

Title: Three point functions in N=4 SYM from integrability

Date: Apr 11, 2017 02:30 PM

URL: <http://pirsa.org/17040052>

Abstract: <p>The talk will review the computation of the three point function of gauge-invariant operators in the planar N=4 SYM theory using integrability-based methods. The structure constant can be decomposed, as proposed by Basso, Komatsu and Vieira, in terms of two form-factor-like objects (hexagons). The multiple sums and integrals implied by the hexagon decomposition can be performed in the large-charge limit, and be compared to the results obtained by semiclassics. I will discuss a method to perform these sums and the contributions currently accessible by this approach.</p>

Three point functions in  $\mathcal{N}=4$  SYM from integrability

w/ Y. Jiang, S. Komatsu, I. Kostov 2016

w/ I. Kostov (in progress)

Basso, Gonçalves, Komatsu 2017



Three point functions in  $\mathcal{N}=4$  SYM

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Barr, Goncalves, Komatsu 2017

planar  $\mathcal{N}=4$  SYM w/ gauge group  $SU(N)$

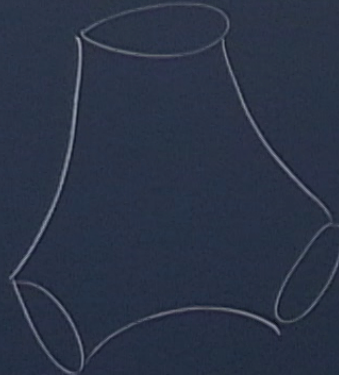
$$g^2 = \frac{\lambda}{16\pi^2} = g_{\text{YM}}^2 N \rightarrow \text{finite}$$

$\mathfrak{so}(4,2)$

$\mathbb{P}^1 \times SU(2,2) \rightarrow SO(5)$  R-symmetry

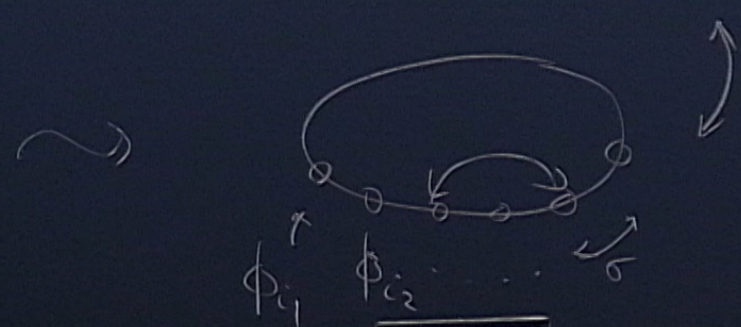
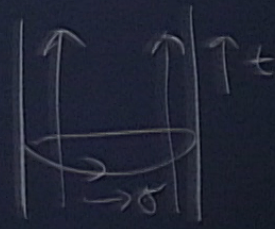


from integrability



$$\mathbb{T}^2_{\text{SU}(N)} (\phi_{c_1} \dots \phi_{c_n} \psi_{A_1} \dots D^k \psi_{A_k}) (x)$$

$\sigma \Rightarrow \text{it}$

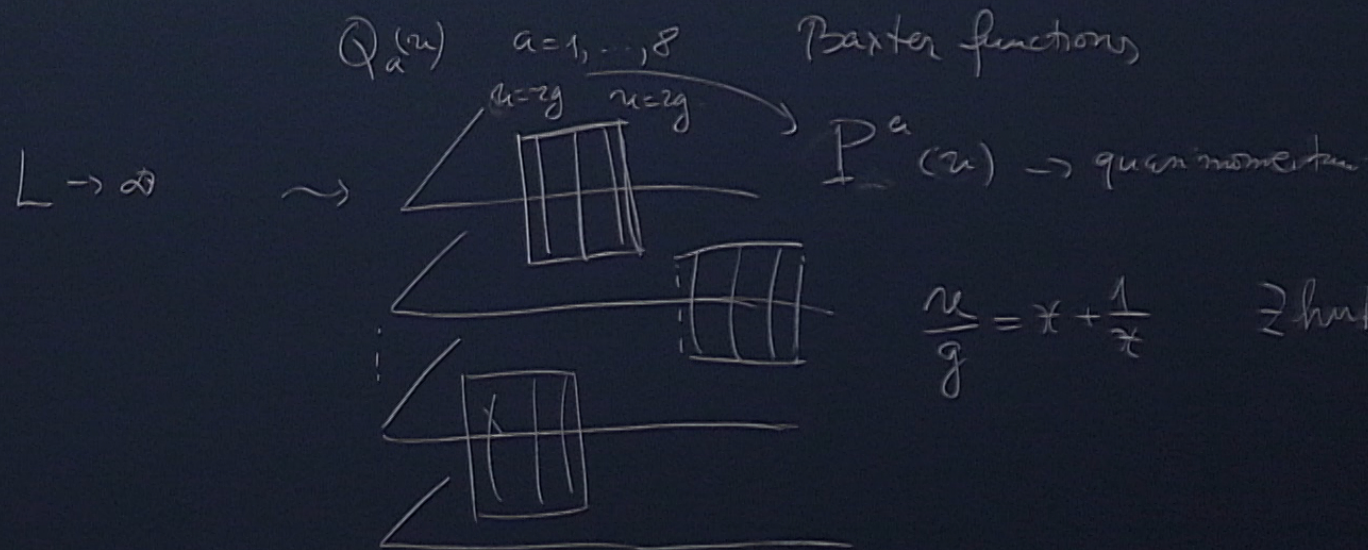


dilatation op  
 $\Leftrightarrow$  integrable hamiltonian



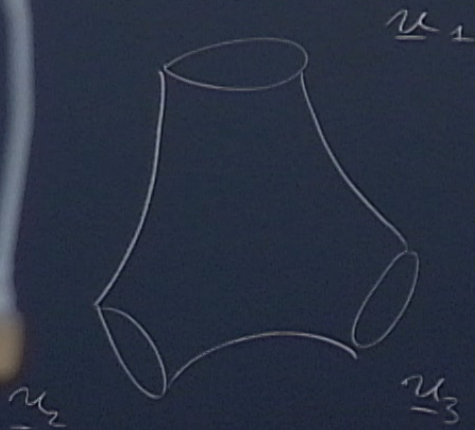
$$E_n \leftrightarrow \Delta_n(g) \leftrightarrow \{u\} = \{\phi\}$$

TBA  $\rightsquigarrow$  Quantum Spectral curve





from integrability



$$\langle \sigma_1(x_1) \sigma_2(x_2) \sigma_3(x_3) \rangle \sim \frac{C_{123}(g)}{|X_{12}|^{\Delta_{12}} |X_{13}|^{\Delta_{13}} |X_{23}|^{\Delta_{23}}}$$

$$\langle \sigma_1(x) \sigma_1(0) \rangle = \frac{1}{|X|^{2\Delta_1}}$$

$$\Delta_g = \Delta_1 + \Delta_2 + \Delta_3$$

$$\{1, 2, 3\} = \{1, 2, 3\}$$



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w/ I. Kostov (in progress)

Basso, Gonçalves, Komatsu 2017

$g \rightarrow 0 \rightsquigarrow$  EGSV 2010

$g \rightarrow \infty \rightsquigarrow$  Jank et al. 2010-2011

KK(N) 2011  $\rightarrow$  2016

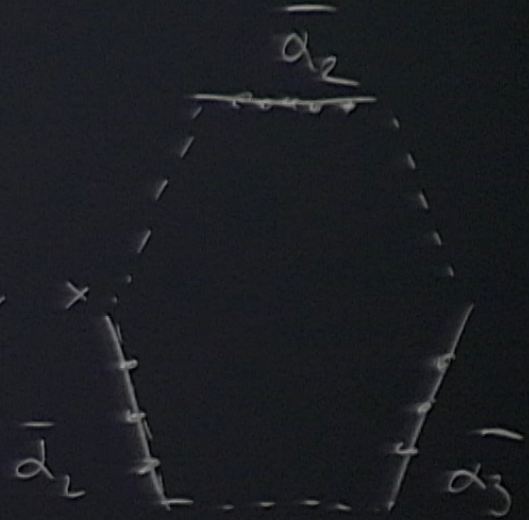
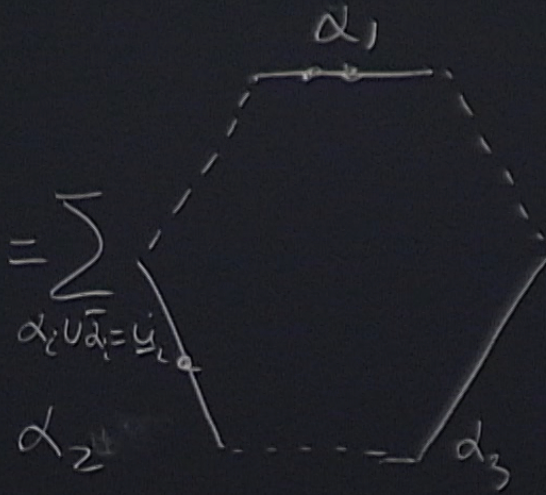
$$\langle \mathcal{O}_1(x_1) \mathcal{O}_2(x_2) \mathcal{O}_3 \rangle$$

$$\langle \overline{\mathcal{O}_1(x)} \mathcal{O}_1(0) \rangle$$





$u_1$



$u_3$

$$(x_3) > \sim \frac{C_{123}(g^2)}{|X_{12}| \Delta_{12} |X_{13}| \Delta_{13} |X_{23}| \Delta_{23}}$$

$$\Delta_y = \Delta_i + \Delta_j - \Delta_k$$



$g$  finite

Bassor, Kenmatsu, Virena 2015

$$C_{123}(g) \sim \sum_{\alpha_i, \bar{\alpha}_i = \bar{u}_i} \underbrace{H(\alpha_1 | \alpha_2 | \alpha_3)} \times \underbrace{H(\bar{\alpha}_1 | \bar{\alpha}_2 | \bar{\alpha}_3)} \underbrace{w(\alpha_1, \bar{\alpha}_1) w(\alpha_2, \bar{\alpha}_2) w(\alpha_3, \bar{\alpha}_3)}$$

$$\ln C_{123}(g) = \sum_* (-1)^{|*|} \oint_{\Gamma_*} \text{Li}_2(e^{iP_*(z)})$$

$$P_*(z) = \begin{cases} P_{ij}(z) = (P_i + P_j + P_k)(z) & \{i, j, k\} = \{1, 2, 3\} \\ 2P_i(z) & i = 1, 2, 3 \\ (P_1 + P_2 + P_3)(z) \end{cases}$$



2015

$$H(\alpha_1 | \alpha_2 | \alpha_3) \times H(\bar{\alpha}_1 | \bar{\alpha}_2 | \bar{\alpha}_3) \underbrace{w(\alpha_1, \bar{\alpha}_1) w(\alpha_2, \bar{\alpha}_2) w(\alpha_3, \bar{\alpha}_3)}_{\text{mirror particles}}$$

$$1) \oint_{\Gamma_*} Li_2 \left( e^{i P_*(z)} \right)$$

$$P_c + P_j + P_k(z) \quad \{(i, j, k)\} = \{1, 2, 3\}$$

$i = 1, 2, 3$

$$P_3(z)$$



$$\frac{1}{n!} \int_{\Gamma_u} \frac{dz_1 \dots dz_n}{(2\pi)^n \varepsilon^n}$$

$$\prod_{i=1}^n \frac{e^{-\varphi(z_i)} \ell_{i3}}{h(z_i, u)} \prod_{i < j} h(z_i, z_j) h(z_j, z_i)$$

$$\prod_i f(z_i)$$

$$z_i = z_j + i\varepsilon$$

$$f(z_i) f(z_j + i\varepsilon)$$

$$\prod_{i < j} \frac{\pi^{-2} D^2(z_i, z_j) (z_i - z_j)^2}{(z_i - z_j)^2 + \varepsilon^2} \approx 1$$

$$1 - \varepsilon \delta(z_i - z_j)$$

$$\text{Det}_{i,j} \frac{1}{z_i - z_j + i\varepsilon}$$

Bettelheim, Kostov 2014



$$| \alpha_3 \rangle \times | \bar{\alpha}_1 | \bar{\alpha}_2 | \bar{\alpha}_3 \rangle \underbrace{w(\alpha_1, \bar{\alpha}_1) w(\alpha_2, \bar{\alpha}_2) w(\alpha_3, \bar{\alpha}_3)} \quad * \quad \underline{\text{mirror particles}}$$

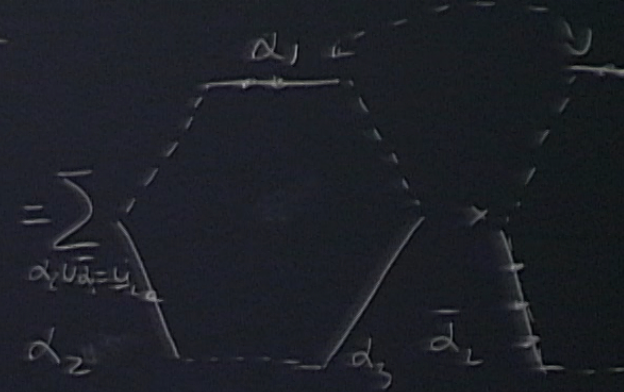
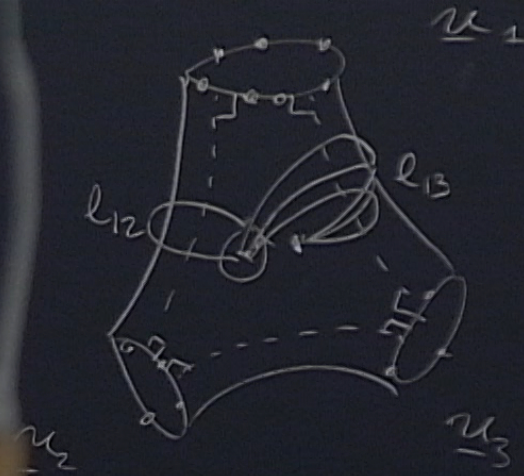
$$L_2 \left( e^{i P_*(z)} \right)$$

$$z) \quad \{i, j, k\} = \{1, 2, 3\} \quad \checkmark$$



# SYM from integrability

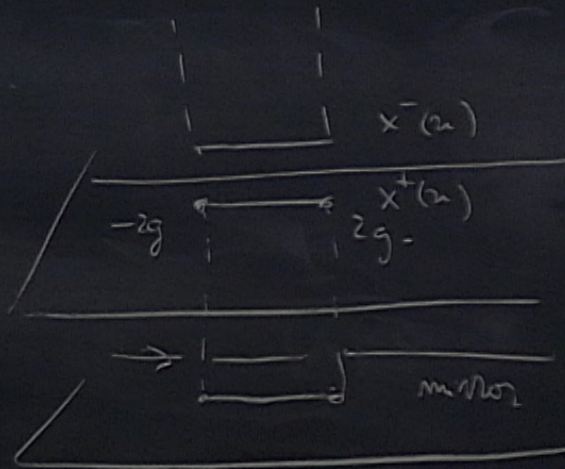
2016



$$l_{ij} = \frac{1}{2}(L_i + L_j - L)$$

bound states with  $a = 1, 2, \dots$

a different domain.



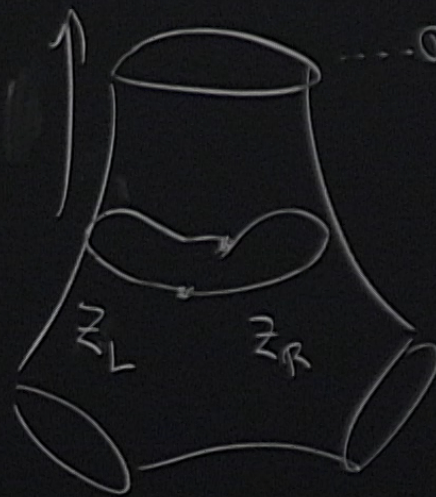
$$x_{\pm}^{\pm}(u) = x(u \pm i/2)$$

$$x^+ \rightarrow 1/x^+$$

$$x^- \rightarrow x^-$$



$$w(\alpha_1, \bar{\alpha}_1) w(\alpha_2, \bar{\alpha}_2) w(\alpha_3, \bar{\alpha}_3) \quad \times \quad \underline{\text{mirror particles}}$$



$$\frac{1}{h(z_L, z_R) h(z_R, z_L)}$$

$$\sim \frac{1}{(z_L - z_R)^2}$$

$$\checkmark \quad \Gamma_u \quad \Gamma_{[-2g, 2g]}$$