

Title: Testing dark matter with Stage-IV CMB experiments

Date: Sep 13, 2016 11:00 AM

URL: <http://pirsa.org/16090046>

Abstract: <p>In the coming decade, ground based CMB telescopes could face a substantial upgrade, to so-called CMB-S4. There are two main science drivers behind this initiative: B-modes, and neutrino mass, and I will focus on the latter. Thought of more generally, constraints on neutrinos can be thought of as generic tests of dark matter. I will discuss the prospects for CMB-S4 in the dark sector, with emphasis on searches for axions and neutrinos. It will be possible to detect percent level departures from standard cold dark matter at many sigma over a wide range of scales: a vast improvement over Planck (+ existing ground based). A large part of the improvement over Planck comes from precision lensing measurements at high multipole. I will briefly discuss some technical challenges in this measurement, based on modelling of dark matter clustering in the non-linear regime.</p>

# Testing Dark Matter with Stage-IV CMB Experiments



Photo Credit: Jon Ward

David J. E. Marsh  
CMB-S4 science book,  
& 1607.08208



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*College*  
LONDON

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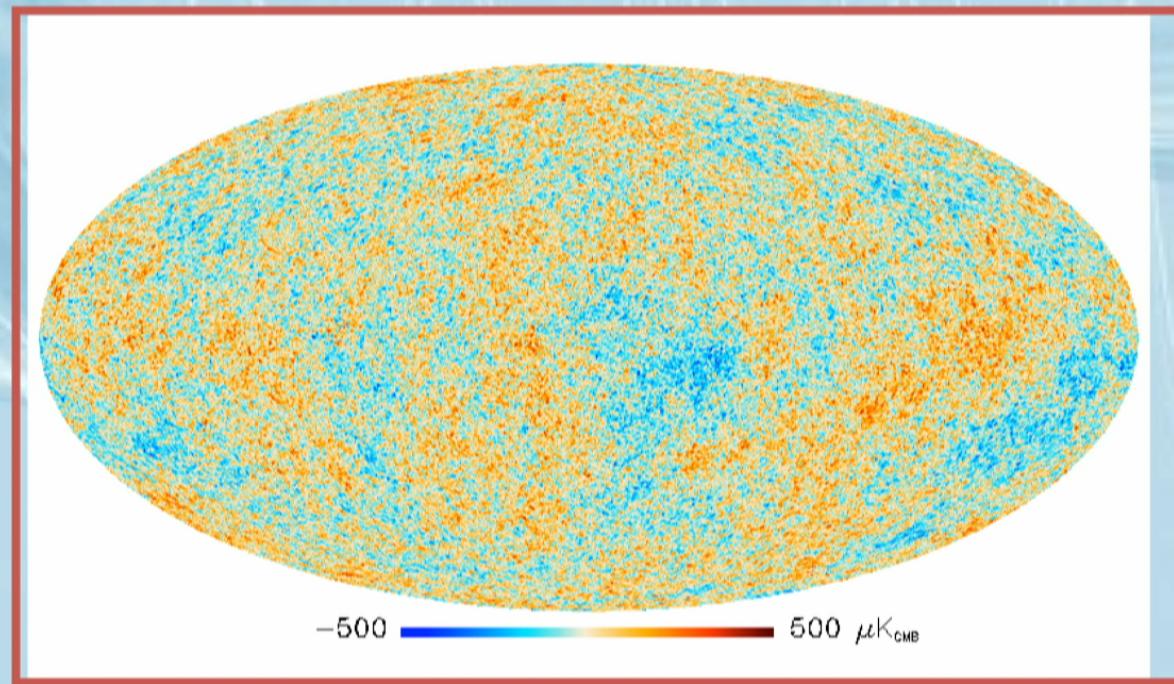
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# Cosmology and the CMB

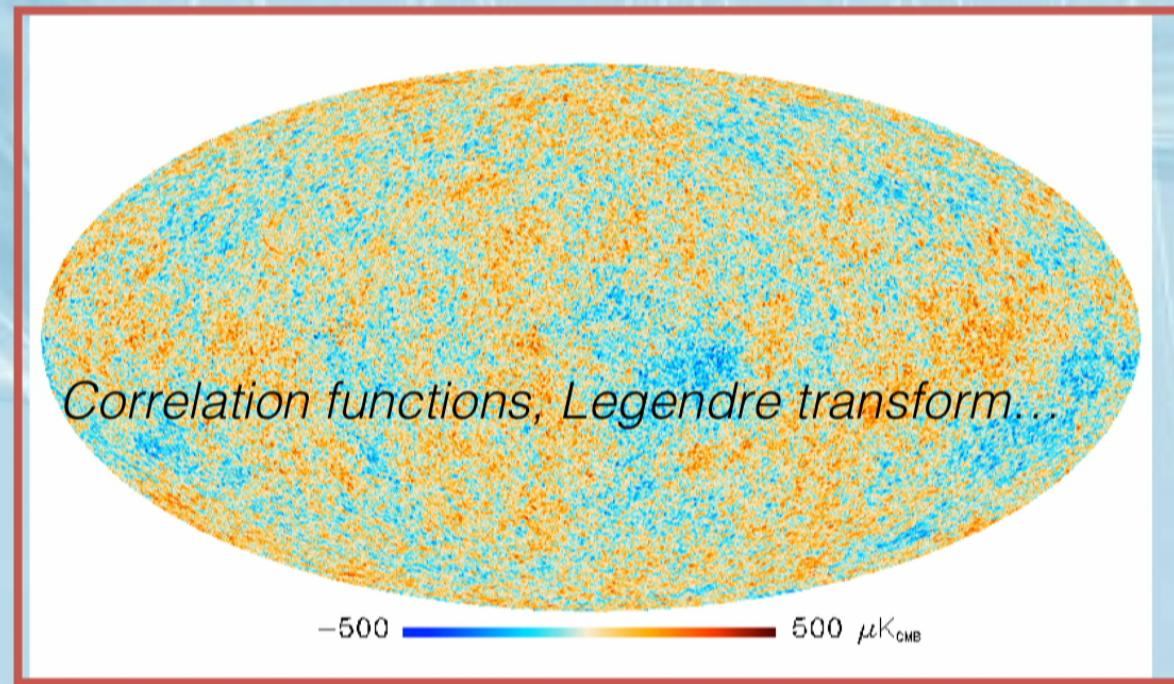
Maps, power spectra, and parameter estimation!



(for a web widget with WMAP, see [http://map.gsfc.nasa.gov/resources/camb\\_tool/index.html](http://map.gsfc.nasa.gov/resources/camb_tool/index.html))

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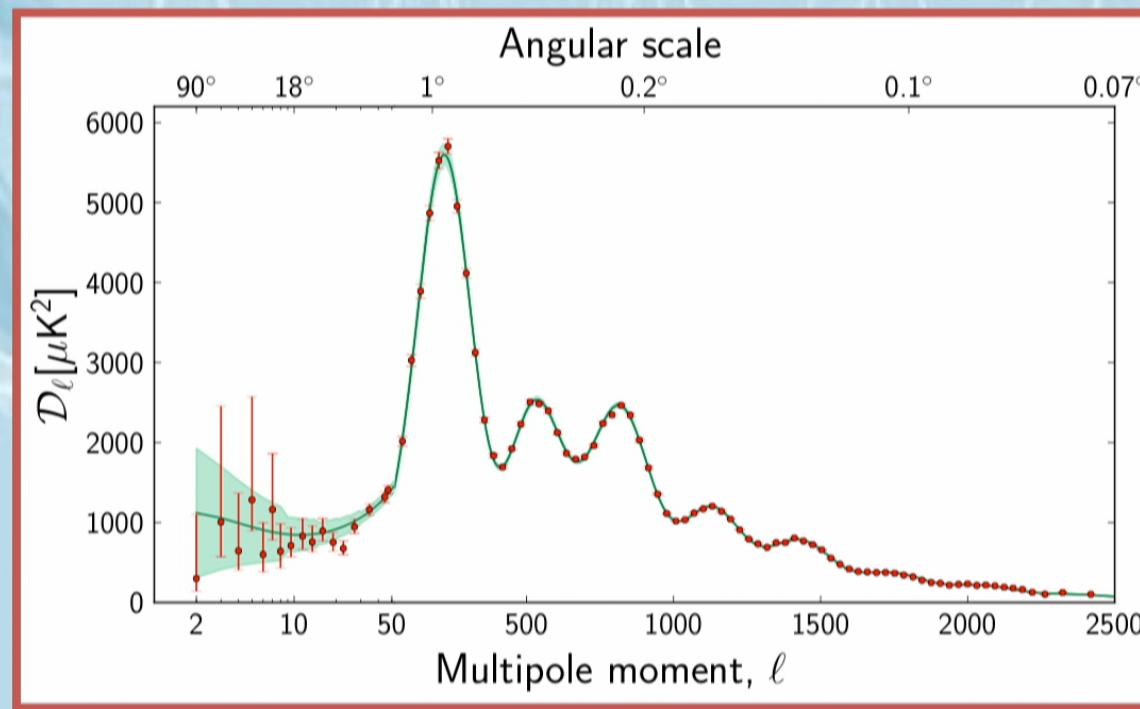
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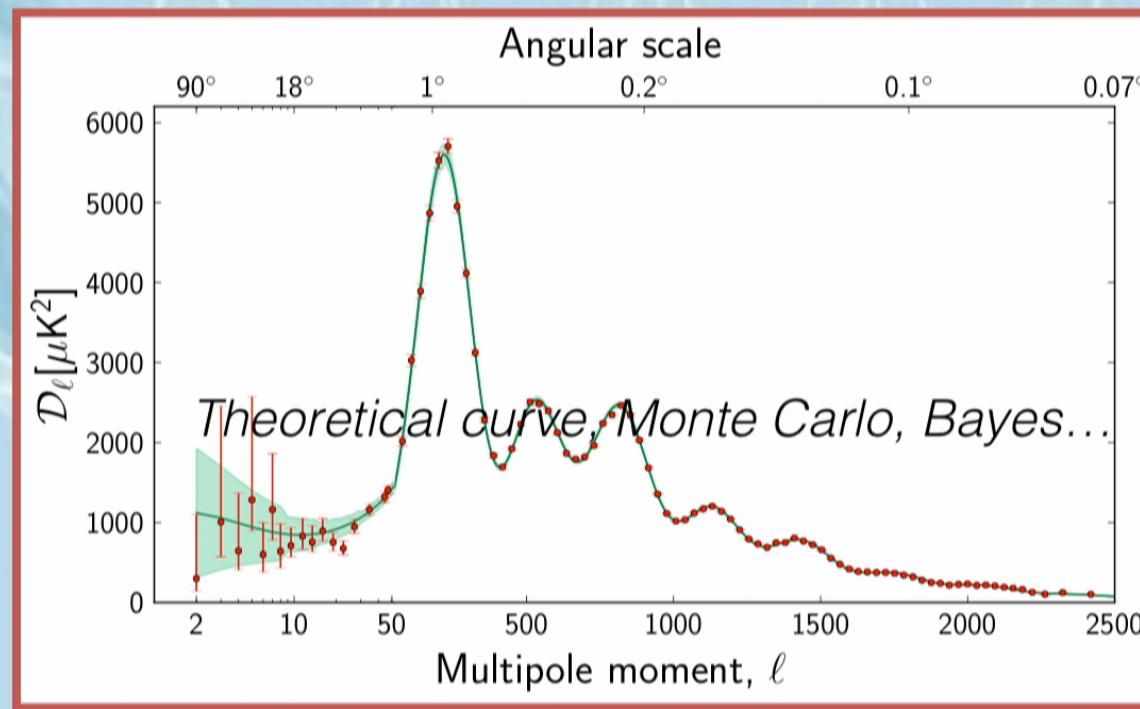
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# Cosmology and the CMB

Maps, power spectra, and parameter estimation!

Parameter	<i>Planck</i> (CMB+lensing)		<i>Planck+WP+highL+BAO</i>	
	Best fit	68 % limits	Best fit	68 % limits
$\Omega_b h^2$ . . . . .	0.022242	$0.02217 \pm 0.00033$	0.022161	$0.02214 \pm 0.00024$
$\Omega_c h^2$ . . . . .	0.11805	$0.1186 \pm 0.0031$	0.11889	$0.1187 \pm 0.0017$
$100\theta_{\text{MC}}$ . . . . .	1.04150	$1.04141 \pm 0.00067$	1.04148	$1.04147 \pm 0.00056$
$\tau$ . . . . .	0.0949	$0.089 \pm 0.032$	0.0952	$0.092 \pm 0.013$
$n_s$ . . . . .	0.9675	$0.9635 \pm 0.0094$	0.9611	$0.9608 \pm 0.0054$
$\ln(10^{10} A_s)$ . . . . .	3.098	$3.085 \pm 0.057$	3.0973	$3.091 \pm 0.025$
$\Omega_\Lambda$ . . . . .	0.6964	$0.693 \pm 0.019$	0.6914	$0.692 \pm 0.010$
$\sigma_8$ . . . . .	0.8285	$0.823 \pm 0.018$	0.8288	$0.826 \pm 0.012$
$z_{\text{re}}$ . . . . .	11.45	$10.8^{+3.1}_{-2.5}$	11.52	$11.3 \pm 1.1$
$H_0$ . . . . .	68.14	$67.9 \pm 1.5$	67.77	$67.80 \pm 0.77$
Age/Gyr . . . . .	13.784	$13.796 \pm 0.058$	13.7965	$13.798 \pm 0.037$
$100\theta_*$ . . . . .	1.04164	$1.04156 \pm 0.00066$	1.04163	$1.04162 \pm 0.00056$
$r_{\text{drag}}$ . . . . .	147.74	$147.70 \pm 0.63$	147.611	$147.68 \pm 0.45$
$r_{\text{drag}}/D_V(0.57)$ . . . . .	0.07207	$0.0719 \pm 0.0011$		

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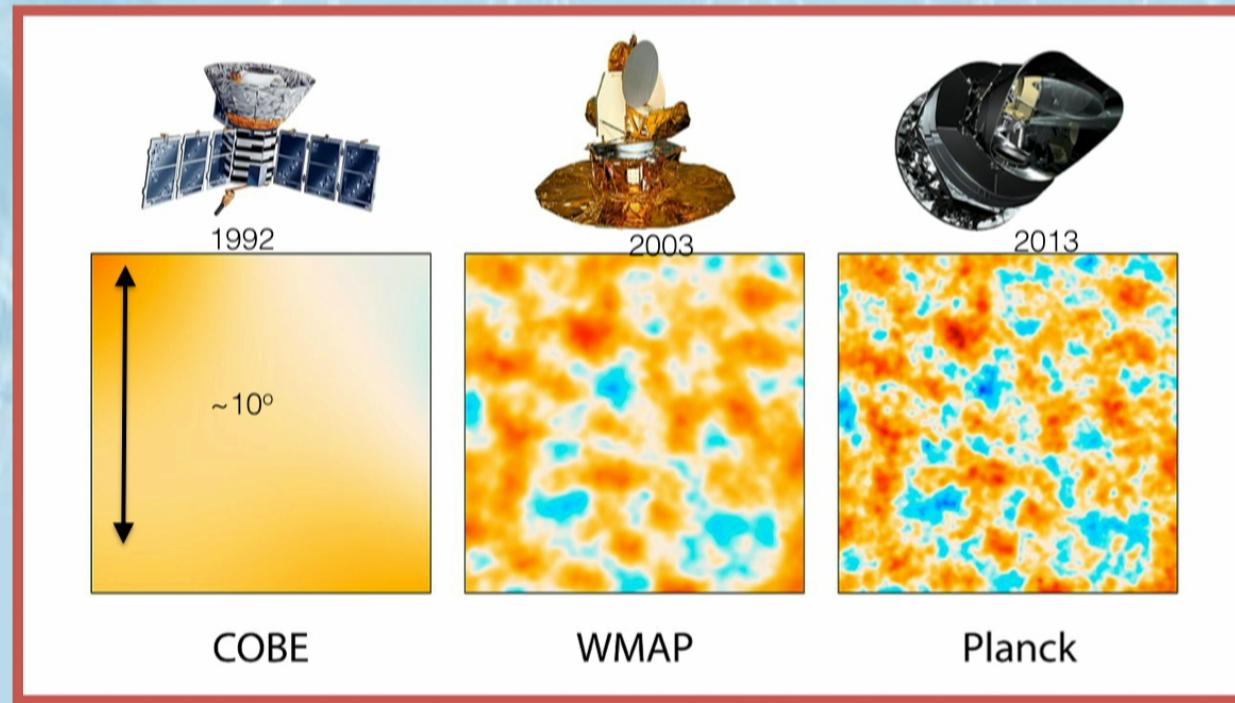


Image modified from NASA

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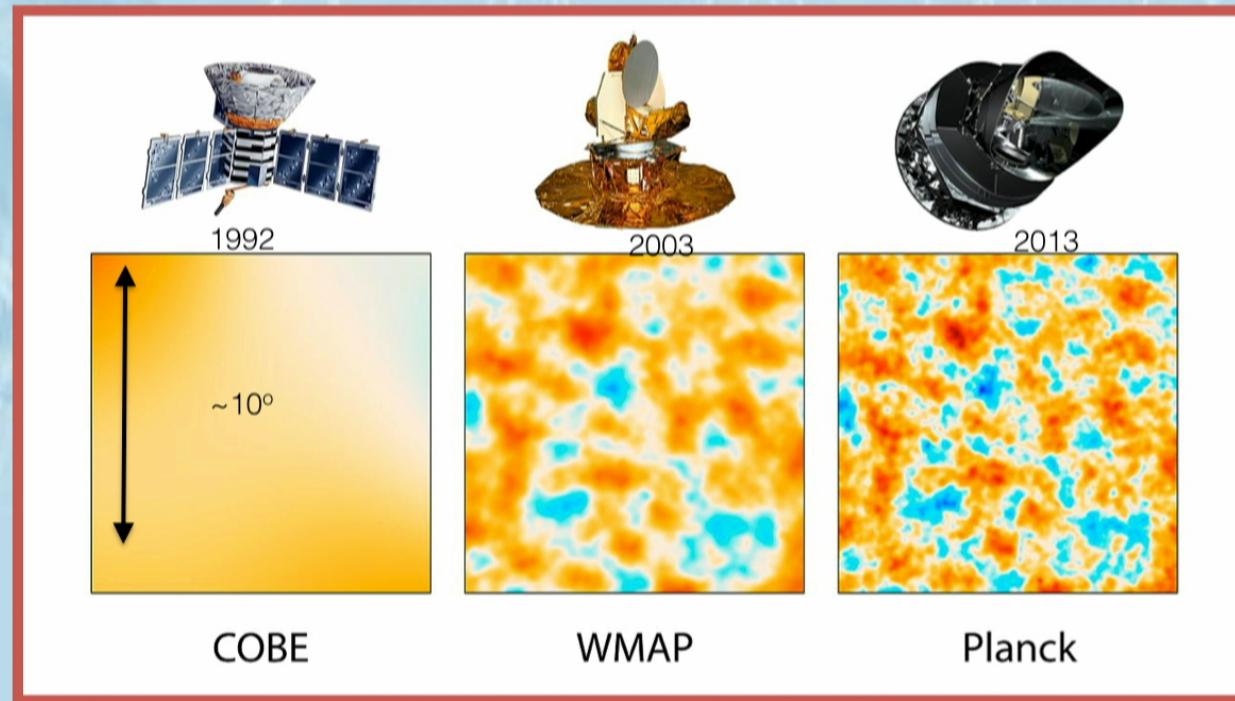


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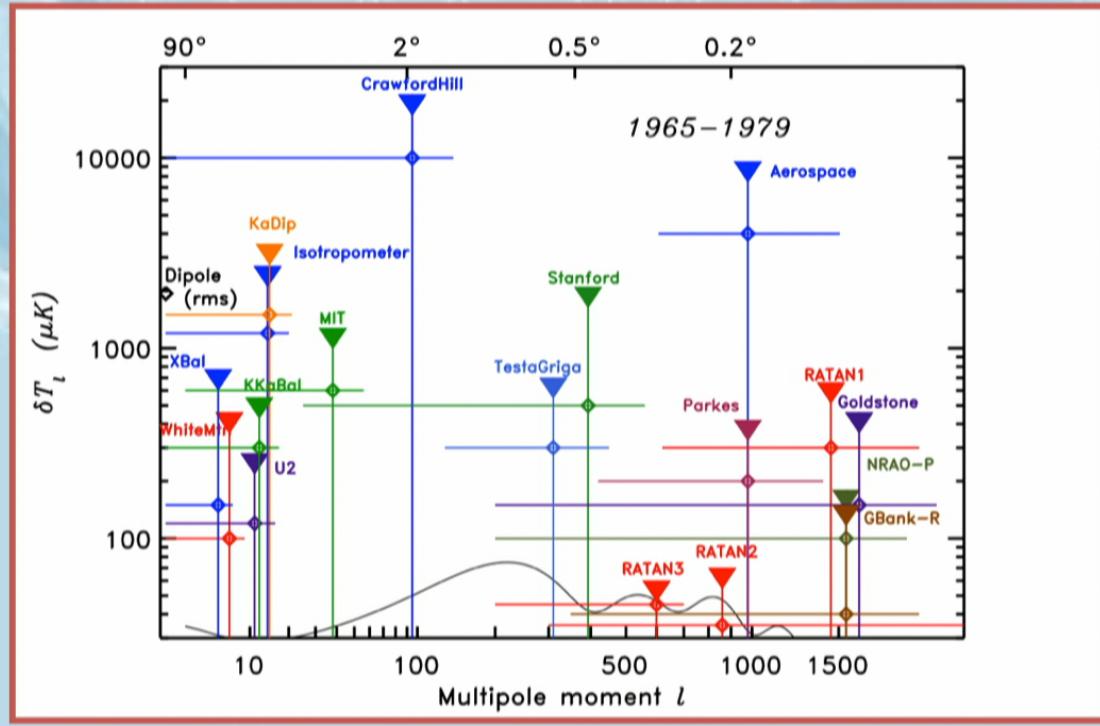
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DISCOVERY: 1965 (Penzias and Wilson)

Image: Lyman Page

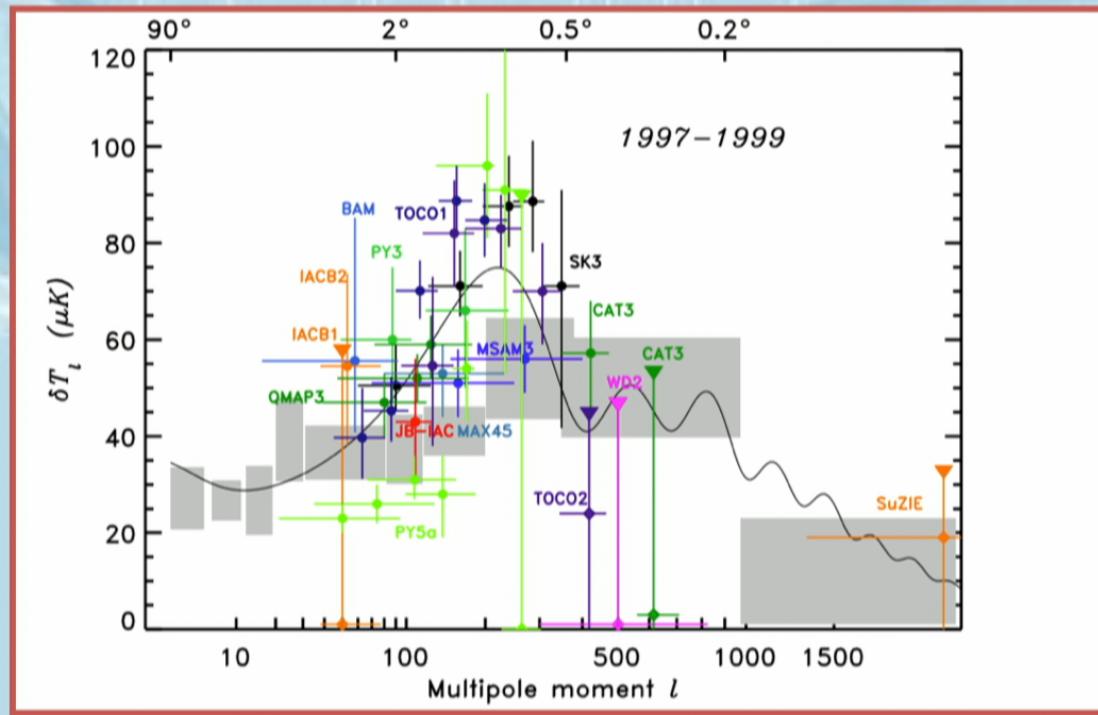


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FIRST ACOUSTIC PEAK: Saskatoon (~1997)

Image: Lyman Page

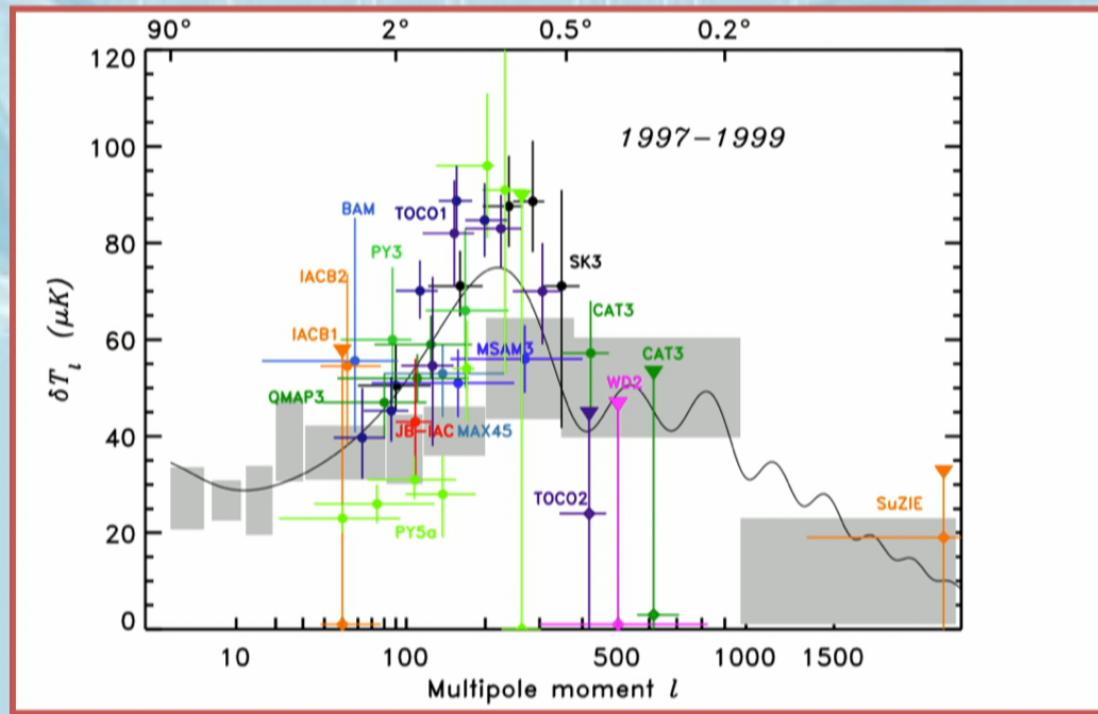


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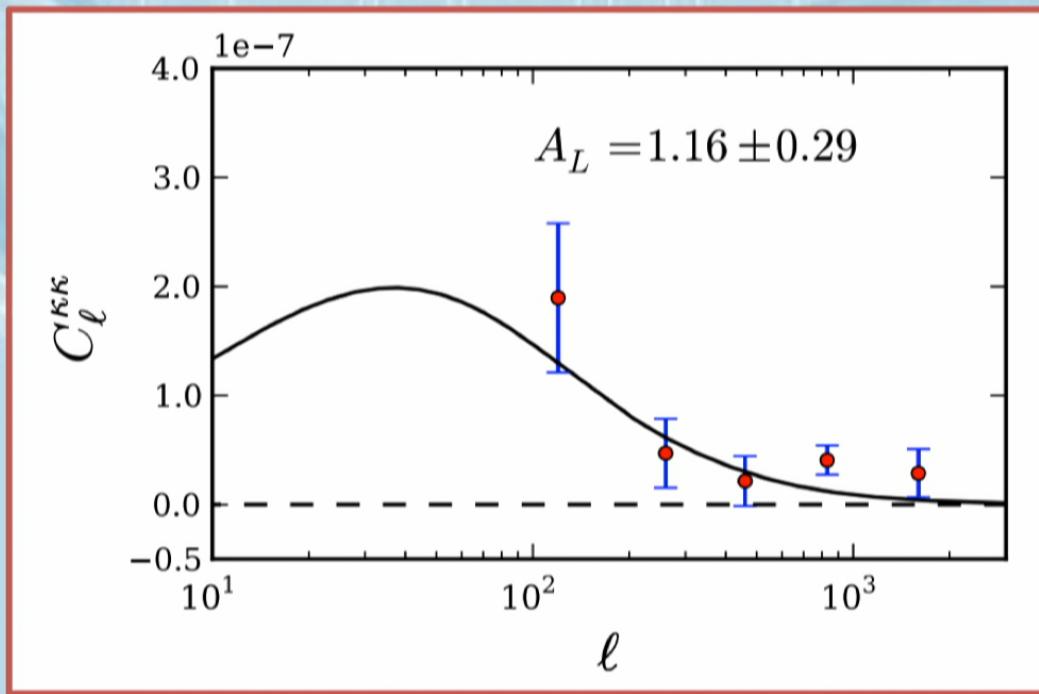


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LENSING DETECTION: ACT (2011)

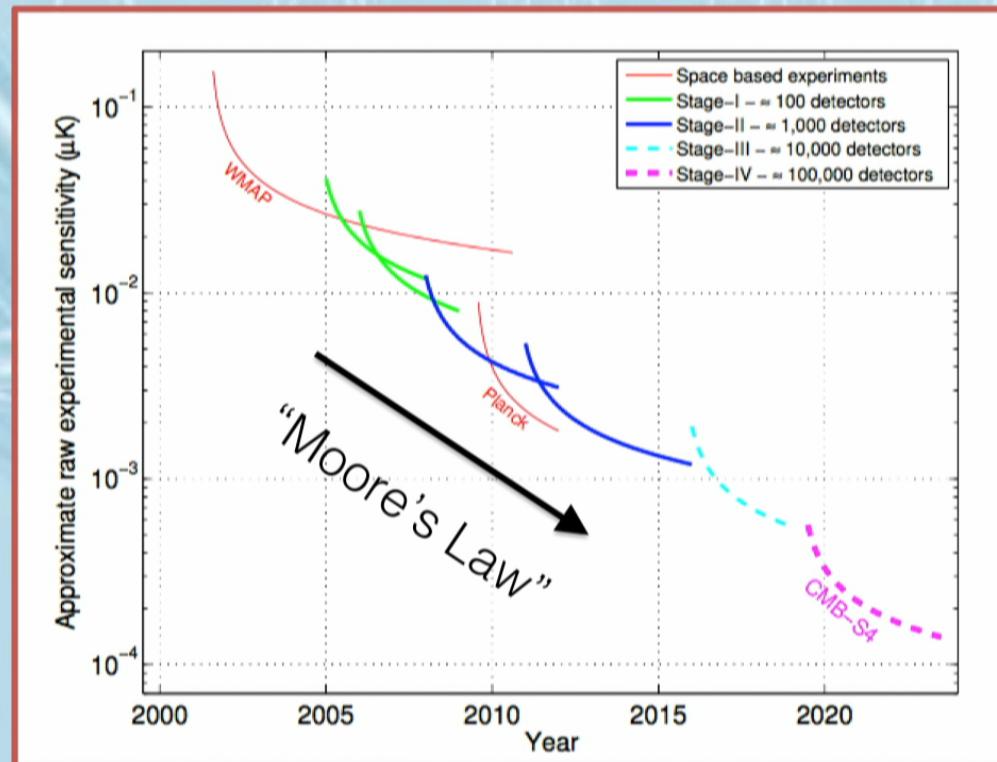
Image: Das et al (2011)



# CMB Stage-IV

Planned upgrade of existing ground-based telescopes: SPT, ACT, BICEP, Polarbear +possible northern hemisphere.

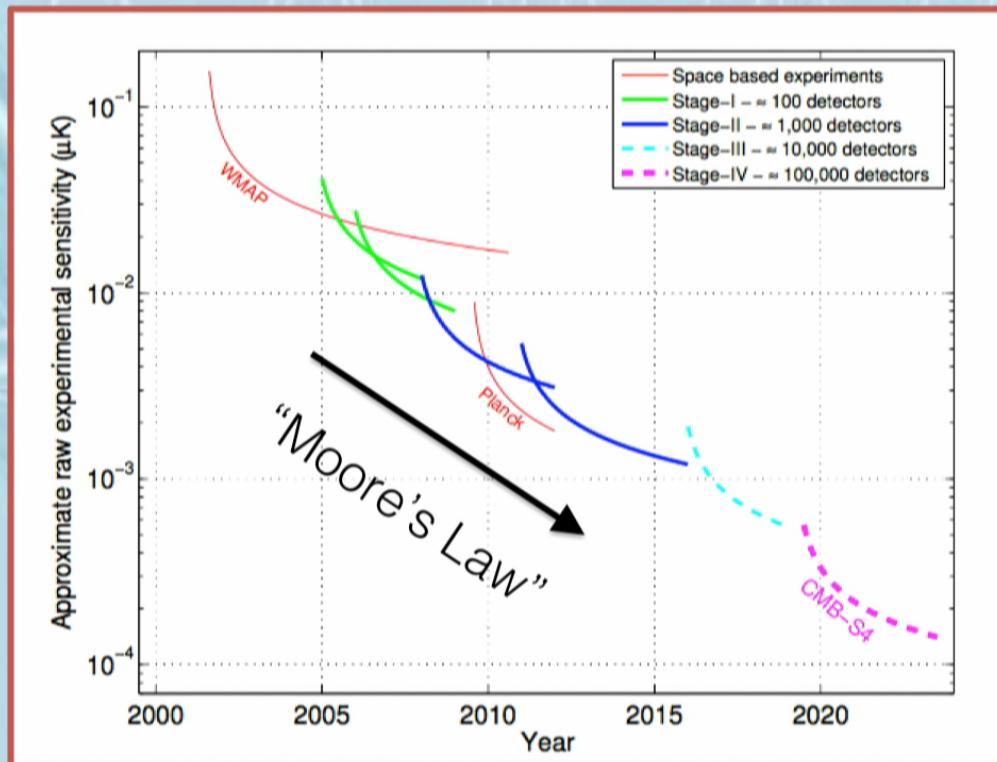
Image: SNOWMASS CFF5 Neutrino planning & CMB-S4 Science Book



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At a glance:

- Run for 4 years beginning 2020 (if funded).
- Temperature, polarization and lensing spectra to  $\ell \sim 4000$ .  
(c.f. Planck  $\ell$ -max  $\sim 2000$  in T,E.  $\ell$ -max  $\sim 500$  lensing).
- Fiducial  $1\mu\text{K}$ -arcmin noise, 1 arcmin beam,  $f_{\text{sky}} = 0.4$   
(c.f. WMAP 12 arcmin, Planck 5 arcmin).
- 8 frequency bands from 30 to 270 GHz (dust etc.)
- Superconducting cameras: existing tech scales up.
- B-modes with  $\sigma(r) \sim 0.001$  (c.f. BICEP2  $r < 0.12$ , 95% C.L.).
- Dark energy “Figure of merit” up by factor of 2 (clusters).
- Neutrino mass with  $\sigma(m_\nu) \sim 15 \text{ meV}$  (c.f.  $m_{\text{min}} \sim 60 \text{ meV}$ ).
- Relativistic species with  $\sigma(N_{\text{eff}}) \sim 0.02$  (c.f. Planck  $\sim 0.2$ ).
- Improve axion DM fraction by factor of 10 from Planck.

More Details: Abazajian et al, 1309.5383; Science Book (soon)

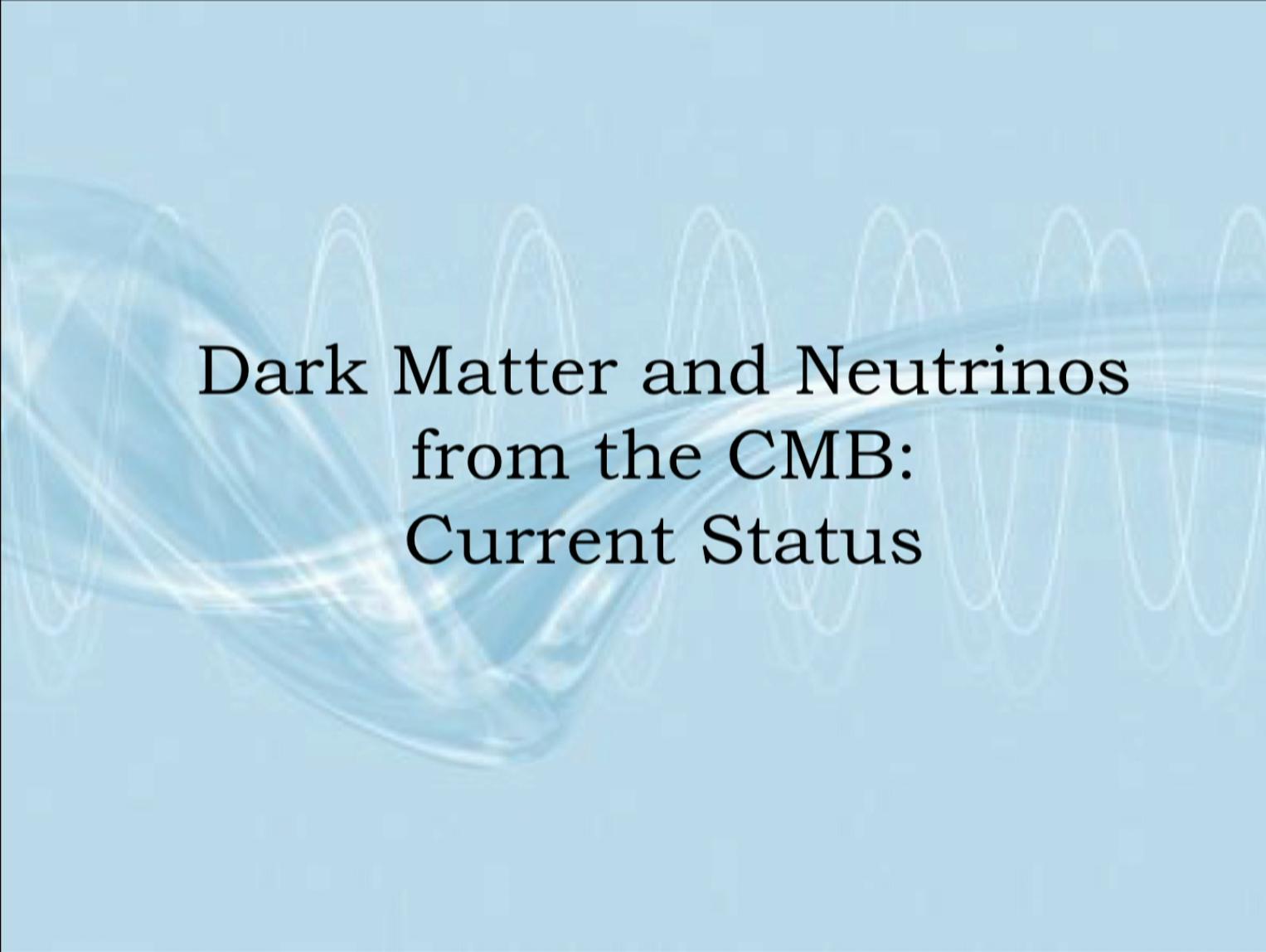
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# Dark Matter and Neutrinos from the CMB: Current Status

# Neutrino mass from Planck

Planck 2015 Paper XIII

Oscillation experiments: neutrino's have mass:  $\sum m_\nu \gtrsim 0.06 \text{ eV}$   
e.g. PDG

Neutrino energy density:

$$\Omega_\nu = \frac{\sum m_\nu}{93.14 \text{ eV}}$$

Hot DM “free streams”: does not cluster on all scales like cold DM does.

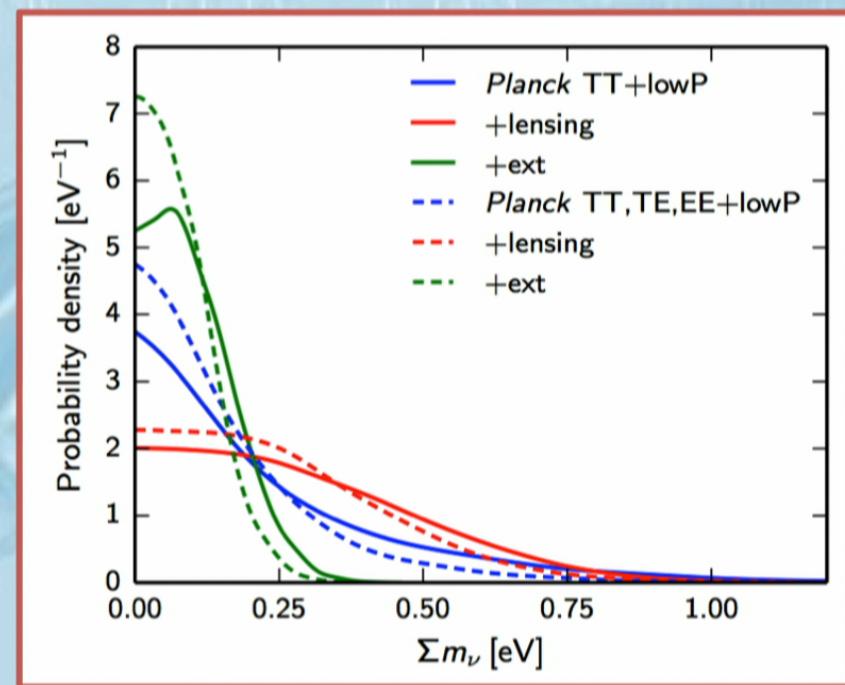
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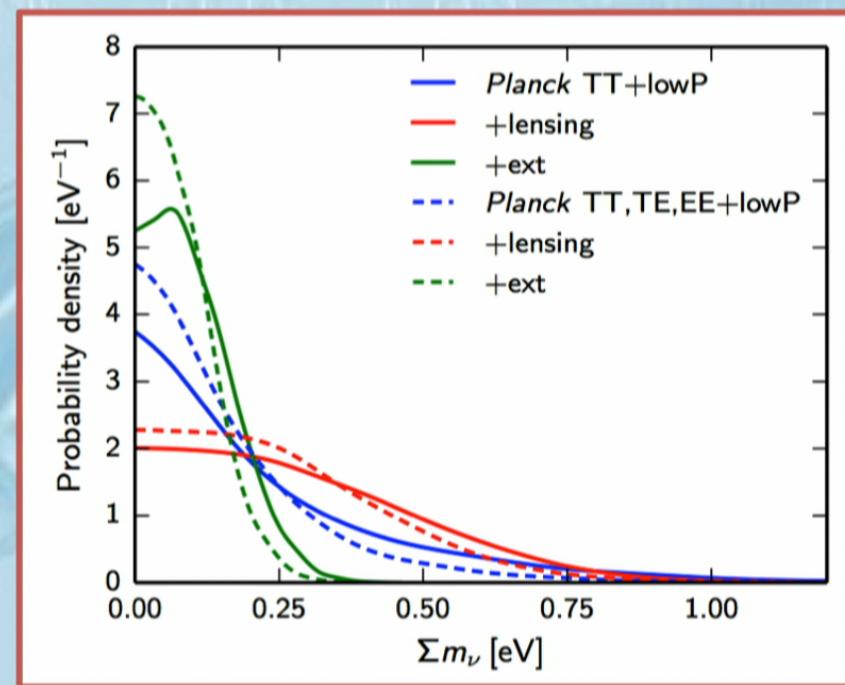
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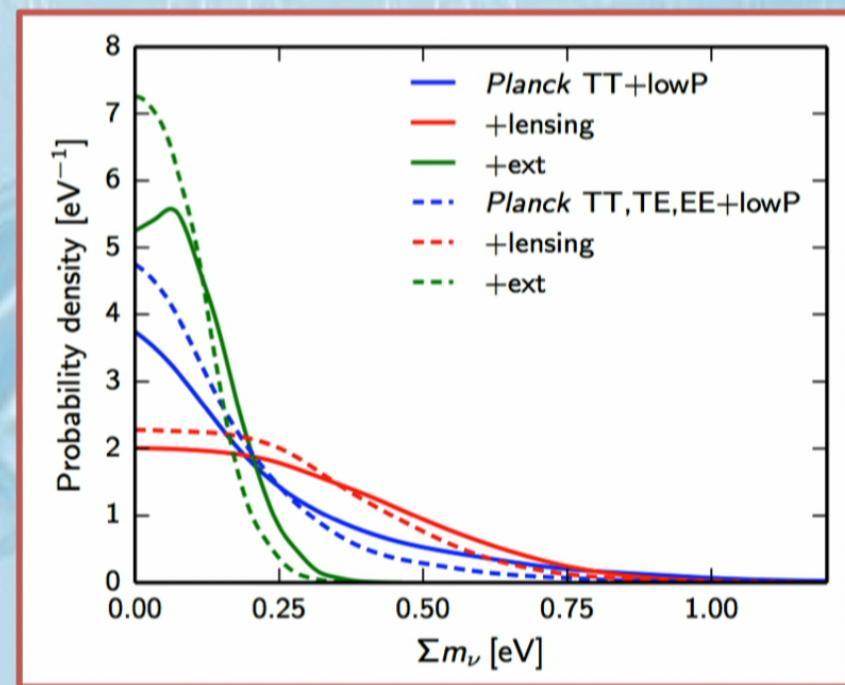
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# “Dark radiation” from Planck

Planck 2015 Paper XIII

Parameterised as “additional neutrino species”.

$$\rho = N_{\text{eff}} \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \rho_\gamma$$

Additional radiation changes the expansion rate at early times.

Planck + BAO 68%:

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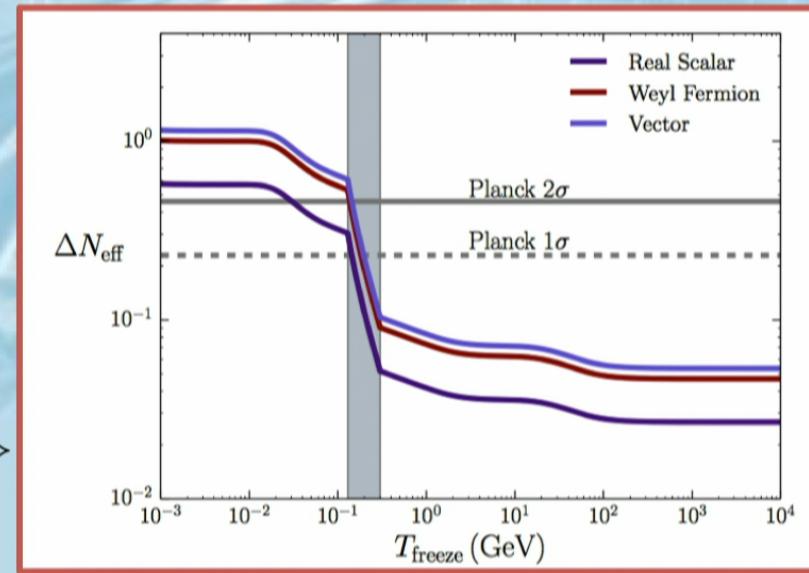
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CMB-S4 Science Book

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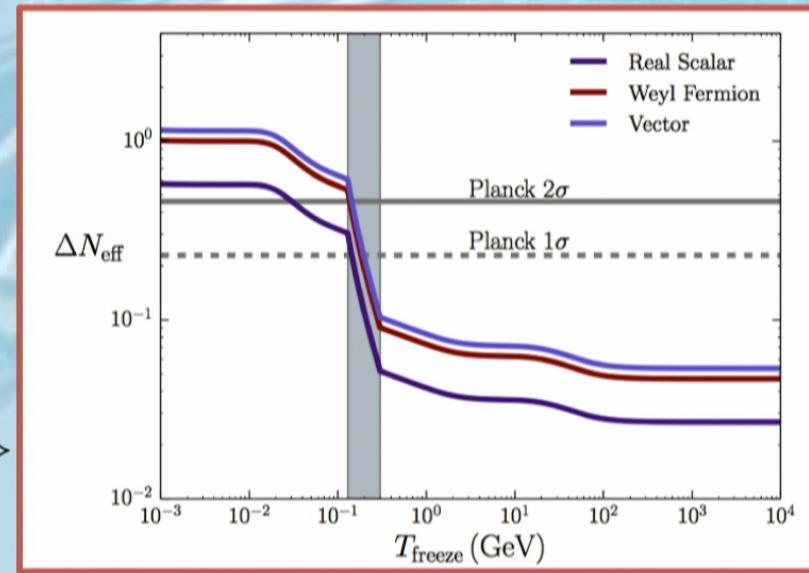
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# Neutrino combinations

Planck 2015 Paper XIII

Are they really neutrinos? Test with perts.:  $c_{\text{eff}}^2 = c_{\text{vis}}^2 = 1/3$

$$c_{\text{eff}}^2 = 0.3242 \pm 0.0059, \quad c_{\text{vis}}^2 = 0.331 \pm 0.037$$

Sterile neutrinos:

$$N_{\text{eff}} < 3.7$$

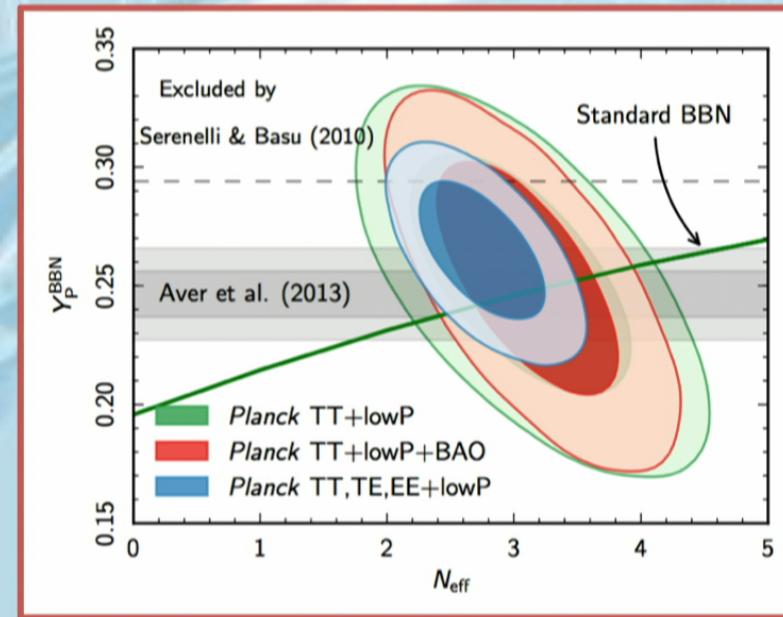
$$m_{\nu, \text{sterile}}^{\text{eff}} < 0.38 \text{ eV}$$

Massive standard + DR:

$$N_{\text{eff}} = 3.2 \pm 0.5$$

$$\sum m_\nu < 0.32 \text{ eV}$$

Consistency with BBN:



# Ultralight Axions (ULAs)

Hlozek et al (2015)

Cold, vacuum realignment axions change expansion rate and clustering relative to CDM if  $H < m$  on some scale of interest.

If ULAs are DM:

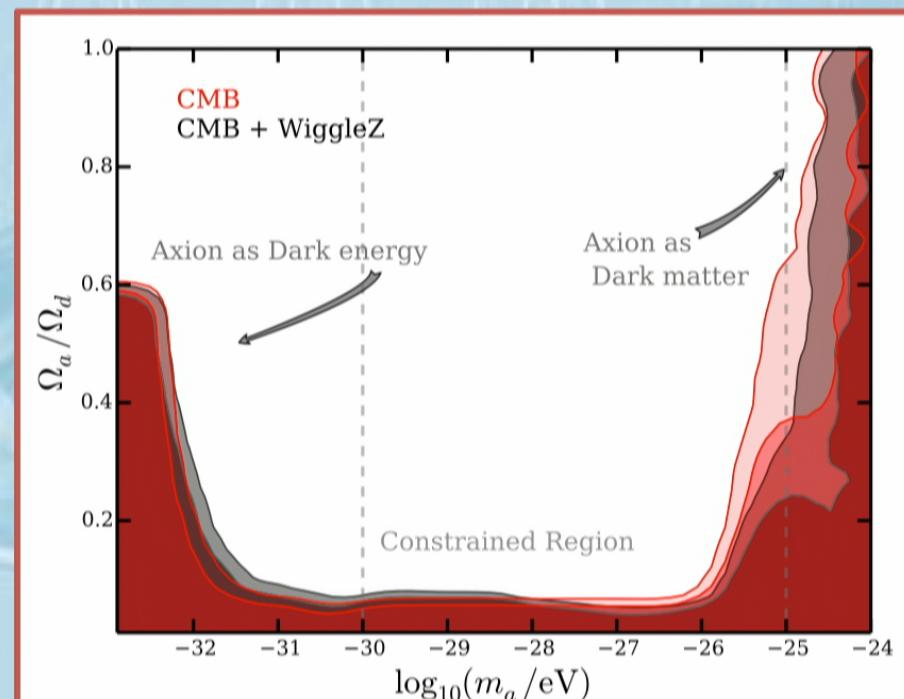
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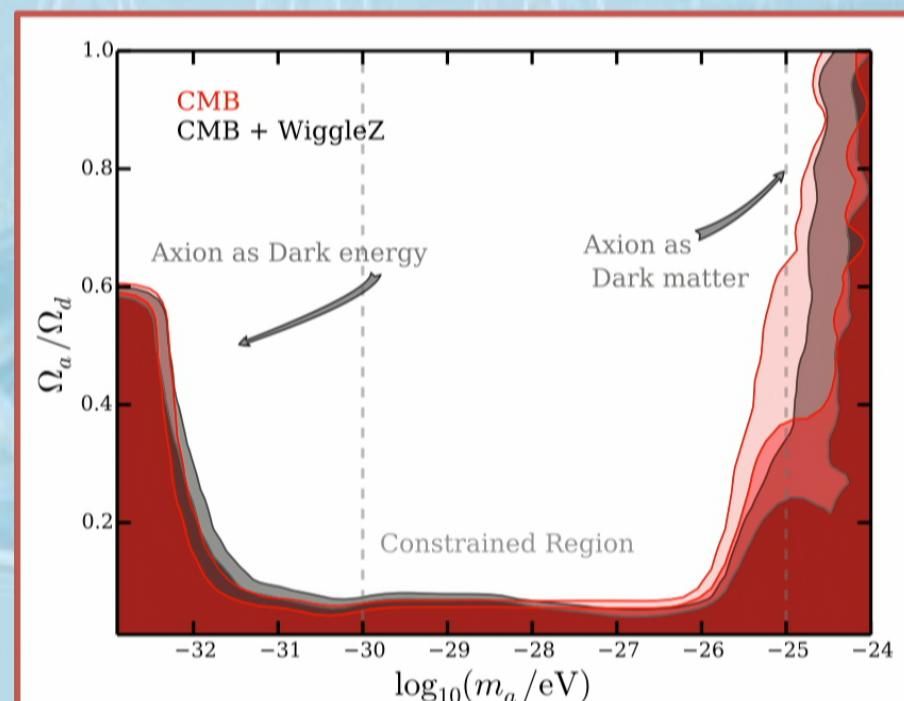
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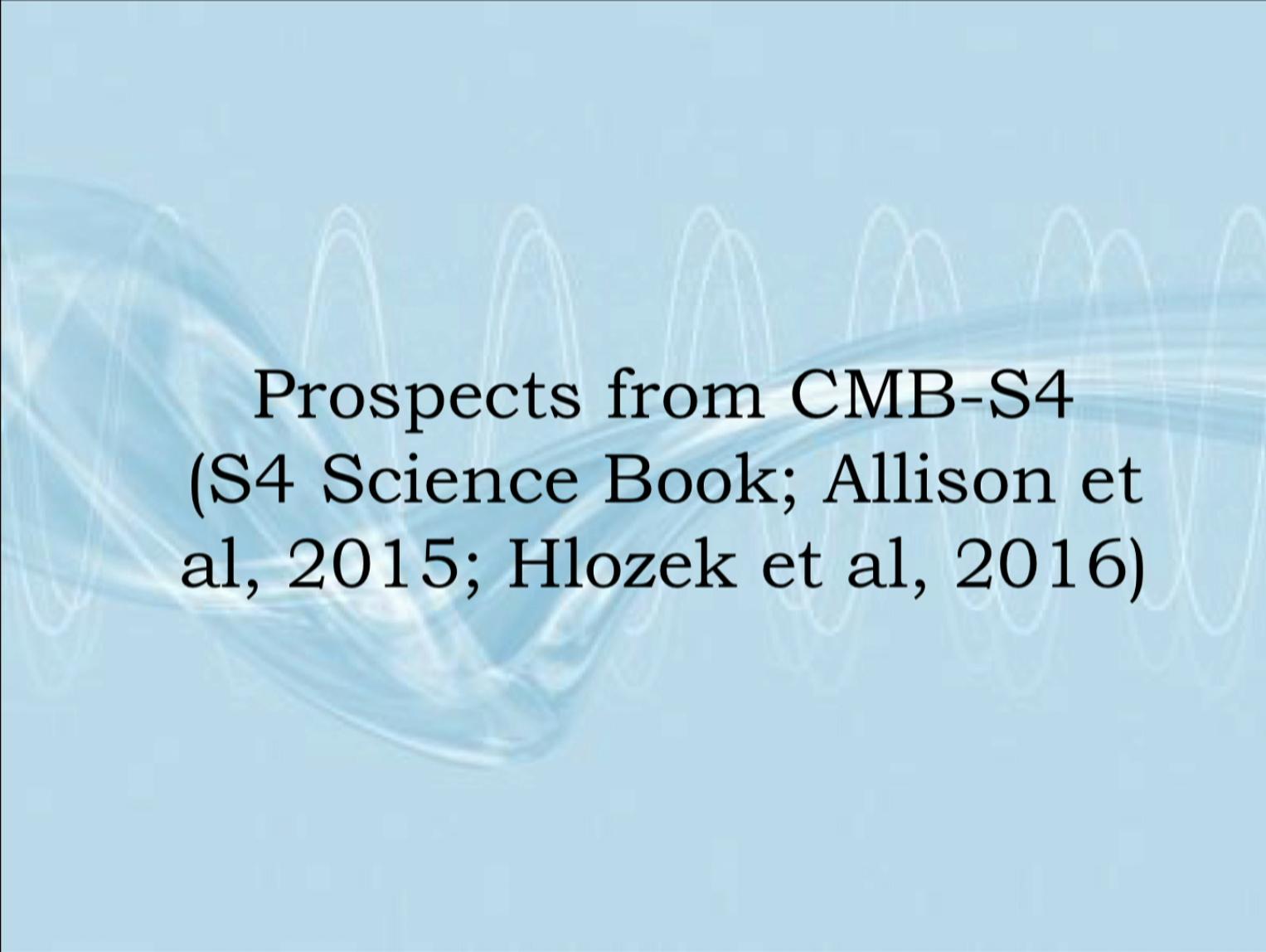
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# Prospects from CMB-S4 (S4 Science Book; Allison et al, 2015; Hlozek et al, 2016)

# Fisher Matrix Forecasts

Intro: e.g. Bassett et al (2011)

Approximate covariance matrix as inverse of Likelihood derivs

$$\mathcal{F}_{ij} = - \left\langle \frac{\partial^2 \ln P(\mathbf{D}|\boldsymbol{\Xi})}{\partial \Xi_i \partial \Xi_j} \right\rangle,$$

Assumes covariances are Gaussian: good for T, E,  $\kappa$ , not B.  
White noise power spectrum, foreground-cleaned to  
 $l_{\max}=3000$  (TT, kk), 4000; (TE, EE), pol is cleaner.

$$N_\ell^{\alpha\alpha} = (\Delta\alpha)^2 \exp\left(\frac{\ell(\ell+1)\theta_{\text{FWHM}}^2}{8 \ln 2}\right), \quad (\alpha = T, E, \kappa)$$

$f_{\text{sky}}$	Beam size (arcmin)	$\Delta T$ ( $\mu\text{K-arcmin}$ )	$\Delta E, B$ ( $\mu\text{K-arcmin}$ )
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lowP Planck, and  $\tau$  prior.  
LSS (e.g. DESI) with  $H_0$  prior.

S4-forecasts with “OxFish” (Allison et al, 2015) + axions.

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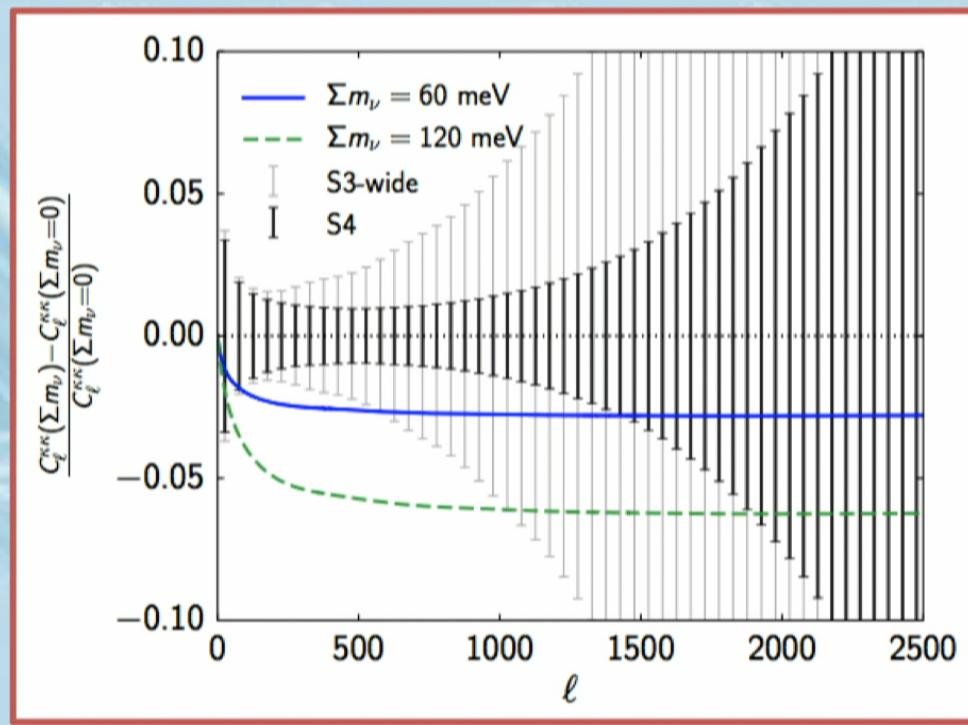
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# Detecting Neutrino Mass

Allison et al (2015)  
CMB-S4 Science Book

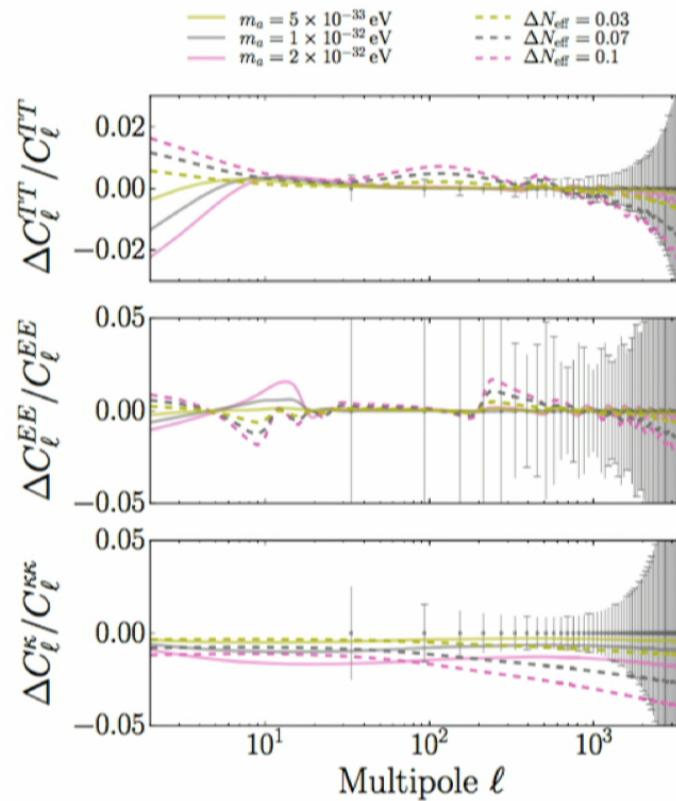
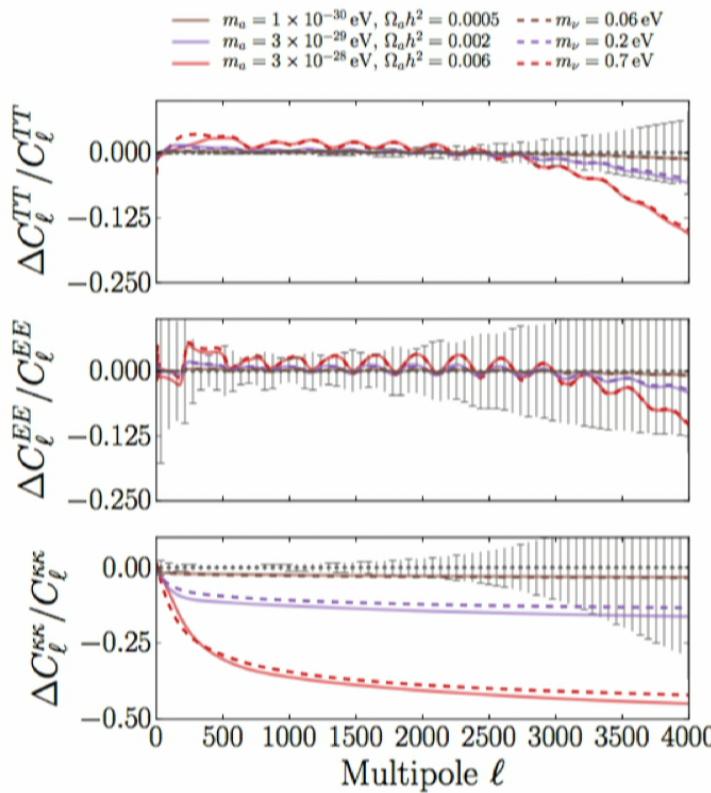
Neutrino mass seen by suppression of lensing power:



Need  $\tau$  prior (low- $\ell$  P) and BAO for  $\Omega_m$  to break degeneracies  
 $\sigma(m_\nu) = 15$  meV  $\rightarrow 4\sigma$  detection in minimal (normal hierarchy)

# ULA and Neutrino CMB Spectra

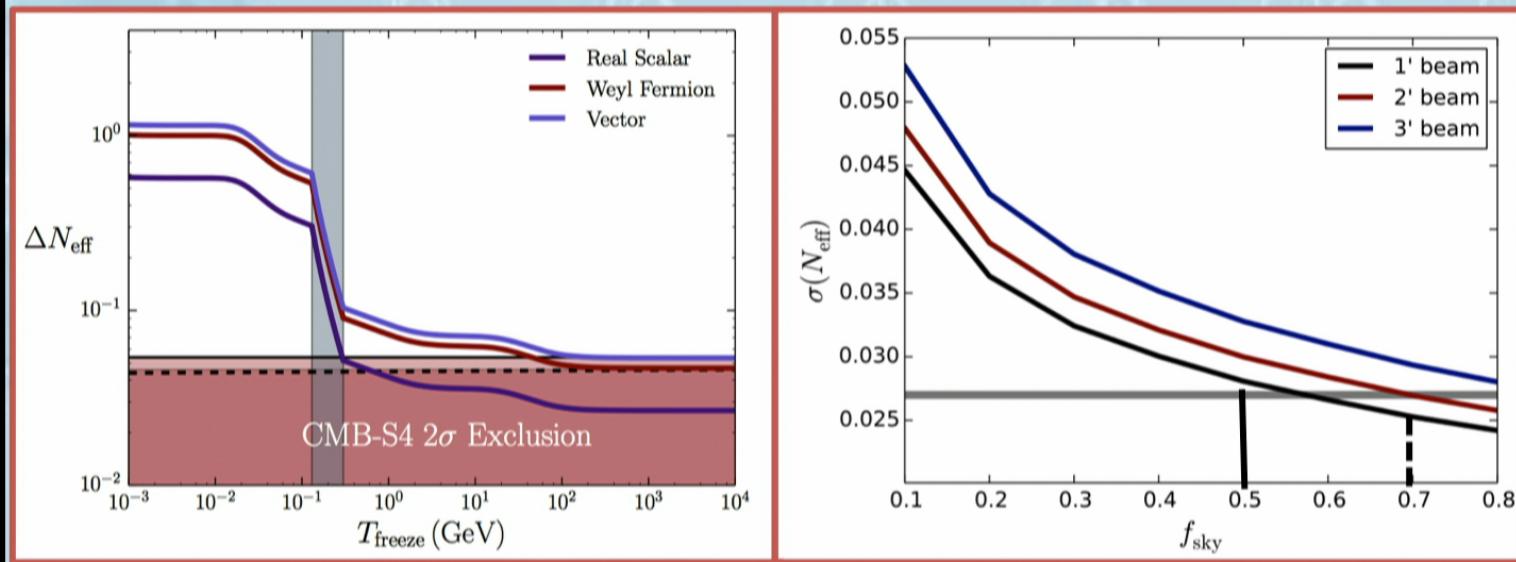
Choose axion models to try and mimic neutrinos.  
 Free streaming degenerate, DR versus DE background not.



# Relativistic Species

CMB-S4 Science Book

Factor  $O(10)$  improvement over Planck in  $\sigma(N_{\text{eff}})$ !

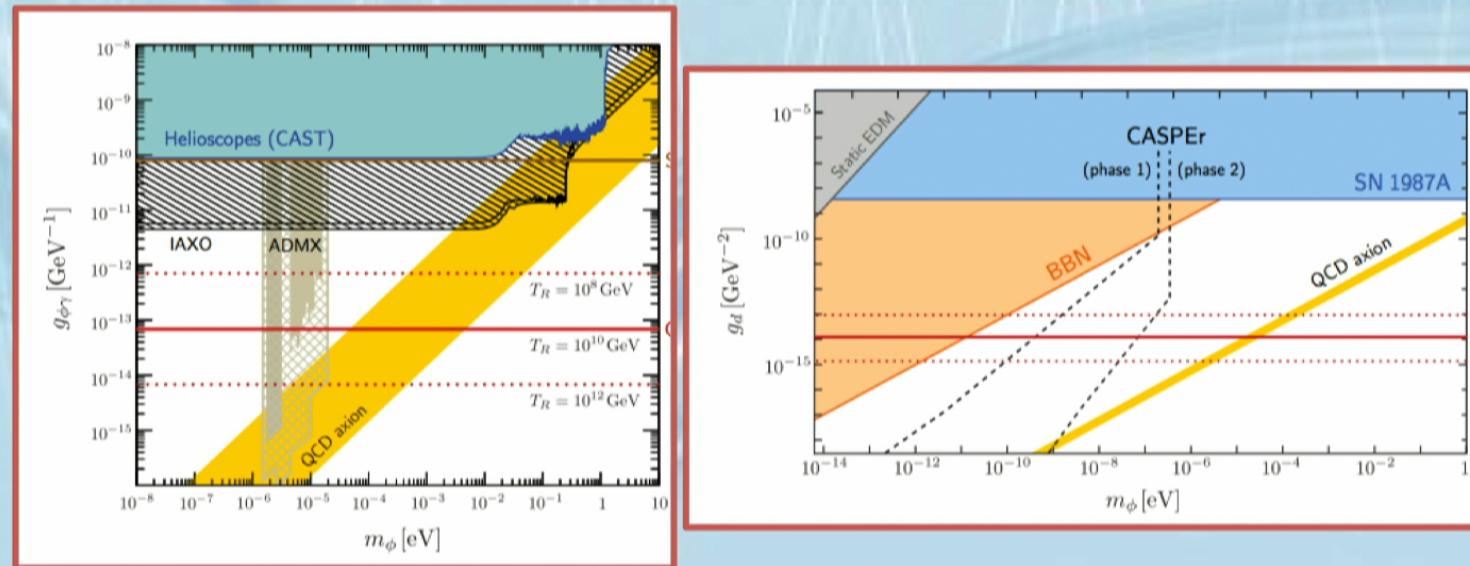


Reach  $2\sigma$  exclusions for fermion and vector ( $1\sigma$  for scalar).  
Survey design for narrow beam and wide survey  
→ Possible conflict with science goals for B-modes?

# Dark Radiation and Axions

Baumann et al (2016)  
CMB-S4 Science Book

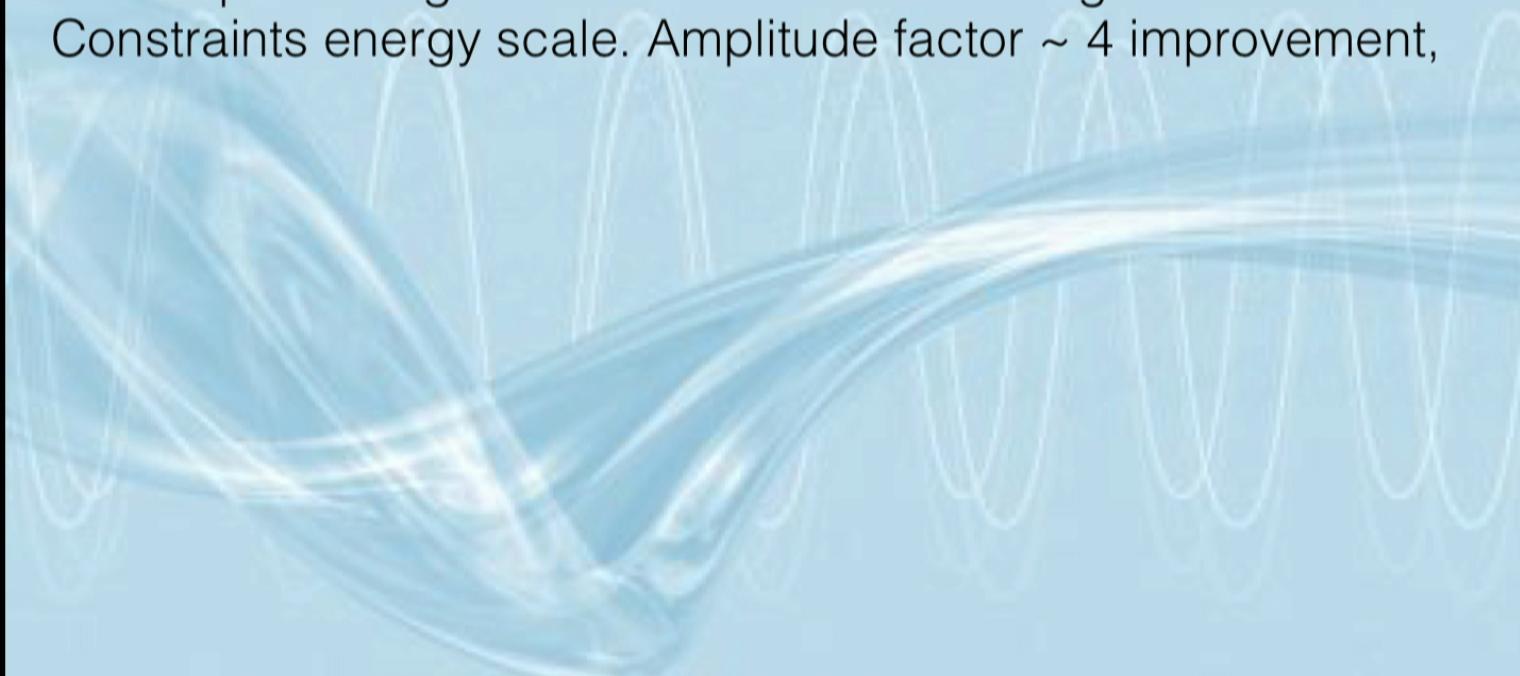
Thermal axions produced by photon or gluon couplings.  
Contribution to  $N_{\text{eff}}$  depends on  $T_F > T_{\text{reh}}$ . Take  $\Delta N_{\text{eff}} = 0.027$ .



Beat existing bounds, and assume nothing about axions as DM.

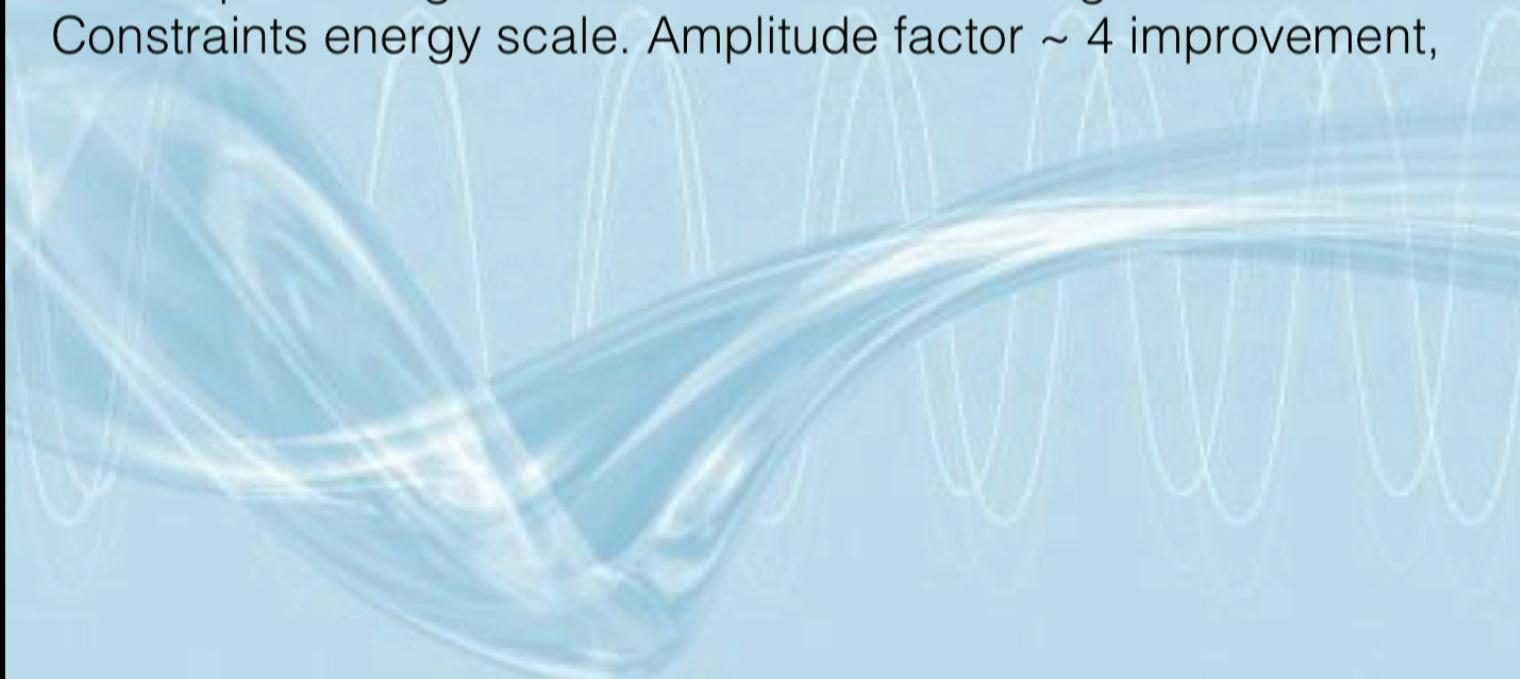
# Isocurvature and Direct Detection

Axion spectator generates isocurvature during inflation.  
Constraints energy scale. Amplitude factor  $\sim 4$  improvement,



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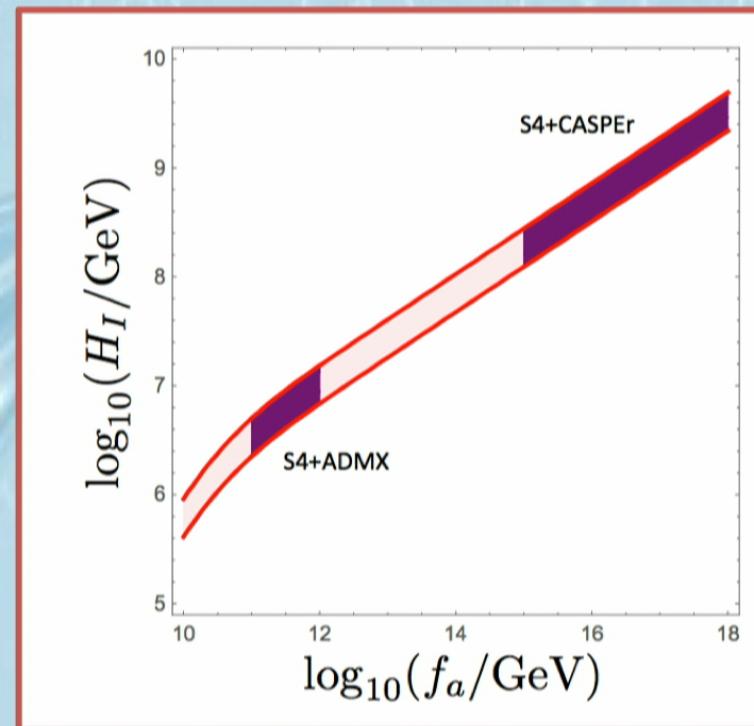
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$$10^6 \text{ GeV} \lesssim H_I \lesssim 10^{10} \text{ GeV}$$

Probe totally different range  
of inflationary models!

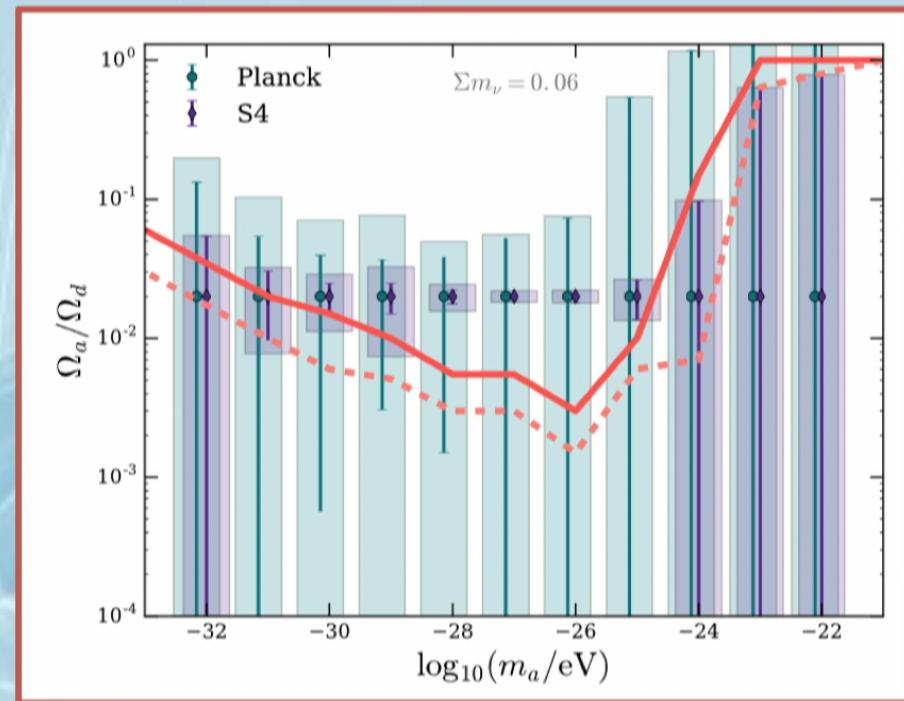


DJEM et al & CMB-S4 Science Book

# ULAs and Tests of CDM

Hlozek et al (2016)

- Bin by mass, include neutrinos, ULA fraction consistent with Planck.
- Error bars: with/w-out marginalise over  $m_\nu$ .
- Fiducial 2% ULAs detectable at  $> 13\sigma$ !
- Lines: 1 and  $2\sigma$  exclusions.

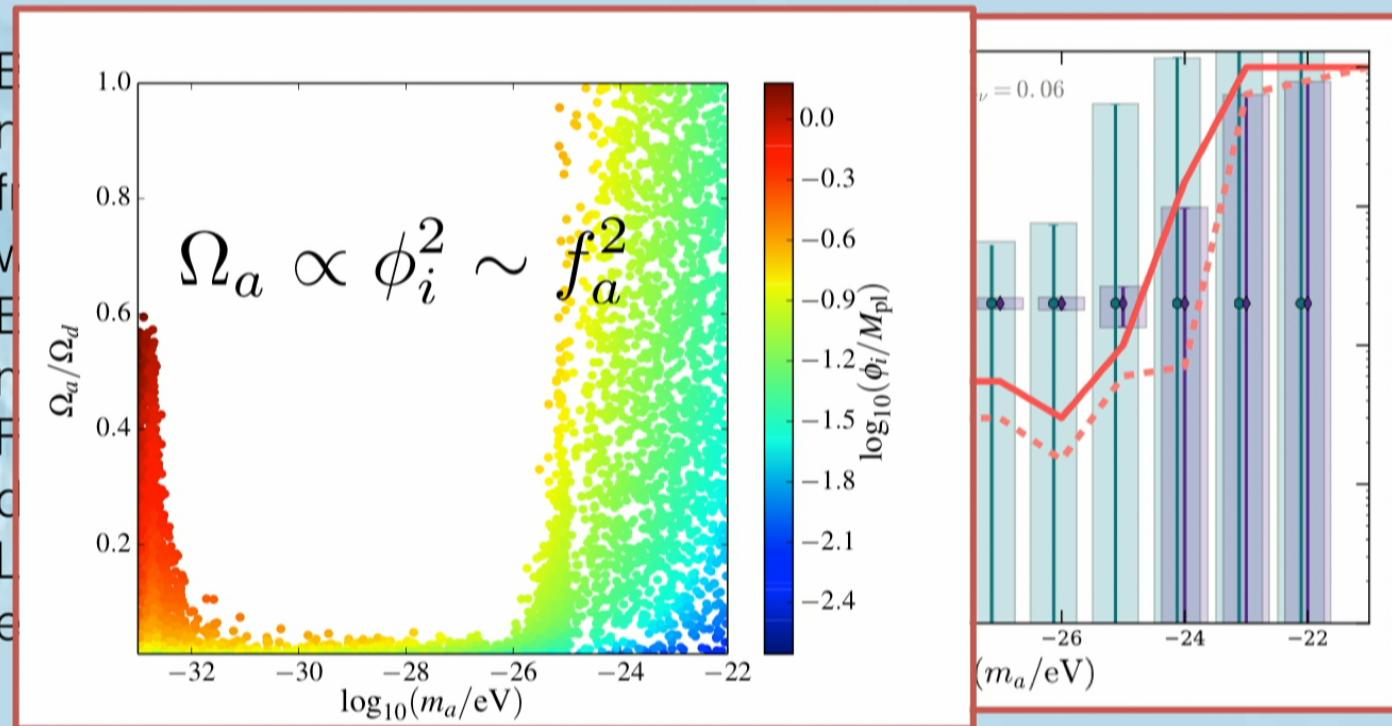


CMB-S4 will test the “one component CDM paradigm” at the sub-percent level. Probes decay constants at < GUT scale.

# ULAs and Tests of CDM

Hlozek et al (2016)

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- E
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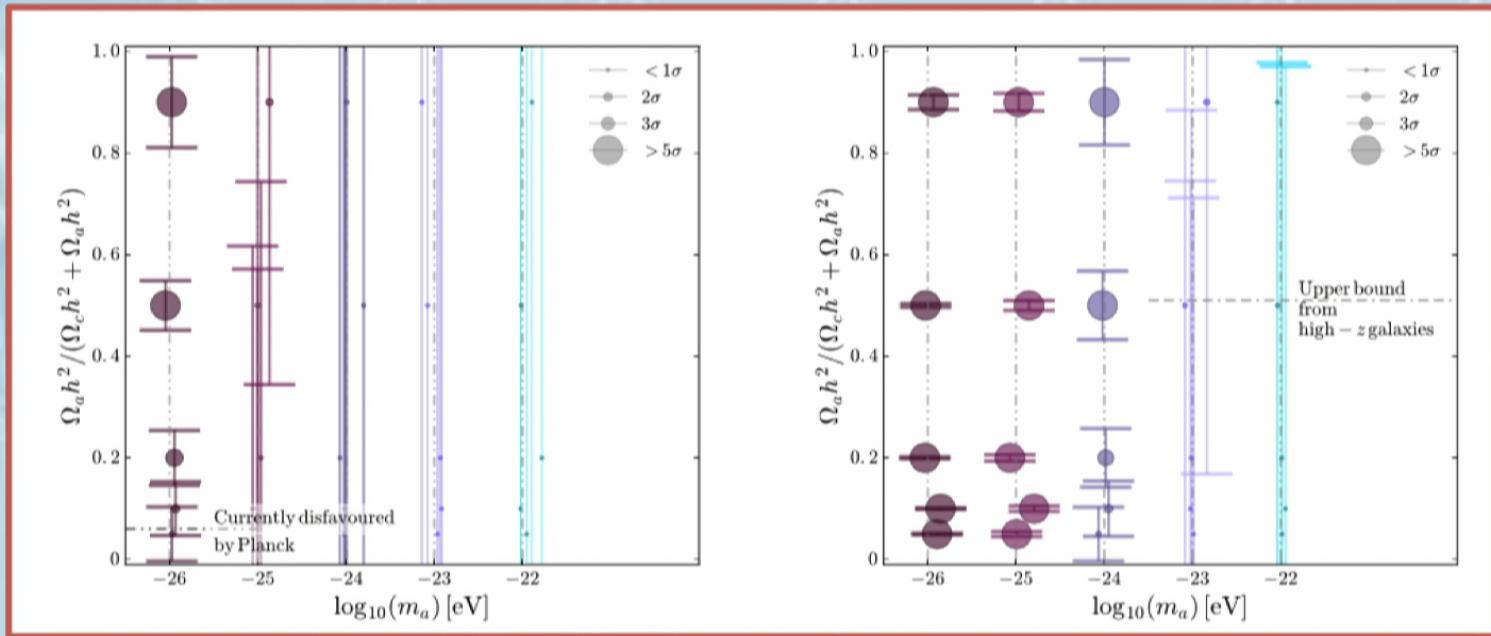


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# Lower limit on DM mass

Hlozek et al (2016)

Vary fiducial fraction. Ball-size → detection significance.

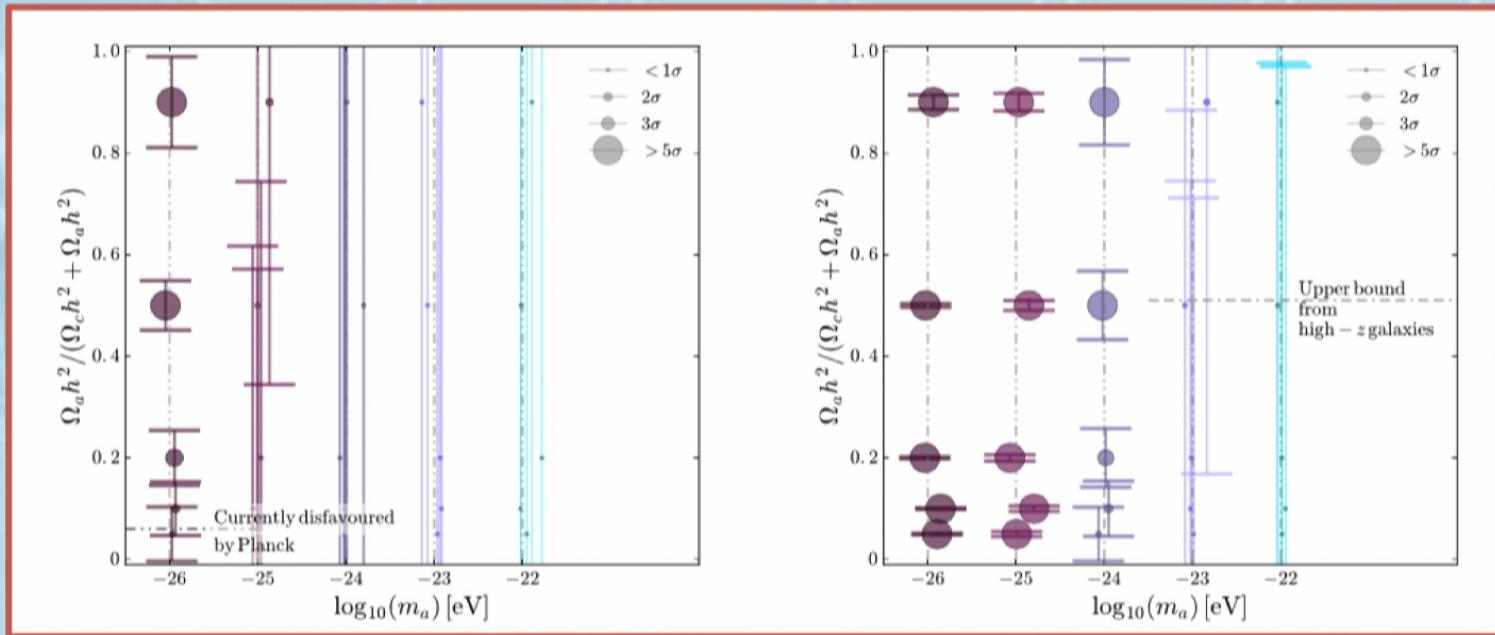


Improve precision region by 2 orders of magnitude over Planck.  
Exclude dominant DM at  $m \sim 10^{-23}$  eV → contact to high-z  
galaxies and “Fuzzy DM” in small-scale-problems. e.g. DJEM & Silk (2013)

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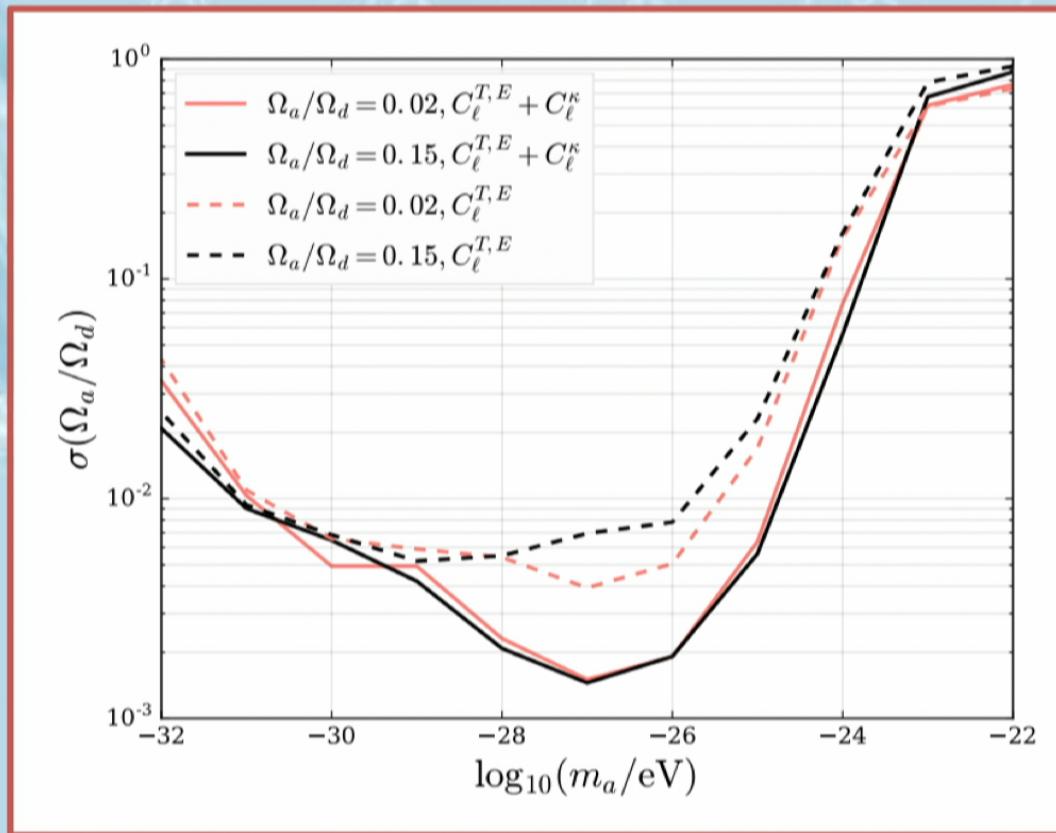


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# The Role of Lensing

Hlozek et al (2016)

Improvements by factor >2 for “DM-like”. Important at high m.



# Non-linear Axions and Lensing: A Cautionary Tale

DJEM: 1605.05973, Hlozek et al: 1607.08208

# Lensing Power

Lensing is an integral along the line of sight of the potential:

$$C_\ell^{\phi\phi} = \frac{8\pi^2}{\ell^3} \int_0^{z_{\text{rec}}} dz \mathcal{P}_\Psi(\ell/x, z) x \frac{dx}{dz} \left( \frac{x_{\text{rec}} - x}{x_{\text{rec}} x} \right)^2.$$

Potential related to matter dist. by Poisson equation. On small-scales/late times matter collapses into halos  $\rightarrow$  non-lin.

$$\mathcal{P}_{\Psi, \text{non-lin}}(k, z) = \frac{P_{m, \text{non-lin}}(k, z)}{P_{m, \text{lin}}(k, z)} \mathcal{P}_{\Psi, \text{lin}}(k, z)$$

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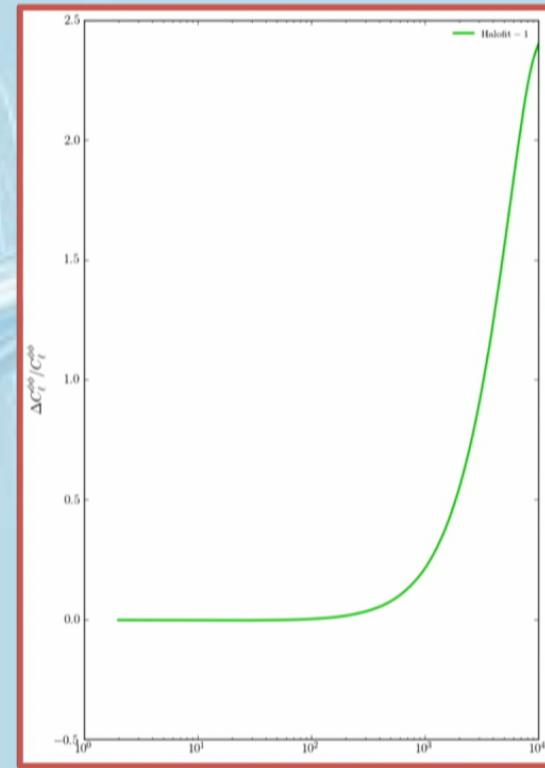
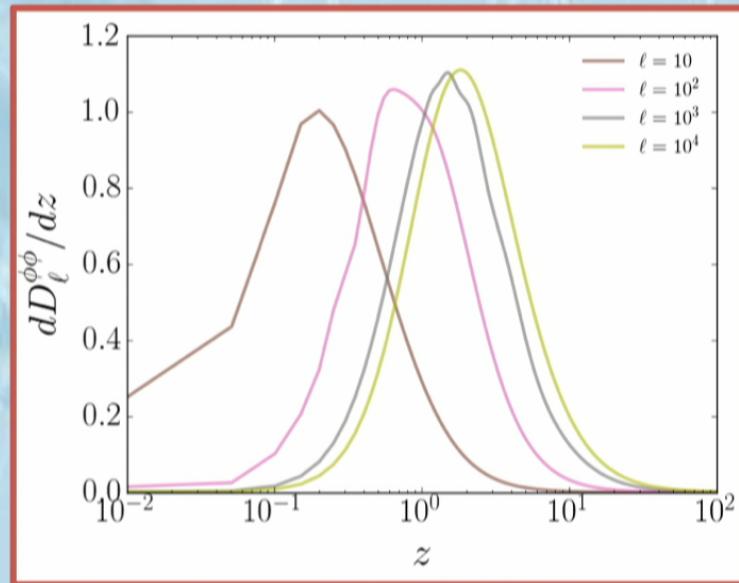
Need to approximate non-lin for integral. But how?

CAMB: uses “halofit” formula, from CDM(+ $\nu$ ) simulations.

Smith et al (2003), Bird et al (2012)

# Lensing Power

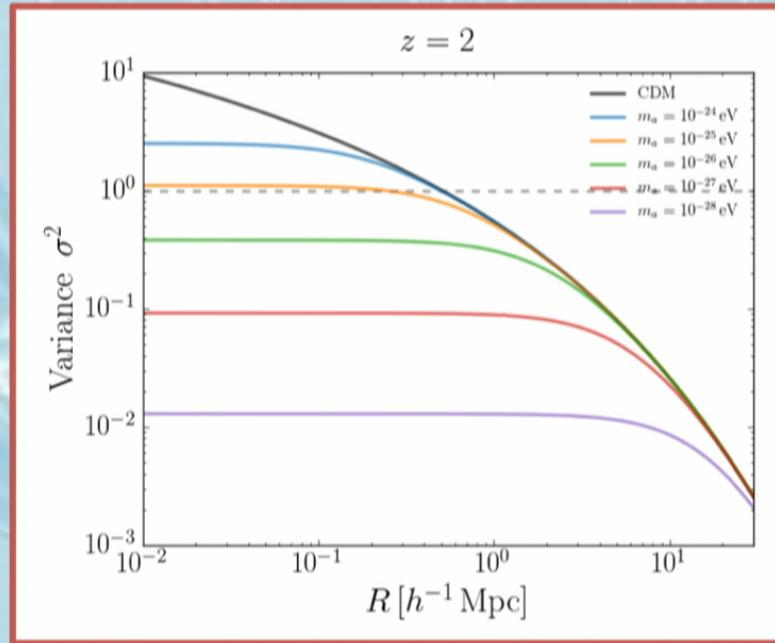
When are non-linearities important?



In lensing, >10% by  $\ell=1000$ , coming from collapse at  $z \sim 2$ .

# What do we treat as “collapsed”?

$\delta \sim 1$ : Halofit defines non-linear scale from  $\sigma_m^2(R_{\text{nl}}) = 1$ .  
Ideally, test this on a component basis. But let's cheat...



→ Only  $m > 10^{-25}$  eV non-lin on scales relevant to lensing.  
(+sub-dominant and large Jeans → no effect on forecasts)

# The Halo Model

e.g. Cooray and Sheth (2002)

For heavy axions as all DM, must use something better.

Halo model code “WarmAndFuzzy” for  $P(k)$ . Mead et al (2015); DJEM (2016)

Image: Hlozek et al (2016)



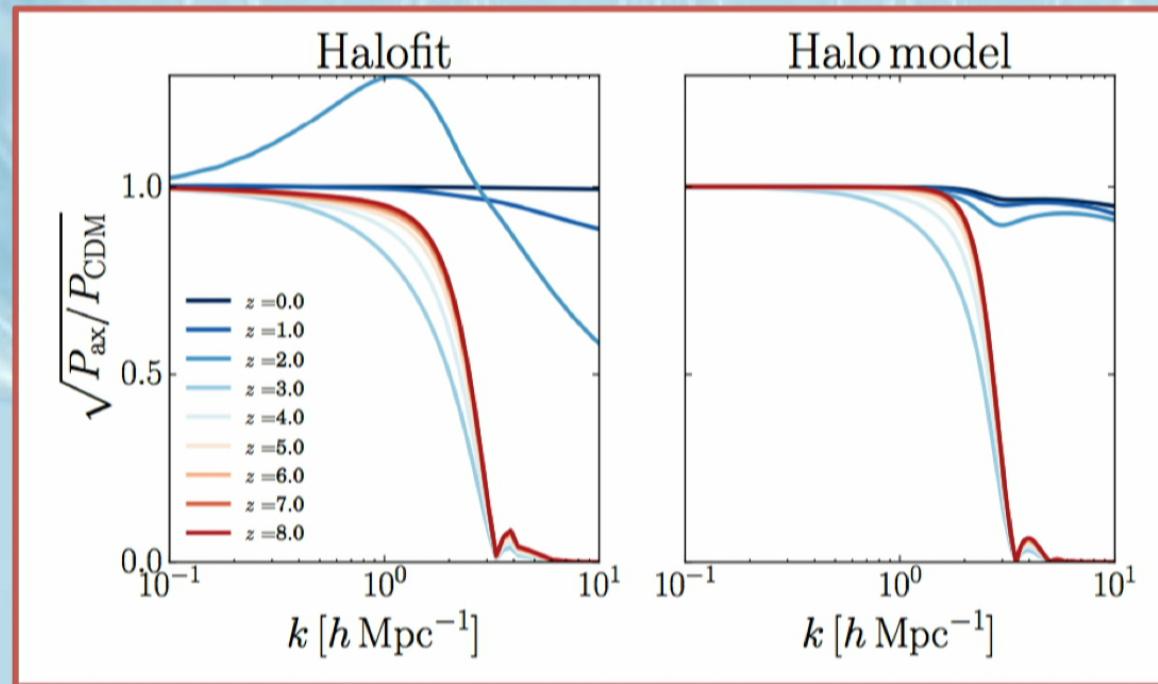
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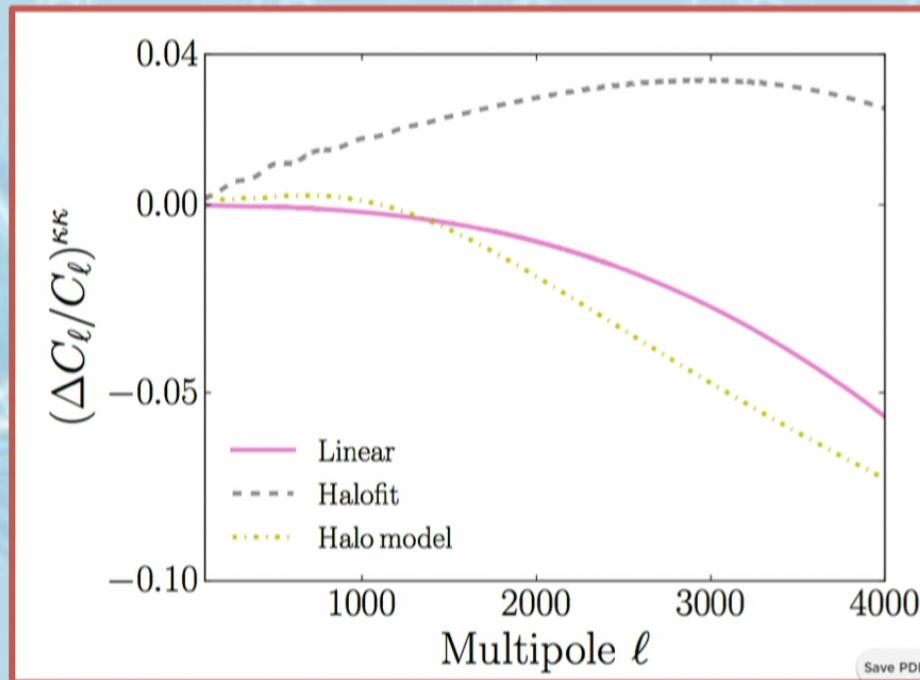


For most interesting masses  $m \sim 10^{-23}$  eV Halofit goes v. wrong!

# Halo Models and Lensing

Hlozek et al (2016)

Halo model NOT integrated into CAMB: need a quick fix.



Linear theory captures sign and magnitude of halo model.  
→ Can use linear theory for forecasts, BUT NOT DATA!

# Conclusions

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- CMB-S4: proposed upgrades for 2020.
- Science goals:  $\sigma(r) \sim 0.001$ ,  $\sigma(m_\nu) \sim 15 \text{ meV}$ ,  $\sigma(N_{\text{eff}}) \sim 0.027$
- Extra DM science: neutrinos degeneracies, new light species, isocurvature and axion detection.
- Axions: detect  $\sim 1\%$  fractions at many  $\sigma \rightarrow$  test CDM paradigm over a vast range of scales!
- Lower limit on DM mass improved by  $\sim 2$  orders of magnitude. Requires new understanding of non-lin effects.

Things I have left out: DM annihilations and ionization, sterile neutrinos, neutrino hierarchy, DE/Modified Gravity, B-modes, de-lensing, foregrounds ...

Contributing yourself, via github: fork us!

axionCAMB: [github.com/dgrin1/axionCAMB](https://github.com/dgrin1/axionCAMB)

WarmAndFuzzy: [github.com/DoddyPhysics/HMcode](https://github.com/DoddyPhysics/HMcode)

## Black hole formation from axion stars

Thomas Helfer,<sup>1</sup> David J. E. Marsh,<sup>1</sup> Katy Clough,<sup>1</sup> Malcolm Fairbairn,<sup>1</sup> Eugene A. Lim,<sup>1</sup> and Ricardo Becerril<sup>2</sup>

<sup>1</sup>*King's College London, Strand, London, WC2R 2LS, United Kingdom*

<sup>2</sup>*Instituto de Física y Matemáticas, Universidad Michoacana de San Nicolás de Hidalgo, Ciudad Universitaria, CP 58040 Morelia, Michoacán, Mexico.*

(Dated: September 11, 2016)

The classical equations of motion for an axion with potential  $V(\phi) = m_a^2 f_a^2 [1 - \cos(\phi/f_a)]$  possess quasi-stable, localized, oscillating solutions, which we refer to as “axion stars”. We study, for the first time, collapse of axion stars numerically using the full non-linear Einstein equations of general relativity and the full non-perturbative cosine potential. We map regions on an “axion star stability diagram”, parameterized by the initial ADM mass,  $M_{\text{ADM}}$ , and axion decay constant,  $f_a$ . We

## Unbiased constraint on ultralight axions from dwarf spheroidal galaxies

Alma X. Gonzalez-Morales<sup>1,2\*</sup>, David J. E. Marsh<sup>3</sup>,  
Jorge Peñarrubia<sup>4</sup>, and Luis Ureña-Lopez<sup>2</sup>

<sup>1</sup>*División de Ciencias e ingenierías, Universidad de Guanajuato, Leon, Guanajuato, Mexico*

<sup>2</sup>*CONACYT*

<sup>3</sup>*Department of Physics, King's College London, Strand, London, WC2R 2LS, UK*

<sup>4</sup>*Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK*