

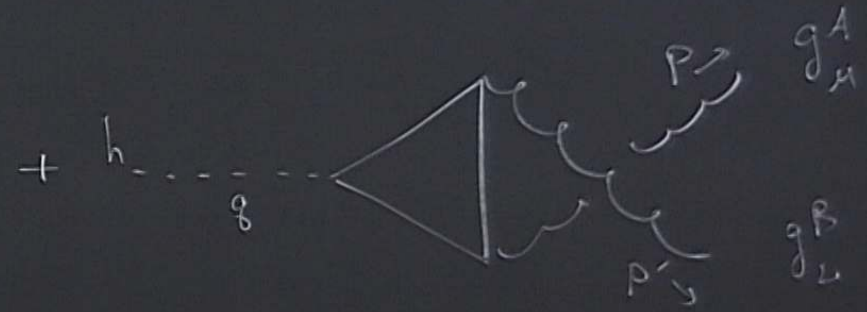
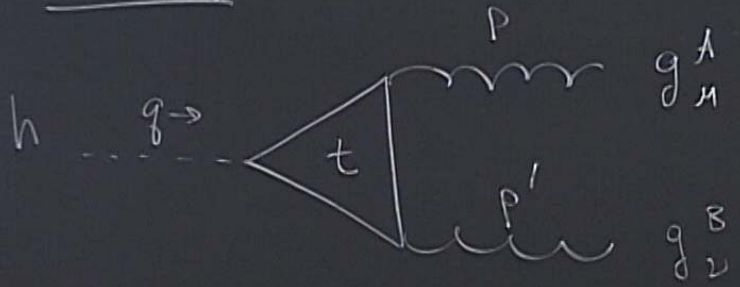
Title: PSI 2016/2017 Standard Model (Review) - Lecture 10

Date: Jan 16, 2017 09:00 AM

URL: <http://pirsa.org/17010014>

Abstract:

$$\underline{h \rightarrow gg}$$



$$i\mathcal{M} = i\mathcal{M}_1 + i\mathcal{M}_2$$

$$i\mathcal{M}_1 = - \frac{i}{16\pi^2} \frac{g^2}{v} \text{Tr}(T^A T^B) \epsilon_\mu(p) \epsilon_\nu(p') \left( 4 p^\nu p'^\mu - \frac{1-4xz}{1-xz} \left( \frac{m_h^2}{m_t^2} \right) \right)$$

$$\times \int_0^1 dx \int_0^{1-x} dz$$

Consider:  $\frac{m_t^2}{m_h^2} \gg \frac{m_h^2}{m_t^2}$

$$i m_1 = - \frac{i}{16\pi^2} \frac{g^2}{v} \text{Tr}(T^A T^B) \epsilon_\mu(p) \epsilon_\nu(p') (4 p^\nu p'^\mu -$$

$$\times \int_0^1 dx \int_0^{1-x} dz \frac{1 - 4xz}{1 - xz} \left( \frac{m_h^2}{m_t^2} \right)$$

Consider:

$$\frac{m_t}{m_h} \gg \frac{m_h}{m_t}$$

$$\rightarrow \int_0^1 dx \int_0^{1-x} dz (1 - 4xz) = \frac{1}{3}$$

$$\frac{g^2}{v} \text{Tr}(T^A T^B) \epsilon_\mu(p) \epsilon_\nu(p') \left( 4 p^\nu p'^\mu - 2 m_h^2 \eta^{\mu\nu} \right)$$

$$\int_0^1 dx \int_0^{1-x} dz \frac{1 - 4xz}{1 - xz} \left( \frac{m_h^2}{m_t^2} \right)$$

$$\frac{m_t^2}{m_h^2} \gg \frac{m_h^2}{m_t^2}$$

$$\int_0^1 dx \int_0^{1-x} dz (1 - 4xz) = \frac{1}{3}$$

$$\text{Tr}(T^A T^B) = \frac{1}{2} \delta^{AB}$$

$$i^{\mathcal{M}_2} = i^{\mathcal{M}_1}$$

$$i^{\mathcal{M}} = -i \frac{\alpha_s}{3\pi V} \epsilon_{\mu}^{\nu}(p) \epsilon_{\nu}^{\rho}(p') \left( p^{\nu} p'^{\mu} - \frac{m_h^2}{2} \eta^{\mu\nu} \right) \delta^{AB}$$

Check:

$$\begin{aligned} \epsilon_{\mu}(p) &\rightarrow p_{\mu} \\ \epsilon_{\nu}(p') &\rightarrow p'_{\nu} \end{aligned}$$

$$\sum |M|^2 = \left( \frac{\alpha_s}{3\pi V} \right)^2 \underbrace{\delta_{AB} \delta^{AB}}_8 \left( p^\nu p'^\mu - \frac{m_h^2}{2} \eta^{\mu\nu} \right) \left( p_\nu p'_\mu - \frac{m_h^2}{2} \eta_{\mu\nu} \right)$$

$$= \frac{8 \alpha_s^2}{9 \pi^2 V^2} \left( -2 \frac{m_h^2}{2} p \cdot p' + \frac{m_h^4}{4} \cdot 4 \right) =$$

$$\underbrace{\delta_{AB} \delta^{AB}}_8 \left( p^\nu p'^\mu - \frac{m_h^2}{2} \eta^{\mu\nu} \right) \left( p_\nu p'_\mu - \frac{m_h^2}{2} \eta_{\mu\nu} \right)$$

$$2p \cdot p' = m_h^2$$

$$\frac{d^2}{ds^2} \left( -2 \frac{m_h^2}{2} p \cdot p' + \frac{m_h^4}{4} \cdot 4 \right) = \frac{4 d^2 m_h^4}{9 \pi^2 v^2}$$

$$\Gamma(h \rightarrow gg) = \frac{\alpha_s^2 M_h^3}{64\pi^3 v^2}$$

$$\approx 0.23 \text{ MeV}$$

$$(5.7\%)^*$$

Needed to divide by 2 to avoid identical final state gluons.

\*QCD corrections enhance

Needed to divide by 2 to avoid double-counting identical final state gluons.

$(5.7\%)^*$  † QCD corrections enhance  $\Gamma(h \rightarrow gg)$  by  $\sim 60\%$

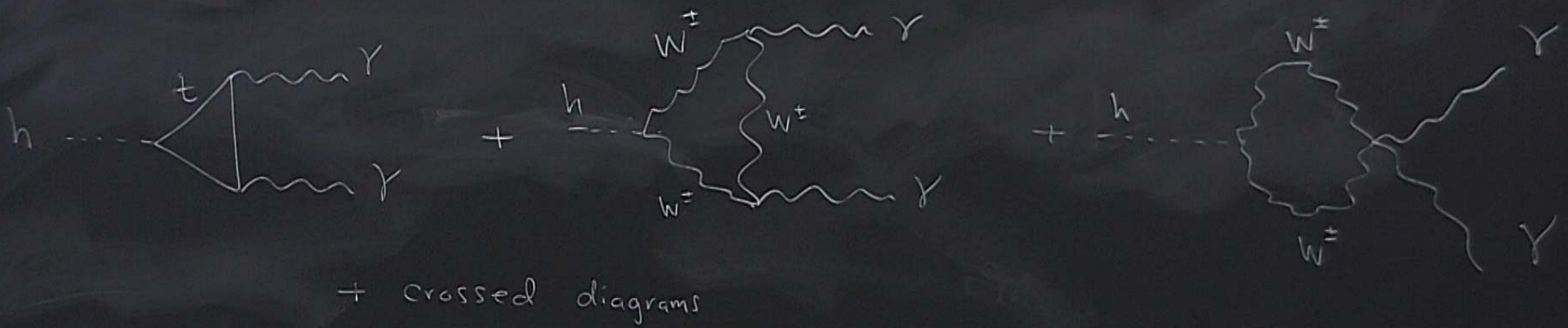
Light quarks:  $m_q = m_u, m_d, m_s, m_c, m_b \ll m_h$  if  $m_q \gg m_h$  ( $q=t$ )

$$\int_0^1 dx \int_0^{1-x} dz \frac{1-4xz}{1-xz(m_h^2/m_q^2)} = \begin{cases} 1/3 & \text{if } m_q \gg m_h \\ \frac{1}{2} \frac{m_q^2}{m_h^2} \log^2 \left( \frac{m_h^2}{m_q^2} \right) & \text{if } m_q \ll m_h \end{cases}$$



$$\int_0^1 dx \int_0^1 dz (1 - 4xz) = 3$$

$h \rightarrow \gamma\gamma$



$\gamma_{\mu\nu}^2$

$$\text{wavy line} = \frac{-i}{k^2 - m_W^2} \left( \gamma_{\mu\nu} - \frac{k_\mu k_\nu}{m_W^2} \right)$$

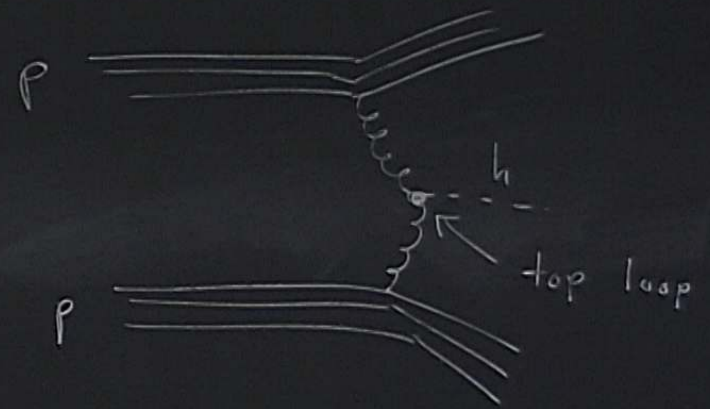
## Higgs production at colliders

LHC: pp collider at  $\sqrt{s} = 7, 8, 13$  TeV

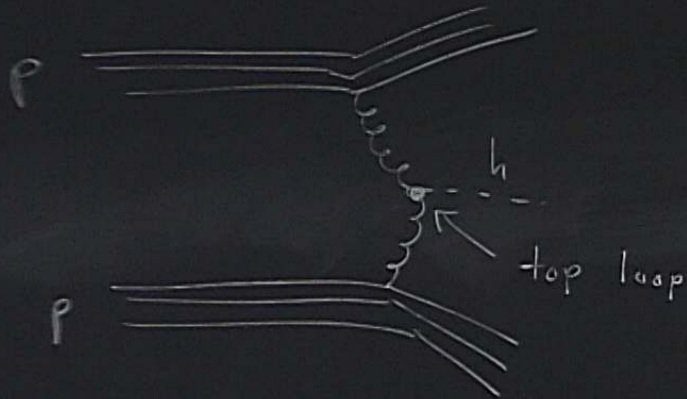
What is cross section? How many h produced?

# Production mechanisms (descending order)

1. gluon-gluon fusion (ggF)

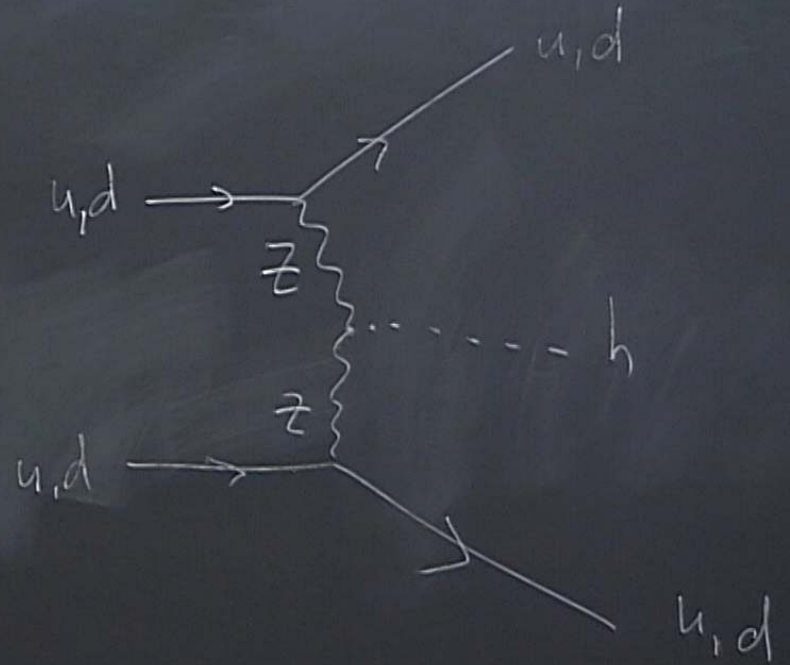
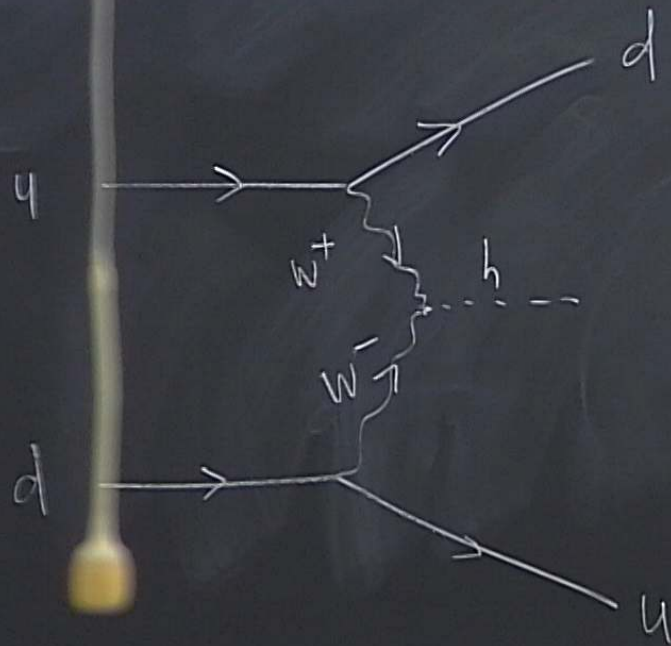


(descending order)

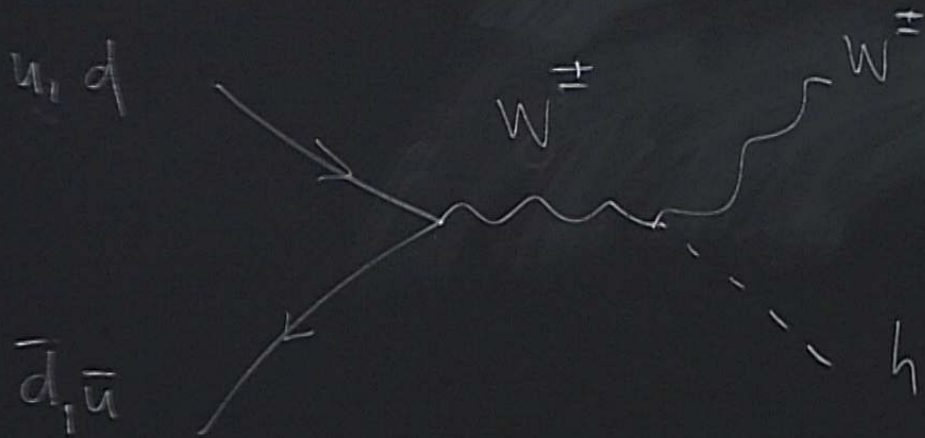


$gg \rightarrow h$  inverse decay

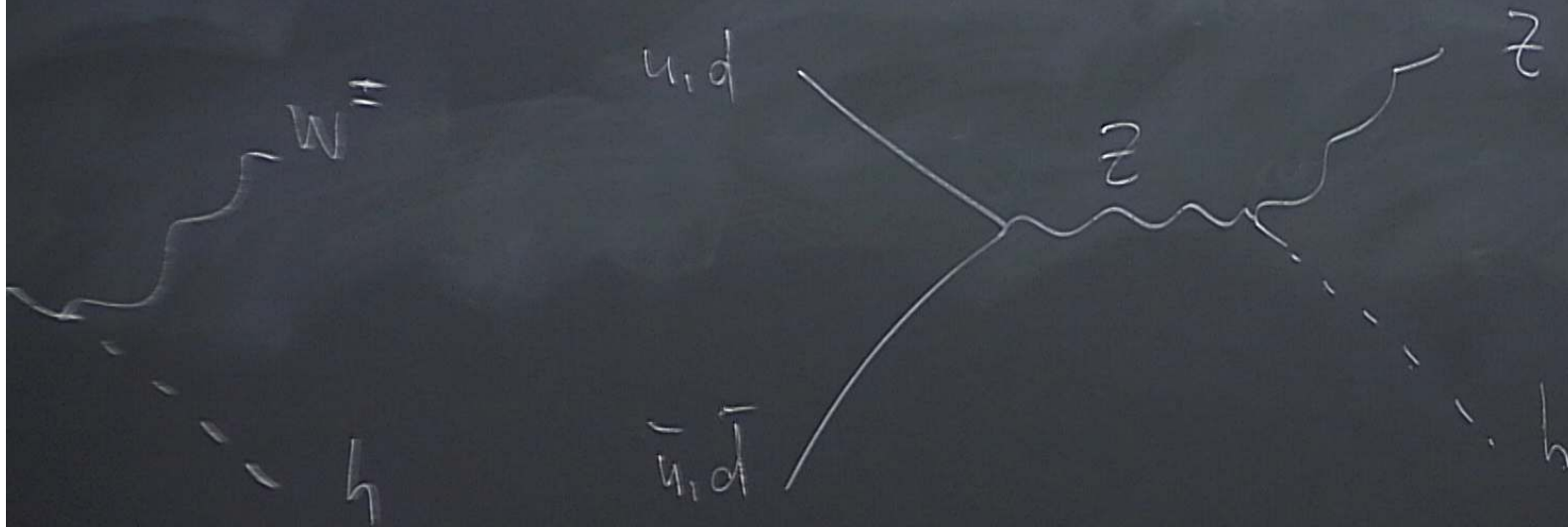
## Σ Vector boson fusion (VBF)



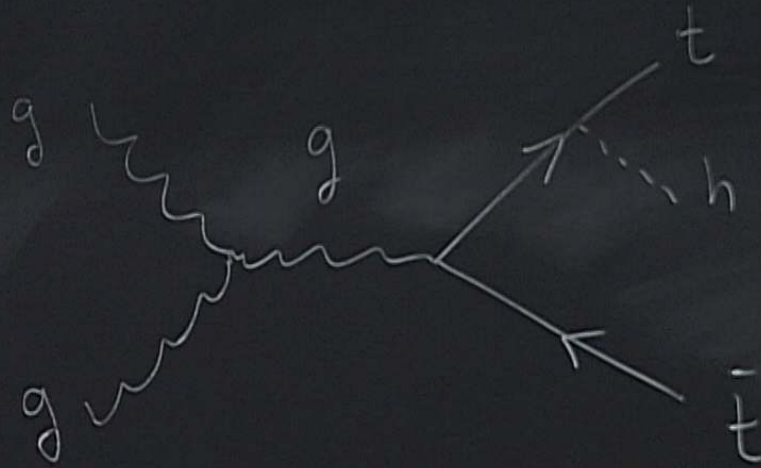
3. vector boson ( $W, Z$ ) associated production ( $WH, ZH$ )



associated production ( $WH, ZH$ )



4. top associated production ( $t\bar{t}H$ )



production ( $t\bar{t}H$ )



h w/  $t\bar{t}$  pair.

$$\hat{\sigma}(gg \rightarrow h) = \frac{1}{2E_1 \cdot 2E_2 |v_{rel}|} \int \frac{d^3q}{(2\pi)^3} \frac{1}{2E_q} (2\pi)^4 \delta^4(p_1 + p_2 - q)$$

$$(2\pi)^4 \delta^4(p_1 + p_2 - q) \left(\frac{1}{2 \cdot 8}\right)^2 \sum_{\text{spins, colors}} |\mathcal{M}(gg \rightarrow h)|^2$$

$$\hat{\sigma}(gg \rightarrow h) = \frac{1}{2E_1 \cdot 2E_2 |V_{\text{rel}}|} \int \frac{d^3q}{(2\pi)^3} \frac{1}{2E_q} (2\pi)^4 \delta^4(p_1 + p_2 - q)$$

CM frame:  $|V_{\text{rel}}| = 2$ ,  $4E_1 E_2 = \hat{s}$ ,  $E_q = m_h$

$$\hat{\sigma}(gg \rightarrow h) = \frac{1}{2 \hat{s}} \frac{1}{2m_h} (2\pi) \delta(m_h - E_1 - E_2) \frac{1}{16^2}$$

$$(2\pi)^4 \delta^4(p_1 + p_2 - q) \left(\frac{1}{2 \cdot 8}\right)^2 \sum_{\text{spins, colors}} |\mathcal{M}(gg \rightarrow h)|^2$$

$$E_g = m_h$$

$$(m_h - E_1 - E_2) \frac{1}{16^2} 2 \sum |\mathcal{M}(h \rightarrow gg)|^2$$

$$\hat{\sigma}(gg \rightarrow h) = \frac{1}{2E_1 \cdot 2E_2 |v_{rel}|} \int \frac{d^3q}{(2\pi)^3} \frac{1}{2E_q} (2\pi)^4 \delta^4(p_1 + p_2 - p_h)$$

CM frame:  $|v_{rel}| = 2$ ,  $4E_1 E_2 = \hat{s}$ ,  $E_q = m_h$

$$\hat{\sigma}(gg \rightarrow h) = \frac{1}{2 \hat{s}} \frac{1}{2m_h} (2\pi) \delta(m_h - E_1 - E_2) \frac{1}{16}$$

$$\Gamma(h \rightarrow gg) = \frac{1}{16\pi m_h} \sum |M(h \rightarrow gg)|^2$$

$$\hat{\sigma}(gg \rightarrow h) = \frac{2 \cdot 8\pi^2 \Gamma(h \rightarrow gg)}{16^2 \hat{s}} \delta(m_h - \underbrace{(E_1 + E_2)}_{\sqrt{\hat{s}}})$$

$$= \frac{\pi^2 \Gamma(h \rightarrow gg)}{16^2 \hat{s}} \delta(\sqrt{\hat{s}} - m_h)$$

$$\delta(\sqrt{\hat{S}} - m_h) = \delta(\hat{S} - m_h^2) 2\sqrt{\hat{S}} = 2m_h \delta(\hat{S} - m_h^2)$$

$$\hat{\sigma}(gg \rightarrow h) = \frac{2 \cdot 8\pi^2 \Gamma(h \rightarrow gg)}{16^2 \hat{s}} \delta\left(m_h - \underbrace{(E_1 + E_2)}_{\sqrt{\hat{s}}}\right)$$

$$= \frac{\pi^2 \Gamma(h \rightarrow gg)}{16 \hat{s}} \delta(\sqrt{\hat{s}} - m_h)$$

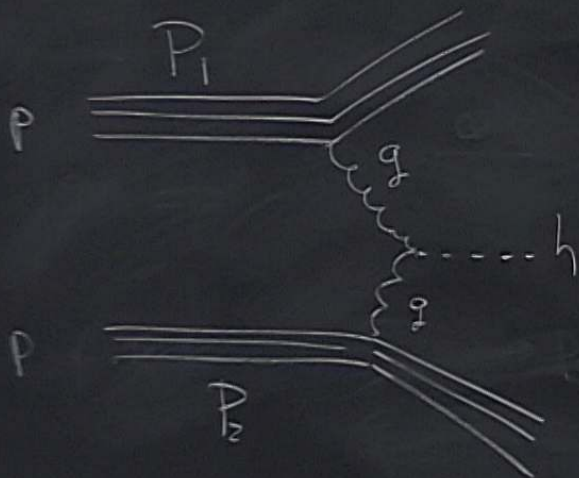
$$= \frac{\pi^2 \Gamma(h \rightarrow gg)}{8 m_h} \delta\left(\frac{\hat{s}}{m_h^2} - m_h\right)$$

$$\delta(\sqrt{\hat{S}} - mh) = \delta(\hat{S} - m_h^2) 2\sqrt{\hat{S}} = 2mh \delta(\hat{S} - m_h^2)$$

$$\hat{S} = m_h^2$$

$\sigma_{MH}$

Hadron level cross section:  $pp \rightarrow hX$   
anything in hadronic final states.



$pp \rightarrow hX$   
anything in hadronic final states.

$$\sigma(pp \rightarrow hX) = \int_0^1 dx_1 \int_0^1 dx_2 f_g(x_1) f_g(x_2) \hat{\sigma}(gg \rightarrow h)$$

$P_{1,2}$  = initial proton momenta.

$p_{1,2}$  = initial parton (gluon) momenta.

$x_{1,2}$  = momentum fractions  $p_{1,2}^\mu = x_{1,2} P_{1,2}^\mu$

Relate  $\hat{S}$  to  $S = (P_1 + P_2)^2 = 2P_1 \cdot P_2$

$$= x_1 x_2 \underbrace{\partial p_1 \cdot p_2}_{\hat{S}} = x_1 x_2 \hat{S}$$

Relate  $\hat{S}$  to  $S = (P_1 + P_2)^2 = 2 P_1 \cdot P_2$  (neg)

$$= x_1 x_2 \underbrace{\partial p_1 \cdot p_2}_{\hat{S}} = x_1 x_2 \hat{S}$$

$$\sigma(pp \rightarrow hX) = \int_0^1 dx_1 f_g(x_1) \int_0^1 dx_2 f_g(x_2) \frac{\pi^2 \Gamma(h \rightarrow gg)}{8mh}$$

$$\hat{S} \text{ to } \hat{S} = (p_1 + p_2)^2 = 2 p_1 \cdot p_2 \quad (\text{neg})$$

$$= x_1 x_2 \underbrace{2 p_1 \cdot p_2}_S = x_1 x_2 S$$

$$\rightarrow hX) = \int_0^1 dx_1 f_g(x_1) \int_0^1 dx_2 f_g(x_2)$$

$$\frac{\pi^2 \Gamma(h \rightarrow gg)}{8 m h}$$

$$\underbrace{\sigma P_1 = P_2 = x_1 x_2 S}_{S}$$

$$\int_a^b dx_2 f_g(x_2) \frac{\pi^2 \Gamma(h \rightarrow gg)}{\delta m_h} \delta \left( \underbrace{x_1 x_2 S}_{\hat{s}} - m_h^2 \right)$$

production (WH, ZH)

Define  $\tau = m_h^2/s$ .

$$\delta(x_1, x_2 s - m_h^2) = \frac{1}{s} \delta(x_1 x_2 - \tau) = \frac{1}{s x_1} \delta(x_2 - \frac{\tau}{x_1})$$

Must have:  $0 \leq x_2 \leq 1 \rightarrow 0 \leq \frac{\tau}{x_1} \leq 1 \rightarrow 0 \leq \tau \leq x_1$

In general:  $0 \leq x_1 \leq 1 \rightarrow \tau \leq x_1 \leq 1$

$$\sigma(pp \rightarrow h X) = \int_{\tau}^1 \frac{dx_1}{x_1} f_g(x_1) f_g(\tau/x_1) \frac{\pi^2 \Gamma(h \rightarrow gg)}{8 m_h s}$$

$f_g(x)$  fit to data.

$$f_g(x) = \frac{8}{x} (1-x)^7$$

Peskin & Schroeder ansatz.

$\sigma_{th}$

At LHC (pp)

P&S ansatz (Lo)

Actual  $f_g(x)$  (Lo)

$\sqrt{s} = 7 \text{ TeV}$

5.3 pb

10.5 pb

6.8 pb

11.4

8 TeV

15.7 pb

14.8

13 TeV

Actual  $f_g(x)$  (Lo)

10.5 pb

11.4

14.8

Actual  $f_g$  (NHEO in  $\alpha$ 's)

15.1 pb

19.3

43.9

(pp)

P&S ansatz (LO)

Actual  $f_g(x)$  (LO)

TeV

5.3 pb

10.5 pb

6.8 pb

11.4

TeV

15.7 pb

14.8

TeV

$$1 \text{ barn} = 10^{-24} \text{ cm}^2, \quad \text{pb} = 10^{-12} \text{ barn} = 10^{-36} \text{ cm}^2$$