

Title: Prospects for cosmological collider physics

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Abstract: <p>If heavy fields are present during inflation, they can leave an imprint in late-time cosmological observables. The main signature of these fields is a small amount of distinctly shaped non-Gaussianity, which if detected, would provide a wealth of information about the particle spectrum of the inflationary Universe. Here we investigate to what extent these signatures can be detected or constrained using futuristic 21-cm surveys. This part of my talk is based on 1610.06559. In the second part of my talk I will discuss how non-adiabatic production of heavy particles, as recently studied in 1606.00513, can generate an interesting and so far unconstrained class of non-Gaussianity in the CMB. </p>

# Prospects for cosmological collider physics

Moritz Münchmeyer, Perimeter Institute

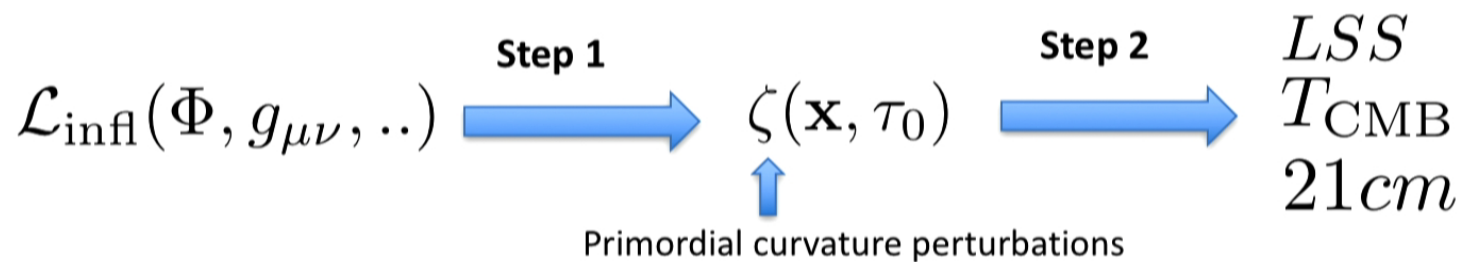
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# From inflation interactions to cosmology

We assume that the primordial density fluctuations are created during inflation.

Primordial non-gaussianities are a **measure of interactions during inflation**.

non-Gaussianity  $\longleftrightarrow$  Connected n-point functions  $\longleftrightarrow$  Interactions of primordial fields



QFT correlators in the sky (in principle)!!!

# Bispectrum basics

Here we are mostly interested in the 3-point function (bispectrum) of curvature perturbations

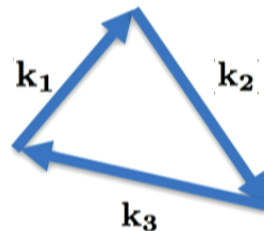
$$\langle \zeta(\mathbf{k}_1) \zeta(\mathbf{k}_2) \zeta(\mathbf{k}_3) \rangle = (2\pi)^3 \delta(\mathbf{k}_{1,2,3}) B(k_1, k_2, k_3)$$

We also define the bispectrum “shape function”

$$S(k_1, k_2, k_3) = \frac{1}{N} (k_1 k_2 k_3)^2 B(k_1, k_2, k_3)$$

Statistical isotropy and homogeneity forces  $k_1, k_2, k_3$  to form a triangle.

**equilateral triangles**



**“equilateral non-Gaussianity”**

**squeezed triangles**



**“local non-Gaussianity”**

So far, all primordial bispectrum searches are consistent with zero.



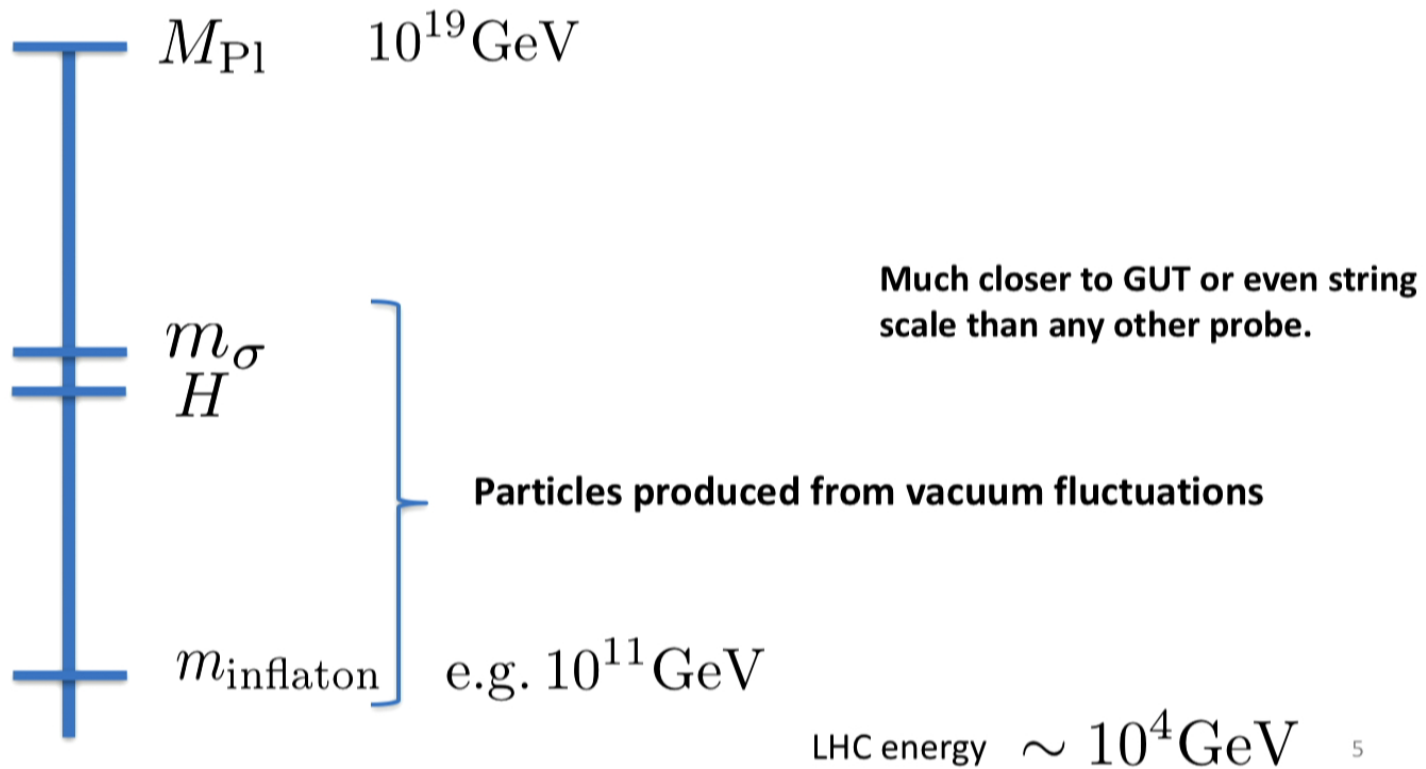
# COSMOLOGICAL COLLIDER PHYSICS

Based on **1610.06559** with Daan Meerburg, Julian Munoz, Xingang Chen

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# Energy scales

Inflation is the highest energy particle collider (indirectly) available to us, probably forever. → We need to **read off the results as precisely as possible**.



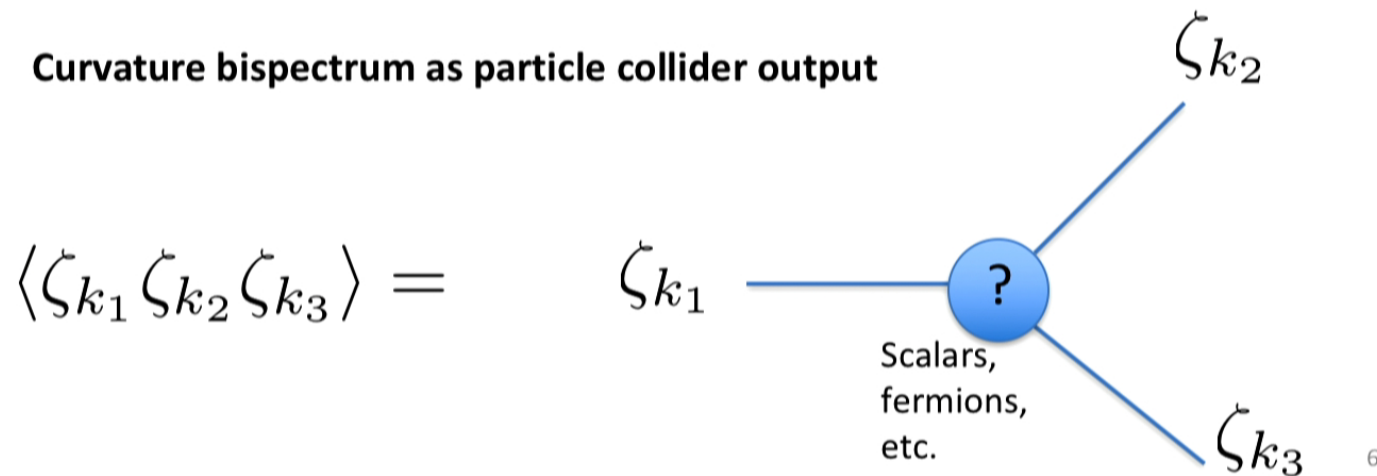
# Theoretical Motivation

The inflationary particle collider in principle probes several orders of magnitude in energy from  $m_{\text{inflation}}$  to  $> H$ .

String theory models strongly suggest many fields. Single field inflation is not natural in this sense.

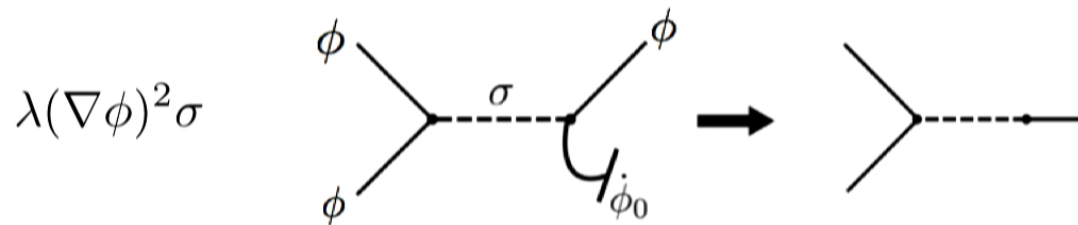
Supersymmetry at order  $H$  to partially protect the slow roll potential suggests super-partners in this energy range.

Curvature bispectrum as particle collider output

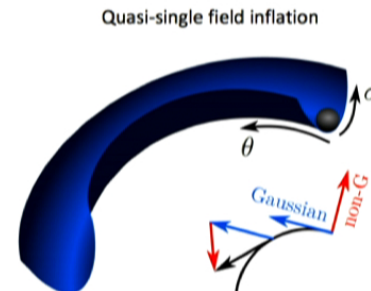
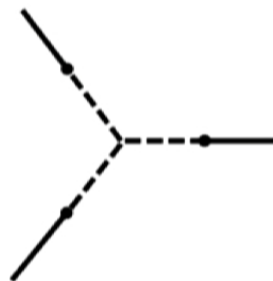


# Two example processes

Derivative 3pt vertex: Arkani-Hamed, Maldacena 2015



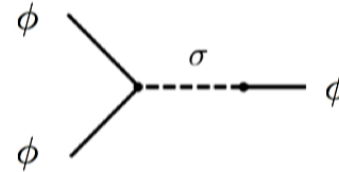
Bilinear term mediates large self-interactions of  $\sigma$  (quasi single field inflation, [Chen/Wang 2010](#)).



More generally: all diagrams from cubic coupling and bilinear mixing term.

# Primordial bispectrum for AHM model

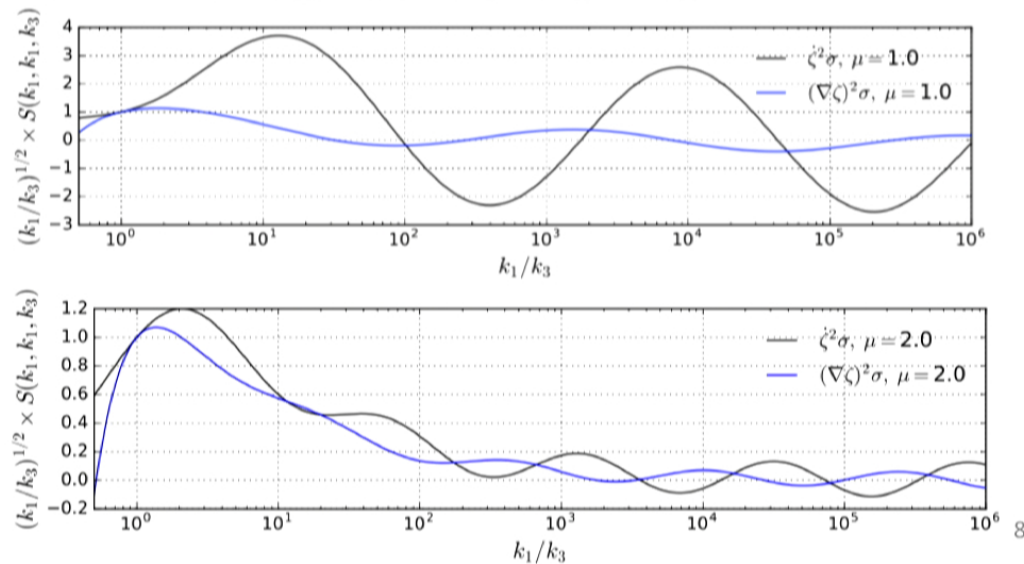
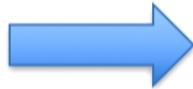
Basis: 2<sup>nd</sup> order in-in perturbation theory



Contains double integrals over Hankel functions, e.g.

$$\int_{-\infty}^0 dx x^{(3/2)} e^{\alpha x} H_{i\mu}^{(1)}(ix) \int_{-\infty}^x dy y^{(-1/2)} e^y H_{i\mu}^{(2)}(iy)$$

(use Wick rotation for numerical convergence (Chen/Wang 2015))



Mass parameter

$$\mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}}$$

# Model independent squeezed limit

## Basic physical reason for squeezed limit behavior

After horizon crossing, massive fields decay and for large  $m$  also oscillate:

$$(\pm\tau)^{3/2\pm i\mu} \text{ where } \mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}}$$

Therefore when the short modes cross the horizon, the amplitude of the long mode is suppressed in a specific way.



## Squeezed limit encodes the mass spectrum

A-H/M, Chen/Wang, Assassi/Baumann/Green

$$S_{\text{squeezed}} \propto \left( \frac{k_{\text{long}}}{k_{\text{short}}} \right)^{1/2\pm i\mu}$$

2 cases:  $\mu$  real or imaginary  oscillation or scaling

Squeezed limit is more generic than equilateral contribution and contains a mass measurement. Acts like a “cosmological collider”.

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# High mass oscillating template

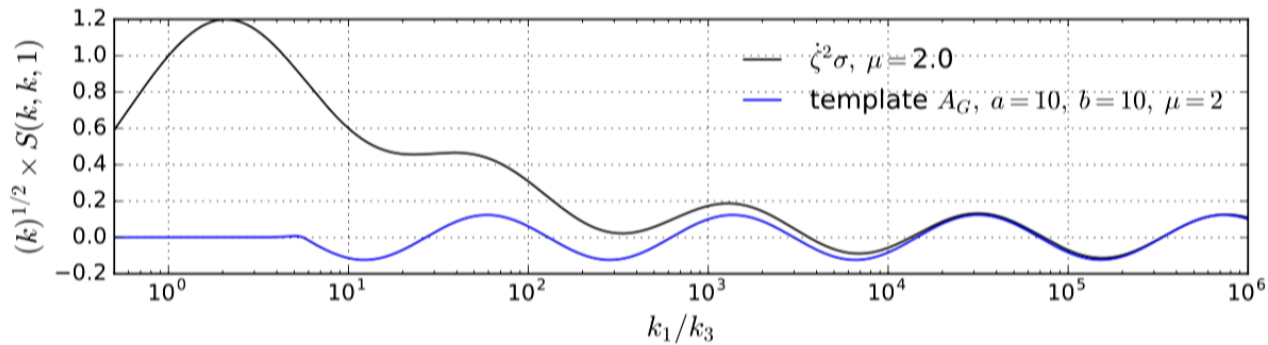
$$S^{\text{clock}}(k_1, k_2, k_3) = f_{\text{NL}} A \left( \frac{k_1 + k_2}{k_3} \right) \left( \frac{k_1 + k_2}{k_3} \right)^{-1/2} \times \sin \left( \mu \ln \left( \frac{k_1 + k_2}{2k_3} \right) + \delta \right) + 2 \text{ perm}$$

amplitude

Gauss-type window  
function to cut off  
equilateral contribution

Squeezed limit oscillations

Mass parameter  $\mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}}$



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# Low mass scaling template

Low mass “intermediate” template was given by [Chen&Wang in 0909.0496](#)

$$S^{\text{int}}(k_1, k_2, k_3) = f_{\text{NL}} A(k_1, k_2, k_3) \frac{3^{\frac{9}{2}-3\nu}}{10} \frac{k_1^2 + k_2^2 + k_3^2}{(k_1 + k_2 + k_3)^{\frac{7}{2}-3\nu}} (k_1 k_2 k_3)^{\frac{1}{2}-\nu}$$

$$\text{Mass parameter} \quad \nu \equiv \sqrt{(9/4) - (m/H)^2} = -i\mu \quad 0 < \nu < 3/2$$

$$\text{squeezed limit } k_3 \ll k_1 = k_2, S^{\text{int}} \sim (k_3/k_1)^{\frac{1}{2}-\nu}$$

## Scaling regions:

- For small  $m$ : scales like local NG (as multi-field inflation should)

$$S^{\text{loc.}} \sim (k_3/k_1)^{-1}$$

- For larger  $m$ : interpolates towards equilateral NG

$$S^{\text{equi.}} \sim k_3/k_1$$



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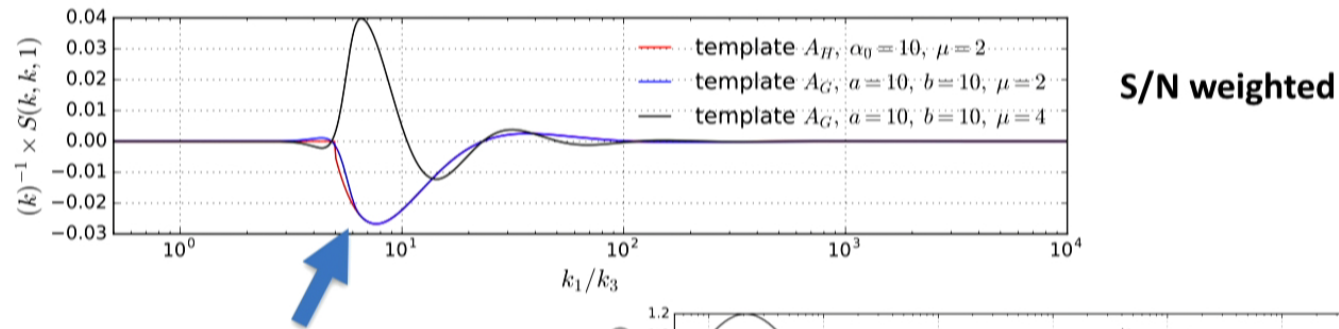
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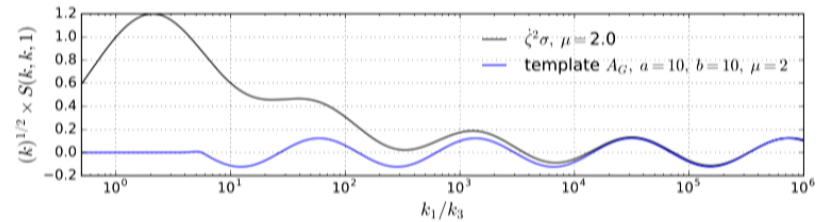
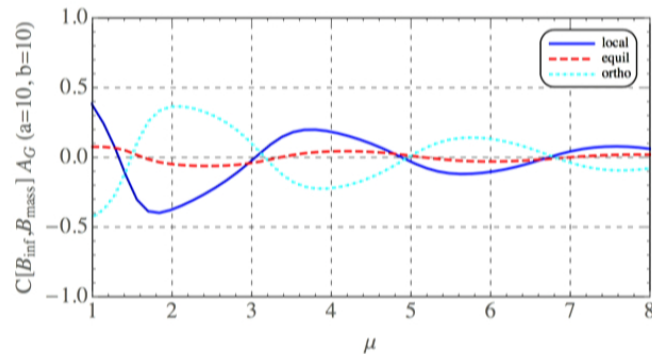
# How much phase space to cut off?

**Objectives:** Avoid equilateral bump, keep template accurate, get as much signal as possible

Cutoff depends on NG from self interactions. We chose a compromise.




Most signal is in the first peak.



# Outlook: Detecting spin

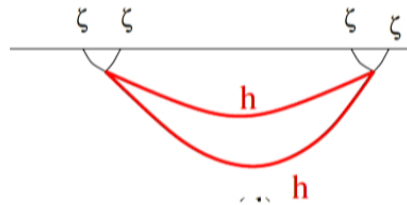
The squeezed limit also tells us about the spin of massive particles!

$$S \propto \left( \frac{k_{\text{long}}}{k_{\text{short}}} \right)^{1/2 \pm \mu} P_s(\cos \Theta)$$



spin                  Angle between  $k_l$  and  $k_s$

Arkani-Hamed, Maldacena 2015 . Extended in Lee, Baumann, Pimentel 2016



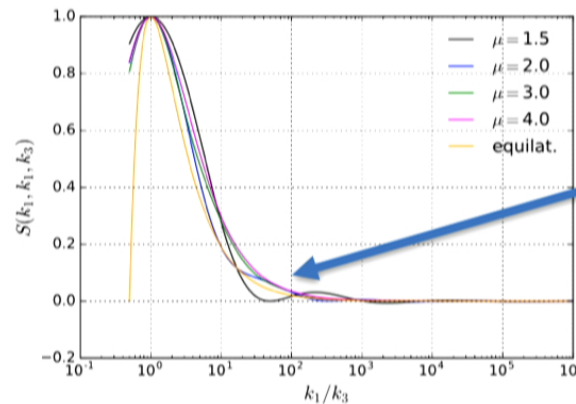
**String theorists dream: Find a particle with  $\text{spin} > 2$ .**

**Not generally predicted by string inflation, but we are way closer to the string energy scale than with any other probe.**

## How about a CMB analysis?

- For the non-oscillating case, this has already been done in [Planck NG 2015](#)
- For the oscillating case the overlap of the full shape with equilateral is large ( $C \sim 0.9$ ).
- Therefore for the oscillating shape a search for the collider signal only makes sense **after equilateral non-Gaussianity has been detected**.

AHM example



Oscillations are  
Boltzmann suppressed  
 $e^{-\frac{\mu}{H}}$

**This does not look good in the near term. But given the very exciting signal we won't give up that quickly. We need a much better probe than CMB!**

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# **A FORECAST FOR 21CM FROM THE DARK AGES**

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# 21 cm signal from the dark ages

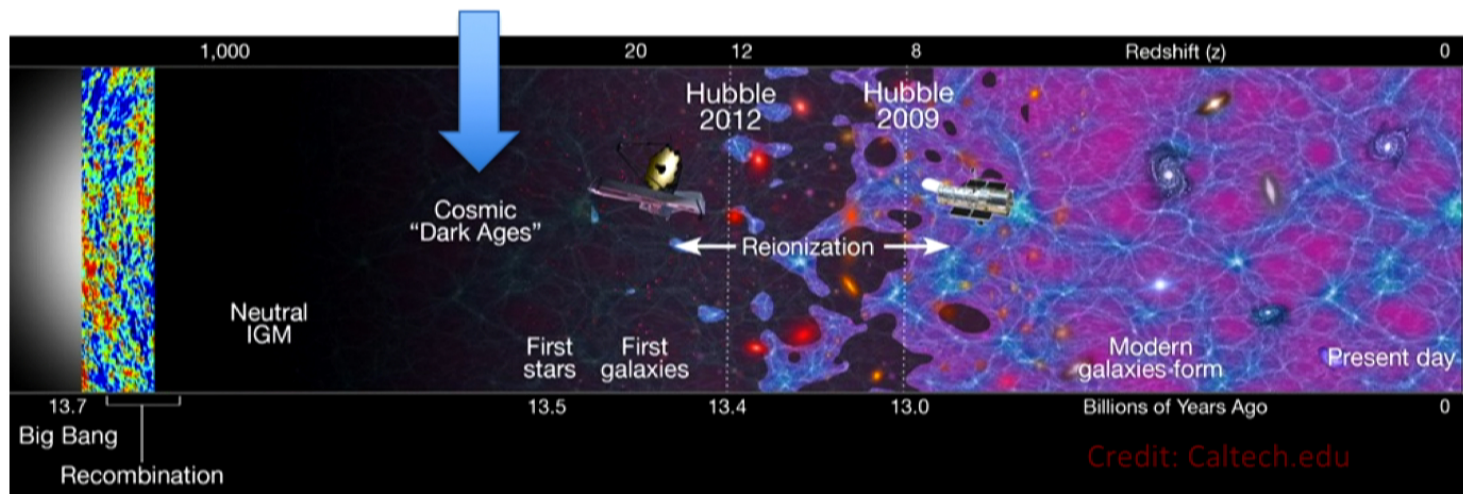
## 21cm tomography prior to structure formation

Ideal probe for inflationary physics: Very large number of Fourier modes, perturbative regime. [Zaldarriaga, Loeb 2004](#)

**Origin:** Cosmic neutral hydrogen prior to star formation maps the matter density.

→ Absorption of CMB photons at 21cm spin flip transition.

→ 21cm radiation anisotropies today at wave length  $21.12[(1+z)/100]m$



# What kind of experiment would we need?

## Mode counting

$$k \sim 10^{-4} \text{Mpc}^{-1} \text{ to } k \sim 10^2 \text{Mpc}^{-1}$$

$$\sigma_a \sim \sqrt{\left(\frac{k_{\min}}{k_{\max}}\right)^3}$$

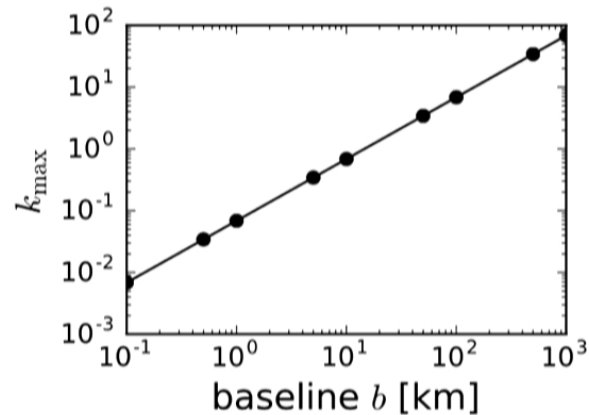
## Radial (Frequency) resolution

We assume  $30 < z < 100$

$$\frac{\delta\nu}{\nu} = \frac{\Delta z}{z+1}$$

## Angular resolution limited by size (baseline) of experiment

$$k_{\max} \simeq 2\pi\nu_0 b \frac{1}{d(z)(1+z)} \frac{1}{c}$$



We assume that the radial resolution matches the angular resolution

# Projecting to the 21cm signal

We use linear perturbation theory and assume that the 21cm signal traces the matter perturbations.

$$\langle \delta T_{21}(\mathbf{k}_1) \delta T_{21}(\mathbf{k}_2) \delta T_{21}(\mathbf{k}_3) \rangle = (2\pi)^3 \delta_D(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) \times B_{\delta T}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$$

## Secondary Non-Gaussianity

- Main sources
  - 21cm temperature depends non-linearly on baryon density and velocity
  - Gravitational interactions create non-Gaussianity
- **Our approach:** We used **templates** from [Munoz et al 2015](#) that parametrize these effects to second order in  $\delta_b$  and  $\delta_v$ . We found  $\mathcal{O}(1)$  changes in sensitivity for test cases.
- In principle N-body sims can determine these effects well (no complicated feedback mechanisms).



# Noise and foregrounds

## Foregrounds

- **Atmosphere partially opaque** at these frequencies  
→ Often the moon is advocated as a possible location
- Noise amplitude many orders of magnitude larger than signal amplitude. Especially **galactic synchrotron radiation**.
- But: **synchrotron is much more smooth in frequency than signal**. Component separation is theoretically possible.
- We assume that one can completely subtract the foregrounds.

We do a cosmic variance limited forecast  
(a very futuristic assumption)

# Rough size of non-Gaussianities

## Gravitational coupling (minimal case)

Heavy fields couple to inflaton only through gravity.  $f_{\text{NL}} \ll 10^{-2}$

Loop corrections to the bispectrum.

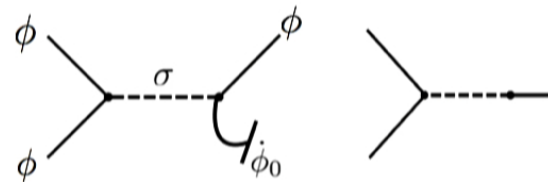
## Direct coupling of heavy fields and inflaton

In principle up to  $f_{\text{NL}} < \mathcal{O}(1)$

(limited by perturbative control)

AHM

$$f_{\text{NL}} \sim \epsilon M_{\text{Pl}}^2 \lambda^2$$



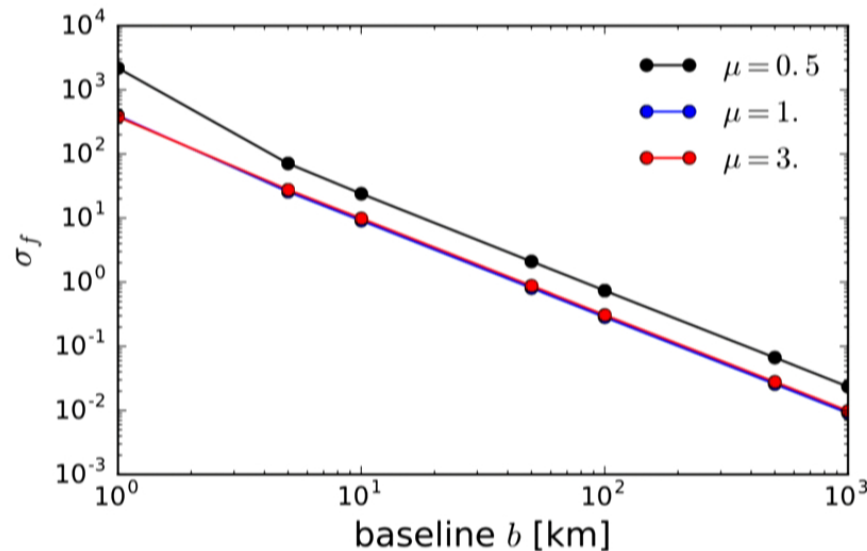
## Self interactions of heavy fields and direct coupling

e.g. Chen/Wang QSFI  $f_{\text{NL}} \gtrsim \mathcal{O}(1)$



This is valid for  $\text{mass} \lesssim \mathcal{O}(H)$ . Above that there is a **Boltzmann factor**, giving exponential suppression.  $e^{-\frac{\mu}{H}}$

## Results for the oscillating template $m > H$



We assume fixed cosmology and do not marginalize over secondary non-Gaussianity.

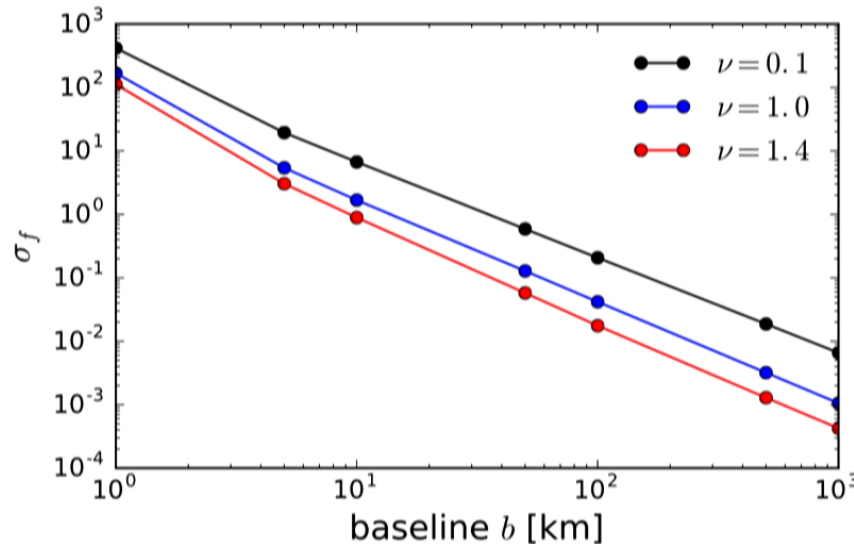
Red shift range:  $30 < z < 100$

$$\mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}}$$

### Rough interpretation:

- Sensitivity almost mass independent (no Boltzmann suppression in our template)
- With an array of O(10) km one can probe O(1) self interactions.
- With an array of O(100) km, one can probe models with direct coupling.
- The AHM amplitude is only realistic if the operator is not Planck suppressed

## Results for the non-oscillating template $m < H$



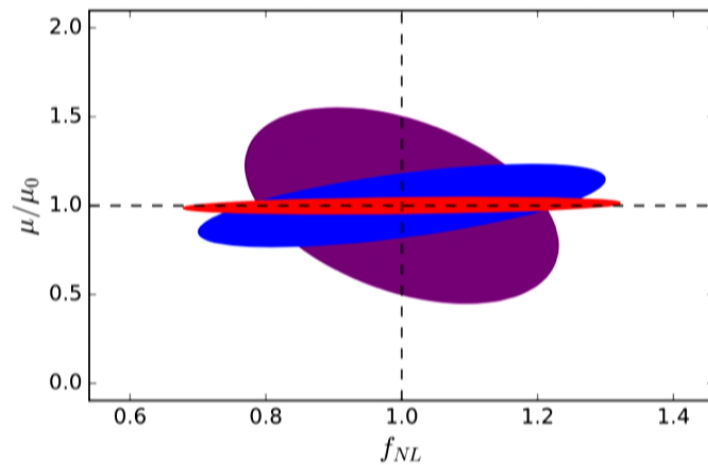
$$\nu \equiv \sqrt{(9/4) - (m/H)^2}$$

Smaller  $\nu$  means larger mass

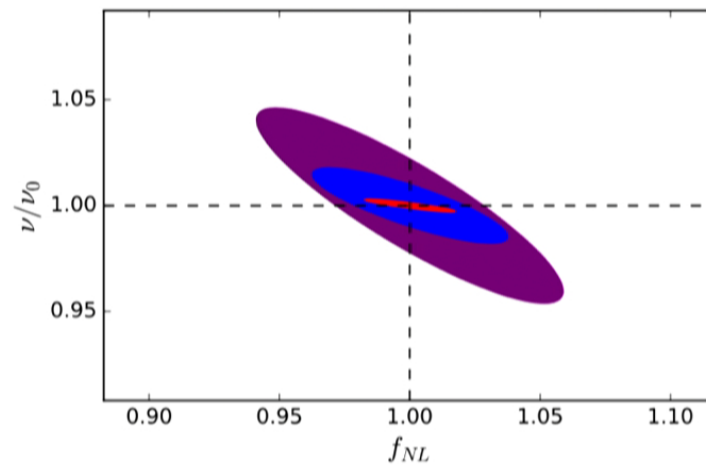
### Rough interpretation:

- Sensitivity is mass dependent because scaling because the scaling in the squeezed limit is mass dependent
- Sensitivity can be 1-2 orders of magnitude better than in the oscillating case.
- For low masses a 10 km array would already give interesting constraints

# Mass determination



$\mu = 0.7$  (purple),  $\mu = 1.0$  (blue),  $\mu = 3.0$  (red)



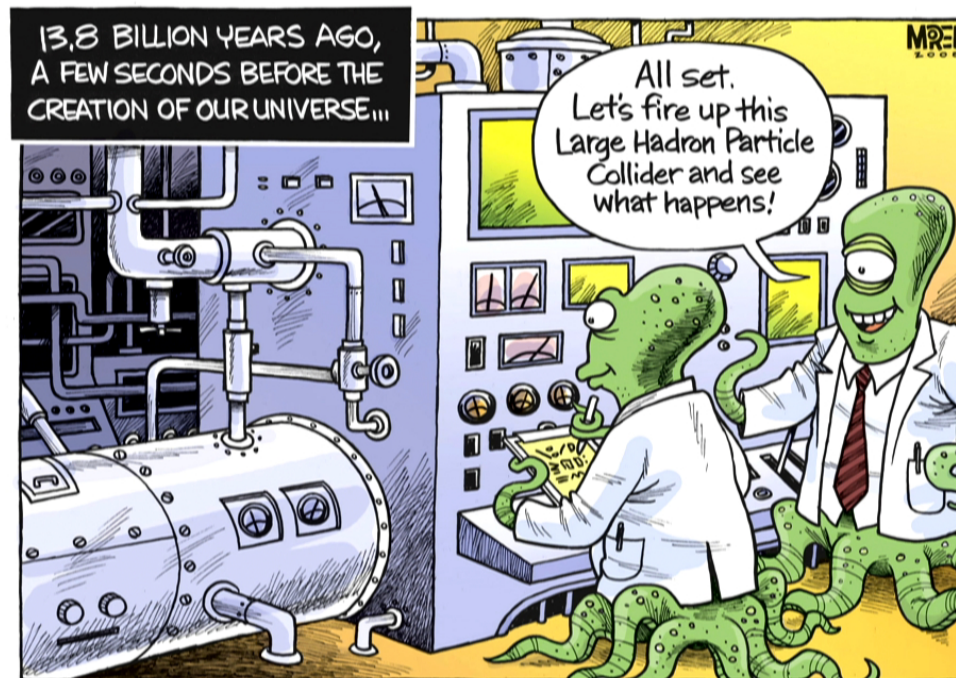
$\nu = 0.8$  (purple),  $\nu = 1.0$  (blue),  $\nu = 1.4$  (red)

**Test case:  $f_{NL} = 1$ , baseline = 100 km**

Under these fortunate assumptions one could measure even a spectrum of particles with well determined masses.

# Prospects for cosmological collider physics?

It seems that in the time frame of decades there is a fair chance, but in the near term there is little chance, because of known limits on local and equilateral NG.



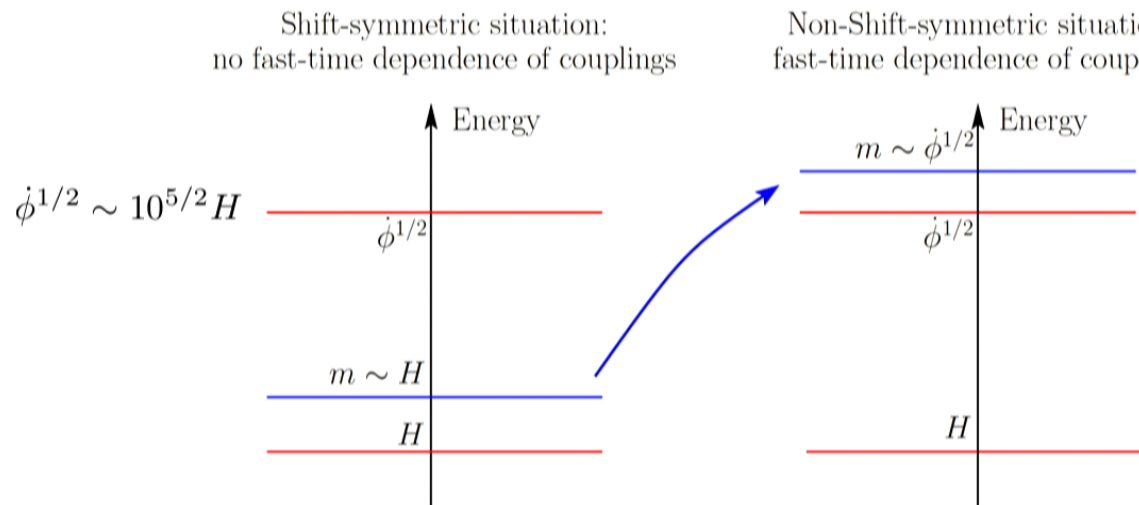
# NON-ADIABATIC HEAVY PARTICLE PRODUCTION

Theoretical model **1606.00513** by Flauger, Mirbabayi, Senatore, Silverstein  
Data analysis ideas from unpublished work MM, Senatore, Silverstein

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# Non-adiabatic particle production

- **Previous part of the talk: slow-roll background and time independent coupling constants.**
- If we relax these assumptions, we get very a different phenomenology.
- **This section of the talk: heavy particles with time dependent mass functions, but inflaton background dynamics are still slow roll.**



Source: Flauger et al 2016

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## 2 classes of mass functions $m_\chi$

### Regular case (discrete shift symmetry)

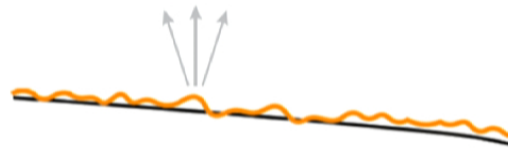
- Shift symmetry  $\Phi \rightarrow \Phi + \text{const.}$  to protect inflaton potential from corrections

$$\Delta\mathcal{L} = \frac{\mathcal{O}_\Delta}{\Lambda^{\Delta-4}} \quad \Lambda : \text{UV scale} \quad \Delta : \text{Operator dimension}$$

- Discrete version  $\varphi \rightarrow \varphi + 2\pi f$ . e.g small sine one top of potential
- In our case e.g.:  $m_\chi^2 = m_0^2 + g^2 \sin\left(\frac{\phi}{f}\right)$  or more “Fourier components”

### Disordered case

Maybe the microphysics in the UV is very complicated, masses and couplings fluctuate stochastically



Source: [Amin, Baumann 2016](#)

# Non-adiabatic particle production

Inflaton background (or time) dependent mass term

$$m_\chi(\phi)^2 \chi^2$$

EOM of the massive field  $\chi$

$$\ddot{\psi}_k + 3H\dot{\psi}_k + \omega_k^2 \psi_k = 0 \quad \omega_k^2 = \mu^2 + \Delta m(t)^2 + (k/a)^2$$

**Particle production** happens when the evolution becomes non-adiabatic

$$|\dot{\omega}_k| > \omega_k^2$$

In this case the **adiabatic vacuum (WKB) is no longer valid** and the particle number  $n_k$  not conserved. (**as in preheating**)

If UV physics is complicated, with many fields and couplings, this condition might arrive generically.



A concrete UV model where this happens is axion monodromy.

# Concrete example from axion monodromy

Coupling **heavy fields via field dependent mass**

$$V(\chi_I, \phi) \simeq \sum_I \frac{1}{2} m_{\chi_I}(\phi)^2 \chi_I^2 + V_0(\phi)$$

Axion monodromy includes two sectors of this type:

- Case 2a  $\mathcal{L}_m = \sum_n \frac{1}{2} \chi^2 (\mu^2 + g^2 (\phi - 2\pi n f)^2)$  
- Case 2b  $\mathcal{L}_m = \frac{1}{2} \chi^2 (\mu^2 + 2g^2 f^2 \cos \frac{\phi}{f})$  

Near production:  $m_\chi^2 = m_0^2 + g^2 \dot{\phi}^2 (t - t_n)$

Source: Flauger et al 2016



These fields are generally included in the theory and their effects **can be large enough to be observable in the CMB.**

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# Calculating n-point functions

Particle production + coupling term --> curvature perturbation source J

$$J = \chi^2 \frac{\delta}{\delta\phi} m_\chi^2$$

Calculate n-pt function of the sources, e.g.  $\langle JJJ \rangle$

and from that the **inflaton/curvature n-point functions**

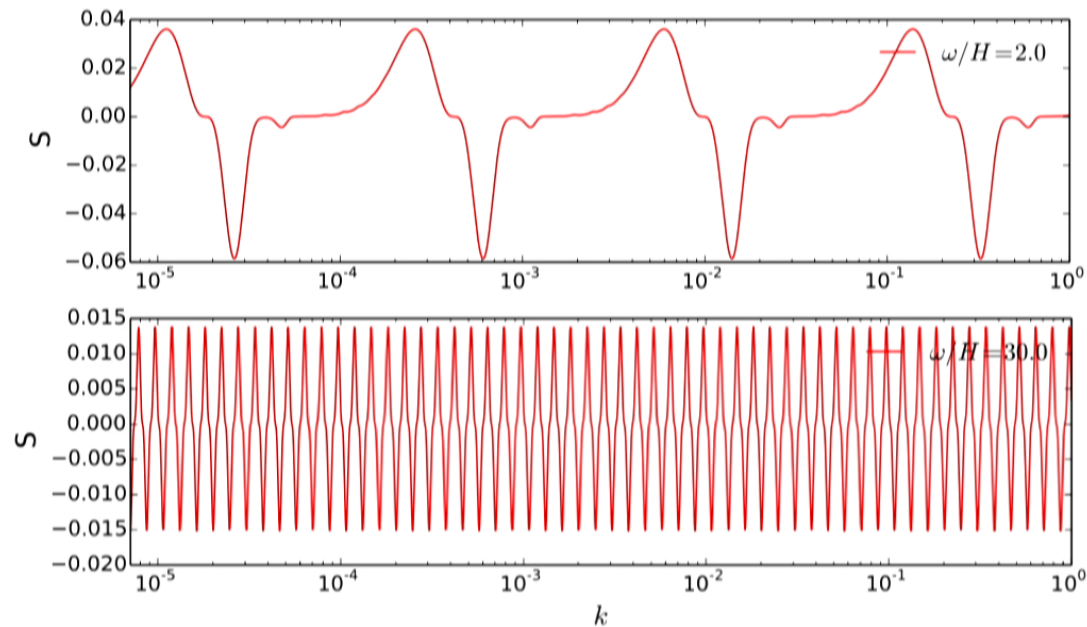
$$\langle \delta\phi_{\mathbf{k}_1} \dots \delta\phi_{\mathbf{k}_N} \rangle \sim (2\pi)^3 \delta(\sum \mathbf{k}_i) \frac{\bar{n}_\chi}{H^3} H^{N+3} \sum_n (H\eta_n)^{-3} \prod_{i=1}^N \frac{\hat{h}(k_i\eta_n)}{k_i^3}$$

Besides these source terms, there are additional interference terms like X particle annihilation that also contribute.

**Interesting extension: produce fermions with this mechanism**

# Unexplored phenomenology

Primordial bispectrum example (for  $k_1=k_2=k_3=k$ ):



No significant overlap with previously examined bispectrum shapes, including resonance and feature shapes.

Can have large amplitude.

CMB analysis needed!

## Inverted signal to noise hierarchy possible

- **Normal case:** Higher N-point functions are smaller because they involve higher powers of the coupling constants (more vertices) or higher order vertices (more suppressed in EFT).
- **Present case:** In part of the parameter space the signal to noise can grow with N. This is possible because non-adiabatic production already modifies the free theory of the heavy particles.
- Roughly:  $(S/N)_N \sim \epsilon x^N$  ( $x > 1$ ,  $\epsilon < 1$ ) up to some N, e.g. O(100)
- **Interesting from a data analysis point of view:** higher N-point functions have been much less constrained. One could easily have a detection in WMAP data.

## N-point CMB estimator

- **Potential problems:** combinatoric explosion of terms in shape function, contamination by lower N-point functions (especially power spectrum), combinatoric explosion of MC estimator correction terms
- None of these are fatal for this shape (for odd N).

- Schematically

Senatore, MM, unpublished

$$M_{\{\ell, m\}}^N = M_{m_1 m_2 \dots \ell_N}^{\ell_1 \ell_2 \dots \ell_N} = \langle a_{\ell_1 m_1} a_{\ell_2 m_2} \dots a_{\ell_N m_N} \rangle_c$$

$$\mathcal{E} = \frac{1}{N!F} \sum_{\ell_i m_i} M_{\{\ell, m\}}^{N*} [(C^{-1}a)_{\ell_1 m_1} (C^{-1}a)_{\ell_2 m_2} \dots (C^{-1}a)_{\ell_N m_N}]$$

- Old KSW trick

$$\mathcal{E} = \frac{1}{N!F} \sum_q \int dr r^2 \int d\Omega (M^{N,q}(\mathbf{r}, \hat{\mathbf{r}}))^N$$

$$M^{N,q}(r, \hat{\mathbf{r}}) = \sum_{\ell_i m_i} (C^{-1}a)_{\ell_1 m_1} M_{\ell}^{N,q}(\mathbf{r}) Y_{\ell m}(\hat{\mathbf{r}})$$



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- Old KSW trick

$$\mathcal{E} = \frac{1}{N!F} \sum_q \int dr r^2 \int d\Omega (M^{N,q}(\mathbf{r}, \hat{\mathbf{r}}))^N$$

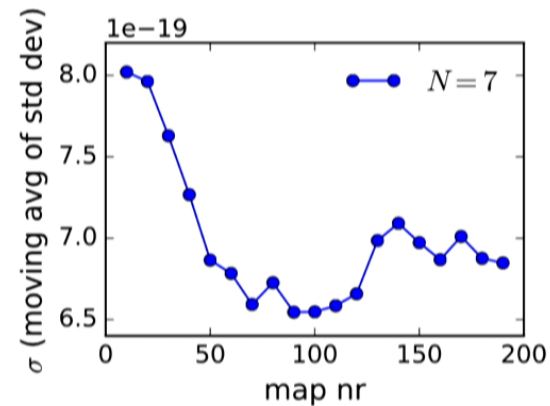
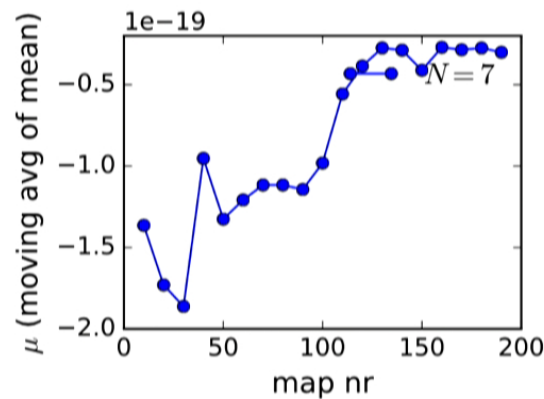
$$M^{N,q}(r, \hat{\mathbf{r}}) = \sum_{\ell_i m_i} (C^{-1}a)_{\ell_1 m_1} M_{\ell}^{N,q}(\mathbf{r}) Y_{\ell m}(\hat{\mathbf{r}})$$

# Monte Carlo Planck maps

- Shape function

$$S^N(k_1, k_2, k_3, \dots) = \frac{k_1^{i\omega/H} k_2^{i\omega/H} k_3^{i\omega/H} \dots}{(k_1 k_2 k_3 \dots)^{3(N-1)/N}} \quad (\text{approximation of the full shape})$$

- Need to scan over frequency and phase (look elsewhere effect).
- Run estimator on Planck sims



- Data results upcoming. First  $N>4$  analysis.

## Outlook: Searching for time dependent couplings

- How to search for non-Gaussianity systematically?
- Well established in the case of slow roll inflation with constant couplings. EFTI action

$$S = \int d^4x \sqrt{-g} \left[ M_{\text{Pl}}^2 \dot{H}(t + \pi) \left( \dot{\pi}^2 - \frac{(\partial_i \pi)^2}{a^2} \right) + \right. \\ \left. + M_1^4(t + \pi) (\dot{\pi}^2 + \dot{\pi}^3 + \dots) + M_2^4(t + \pi) (\dot{\pi}^3 + \dots) + M_3^4(t + \pi) (\dot{\pi}^4 + \dots) \right]$$

- Less well understood: How to look systematically for time dependent masses/couplings.
- Basic Idea ([Flauger et al.](#)): Fourier expand couplings

$$M_I^4(t) = \int d\omega e^{i\omega t} \tilde{M}_I^4(\omega) \simeq \sum_{J=-J_{\text{max}}}^{J_{\text{max}}} e^{i\Delta\omega J t} \tilde{M}_{I,J}^4$$

- BUT: large look elsewhere effect. Adiabatic and non-adiabatic effects. Higher N point functions etc. Can we be systematic?

# Conclusions

## The good side

- The weakly non-linear modes contained in the observable universe may well allow the detection of heavy particles  $m \sim H$ .
- Heavy particles are very common in UV models of inflation
- Cosmological perturbations have access to 3-5 orders of magnitude in energy, lots of room for discoveries.
- We have reviewed adiabatic and non-adiabatic particle production. The latter has unexplored phenomenology with CMB data.

## The bad side

- CMB sensitivity on equilateral non-Gaussianity will not be significantly beaten any time soon.
- 21cm mapping of the dark ages is decades away.

**We are at the beginning of cosmological collider physics.**