

Title: PSI 2016/2017 Explorations in Quantum Information - Lecture 15

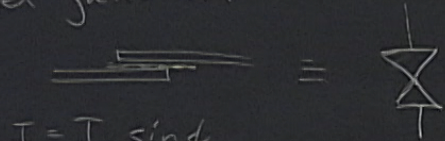
Date: Apr 07, 2017 09:00 AM

URL: <http://pirsa.org/17040014>

Abstract:

$$\Phi_0 = \frac{h}{2e} \quad \text{flux quantum}$$

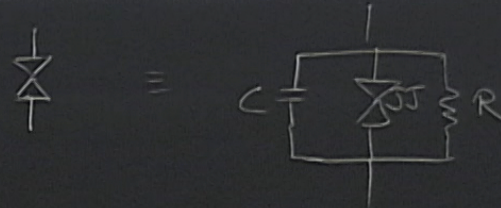
tunnel junction



$$I = I_c \sin \phi$$

phase difference over the junction.
critical current

$$\frac{d\phi}{dt} = \frac{2e}{h} V = \frac{2\pi}{\Phi_0} V$$

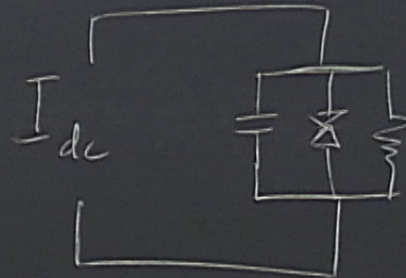


$$I_J = I_c \sin \phi$$

$$I_R = \frac{V}{R} \quad ; \quad V = \frac{h}{2e} \frac{d\phi}{dt} \quad \therefore \quad I_R = \frac{h}{2eR} \frac{d\phi}{dt}$$

$$I_c = C \frac{dV}{dt} \quad ; \quad \frac{dV}{dt} = \frac{h}{2e} \frac{d^2\phi}{dt^2} \quad \therefore \quad I_{cap} = \frac{hC}{2e} \frac{d^2\phi}{dt^2}$$

R



$$I_{dc} = I_{cap} + I_J + I_R$$

$$I_{dc} = \frac{h_c}{2e} \frac{d^2\phi}{dt^2} + \frac{h_c}{2eR} \frac{d\phi}{dt} + I_c \sin\phi$$

driven pendulum,

$$\frac{h_c}{2e} \frac{d\phi}{dt} \therefore I_R = \frac{h_c}{2eR} \frac{d\phi}{dt}$$

$$\frac{h_c}{2e} \frac{d^2\phi}{dt^2} \therefore I_{cap} = \frac{h_c}{2e} \frac{d^2\phi}{dt^2}$$

Current biased JJ

Coordinate

ϕ

Frequency

$$\sqrt{\frac{2eI_c}{\hbar C}}$$

damping

$$\frac{1}{RC}$$

Forcing

$$I_{DC}$$

Critical Forcing

Current biased JJ

Coordinate ϕ

Frequency $\sqrt{\frac{2eI_c}{\hbar C}}$

damping $\frac{1}{RC}$

Forcing I_{DC}

Critical Forcing $I_{DC} = I_c$

over the JJ

$I_{DC} < I_c$, $V = 0$
 $\therefore I_{DC} = 0 = I_{cap}$

take I_{DC} ramp slowly from 0,

Kinetic Inductance of charge carriers.

time voltage JJ

$= 0$
 $= I_{cap}$

o,
Kinetic Inductance
of charge carriers.
time voltage
JJ

$$-\frac{dU}{dt} = \text{Force}$$

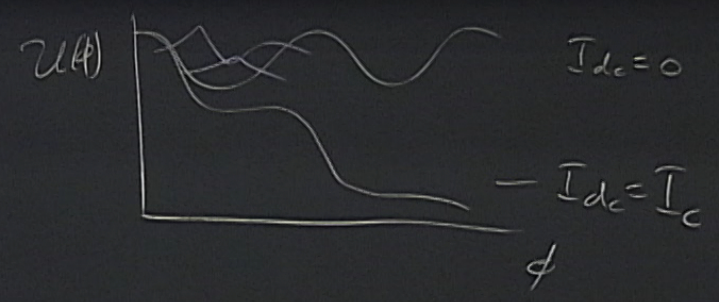
$$\frac{\hbar^2 C}{2e} \frac{d^2 \phi}{dt^2} + \frac{\hbar^2}{2eR} \frac{d\phi}{dt} = \underbrace{-\frac{I_c}{e} \sin \phi + I_{dc}}_{\text{Force}}$$

$$U(\phi) = - \left(\frac{I_{dc}}{I_c} \phi + \cos \phi \right)$$

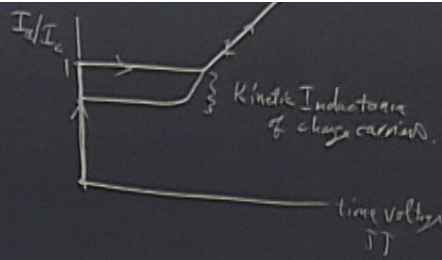
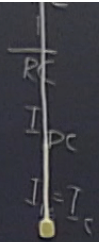
critical forcing

$$I_{DC}$$
$$I_{DC} = I_c$$

time vol
JT



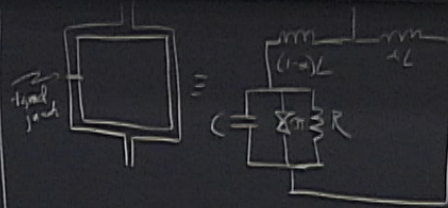
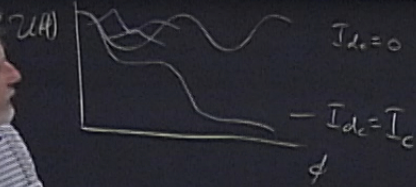
damping
 forcing
 critical forcing



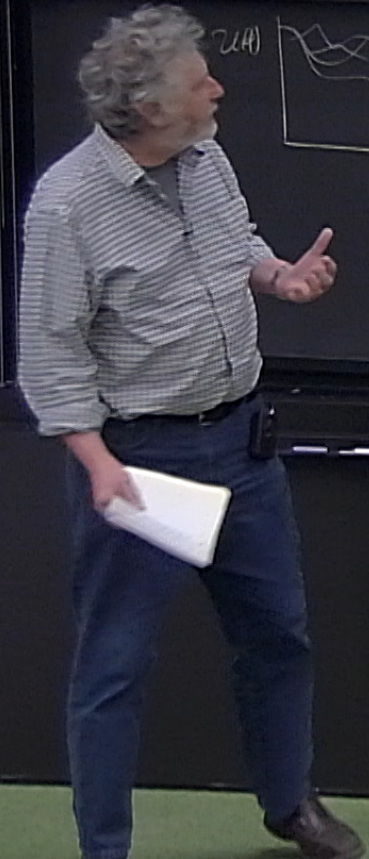
$$2e \frac{d\phi}{dt} + 2eR \frac{d\phi}{dt} = \dots$$

$$Z(\phi) = - \left(\frac{I_{dc}}{I_c} \phi + \cos \phi \right)$$

$0 \rightarrow 1$

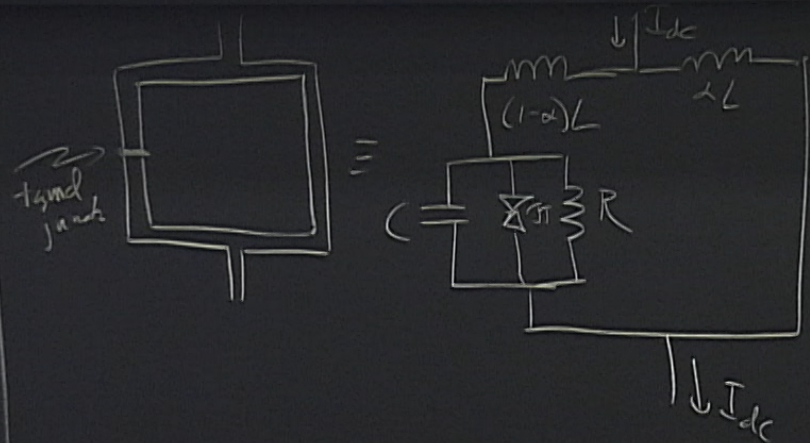


$$\frac{\hbar C}{2e} \frac{d^2 \phi}{dt^2} + \frac{\hbar}{2eR} \frac{d\phi}{dt} + I_c \sin \phi + \frac{\Phi_0}{2\pi L} \phi = 2I_{dc}$$



time voltage
JT

0 → 1



$$\frac{\hbar C}{2e} \frac{d^2 \phi}{dt^2} + \frac{\hbar}{2eR} \frac{d\phi}{dt} + I_c \sin \phi + \frac{\Phi_0}{2\alpha L} \phi = I_{dc}$$

noise ↑

organize just 2 bound states

