Title: PSI 2016/2017 Quantum Information (Review) - Lecture 9 (Eduardo Martin-Martinez) Date: Mar 06, 2017 09:00 AM URL: http://pirsa.org/17030033

Abstract:

March 5-6th 2017 PSI

Relativistic Quantum Information

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Fundamental Topics: Cosmology



How much can we learn about the Early Universe nowadays?

Fundamental Topics: Black Hole Information Loss Problem



Quantum Mechanics preserves information.

Black Holes: Does Nature destroy information?

Or does the information escape in the form of Hawking Radiation?

Fundamental Topics: Vacuum Fluctuations



In Nature, the vacuum is not empty. Only on average.

Vacuum Fluctuations contain Information about curvature of spacetime.

Quantum noise is special: It can assist communication!

Fundamental Topics: Quantum Measurements and Localization





Quantum Theory is a probabilistic theory.

The outcome of measurements is not deterministically predictable.

Quantum-to-Classical transition.

Relativistic considerations in the localization of Information

Fundamental Topics: Fixed points in Quantum evolution



The problem of equilibration in Quantum Theory and in Gravity.

Quantum Thermodynamics

Quantum Control

Fundamental Topics: Quantum Gravity



One of the most important challenges of modern Mathematical Physics:

Quantum Theory for Gravitation

Fundamental Topics: "Spacetime Engineering"

Violate energy conditions:



For more info: N.Funai, E. martin-Martinez: arXiv:1701.03805

Technological Applications

Development of Mathematical tools that can be applied to experiments and technologies:



- -Quantum Entanglement and Quantum Resources
- -Communication
- -Metrology
- -Quantum Control and Simulations

Getting Familiar with Spacetime

Relativity Matters for Quantum Information

Same Physics, Different Descriptions

Bell Rocket "Paradox"







Same Physics, Different Descriptions







Same Physics, Different Descriptions

PHYSICS:

The rope breaks, all right!

PHENOMENOLOGY:

For the accelerated observer A: Because rocket B is faster than us!

For the observer on the ground: Because both rockets go equally faster and faster, the length of the rope Lorentz-contracts!

Getting Familiar with Spacetime

Simultaneity is Relative!



Two observers in different states of motion would not agree about what happens first

Getting Familiar with Quantum Mechanics

Schrödinger's cat



Quantum Entanglement



EINSTEIN ATTACKS QUANTUM THEORY

Scientist and Two Colleagues Find It Is Not 'Complete' Even Though 'Correct.'

SEE FULLER ONE POSSIBLE

Believe a Whole Description of 'the Physical Reality' Can Be Provided Eventually.





I pick one ball at random... It's white!

I know the one inside is black!





I pick one set of dice at random... I throw it and it gives 10!

Classically: I don't know anything about what would be the result of throwing the other set

What entanglement is not



The Race To Prove 'Spooky' Quantum Connection May Have a Winner

Entanglement breakthrough could lead to unhackable Internet

By Devin Powell August 29, 2015

Particles don't obey the same rules as people. Poke a particle, and another one far away can instantly respond the touch -- without any messages passing through the space between, as if the two particles were one. "Entanglement" is what quantum physics calls the intimate connection.

Einstein called it "spooky." To his dying day, he refused to believe that nature could be so unreasonable.

From http://www.popsci.com

Getting Familiar with Spacetime

Simultaneity is Relative! Who collapses what?? Who pokes what??



A happens after C



A and C are simultaneous



A happens before C

Relativistic Quantum Information



General relativity



Quantum field theory



Quantum information

- Harness relativistic approaches to "do more" in quantum information processing.
- Study the structure of spacetime and the quantum nature of gravity via quantum informational tools

THE BLACK HOLE INFORMATION PARADOX



Entanglement in a Stellar Collapse

Once upon a time...

There was... NADA $\Psi_0 = |0\rangle$

But then...

What happened to the field!?





Entanglement in a Stellar Collapse

Vacuum in the far past evolves into two mode squeezed state between infalling and outgoing modes in the far future

$$\operatorname{Tr}_{\operatorname{hor}}\left(\left|0\right\rangle\left\langle 0\right|\right) = \bigotimes_{\omega} \frac{1}{\cosh^{2} r} \sum \tanh^{2n} r_{\omega} \left|n_{\omega}\right\rangle_{\operatorname{out}} \left\langle n_{\omega}\right|_{\operatorname{out}}$$

We only see the modes that reach the future!

Black hole Information loss problem

If we believe in quantum theory, information cannot be lost...

Black hole Information loss problem

If we believe in quantum theory, information cannot be lost...

After corrections, the outflow may not be entirely thermal...

Like when a piece of charcoal burns





Page Hypothesis:

Entanglement between radiation emitted at different times in the black hole life!



Black holes Information loss problem

So... The outflow is not entirely thermal...

Hold on !! that's potentially even worse !!
Black hole Information Paradox

A: Radiation emitted after Page Time B: Infalling Radiation C: Radiation emitted before Page Time

Entropy subadditivity:

 $S(\rho_{\text{ABC}}) + S(\rho_{\text{A}}) \le S(\rho_{\text{AB}}) + S(\rho_{\text{AC}})$

Entanglement subadditivity:

 $\mathcal{E}(A,B) + \mathcal{E}(A,C) \le \mathcal{E}(A,BC)$

HAWKING RADIATION

What about monogamy?



Susskind's Black Hole complementary The Harlow-Hayden Conjecture

Black hole Information Paradox

Possible Solution: Firewalls!

Almheiri, Ahmed; Marolf, Donald; Polchinski, Joseph; Sully, James. Journal of High Energy Physics 2013 (2).

Black hole Information Paradox (Firewalls)

What-if scenario:

Somehow dynamics is such that it destroys the correlations between "in" and "out" regions

> Entanglement subadditivity: $\mathcal{E}(A, B) + \mathcal{E}(A, C) \leq \mathcal{E}(A, BC)$

Make this zero

Black hole Information Paradox (Firewalls)



Are Firewalls really 'Monsters'?



PRL 115, 031301 (2015)

Divergences in the stress-energy tensor: Violence at the horizon

> week ending 17 JULY 2015

(1 + 1)D Calculation Provides Evidence that Quantum Entanglement Survives a Firewall

PHYSICAL REVIEW LETTERS

Eduardo Martín-Martíne2^{1,2,3} and Jorma Louko⁴ ¹Institute for Quantum Computing, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada ²Department of Applied Mathematics, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada ³Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada ⁴School of Mathematical Sciences, University of Nottingham, Nottingham NG7 2RD, United Kingdom (Received 26 February 2015; published 14 July 2015)

We analyze how preexisting entanglement between two Unruh-DeWitt particle detectors evolves when one of the detectors falls through a Rindler firewall in (1 + 1)-dimensional Minkowski space. The firewall effect is minor and does not wash out the detector-detector entanglement, in some regimes even preserving the entanglement better than Minkowski vacuum. The absence of cataclysmic events should continue to hold for young black hole firewalls. A firewall's prospective ability to resolve the information paradox must hence hinge on its detailed gravitational structure, presently poorly understood.

DOI: 10.1103/PhysRevLett.115.031301

PACS numbers: 04.70.Dy, 04.60.-m, 04.62.+v

The two results we will talk about

Vacuum Entanglement Harvesting and Farming

Quantum Collect Calling

Communication through massless fields



General properties of wireless communication

Communication through the EM field

Communcation mediated by 'real' energy-carrying quanta



An emitter emits photons. A receiver captures photons.

Communication through the EM field

Information flow carried by (an average) energy flow



Information reaches you when energy reaches you

Communication through the EM field

Communication is only possible at the speed of light (in vacuum)



If you miss the beam, you miss the message





Communication through massless fields

Communication through a masses fields in the vacuum

- -Only At the speed of light.
- -Through the exchange of real quanta
- -Information flow carried by energy flow. 👩
- -Miss the beam, miss the message





Communication through massless fields

Communication through a massless fields in vacuum

-Information propagates arbitrarily slow even for massless field.

-Recover the message even if the beam is missed.

-Information flow not supported by real quanta (photons) flow.

-Information flow in absence of energy flow.



Home » Physics » Quantum Physics » March 31, 2015

Photon 'afterglow' could transmit information without transmitting energy March 31, 2015 by Lisa Zyga [eature]

(Phys.org)—Physicists have theoretically shown that it is possible to transmit information from one location to another without transmitting energy. Instead of using real photons, which always carry energy, the technique uses a small, newly predicted quantum afterglow of virtual photons that do not need to carry energy. Although no energy is transmitted, the receiver must provide the energy needed to detect the incoming signal—similar to the

Mathematical Methods: Beyond the Strong Huygens Principle

Subtleties in the behaviour of the solutions of certain PDEs: The strong Huygens principle

The Green's function of the (massless) wave equation in 3+1D Minkowski space has support only on the light cone. Hence, any disturbances propagate strictly along null geodesics (at the speed of light)

Mathematical Methods: Beyond the Strong Huygens Principle

Subtleties in the behaviour of the solutions of certain PDEs: The strong Huygens principle

The Green's function of the (massless) wave equation in 3+1D Minkowski space has support only on the light cone. Hence, any disturbances propagate strictly along null geodesics (at the speed of light)

Exploitable when emitters are quantum!

TECHNICAL DETAILS

R. H. Jonsson, E. Martin-Martinez, A. Kempf, Phys. Rev. Lett. 114, 110505 (2015)
A. Blasco, L. J. Garay, M. Martin-Benito, E. Martin-Martinez, Phys. Rev. Lett. 114, 141103 (2015)
A. Blasco, L. J. Garay, M. Martin-Benito, E. Martin-Martinez, Phys. Rev. D 93, 024055 (2016)
P. Simidzija, E. Martin-Martinez, Phys. Rev. D 95, 025002 (2017)

See also:

R. H. Jonsson, J. of Phys. A, 44, 445402 (2016)

The radiation Green's function (or equivalently the commutator) of a massless field has support only on the light-cone

$$\Box G(x, x') = -4\pi \delta_4(x, x') \qquad [\Phi(x), \Phi(x')] = \frac{i}{4\pi} G(x, x')$$

→ Communication has support only on the light-cone

True in 3+1 Flat spacetime

BEYOND THE STRONG HUYGENS PRINCIPLE

In general: if there is curvature (unless there is conformal invariance)

In curved spacetimes, **communication through massless fields** is not confined to the light-cone, but there can be a leakage of information towards the **inside of the light-cone decoupled from energy propagation**. SPATIALLY **FLAT**, **OPEN FRW** SPACETIME **3+1D**:

$$ds^2 = a(\eta)^2(-d\eta^2 + dr^2 + r^2 d\Omega^2)$$

 η : conformal time $a(\eta)$: scale factor t : cosmological time, $\mathrm{d}t = a(\eta)\mathrm{d}\eta$ units: $\hbar = c = 1$

This geometry will be generated by:

a perfect fluid with a constant density-to-presure ratio $\left(\ p = w
ho
ight)$

 \rightarrow

the scale factor evolves as $\left[a \propto \eta^{lpha+rac{1}{2}} \propto t^{rac{2lpha+1}{2lpha+3}}
ight]$

 $\alpha = \frac{3 - 3w}{6w + 2}$

with

A TEST **SCALAR FIELD** QUANTIZED IN THE **BUNCH-DAVIS VACUUM** WILL BE COUPLED TO THE BACKGROUND GEOMETRY.









THE BIG BANG Setting



- Area II . - C. MAL .I

BIG BANG CASE, ST. COSMOLOGICAL MODEL: GENERAL RELATIVITY

KLEIN-GORDON EQUATION

$$(\Box - m^2 + \xi R)\phi = 0 \qquad \Box = \frac{1}{\sqrt{|g|}}\partial_\mu \left(\sqrt{|g|}g^{\mu\nu}\partial_\nu\right)$$

CONFORMAL COUPLING

$$\xi=rac{1}{6}$$
 Yields Conformally Invariant Action

MINIMAL COUPLING

$$\xi=0$$
 Gives good predictions (Cosmology, etc..)

CASE : Variation of temporal separation



CASE: Variation of spatial separation





$$SIGNALING ESTIMATOR, S$$

$$S = \lambda_A \lambda_B S_2 + \mathcal{O}(\lambda_\nu^4)$$

$$S_2 = 4 \int a(t)^3 d^3 x dt \int a(t')^3 d^3 x' dt' \chi_A(t) \chi_B(t') \operatorname{Re}(\alpha_A^* \beta_A) F(x - x_A, t)$$

$$\times F(x' - x_B, t) \operatorname{Re}(\alpha_B^* \beta_B [\phi(x, t), \phi(x', t')])$$

$$[\phi(x, t), \phi(x', t')] = \frac{i}{4\pi} \left[\frac{\delta(\Delta \eta + |x - x'|) - \delta(\Delta \eta - |x - x'|)}{a(t)a(t')|x - x'|} \right]$$

$$egin{aligned} \Delta\eta &= \eta(t) - \eta(t') \ &|\psi_{0,
u}
angle &= lpha_
u|e_
u
angle + eta_
u|g_
u
angle \end{aligned}$$

CHANNEL CAPACITY

To obtain a lower bound to the channel capacity, we use a simple **COMMUNICATION PROTOCOL:**

Alice encodes "1" by coupling her detector A to the field, and "0" by not coupling it.

Later Bob switches on B and measures its energy. If B is excited, Bob interprets a "1", and a "0" otherwise.

$$C \simeq \lambda_A^2 \lambda_B^2 rac{2}{\ln 2} \left(rac{S_2}{4|lpha_B||eta_B|}
ight)^2 + \mathcal{O}(\lambda_
u^6)$$

(noisy asymmetric binary channel)

Robert H. Jonsson, Eduardo Martín-Martinez, and Achim Kempf. Quantum Collect Calling. Phys. Rev. Lett. 114, 110505 (2015).





Not surprising:

Conformal Symmetry makes it too similar to flat spacetime

SIGNALING ESTIMATOR, S

$$\begin{split} \left[\phi(\boldsymbol{x}_{A}, t_{A}), \phi(\boldsymbol{x}_{B}, t_{B})\right] &= \mathrm{i} \frac{\theta(\eta(t_{B}) - \eta(t_{A})) - \theta(\eta(t_{A}) - \eta(t_{B}))}{(2\pi)^{3} |\boldsymbol{x} - \boldsymbol{x}'| a(\eta(t_{A})) a(\eta(t_{B}))} \int_{0}^{\infty} \mathrm{d}k \; k \; \sin(k |\boldsymbol{x} - \boldsymbol{x}'|) \hat{g}(\eta(t_{A}), \eta(t_{B}), k) \right] \\ \hat{g}(\eta, \eta', k) &= \frac{8\pi}{k} \sqrt{\left|\frac{\eta}{\eta'}\right|} \frac{\mathrm{sgn}(\eta') [J_{\alpha-1/2}(k|\eta|) Y_{\alpha-1/2}(k|\eta'|) - Y_{\alpha-1/2}(k|\eta|) J_{\alpha-1/2}(k|\eta'|)]}{Y_{\alpha-1/2}(k|\eta'|) - J_{\alpha+1/2}(k|\eta'|) - J_{\alpha-1/2}(k|\eta'|) \left[Y_{\alpha-3/2}(k|\eta'|) - Y_{\alpha+1/2}(k|\eta'|)\right]} \end{split}$$

$J_{lpha} \, \, Y_{lpha} \,\,\,$ BESSEL FUNCTIONS

$$\begin{array}{l} \text{MATTER DOMINATED} & \longrightarrow & \alpha = 2 & \longrightarrow & a \propto \eta^2 \propto t^{2/3} \\ \\ J_{2-1/2}(k|\eta|) = \sqrt{2/\pi} \frac{1}{\sqrt{k|\eta|}} \left[-\cos(k\eta) + \frac{\sin(k\eta)}{k\eta} \right] \\ \\ Y_{2-1/2}(k|\eta|) = \sqrt{2/\pi} \frac{\operatorname{sgn}(\eta)}{\sqrt{k|\eta|}} \left[-\sin(k\eta) + \frac{\cos(k\eta)}{k\eta} \right] \end{array}$$

SIGNALING ESTIMATOR, S

MINIMAL COUPLING

$$\begin{array}{ccc} \text{MATTER DOMINATED} & \longrightarrow & \alpha = 2 & \longrightarrow & a \propto \eta^2 \propto t^{2/3} \\ \text{UNIVERSE} & \longrightarrow & \alpha = 2 & \longrightarrow & a \propto \eta^2 \propto t^{2/3} \end{array}$$

$$\left[\phi(\boldsymbol{x},t),\phi(\boldsymbol{x}',t')\right] = \frac{\mathrm{i}}{4\pi} \left[\frac{\delta(\Delta\eta + |\boldsymbol{x} - \boldsymbol{x}'|) - \delta(\Delta\eta - |\boldsymbol{x} - \boldsymbol{x}'|)}{a(t)a(t')|\boldsymbol{x} - \boldsymbol{x}'|} + \frac{\theta(-\Delta\eta - |\boldsymbol{x} - \boldsymbol{x}'|) - \theta(\Delta\eta - |\boldsymbol{x} - \boldsymbol{x}'|)}{a(t)a(t')\eta(t)\eta(t')} \right]$$













Exponential Expansion (deSitter): No decay in time!

P. Simidzija, E. Martin-Martinez, Phys. Rev. D 95, 025002 (2017)



Setting QUANTUM BOUNCE

EXAMPLE: LOOP QUANTUM COSMOLOGY

- Replaces the Big Bang by a Big Bounce

- Bridge between two large classical universes: a contracting and an expanding cosmological phase



BIG BOUNCE

Martin Bojowald. Loop quantum cosmology. Living Rev.Rel., 11:4, 2008.

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Setting QUANTUM BOUNCE

Atoms (or any complex system) will not survive a quantum bounce

Imagine an ancient (pre-bounce) and very advanced civilization



What would you do if you wanted your legacy to survive?

Encode the information in the quantum field: detectors and field get entangled.