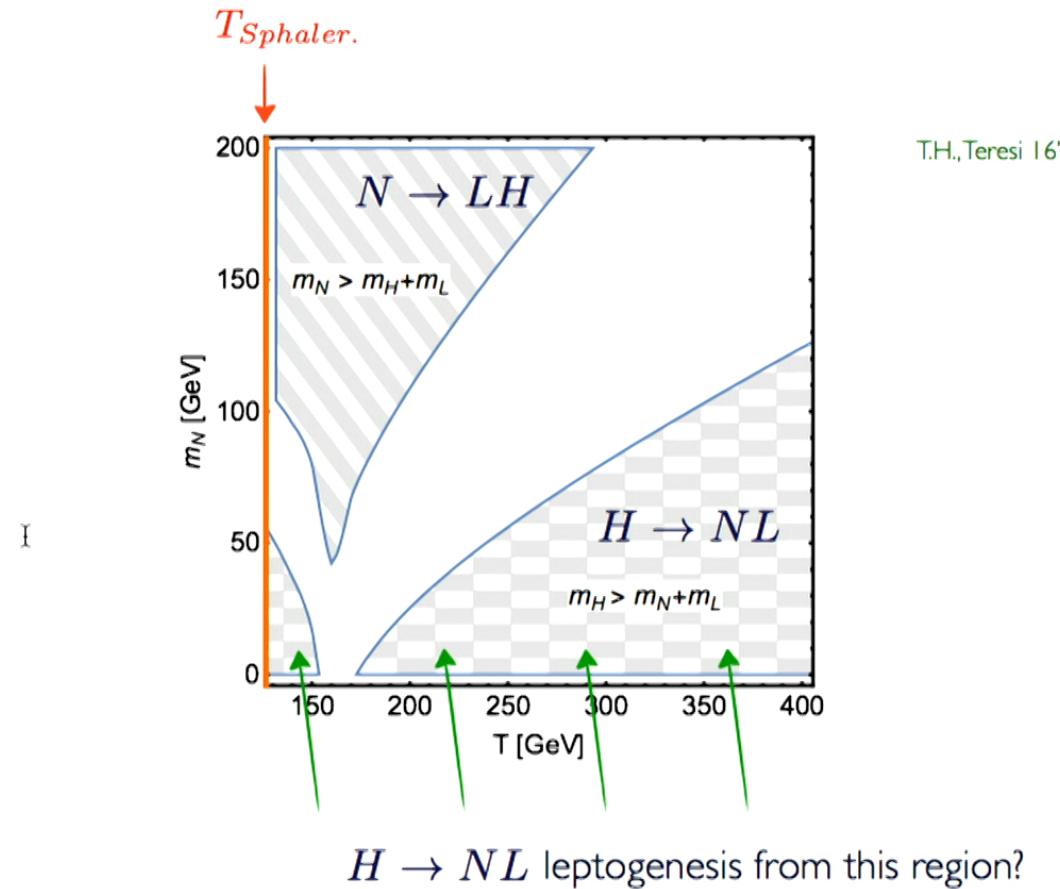
↳ creation of L asymmetry at  $T > T_{Sphaler.} >> m_N \Rightarrow \neq$  regime

↳ thermal effects are fully relevant:  $T > T_{Sphaler.} > m_H >> m_{N,L}$

$$m_H^2(T) = m_H^2 + c_H \cdot T^2 \quad m_L^2(T) = m_L^2 + c_L \cdot T^2 \quad m_N^2(T) = m_N^2 + c_N \cdot T^2$$

I ↳  $N \rightarrow LH$  forbidden but  $H \rightarrow NL$  allowed

## Temperatures allowing the $N \rightarrow LH$ and $H \rightarrow NL$ decays



## L asymmetry production from $H \rightarrow NL$ decay

T.H., Teresi 16'



2 issues at first sight:

I) out-of-equilibrium decay?      ← 3rd Sakharov condition

↪  $H$  decaying particle is in deep thermal equilibrium at  $T > T_{Sphaleron}$ .

but  $N$  in decay product is not necessarily in thermal equilibr.

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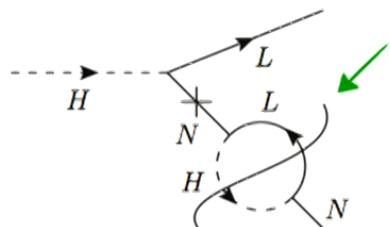
$$\frac{dn_N}{dt} \propto (n_N^{eq} - n_N) \cdot \Gamma_{H \rightarrow NL}$$

$\uparrow$        $\uparrow$   
 $H \rightarrow NL$      $NL \rightarrow H$

## L asymmetry production from $H \rightarrow NL$ decay

2) Absorptive part for CP violation?

T.H., Teresi 16'



$m_H + m_L > m_N \Rightarrow$  no absorptive part?

but only for  $T = 0$ !

finite T corrections: thermal cut: if  $H$  or  $L$  comes from the thermal bath the cut is kinematically allowed

Giudice, Notari, Raidal, Riotto, Strumia 03'

Frossard, Garny, Hohenegger, Kartavtsev, Mitrouskas 12'

$\Rightarrow$  absorptive part  $\Gamma_N(T)$  (calculated in Kadanoff Baym formalism)

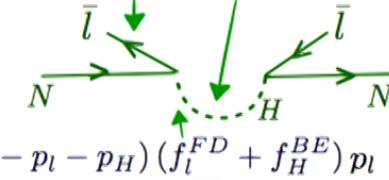
Frossard, Garny, Hohenegger, Kartavtsev, Mitrouskas 12'

$$\Pi^{\alpha\beta}(q_N) = \underbrace{\Pi_{>}^{\alpha\beta}(q_N)} + \underbrace{\Pi_{<}^{\alpha\beta}(q_N)}$$

$$\hookrightarrow -2 \int \frac{d^4 p_l}{(2\pi)^4} \frac{d^4 p_H}{(2\pi)^4} (2\pi)^4 \delta^4(q_N - p_l - p_H) (Y_N^\dagger Y_N)_{\alpha\beta} [ \underbrace{P_L S_{>}^l(t, p_l)}_{\propto f_{\bar{l}}^{FD}} \underbrace{P_R \Delta_{>}^H(t, p_H)}_{\propto 1 + f_H^{BE}} ]$$

$$\Rightarrow \Gamma_N(T) = \frac{1}{8\pi} m_{N_2} (Y_N Y_N^\dagger)_{22} \cdot \frac{p \cdot L_N}{q_N \cdot p_l}$$

$$\hookrightarrow L_N = 16\pi \int \frac{d^3 p_l}{(2\pi)^3 2E_l} \frac{d^3 p_H}{(2\pi)^3 2E_H} (2\pi)^4 \delta^4(q_N - p_l - p_H) (\underbrace{f_{\bar{l}}^{FD} + f_H^{BE}}_{\propto 1 + f_{\bar{l}}^{FD}}) p_l$$



## Total $L$ number violating $CP$ asymmetry

$$\varepsilon_{CP} = \frac{\text{Im}[(Y_N Y_N^\dagger)_{12}^2]}{(Y_N Y_N^\dagger)_{11}(Y_N Y_N^\dagger)_{22}} \cdot \frac{2 \Delta m_N^0 \Gamma_N(T)}{4 \Delta m_N(T)^2 + \Gamma_N(T)^2}$$

with thermal mass splitting:  $\Delta m_N(T) \simeq \Delta m_N^0 + \frac{\pi T^2}{4 m_N^2} \Gamma_{22} \sqrt{\left(1 - \frac{\Gamma_{11}}{\Gamma_{22}}\right)^2 + 4 \frac{|\Gamma_{12}|^2}{\Gamma_{22}^2}}$

$$\Gamma_{ij} \equiv m_N (Y_N Y_N^\dagger)_{ij} / (8\pi)$$

Boltzmann equations:

I

$$\frac{n_\gamma H_N}{z} \frac{d\eta_N}{dz} = \left(1 - \frac{\eta^N}{\eta_N^{\text{eq}}}\right) \left[ \gamma_D + 2(\gamma_{Hs} + \gamma_{As}) + 4(\gamma_{Ht} + \gamma_{At}) \right],$$

$$\begin{aligned} \frac{n_\gamma H_N}{z} \frac{d\eta_L}{dz} &= \gamma_D \left[ \left( \frac{\eta^N}{\eta_N^{\text{eq}}} - 1 \right) \epsilon_{CP}(z) - \frac{2}{3} \eta_L \right] \\ &\quad - \frac{4}{3} \eta_L \left[ 2(\gamma_{Ht} + \gamma_{At}) + \frac{\eta^N}{\eta_N^{\text{eq}}} (\gamma_{Hs} + \gamma_{As}) \right] \end{aligned}$$

$$\eta_N \equiv n_N / n_\gamma$$

$$z \equiv m_N / T$$

## Total $L$ number violating $CP$ asymmetry

$$\varepsilon_{CP} = \frac{\text{Im}[(Y_N Y_N^\dagger)_{12}^2]}{(Y_N Y_N^\dagger)_{11}(Y_N Y_N^\dagger)_{22}} \cdot \frac{2 \Delta m_N^0 \Gamma_N(T)}{4 \Delta m_N(T)^2 + \Gamma_N(T)^2}$$

with thermal mass splitting:  $\Delta m_N(T) \simeq \Delta m_N^0 + \frac{\pi T^2}{4 m_N^2} \Gamma_{22} \sqrt{\left(1 - \frac{\Gamma_{11}}{\Gamma_{22}}\right)^2 + 4 \frac{|\Gamma_{12}|^2}{\Gamma_{22}^2}}$

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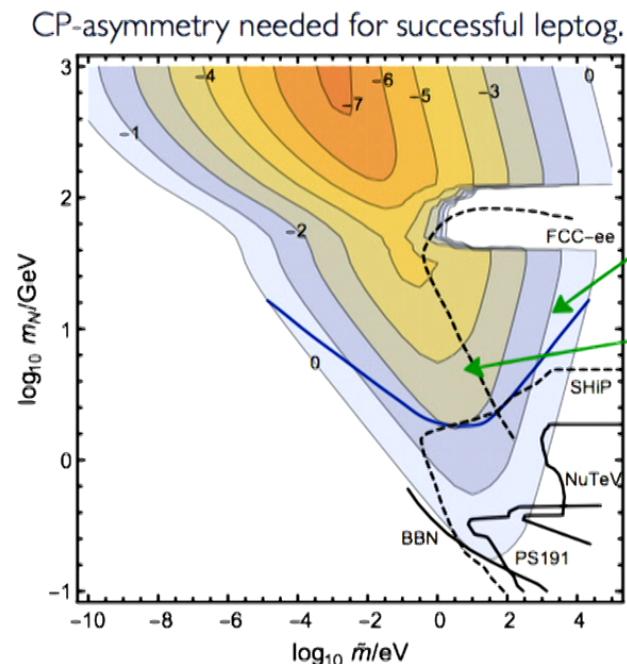
$$\begin{aligned} \frac{n_\gamma H_N}{z} \frac{d\eta_L}{dz} &= \gamma_D \left[ \left( \frac{\eta^N}{\eta_N^{\text{eq}}} - 1 \right) \epsilon_{CP}(z) - \frac{2}{3} \eta_L \right] \\ &\quad - \frac{4}{3} \eta_L \left[ 2(\gamma_{Ht} + \gamma_{At}) + \frac{\eta^N}{\eta_N^{\text{eq}}} (\gamma_{Hs} + \gamma_{As}) \right] \end{aligned}$$

$$\eta_N \equiv n_N/n_\gamma$$

$$z \equiv m_N/T$$

## Results for the case where the $N$ have thermalized

if  $N$  thermalized by large  $Y_N$  Yukawas or other interaction (e.g. a  $W_R$ ) before an asymmetry is produced



$$\tilde{m} \equiv \frac{Y_N Y_N^\dagger v^2}{2m_N}$$

requires that at least 2 of the  $N$  have quasi-degenerate masses

T.H., Teresi 16'

the lower is  $m_N$ , the later it goes out-of-equilibrium, the more it will be in equilibr. at  $T > T_{Sphaler}$ .



lower bound on  $m_N$   
 $m_N > 2.2 \text{ GeV}$

if only  $N \rightarrow LH$  decay we get:  $m_N > 50 \text{ GeV}$

## Results for the case where the $N$ have not thermalized

- if no extra interaction thermalizing  $N$ , no thermalization is much more natural than in ordinary leptogenesis: thermalization at  $T > T_{Sphaler.} \gg m_N$  requires much larger  $Y_N$  Yukawas than in ordinary leptogenesis at  $T \sim m_N$

$$\tilde{m} \equiv \frac{Y_N Y_N^\dagger v^2}{2m_N}$$

$$\tilde{m} \gg 10^{-3} \text{ eV}$$

$$\tilde{m} \gtrsim 10^{-3} \text{ eV}$$

- for  $H \rightarrow NL$  decay, to start from no  $N$  in the thermal bath boosts the asymmetry production, unlike for ordinary  $N \rightarrow LH$  leptogenesis

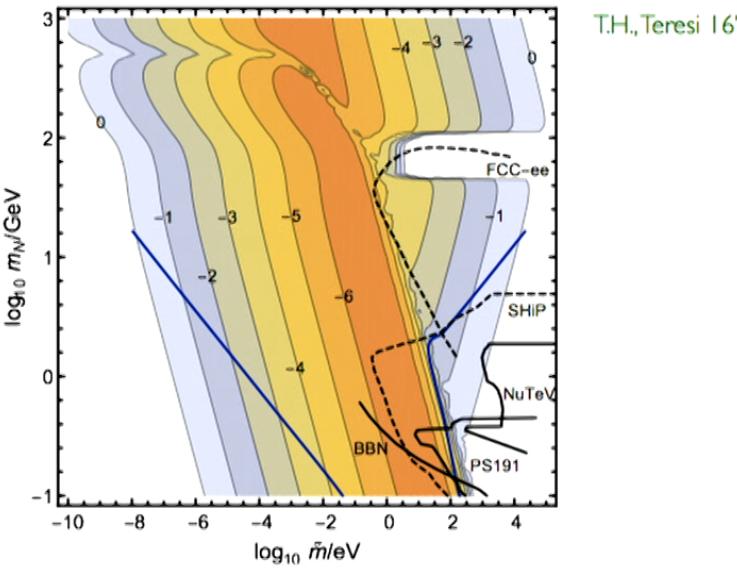
  $H \rightarrow NL$ : many  $H$  to decay and produce the asymmetry but few

$N$  to  $NL \rightarrow H$  inverse decay

$$n_N^{eq} - n_N \sim n_N^{eq} \gg n_N$$

## Results for the case where the $N$ have not thermalized

I

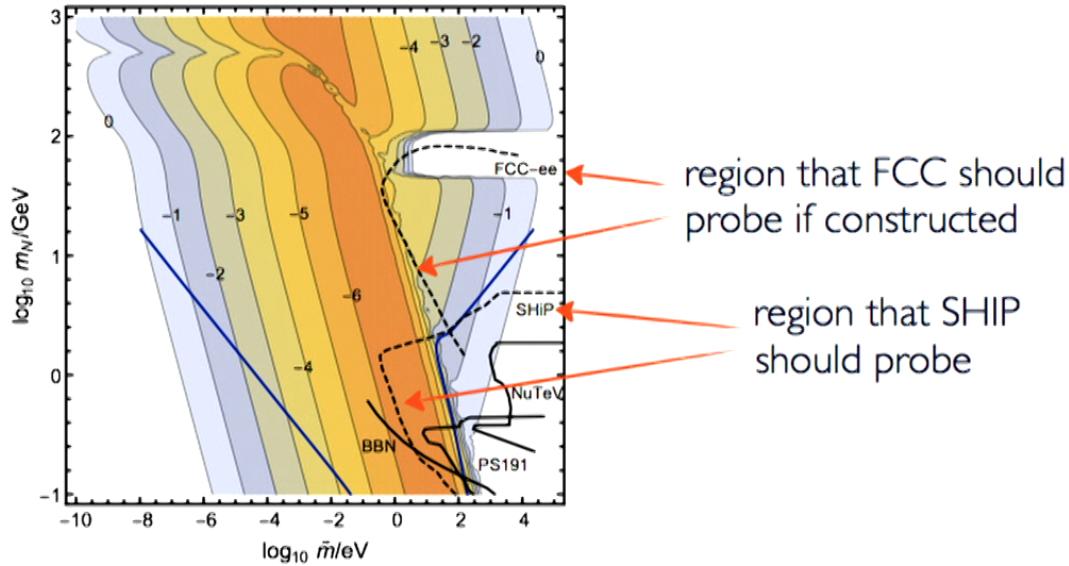


- ↪ for example for  $m_N \sim 10 \text{ GeV}$  and  $\tilde{m} \sim 0.1 \text{ eV}$  one needs  $\Delta m_N^0/m_N \lesssim 10^{-5}$
- ↪ leptogenesis for  $m_N$  as low as  $\sim 20 \text{ MeV}$  is possible (but BBN concerns)
- ↪ in all cases: asymmetry production at  $T$  just above  $T_{Sphaler}$ .  $\Rightarrow$  no dependence on UV physics!

## Testability!

T.H., Teresi 16'

I



## *Two important comparisons to do*

- for  $m_N \sim \text{GeV}$  : well-known baryogenesis mechanism in seesaw model:  
baryogenesis from right-handed neutrino oscillations: ``ARS'' mechanism

Akhmedov, Rubakov, Smirnov 98'  
Asaka, Shaposhnikov 05'; Shaposhnikov 08'  
Drewes, Garbrecht 11'  
Canetti, Drewes, Frossard, Shaposhnikov 13'  
Hernandez, Kekic, Lopez-Pavon, Racker, Rius 15'  
.....

 comparison of ARS with L-violating Higgs decay setup???

- to compute evolution of asymmetries with thermal effects: another  
<sup>I</sup> well-known formalism: density matrix formalism

 comparison of results in decay formalism above and in density  
density matrix formalism???

## Density matrix formalism

$N_{R_\alpha}$  quantum system is described by density matrix :  $n_{\alpha\beta}^N \equiv \langle a_\beta^{+\dagger} a_\alpha^+ \rangle = \text{Tr}(\rho a_\beta^{+\dagger} a_\alpha^+)$

$\overline{N_{R_\alpha}}$  quantum system is described by density matrix :  $n_{\alpha\beta}^{\bar{N}} \equiv \langle a_\beta^{-\dagger} a_\alpha^- \rangle = \text{Tr}(\rho a_\beta^{-\dagger} a_\alpha^-)$

$n_{\alpha\alpha}^N = n_\alpha^N =$  number density of  $N_\alpha$  states

$n_{\alpha\beta}^N =$  coherence between  $N_\alpha$  and  $N_\beta$  states

→ evolution of density matrix:

$$\frac{d}{dt} n_{q\beta}^N(\mathbf{k}, t) = i \langle [H_0^N, n_{\alpha\beta}^N(\mathbf{k}, t)] \rangle - \frac{1}{2} \int_{-\infty}^{\infty} dt' \langle [H_{\text{int}}(t'), [H_{\text{int}}(t), n_{\alpha\beta}^N(\mathbf{k}, t)]] \rangle_t$$

oscillation term    interaction term

$$H_{\text{int}} = h_{l\alpha} \bar{L}_l \tilde{H} P_R N_\alpha + \text{h.c.}$$

↙  $H_{\text{int}} \cdot H_{\text{int}}$  ↘ terms in  $a_\beta^{+\dagger} a_\alpha^+ \rightarrow n_{\alpha\beta}^N$   
      ↙ terms in  $a_\alpha^- a_\beta^{-\dagger} \rightarrow 1 - n_{\alpha\beta}^N$

## Density matrix formalism

$$\Rightarrow \frac{d}{dt} n_{\alpha\beta}^N(\mathbf{k}) = -i [E_N, n^N(\mathbf{k})]_{\alpha\beta} - \frac{1}{2E_N} \left( \frac{1}{2} \{\Gamma^>(\mathbf{k}), n^N(\mathbf{k})\} - \frac{1}{2} \{\Gamma^<(\mathbf{k}), I - n^N(\mathbf{k})\} \right)_{\alpha\beta},$$

$N + \bar{L} \rightarrow H$        $H \rightarrow N + \bar{L}$

with:

$$\Gamma_{\alpha\beta}^{\leq}(\mathbf{k}) = -i \text{tr} \{ P_R u_+(\mathbf{k}) \bar{u}_+(\mathbf{k}) P_L \Sigma_{\alpha\beta}^{\leq}(k) \}$$

↑  
keeping only the transitions where there is no  $m_N$  mass  
insertions because the asymmetry is produced at  $T \gg T_{\text{sphaler}} \gg m_N$

ARS scenario

if mass insertion:  $m_N^2/T^2$  suppression

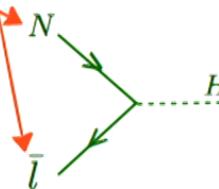
with:

$$-i \Sigma_{\alpha\beta}^{\leq}(k) = \int \frac{d^4 p}{(2\pi)^4} \int \frac{d^4 q}{(2\pi)^4} (2\pi)^4 \delta^{(4)}(q - k - p) i S_l^{\leq}(-p) i \Delta^{\geq}(-q) h_{l\alpha}^* h_{l\beta}$$

Wightman propagator of  $L$       Wightman propagator of  $H$

for example:

$$n_N \Gamma^> \sim n_N \Sigma^> \propto n_N \cdot S_l^> \cdot \Delta^< \cdot h_{l\alpha}^* h_{l\beta} \propto n_N \cdot n_{\bar{l}} \cdot (1 + n_H) \cdot h_{l\alpha}^* h_{l\beta}$$



## Density matrix formalism

$$\Rightarrow \frac{d}{dt} n_{\alpha\beta}^N(\mathbf{k}) = -i [E_N, n^N(\mathbf{k})]_{\alpha\beta} - \frac{1}{2E_N} \left( \frac{1}{2} \{\Gamma^>(\mathbf{k}), n^N(\mathbf{k})\} - \frac{1}{2} \{\Gamma^<(\mathbf{k}), I - n^N(\mathbf{k})\} \right)_{\alpha\beta},$$

$N + \bar{L} \rightarrow H$        $H \rightarrow N + \bar{L}$

with:

$$\Gamma_{\alpha\beta}^{\leq}(\mathbf{k}) = -i \text{tr} \{ P_R u_+(\mathbf{k}) \bar{u}_+(\mathbf{k}) P_L \Sigma_{\alpha\beta}^{\leq}(k) \}$$

↑  
keeping only the transitions where there is no  $m_N$  mass  
insertions because the asymmetry is produced at  $T \gg T_{\text{sphaler}} \gg m_N$   
if mass insertion:  $m_N^2/T^2$  suppression

ARS scenario

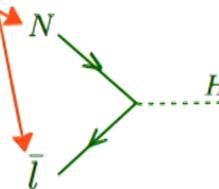
with:

$$-i \Sigma_{\alpha\beta}^{\leq}(k) = \int \frac{d^4 p}{(2\pi)^4} \int \frac{d^4 q}{(2\pi)^4} (2\pi)^4 \delta^{(4)}(q - k - p) i S_l^{\leq}(-p) i \Delta^{\geq}(-q) h_{l\alpha}^* h_{l\beta}$$

↑ Wightman propagator of  $L$  ↑  
↑ Wightman propagator of  $H$  ↑

for example:

$$n_N \Gamma^> \sim n_N \Sigma^> \propto n_N \cdot S_l^> \cdot \Delta^< \cdot h_{l\alpha}^* h_{l\beta} \propto n_N \cdot n_{\bar{l}} \cdot (1 + n_H) \cdot h_{l\alpha}^* h_{l\beta}$$



## Density matrix formalism: final evolution equations for $N$ and $\bar{N}$

with no Majorana mass insertion  
= ARS scenario

writing  $n_l = n_l^{Eq} + \frac{\delta n_l}{2}$   
 $n_{\bar{l}} = n_l^{Eq} - \frac{\delta n_l}{2}$  a term proportional to  $\delta n_l$  shows up: washout term:  $W$

$$\frac{dn_{\alpha\beta}^N}{dt} = -i [\mathcal{E}_N, n^N(k)]_{\alpha\beta} - \frac{1}{2} \left\{ \gamma^{LC}, \frac{n^N}{n_{eq}^N} - I \right\}_{\alpha\beta} + \frac{\delta n_l^L}{2n_{eq}^L} \left( (\gamma_{WQ,l}^{LC}) + \frac{1}{2} \left\{ \gamma_{WC,l}^{LC}, \frac{n^N}{n_{eq}^N} \right\} \right)_{\alpha\beta}$$

$$\begin{aligned} \gamma_{\alpha\beta}^{LC} &\equiv \int d\Pi_{PS} n_{eq}^N(\mathbf{k}) (n_{eq}^L(\mathbf{p}) + n_{eq}^H(\mathbf{q})) \times \text{tr} \{ P_R u_+(\mathbf{k}) \bar{u}_+(\mathbf{k}) P_L \not{p} \} h_{l\alpha}^* h_{l\beta} \\ &\pm \frac{g_{iso}}{4\pi^2} \int_0^\infty dk \frac{k}{e^{k/T} + 1} \frac{M_H^2 - M_L^2}{8\pi k} \times \int_{E^*}^\infty dE \left( \frac{1}{e^{\frac{E}{T}} + 1} + \frac{1}{e^{\frac{E+k}{T}} - 1} \right) h_{l\alpha}^* h_{l\beta} \\ &\simeq 3.26 \times 10^{-4} T^4 h_{l\alpha}^* h_{l\beta} \end{aligned}$$

$$\gamma_{WQ}^{LC} = \frac{g_{iso}}{4\pi^2} \int_0^\infty dk k \frac{M_H^2 - M_L^2}{8\pi k} \times \int_{E^*}^\infty dE \frac{1}{e^{\frac{E}{T}} + 1} \frac{1}{e^{\frac{E+k}{T}} - 1} h_{l\alpha}^* h_{l\beta} \simeq 1.05 \times 10^{-4} T^4 h_{l\alpha}^* h_{l\beta}$$

$$\gamma_{WC}^{LC} = \frac{g_{iso}}{4\pi^2} \int_0^\infty dk \frac{k}{e^{k/T} + 1} \frac{M_H^2 - M_L^2}{8\pi k} \int_{E^*}^\infty dE \frac{1}{e^{\frac{E}{T}} + 1} h_{l\alpha}^* h_{l\beta} \simeq 1.86 \times 10^{-4} T^4 h_{l\alpha}^* h_{l\beta}$$

and similarly for  $\bar{N}$

## Density matrix formalism: final evolution equation for $\delta n_l$

with no Majorana mass insertion

= ARS scenario

$$\frac{d\delta n_l^L}{dt} = \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC}) n^N\} - \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC*}) \bar{n}^N\} \\ - \frac{\delta n_l^L}{n_{eq}^L} \text{tr}\{\gamma_{WQ,l}^{LC}\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{n^N (\gamma_{WC,l}^{LC})\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{\bar{n}^N (\gamma_{WC,l}^{LC*})\}$$

for not too large Yukawa coupling these equations can be analytically solved order by order in the Yukawa couplings

→ at  $\mathcal{O}(h^4)$ :

$$Y_l(z) \simeq 4(\kappa^{LC})^2 \rho_{eq} (h^\dagger h)_{11} (h^\dagger h)_{22} \delta_l^{LC} \int_0^z \text{Im} f(z') dz' \quad f(z) \equiv \int_0^z dz' e^{i \frac{\Delta m_N^2}{3\mu_{osc}^2} (z^3 - z'^3)} \\ \delta_l^{LC} = \frac{\text{Im}[h_{l1}^* h_{l2} (h^\dagger h)_{21}]}{(h^\dagger h)_{11} (h^\dagger h)_{22}}$$

CP-violating Yukawa combination which leaves the SM total lepton number unchanged:

$$\delta n_{l_i} \equiv n_{L_i} - n_{\bar{L}_i} \neq 0 \quad \text{but} \quad \sum_{i=e,\mu,\tau} \delta n_{l_i} = 0 \quad \Rightarrow \quad \sum_{i=e,\mu,\tau} Y_l = 0$$

→ no contribution at  $\mathcal{O}(h^4)$  !

## Density matrix formalism: final result with no Majorana mass insertion

$$Y_{LC} \simeq -18.5 \times (\alpha^{LC})^2 \alpha_W^{LC} \frac{M_0^{7/3}}{T_c(\Delta m_N^2)^{2/3}} \times (h^\dagger h)_{11} (h^\dagger h)_{22} \sum_l \delta_l^{LC} (h h^\dagger)_ll$$

 what happens is that since there is no  $m_N$  mass insertions in the processes nowhere, all processes conserve total lepton number: assigning  $L = 1$  to  $N_R$  and  $L = -1$  to  $\bar{N}_R$ , all processes conserve  $L$

$\Rightarrow$  at  $\mathcal{O}(h^4)$ : SM lepton number and  $N$  lepton number are separately conserved:

$$\sum_{i=e,\mu,\tau} (n_{L_i} - n_{\bar{L}_i}) = 0 \quad \sum_{\alpha} (n_{N_{\alpha}} - n_{\bar{N}_{\alpha}}) = 0$$

but flavour lepton number is not conserved:  $\delta n_{l_i} \equiv n_{L_i} - n_{\bar{L}_i} \neq 0$

$\Rightarrow$  at  $\mathcal{O}(h^6)$ : if Yukawa for electron much smaller than for muon:

$n_{L_\mu} - n_{\bar{L}_\mu}$  strongly washed-out

$n_{L_e} - n_{\bar{L}_e}$  much less washed-out

$$\Rightarrow \sum_{i=e,\mu,\tau} (n_{L_i} - n_{\bar{L}_i}) = - \sum_{\alpha} (n_{N_{\alpha}} - n_{\bar{N}_{\alpha}}) \neq 0$$

 converted to B asym by sphalerons

 not converted to B asym by sphalerons

$\Rightarrow$  baryon asymmetry!

## Density matrix formalism: final evolution equation for $\delta n_l$

with no Majorana mass insertion

= ARS scenario

$$\frac{d\delta n_l^L}{dt} = \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC}) n^N\} - \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC*}) \bar{n}^N\}$$

$$- \frac{\delta n_l^L}{n_{eq}^L} \text{tr}\{\gamma_{WQ,l}^{LC}\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{n^N (\gamma_{WC,l}^{LC})\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{\bar{n}^N (\gamma_{WC,l}^{LC*})\}$$

for not too large Yukawa coupling these equations can be analytically solved order by order in the Yukawa couplings

→ at  $\mathcal{O}(h^4)$ :

$$Y_l(z) \simeq 4(\kappa^{LC})^2 \rho_{eq} (h^\dagger h)_{11} (h^\dagger h)_{22} \delta_l^{LC} \int_0^z \text{Im} f(z') dz'$$

$$f(z) \equiv \int_0^z dz' e^{i \frac{\Delta m_N^2}{3\mu_{osc}^2} (z^3 - z'^3)}$$

$$\delta_l^{LC} = \frac{\text{Im}[h_{l1}^* h_{l2} (h^\dagger h)_{21}]}{(h^\dagger h)_{11} (h^\dagger h)_{22}}$$

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$$\delta n_{l_i} \equiv n_{L_i} - n_{\bar{L}_i} \neq 0 \quad \text{but} \quad \sum_{i=e,\mu,\tau} \delta n_{l_i} = 0 \quad \Rightarrow \quad \sum_{i=e,\mu,\tau} Y_l = 0$$

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$n_{L_e} - n_{\bar{L}_e}$  much less washed-out

$$\Rightarrow \sum_{i=e,\mu,\tau} (n_{L_i} - n_{\bar{L}_i}) = - \sum_{\alpha} (n_{N_{\alpha}} - n_{\bar{N}_{\alpha}}) \neq 0$$

converted to B asym  
by sphalerons

not converted to B asym  
by sphalerons

$\rightarrow$  baryon  
asymmetry!

## Density matrix formalism: final evolution equation for $\delta n_l$

with no Majorana mass insertion

= ARS scenario

$$\frac{d\delta n_l^L}{dt} = \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC}) n^N\} - \frac{1}{n_{eq}^N} \text{tr}\{(\gamma_l^{LC*}) \bar{n}^N\}$$

$$- \frac{\delta n_l^L}{n_{eq}^L} \text{tr}\{\gamma_{WQ,l}^{LC}\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{n^N (\gamma_{WC,l}^{LC})\} - \frac{\delta n_l^L}{2n_{eq}^L} \frac{1}{n_{eq}^N} \text{tr}\{\bar{n}^N (\gamma_{WC,l}^{LC*})\}$$

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$$\delta n_{l_i} \equiv n_{L_i} - n_{\bar{L}_i} \neq 0 \quad \text{but} \quad \sum_{i=e,\mu,\tau} \delta n_{l_i} = 0 \quad \Rightarrow \quad \sum_{i=e,\mu,\tau} Y_l = 0$$

→ no contribution at  $\mathcal{O}(h^4)$  !

## Total lepton number violating density matrix contribution

T.H., Teresi 17

the L-violating Higgs decay contribution to baryogenesis is clearly  $\neq$  from the ARS one since it is a  $\mathcal{O}(h^4)$  contribution based on processes which do involve a Majorana mass insertion, i.e. which do violate total lepton number, unlike ARS

where to find this contribution in density matrix formalism??

the density matrix commutators lead also to contributions  $\propto m_N^2$  which corresponds to processes with a Majorana mass insertion

I

$N$  to  $\bar{L}$  transition instead of  $N$  to  $L$  transition

$$\Gamma_{\alpha\beta}^{\leqslant}(\mathbf{k}) \ni +i \operatorname{tr} \{ P_R v_+(\mathbf{k}) \bar{v}_+(\mathbf{k}) P_L \Sigma_{\beta\alpha}^{\leqslant}(-k) \}$$

## Full set of density matrix equation with LC and LV contributions

T.H., Teresi 17'

$$\begin{aligned}
 \frac{d n_{\alpha\beta}^N}{dt} &= -i [\mathcal{E}_N, n^N(\mathbf{k})]_{\alpha\beta} - \frac{1}{2} \left\{ \gamma^{LC} + \gamma^{LV}, \frac{n^N}{n_{eq}^N} - I \right\}_{\alpha\beta} \\
 &\quad + \frac{\delta n_l^L}{2n_{eq}^L} \left( (\gamma_{WQ,l}^{LC} - \gamma_{WQ,l}^{LV}) + \frac{1}{2} \left\{ \gamma_{WC,l}^{LC} - \gamma_{WC,l}^{LV}, \frac{n^N}{n_{eq}^N} \right\} \right)_{\alpha\beta}, \\
 \frac{d \bar{n}_{\alpha\beta}^N}{dt} &= -i [\mathcal{E}_N, \bar{n}^N(\mathbf{k})]_{\alpha\beta} \\
 &\quad - \frac{1}{2} \left\{ \gamma^{LC*} + \gamma^{LV*}, \frac{\bar{n}^N}{n_{eq}^N} - I \right\}_{\alpha\beta} \\
 &\quad - \frac{\delta n_l^L}{2n_{eq}^L} \left( (\gamma_{WQ,l}^{LC*} - \gamma_{WQ,l}^{LV*}) + \frac{1}{2} \left\{ \gamma_{WC,l}^{LC*} - \gamma_{WC,l}^{LV*}, \frac{\bar{n}^N}{n_{eq}^N} \right\} \right) \\
 &\qquad \vdots \\
 \gamma^{LV} &= \frac{g_{iso}}{4\pi^2} \int_0^\infty dk \frac{k}{e^{k/T} + 1} \frac{m_N^2}{32\pi k^3} \times \int_{E^*}^\infty dE (4Ek + M_L^2 - M_H^2) \left( \frac{1}{e^{\frac{E}{T}} + 1} + \frac{1}{e^{\frac{E+k}{T}} - 1} \right) h_{l\alpha}^* h_{l\beta} \\
 &\simeq 3.35 \times 10^{-3} m_N^2 T^2 h_{l\alpha}^* h_{l\beta} \\
 \gamma_{WQ}^{LV} &= \frac{g_{iso}}{4\pi^2} \int_0^\infty dk k \frac{m_N^2}{32\pi k^3} \times \int_{E^*}^\infty dE (4Ek + M_L^2 - M_H^2) \left( \frac{1}{e^{\frac{E}{T}} + 1} + \frac{1}{e^{\frac{E+k}{T}} - 1} \right) h_{l\alpha}^* h_{l\beta} \simeq 5.49 \times 10^{-4} m_N^2 T^2 h_{l\alpha}^* h_{l\beta} \\
 \gamma_{WC}^{LV} &= \frac{g_{iso}}{4\pi^2} \int_0^\infty dk \frac{k}{e^{k/T} + 1} \frac{m_N^2}{32\pi k^3} \times \int_{E^*}^\infty dE (4Ek + M_L^2 - M_H^2) \frac{1}{e^{\frac{E}{T}} + 1} h_{l\alpha}^* h_{l\beta} \simeq 1.79 \times 10^{-3} m_N^2 T^2 h_{l\alpha}^* h_{l\beta}
 \end{aligned}$$

## Analytical solution for the LV contribution

T.H., Teresi 17'

$$Y_{LV} \simeq 7.9 \times \alpha^{LC} \alpha^{LV} \frac{M_0}{T_c} \frac{m_N^2}{\Delta m_N^2} (h^\dagger h)_{11} (h^\dagger h)_{22} \delta^{LV}$$

$\delta^{LV} \equiv \sum_l \delta_l^{LV} \neq 0$   
 $\delta_l^{LV} = \frac{\text{Im}[h_{l1}^* h_{l2} (h^\dagger h)_{12}]}{(h^\dagger h)_{11} (h^\dagger h)_{22}}$   
 CP-violating Yukawa combination which break total lepton number

→ already non vanishing at  $\mathcal{O}(h^4)$  instead of  $\mathcal{O}(h^6)$  for the LC contribution

suppressed by 2 rates instead of 3 rates for the LC contribution

$$\alpha^{LC} \alpha^{LV} \quad (\alpha^{LC})^2 \alpha_W^{LC}$$

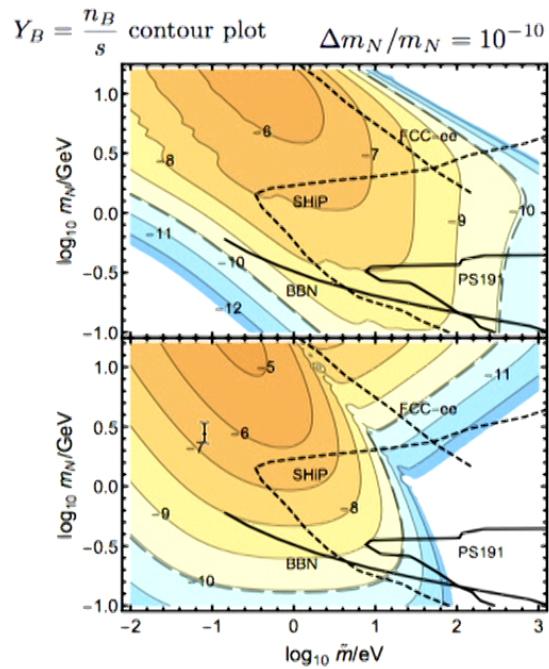
but  $m_N^2$  suppression with different  $\Delta m_N^2$  and  $M_{Planck}$  dependence

→ all in all the various factors more or less compensate each other  
with dominance of one or the other contribution depending on the parameters

## Numerical results: comparison of decay and density matrix formalisms for the LV contribution

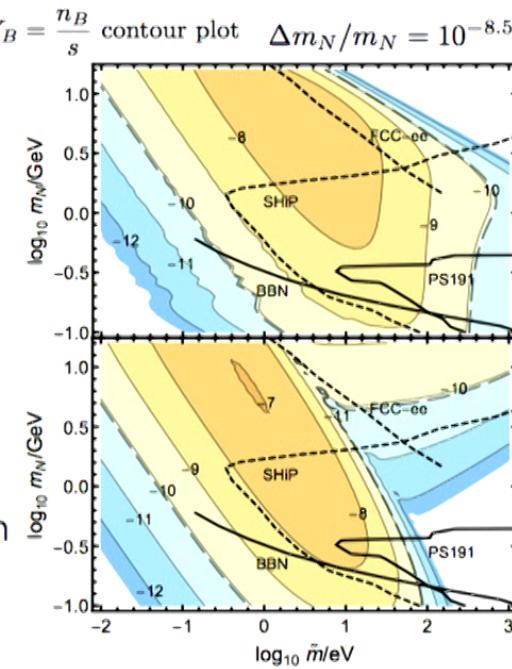
T.H., Teresi 17'

with only one lepton flavour: no ARS, only LV contribution



density  
matrix

decay  
formalism



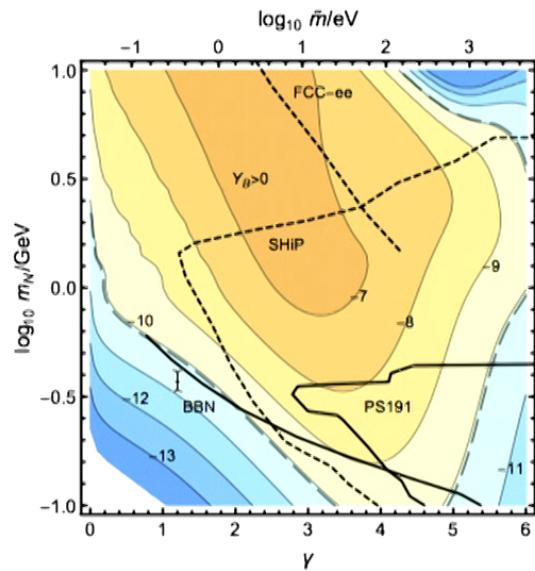
→ qualitative or even quantitative agreement:

- except for small  $m_N$ : different thermal masses taken
- except for large  $\tilde{m}$ : washout suppression too big in decay formalism because doesn't take into account formation of  $N - \bar{N}$  asymmetries

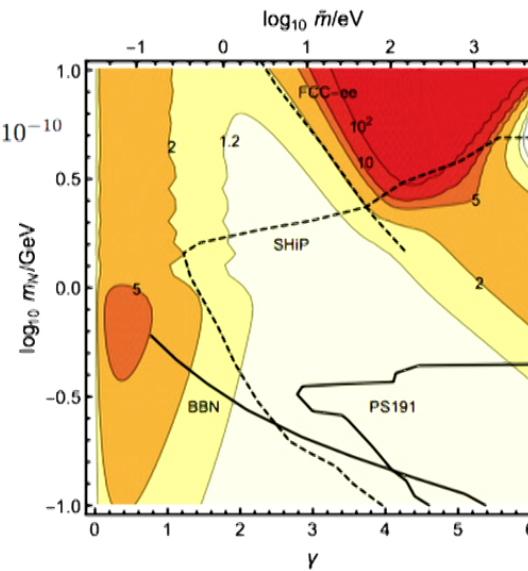
## Numerical results: comparison of LC and LV contributions in matrix density formalism

T.H., Teresi 17'

$Y_B = \frac{n_B}{s}$  contour plot: full LC+LV result



ratio of LV+LC over LC



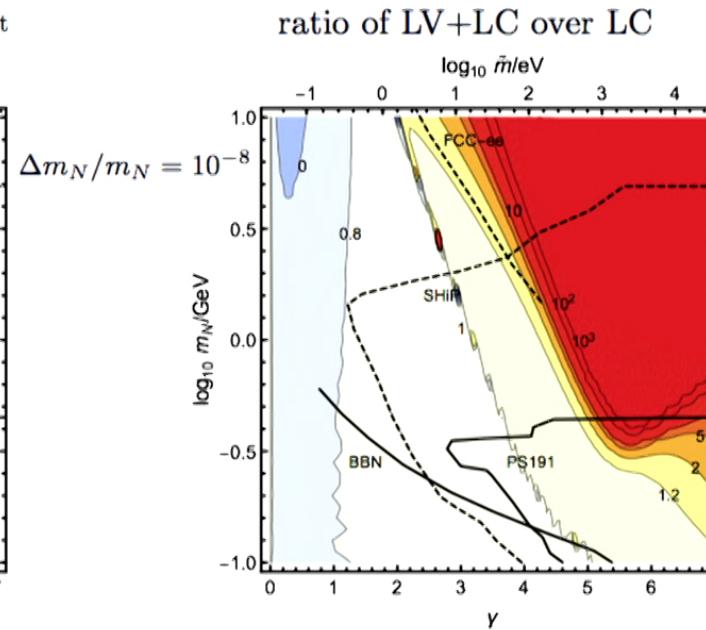
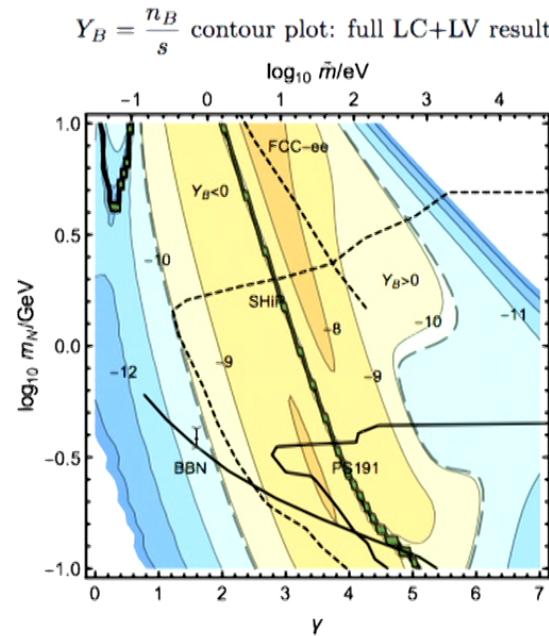
dominance of LV=

- for small ``seesaw'' expected Yukawa couplings

- for very large Yukawas: less washout for LV than for LC
- the smaller  $\Delta m_N/m_N$  the more LV dominates
- the larger  $m_N$  the more LV dominates

## Numerical results: comparison of LC and LV contributions in matrix density formalism

T.H., Teresi 17'



dominance of LV=

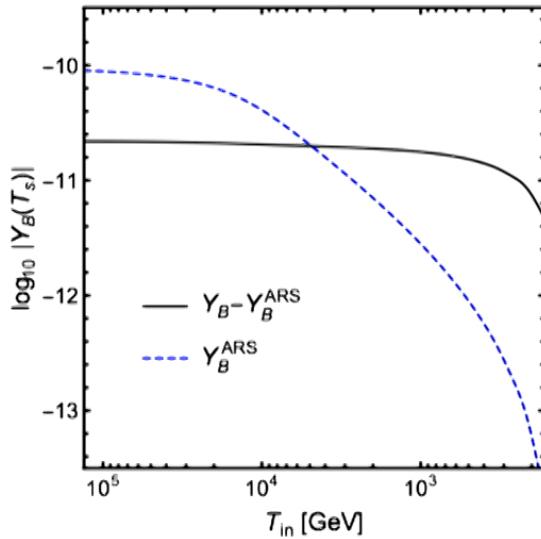
- for small ``seesaw'' expected Yukawa couplings

- for very large Yukawas: less washout for LV than for LC
- the smaller  $\Delta m_N/m_N$  the more LV dominates
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## Dominance of the LV contribution for low reheating temperatures

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LV contribution produced at lower temperature than the ARS-LC contribution due to the  $m_N^2/T^2$  relative factor



## Summary

In usual leptogenesis decay formalism the L violating  $H \rightarrow NL$  decay can easily lead to enough baryon asymmetry for  $m_N < m_H$

- ↪ in type-I seesaw model with nothing else
- ↪ thanks to thermal effect leading to  $N$  self-energy thermal cut
- ↪ from total L number violating CP asymmetries: no need for flavour interplay
- ↪ at electroweak scale temperatures:  $T \gtrsim T_{Sphaler}$ .
- ↪ with boosted production if no  $N$  to begin with
- ↪ in a testable way (SHIP,...) for part of the parameter space

We have confirmed these results in density matrix formalism...

- ↪ both ARS-LC and LV contributions can dominate baryogenesis depending on parameters