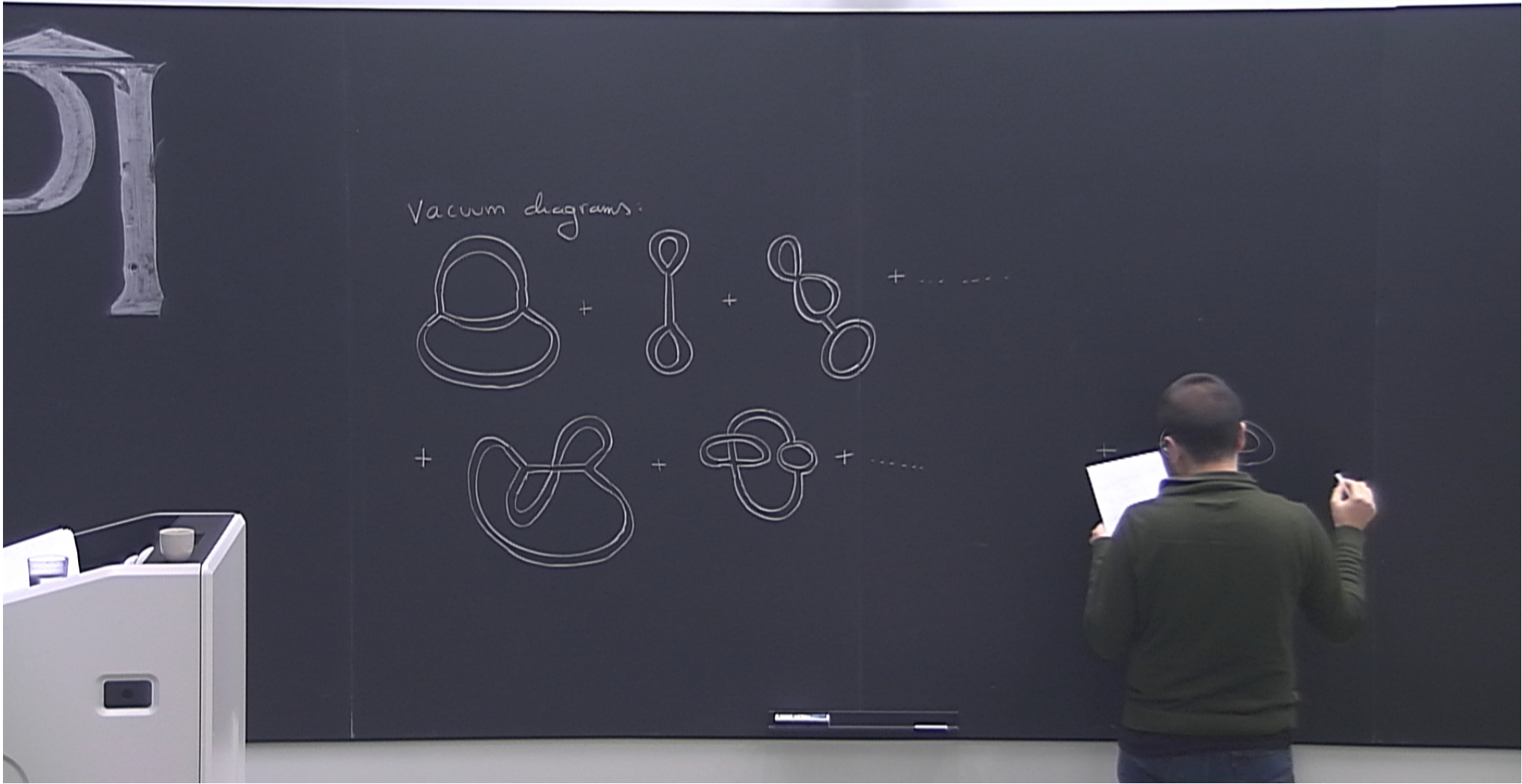


Title: PSI 2015/2016 Explorations in String Theory - Pedro Vieira - 2

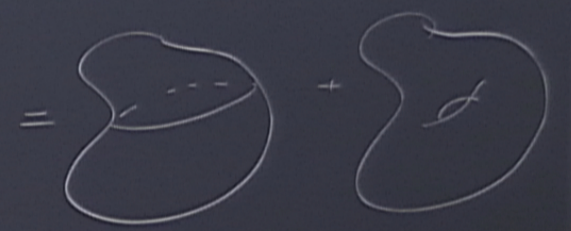
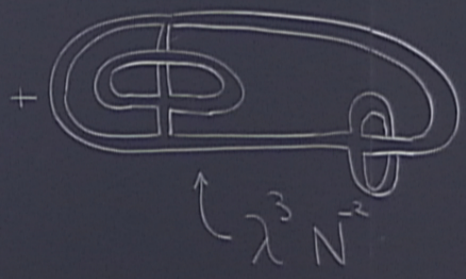
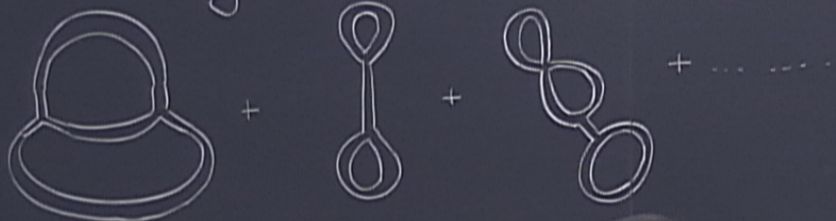
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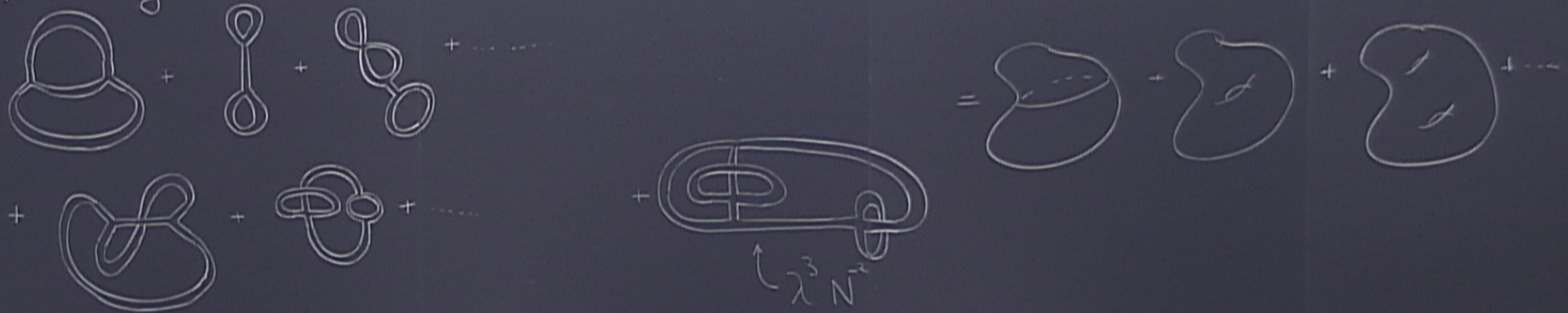
Abstract:



Vacuum diagrams:



Vacuum diagrams:



$$\text{String } S\text{-matrix} = g_s \text{ (sphere) } + g_s^3 \text{ (torus) } + \dots = \sum_{\text{genus } g} (g_s)^{2g-2+n} \int \mathcal{D}X \exp(-\text{Tension } S[X]) V_1 V_2 V_n$$

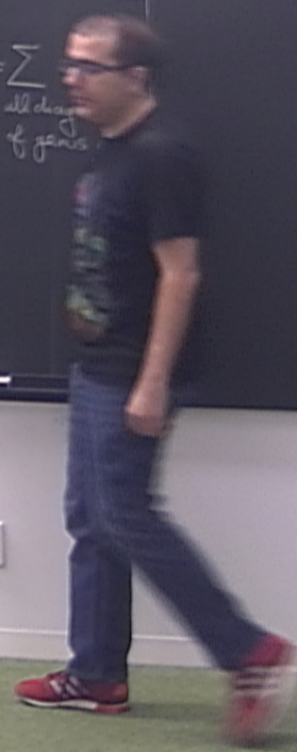
Sixfermer
of genus g

$$\langle \text{Tr } \Phi(x_1)^{\vec{J}_1} \text{Tr } \Phi(x_2)^{\vec{J}_2} \text{Tr } \Phi(x_3)^{\vec{J}_3} \rangle = \underbrace{\text{ (diagram) } }_{\mathcal{U}(x_3)} \left(\frac{1}{N} \right)^{2g-2+n} \left[\mathcal{F}_g(\lambda) = \sum_{\text{all diagrams of genus } g} \right]$$

$$\text{String S-matrix} = g_s \text{ (disk)} + g_s^3 \text{ (pair of pants)} + \dots = \sum_{\text{genus } g} (g_s)^{2g-2+n} \int \mathcal{D}X \exp(-\text{Tension } S[X]) V_1 V_2 V_n$$

Surface of genus g

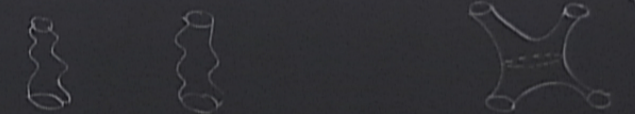
$$\langle \text{Tr } \Phi(x_1)^{\vec{J}_1} \text{Tr } \Phi(x_2)^{\vec{J}_2} \text{Tr } \Phi(x_3)^{\vec{J}_3} \rangle = \text{ (diagrams)} + \dots = \sum_{\text{genus } g} \left(\frac{1}{N} \right)^{2g-2+n} \left[\mathcal{F}_g(\lambda) = \sum_{\text{all diagrams of genus } g} \dots \right]$$



* planar 2π function in N ind. , planar 3π = $\mathcal{O}(1/N \equiv g_s)$

* planar 2π function is N ind. , planar 3π = $\mathcal{O}(1/N \equiv g_s)$

* $\langle 0000 \rangle = \sum \langle 00 \rangle \langle 00 \rangle + \langle 0000 \rangle_{\text{connected}}$

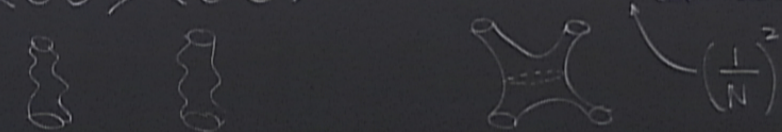


large N

$(\frac{1}{N})^2$

* planar 2pt function in N ind. , planar 3pt = $\mathcal{O}(\frac{1}{N} \equiv g_s)$

* $\langle \text{oooo} \rangle = \sum \langle \text{oo} \rangle \langle \text{oo} \rangle + \langle \text{oooo} \rangle_{\text{connected}}$



large $N \rightsquigarrow$ free strings

* planar 2pt function in N ind. , planar 3pt = $\mathcal{O}(\frac{1}{N} \equiv g_s)$

* $\langle \text{oooo} \rangle = \sum \langle \text{oo} \rangle \langle \text{oo} \rangle + \langle \text{oooo} \rangle_{\text{connected}} + \text{large } N \sim \text{free strings}$

$(\frac{1}{N})^2$

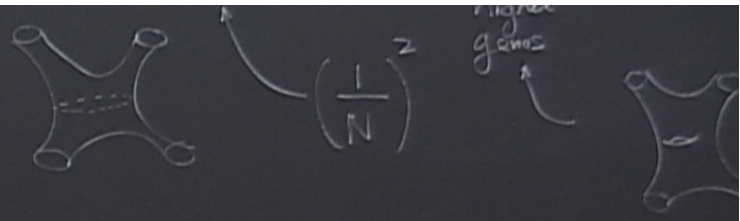
higher genus

$\frac{1}{N^4}$

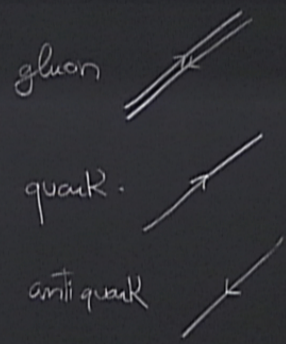
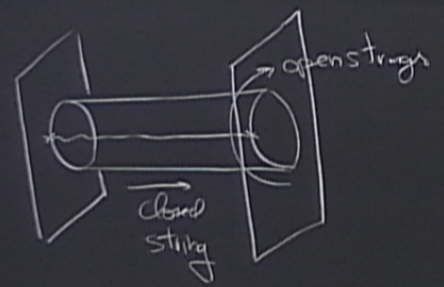
$$\mathcal{O} \equiv \text{tr } \Phi^J \leftrightarrow \text{single closed string}$$

$$\tilde{\mathcal{O}} = \prod_{i=1}^n \text{tr } \Phi^{J_i}(x)$$

$$\langle \tilde{\mathcal{O}}(x) \tilde{\mathcal{O}}(y) \rangle \approx \prod_{i=1}^n \langle \mathcal{O}_i(x) \mathcal{O}_i(y) \rangle \stackrel{\text{CFT}}{\approx} \frac{1}{(x-y)^{2\sum \Delta_i}}$$



Open vs Closed



$$1) \left\langle \underbrace{\text{tr } F^2}_{\text{composite gauge inv. ops.}} \text{tr } F^2 \right\rangle$$

Composite gauge inv. ops.

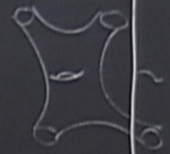
$$A \rightarrow \Omega A \Omega^{-1} + \Omega d \Omega^{-1}$$

$$F \text{ is better, } F \rightarrow \Omega F \Omega^{-1}, \text{tr } F^2$$

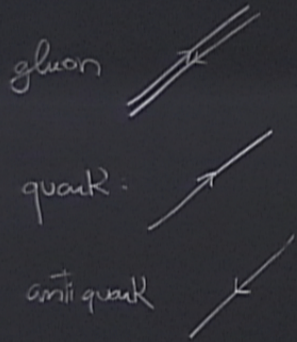


$$\left(\frac{1}{N}\right)^2$$

higher
genus



$$\frac{1}{N^4}$$



$$1) \left\langle \underbrace{\text{tr } F^2}_{\text{Composite gauge inv. ops.}} \text{tr } F^2 \right\rangle$$

Composite gauge inv. ops.

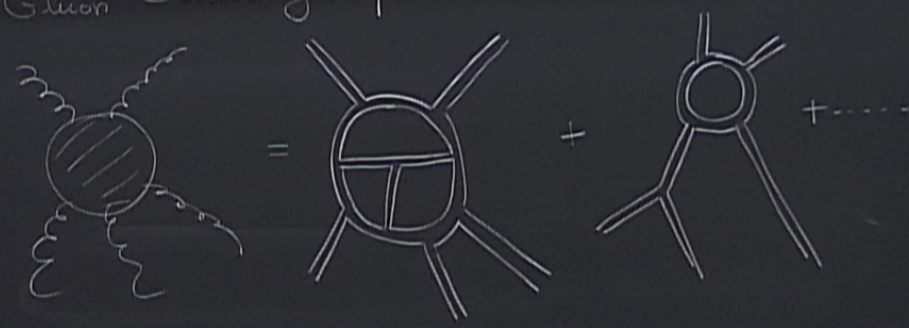
$$A \rightarrow \Omega A \Omega^{-1} + \Omega d \Omega^{-1}$$

$$F \text{ is better, } F \rightarrow \Omega F \Omega^{-1}, \text{tr } F^n \text{ is perfect.}$$

$$\langle \tilde{O}(x) \tilde{O}(y) \rangle \approx \prod_{i=1}^n \langle O_i(x) O_i(y) \rangle \approx \frac{1}{(x-y)^{2\sum \Delta_i}}$$

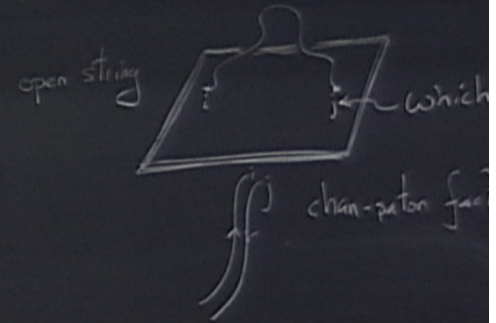
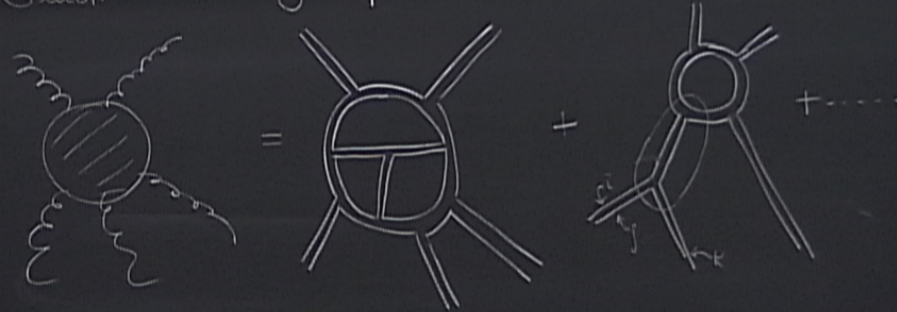
multi-string

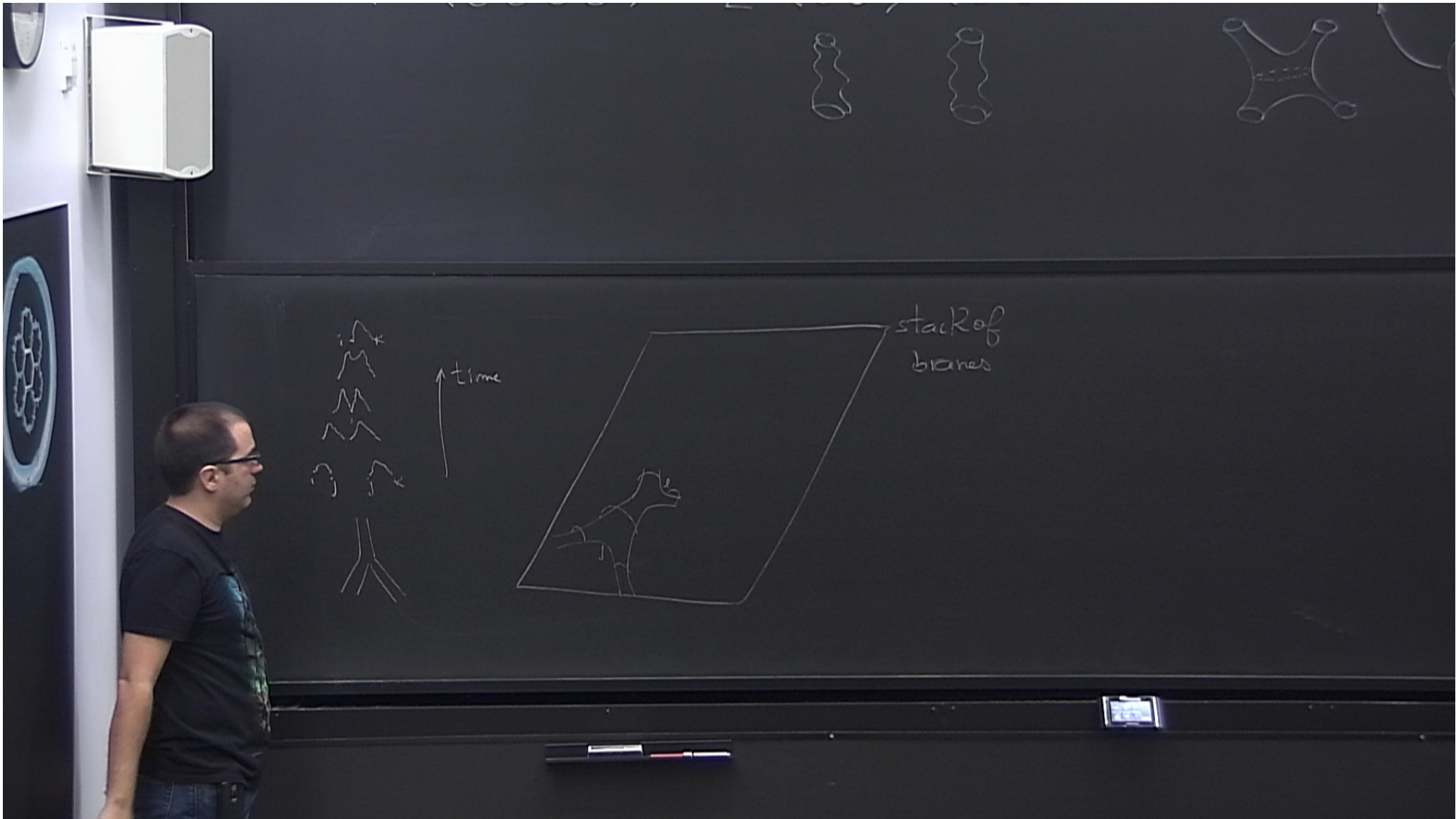
⇒ Gluon Scattering amplitudes

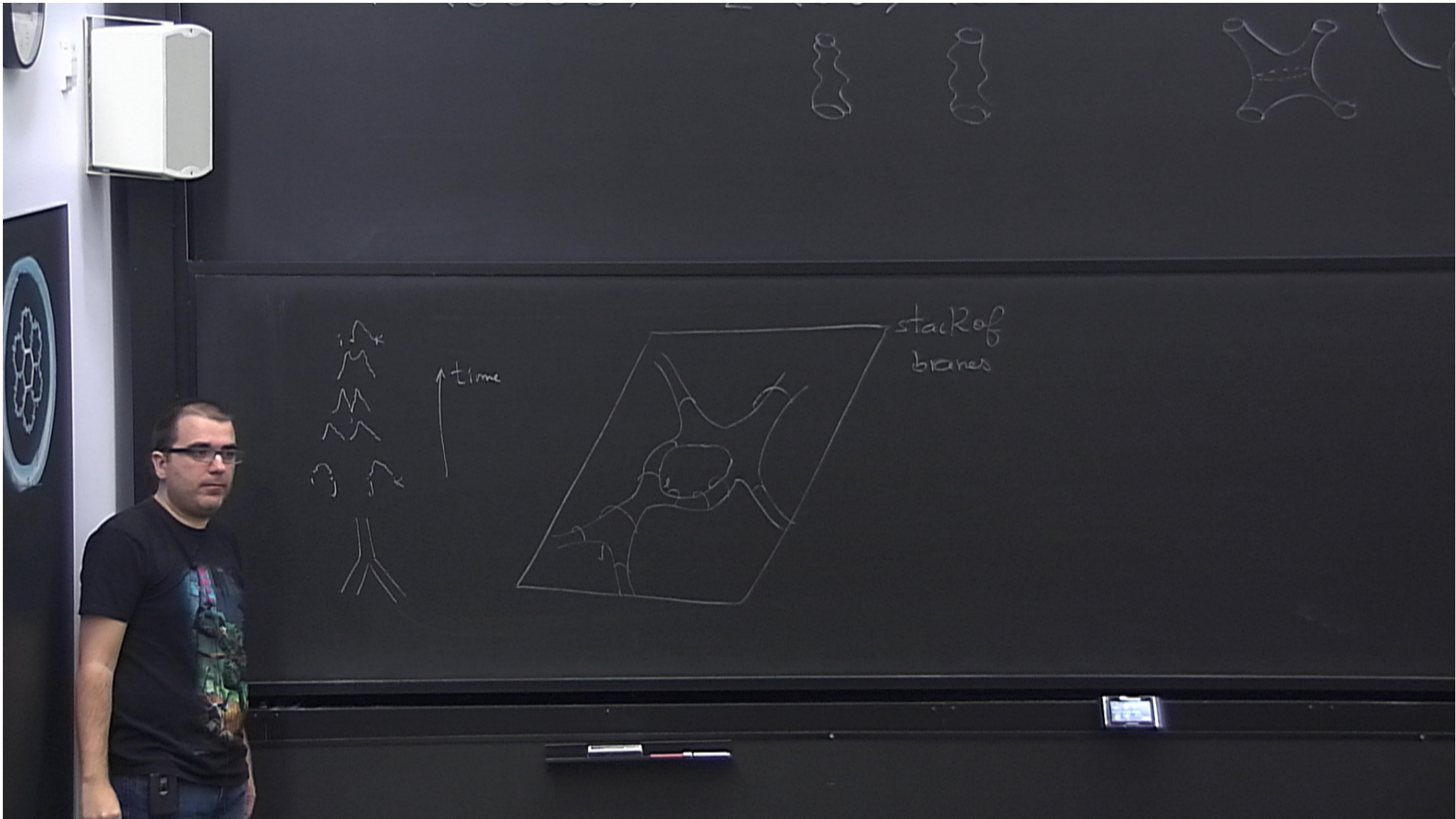


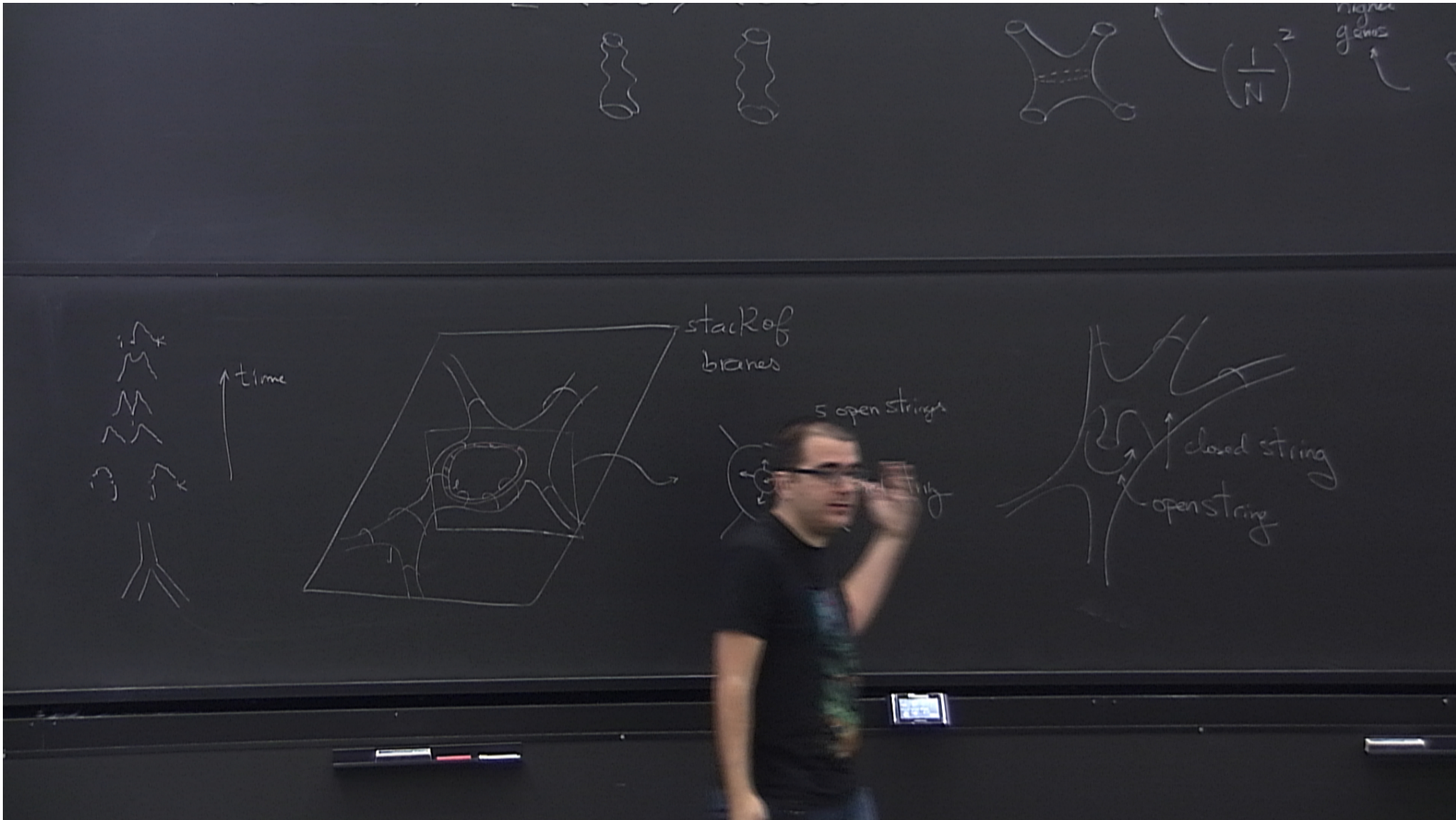
$$\langle \tilde{O}(x) \tilde{O}(y) \rangle \approx \prod_{i=1}^n \langle O_i(x) O_i(y) \rangle \approx \frac{1}{(x-y)^{2\sum \Delta_i}}$$

⇒ Gluon Scattering amplitudes











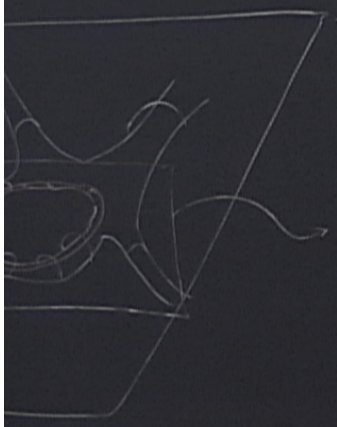
$$\left(\frac{1}{N}\right)^2$$

higher
genus

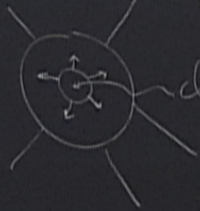


$$\frac{1}{N^4}$$

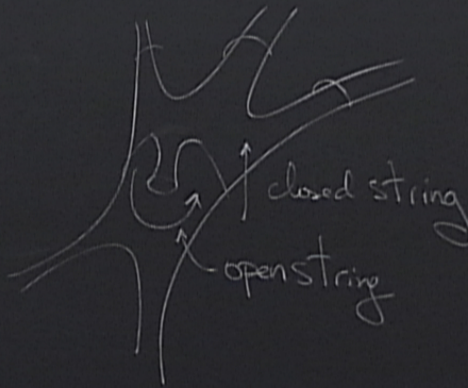
stack of
branes



5 open strings

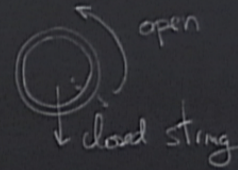


closed string



closed string

open string



open

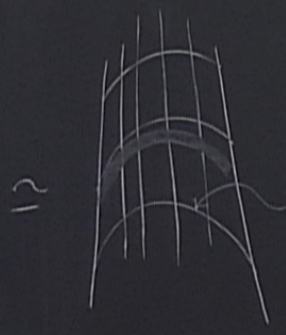
closed string

3) $g \bar{g}$ potential



multi-string too

$$\langle \tilde{O}(x) \tilde{O}(y) \rangle \approx \prod_{i=1}^n \langle O_i(x) O_i(y) \rangle \approx \frac{1}{(x-y)^{2\sum \Delta_i}}$$



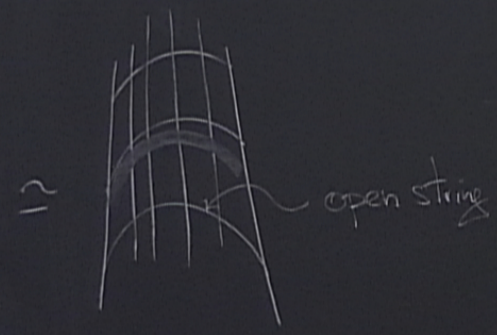
open string

$$\int \mathcal{D}X \approx e^{-S_{\min} T} \text{ for } T \gg 1$$

easy for $T \gg 1$
($\lambda \gg T$)

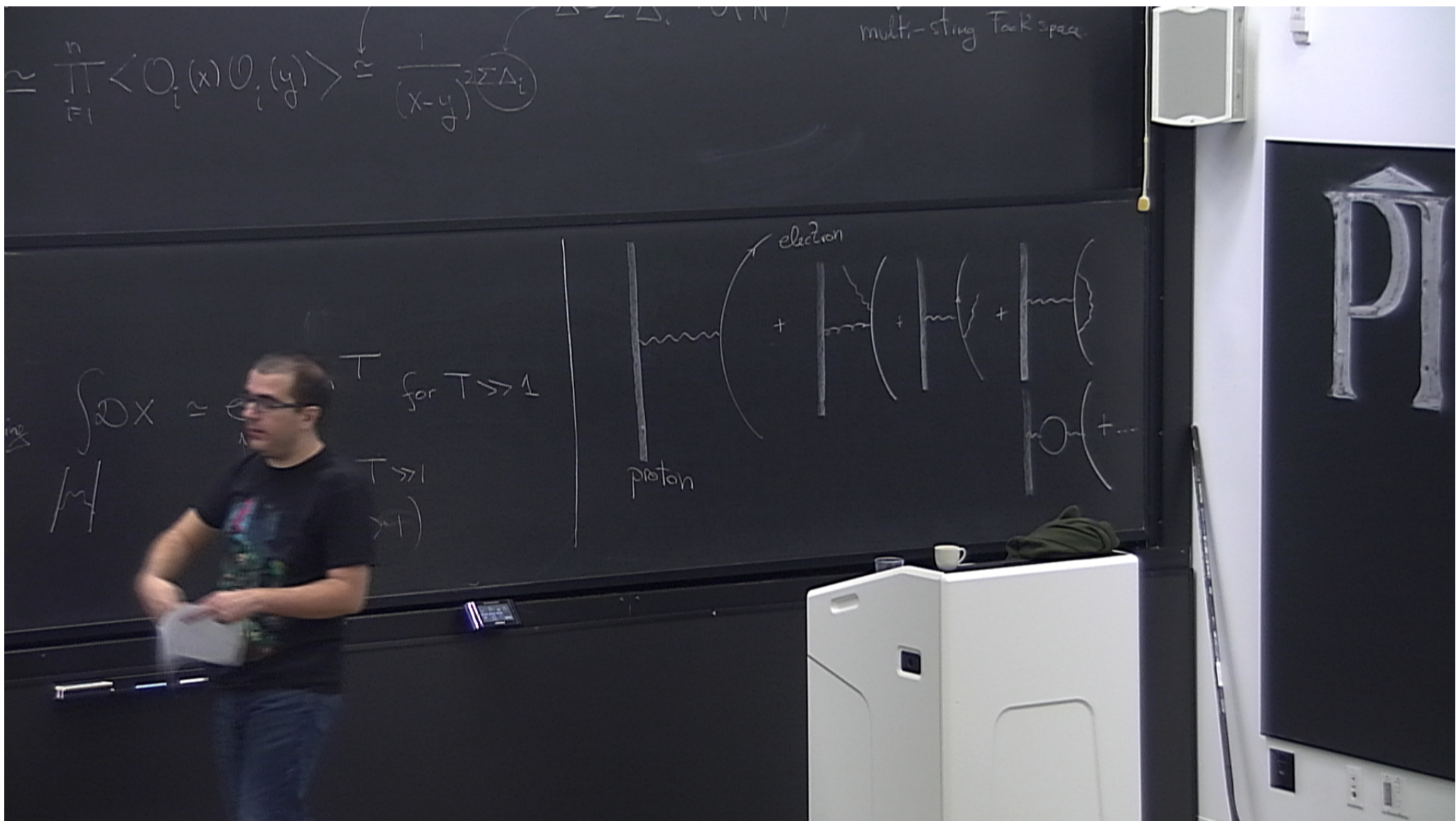
multi-string Fock space

$$\langle \tilde{O}(x) O(y) \rangle \approx \prod_{i=1}^s \langle O_i(x) O_i(y) \rangle \approx \frac{1}{(x-y)^{2\sum \Delta_i}}$$



$$\int \mathcal{D}X \approx e^{-S_{\min} T} \text{ for } T \gg 1$$

easy for $T \gg 1$
($\lambda \gg T$)

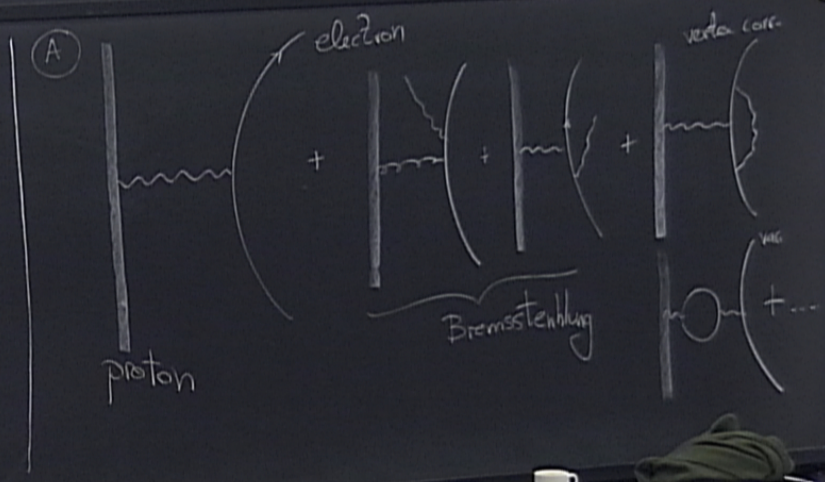


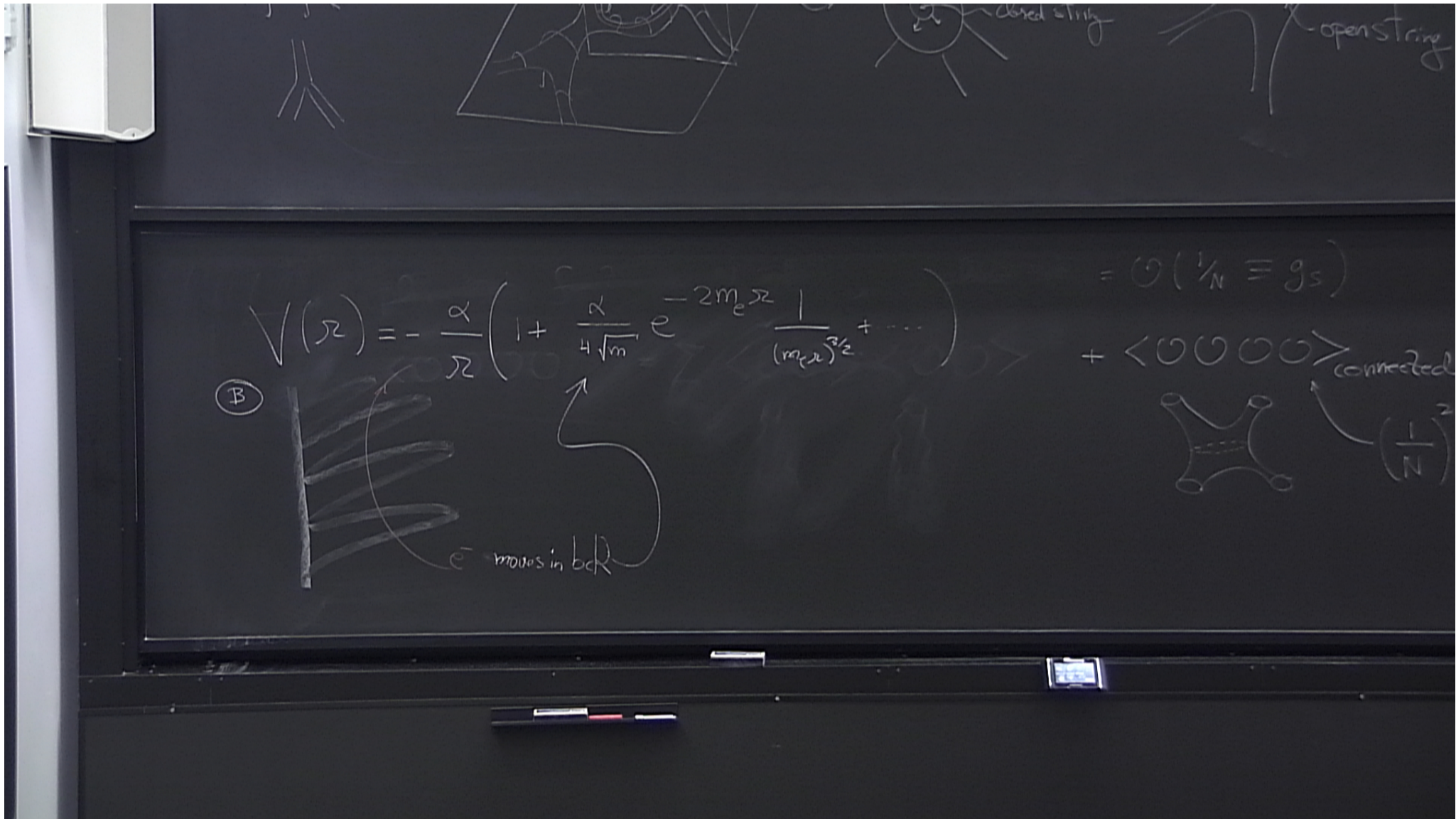
$$\approx \frac{1}{\Gamma} \langle O_i(x) O_i(y) \rangle \approx \frac{1}{(x-y)^{2\sum \Delta_i}}$$

multi-string Tack space

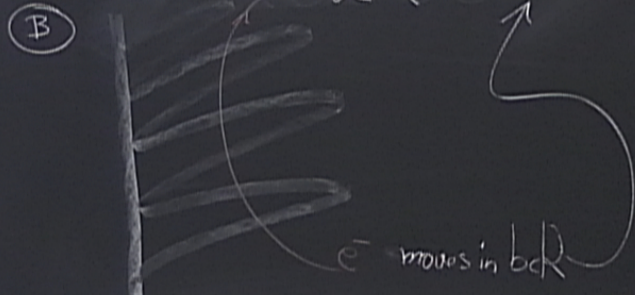
$$\int \mathcal{D}X \approx e^{-S_{\min} T} \text{ for } T \gg 1$$

easy for $T \gg 1$
($\lambda \gg T$)





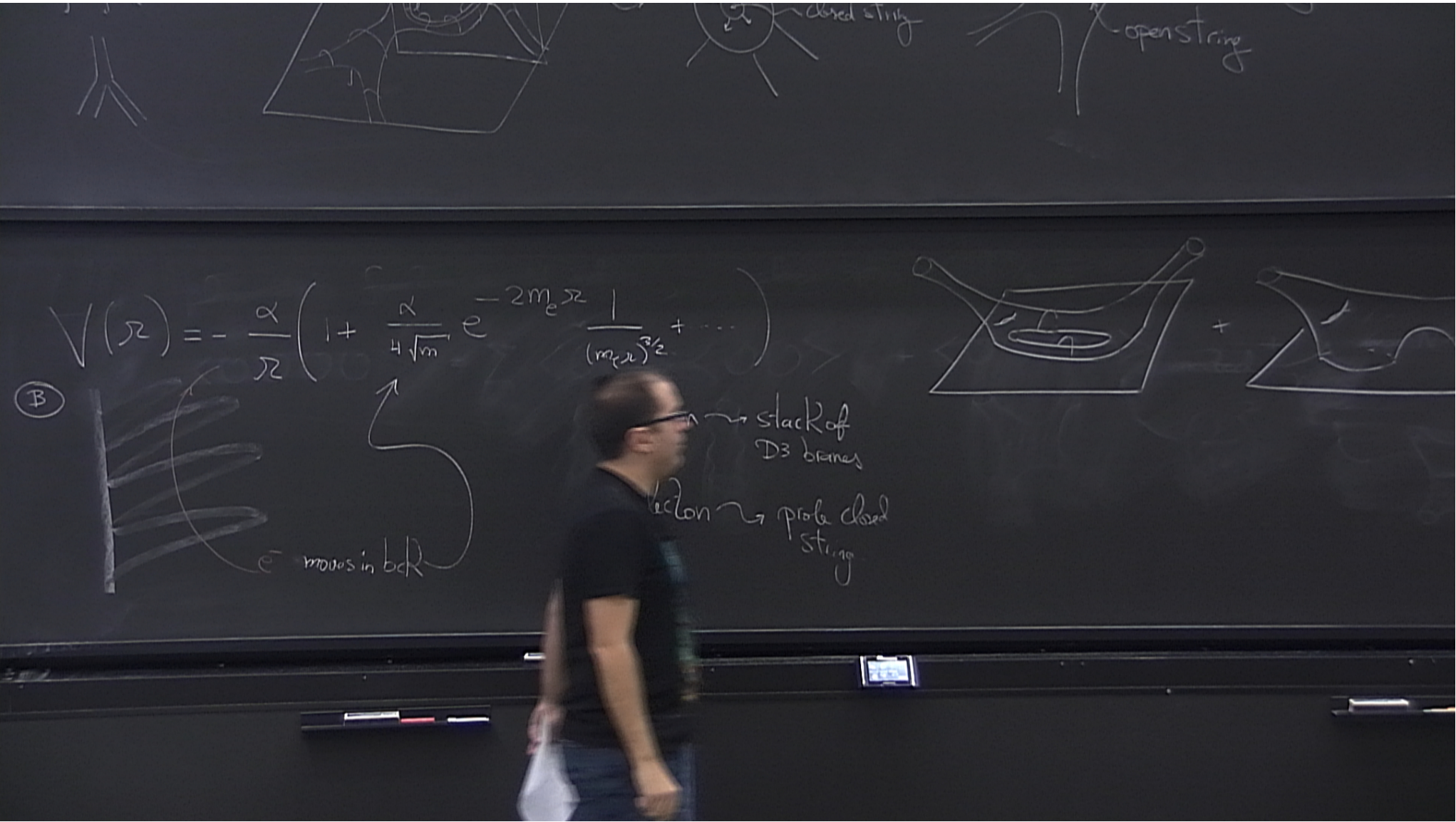
$$V(x) = -\frac{\alpha}{x} \left(1 + \frac{\alpha}{4\sqrt{m}} e^{-2m_e x} \frac{1}{(m_e x)^{3/2}} + \dots \right)$$



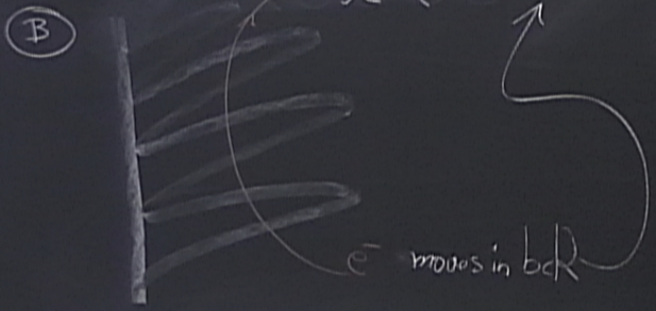
$$= \mathcal{O}\left(\frac{1}{N} \equiv g_s\right)$$

+ <OOOO> connected

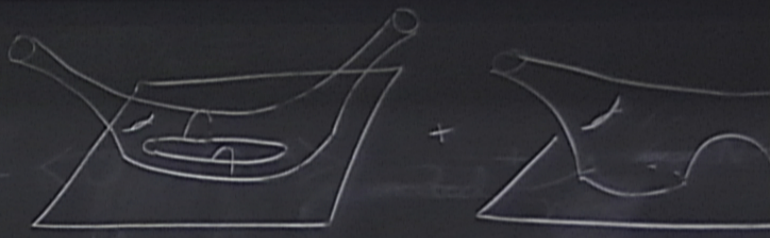
$\left(\frac{1}{N}\right)^2$



$$V(\rho) = -\frac{\alpha}{\rho} \left(1 + \frac{\alpha}{4\sqrt{m}} e^{-2m_e\rho} \frac{1}{(m_e\rho)^{3/2}} + \dots \right)$$



stack of D3 branes
 probe closed string

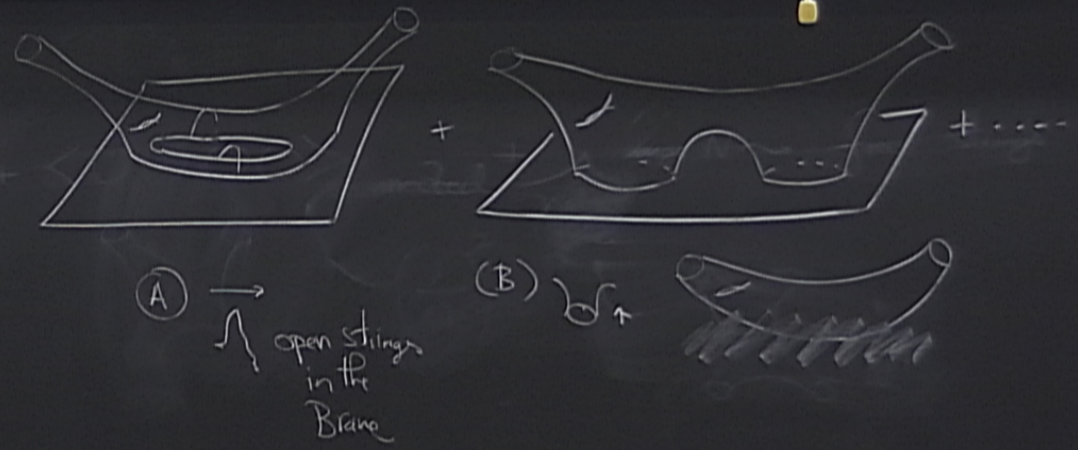


closed string open string

9 ← easy for $\lambda \ll 1$ → 9

$$e^{-2m_e r} \left(\frac{1}{(m_e r)^{3/2}} + \dots \right)$$

proton \rightarrow stack of D3 branes
 electron \rightarrow probe closed string

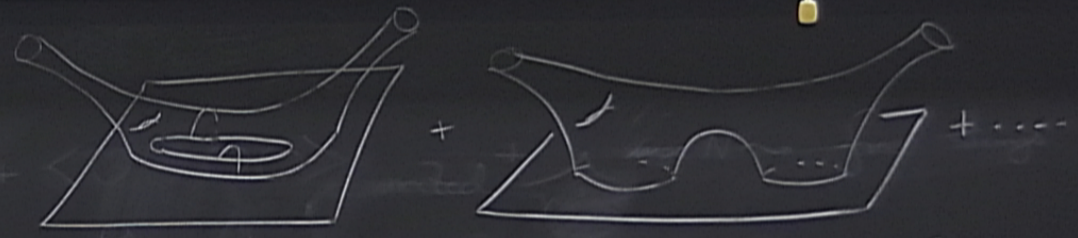


closed string open string

9 ← long for $\lambda \ll 1$ mm 9

$$e^{-2m_e \alpha'} \frac{1}{(m_e \alpha')^{3/2}} + \dots$$

proton \rightarrow stack of D3 branes
 electron \rightarrow probe closed string



(A) \rightarrow open strings in the Brane
 \equiv YM + massive stuff

(B) \rightarrow background
 Gravitly + massive stuff

closed string open string

easy for $\lambda \ll 1$ g

$$e^{-2m_e r} \frac{1}{(m_e r)^{3/2}} + \dots$$

proton \rightarrow stack of D3 branes
 electron \rightarrow probe closed string

