

Title: Structure Formation in a ν CDM Universe

Date: Jun 17, 2016 10:50 AM

URL: <http://pirsa.org/16060024>

Abstract: Cosmic background neutrinos are nearly as abundant as cosmic microwave background photons, but their mass, which determines the strength of their gravitational clustering, is unknown. Neutrino oscillation data gives a strict lower limit on neutrino mass, while cosmological datasets provide the most stringent upper limit. Even if the neutrino masses are the minimum required by oscillation data, their gravitational effects on structure formation will nevertheless be detectable in $\sim 10^7$ and in fact required to explain $\sim 10^7$ data within the next decade. I will discuss the physical effects of the cosmic neutrino background on structure formation and present a new signature that may be used to measure neutrino mass with large galaxy surveys.

Structure Formation in ν CDM

Marilena LoVerde

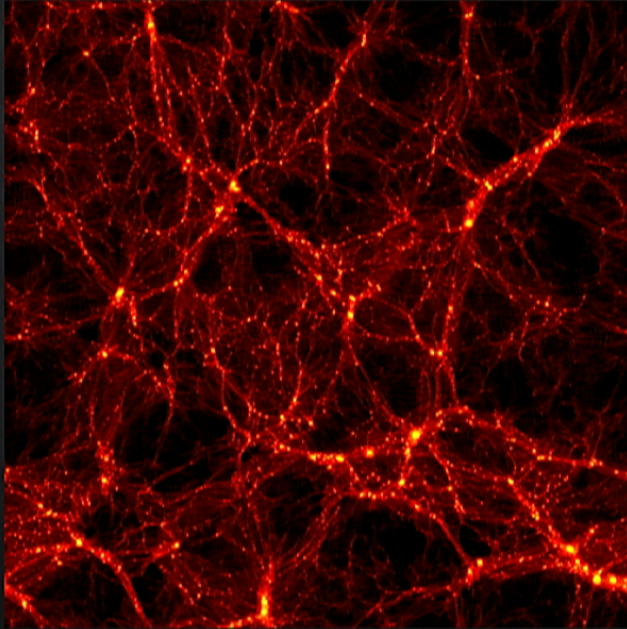
C. N. Yang Institute for Theoretical Physics, Stony Brook University

Outline

- Neutrino CDM Universe!
- Neutrino effects in large-scale structure:
The linear regime
- *NEW* neutrino effects in large-scale
structure
- Conclusion

Large-scale Structure

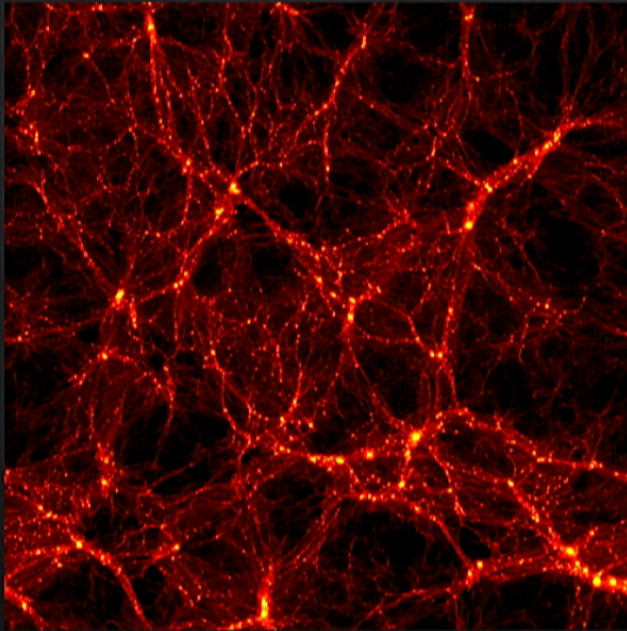
cold dark matter



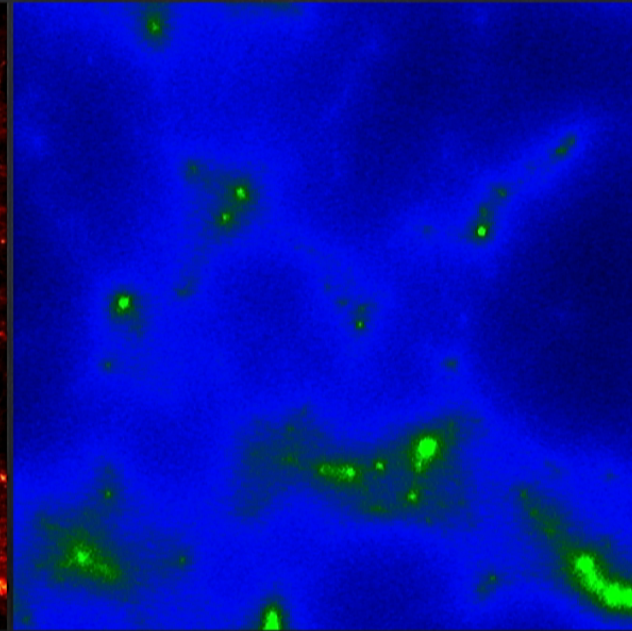
(Villaescusa-Navarro, Bird, Pena-Garay, Viel 2013)

Large-scale Structure

cold dark matter



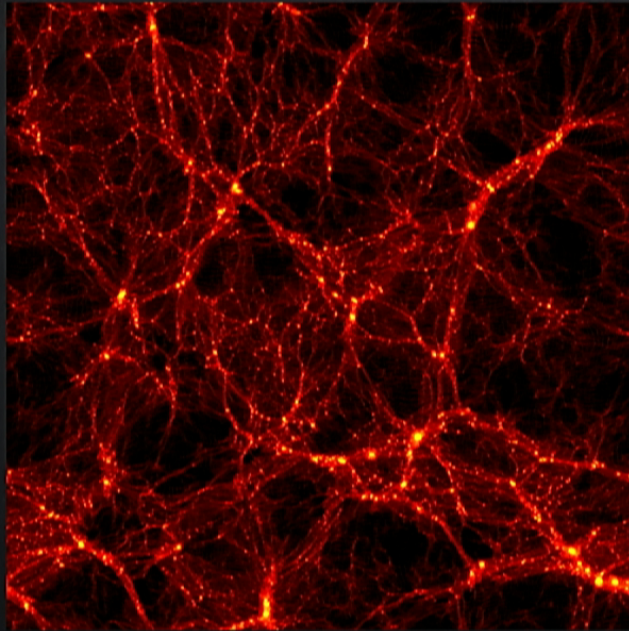
neutrino dark matter



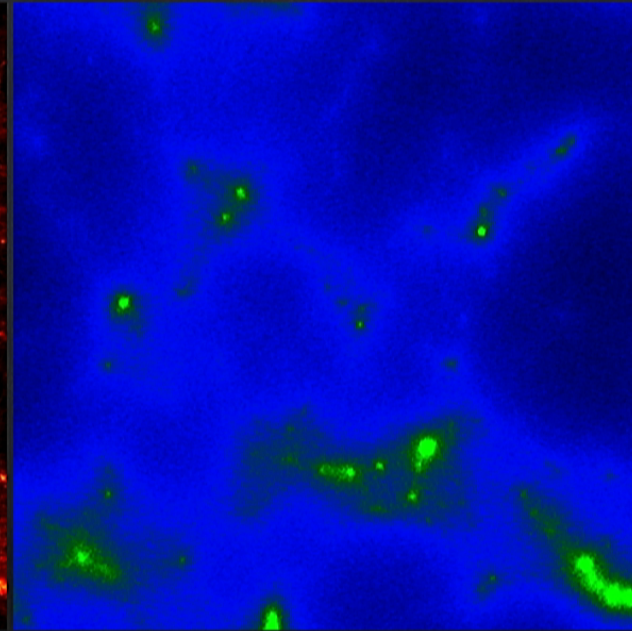
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Large-scale Structure

cold dark matter



neutrino dark matter



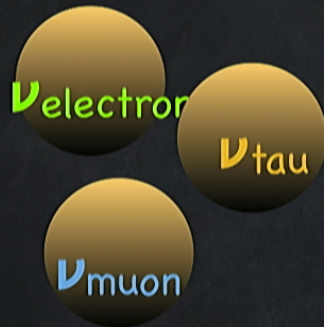
$$\rho_{\text{cdm}} + \frac{\rho_{\nu}}{\rho_{\text{baryon}} + \rho_{\nu}} \gtrsim 0.005$$

$$n_{\nu} \sim 10^{10} n_{\text{baryon}}$$

(Villaescusa-Navarro, Bird, Pena-Garay, Viel 2013)

Neutrinos: what do we know?

flavor eigenstates



mass eigenstates



Pontecorvo 1957, 1958, 1967; Maki, Nakagawa, Sakata 1962

Neutrinos: what do we know?

flavor eigenstates



mass eigenstates



flavor eigenstates \neq mass eigenstates

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

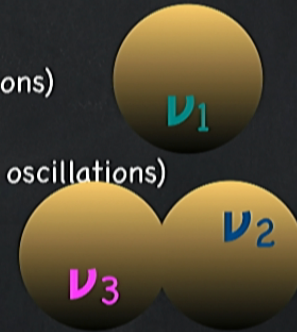
Pontecorvo 1957, 1958, 1967; Maki, Nakagawa, Sakata 1962

Neutrinos: what do we know?

Oscillation data gives mass splittings

$$m_2^2 - m_1^2 = (7.5 \pm 0.2) 10^{-5} \text{ eV}^2 \quad (\text{solar neutrino oscillations})$$

$$|m_3^2 - m_2^2| = (2.32_{-0.08}^{+0.12}) 10^{-3} \text{ eV}^2 \quad (\text{atmospheric neutrino oscillations})$$



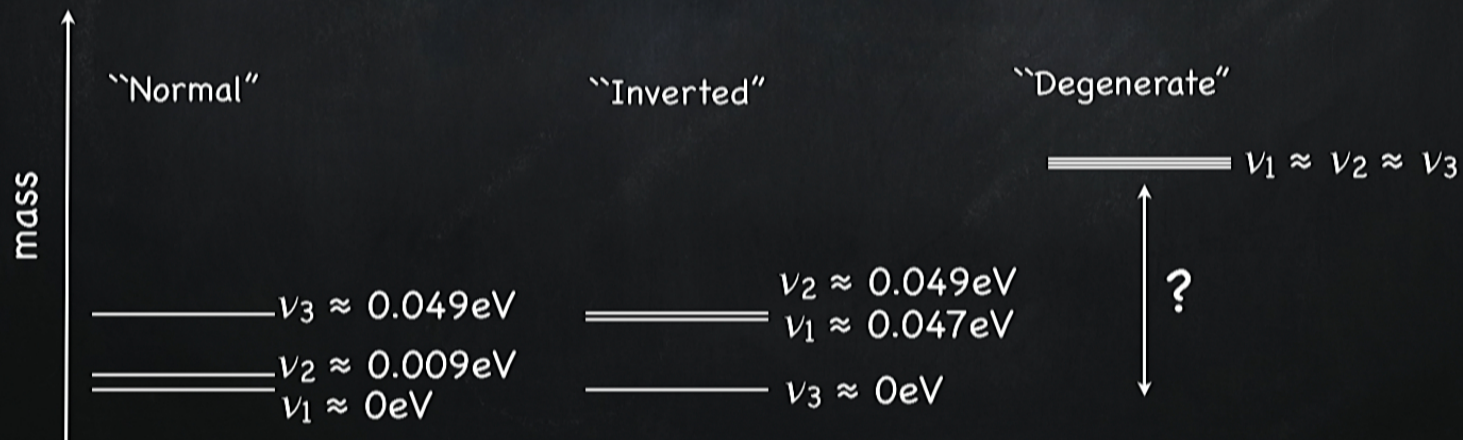
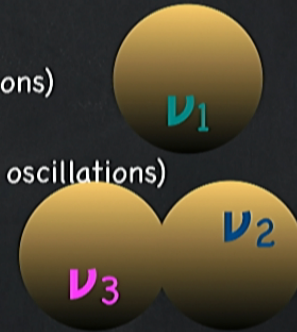
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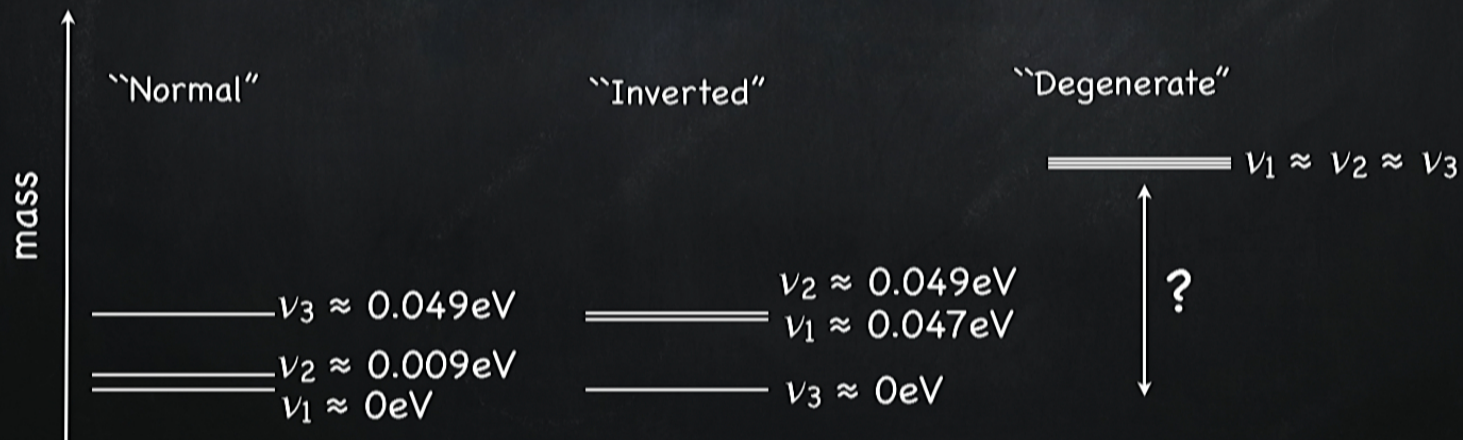
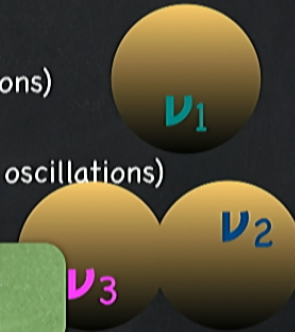
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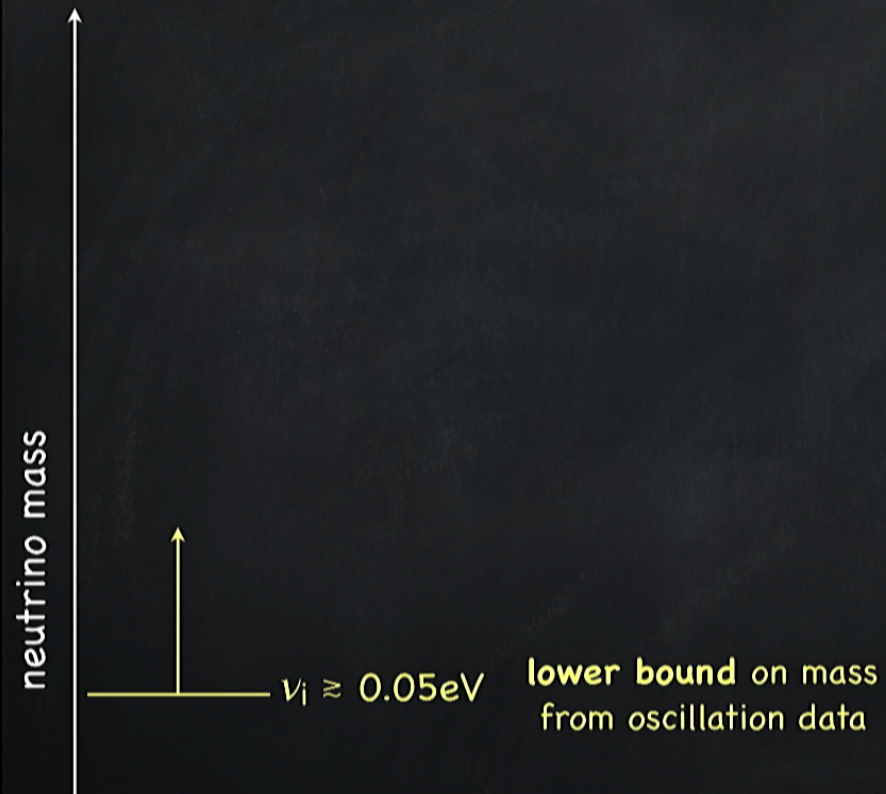
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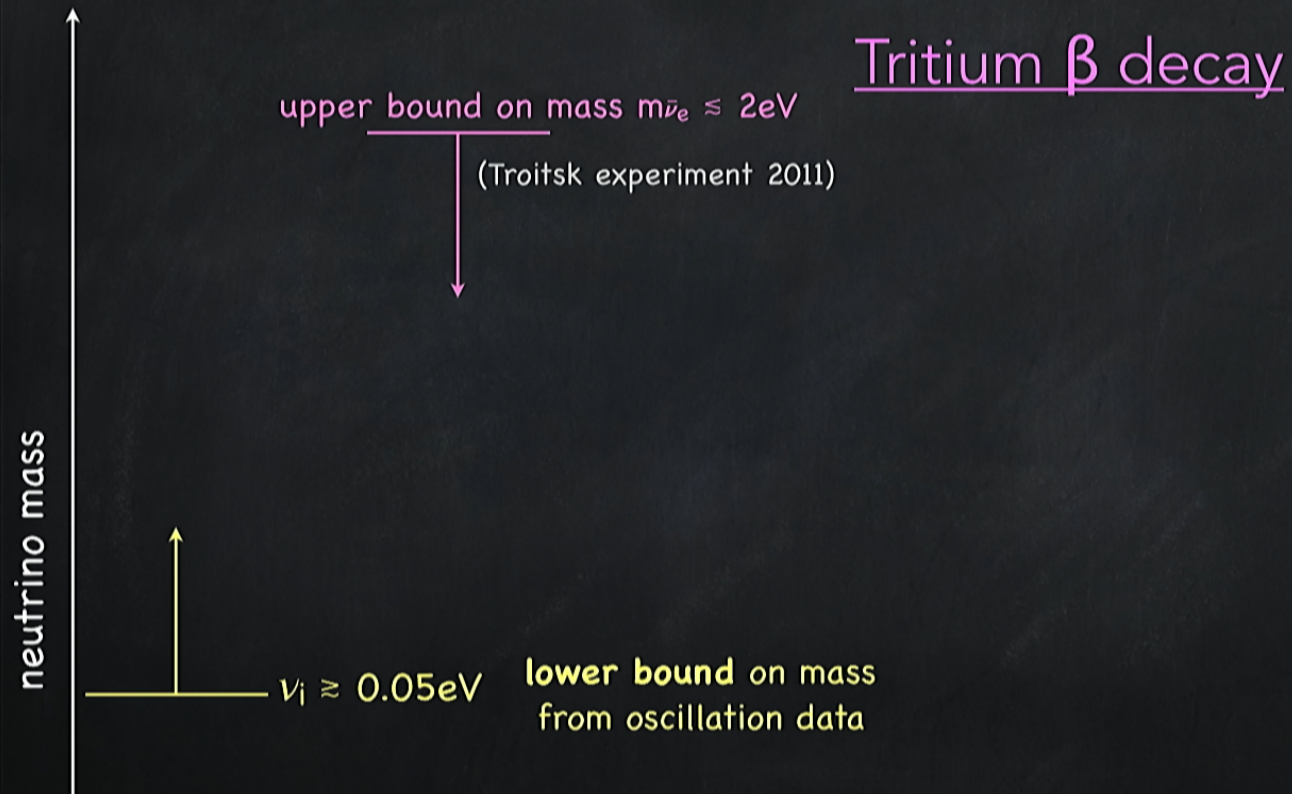
at least one neutrino mass is $\approx 0.05\text{eV}$



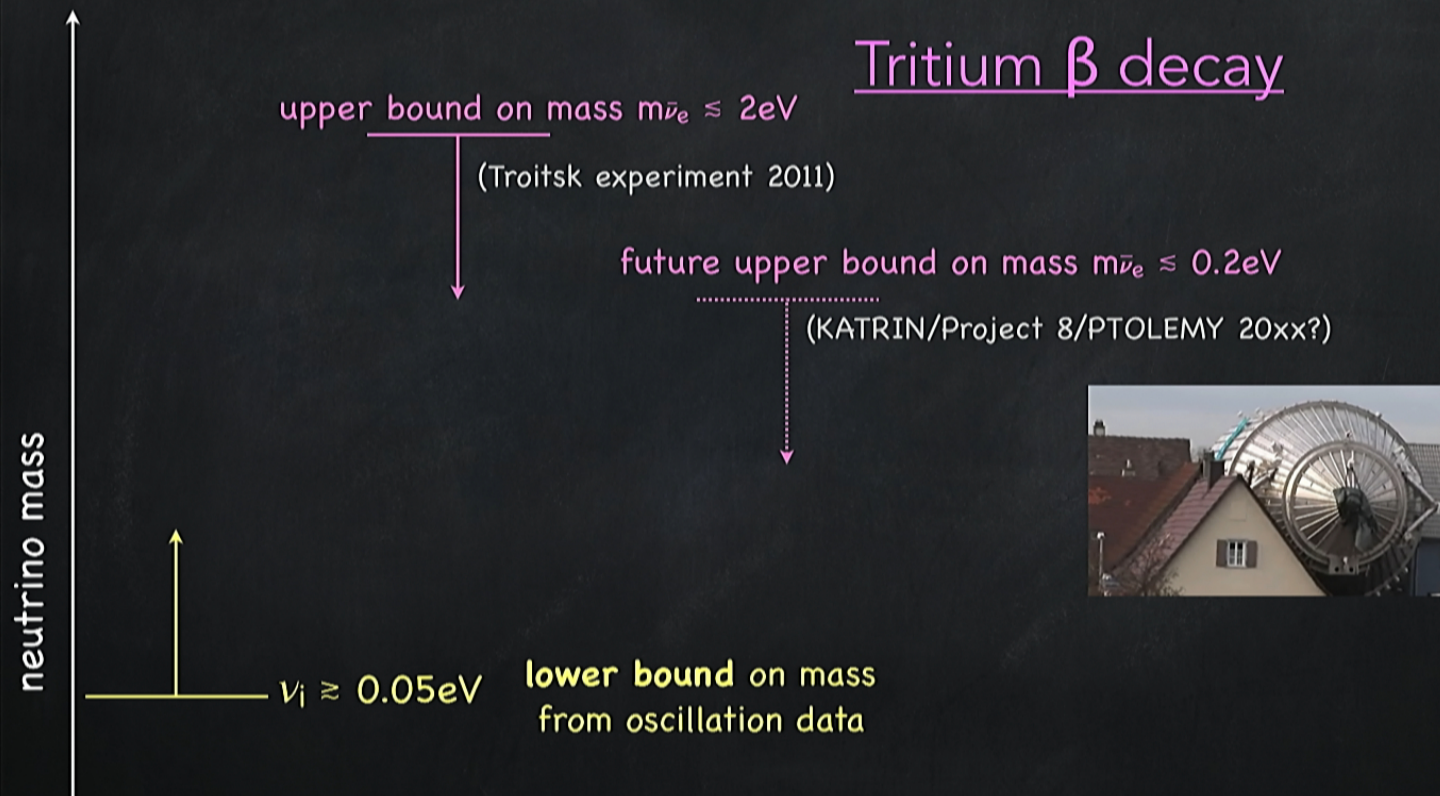
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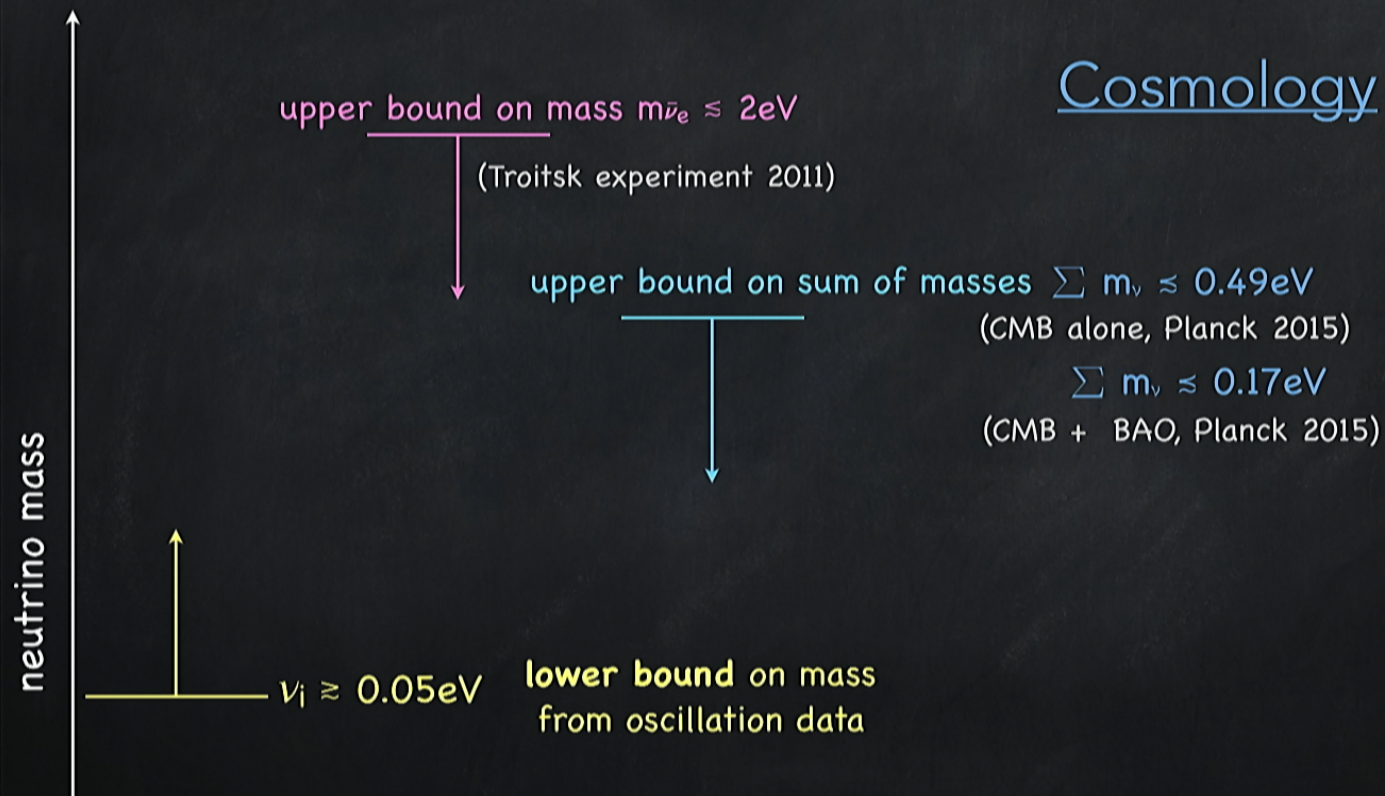
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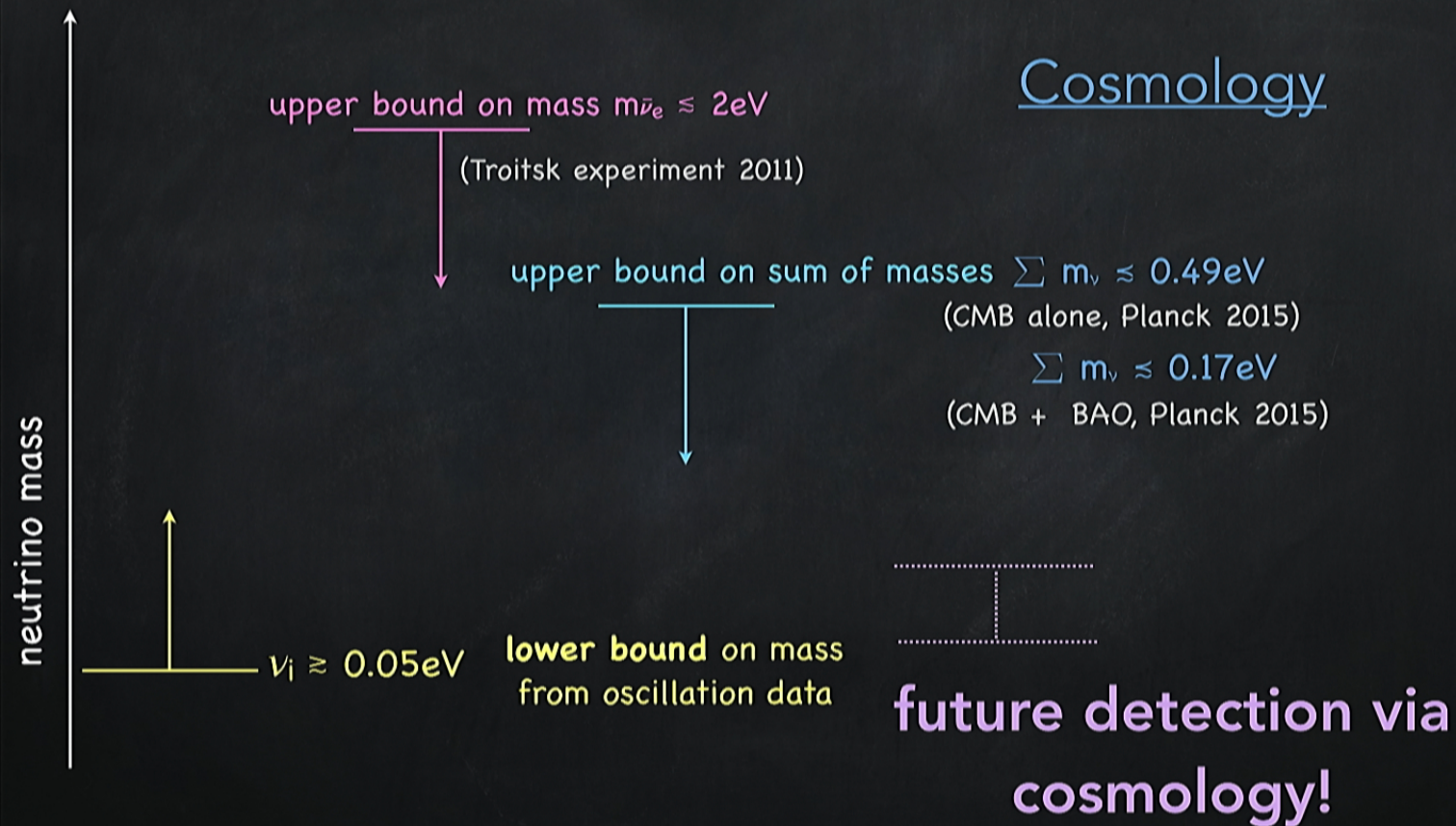
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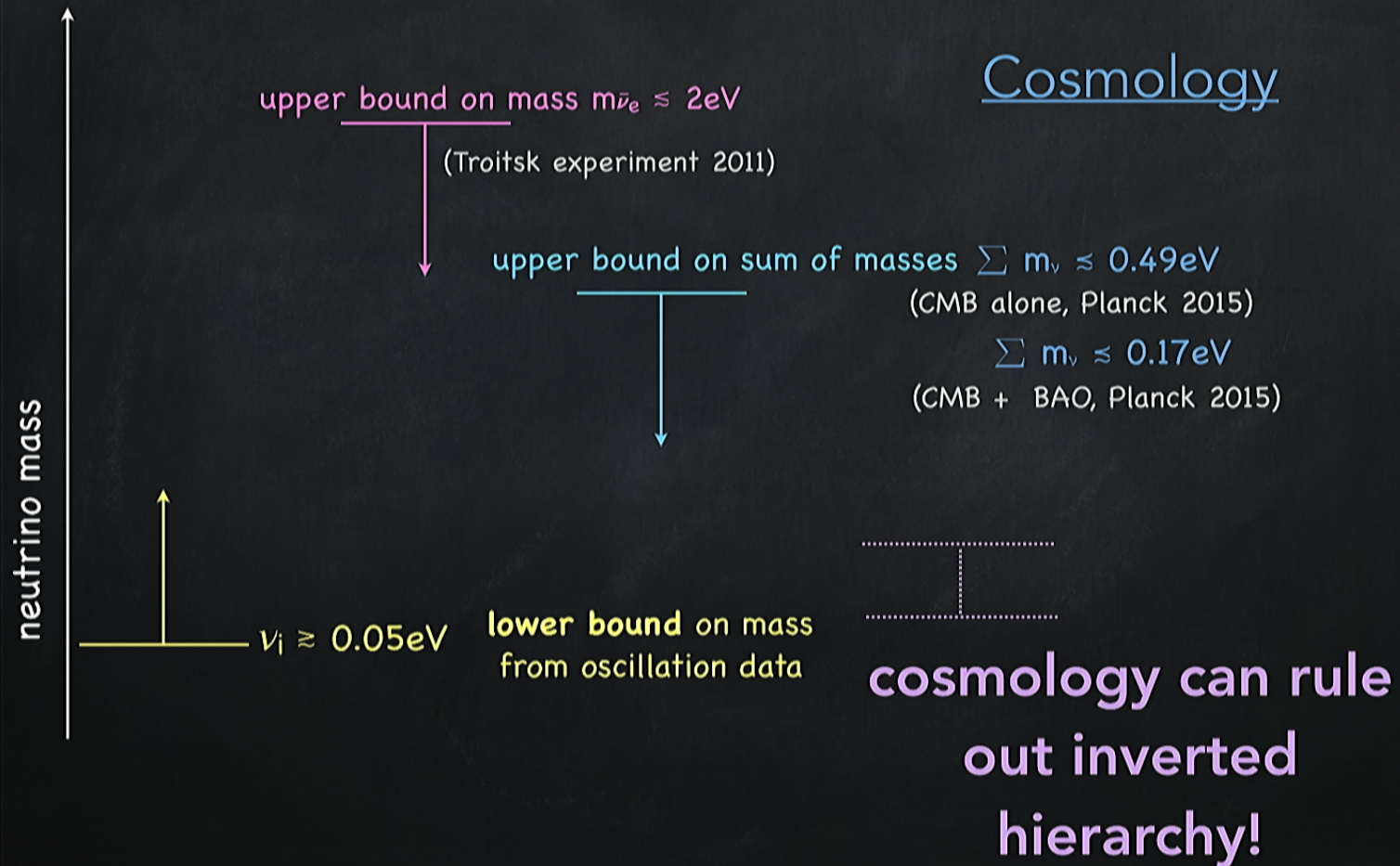
Neutrinos: what do we know?



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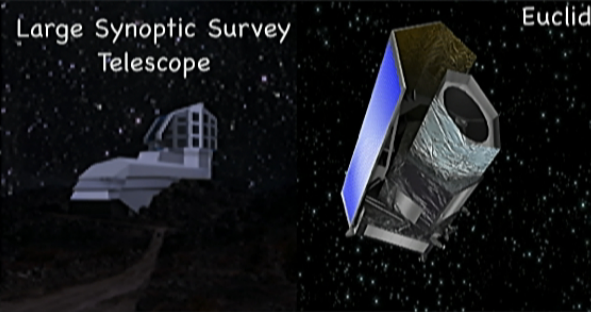
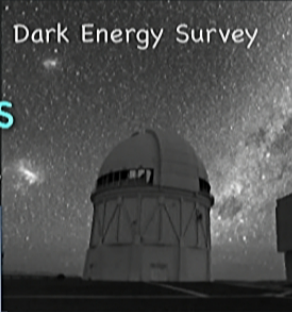
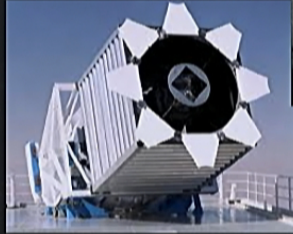
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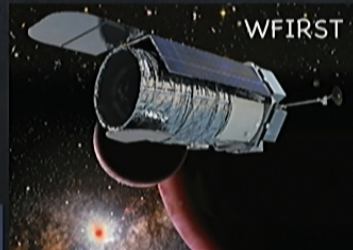
Future detection via astrophysical datasets

Large-scale structure surveys

Sloan Digital Sky Survey



Subaru Hyper Suprime Cam and Prime Focus Spectrograph



Hobby-Eberly Telescope Dark Energy EXperiment



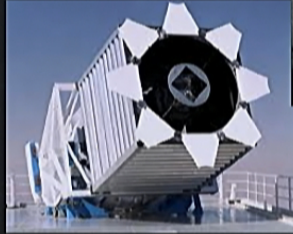
21 CM experiments

SPHEREX

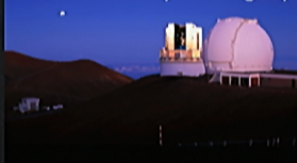
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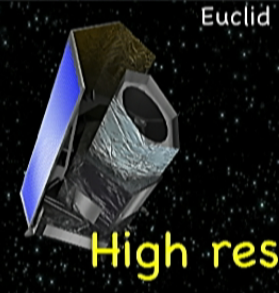
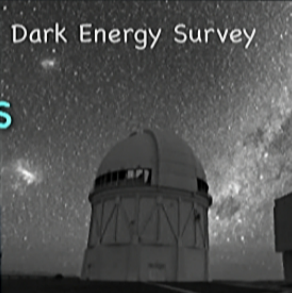
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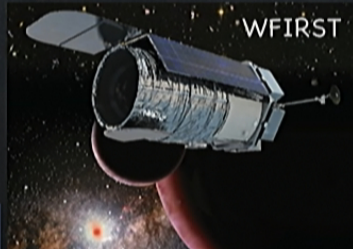
Subaru Hyper Suprime Cam and Prime Focus Spectrograph



Hobby-Eberly Telescope Dark Energy Experiment



High resolution cosmic microwave background experiments



SPHEREX



Planck



CMB "Stage IV"

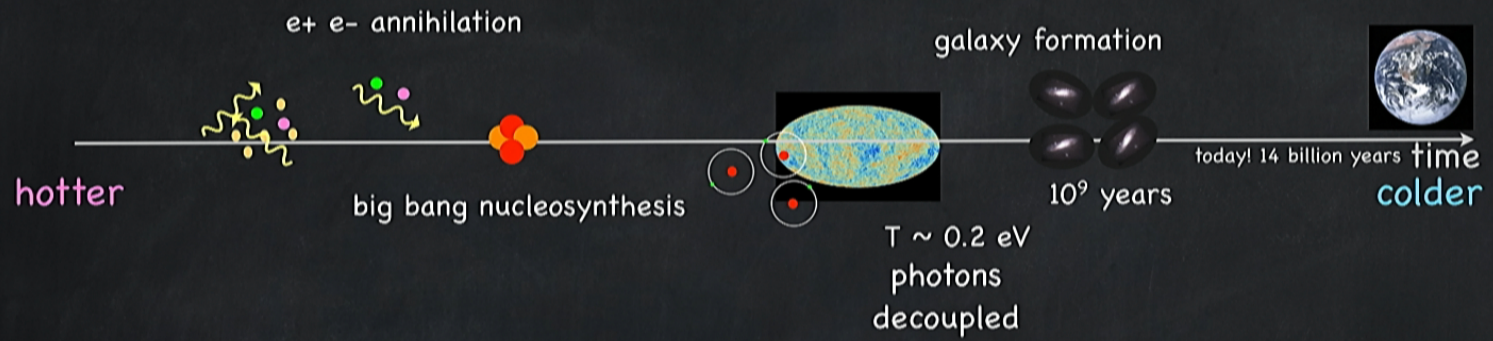
21 CM experiments

$$\sigma_{\Sigma m_\nu} \sim 0.02 eV$$

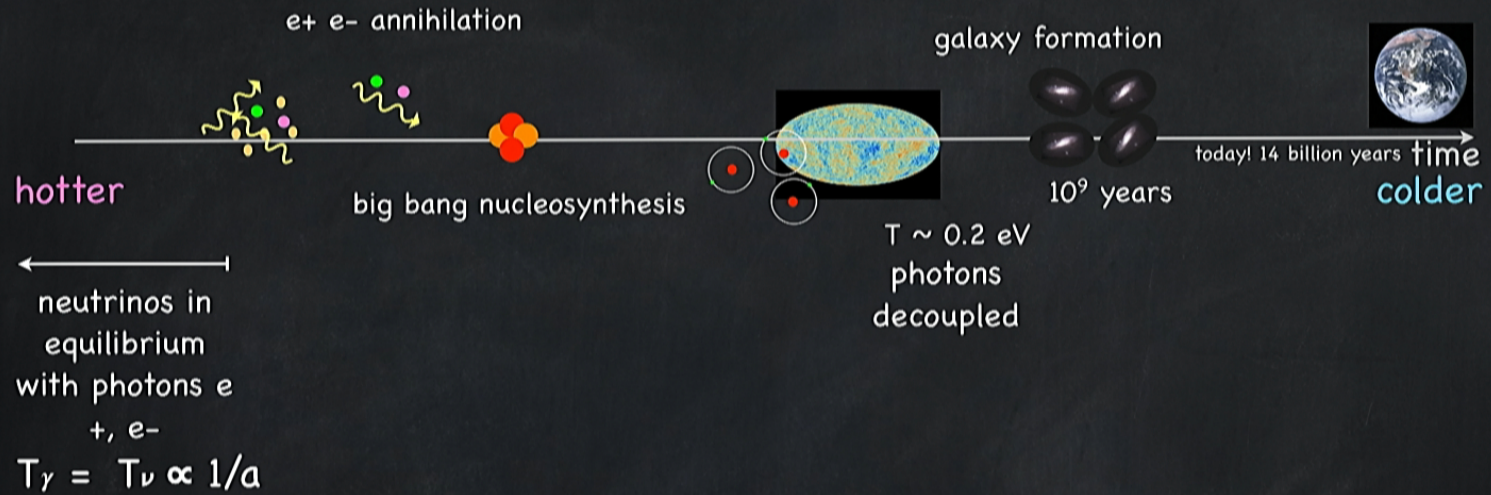
e.g. Snowmass 2013 1309.5383

Neutrinos in Cosmology

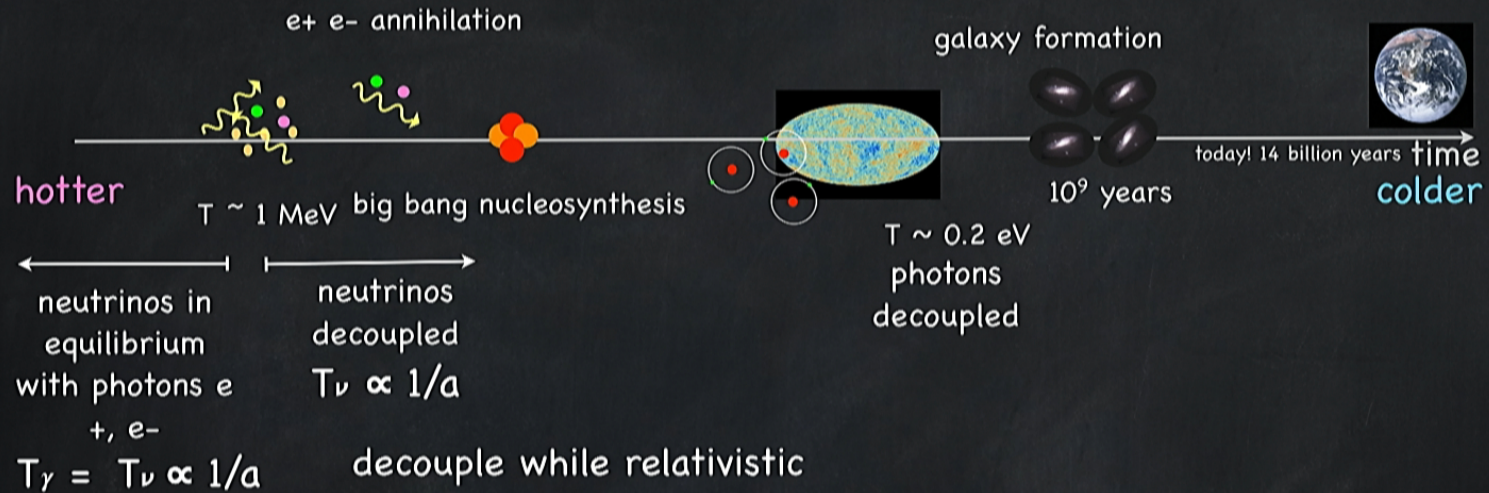
Neutrinos in Thermal History of the Universe



Neutrinos in Thermal History of the Universe



Neutrinos in Thermal History of the Universe



$$n_{1\nu} = 2 \int \frac{d^3p}{(2\pi)^3} \frac{1}{e^{p/T_\nu} + 1} \sim T_\nu^3$$

$$\rho_{1\nu} = 2 \int \frac{d^3p}{(2\pi)^3} \frac{\sqrt{p^2 + m^2}}{e^{p/T_\nu} + 1} \sim T_\nu^4$$

Neutrinos in Thermal History of the Universe

Total energy density in radiation:

$$\rho_{\text{radiation}} = \frac{\pi^2}{30} (2T_\gamma^4 + \frac{7}{8} N_{\text{eff}} \times 2 T_\nu^4)$$

cosmic microwave background

cosmic neutrino background

Neutrinos in Thermal History of the Universe

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cosmic microwave background

cosmic neutrino background

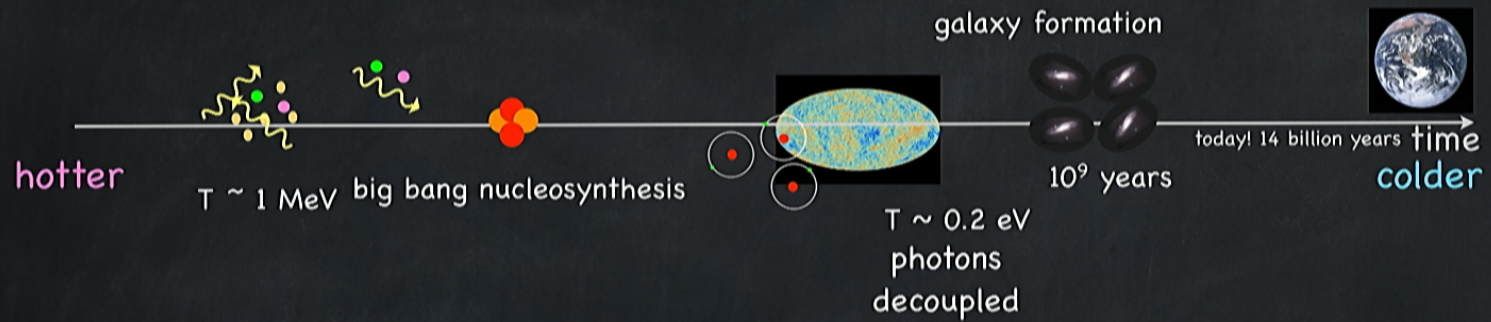
measurements of the radiation density in the early universe can be used to test the number of neutrino-like degrees of freedom

| | |
|----------------------------------|------------------------------------|
| $N_{\text{eff}} = 3.13 \pm 0.32$ | <i>Planck TT+lowP;</i> |
| $N_{\text{eff}} = 3.15 \pm 0.23$ | <i>Planck TT+lowP+BAO;</i> |
| $N_{\text{eff}} = 2.99 \pm 0.20$ | <i>Planck TT, TE, EE+lowP;</i> |
| $N_{\text{eff}} = 3.04 \pm 0.18$ | <i>Planck TT, TE, EE+lowP+BAO.</i> |

The expected number of neutrino species is seen in the CMB!

Planck 2015

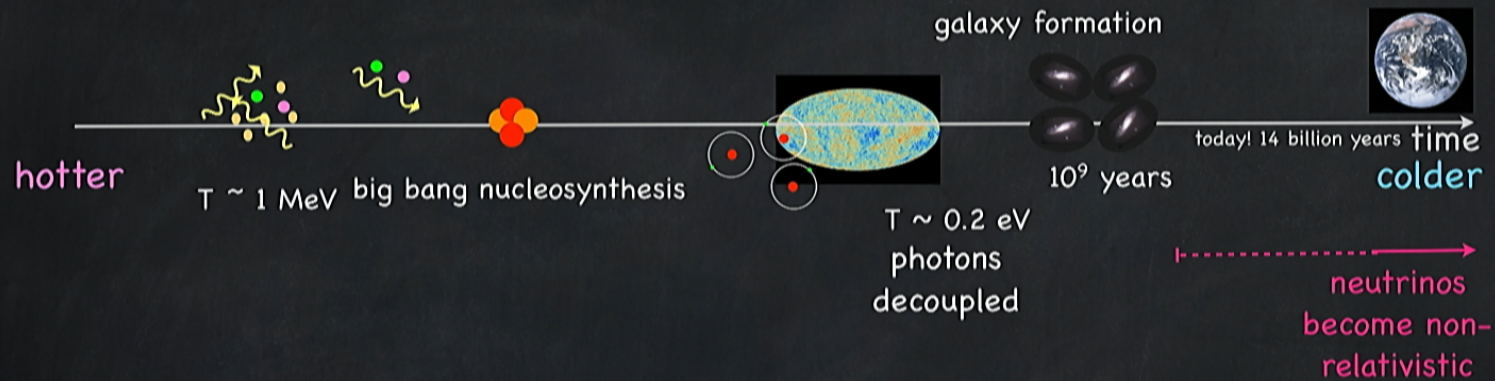
Neutrinos in Thermal History of the Universe



Neutrino momenta decrease with the expansion of the universe

$$p_\nu \propto 1/a$$

Neutrinos in Thermal History of the Universe

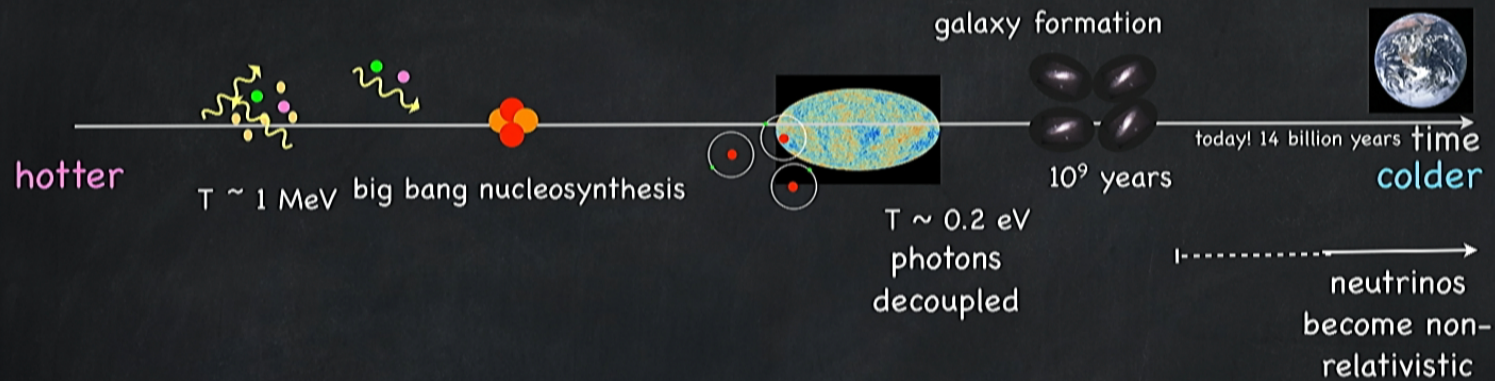


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When $p_\nu \ll m_\nu$, neutrinos are non-relativistic
and energy density is dominated by mass

Neutrinos in Thermal History of the Universe



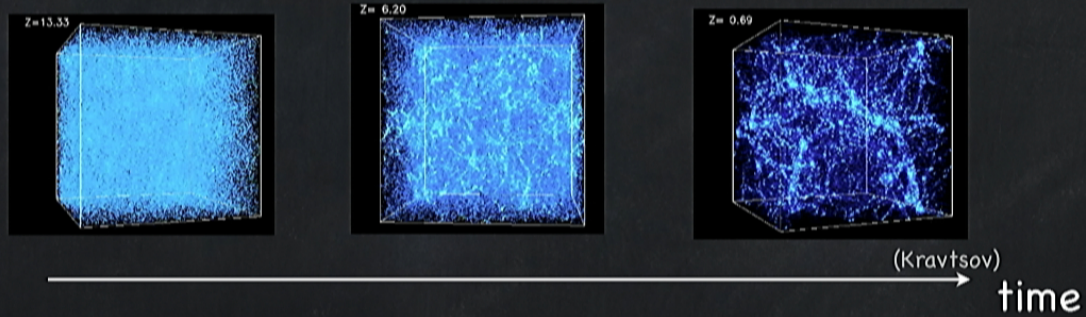
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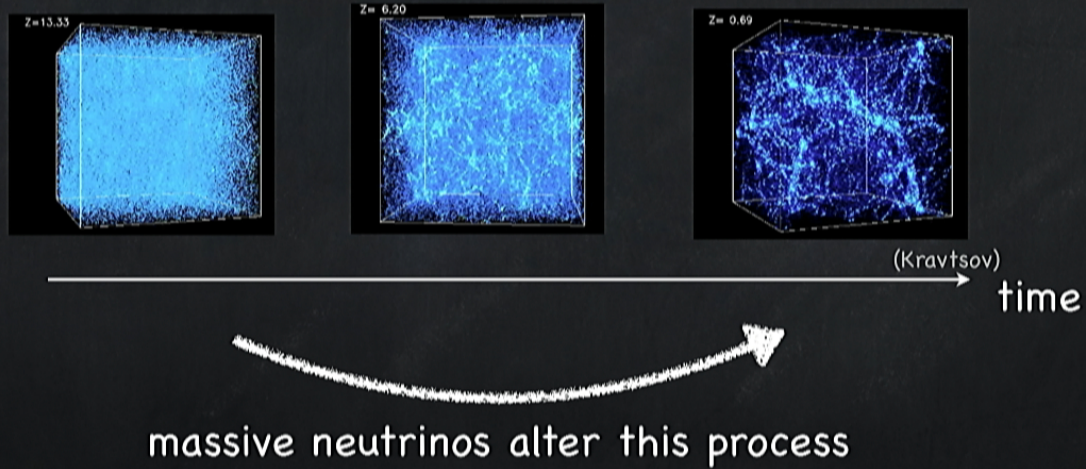
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neutrino energy density, $\rho_\nu \propto \sum (\text{number density}) m_\nu$

Neutrinos in Large-scale Structure

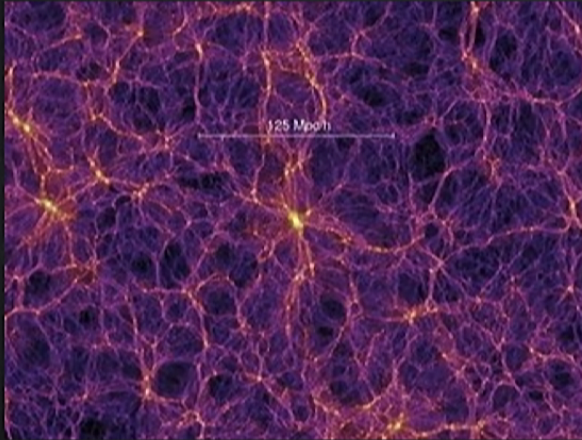


Neutrinos in Large-scale Structure



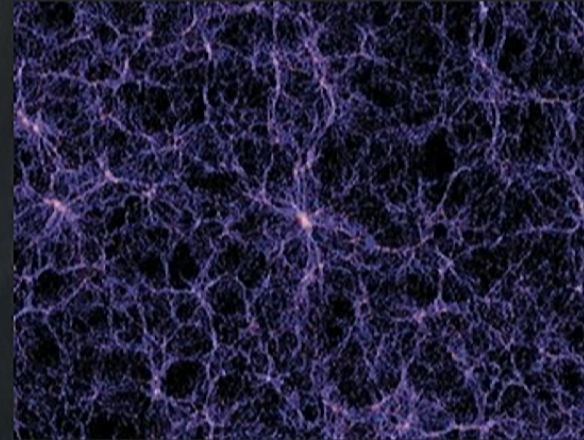
Large-scale Structure

matter distribution $\delta_m = \delta\rho_m/\rho_m$



(Springel)

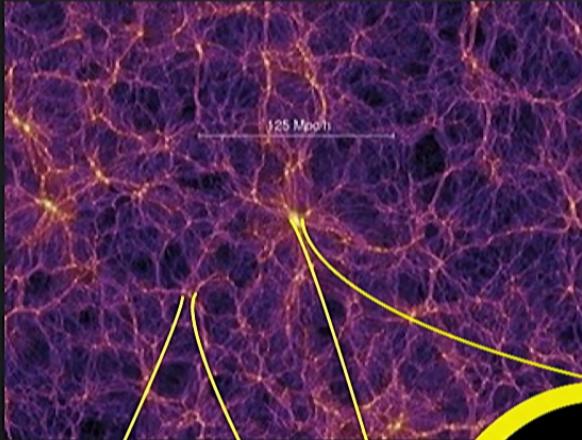
galaxy distribution $\delta_g = \delta n_g/n_g$



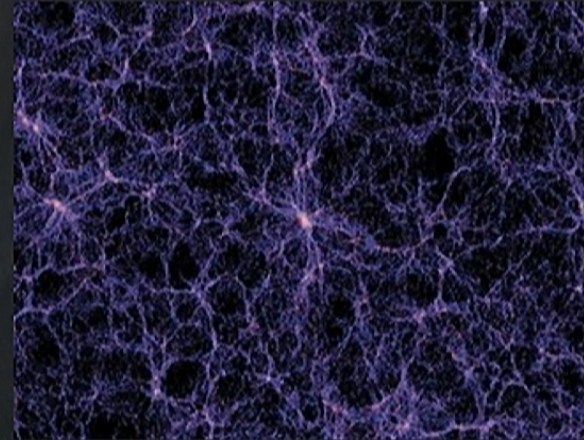
(Springel)

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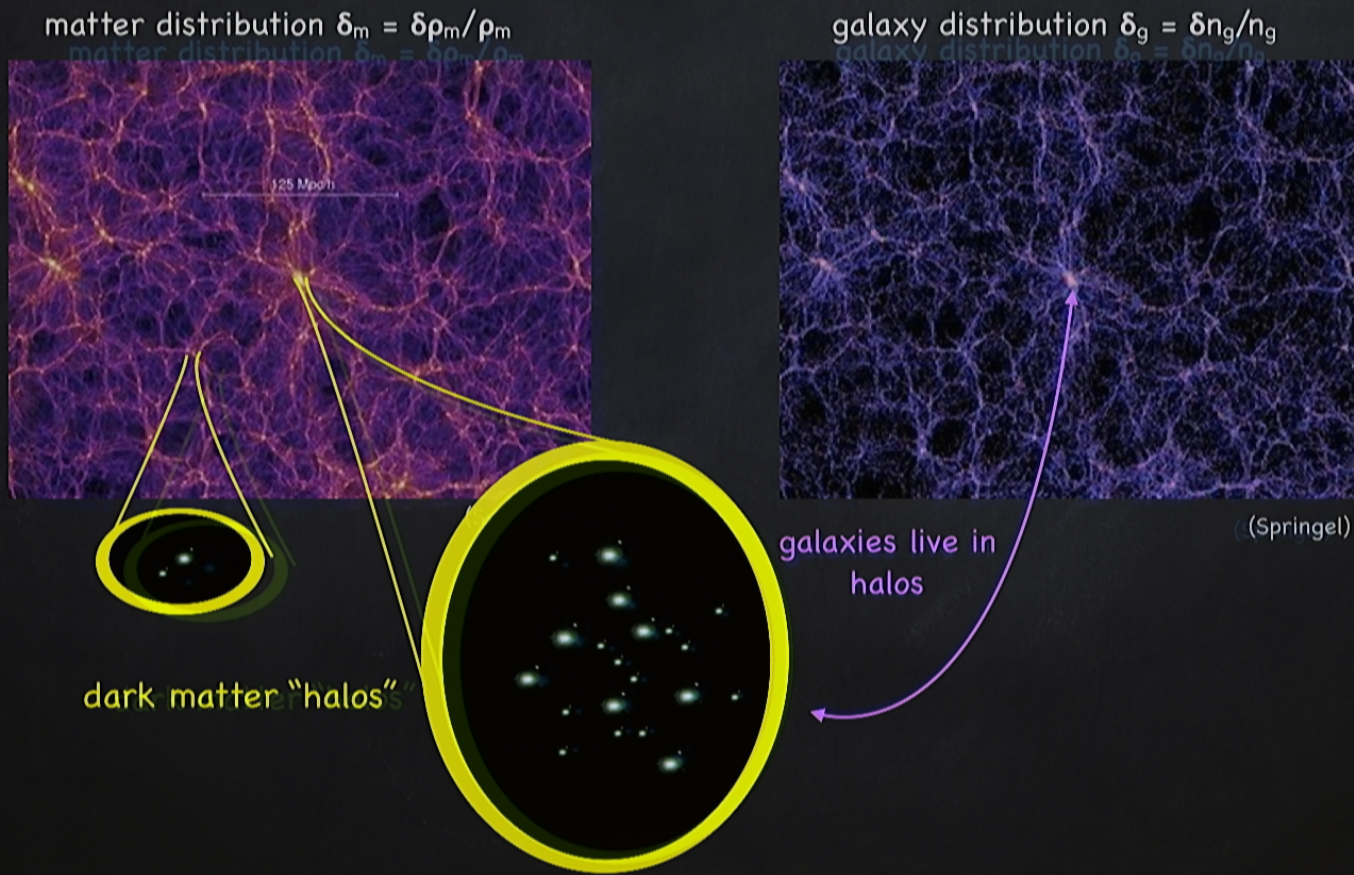


(Springel)

dark matter "halos"

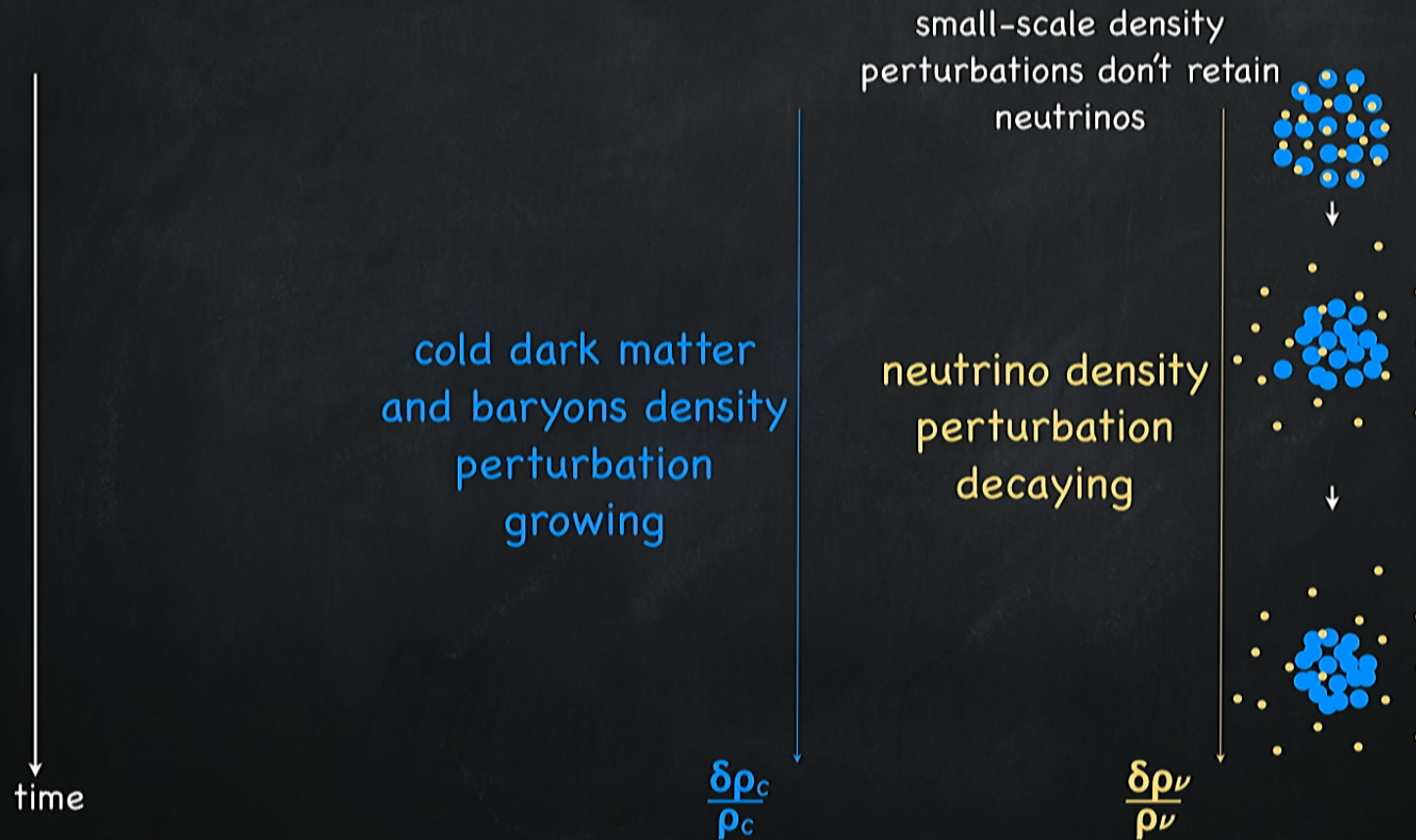


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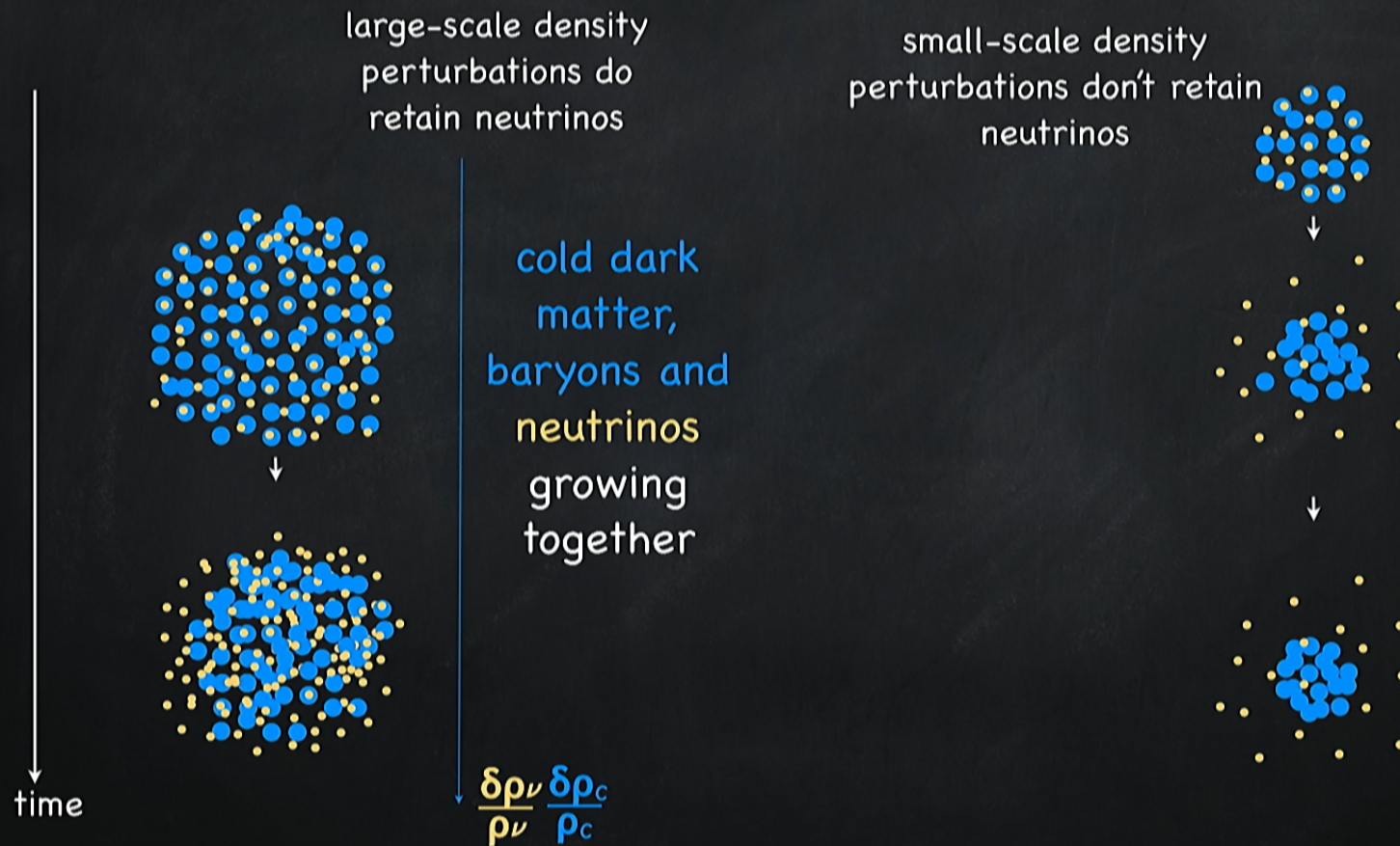


Neutrinos in large-scale structure: Linear regime

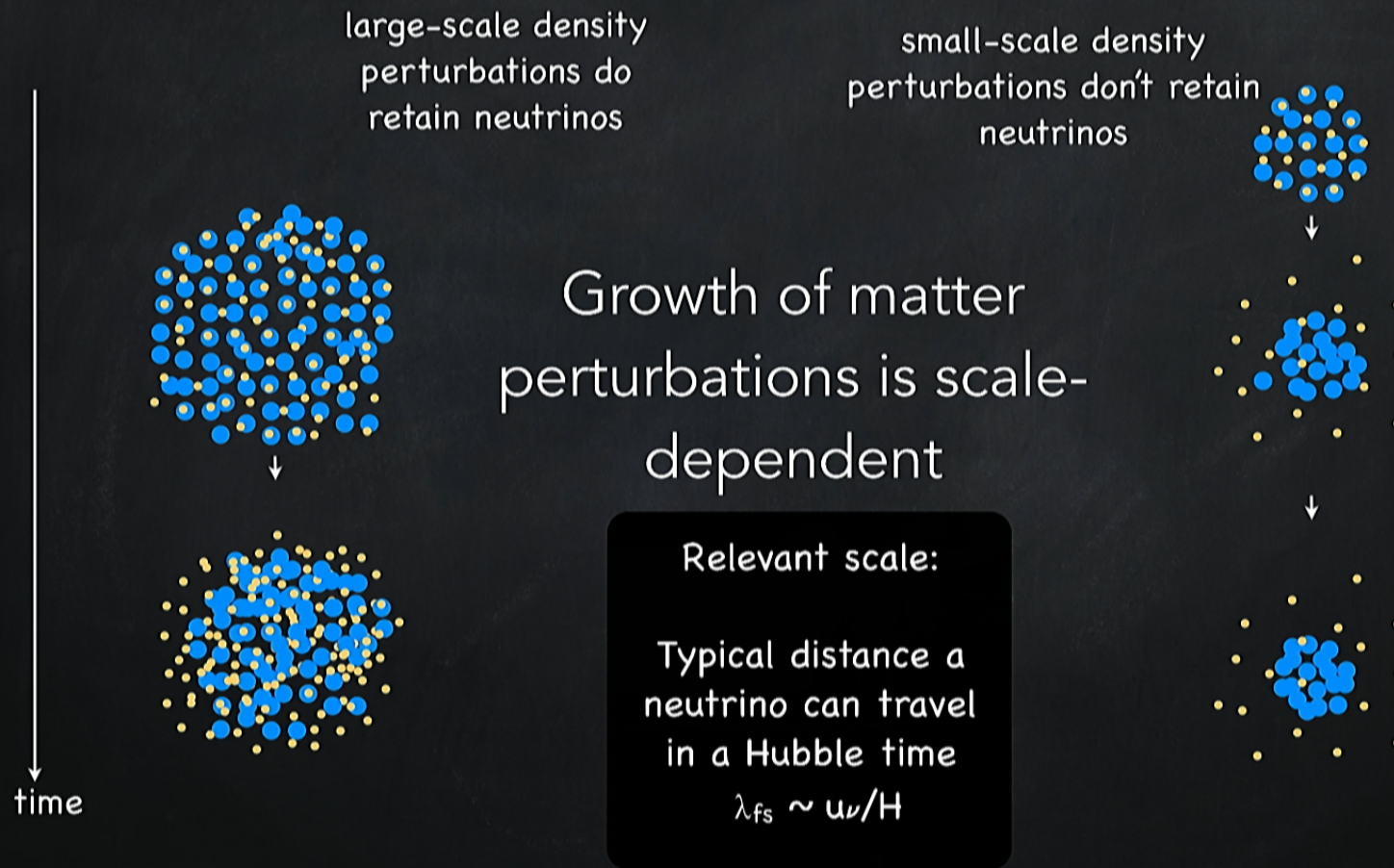
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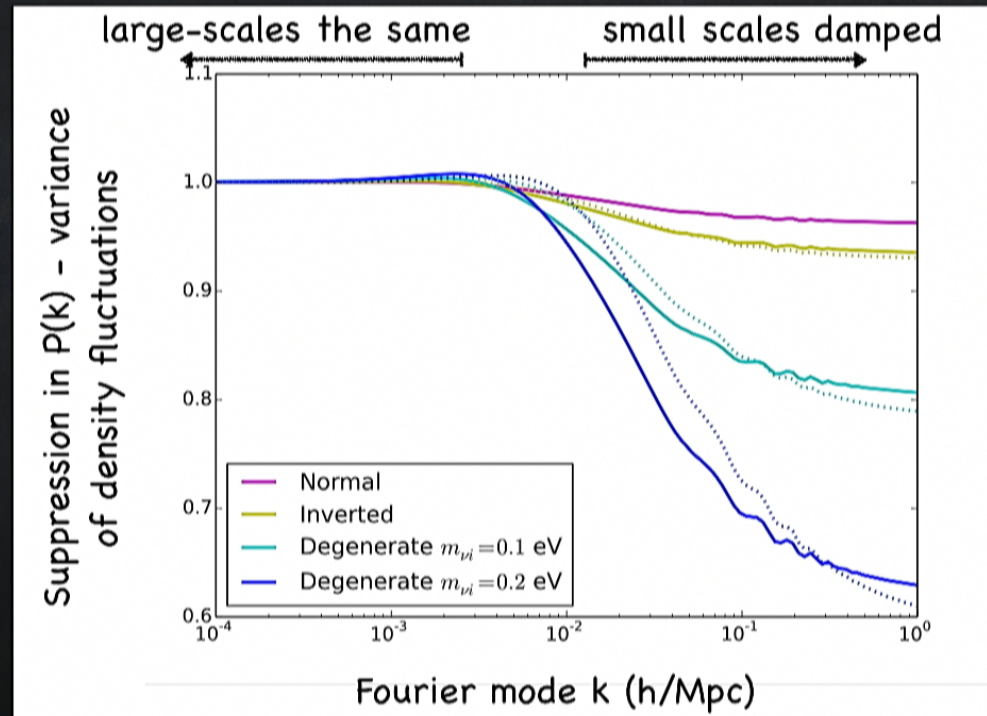
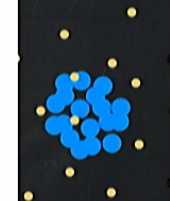


Neutrinos in large-scale structure: Linear regime



Neutrinos in large-scale structure: Linear regime

massive neutrinos reduce the typical amplitude of density perturbations

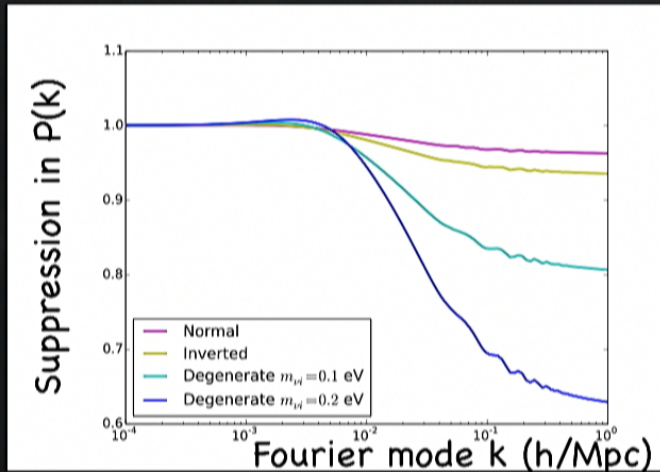


Bond, Efstathiou, Silk 1980
Hu, Eisenstein, Tegmark 1998

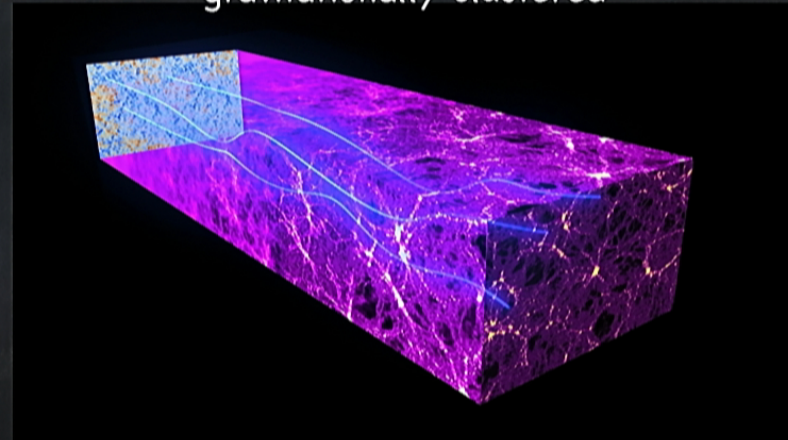
$$P(k) = \langle \delta_m(k) \delta_m(k) \rangle \quad \text{where} \quad \delta_m(k) = \frac{\delta \rho_{\text{matter}}}{\rho_{\text{matter}}}$$

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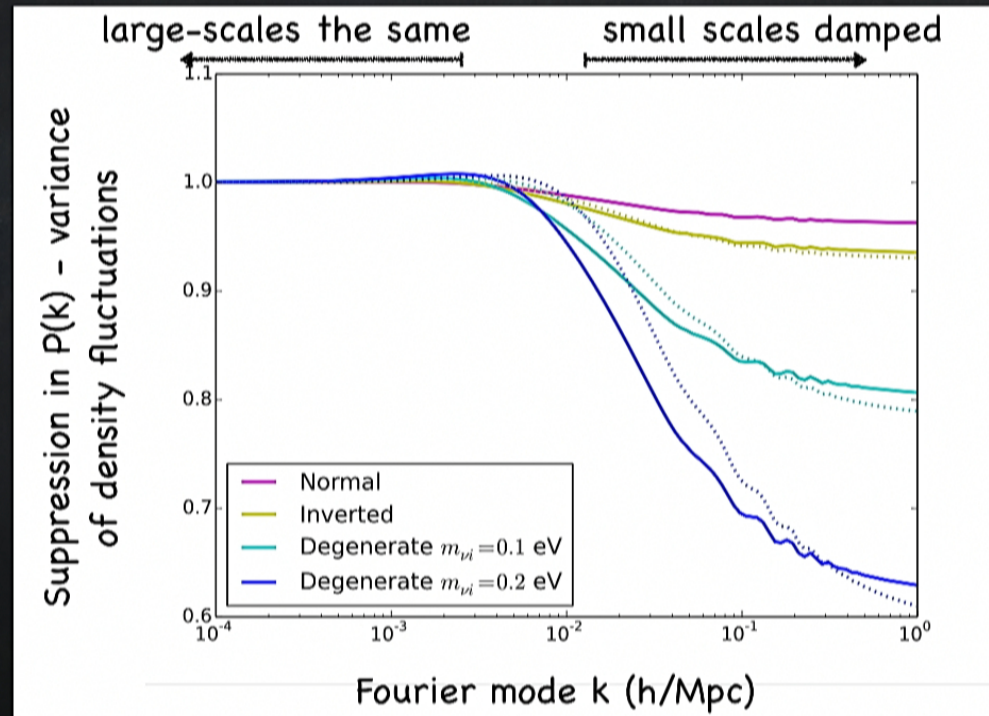
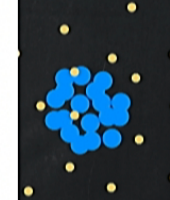
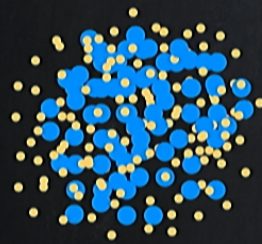
→ less gravitational lensing than a universe where all matter is gravitationally clustered



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Neutrinos in large-scale structure: Linear regime

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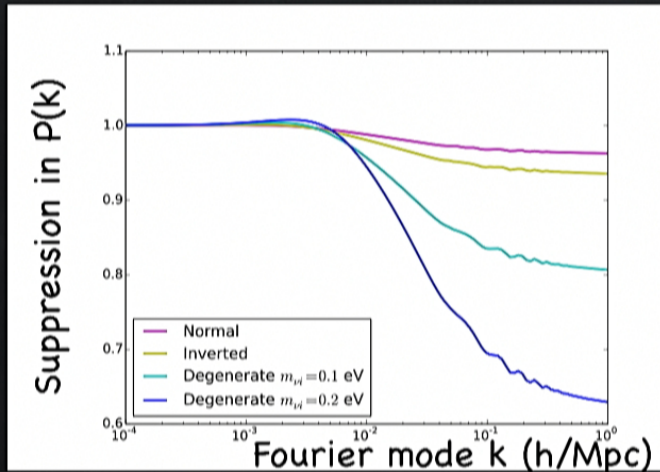


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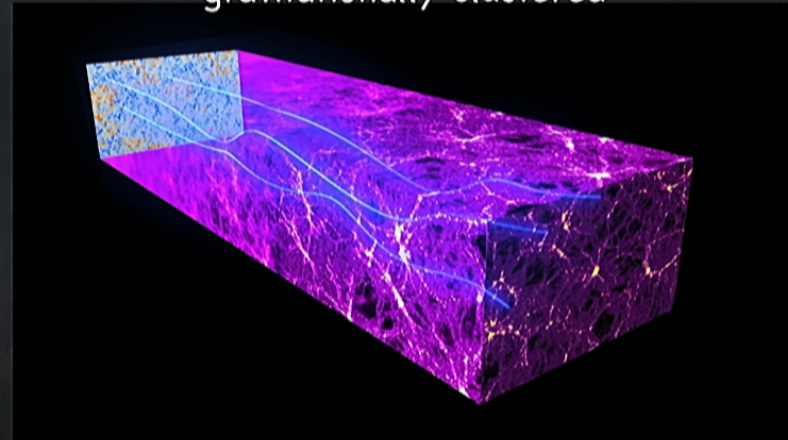
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Neutrinos in large-scale structure: Linear regime

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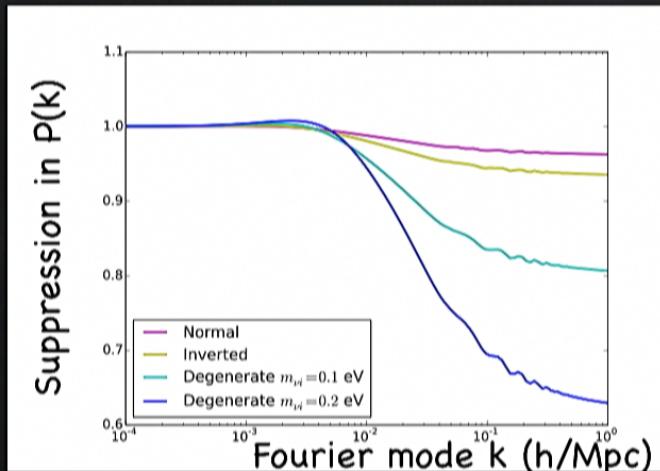
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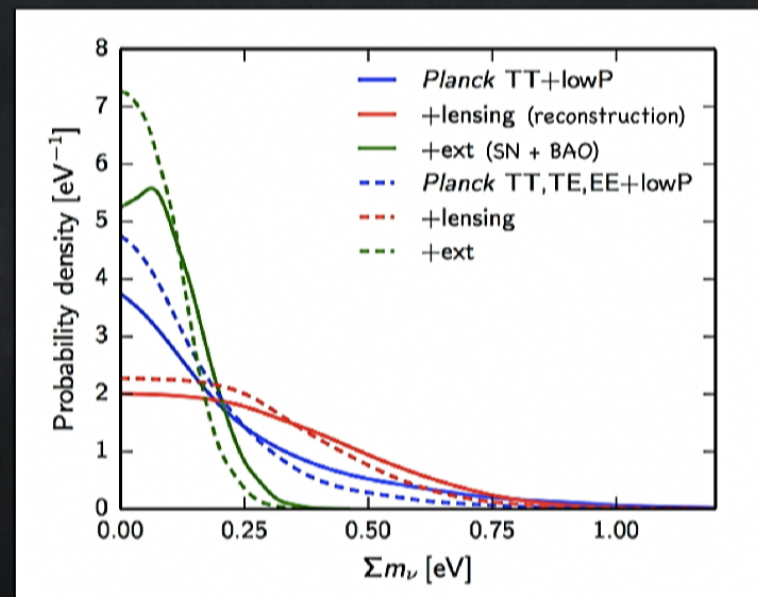
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Current constraints from CMB



Bond, Efstathiou, Silk 1980
Hu, Eisenstein, Tegmark 1998

Planck 2015

Neutrinos in large-scale structure: Linear regime

Future:

$$\sigma_{MV} \approx 0.02 \text{ eV}$$

3 σ detection of Normal
Hierarchy (0.06eV)

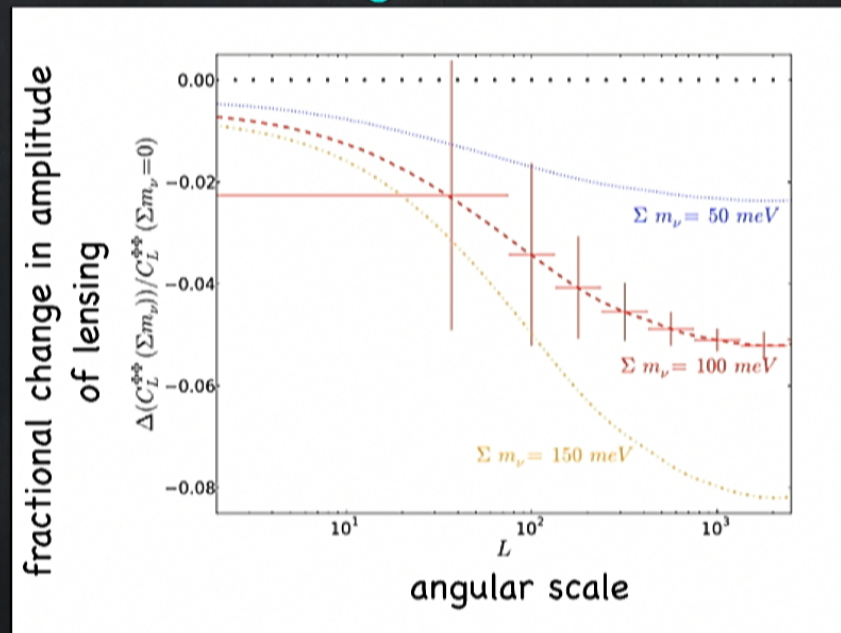
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"Stage IV CMB"



Abazajian et al 2013

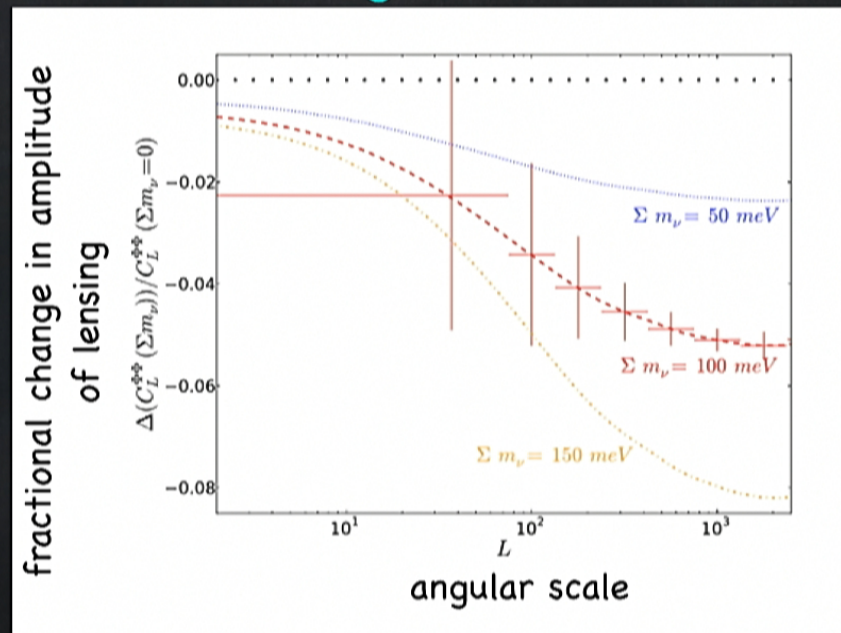
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"Stage IV CMB"



Abazajian et al 2013

CMB S4, LSST (Large Synoptic Survey Telescope), DESI (Dark Energy Spectroscopic Instrument), Euclid (ESA mission), SPHEREx . . .

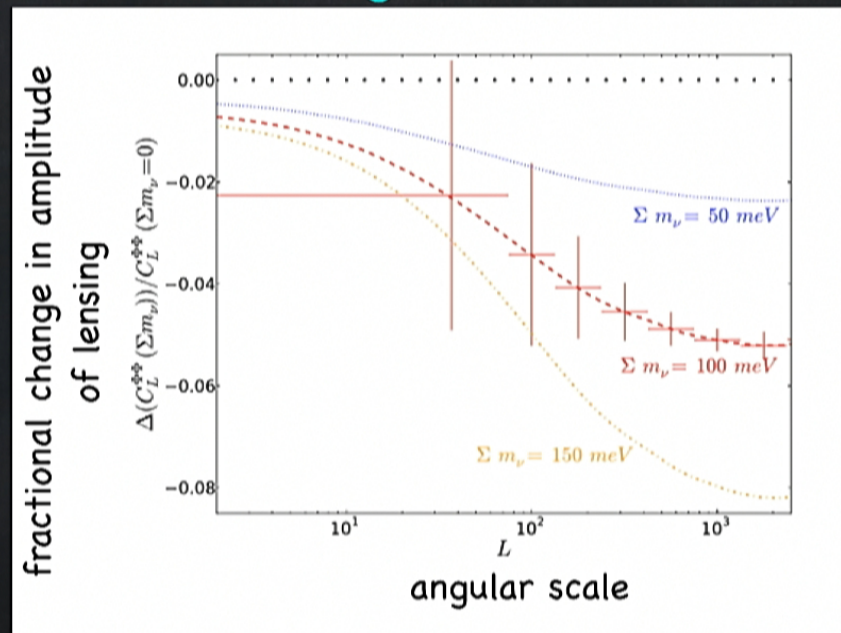
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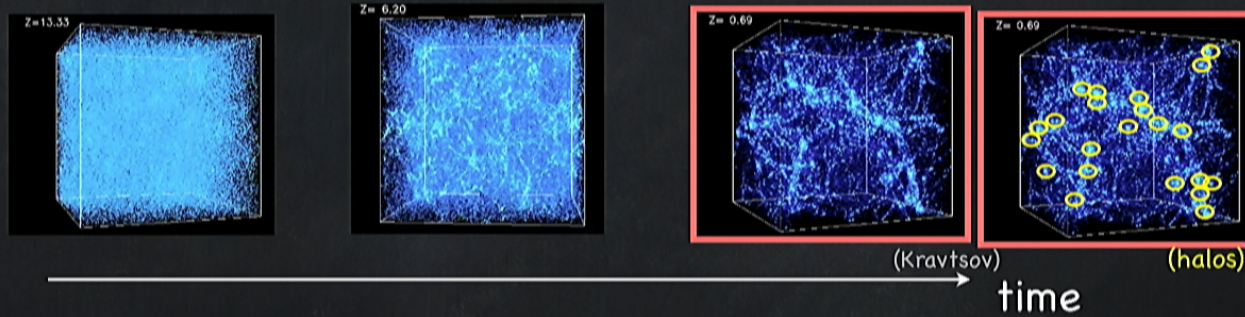
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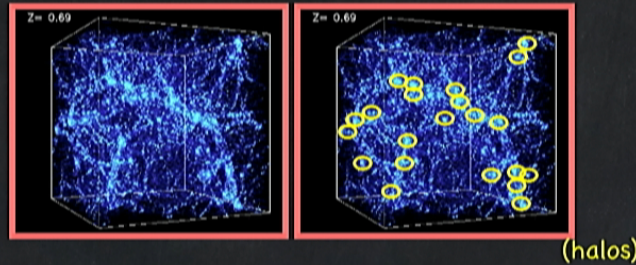
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CMB S4, LSST (Large Synoptic Survey Telescope), DESI (Dark Energy Spectroscopic Instrument), Euclid (ESA mission), SPHEREx . . .

Neutrinos in Large-scale Structure



Neutrinos in Large-scale Structure



- Suppressed matter power spectrum (test via ✓
gravitational lensing, galaxy power spectra,
cluster abundance)



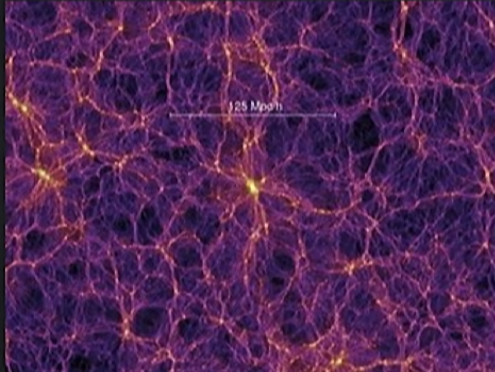
- Neutrino feature in the halo bias
- Neutrino Halos are not like CDM halos

Scale-dependent halo bias from massive neutrinos

Halo bias

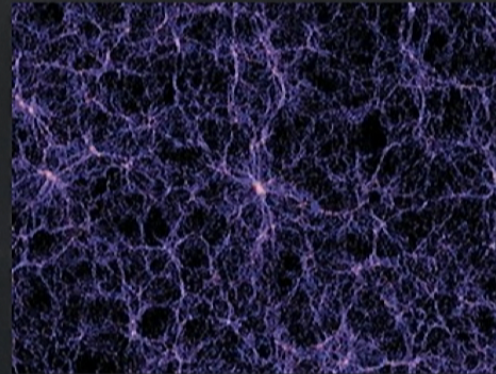
Halo bias

matter distribution $\delta_m(x) = \delta\rho_m/\rho_m$



(Springel)

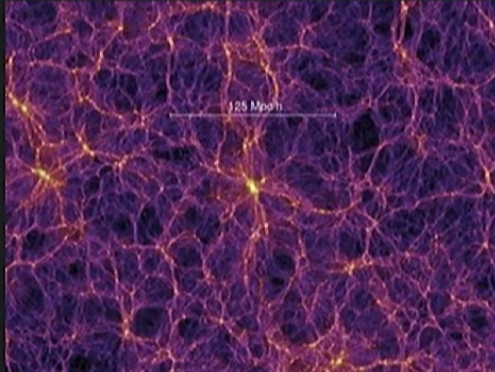
galaxy distribution $\delta_g(x) = \delta n_g/n_g$



(Springel)

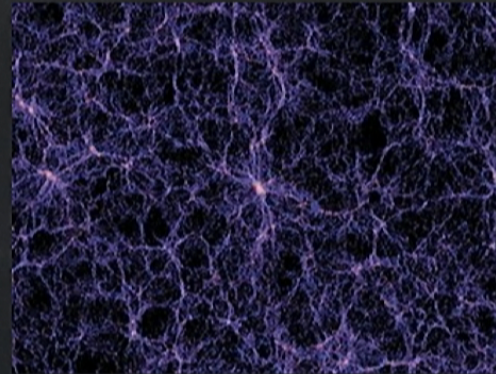
Halo bias

matter distribution $\delta_m(x) = \delta\rho_m/\rho_m$



(Springel)

galaxy distribution $\delta_g(x) = \delta n_g/n_g$

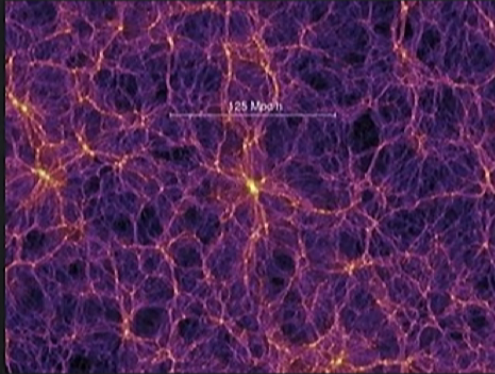


(Springel)

For large separations, $\langle \delta_g(x_1)\delta_g(x_2) \rangle \approx b^2 \langle \delta_m(x_1)\delta_m(x_2) \rangle$, where b is what astronomers call the bias

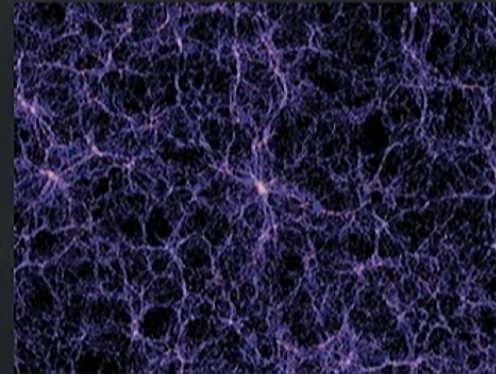
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For large separations, $\langle \delta_g(x_1)\delta_g(x_2) \rangle \approx b^2 \langle \delta_m(x_1)\delta_m(x_2) \rangle$, where b is what astronomers call the bias

The value of b depends on the type of object you are looking at (e.g. the mass or luminosity of the galaxies you've measured) and rare objects have a larger value of b .

Halo bias

matter distribution $\delta_m(x) = \delta\rho_m/\rho_m$

galaxy distribution $\delta_g(x) = \delta n_g/n_g$



Galaxies live in halos, so I'm going to use halo bias and galaxy bias interchangeably but reality is more complicated.

Halo bias - simplest model

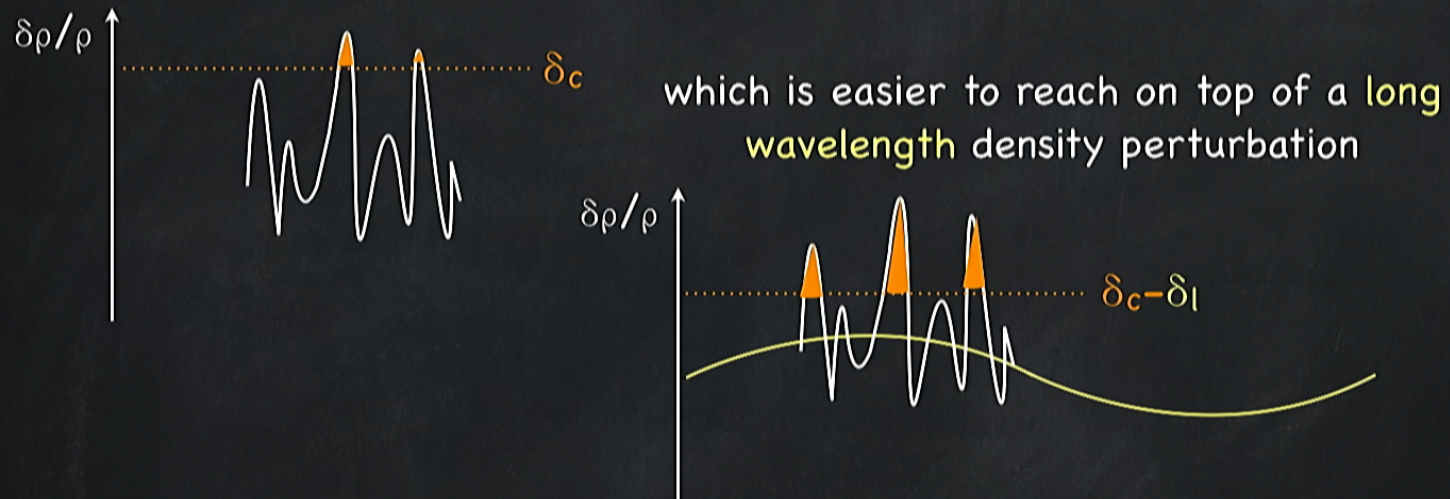
Halo bias - simplest model

a dark matter halo forms when $\delta\rho/\rho$ is larger than the collapse threshold



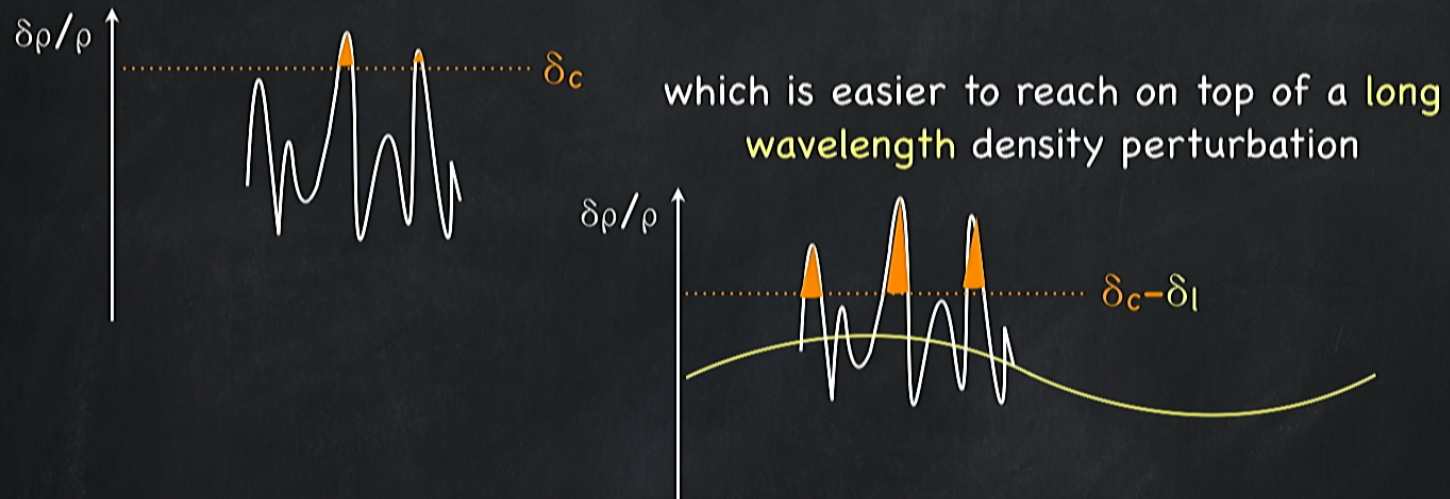
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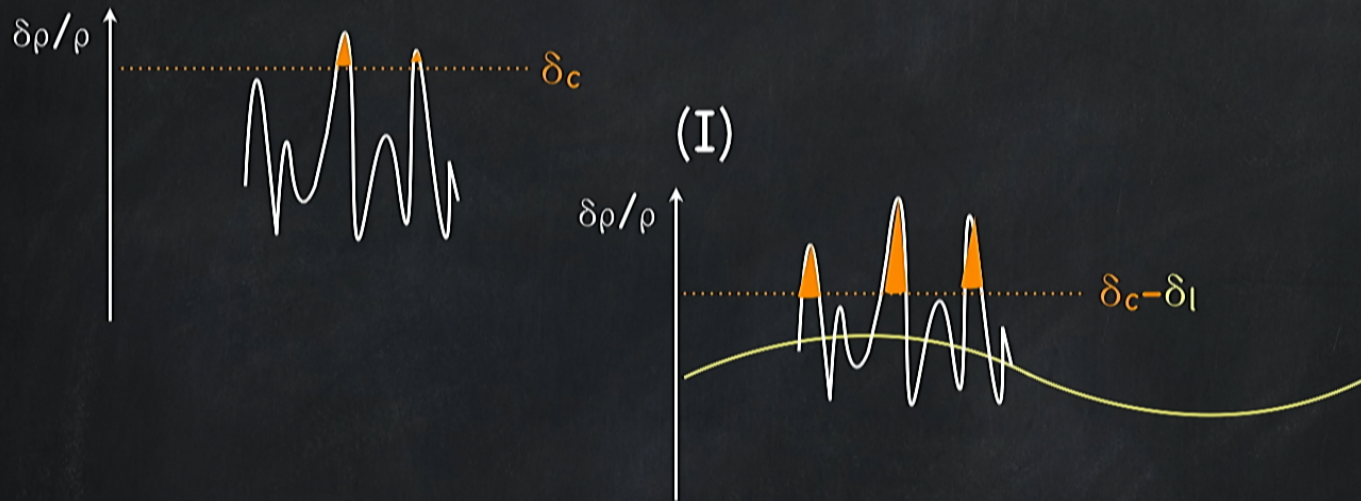
a dark matter halo forms when $\delta\rho/\rho$ is larger than the collapse threshold



initially over-dense regions occupy less volume at late times, so the number density there is increased



Halo bias - simplest model



(II)

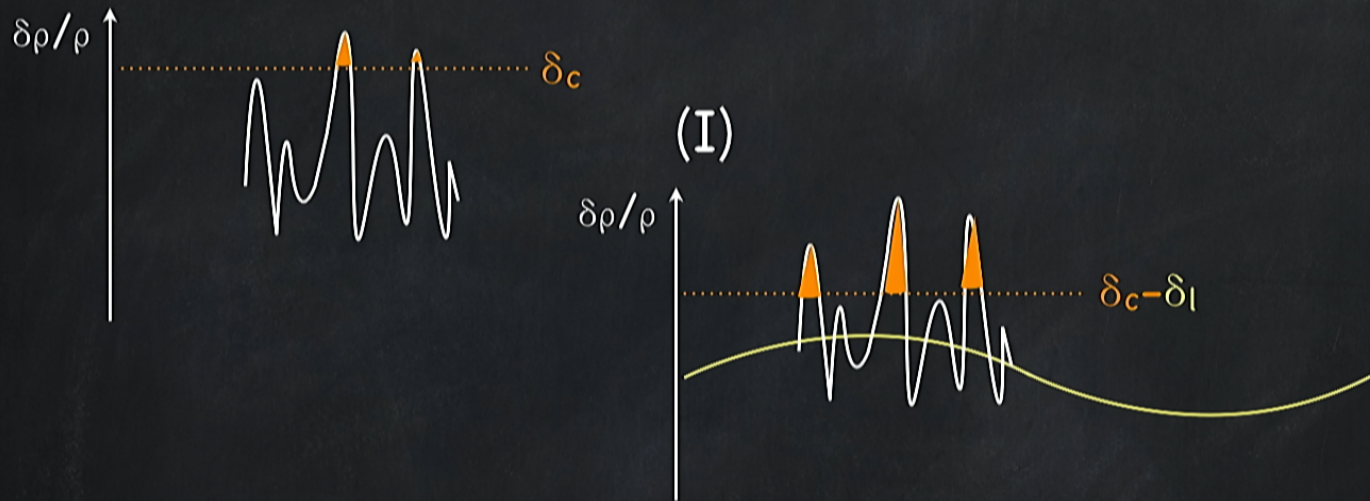


(I) and (II) predict how the **number** density of halos fluctuates with δ_l

$$\delta n/n = \frac{1}{n} \frac{\partial n}{\partial \delta} \delta_l \dots$$

Gunn & Gott 1972 Press & Schechter 1974

Halo bias - simplest model



(II)



(I) and (II) predict how the **number** density of halos fluctuates with δ_l

$$\delta n/n = \frac{1}{n} \frac{\partial n}{\partial \delta} \delta_l \dots$$

\equiv **b halo bias**

Gunn & Gott 1972 Press & Schechter 1974

Halo bias - simplest model

Add neutrinos:

- For low neutrino masses, can ignore neutrino contribution to halo mass ($M_\nu \text{ in halo} \ll M_{\text{halo}}$)

ML and Zaldarriaga 2013

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ML and Zaldarriaga 2013

- BUT, neutrino effects on evolution of δ_l can't be ignored — halos are forming in different background



(same as a universe with only CDM)

(grows more slowly)

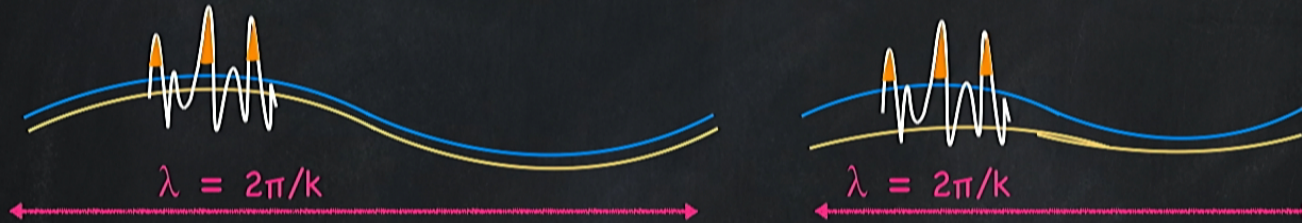
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ML and Zaldarriaga 2013

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The k -dependent evolution of δ_l causes the threshold for collapse to depend on k also

ML 2014b

(see also Hui & Parfrey 2008; Parfrey, Hui, Sheth 2011)

Halo bias - simplest model

Add neutrinos:

The k -dependent evolution of δ_l causes the threshold
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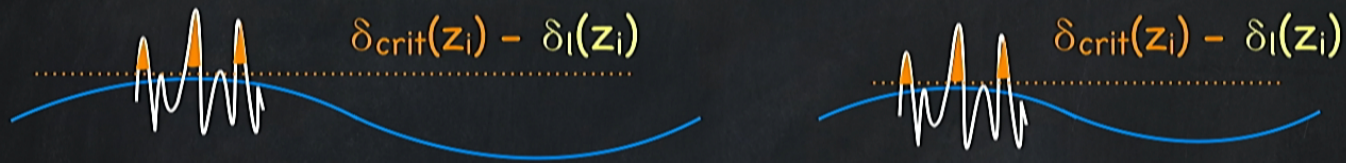
(see also Hui & Parfrey 2008; Parfrey, Hui, Sheth 2011)

Halo bias - simplest model

Add neutrinos:

The k -dependent evolution of δ_l causes the threshold
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Sketch:



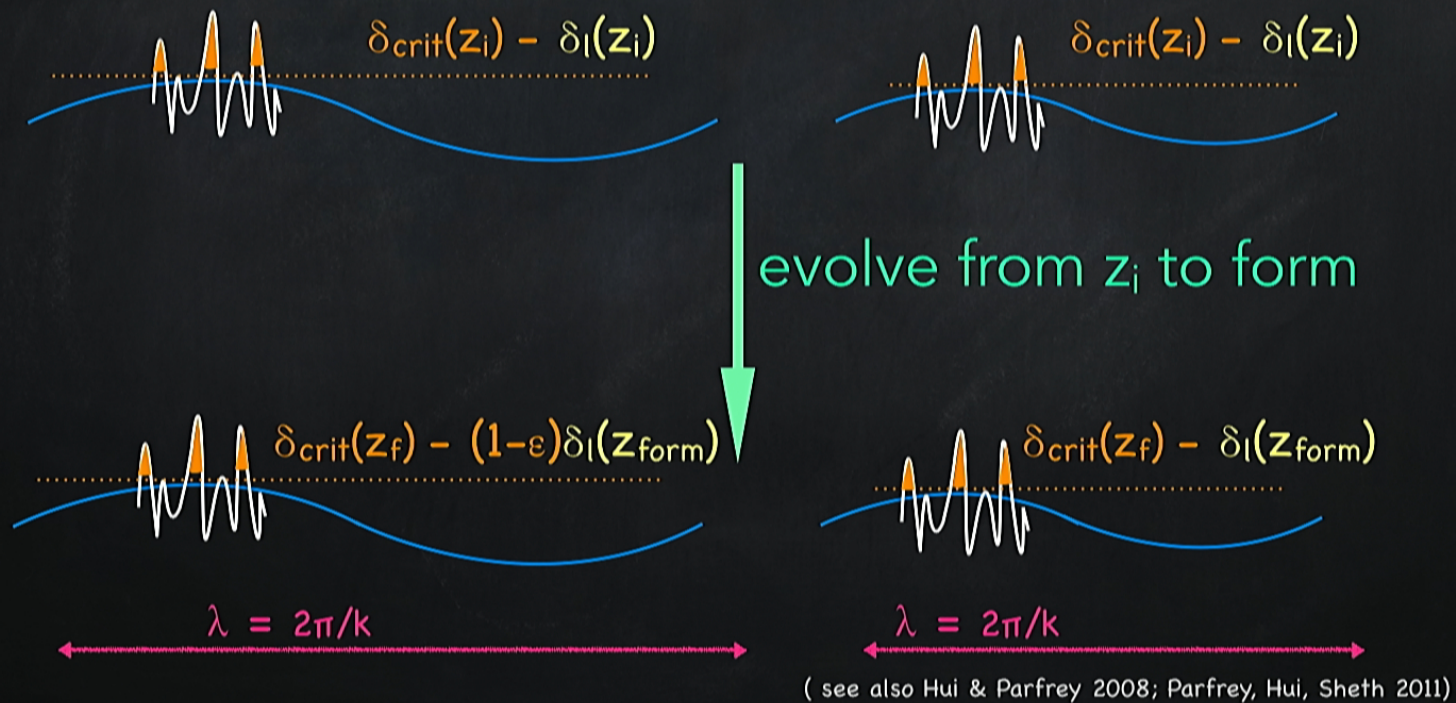
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Halo bias - simplest model

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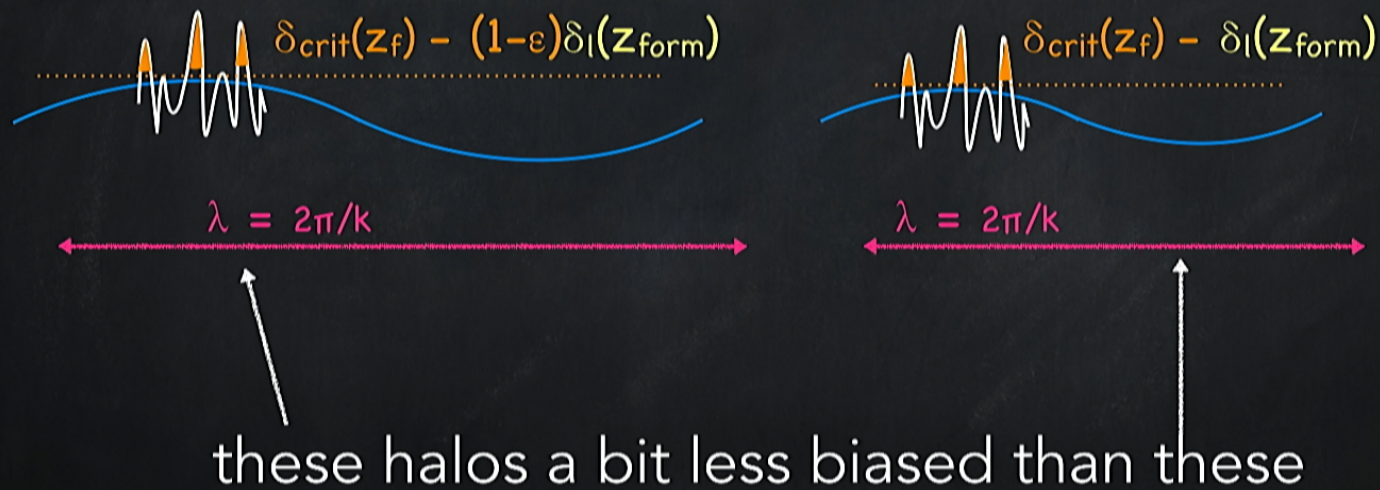


Halo bias - simplest model

Add neutrinos:

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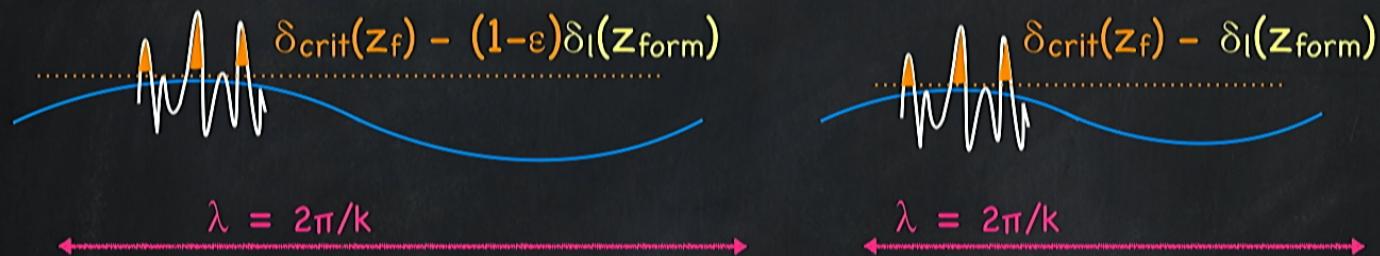
(see also Hui & Parfrey 2008; Parfrey, Hui, Sheth 2011)

Halo bias - simplest model

Add neutrinos:

The k -dependent evolution of δ_l causes the threshold for collapse to depend on k also ML 2014b

Sketch:



these halos a bit less biased than these

** Neutrinos have scale-dependent growth at all times, so the truth is more complicated than the sketch here **

(see also Hui & Parfrey 2008; Parfrey, Hui, Sheth 2011)

Halo bias - simplest model

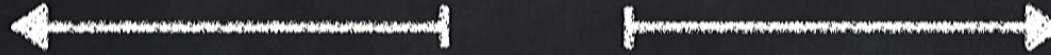
In a universe with massive neutrinos:

$$b(k < k_{\text{free-streaming}}) \neq b(k > k_{\text{free-streaming}})$$

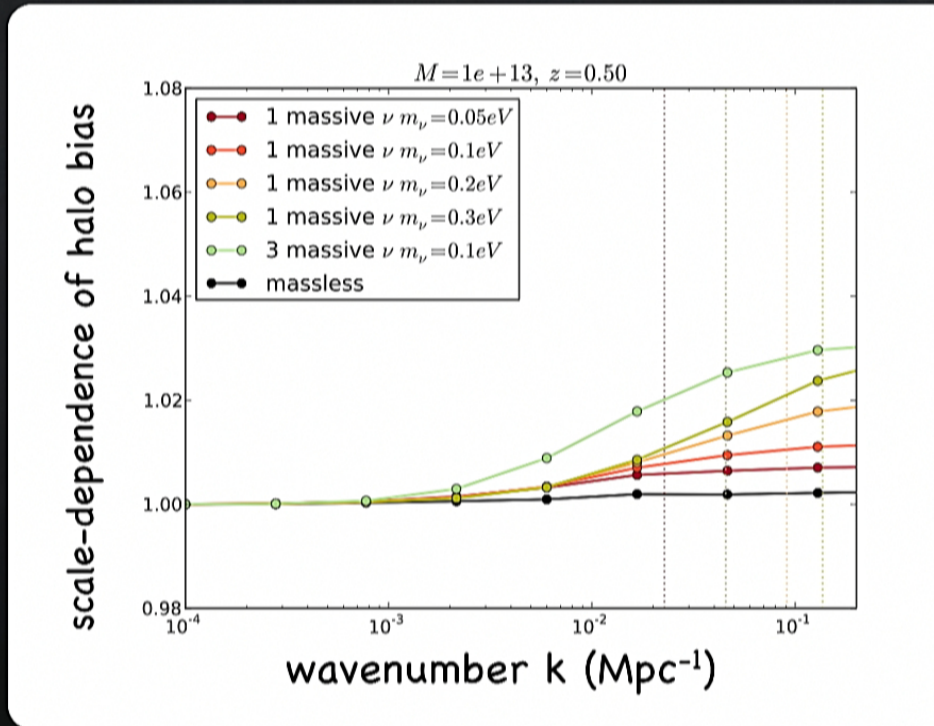
Halo bias - simplest model

In a universe with massive neutrinos:

$$b(k < k_{\text{free-streaming}}) \neq b(k > k_{\text{free-streaming}})$$



$$b(k) = \sqrt{P_{hh}(k)/P_{mm}(k)}$$

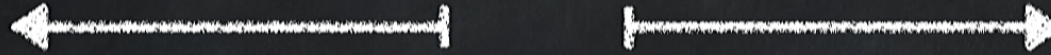


(ML 2014)

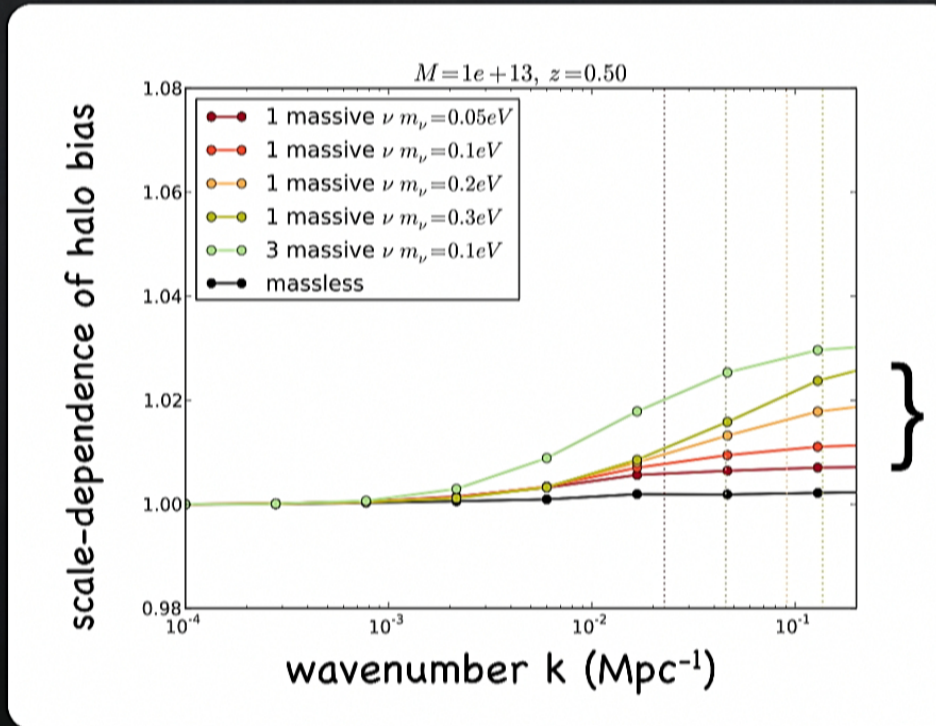
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$$\sim \frac{\rho_\nu}{\rho_{\text{matter}}}$$

(ML 2014)

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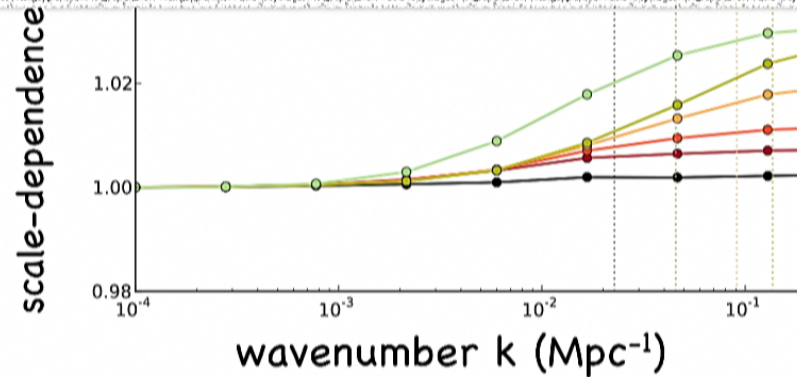
$$b(k) = \sqrt{P_{hh}(k)/P_{mm}(k)}$$

In general,

$$\frac{\Delta b}{b} \approx f_\nu + \frac{b-1}{b} (\# f_\nu)$$

where

$$f_\nu = \frac{\rho_\nu}{\rho_{\text{cdm}} + \rho_\nu}$$



$$\sim \frac{\rho_\nu}{\rho_{\text{matter}}}$$

(ML 2014)

Observational consequences

Scale-dependent change in the halo bias:

$$\frac{\Delta b}{b} \approx f_\nu + \frac{b-1}{b} (\# f_\nu) \quad \text{where} \quad f_\nu = \frac{\rho_\nu}{\rho_{\text{cdm}} + \rho_\nu}$$

The fraction of energy in neutrinos may be tiny ($f_\nu \approx 0.5\%$)

(ML 2014)

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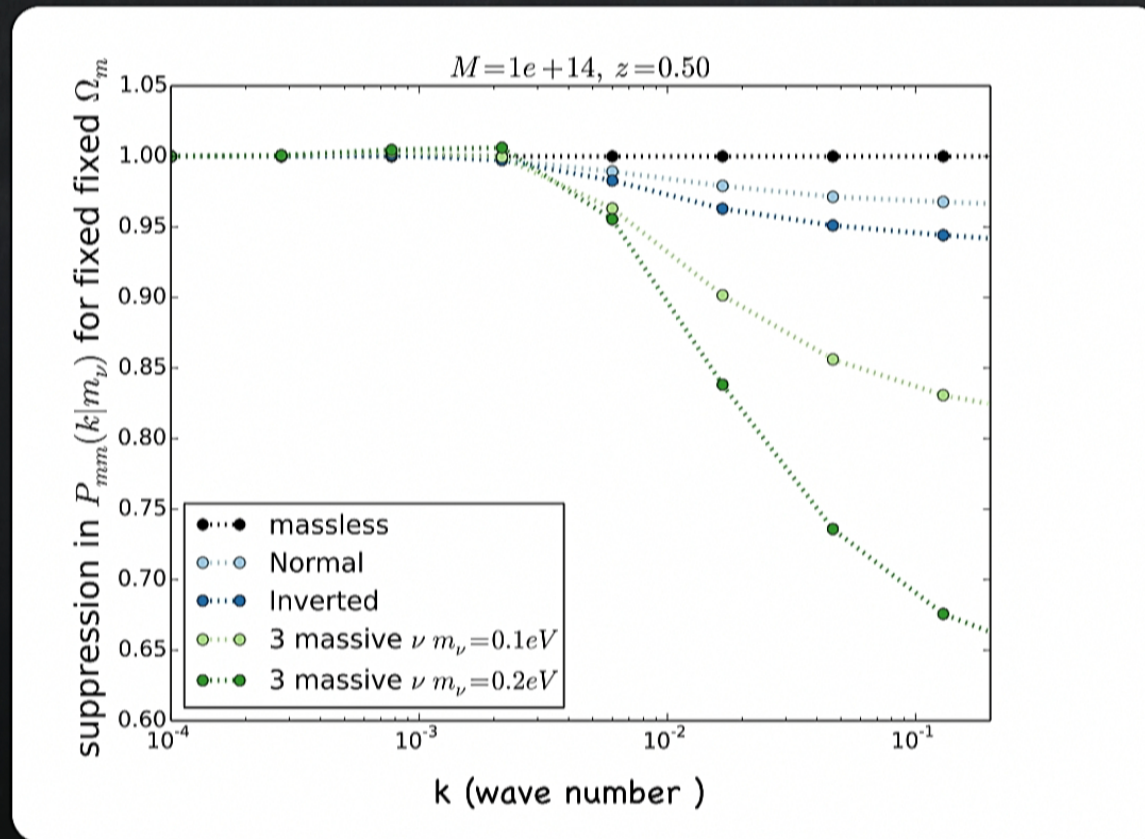
Why care about such a small change to the halo bias?

- Because the feature in the halo bias can be used to measure neutrino mass

(ML 2014)

A systematic for measurements of m_ν from galaxy clustering

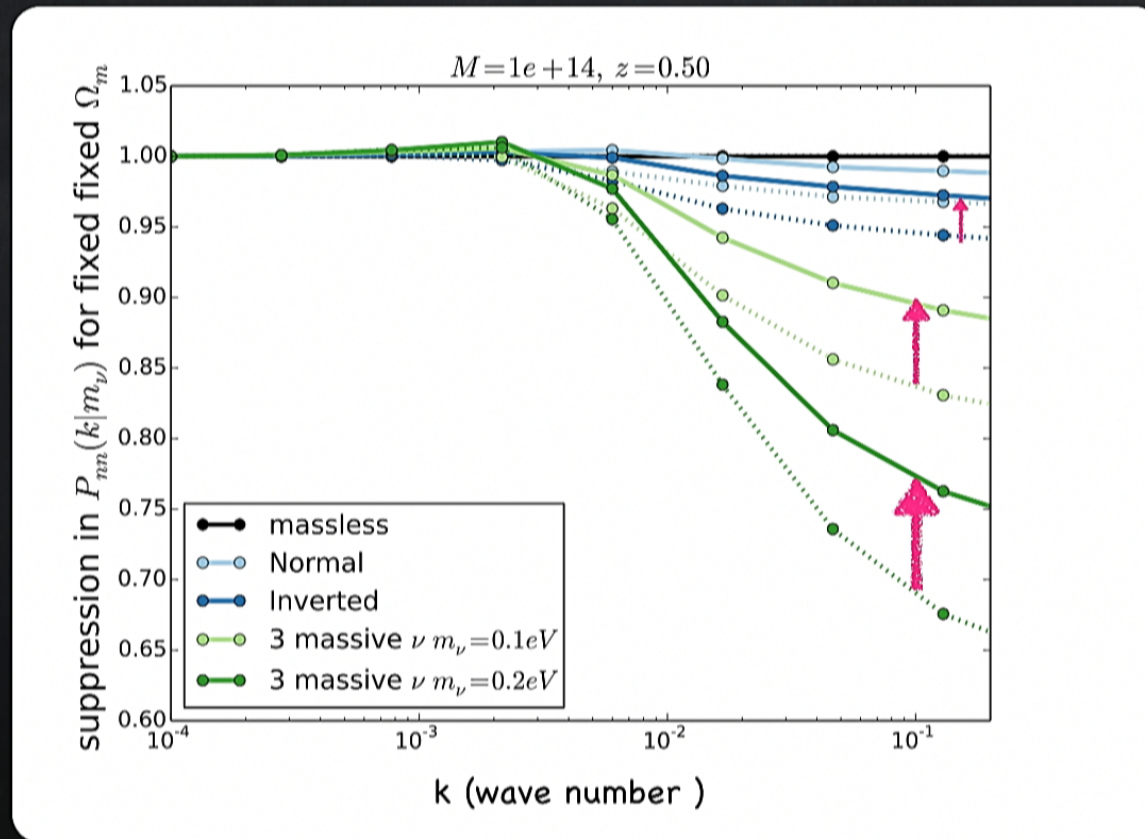
Without scale-dependent bias neutrinos produce identical changes to $P_{\text{galaxy-galaxy}}(k)$ and $P_{\text{matter-matter}}(k)$, ($P_{\text{galaxy-galaxy}}(k) = b^2 P_{\text{matter-matter}}(k)$)



(ML 2014)

A systematic for measurements of m_ν from galaxy clustering

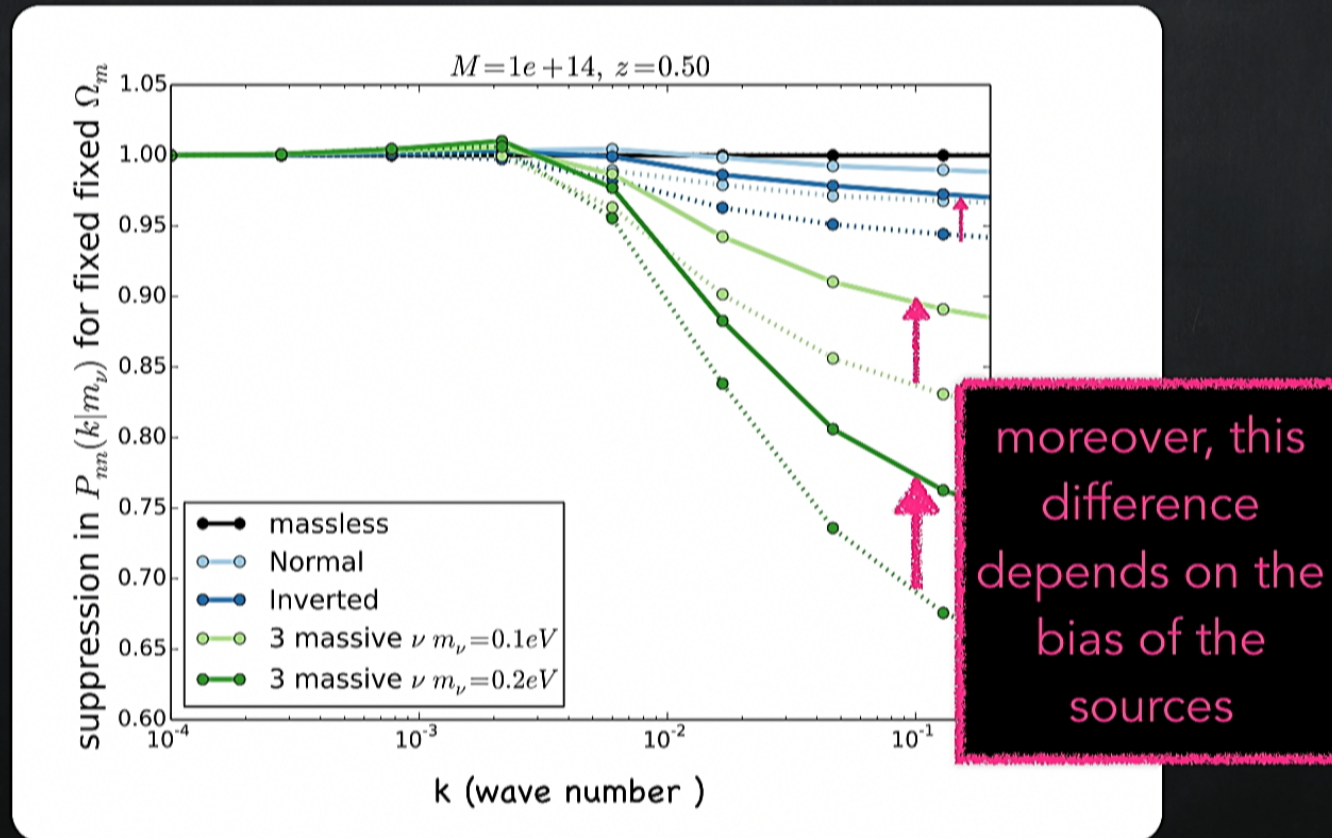
With scale-dependent bias neutrinos don't suppress $P_{\text{galaxy-galaxy}}(k)$ as much as $P_{\text{matter-matter}}(k)$, ($P_{\text{galaxy-galaxy}}(k) = b(k)^2 P_{\text{matter-matter}}(k)$)



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(ML 2014)

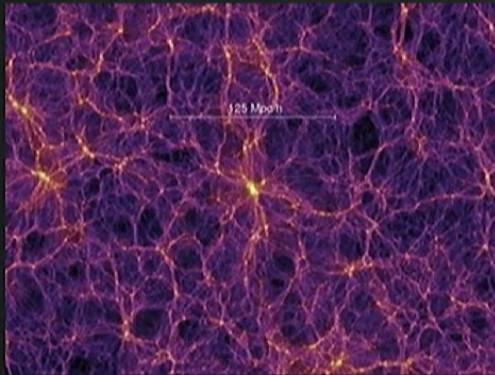
The feature in the halo bias can be used to measure neutrino mass

The feature in the halo bias can be used to measure neutrino mass

Suppose one has high number density of sources that trace the matter field

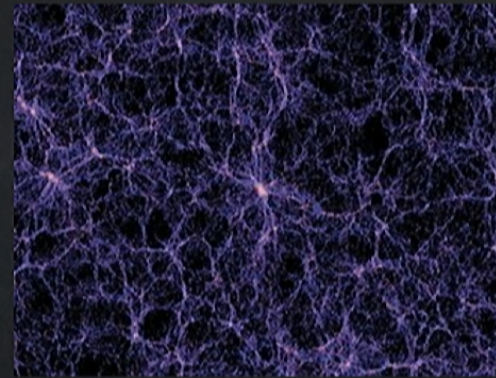
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matter distribution $\delta_m = \delta\rho_m/\rho_m$



(Springel)

galaxy distribution $\delta_g = \delta n_g/n_g$



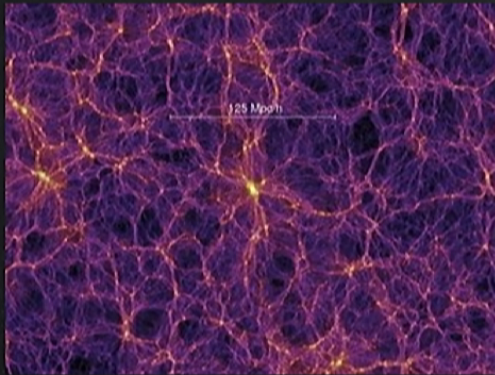
(Springel)

The feature in the halo bias can be used to measure neutrino mass

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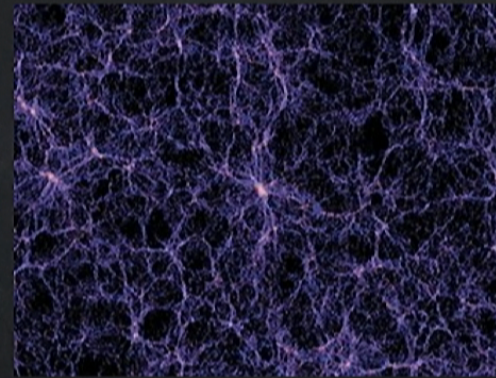
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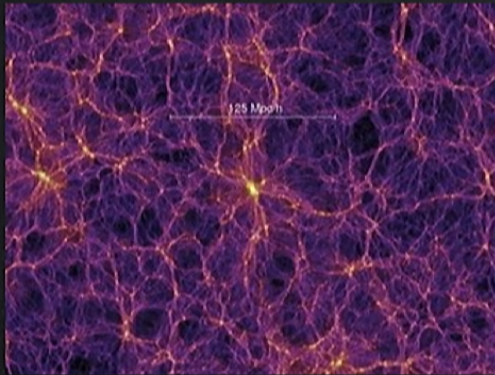
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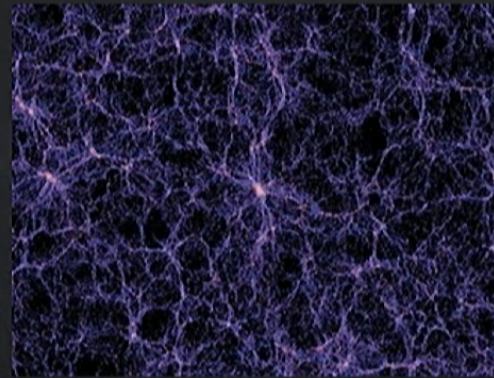
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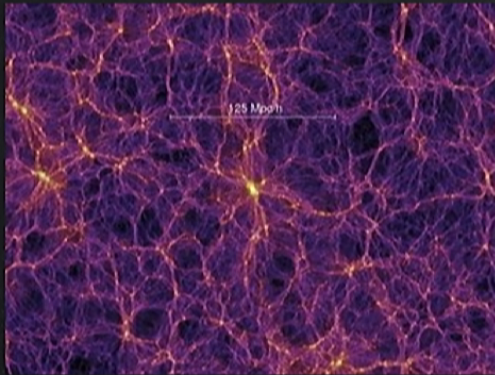
(Springel)

It turns out that the bias \mathbf{b} can be measured without cosmic variance (Pen 2004, Seljak 2008)

The feature in the halo bias can be used to measure neutrino mass

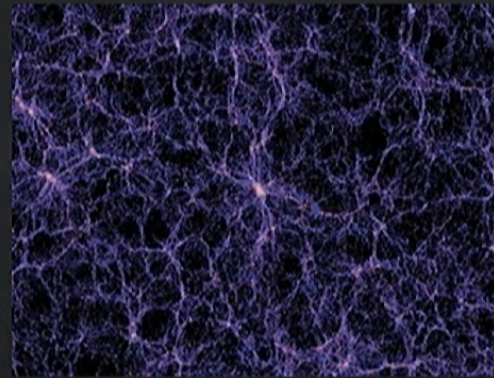
Suppose one has high number density of sources that trace the matter field $\delta\rho_m/\rho_m$ with a bias factor b , i.e. $\delta n_g/n_g = b \delta\rho_m/\rho_m$

matter distribution $\delta_m = \delta\rho_m/\rho_m$



(Springel)

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(Springel)

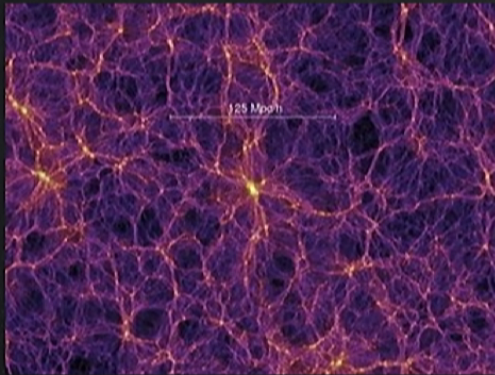
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$$\sigma_b \sim \frac{1}{\sqrt{n_{\text{galaxies}} P_{\text{matter}}}}$$

The feature in the halo bias can be used to measure neutrino mass

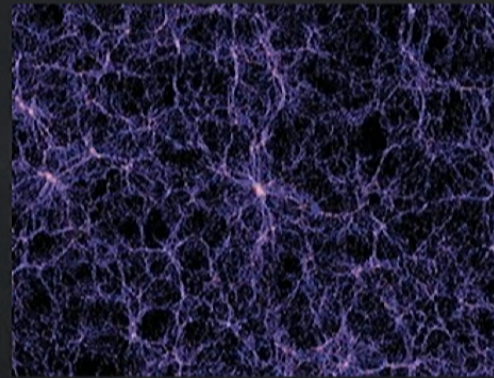
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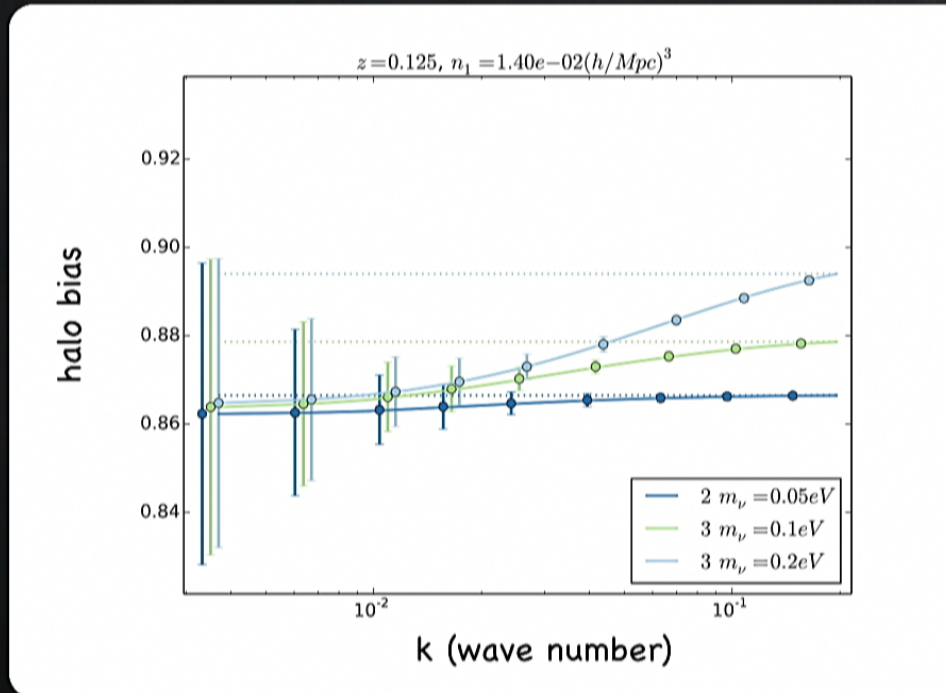
It turns out that the bias b can be measured without cosmic variance (Pen 2004, Seljak 2008)

$$\sigma_b \sim \frac{1}{\sqrt{n_{\text{galaxies}} P_{\text{matter}}}}$$

Compare:

$$\sigma_{P_k} \sim \sqrt{\frac{P(k)}{N_k}}$$

The feature in the halo bias can be used to measure neutrino mass

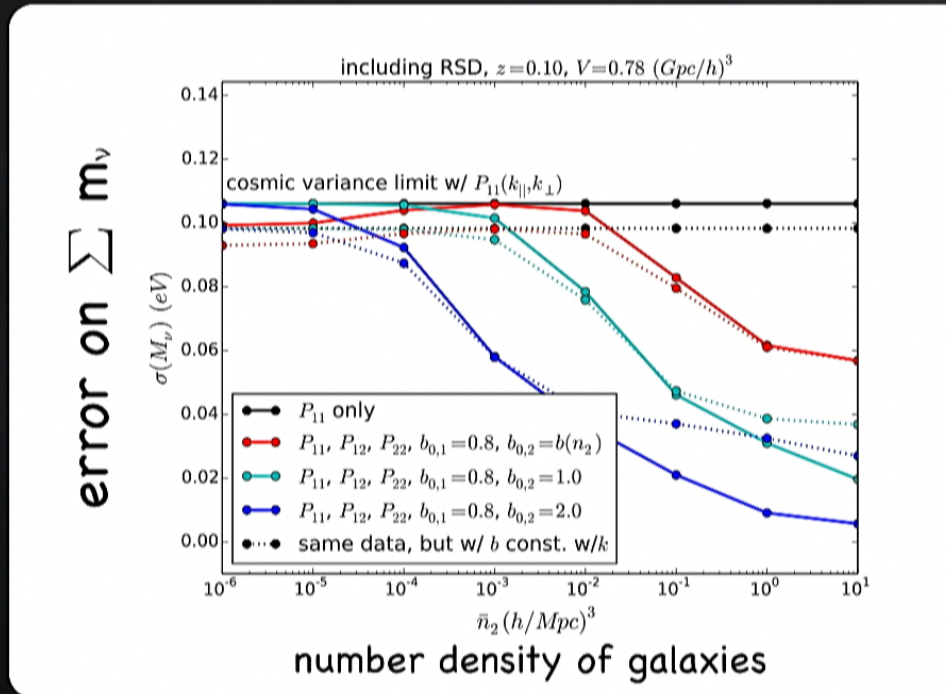


$$\sigma_b \sim \frac{1}{\sqrt{n_1 P_{mm}}}$$

(ideal huge number density of sources, super-ideal lack of systematics)

(ML 2016)

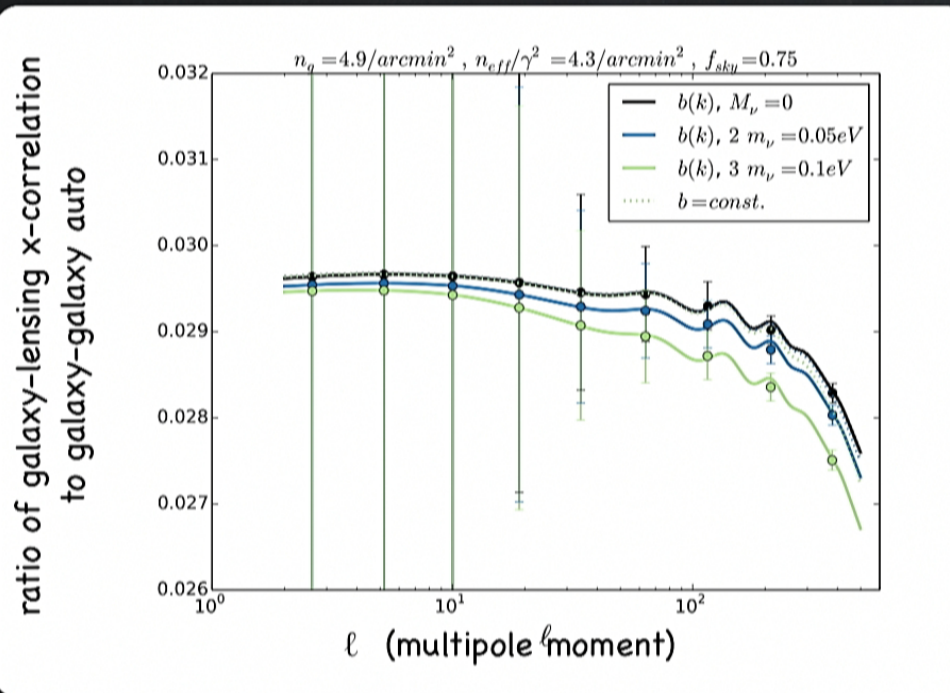
The feature in the halo bias can be used to measure neutrino mass



$$\sigma_b \sim \frac{1}{\sqrt{n_1 P_{mm}}}$$

(ML 2016)

The feature in the halo bias can be used to measure neutrino mass



(LSST-like number density of sources, super-ideal lack of systematics)

(ML 2016)

The key point

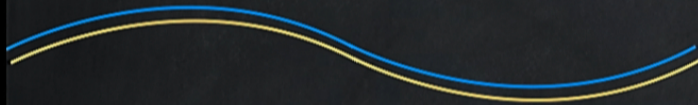
The key point

To a local observer, these backgrounds are *inequivalent*



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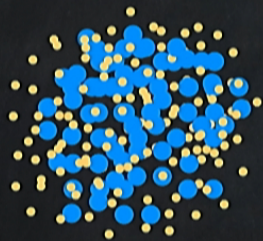
This can be mapped
to an closed FRW
with CDM and
neutrinos evolving as
 $1/a_c^3$



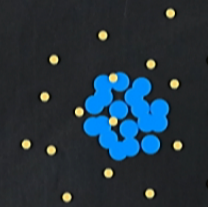
Hu, Chiang, Li, LoVerde 2016

The key point

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This can be mapped
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 $1/a_c^3$



This can be mapped
to closed FRW with
CDM evolving as $1/a_c^3$, but the
neutrinos appear to
dilute faster, and
curvature is not
conserved

Hu, Chiang, Li, LoVerde 2016

The key point

To a local observer, these backgrounds are *inequivalent*



* If CDM is the only thing clustering on small scales, the nonlinear dynamics in both cases can still be described by the local comoving coordinate a_c defined by the dark matter

Hu, Chiang, Li, LoVerde 2016

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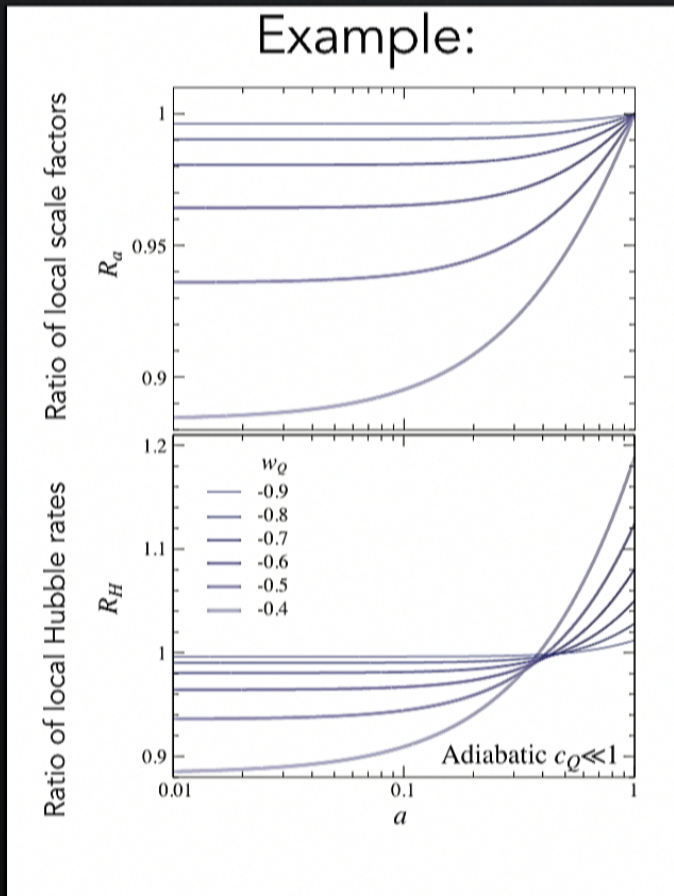
**This gives a *general* formalism for studying bias and mode-coupling with multiple fluids — e.g. massive neutrinos or clustered quintessence

Hu, Chiang, Li, LoVerde 2016

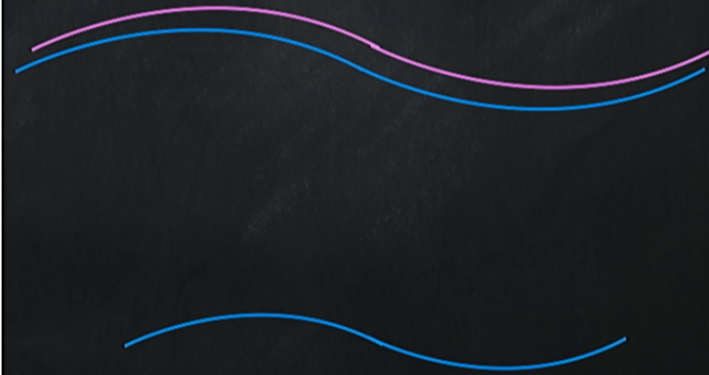
The key point

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Example:



Compare local evolution
for perturbations larger
and smaller than
quintessence Jeans scale

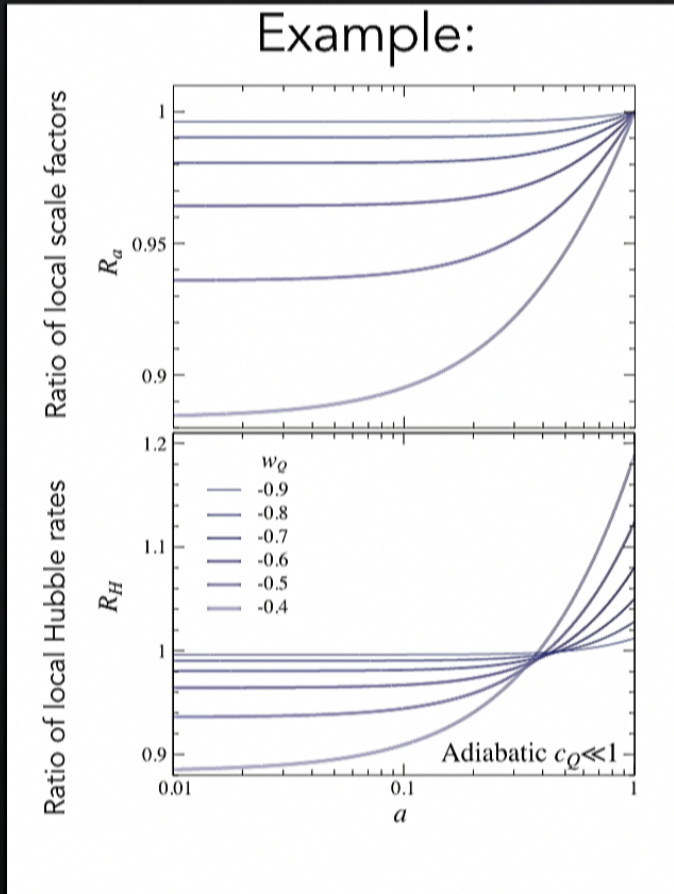


Hu, Chiang, Li, LoVerde 2016

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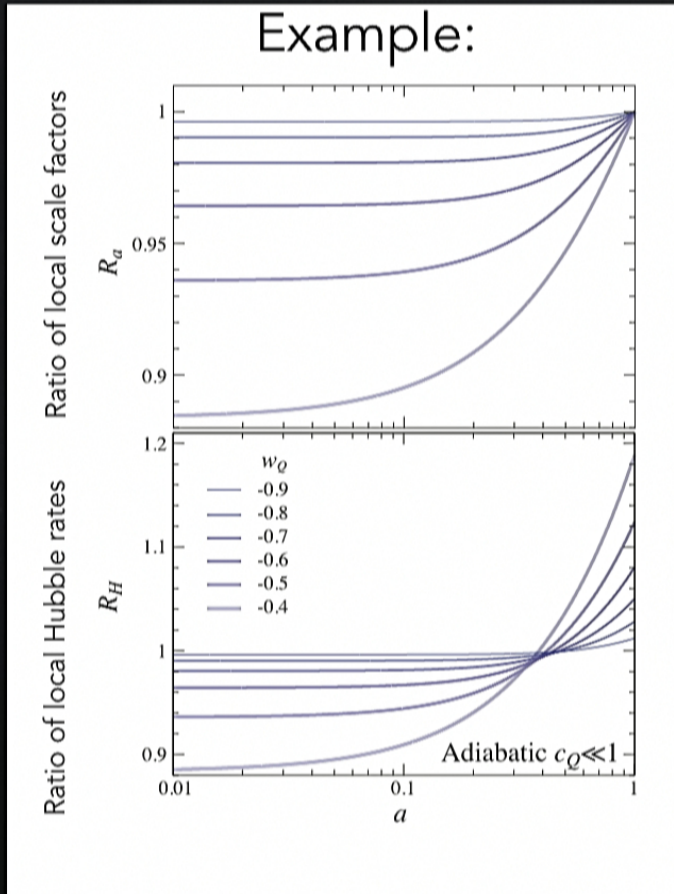
Stay Tuned!

Hu, Chiang, Li, LoVerde 2016

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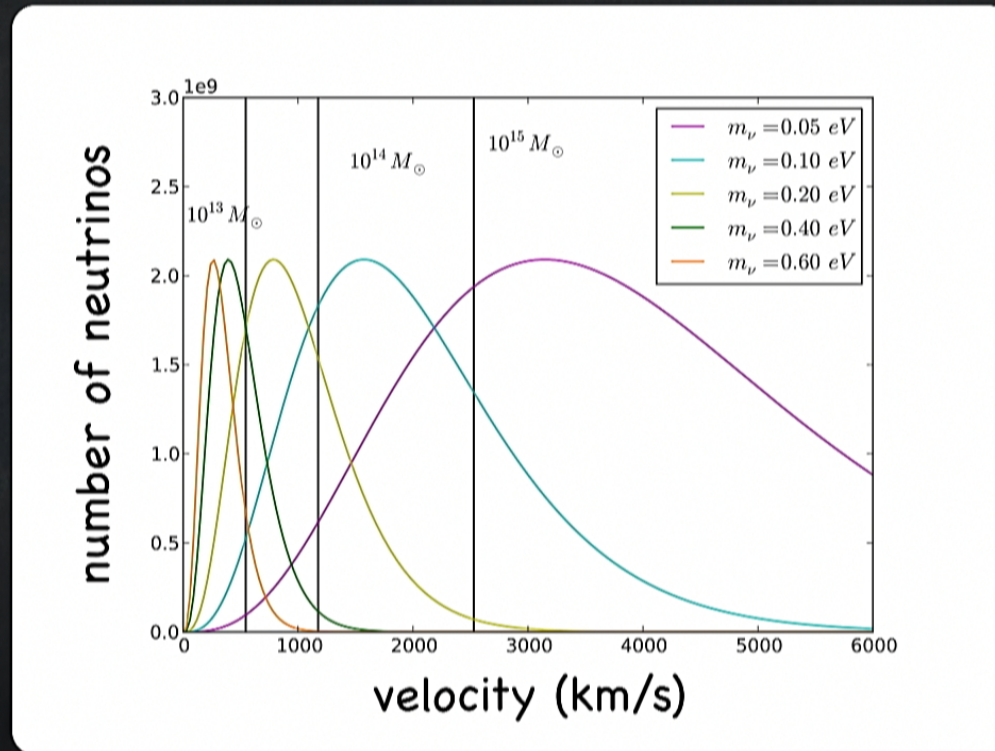
Stay Tuned!

Hu, Chiang, Li, LoVerde 2016

Neutrino Halos

ML & Zaldarriaga 2013

Neutrino Halos

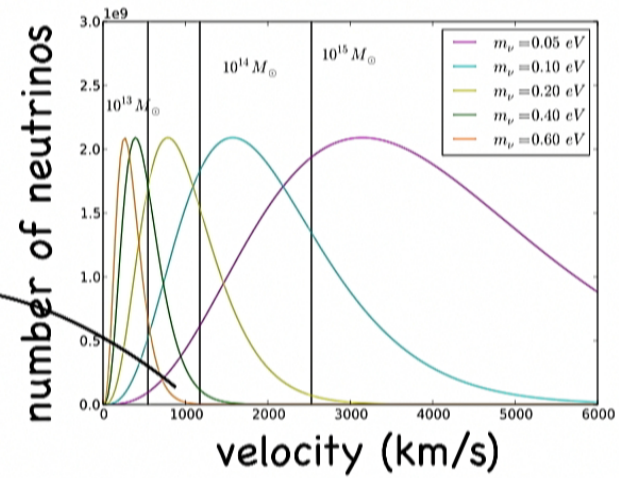
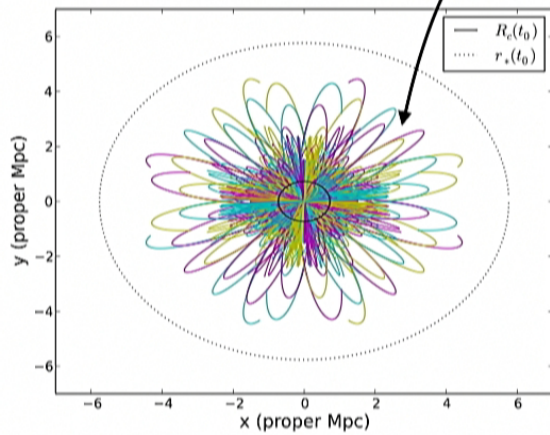


ML & Zaldarriaga 2013

Neutrino Halos

low velocity
neutrinos end
up bound in
halos

shown are $m_\nu = 0.05\text{eV}$ neutrinos
around $M = 10^{14} M_{\text{sun}}$ halo

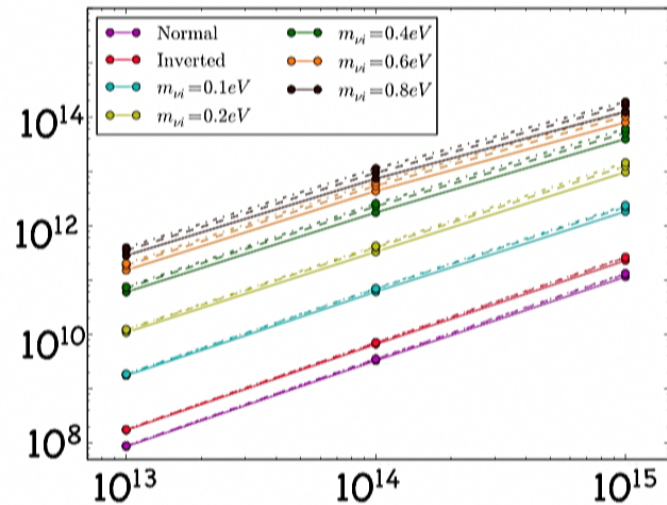


see also Ringwald & Wong 2004; Brandbyge, Hannestad, Haugboelle, Wong 2010
Villaescusa-Navarro, Bird, Pena-Garay, Viel 2013

ML & Zaldarriaga 2013

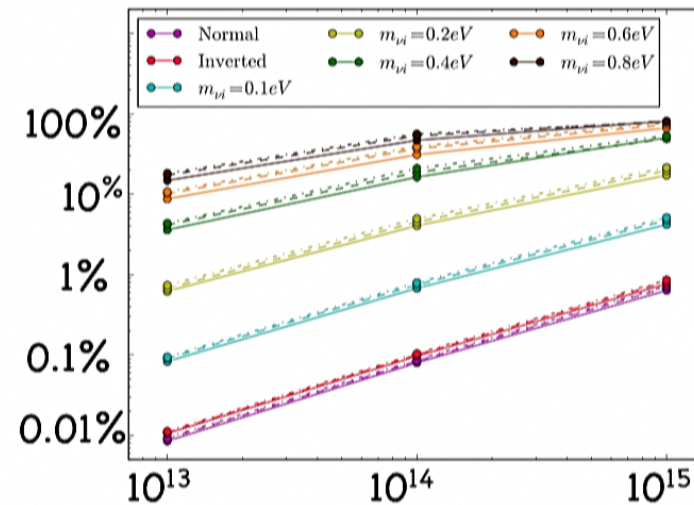
Neutrino Halos

neutrino mass around halo (M_{sun})



halo mass (M_{sun})

fraction that's bound to the halo



halo mass (M_{sun})

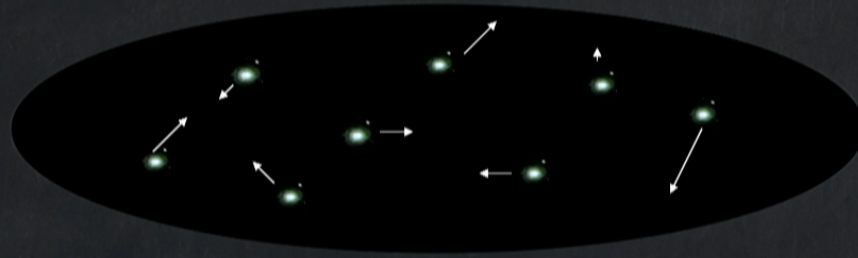
ML & Zaldarriaga 2013

Neutrino Halos - Relative Velocity Effects



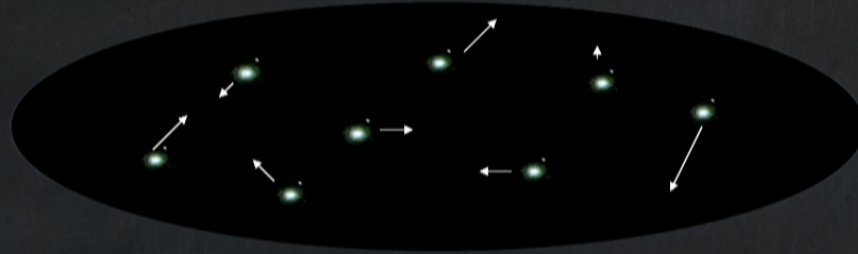
Neutrino Halos - Relative Velocity Effects

Cold dark matter halos are not at rest w.r.t. cosmic frame!



Neutrino Halos - Relative Velocity Effects

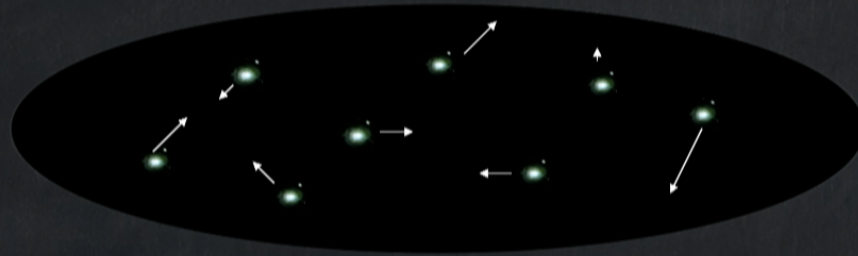
Cold dark matter halos are not at rest w.r.t. cosmic frame!



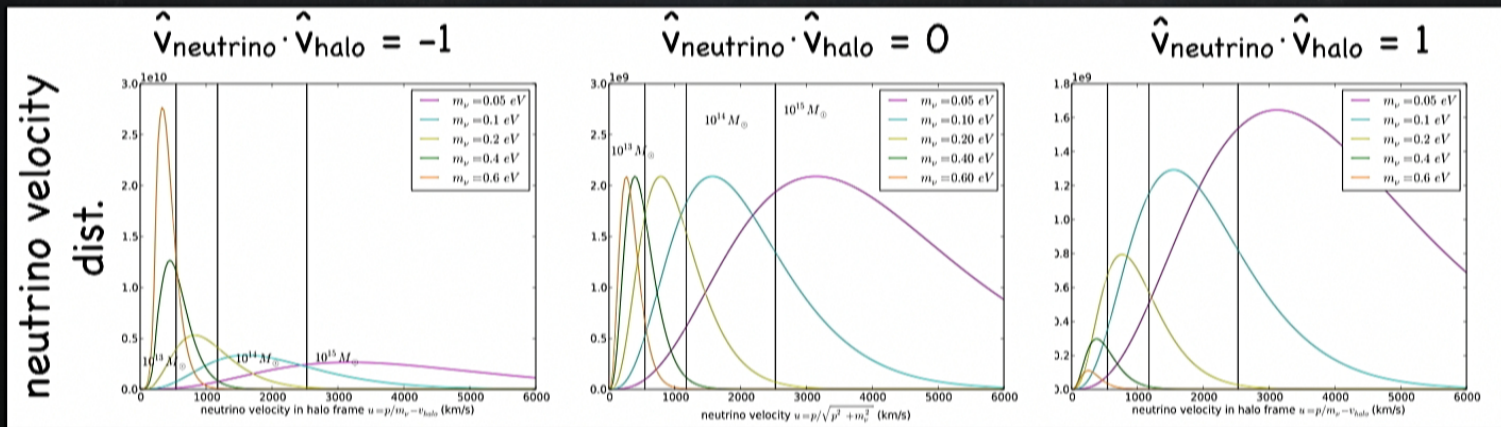
(The Milky Way is moving at ~ 550 km/s w.r.t the CMB)

Neutrino Halos - Relative Velocity Effects

Cold dark matter halos are not at rest w.r.t. cosmic frame!



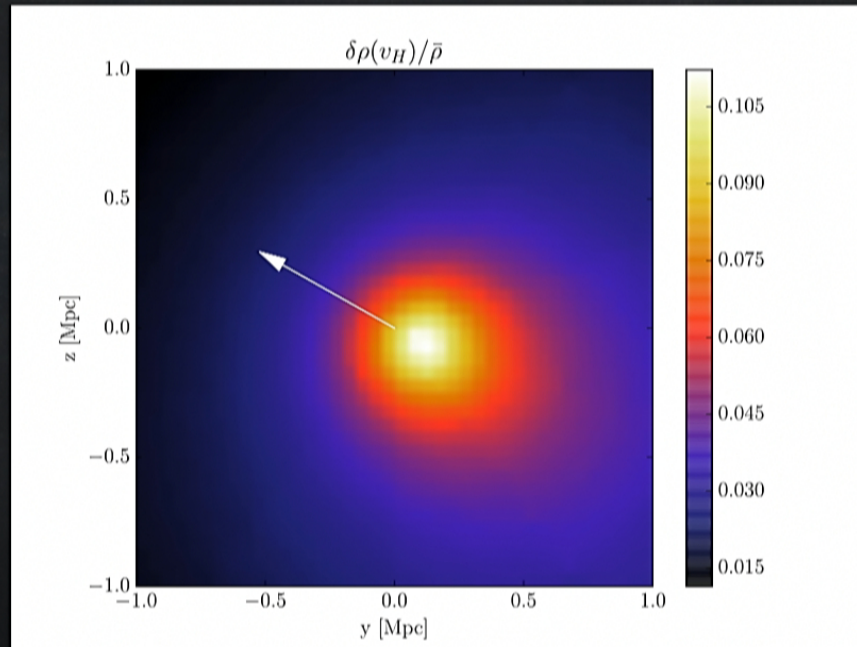
(The Milky Way is moving at ~ 550 km/s w.r.t the CMB)
Halos moving through neutrino "wind"



ML & Zaldarriaga

Neutrino Halos - Relative Velocity Effects

Qualitative difference between how halos acquire CDM and neutrino mass



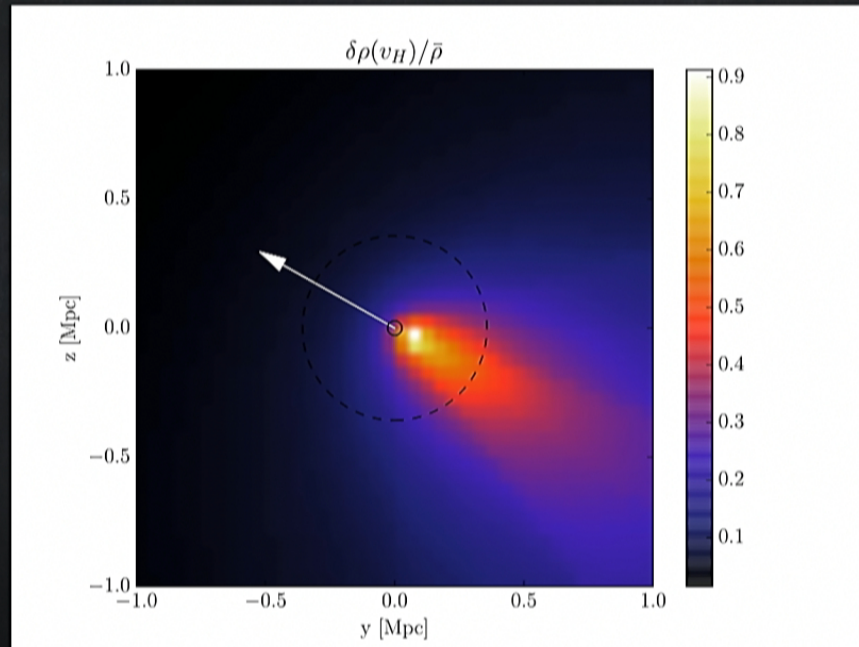
$$M_{\text{halo}} = 10^{12} M_{\text{sun}}; \quad v_{\text{halo}} = v_{\text{milky-way}}; \quad m_{\nu} = 0.1 \text{ eV}$$



work in progress with TY Lin, Ben Safdi

Neutrino Halos - Relative Velocity Effects

Qualitative difference between how halos acquire CDM and neutrino mass



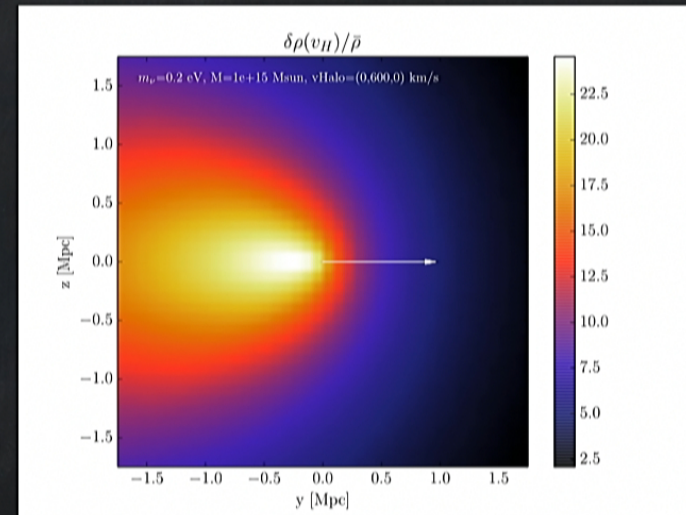
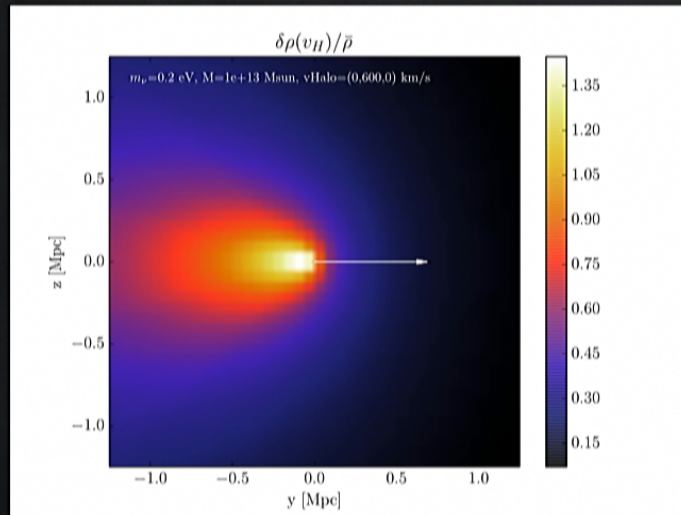
$$M_{\text{halo}} = 10^{12} M_{\text{sun}}; \quad v_{\text{halo}} = v_{\text{milky-way}}; \quad m_{\nu} = 0.3 \text{ eV}$$



work in progress with TY Lin, Ben Safdi

Neutrino Halos - Relative Velocity Effects

Qualitative difference between how halos acquire CDM and neutrino mass



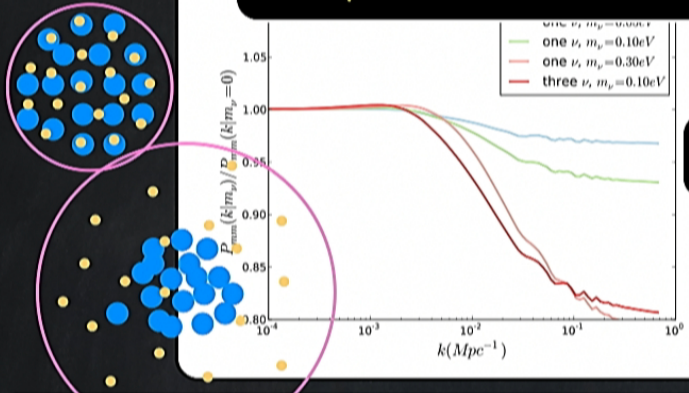
Stay Tuned!



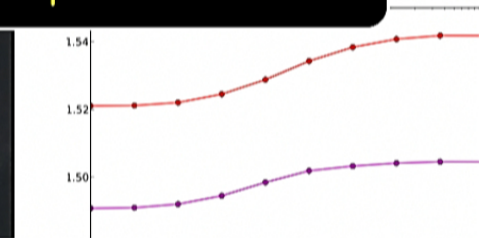
work in progress with TY Lin, Ben Safdi

Summary — Massive Neutrino Effects in Cosmology

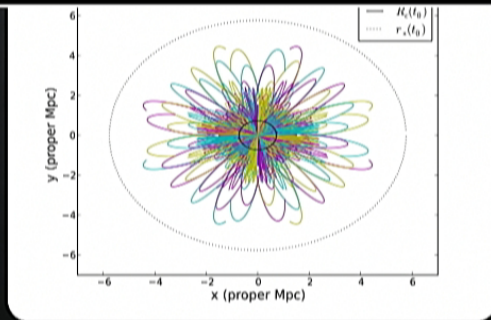
less power in small-scale density fluctuations



scale-dependent halo bias



puffy neutrino halos around CDM halos



Relative velocity effects

