

Title: Single-photon test of Hyper-Complex Quantum Theories

Date: Sep 23, 2016 11:00 AM

URL: <http://pirsa.org/16090053>

Abstract: One of the most successful theories in physics until now is quantum mechanics. However, the physical origins of its mathematical structure are still under debate, and a "generalized" quantum theory to unify quantum mechanics and gravity is still missing. Recently, in an effort to better understand the mathematical structure of quantum mechanics, theories containing the essence of quantum mechanics, while also having a broader description of physical phenomena, have been proposed. These so-called "post-quantum theories" have only been recently tested at the lab. In this talk, I will present the results of our experimental test using single photons to probe one of these post-quantum theories; namely, hyper-complex quantum theories. Interestingly, in hyper-complex theories simple phases do not necessarily commute. To study this effect, we apply two physically different optical phases, one with a positive and one with a negative refractive index, to single photons inside of a Sagnac interferometer. Through our measurements we are able to put bounds on this particular prediction of hyper-complex quantum theories.

## Outline

- Motivation(QQM)
- Experimental Status
- Our proposal
- Results
- Criticism and replay
- Conclusions

# Motivation

ANNALS OF MATHEMATICS  
Vol. 37, No. 4, October, 1936



Pioneer in the foundation  
of quantum mechanics  
John von Neumann (1903-1957)

## THE LOGIC OF QUANTUM MECHANICS

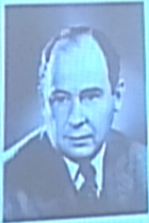
BY GARRETT BIRKHOFF AND JOHN VON NEUMANN

(Received April 4, 1936)

**1. Introduction.** One of the aspects of quantum theory which has attracted the most general attention, is the novelty of the logical notions which it presupposes. It asserts that even a complete mathematical description of a physical system  $\mathcal{S}$  does not in general enable one to predict with certainty the result

# Motivation

ANNALS OF MATHEMATICS  
Vol. 37, No. 4, October, 1936



Pioneer in the foundation  
of quantum mechanics  
John von Neumann (1903-1957)

## THE LOGIC OF QUANTUM MECHANICS

By GARRETT BIRKHOFF AND JOHN VON NEUMANN

(Received April 4, 1936)

1. Introduction. One of the aspects of quantum theory which has attracted the most general attention, is the novelty of the logical notions which it presupposes. It asserts that even a complete mathematical description of a physical system  $\mathfrak{S}$  does not in general enable one to predict with certainty the result

- Finkelstein, David, et al. "Foundations of quaternion quantum mechanics." *Journal of mathematical physics* 3.2 (1962): 207-220.
- Adler, Stephen L. *Quaternionic quantum mechanics and quantum fields*. Vol. 88. Oxford University Press on Demand, 1995.



## What are Quaternions?



The father of quaternions

William Rowan Hamilton  
(1805–1865)

They are an extension of complex numbers:

$$q = q_0 + q_1 i + q_2 j + q_3 k$$

where,

$$i^2 = j^2 = k^2 = -1, \\ ij = -ji = k.$$

## What are Quaternions?



The father of quaternions

William Rowan Hamilton  
(1805–1865)

They are an extension of complex numbers:

$$q = q_0 + q_1 i + q_2 j + q_3 k$$

where,

$$\Psi = \Psi_0 + i\Psi_1 + j\Psi_2 + k\Psi_3$$

Quaternions do not commute !!!

$$qp \neq pq$$

# Peres proposal



Pioneer of quantum information theory  
Asher Peres (1934–2005)

## PHYSICAL REVIEW LETTERS

---

---

VOLUME 42

12 MARCH 1979

NUMBER 11

---

---

### Proposed Test for Complex versus Quaternion Quantum Theory

Asher Peres

*Department of Physics, Technion-Israel Institute of Technology, Haifa, Israel*  
(Received 7 December 1978)

If scattering amplitudes are ordinary complex numbers (not quaternions) then there is a universal algebraic relationship between the six coherent cross sections of any three scatterers (taken singly and pairwise). A violation of this relationship would indicate either that scattering amplitudes are quaternions, or that the superposition principle fails. Some experimental tests are proposed, involving neutron diffraction by crystals made of three different isotopes, neutron interferometry, and  $K_s$ -meson regeneration.

# Peres proposal



Pioneer of quantum information theory  
Asher Peres (1934–2005)

## PHYSICAL REVIEW LETTERS

VOLUME 42

12 MARCH 1979

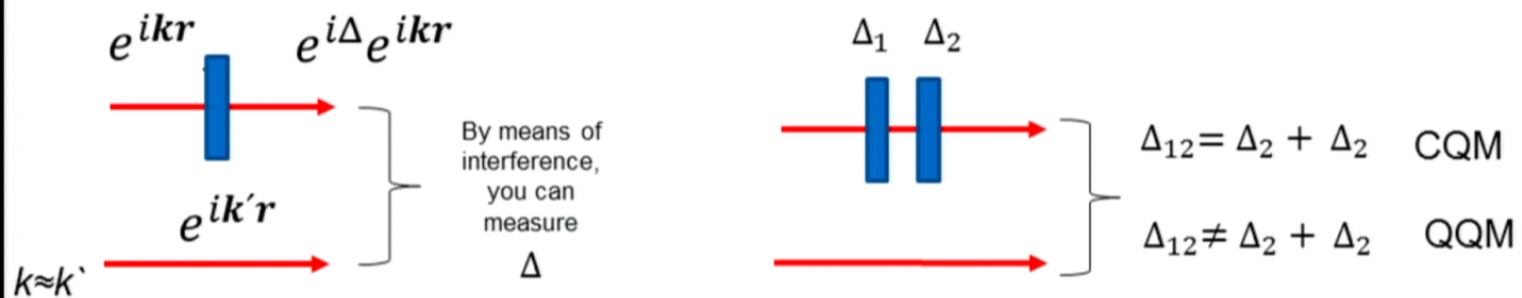
NUMBER 11

### Proposed Test for Complex versus Quaternion Quantum Theory

Asher Peres

*Department of Physics, Technion-Israel Institute of Technology, Haifa, Israel*  
(Received 7 December 1978)

If scattering amplitudes are ordinary complex numbers (not quaternions) then there is a universal algebraic relationship between the six coherent cross sections of any three scatterers (taken singly and pairwise). A violation of this relationship would indicate either that scattering amplitudes are quaternions, or that the superposition principle fails. Some experimental tests are proposed, involving neutron diffraction by crystals made of three different isotopes, neutron interferometry, and  $K_s$ -meson regeneration.





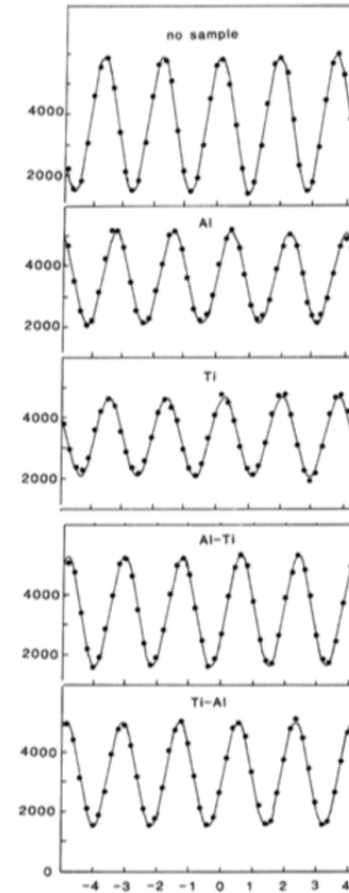
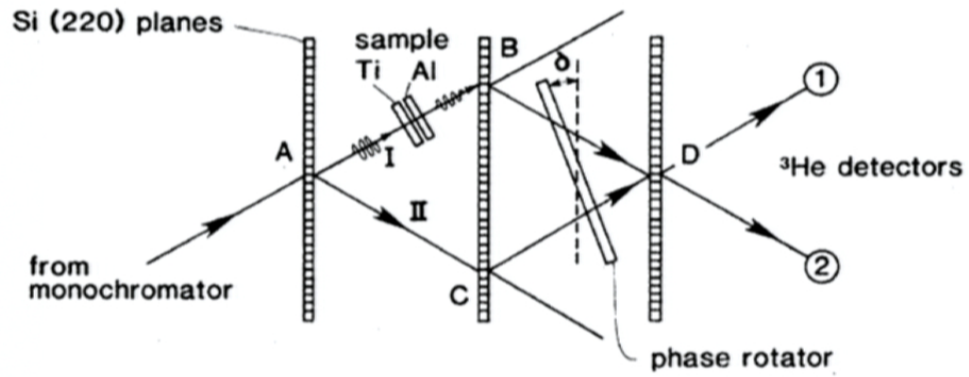
## Our motivation

To test complex quantum mechanics(CQM) against exotic alternative theories which use hyper-complex numbers **into the phase transformations.**

**The non-commutativity of phases**

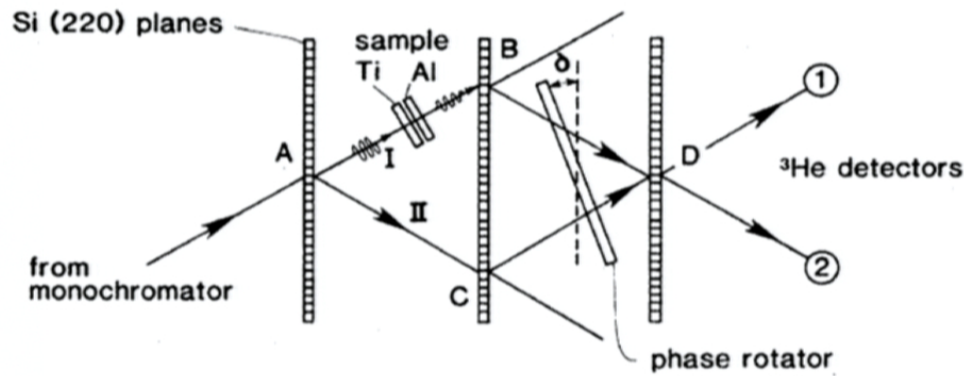
# Neutron Interferometry<sup>1</sup>

<sup>1</sup>H. Kaiser *et al*, *Phys. Rev. A* 29, 4, 1984



# Neutron Interferometry<sup>1</sup>

<sup>1</sup>H. Kaiser *et al*, *Phys. Rev. A* 29, 4, 1984

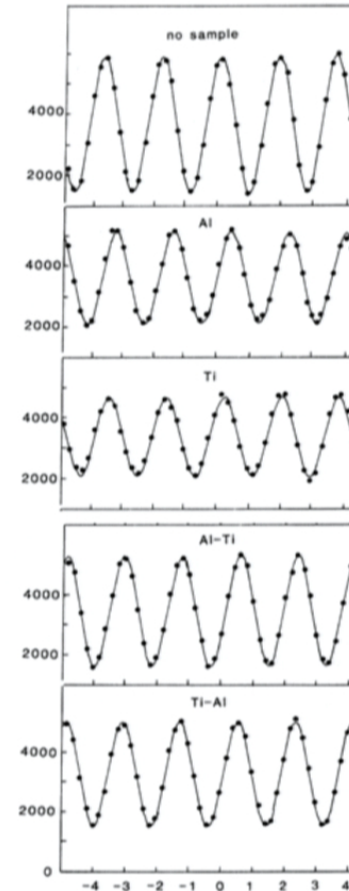


Phase shift  $\phi = -\lambda N b D$

Null result found:



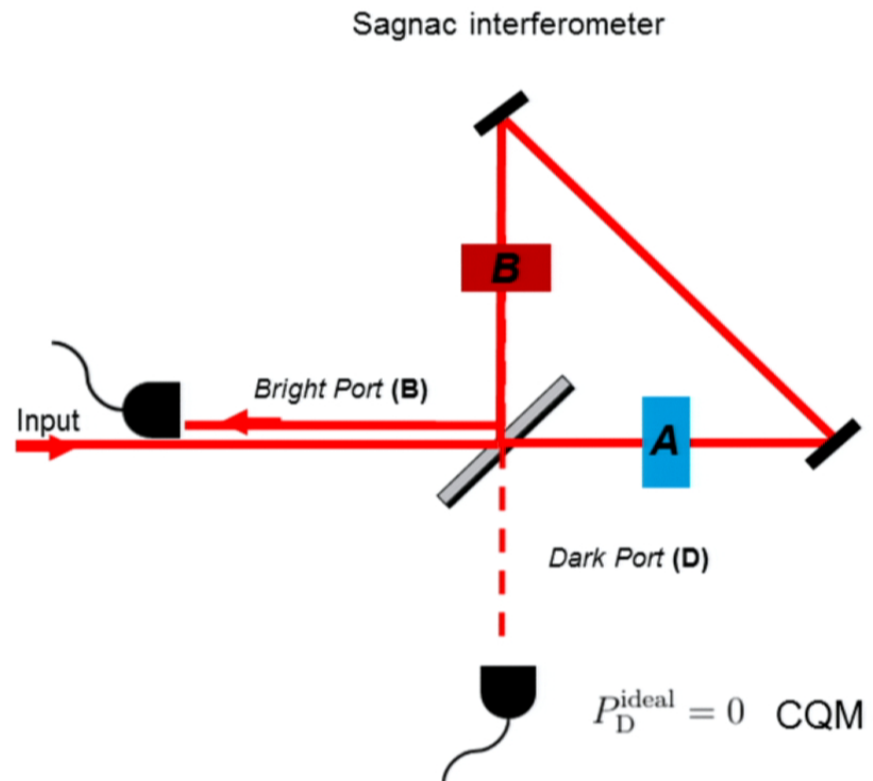
$$|\phi_{\text{Al-Ti}} - \phi_{\text{Ti-Al}}| \ll 0.3^\circ$$



## Theoretical background

Operators

$$A = \alpha \mathcal{I} \quad B = \beta \mathcal{I}$$





# Theoretical background

Operators

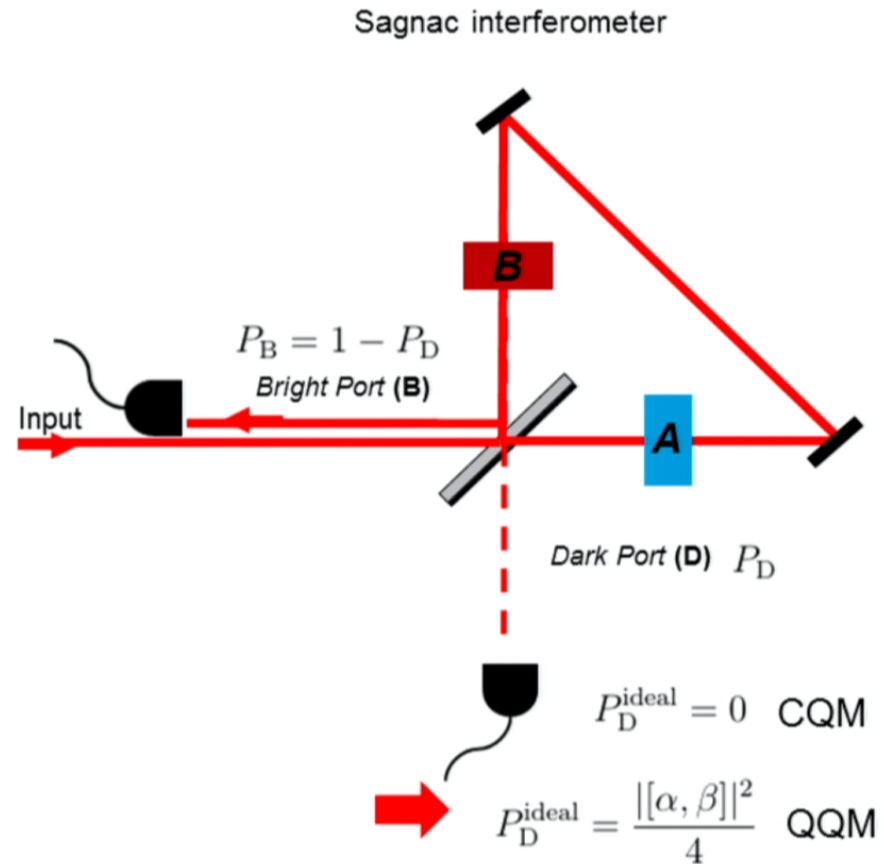
$$A = \alpha \mathcal{I} \quad B = \beta \mathcal{I}$$

Quaternionic Phases

$$\alpha = e^{i\phi_A^1 + j\phi_A^2 + k\phi_A^3}$$

$$\beta = e^{i\phi_B^1 + j\phi_B^2 + k\phi_B^3}$$

$$i^2 = j^2 = k^2 = ijk = -1$$



# Theoretical background

Operators

$$A = \alpha \mathcal{I} \quad B = \beta \mathcal{I}$$

Quaternionic Phases

$$\alpha = e^{i\phi_A^1 + j\phi_A^2 + k\phi_A^3}$$

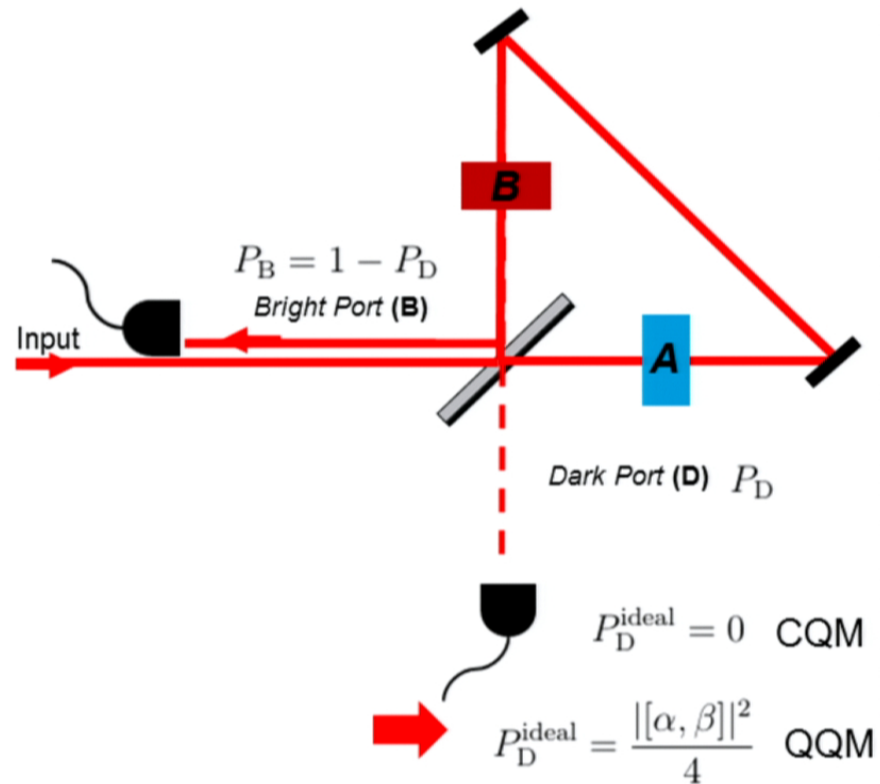
$$\beta = e^{i\phi_B^1 + j\phi_B^2 + k\phi_B^3}$$

$$i^2 = j^2 = k^2 = ijk = -1$$

Imperfect Sagnac

- Spatial-mode mismatch
  - Polarization mismatch
  - No 50:50 BS condition
- }  $v$

Sagnac interferometer



# Theoretical background

Operators

$$A = \alpha \mathcal{I} \quad B = \beta \mathcal{I}$$

Quaternionic Phases

$$\alpha = e^{i\phi_A^1 + j\phi_A^2 + k\phi_A^3}$$

$$\beta = e^{i\phi_B^1 + j\phi_B^2 + k\phi_B^3}$$

$$i^2 = j^2 = k^2 = ijk = -1$$

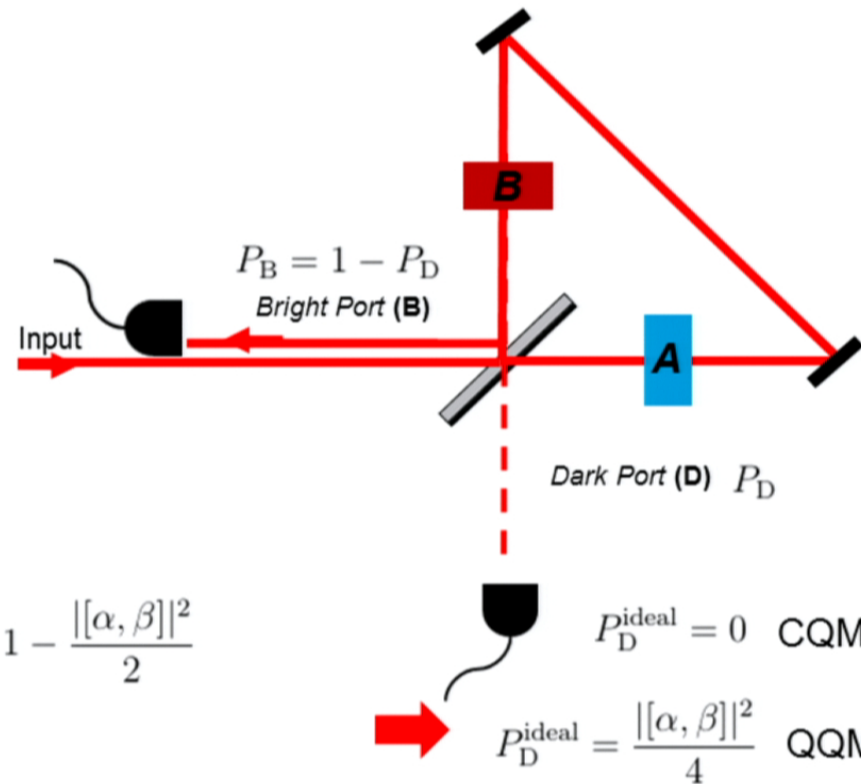
Imperfect Sagnac

$$P_D = \frac{1}{2} - \frac{v\Gamma}{2}$$

Visibility Sagnac

$$\Gamma = 1 - \frac{||[\alpha, \beta]||^2}{2}$$

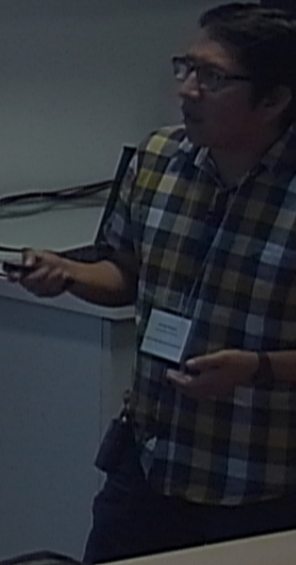
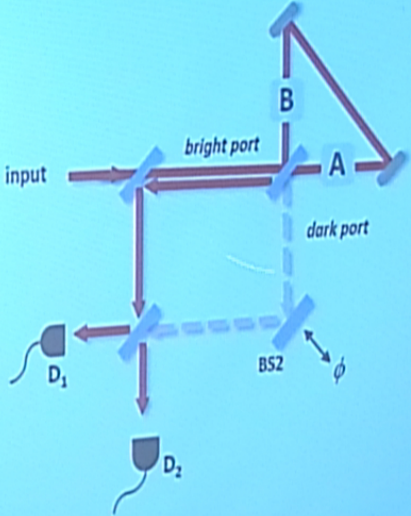
Sagnac interferometer



# Coupling Sagnac to MZ

$P_D$  is expected to be very small...

Amplification: Interfering B and D ports.





## Coupling Sagnac to MZ

$P_D$  is expected to be very small...

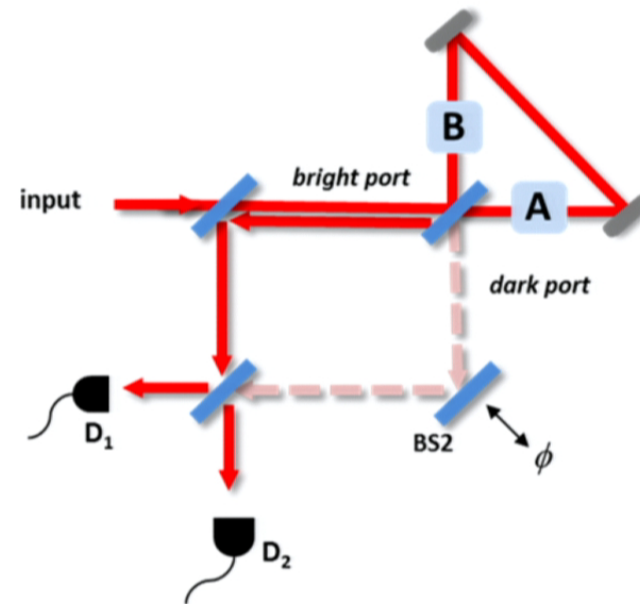
Amplification: Interfering B and D ports.

→ 
$$P_{MZ} \sim \frac{1}{2} + \frac{1}{2}V \cos \phi.$$

Our Goal:

→ 
$$V = \sqrt{1 - v^2 \Gamma^2}$$

MZ      Sagnac      Commutation relation       $\Gamma = 1 - \frac{||[\alpha, \beta]||^2}{2}$



# Our phases

Peres:

➔ Complex scattering amplitudes  
(more likely to have quaternionic phases)

Kaiser *et al.*

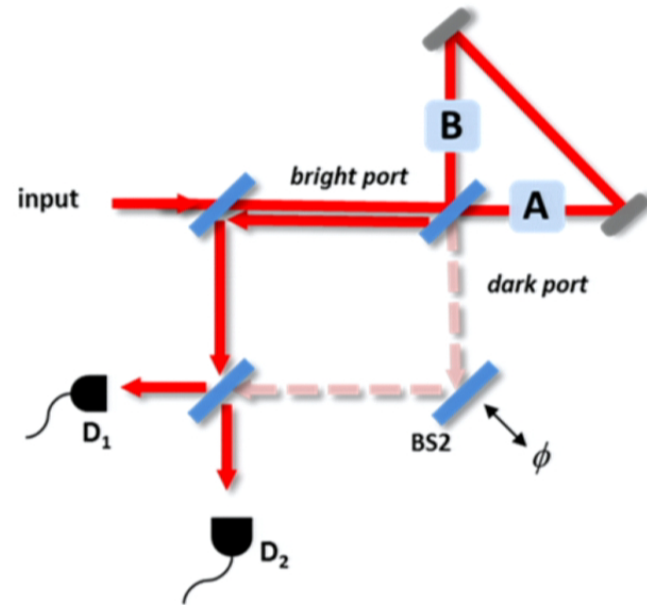
➔ Phase shift =  $-\lambda NbD$

Positive scattering length
Negative scattering length

Optical analog:

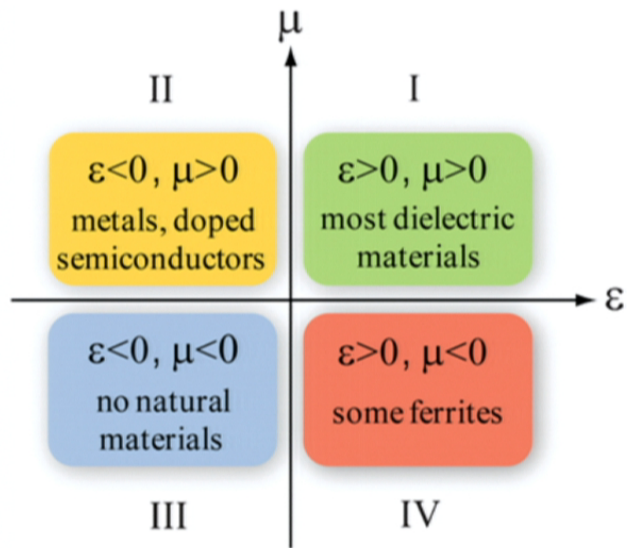
➔ Positive refractive index    **A** ➔ Liquid crystal

➔ Negative refractive index    **B** ➔ Metamaterial



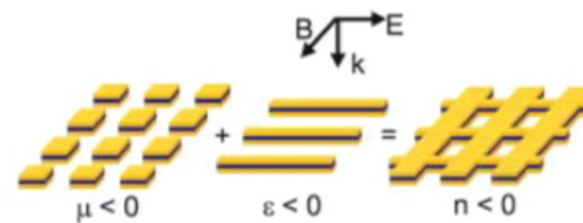
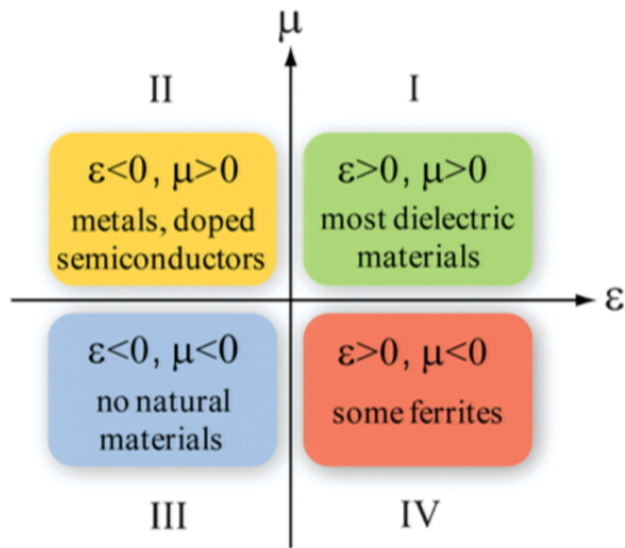
## Metamaterials

Metamaterials consist of periodically or randomly distributed structured elements, whose size and spacing are much smaller than the wavelength of EM waves.



## Metamaterials

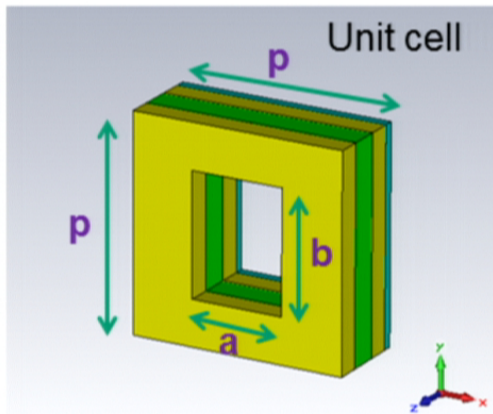
Metamaterials consist of periodically or randomly distributed structured elements, whose size and spacing are much smaller than the wavelength of EM waves.



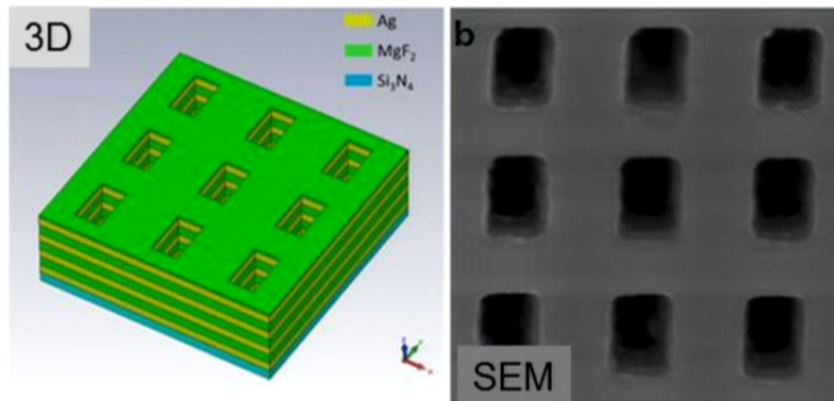
Negative phase shift



## Negative index metamaterial (NIM) (Fishnet structure)



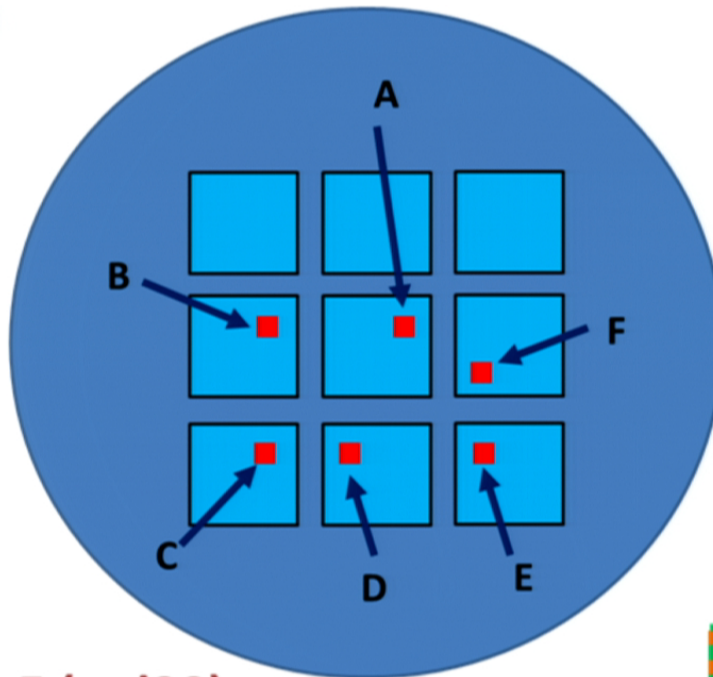
$p = 350 \text{ nm}$   
 $a = 150 \text{ nm}$   
 $b = 200 \text{ nm}$



Silver / magnesium fluoride / silver / silicon nitride

Thickness = 40nm / 50nm / 40nm / 15nm

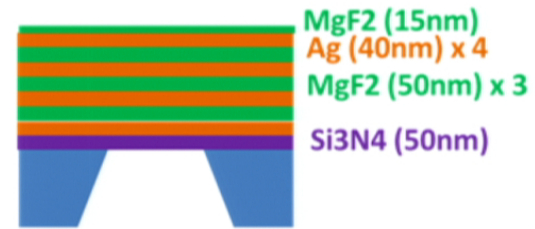
# NIM



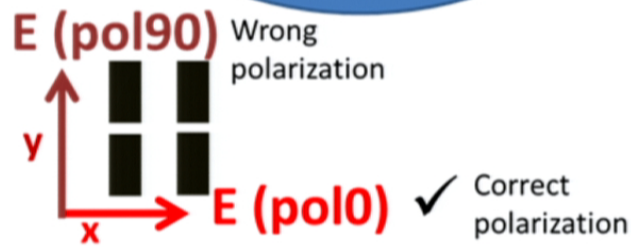
Transmission= 13%  
Index=-0.4

■ 20um x 20um fishnets

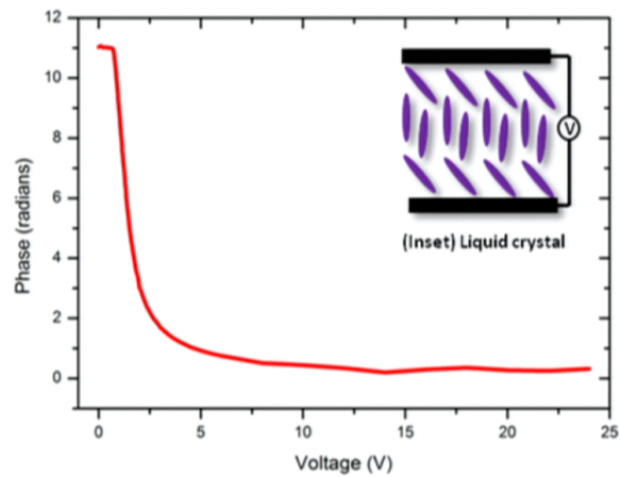
Q02



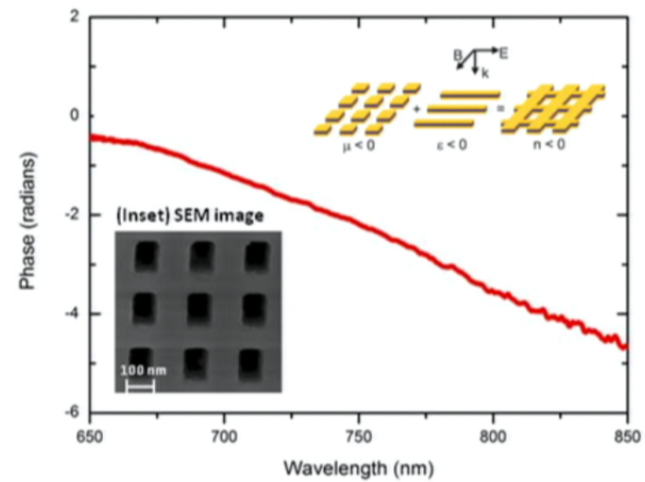
Total thickness = 375nm



## Our phases

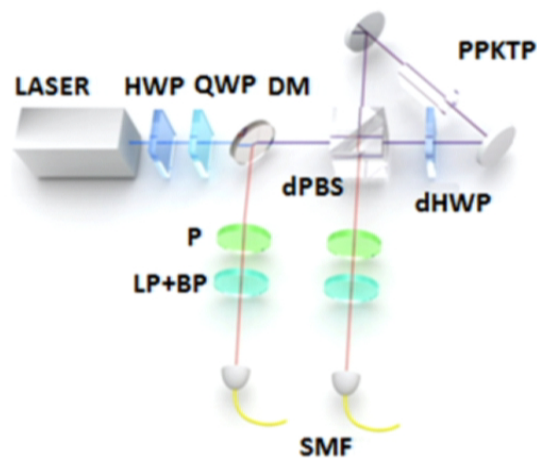


Standard Liquid Phase retarder  
Phase shift=  $+\pi$



Negative index Metamaterial  
Phase shift=  $-\pi$

## Sagnac scheme

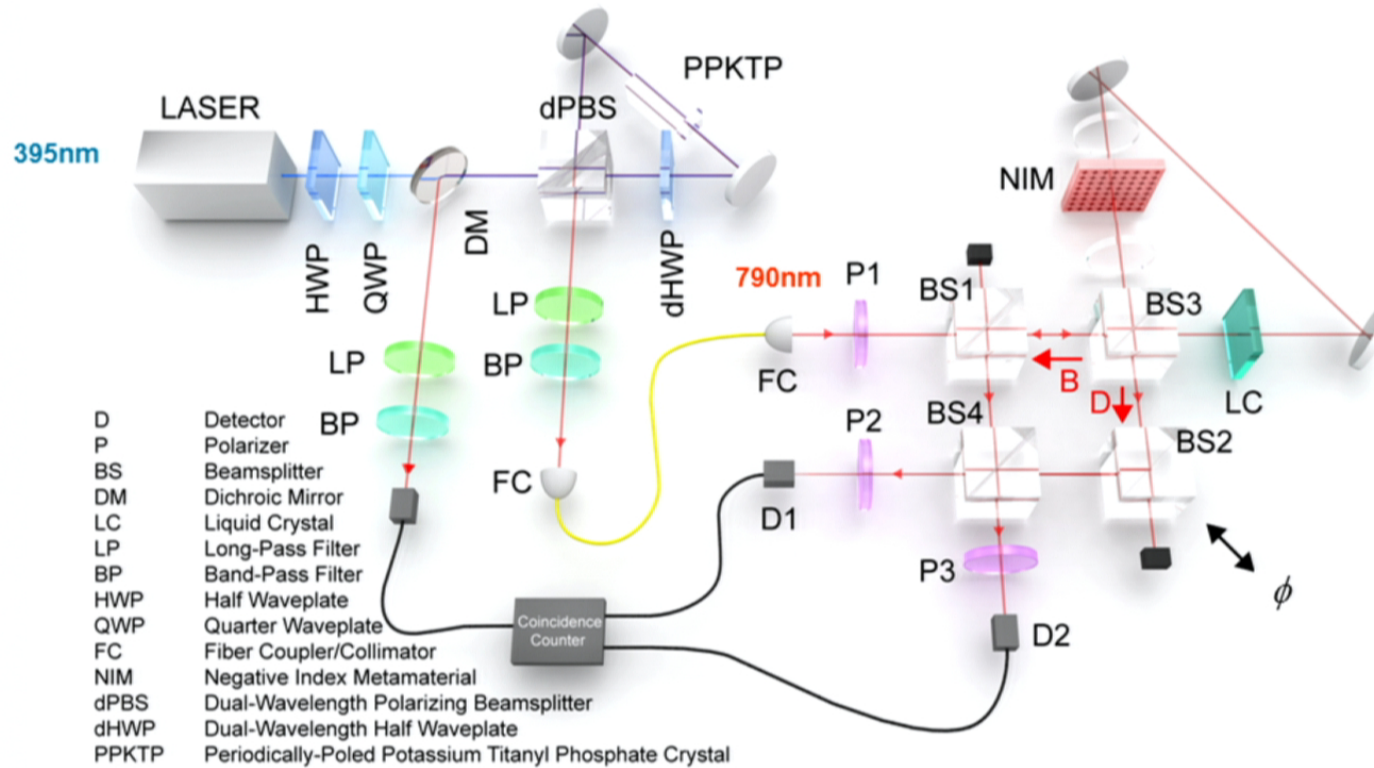


- Nonlinear crystal type-II, 20-mm-length PPKTP
- Pump laser 23.7mW at 395 nm
- Degenerate case at 790 nm
- Down-converted photons in a separable polarization state  $|H\rangle|V\rangle$
- 2 millions of single

PPKTP: periodically-poled potassium titanyl phosphate  
HWP(QWP): Half wave-plate(Quarter wave-plate)  
DM: Dichroic Mirror  
SMF: Single-mode fiber  
dPBS: dual polarizer beam splitter  
P:Polorizer



## Our setup



Lorenzo Procopio *et al.* arXiv:1602.01624, under review at *Nat. Comm.*



## Our measurements

Our Goal

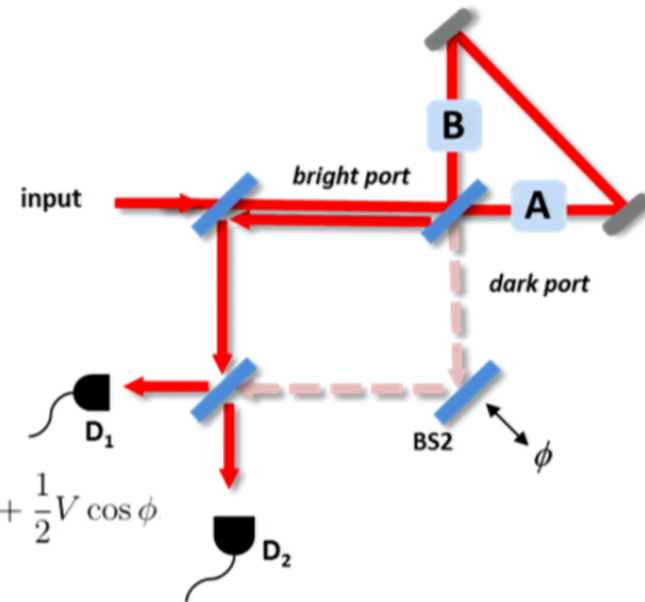
$$V = \sqrt{1 - v^2\Gamma^2}$$

Four settings:

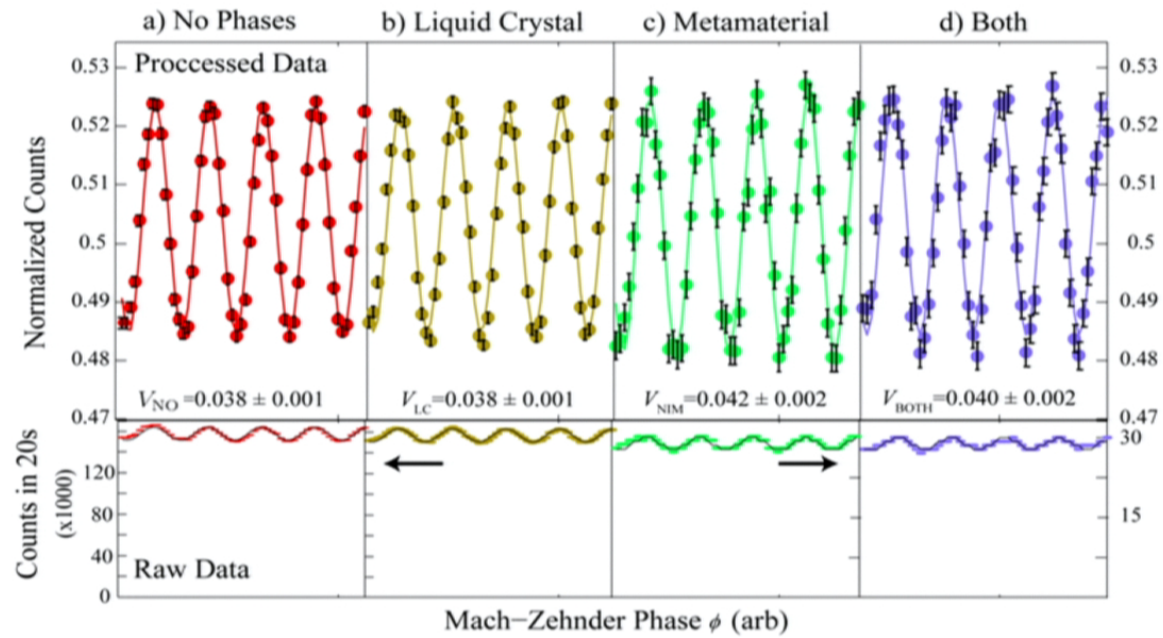
➔ **Characterization of apparatus**

- a) No phases  $V_{NO}$
- b) Positive Phase  $V_{LC}$

$$P_{MZ\sim} = \frac{1}{2} + \frac{1}{2}V \cos \phi$$



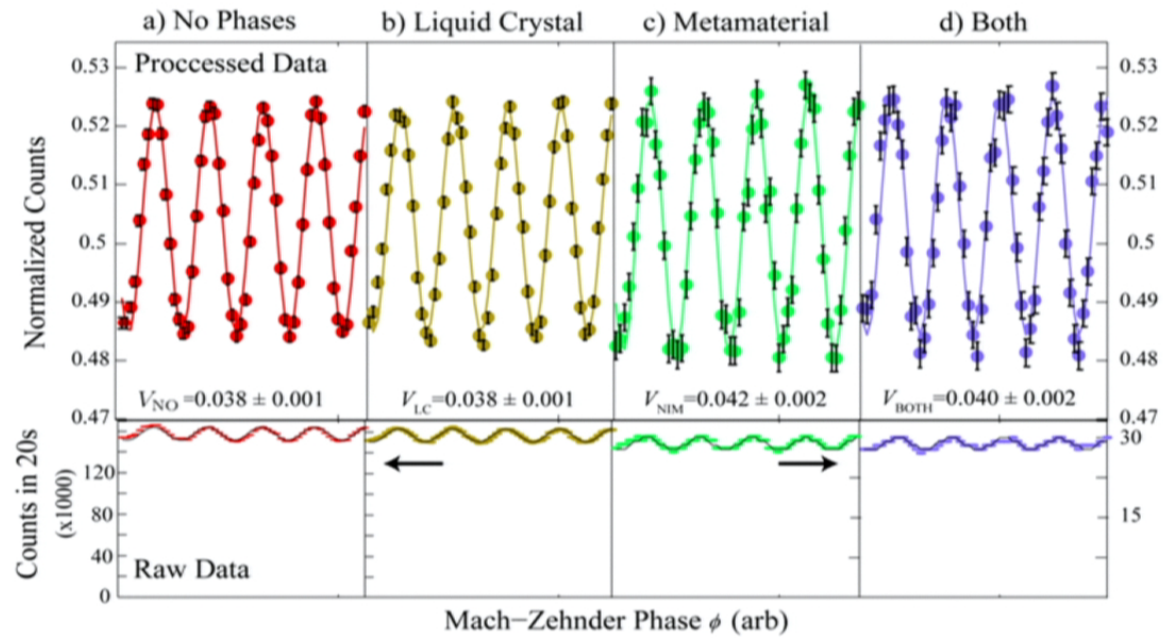
## Results



### Characterization of apparatus

On a single run:  $V_{NO} = V_{LC}$

## Results

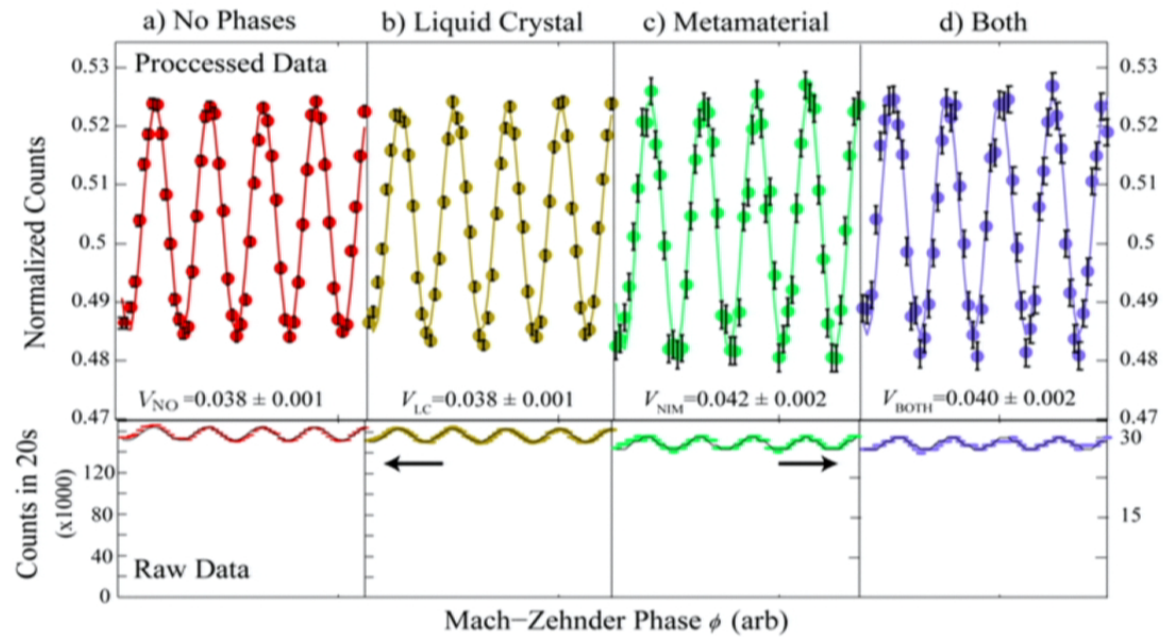


### Characterization of apparatus

On a single run:  $V_{NO} = V_{LC}$

After 402 times:  $\Delta_{LC} = V_{NO} - V_{LC} = 0.002 \pm 0.003$

## Results



### Characterization of apparatus

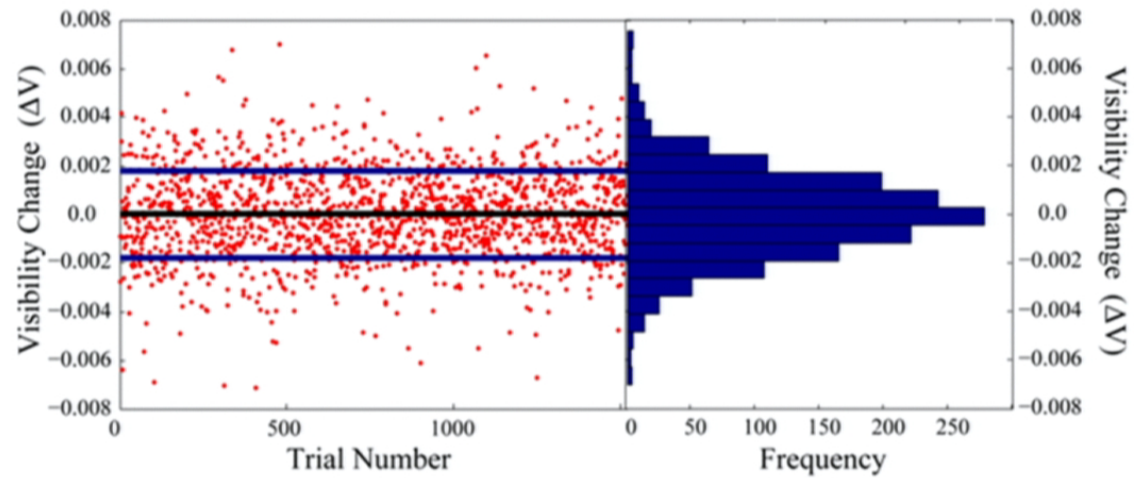
On a single run:  $V_{NO} = V_{LC}$

After 402 times:  $\Delta_{LC} = V_{NO} - V_{LC} = 0.002 \pm 0.003$

### Testing QQM

On a single run:  $V_{NIM} = V_{BOTH}$

## Visibility change distribution

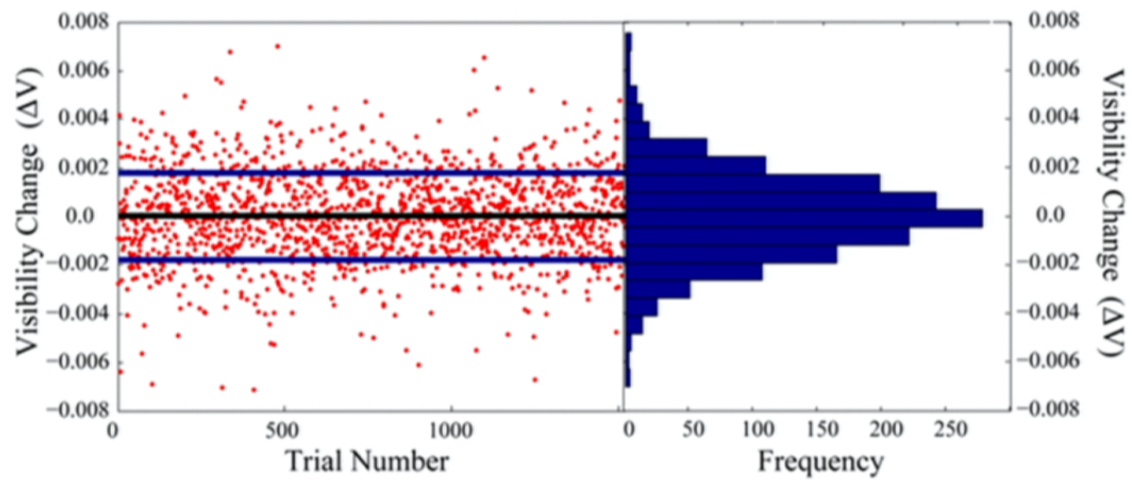


### Testing QQM

After 1522 times:  $\Delta V = V_{\text{BOTH}} - V_{\text{NIM}} = 0.0006 \pm 0.005$



## Visibility change distribution



### Testing QQM

After 1522 times:  $\Delta V = V_{\text{BOTH}} - V_{\text{NIM}} = 0.0006 \pm 0.005$



Sagnac effect:  $10^{-4}$   
Faraday effect:  $10^{-6}$



Decrease  $v$

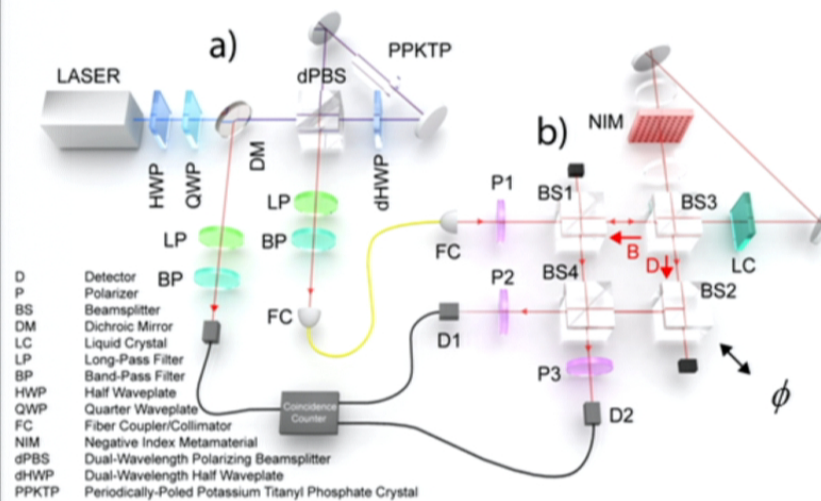
But...

## Does the Peres experiment using photons test for hyper-complex (quaternionic) quantum theories?

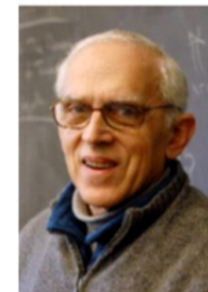
Stephen L. Adler

(Submitted on 18 Apr 2016)

Assuming the standard axioms for quaternionic quantum theory and a spatially localized scattering interaction, the  $S$ -matrix in quaternionic quantum theory is complex valued, not quaternionic. Using the standard connections between the  $S$ -matrix, the forward scattering amplitude for electromagnetic wave scattering, and the index of refraction, we show that the index of refraction is necessarily complex, not quaternionic. This implies that the recent optical experiment of Procopio et al. based on the Peres proposal does not test for hyper-complex or quaternionic quantum effects arising within the standard Hilbert space framework. Such a test requires looking at near zone fields, not radiation zone fields.



Hey guys, your experiment will never see quaternions



Stephen L. Adler

S.L.A , arXiv:1604.04950

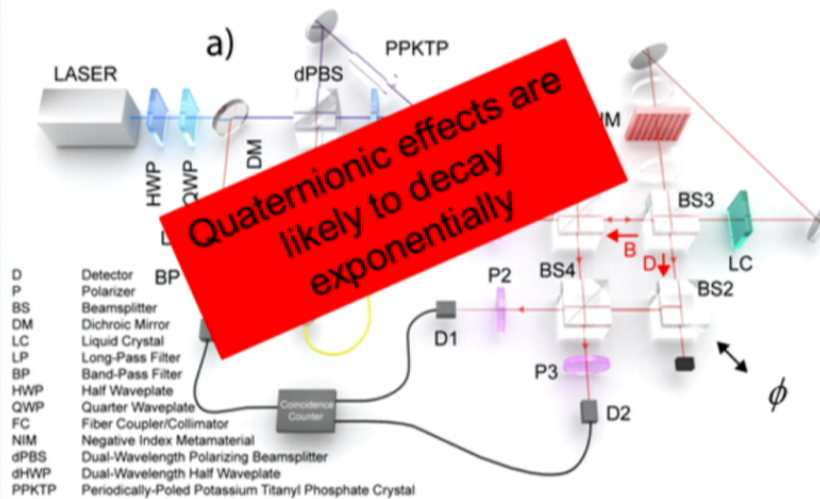
But...

## Does the Peres experiment using photons test for hyper-complex (quaternionic) quantum theories?

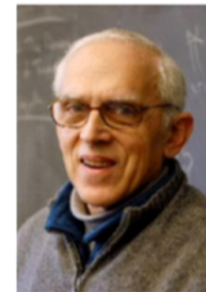
Stephen L. Adler

(Submitted on 18 Apr 2016)

Assuming the standard axioms for quaternionic quantum theory and a spatially localized scattering interaction, the  $S$ -matrix in quaternionic quantum theory is complex valued, not quaternionic. Using the standard connections between the  $S$ -matrix, the forward scattering amplitude for electromagnetic wave scattering, and the index of refraction, we show that the index of refraction is necessarily complex, not quaternionic. This implies that the recent optical experiment of Procopio et al. based on the Peres proposal does not test for hyper-complex or quaternionic quantum effects arising within the standard Hilbert space framework. Such a test requires looking at near zone fields, not radiation zone fields.



Hey guys, your experiment will never see quaternions



Stephen L. Adler

S.L.A , arXiv:1604.04950

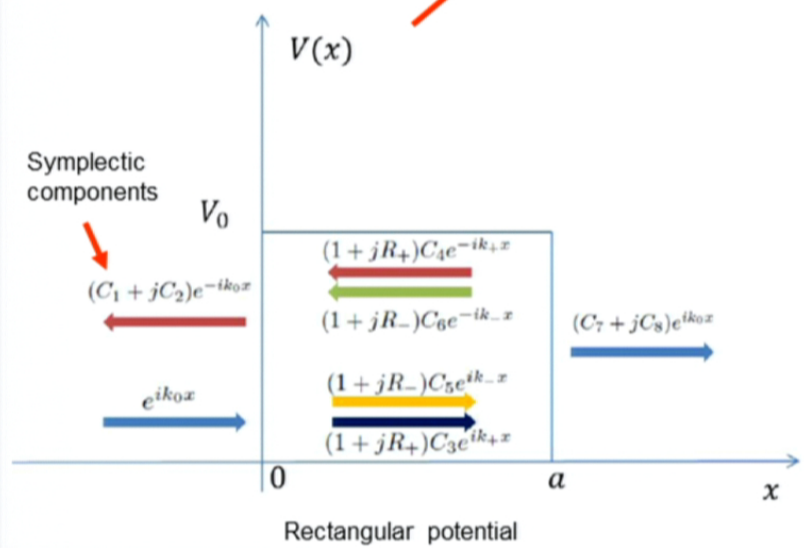
$$\Psi = \Psi_\alpha + j\Psi_\beta \quad \leftarrow \quad \Psi_\beta \sim e^{-p|x|}$$

# Counterexample

Klein-Gordon Equation

Massless relativistic particles  
m=0

$$\left[ - \left( \frac{\partial}{\partial t} - iV(x) \right)^2 + \frac{\partial^2}{\partial x^2} \right] \phi(x, t) = m^2 \phi(x, t).$$



We found that a non-decaying quaternionic phase remains

$$C_8, C_2 \neq 0$$

L.M. Procopio et. al., arXiv:1607.01648



Thus...

### Comment on Adler's "Does the Peres experiment using photons test for hyper-complex (quaternionic) quantum theories?"

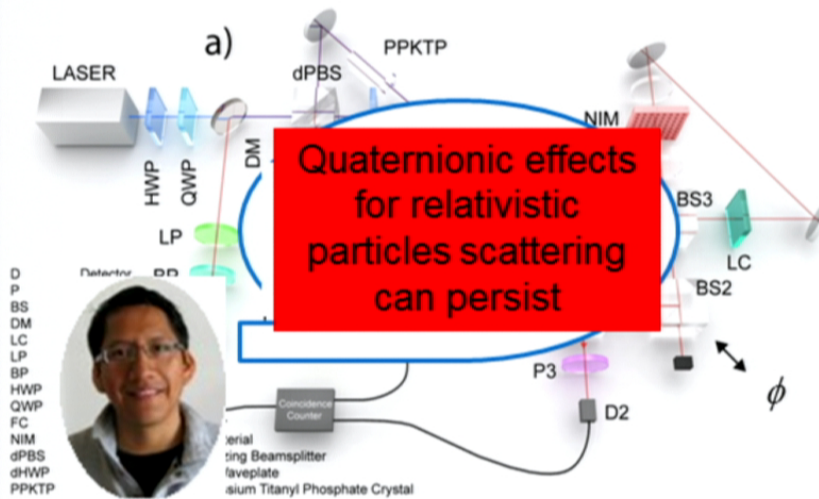
Lorenzo M. Procopio,<sup>1</sup> Lee A. Rozema,<sup>1</sup> Borivoje Dakić,<sup>1,2</sup> and Philip Walther<sup>1</sup>

<sup>1</sup>Faculty of Physics, University of Vienna, Boltzmannngasse 5, A-1090 Vienna, Austria

<sup>2</sup>Institute of Quantum Optics and Quantum Information,

Austrian Academy of Sciences, Boltzmannngasse 3, A-1090 Vienna, Austria

(Dated: July 7, 2016)





## Summary and Outlook

- Our experiment is the first direct search for QQM using massless particles
- Quaternionic effects for relativistic Klein-Gordon scattering can persist
- Our work was enabled by the combination of novel negative-index metamaterial with standard optical photonic technology
- Further tests of QQM can be performed within optics using other methods, regimes, for instance, near-field measurements.