

Title: Quantum Thermodynamics

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Abstract:

What is ^{quantum} thermodynamics?

- 3 laws
- Resource Theory

Many second laws

Embezzling work

Q Fluctuation relations

Third law

1st law

2nd law

$$dE = dQ - dW$$

conservation of energy

heat can never pass from a cold system to a warm one without some other "change" occurring elsewhere

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$$F = \langle E \rangle - TS(p)$$

$$\langle W \rangle \leq \Delta F$$

$$\Delta F \leq 0$$

O^{th} T_1 in equil w/ T_2

T_2

T_3

$\rightarrow T$

T_3

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$\mathcal{C}$ class of operations Λ_c

$\mathcal{F}$ free states

$$D(\Lambda_c(\rho) \| \Lambda_c(\sigma)) \leq D(\rho \| \sigma)$$

$$F_c := \inf_{\sigma \in \mathcal{F}} D(\rho \| \sigma)$$

$$\inf_{\sigma \in \mathcal{F}} D(\Lambda(\rho) \| \Lambda(\sigma)) = D(\rho' \| \sigma') \geq \inf_{\sigma \in \mathcal{F}} D(\rho' \| \sigma)$$

(Catalytic) Thermal Operations (C) T.O.

- ρ_s, H_s

quasi-classical $[\rho_s, H_s] = 0$

- Free γ_B, H_R

- w, H_w

$[\Delta, H_w] = -i$ $H_w = \sum \omega_n |n\rangle\langle n|$

- $[U, H_s + H_R + H_w] = 0$

- $[U, \Delta] = 0$

- allow borrowing σ_c, H_c as long as it's returned in the "same" state



0th law $\gamma_B = e^{-\beta H_R} / Z$, H_R or we can draw
 an arbitrarily large amount of work
 (complete passivity)

$$\Lambda(\gamma_B) = \gamma_B$$

$$TD_1(p \| \gamma_B) = \mathbb{E}[\text{tr} p \log p - \text{tr} p \log \gamma_B] \\ = \langle E \rangle - TS + \log Z$$

take $H_S = H_R = 0$

Λ is a doubly stochastic map

$\rho \rightarrow \sigma$ iff $\rho \succ \sigma$

$$D_\alpha(\rho|\sigma) = \frac{1}{1-\alpha} \log \text{tr} \rho^\alpha \sigma^{1-\alpha}$$

$D_\alpha(\rho|\gamma_\beta)$ is a monotone under (C)TO

$$\rho \xrightarrow{\text{CTO}} \sigma \quad \text{iff} \quad D_\alpha(\rho|\gamma_\beta) \geq D_\alpha(\sigma|\gamma_\beta)$$

in thermodynamic limit $D_\alpha \stackrel{\alpha \rightarrow 0}{\sim} D_1$

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Equality version of second law

$$\langle e^{\beta W} \rangle = e^{\beta \Delta F}$$

$$D_\alpha(p||q) = \frac{1}{1-\alpha} \log \text{tr} \rho^\alpha \sigma^{1-\alpha} \left| \sum_s p(s', w|s) e^{-\beta E_{s'}} = e^{-\beta E_s} \right.$$

$D_\alpha(p||\gamma_\beta)$ is a monotone under (C)TO

$$\rho \xrightarrow{\text{CTO}} \sigma \quad \text{iff} \quad D_\alpha(\rho||\gamma_\beta) \geq D_\alpha(\sigma||\gamma_\beta)$$

in thermodynamic limit $D_\alpha \approx D_1^{\alpha \geq 0}$

$$\sigma^{1-\alpha} \left[\sum_s p(s', w | s) e^{-\beta E_s + w\beta} \right]^{-\alpha} = e^{-\beta E_{s'}}$$

is a monotone under (C)TO

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to $(\rightarrow 0)$ many
number of steps

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$$\langle e^{\beta W} \rangle = e^{\beta \Delta F}$$

$$\sum_{ssw} e^{\beta W} p(s, s', w)$$

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