

Title: Weak and continuous measurements in superconducting circuits

Date: Jun 20, 2016 04:00 PM

URL: <http://pirsa.org/16060040>

Abstract: Superconducting circuit technology has rapidly developed over the past several years to become a leading contender for realizing a scalable quantum computer. Modern circuit designs are based on the transmon qubit, which coherently superposes macroscopic charge oscillations. Measurements of a transmon are fundamentally weak and continuous in time, with projective measurements emerging only after a finite duration. Adding gates, such measurements may then implement ancilla-based measurements of controllable strength. Recent experiments have used both types of weak measurement to great effect: for monitoring qubit evolution, and for showing violations of a hybrid Bell-Leggett-Garg inequality.

# Institute for Quantum Studies



**Luis Pedro García-Pintos**  
Postdoctoral Scholar

## Group



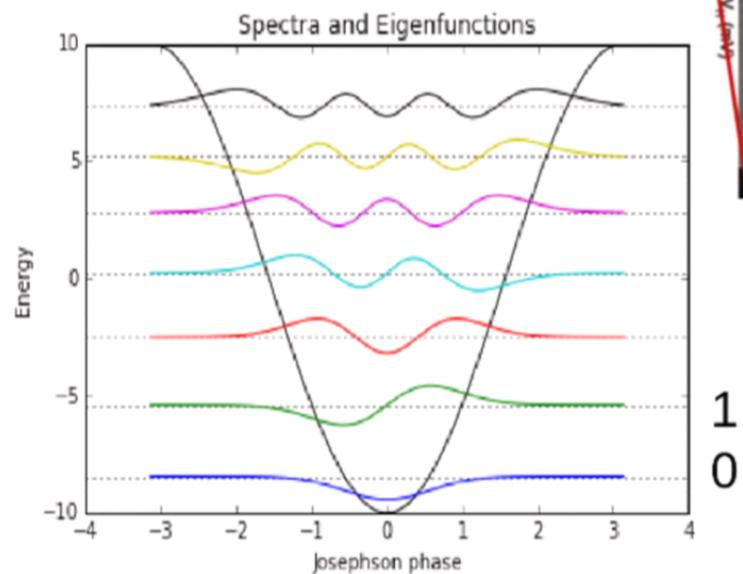
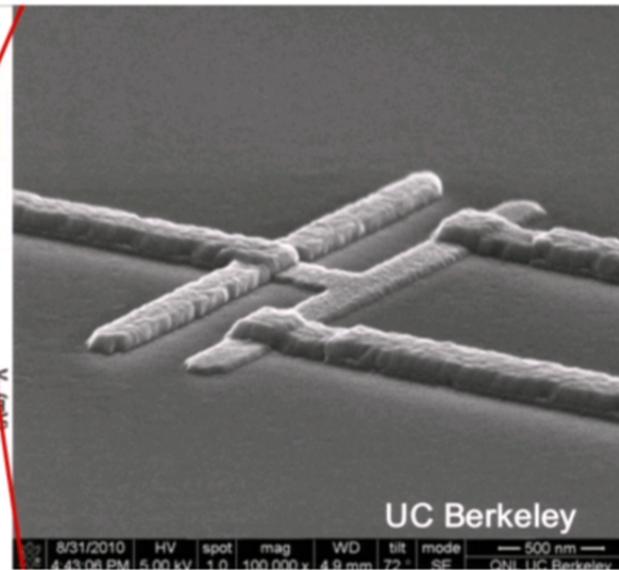
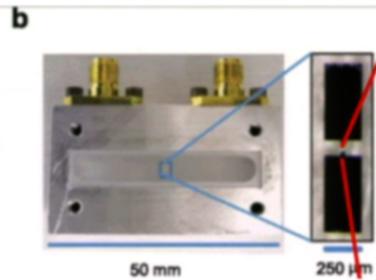
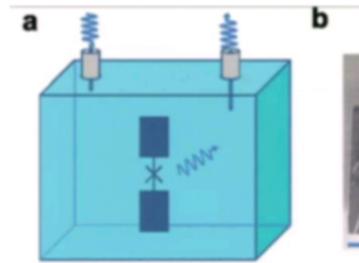
**Shiva Barzili**  
Graduate Student

# Outline

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- Superconducting qubit technology overview
- Weak continuous monitoring of a Rabi drive
  - Stochastic readout filtering and quantum state trajectories
  - Time-symmetric signal smoothing
  - Weak-valued state estimation, and jump dynamics
- Partial projections and weak measurements
- Hybrid Bell-Leggett-Garg inequality violation with weak measurements

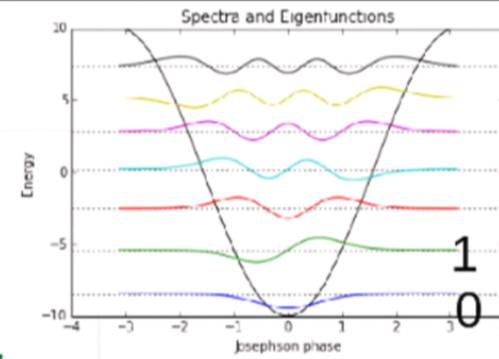
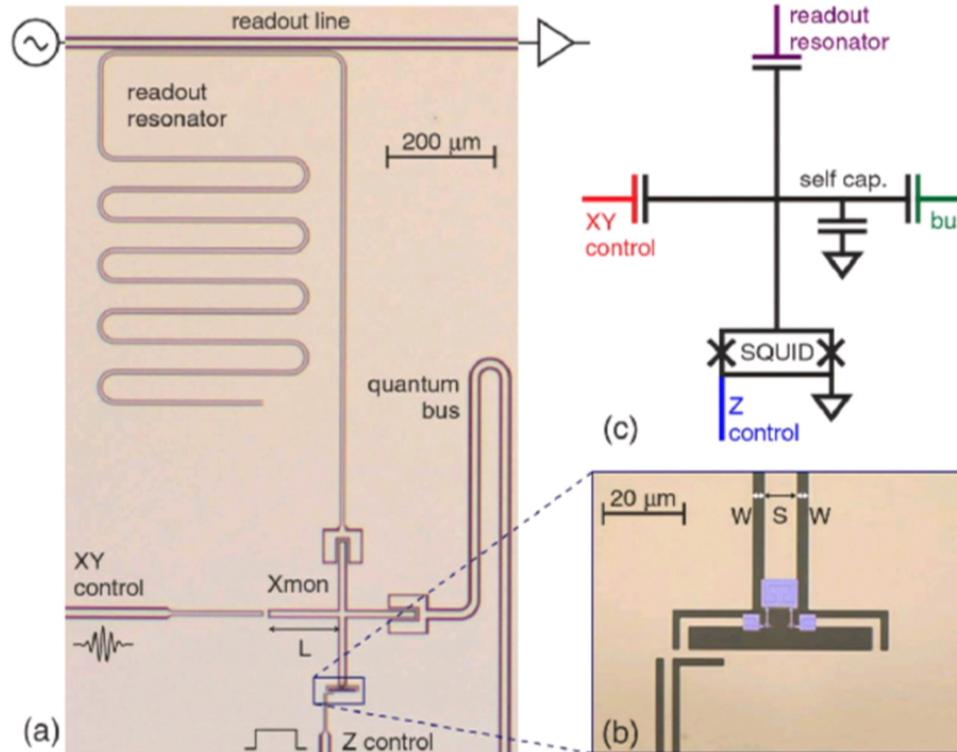
# Superconducting 3D Transmon qubit



Transmon is LC oscillator  
with nonlinear inductance  
from a Josephson junction

**qubit is the lowest two  
energy levels in a cosine  
potential well**

# 2D planar Xmon qubit

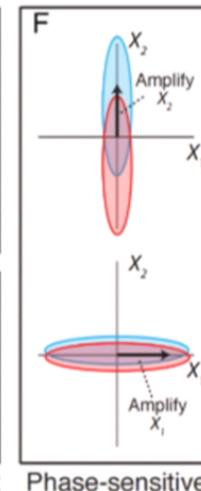
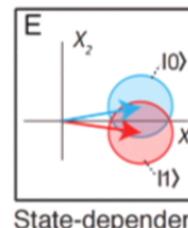
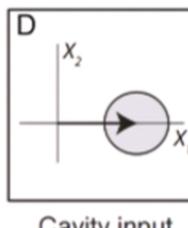
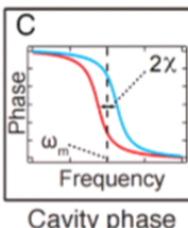
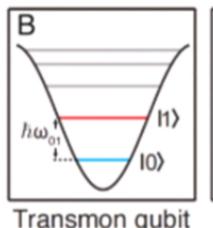
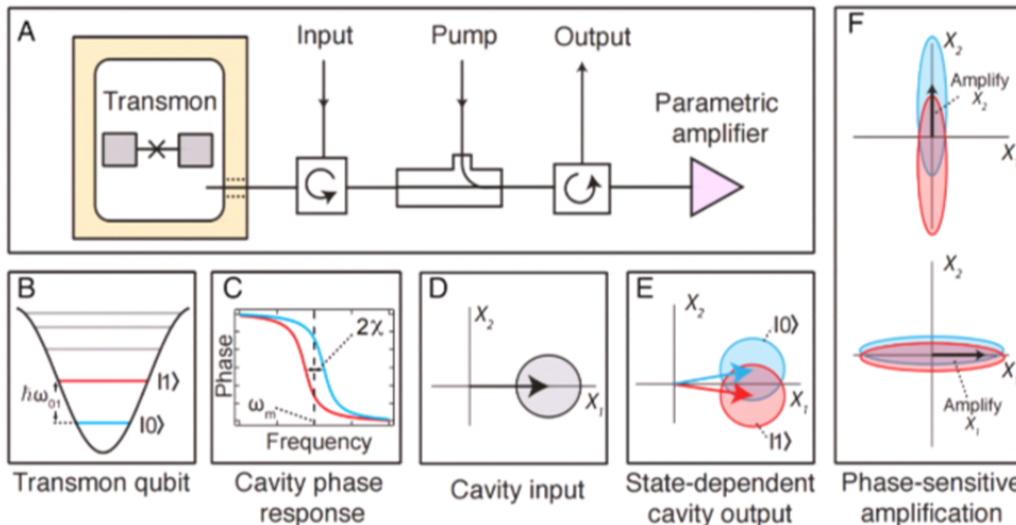


Xmon is a modified transmon optimized for a 2D lattice layout with nearest neighbor capacitive coupling

double Josephson junctions (SQUID) for flux control of qubit frequency

PRL 111, 080502 (2013)

# Circuit QED Qubit Measurement



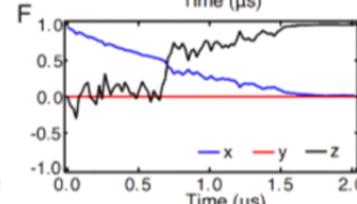
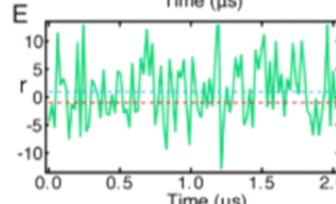
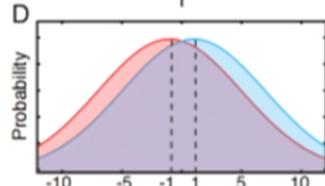
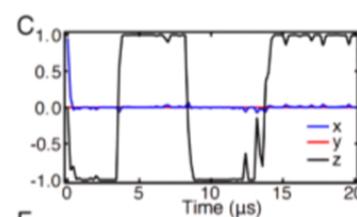
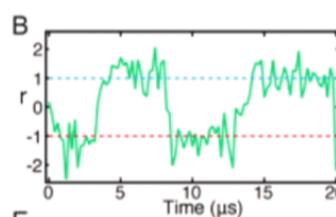
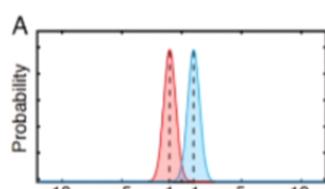
**Problem:** Transmon on chip inside fridge – how to measure?

**Solution:** Use microwaves to peek at state-dependent frequency shift

**Signal:** Continuous noisy homodyne readout

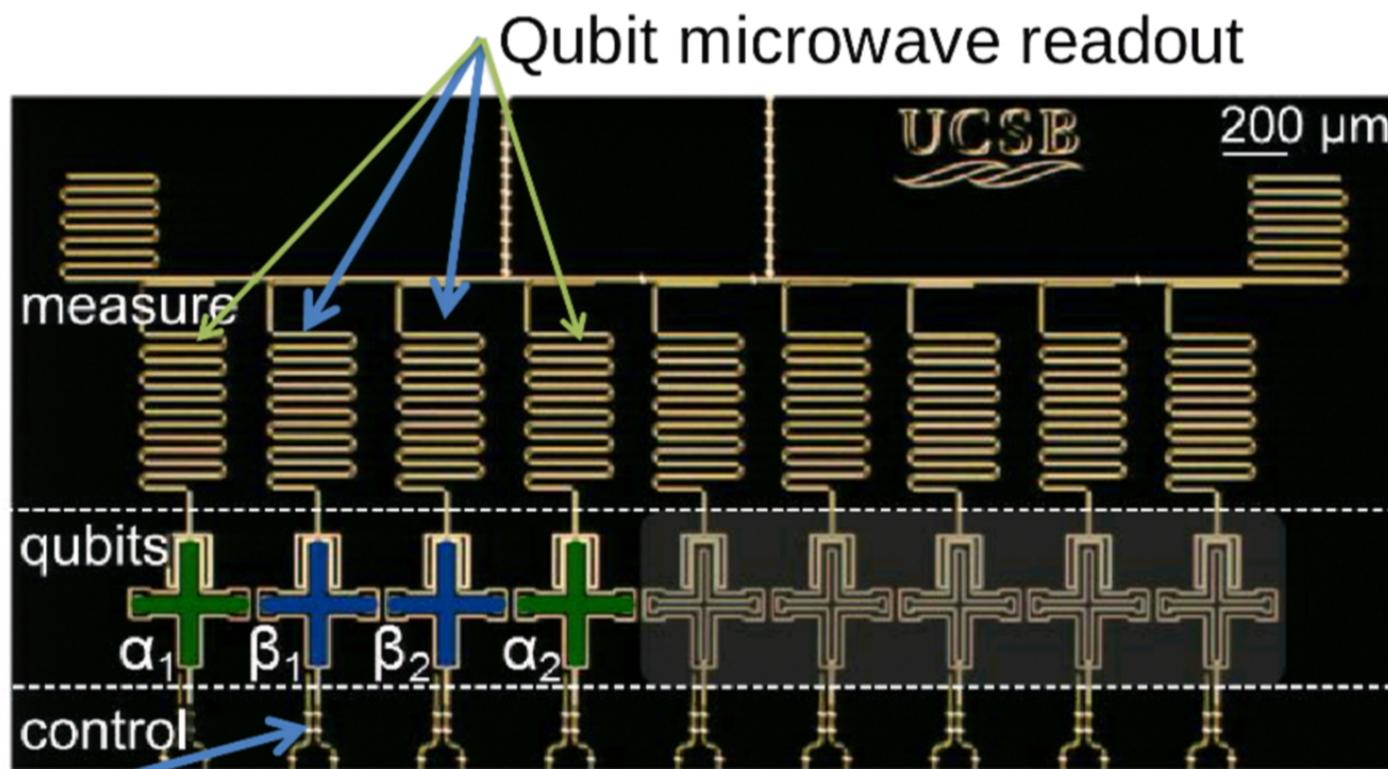
**Histograms:** Gaussians centered on state-dependent means

**Strength:** Wide, overlapping peaks are weak (noisy) measurements that partially collapse the qubit less per unit time



arXiv:1506.08165

## 9 Xmon individual qubit control



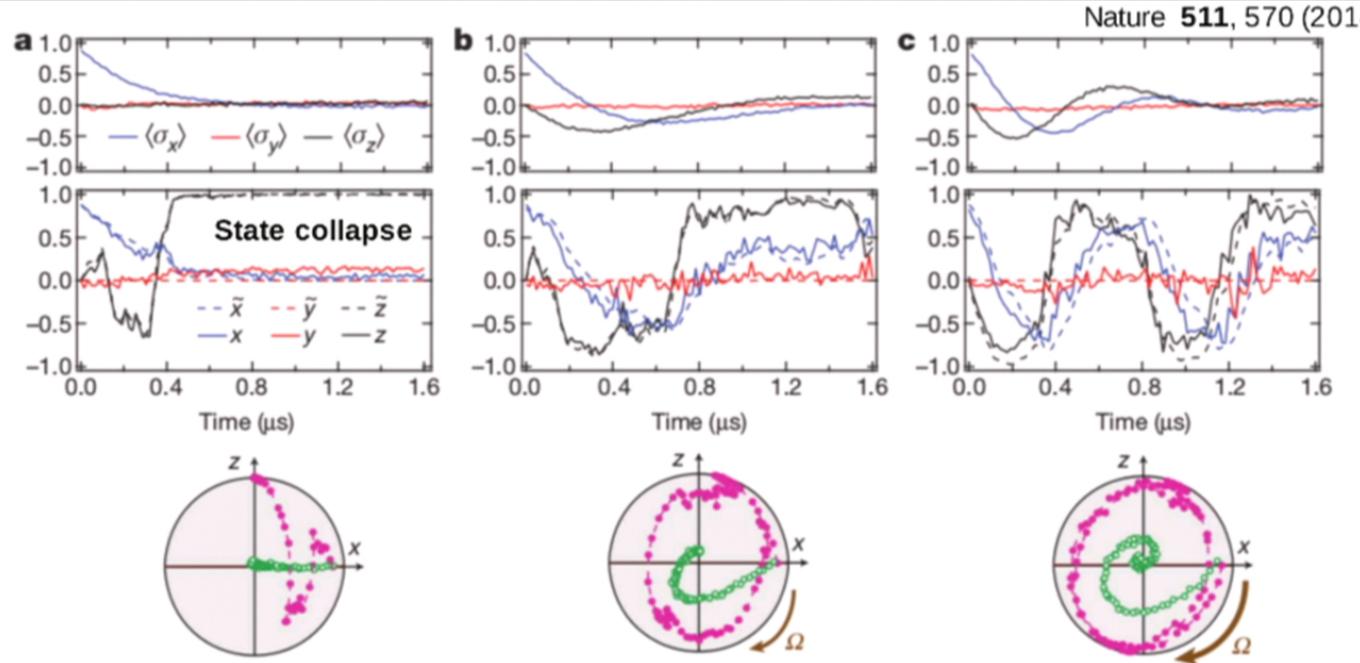
Individual  
microwave  
controls

DC pulses: qubit-qubit ZZ interactions  
AC pulses: fast single-qubit rotation gates

# Outline

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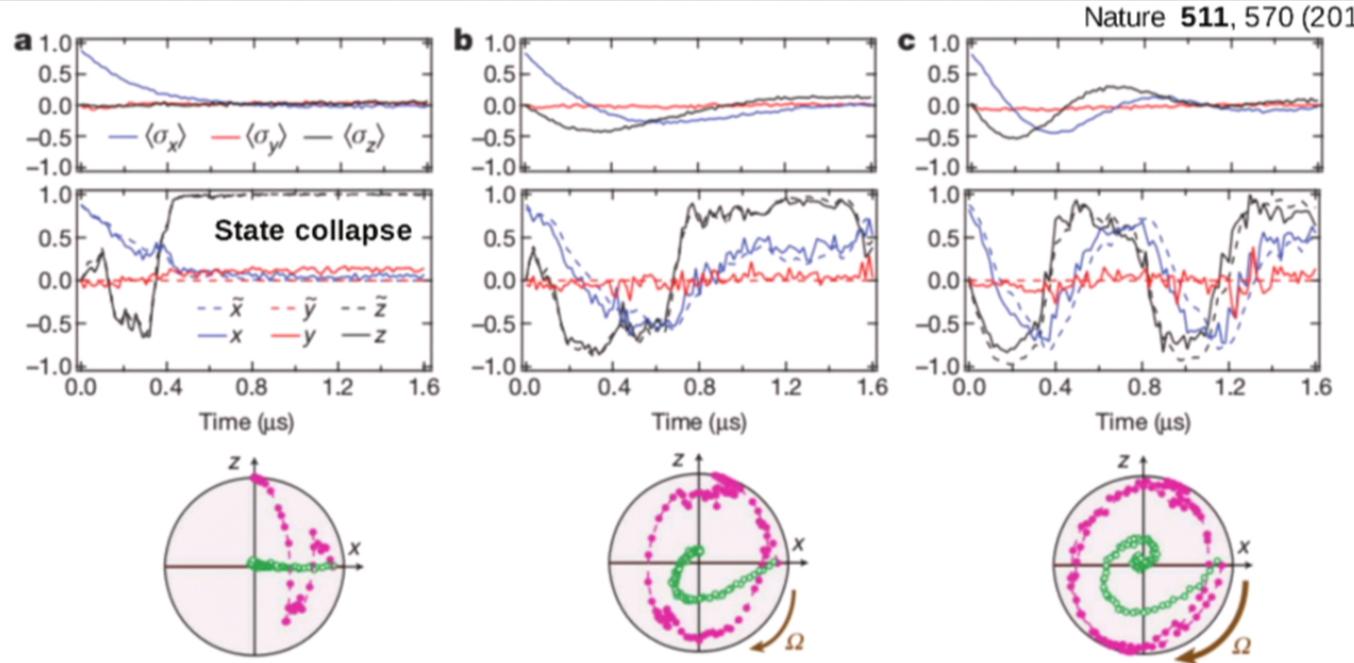
# Weakly Monitoring a Rabi Drive



**Pink:** Individual quantum trajectory – stochastic dynamics  
(best state tracking estimate given collected readout)

**Green:** Ensemble average of  $10^5$  trajectories – smooth dynamics  
(best dissipative state estimate with no collected readout)

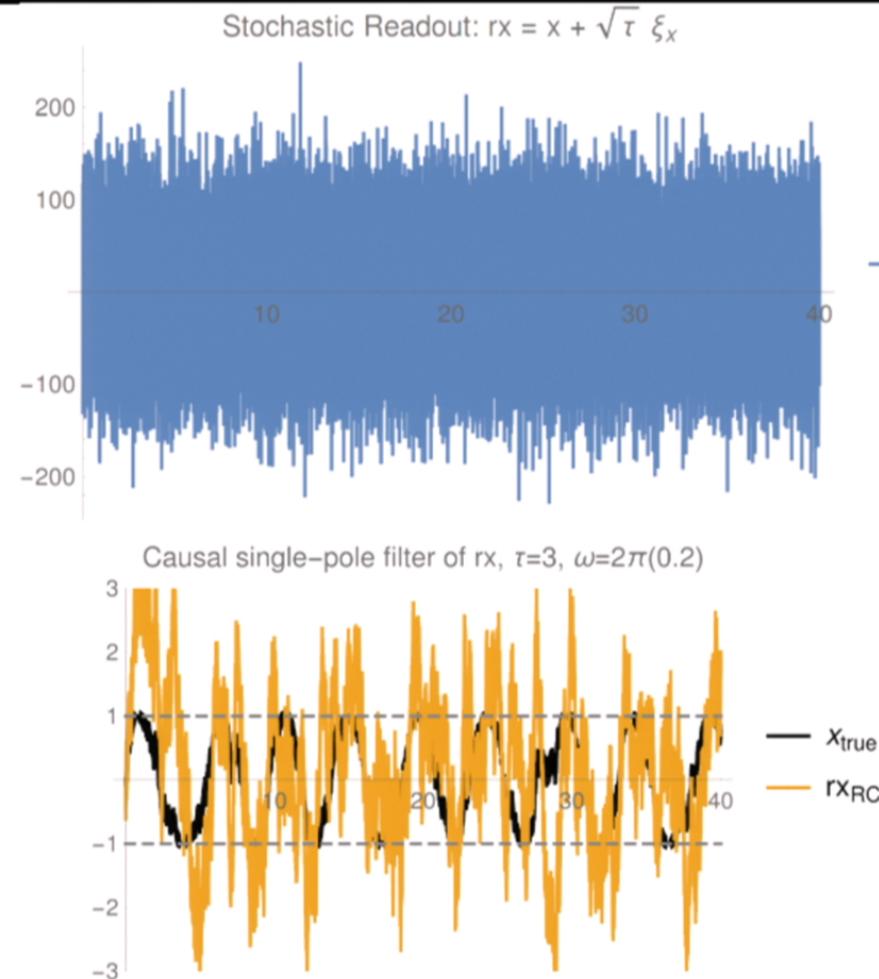
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# Filtering Raw Measurement Readout



## Raw Readout:

Moving-average stochastic process – hides monitored state component with white noise

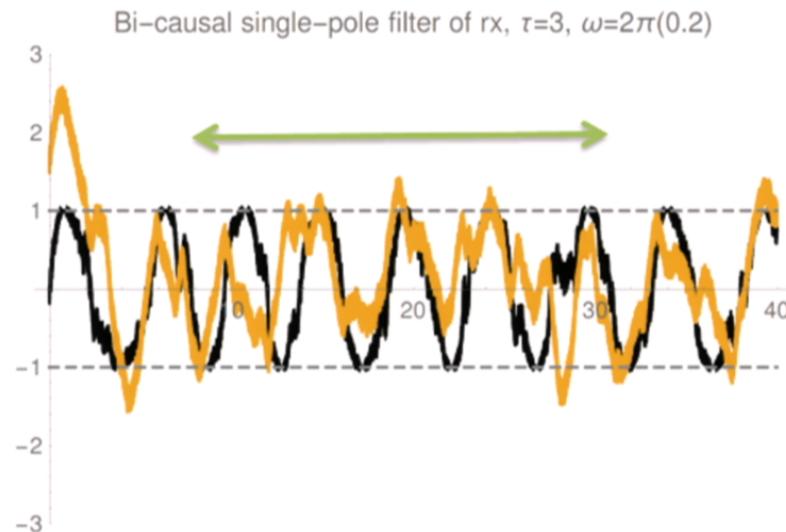
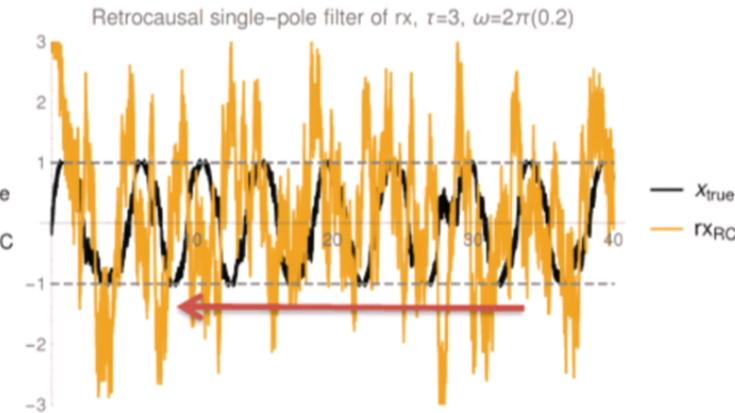
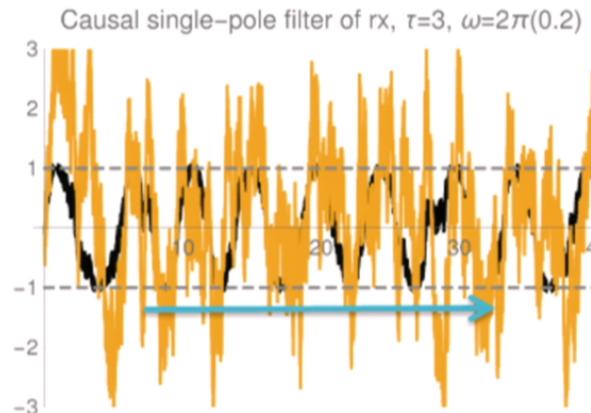
## Filtered Readout:

Smooths out noise to recover monitored state information – trade-off between size of temporal averaging window and detailed knowledge of state dynamics

## Quantum State Trajectory:

Using prior dynamical knowledge, noise can be optimally used to reconstruct the state

# Bidirectional Smoothing



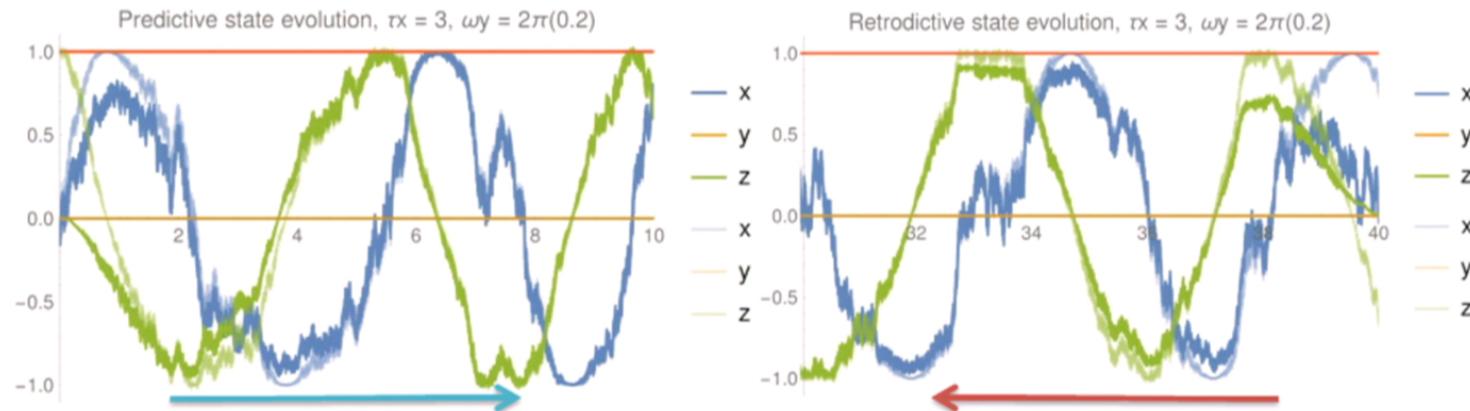
## Fixed-delay smoothing:

For a time-interval, both causal (forward in time) and retrocausal (backward in time) averaging is possible. Combining both uses the data in the most efficient way (interval smoothing)

## Model independent:

Only physical readout used to extract information without prior state knowledge

# Erasure of Boundary Conditions



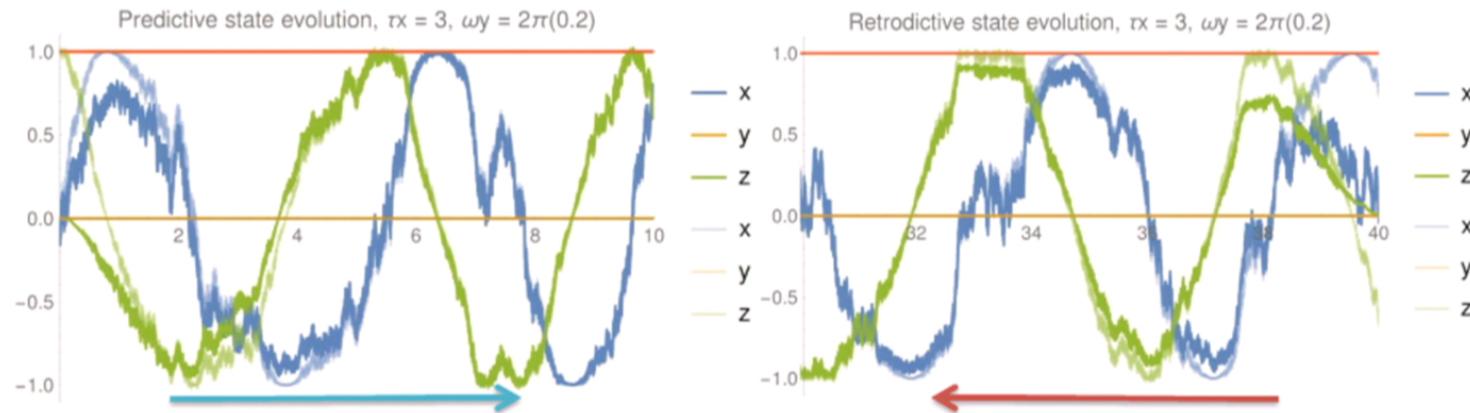
## Forward and backward evolution:

The readout completely determines both the forward-evolved (predictive) quantum state, and the backward-evolved (retrodictive) quantum state, which are not the same

## Readout determines evolution:

Boundary conditions only survive for a few collapse times – shown are two different prior and posterior boundary conditions converging to the same intermediary evolution

# Erasure of Boundary Conditions



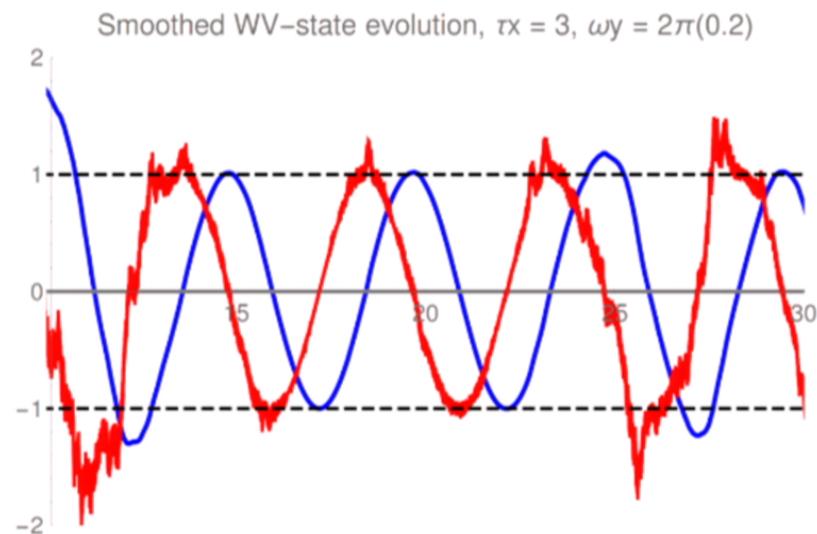
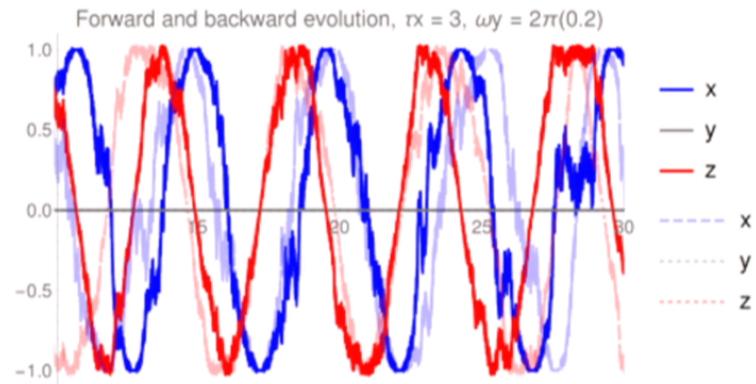
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# Weak Value as Best Estimate



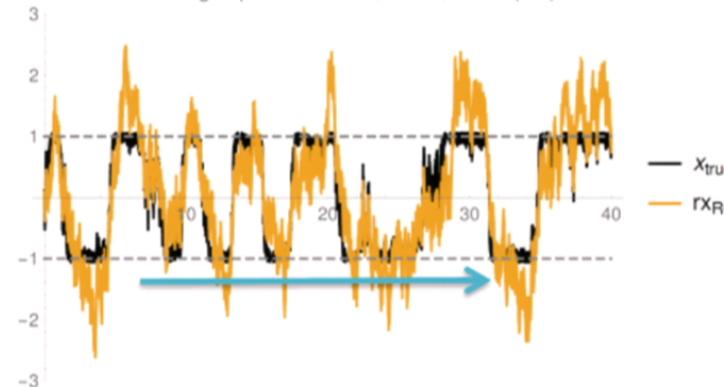
**Forward and backwards states disagree in between:**  
Which is the "correct" state?

**Weak Value minimizes error:**  
Given prior and posterior states, the real part of the weak value minimizes the RMS error for an observable, and is thus the best estimate of the observable value in between.

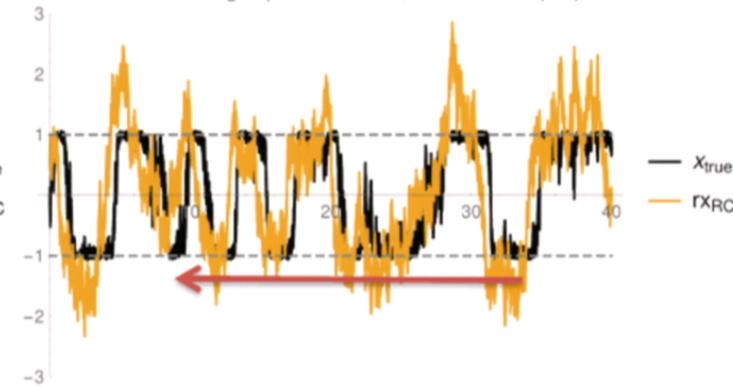
**WV-state fixed by readout:**  
Since both prior and posterior states are fixed, the WV estimates of the state components are also fixed.  
Magically, the monitored component becomes almost completely smooth with such an estimate (but may stray from eigenvalue bounds).

# Quantum Jump Dynamics

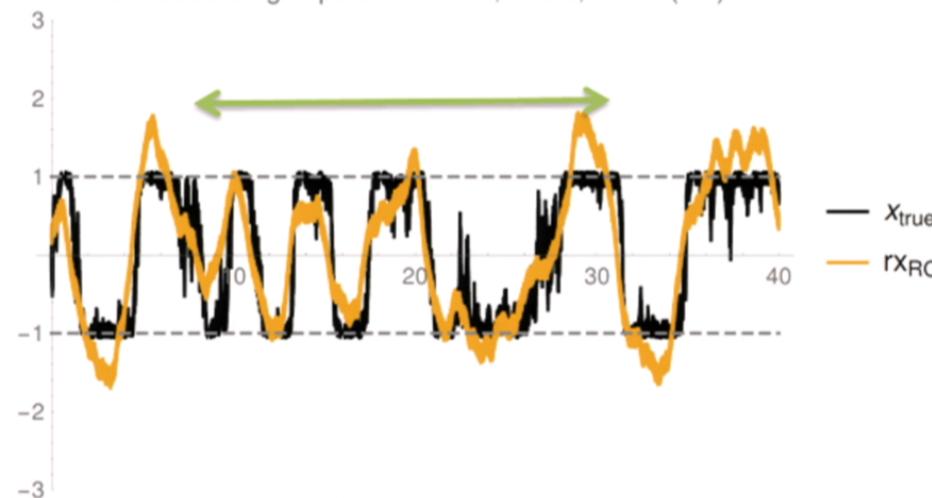
Causal single-pole filter of rx,  $\tau=0.3$ ,  $\omega=2\pi(0.2)$



Retrocausal single-pole filter of rx,  $\tau=0.3$ ,  $\omega=2\pi(0.2)$



Bi-causal single-pole filter of rx,  $\tau=0.3$ ,  $\omega=2\pi(0.2)$



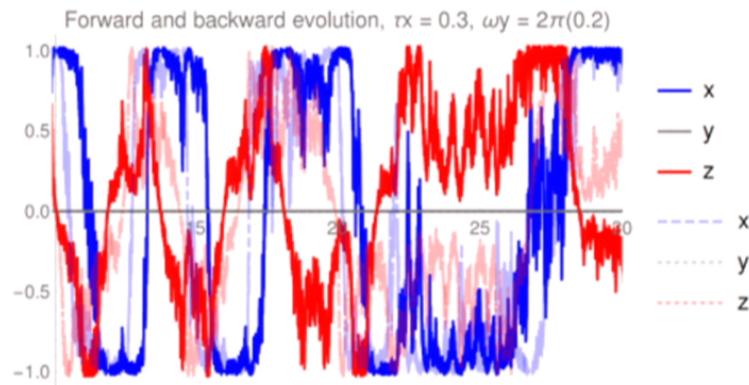
## Quantum Zeno effect:

Stronger measurements tend to pin the state to an eigenstate of the measurement, leading to stochastic jumps between eigenstates

## Filtering improves:

The stronger the measurements, the better the information contained in the record, so the better the filtering performs

# Weak-Valued Jumps



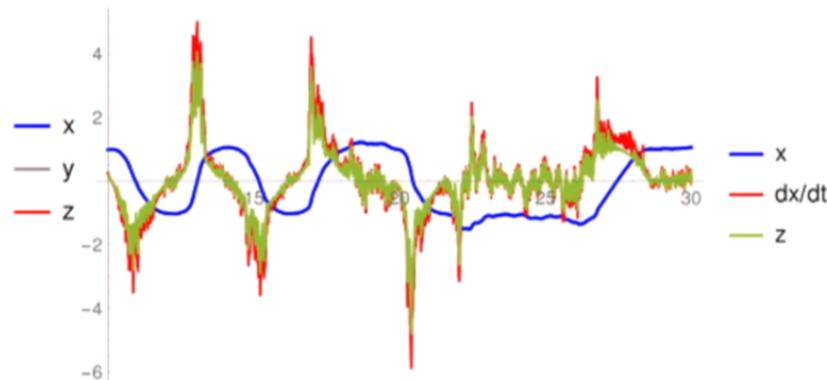
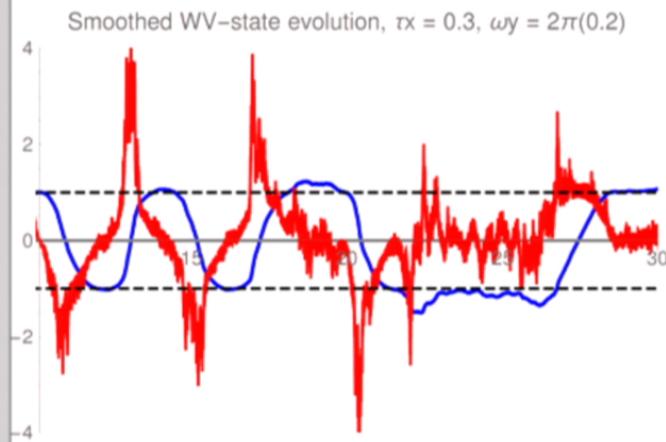
## WV state smooths jumps:

Remarkably, the WV state estimation can track jumps nearly noiselessly.

## Conjugate anomalous:

The monitored coordinate remains relatively well-behaved; however, the conjugate coordinate displays highly anomalous values well outside its usual eigenvalue range.

It has become a **time derivative** from Heisenberg picture dynamics



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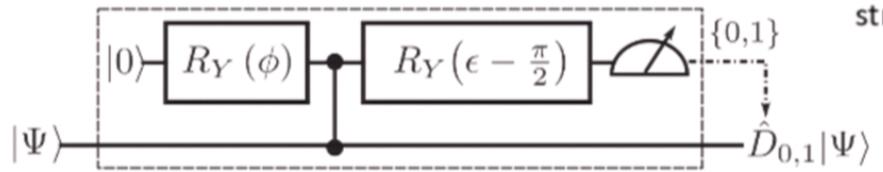
# Partial Projection Circuit

Any qubit measurement is a combination of unitary rotations and a **partial projection** with two possible outcomes:

$$D_0 = \sqrt{p} |0\rangle\langle 0| + \sqrt{1-p} |1\rangle\langle 1|,$$

$$D_1 = \sqrt{1-p} |0\rangle\langle 0| + \sqrt{q} |1\rangle\langle 1|,$$

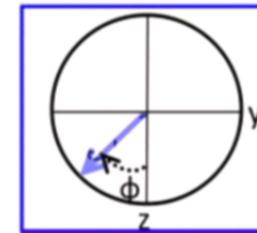
An ancilla qubit with a control-Z gate can be used to implement any desired partial projection in a tightly controlled way



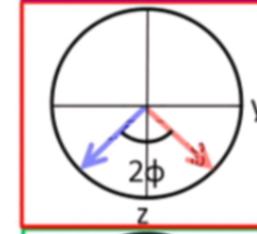
## Use ancilla qubit

Target  $|0\rangle$       Target  $|1\rangle$

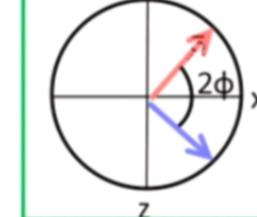
Step 1: Arbitrary rotation  $\phi$  on ancilla



Step 2: perform cZ rotation and equalize rotation around 0

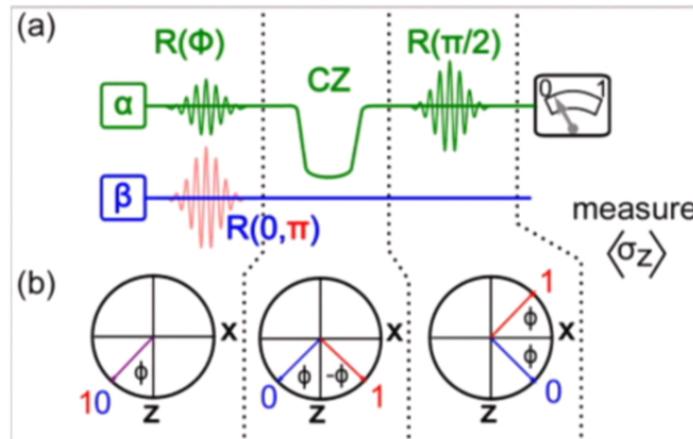
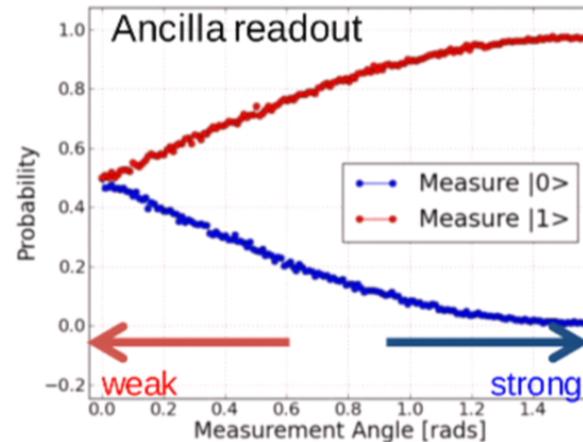
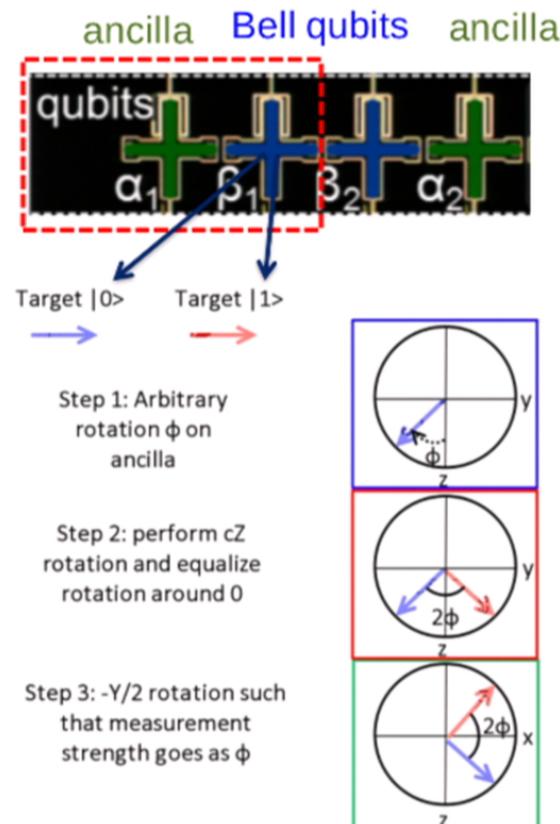


Step 3: -Y/2 rotation such that measurement strength goes as  $\phi$



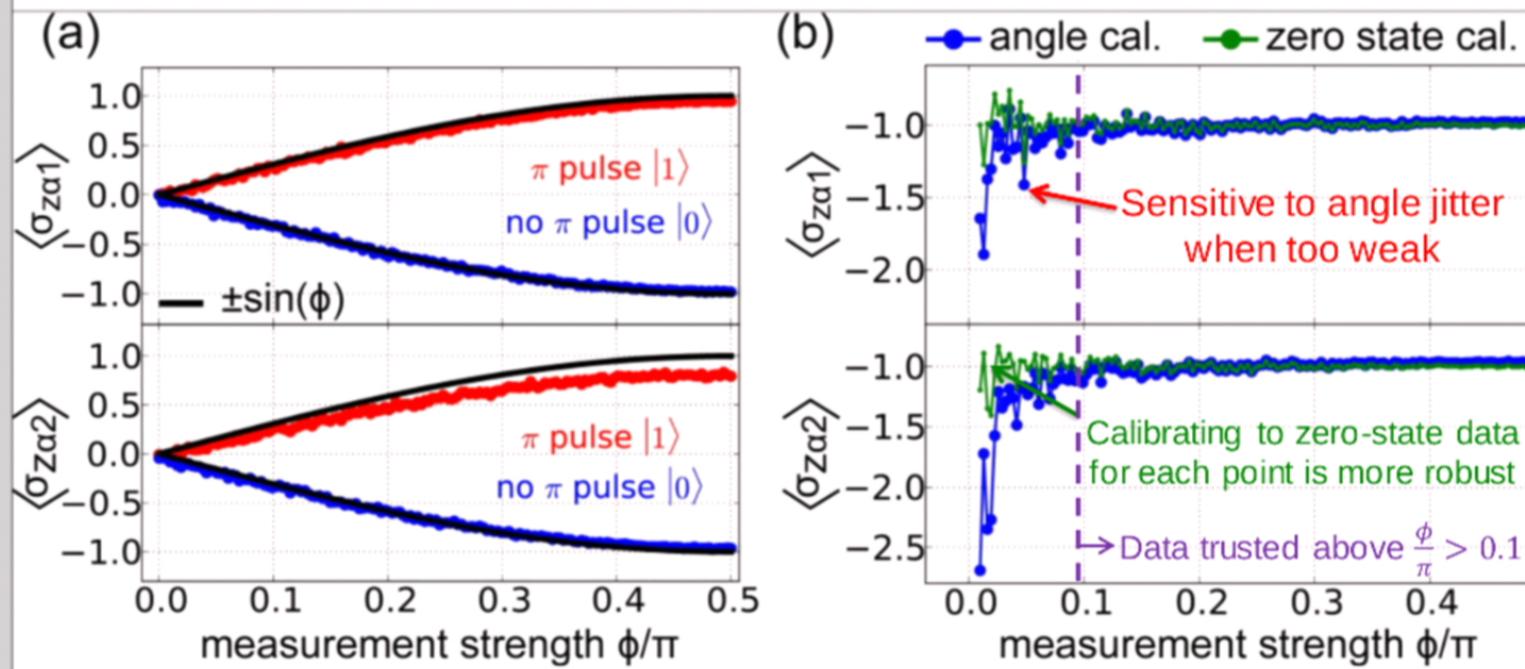
JD, PRA **90**, 032302 (2014)

# Microwave pulse implementation



# Calibrating the Z-measurement

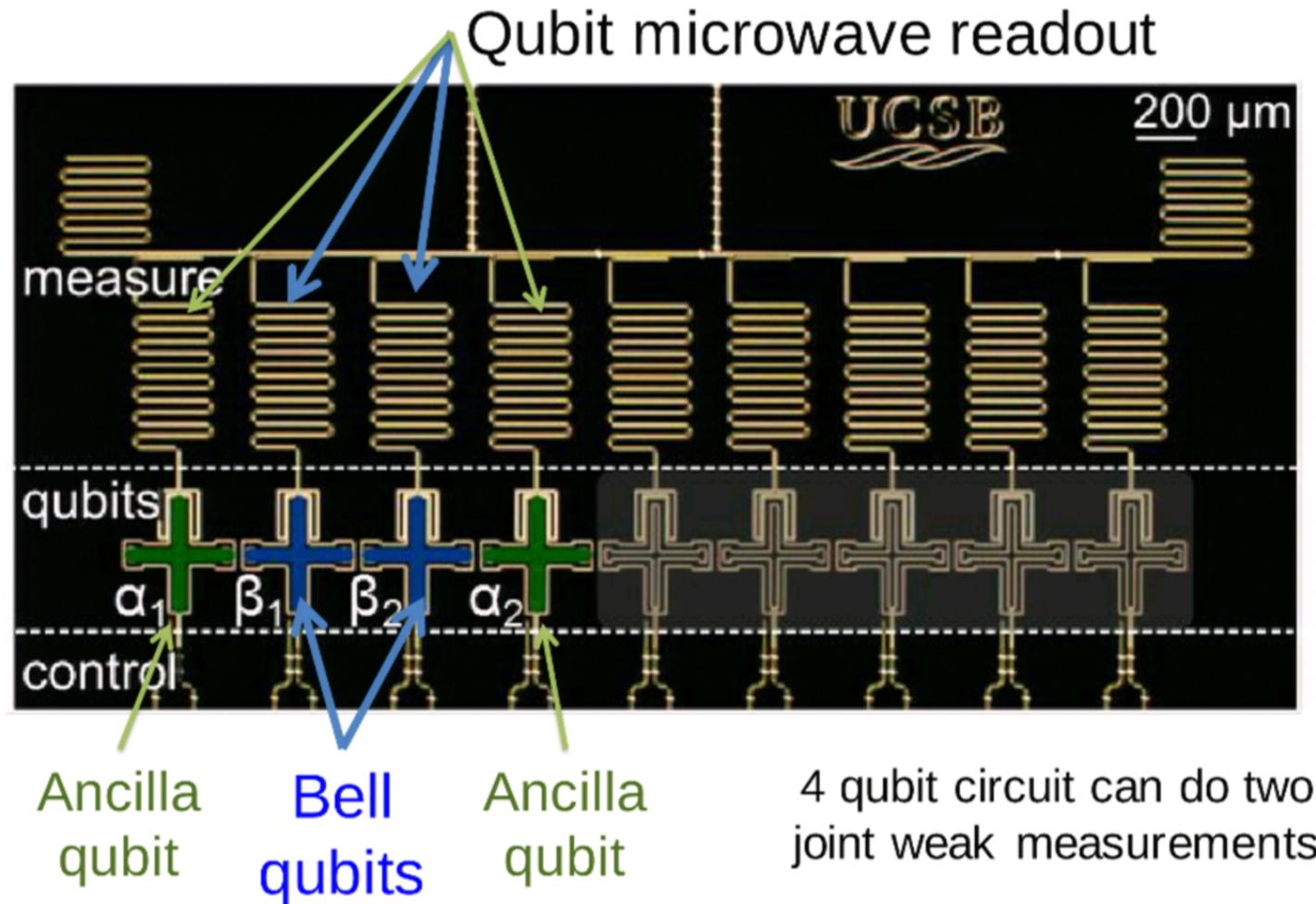
Rescale signal to known  $\pm 1$  Z-preparations



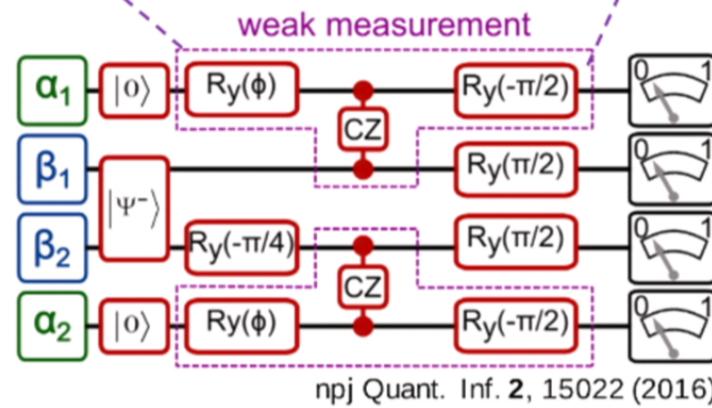
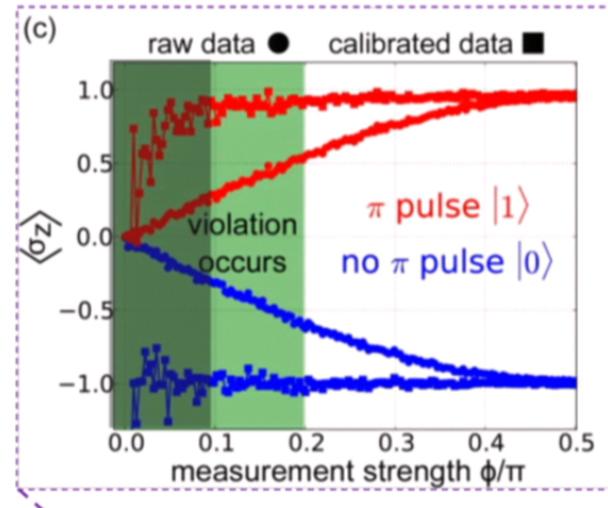
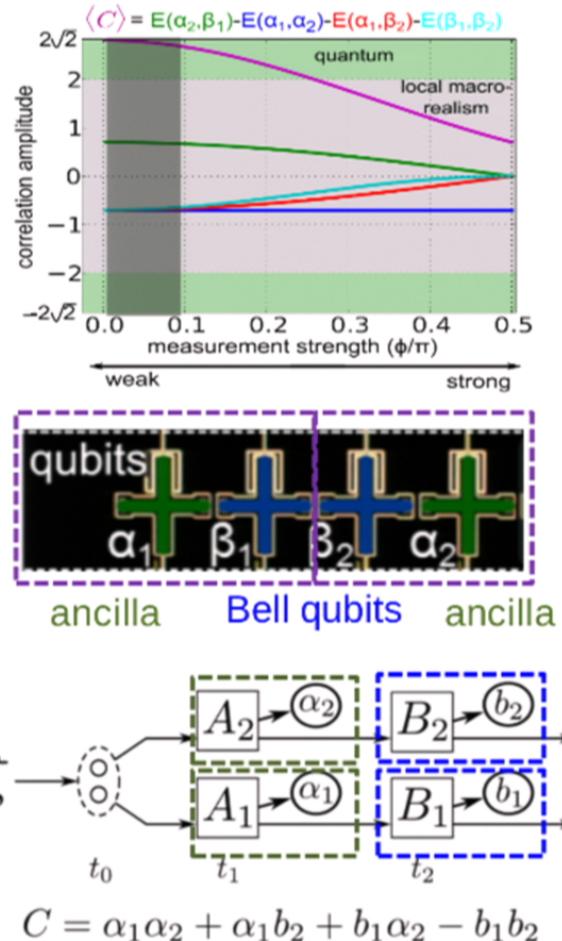
Two calibration methods: analytic ( $\frac{\pm 1}{\sin \phi}$ ), and point-by-point

# Superconducting 9 Xmon sample

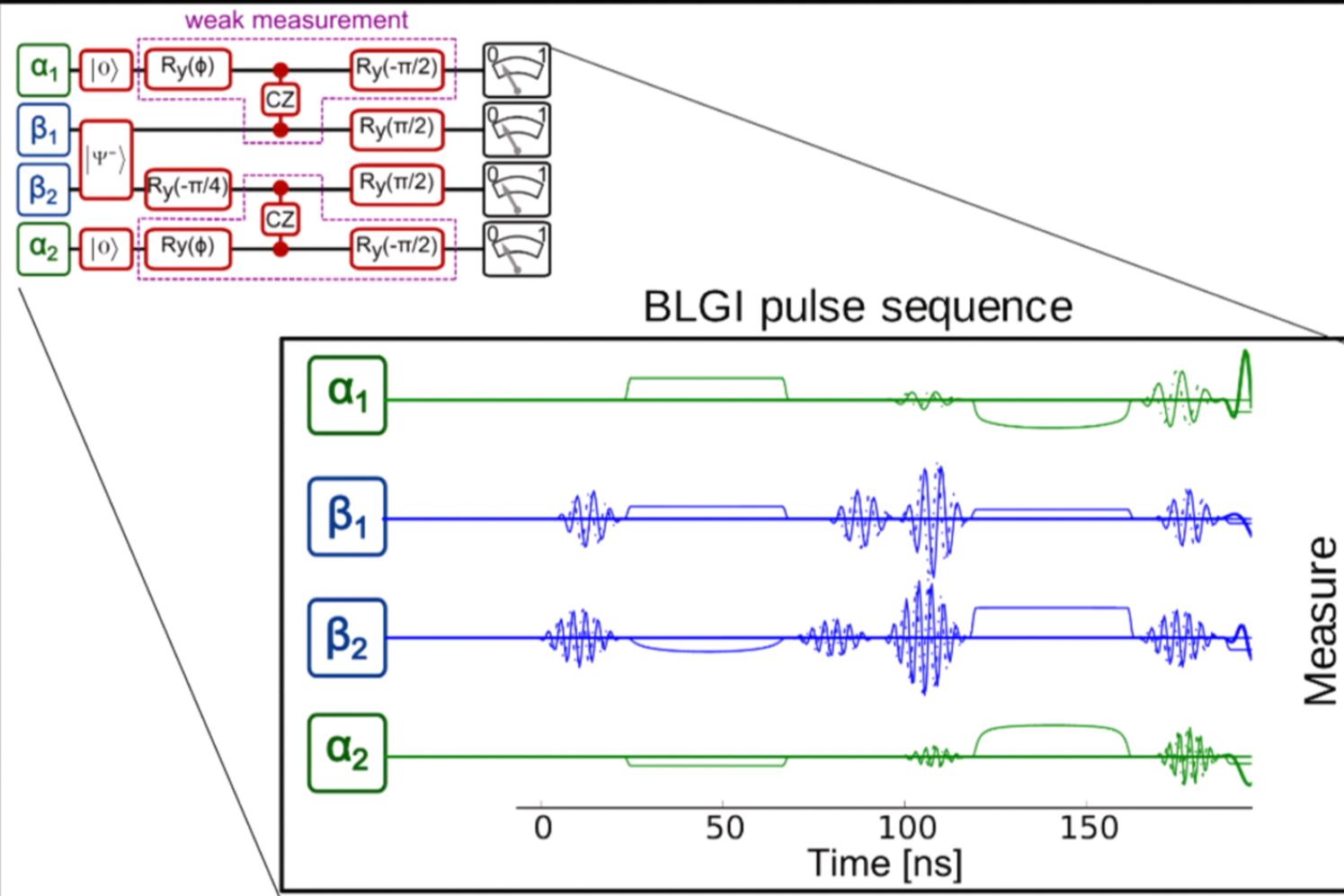
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# Bell-Leggett-Garg circuit

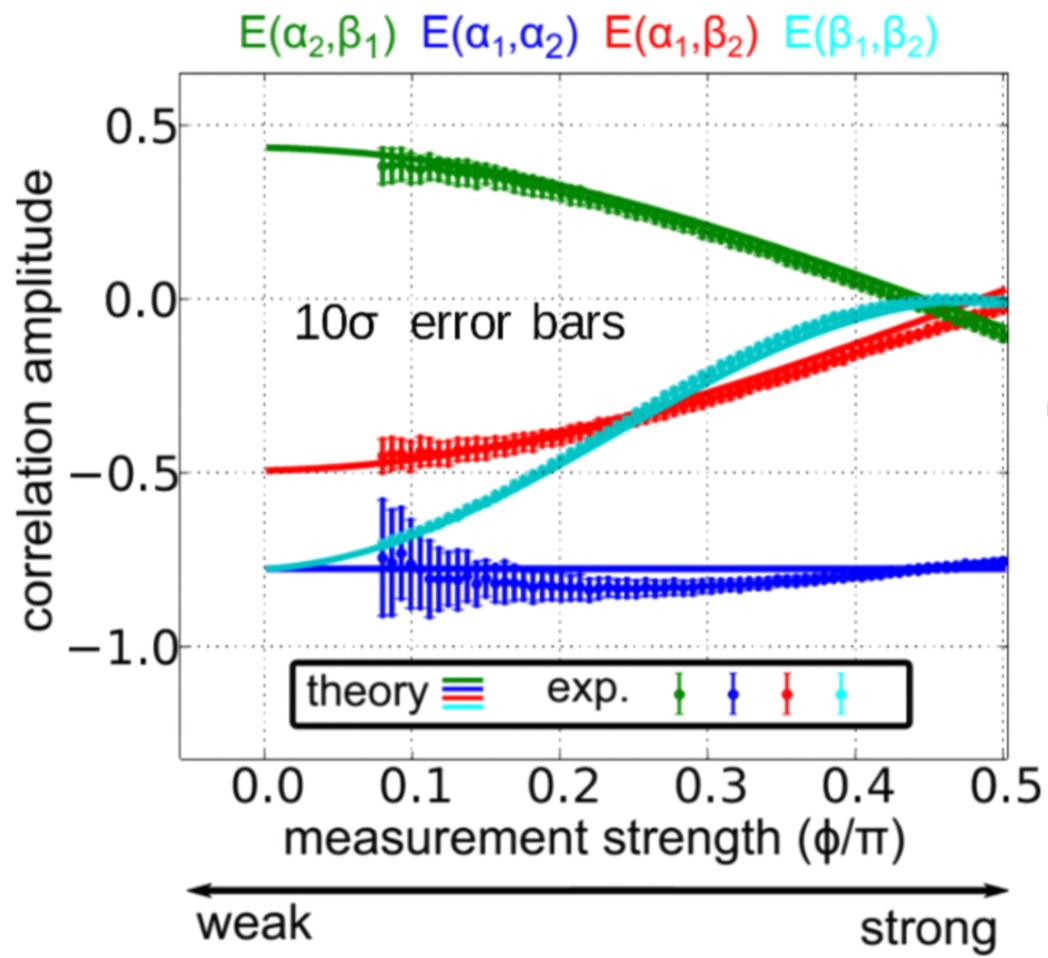


# BLGI microwave pulse sequence



# Individual BLGI terms

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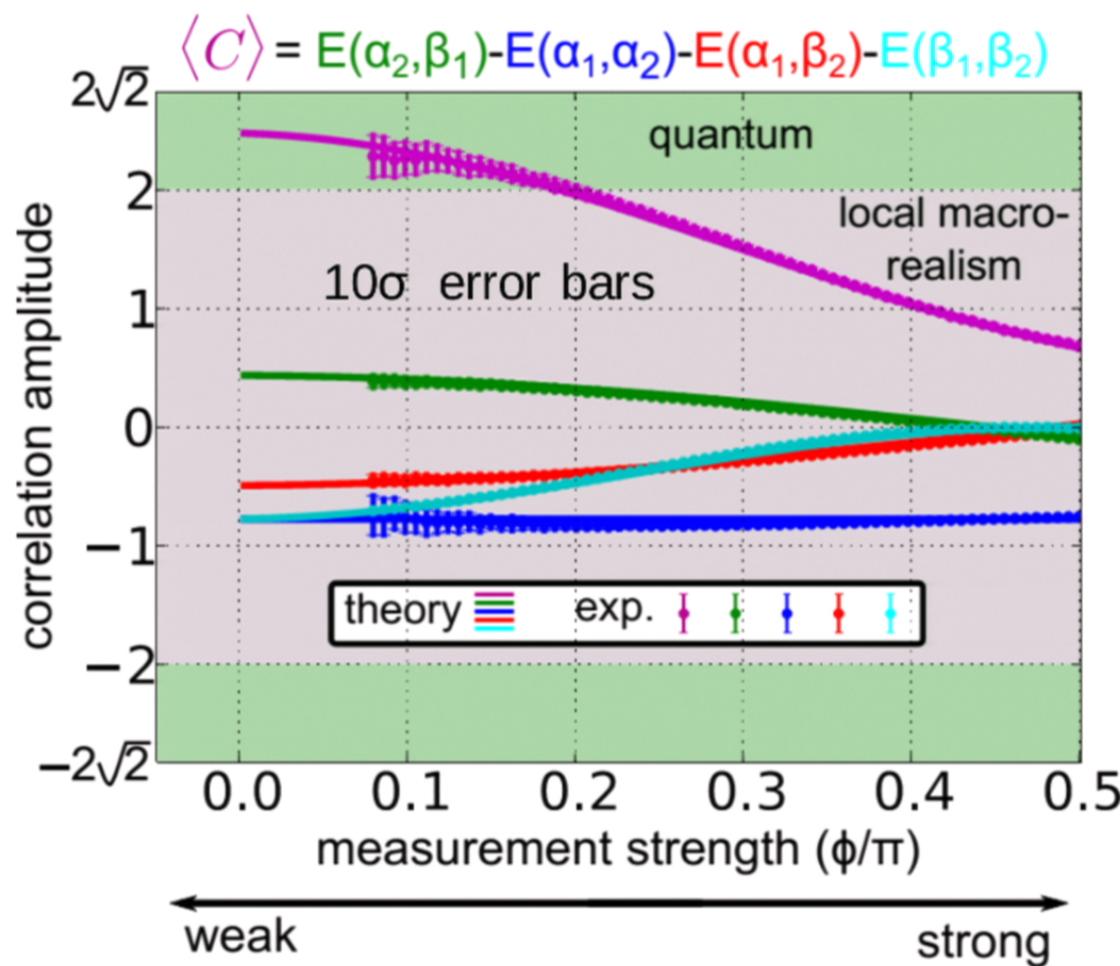


Theory curves include error models for systematics (rotation errors, decoherence, etc.)

Deviations in  $E(\alpha_1, \alpha_2)$  likely due to imperfect measurement calibration

# Full BLGI data - violation!

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Violation occurs just below  $0.2\pi$

Maximum violation occurs with  $> 27\sigma$  of certainty

# Conclusions

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- Superconducting processors work
- Both continuous weak measurements and discrete measurements of tunable strength are natural and useful
- Time-symmetric readout and state estimation has advantages

