

Title: Growth dynamics and scaling laws across levels of biological organization.

Date: May 16, 2016 11:00 AM

URL: <http://pirsa.org/16050031>

Abstract: <p>Recent findings on quantitative growth patterns have revealed striking generalities across the tree of life, and recurring over distinct levels of organization. Growth-mass relationships in 1) individual growth to maturity, 2) population reproduction, 3) insect colony enlargement and 4) community production across wholeecosystems of very different types, often follow highly robust near  $\hat{\sim}3/4$  scaling laws. These patterns represent some of the most general relations in biology, but the reasons they are so strangely similar across levels of organization remains a mystery. The dynamics of these distinct levels are connected, yet their scaling can be shown to arise independently, and free of system-specific properties. Numerous experiments in prebiotic chemistry have shown that minimal self-replicating systems that undergo template-directed synthesis, typically show reaction orders (ie. growth-mass exponents) between  $\hat{\sim}1/2$  and 1. I will outline how modifications to these simplified reaction schemes can yield growth-mass exponents near  $\hat{\sim}3/4$ , which may offer insight into dynamical connections across hierarchical systems.</p>

# Growth dynamics and scaling laws across levels of organization

Ian Hatton

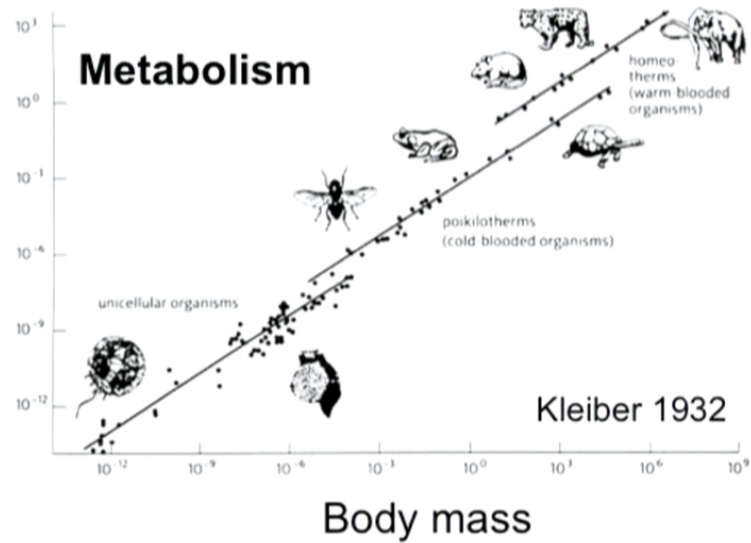
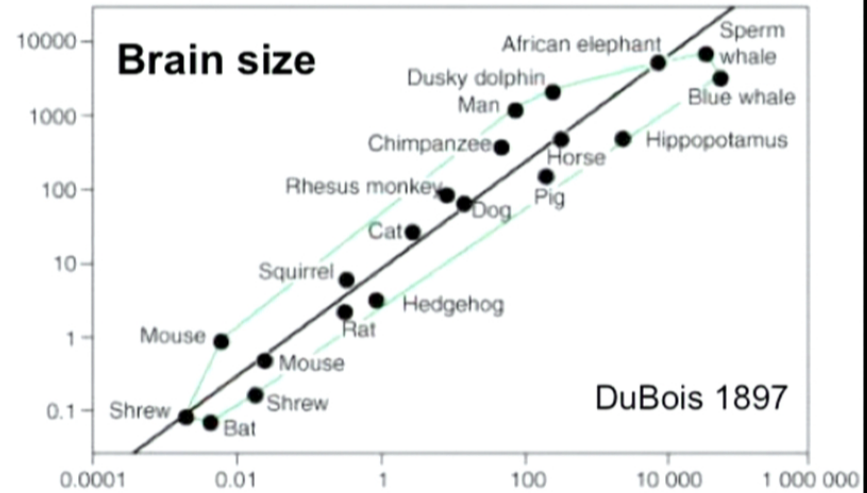
16 May 2016



# Power laws in biology

$$y = c x^k$$

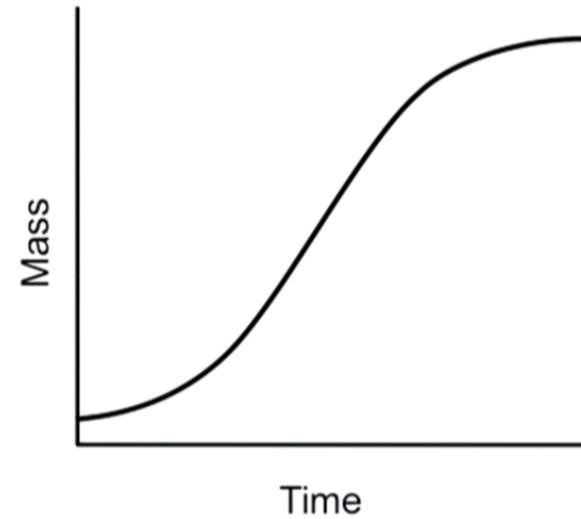
$$\log y = \log c + k \log x$$



# Growth dynamics across levels of organization

Mass may be:

- Bacteria / algae
- Tumor
- Individual body
- Population / colony
- Community



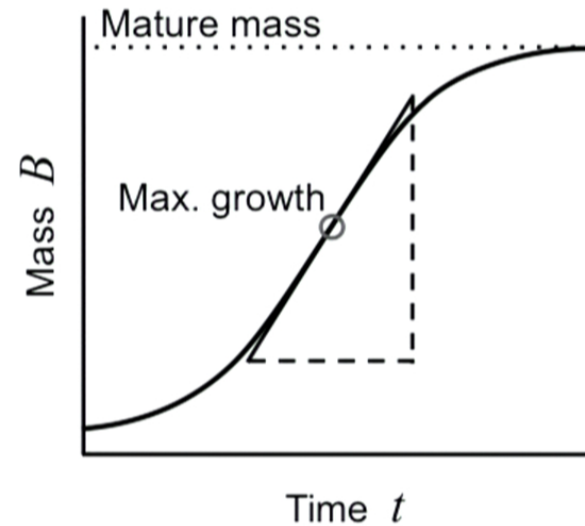
# Growth dynamics across levels of organization

Model may be :

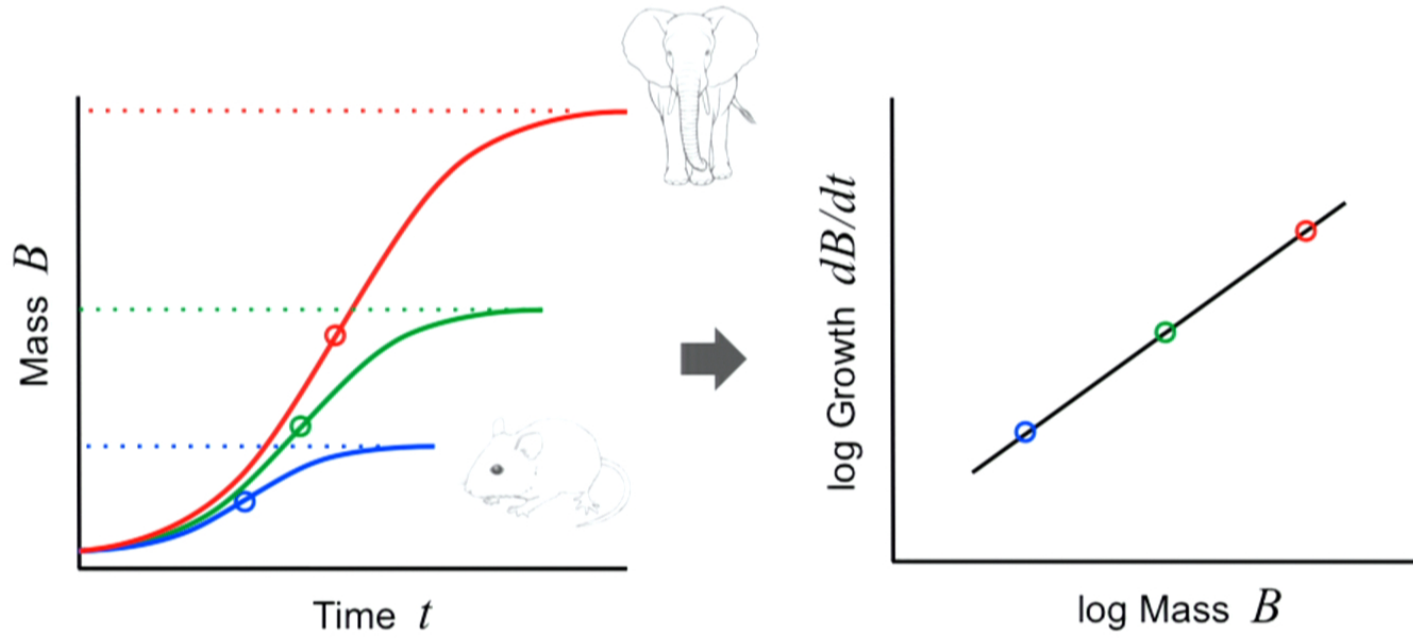
- Logistic 
$$\frac{dB}{dt} = pB \left( 1 - \frac{B}{q} \right)$$

- Gompertz 
$$\frac{dB}{dt} = pB(\ln q - \ln B)$$

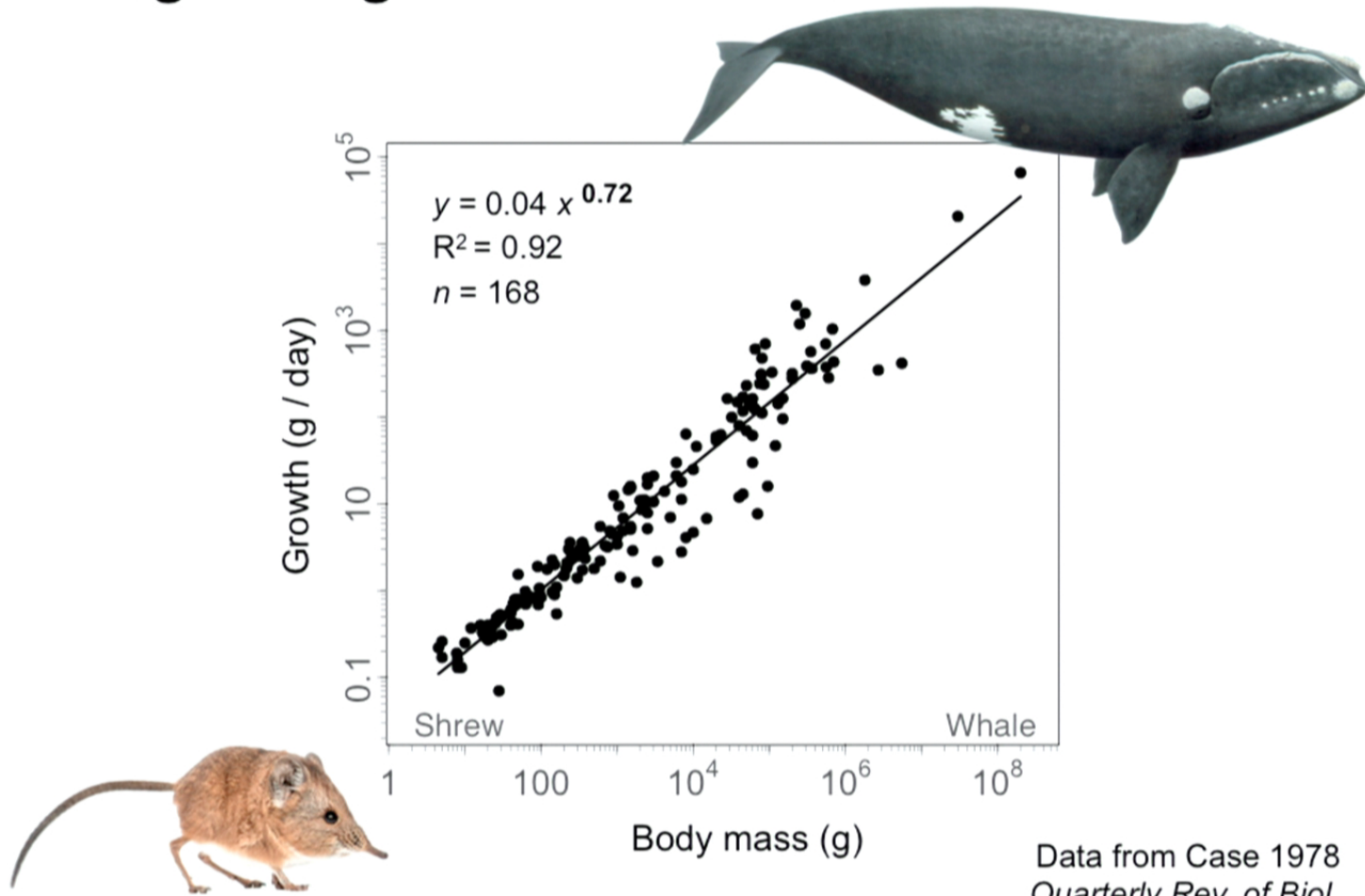
- Bertalanffy 
$$\frac{dB}{dt} = pB^k - qB$$



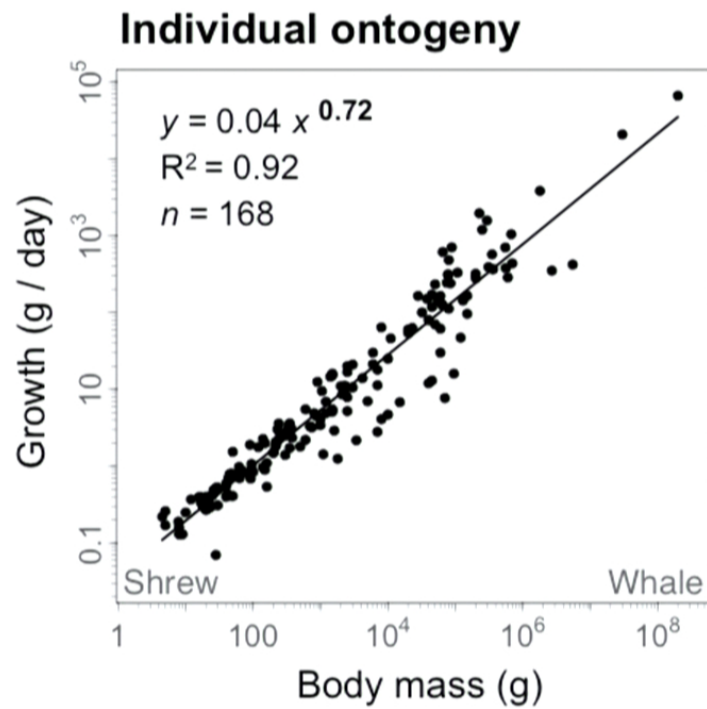
# Growth vs. mass power law



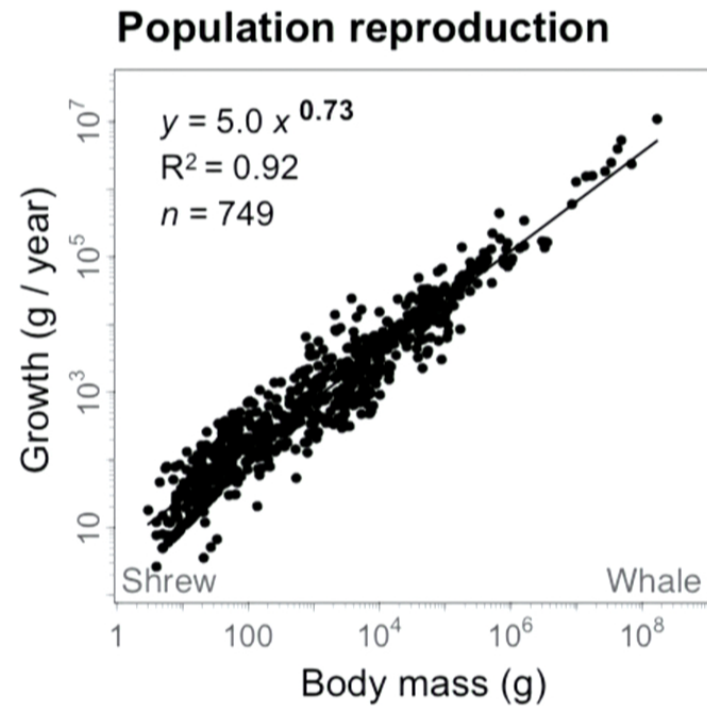
# Ontogenetic growth in mammals



# Growth in mammals



Data from Case 1978  
*Quarterly Rev. of Biol.*

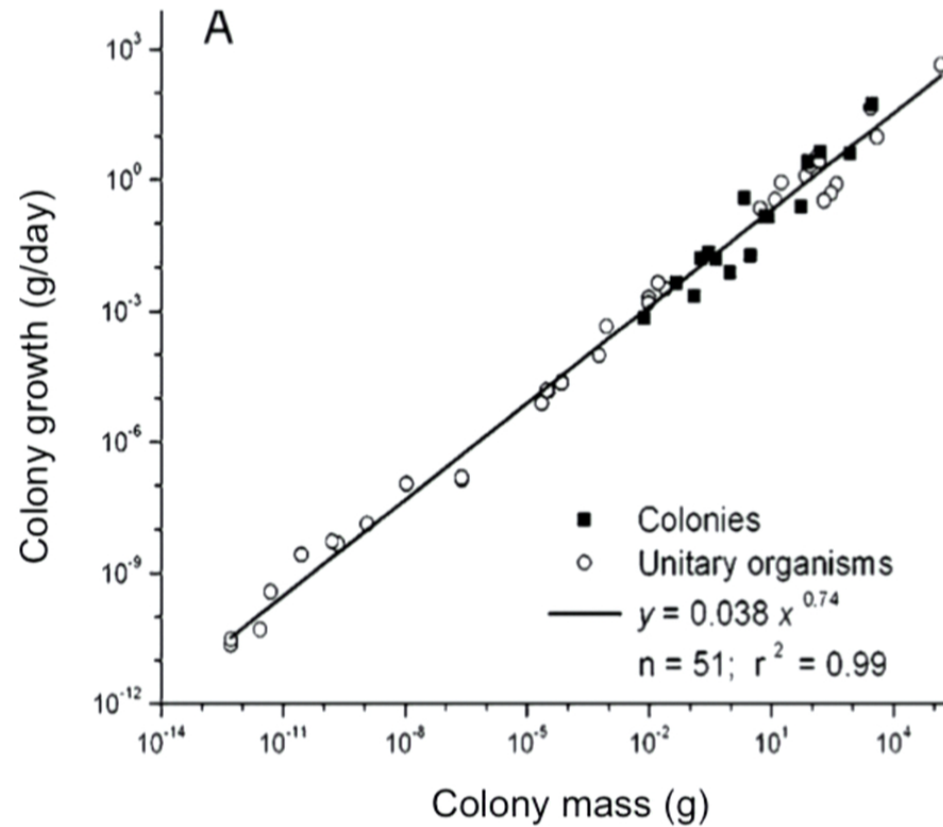


Data from Hatton et. al. 2015  
*Science*





## Social insects colonies



Hou et. al. 2010  
PNAS

## Growth of whole communities

> 1000 peer-reviewed sources from past 50 yrs

> 2000 ecosystems worldwide (mammal, invertebrate, plant and plankton communities)

**RESEARCH ARTICLE**

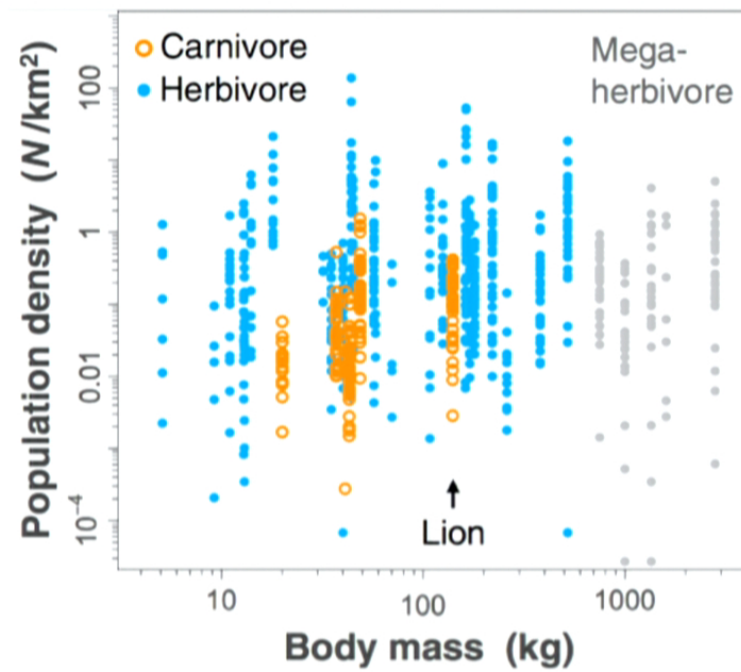
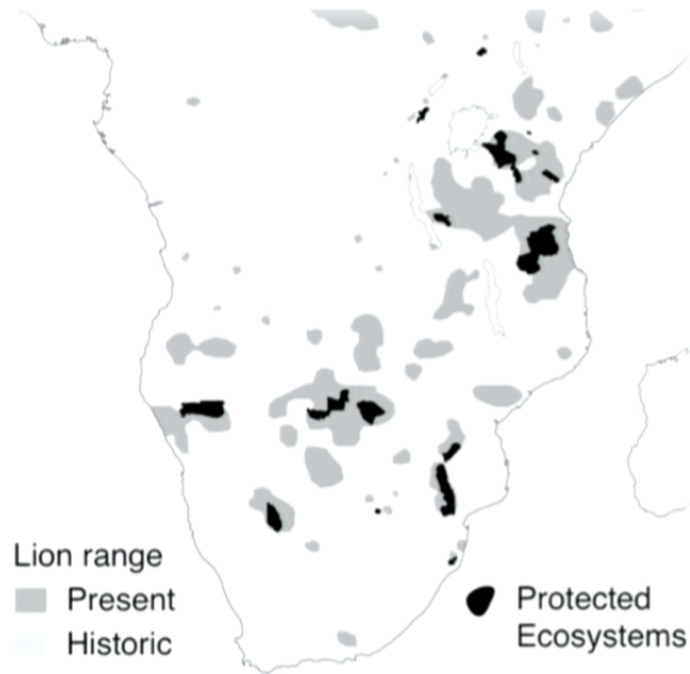
MACROECOLOGY

### **The predator-prey power law: Biomass scaling across terrestrial and aquatic biomes**

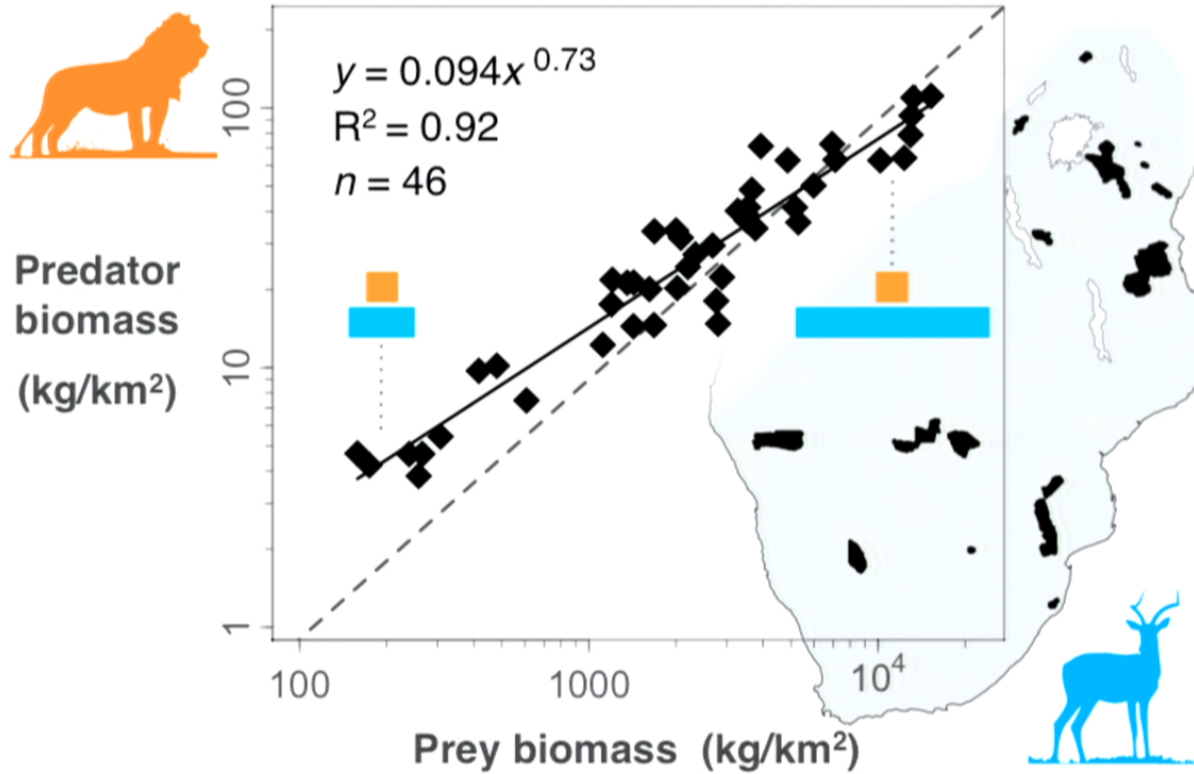
- Collaborators: Kevin McCann, John Fryxell, Jonathan Davies, Matteo Smerlak, Tony Sinclair and Michel Loreau



# Animal abundance is variable in African savanna



# Ecosystem structure changes systematically



# Predator-prey model

Equilibrium Solution:

$$C^* = cB^{*k}$$

Model:

$$\frac{dC}{dt} = gQ - mC$$

$$\frac{dB}{dt} = P - Q$$

Prey production function:

$$P = rB^k$$

Linking structure and function:

$$c = rg/m$$



**Lion range**



**Tiger range**



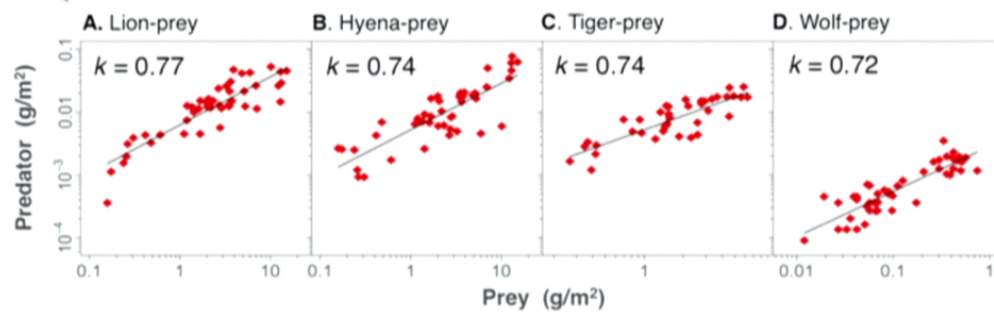


Predator-prey scaling



◆ Top-carnivore biomass vs total herbivore prey biomass

$k = 0.74$  (0.68-0.81),  $n = 184$

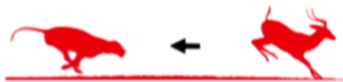


$$C^* = cB^{*k}$$

$$k \approx 3/4$$

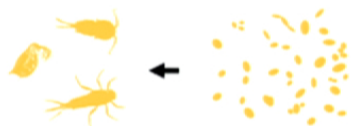


### Predator-prey scaling



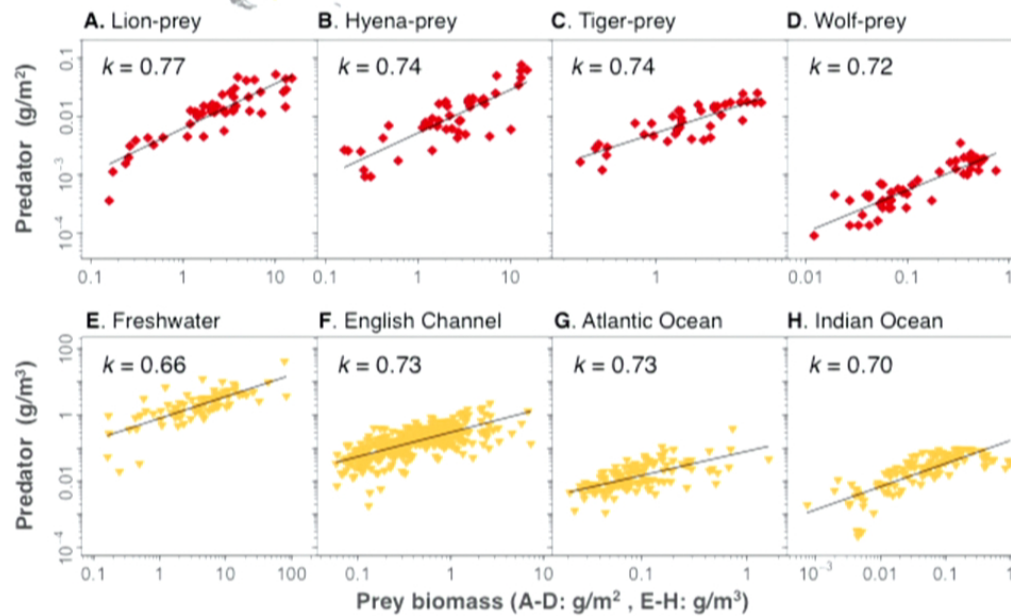
- Top-carnivore biomass vs total herbivore prey biomass

$$k = 0.74 \text{ (0.68, 0.81), } n = 184$$



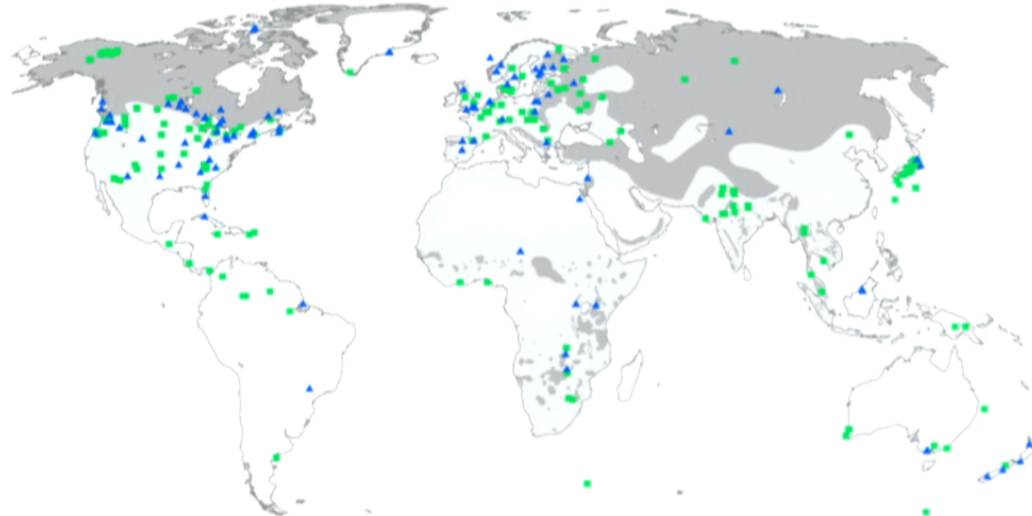
- ▼ Zooplankton biomass vs total algal community biomass

$$k = 0.71 \text{ (0.65, 0.76), } n = 667$$

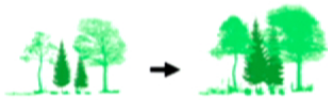


$$P = rB^k$$

$$k \approx 3/4$$

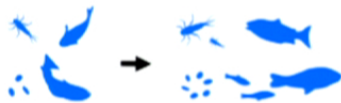


### Production-biomass scaling



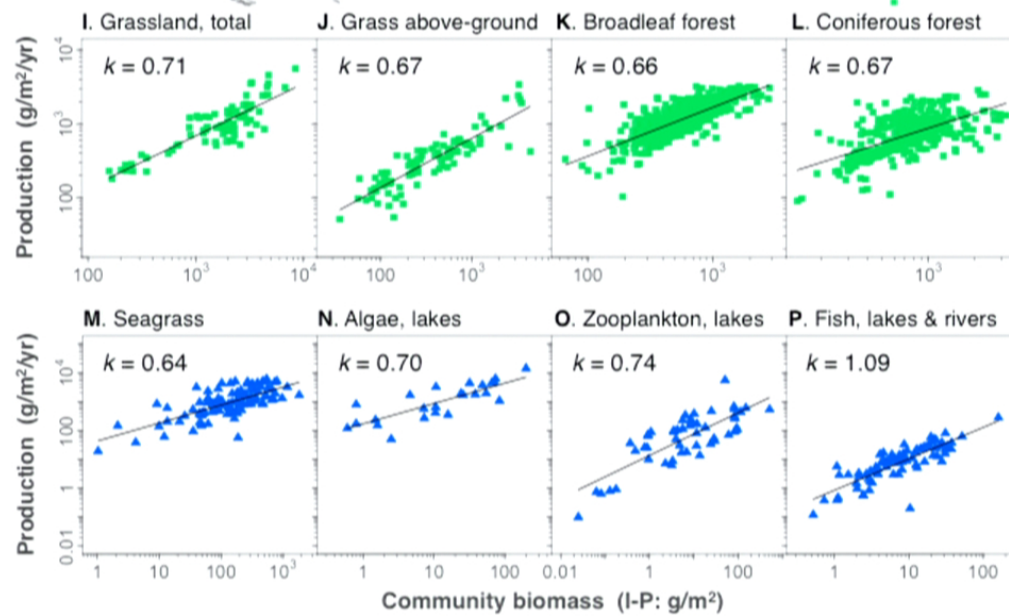
■ Plant community production vs total foliage biomass

$k = 0.67$  (0.64, 0.71),  $n = 1153$



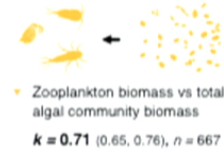
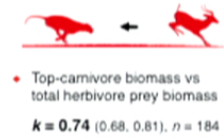
▲ Aquatic trophic community production vs total biomass

$k = 0.76$  (0.68, 0.83),  $n = 256$

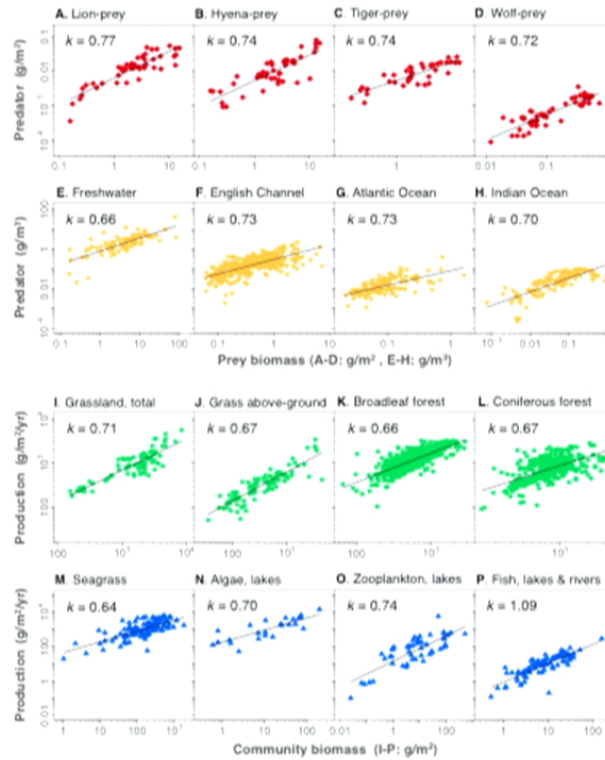
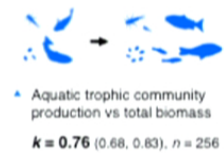
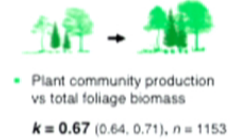




Predator-prey scaling

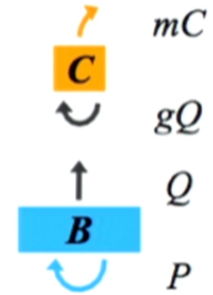


Production-biomass scaling



$$\frac{dC}{dt} = gQ - mC$$

$$\frac{dB}{dt} = P - Q$$

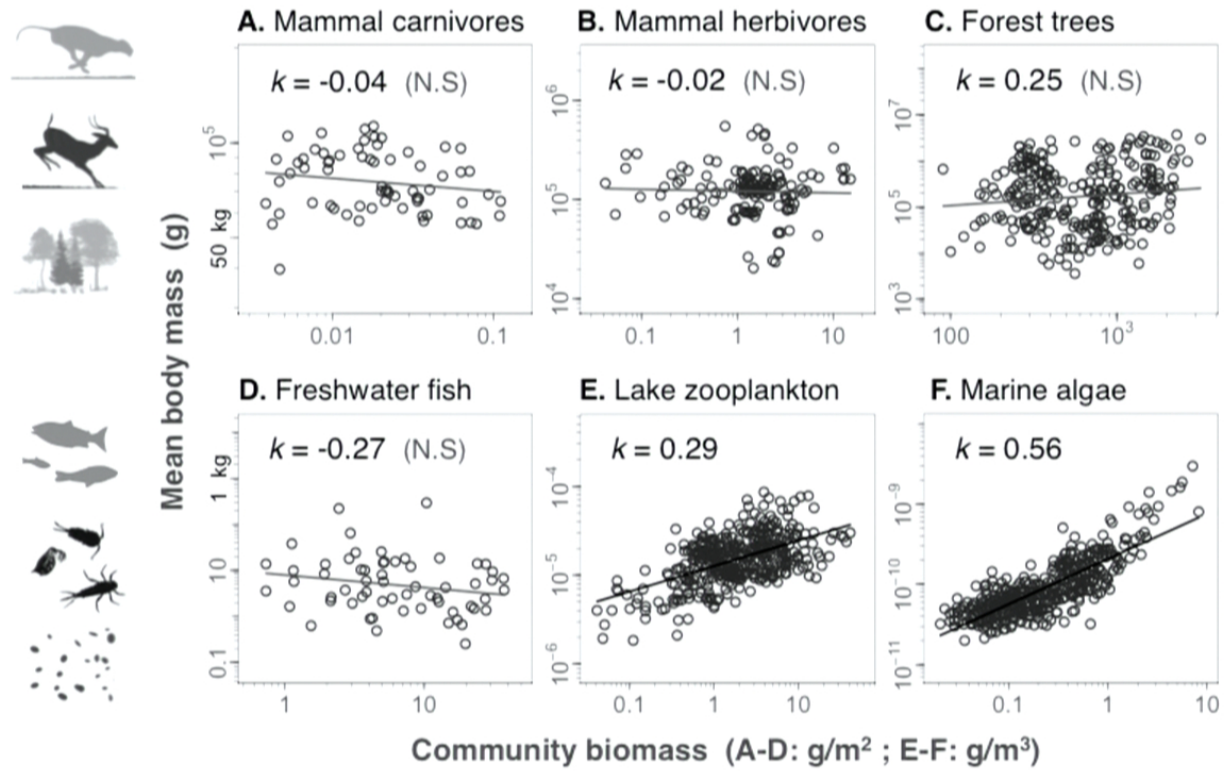


$$C^* = cB^{*k}$$

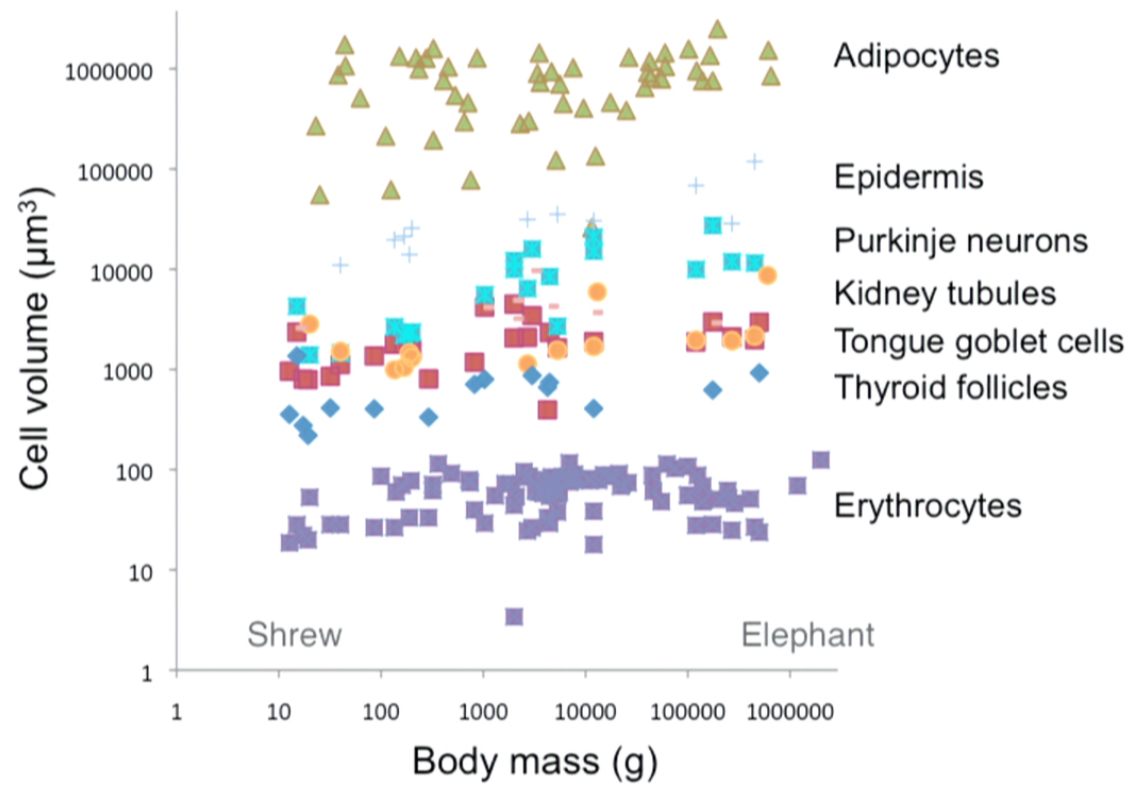
$$c = rg/m$$

$$\frac{dB}{dt} = rB^k$$

# These patterns arise independently



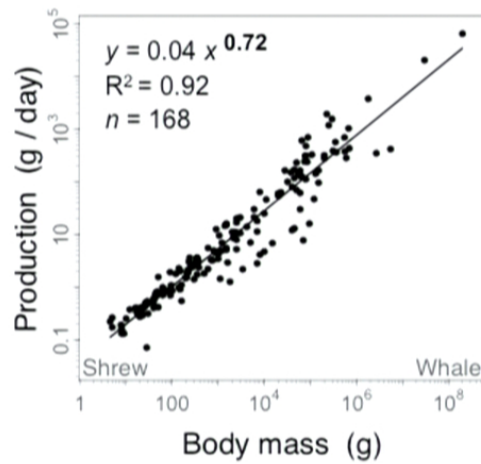
# Cells are also size-invariant



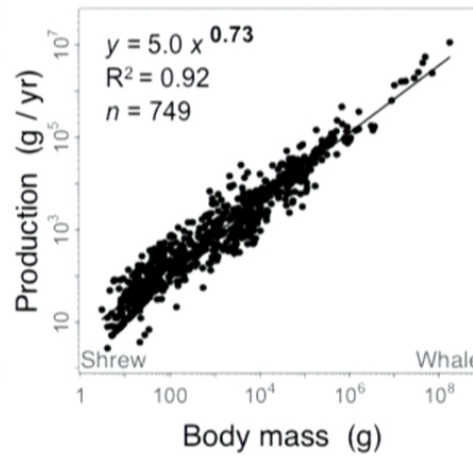
Data from Savage *et. al.* 2007  
PNAS

# Mammal growth across levels of organization

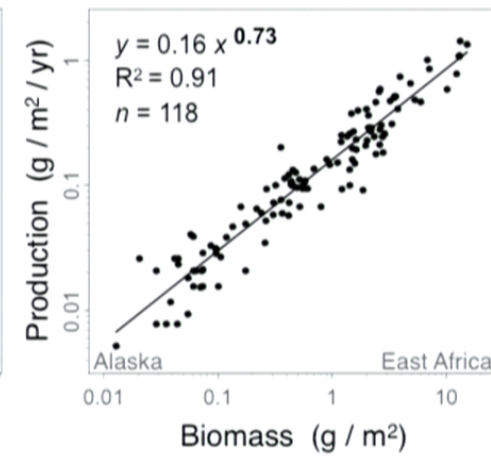
Individual somatic growth



Population reproduction

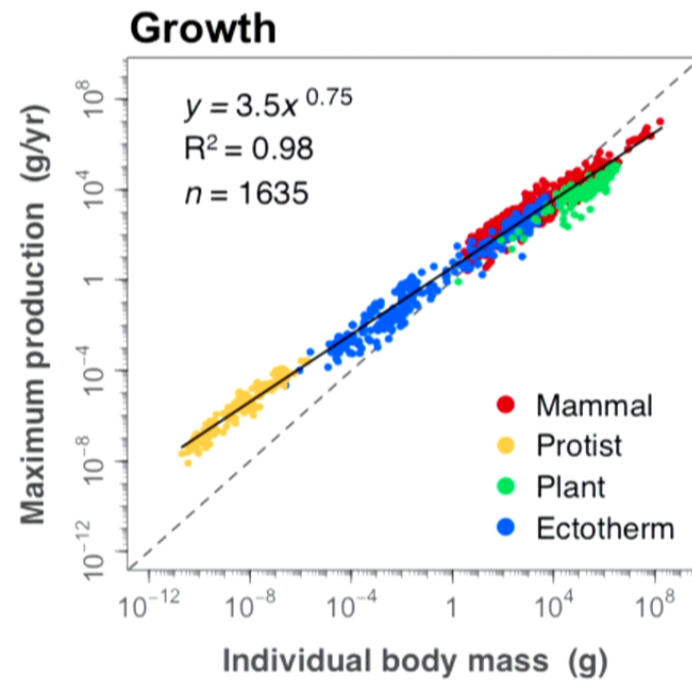
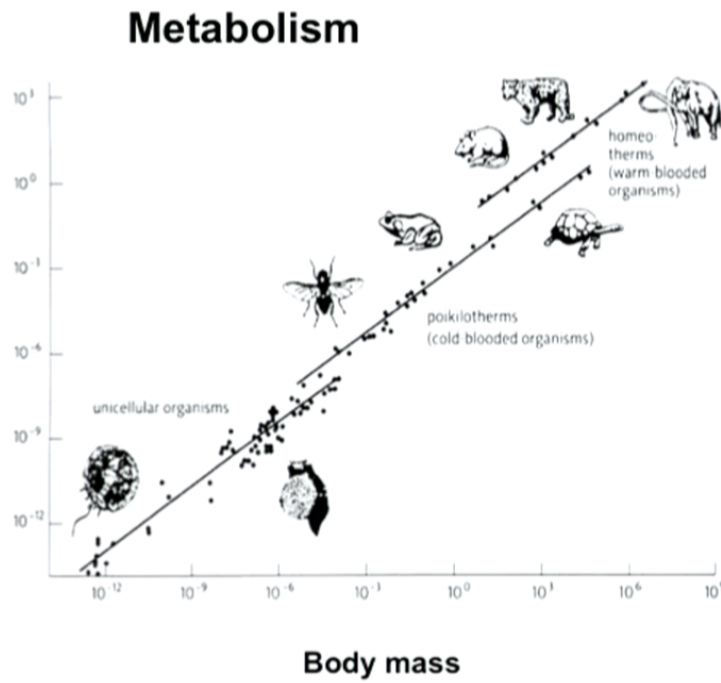


Community production



# The cart before the horse?

Do energetic constraints limit growth, or did energy supply evolve to fuel growth most efficiently?



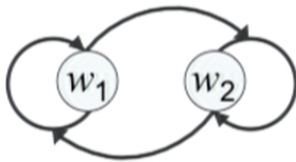


# Classic self-replication



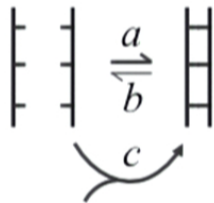
Exponential growth  $k=1$

$$\frac{dB}{dt} = rB$$



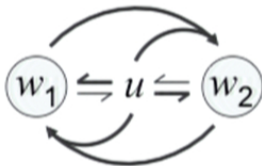
Hypercyclic growth  $k=2$

$$\frac{dB}{dt} = rB^2$$



Template formation  $k=1/2$

$$\frac{dB}{dt} = rB^{1/2}$$



Other schemes?

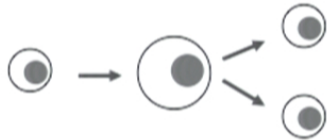
$$\frac{\overset{\circ\circ}{M}}{\overset{\circ}{M}} = K \frac{\overset{\circ}{M}}{M}$$

$$K = \frac{\overset{\circ}{M} / \overset{\circ}{M}}{\overset{\circ}{M} / M}$$

## Likely ingredients for theory



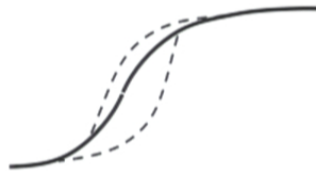
Replicators are size invariant



Continuous and discrete dynamics

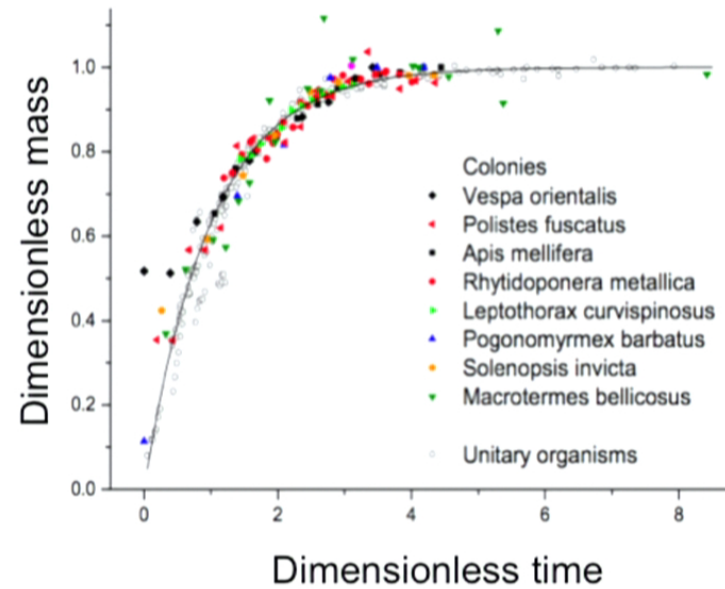
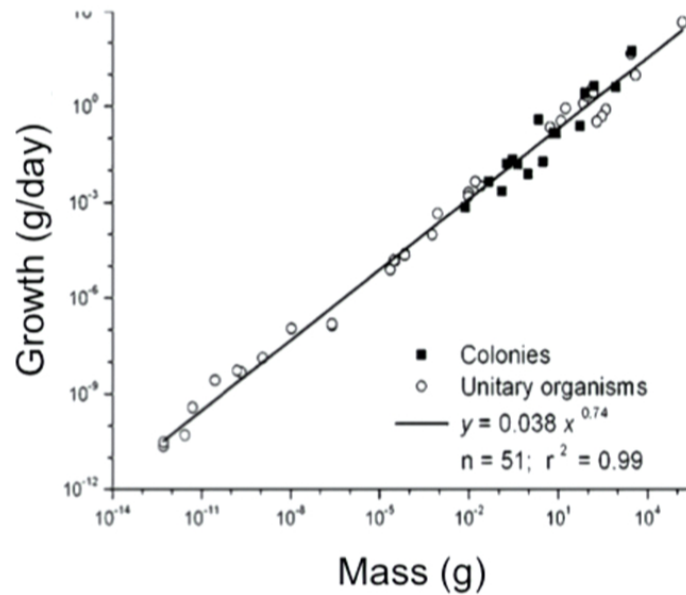


Promoter and inhibitor signals



Negative feedbacks

# Social insects – individuals and whole colonies



Hou et. al. 2010  
PNAS