

Title: PSI 2015/2016 More/Beyond Standard Model - Lecture 11

Date: Mar 07, 2016 09:00 AM

URL: <http://pirsa.org/16030040>

Abstract:

Recall: $\mathcal{L} = \frac{1}{2} |\partial \Phi|^2 - (-m^2 |\Phi|^2 + \frac{1}{2} |\Phi|^4)$

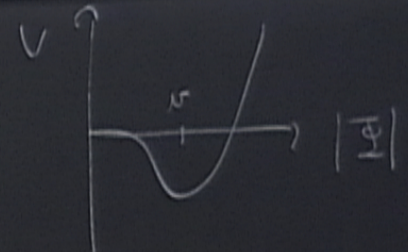
$\langle \Phi \rangle = N e^{i\beta}, \quad \beta \in [0, 2\pi)$

Expand around $\beta=0$: $\Phi(x) = (N + r(x)/\sqrt{2}) e^{i a(x)/\sqrt{2} N}$

$\mathcal{L} = \frac{1}{2} (\partial r)^2 + \frac{1}{2} \left(1 + \frac{r}{\sqrt{2} N}\right)^2 (\partial a)^2 - V(r)$

Symmetric under: $r \rightarrow r, \quad a \rightarrow a + \sqrt{2} N \alpha$

Recall: $\mathcal{L} = \frac{1}{2} |\partial \Phi|^2 - (-m^2 |\Phi|^2 + \frac{\lambda}{2} |\Phi|^4)$



$\langle \Phi \rangle = N e^{i\beta}, \beta \in [0, 2\pi)$

Expand around $\beta=0$: $\Phi(x) = (N + r(x)/\sqrt{2}) e^{i a(x)/\sqrt{2} N}$

$\mathcal{L} = \frac{1}{2} (\partial r)^2 + \frac{1}{2} \left(1 + \frac{r}{\sqrt{2} N}\right)^2 (\partial a)^2 - V(r)$

Symmetric under: $r \rightarrow r, a \rightarrow a + \sqrt{2} N \alpha$

$$\mathcal{L} = -\frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} + \bar{Q}_L i \gamma^\mu D_\mu Q_L + \bar{Q}_R i \gamma^\mu D_\mu Q_R$$

$SU(2)_L \times SU(2)_R \times U(1)_V$ global symmetry.

$$Q_{L,R} = \begin{pmatrix} u_{L,R} \\ d_{L,R} \end{pmatrix}$$

$$\langle \bar{Q}_J Q_I \rangle = \Lambda_{QCD}^3 \delta_{IJ}$$

$$\mathbb{1} \rightarrow L \mathbb{1} R^\dagger$$

$$SU(2)_L: Q_L \rightarrow L Q_L$$

$$SU(2)_R: Q_R \rightarrow R Q_R$$

$$U(1)_V: Q_L \rightarrow e^{i\alpha} Q_L$$

$$Q_R \rightarrow e^{i\alpha} Q_R$$

$$SU(2)_L \times SU(2)_R \times U(1)_V \rightarrow SU(2)_V \times U(1)_V$$

subgroup with $L=R$.

$$Q_L + \bar{Q}_R i \gamma^5 \gamma_\mu Q_R$$

$$Q_{L,R} = \begin{pmatrix} u_{L,R} \\ d_{L,R} \end{pmatrix}$$

$$R^\dagger$$

$$SU(2)_V \times U(1)_V$$

subgroup with $L=R$

$$\Sigma(x) = \exp[2i \pi^a(x) t^a / f]$$

$$\Sigma(x) \rightarrow L \Sigma(x) R^\dagger$$

$$L = e^{i c_A^a t^a} e^{i c_V^b t^b}$$

$$R = e^{-i c_A^a t^a} e^{i c_V^b t^b}$$

$$C_V^b = 0$$

$$\pi \rightarrow \pi' = \pi + f c_A^a t^a$$

↳ non-linear shift

$$\pi^a \rightarrow \pi^a(1+)$$

$$C_A^a = 0 \quad \Sigma \rightarrow V \Sigma V^\dagger \rightarrow \exp[2i \underbrace{V \pi^a t^a V^\dagger}_{\pi^a} / f]$$

$$\partial_\mu \Sigma^\dagger \partial^\mu \Sigma \rightarrow R(\partial_\mu \Sigma^\dagger \partial^\mu \Sigma) R^\dagger$$

$$\mathcal{L}_{P^2} = \frac{f^2}{4} \text{tr}(\partial_\mu \Sigma^\dagger \cdot \partial^\mu \Sigma)$$

$$= \frac{1}{2} (\partial \pi^a)^2 + \frac{1}{3f^2} \cdot \text{tr} \left[(\partial \pi^a \cdot \pi^a)^2 \right] + \dots$$

~~$$\sim \frac{p^2}{f^2}$$~~

$$j_V^\mu = \bar{Q} \gamma^\mu Q$$

$$j_L^{\mu a} = \bar{Q} \gamma^\mu P_L t^a Q$$

$$j_A^\mu = \bar{Q} \gamma^\mu \gamma^5 Q$$

$$j_R^{\mu a} = \bar{Q} \gamma^\mu P_R t^a Q$$

$$j_V^\mu = i(\pi^+ \partial^\mu \pi^- - \pi^- \partial^\mu \pi^+)$$

$$j_L^{\mu a} = -i \frac{f^2}{2} \text{tr}(\Sigma^\dagger t^a \partial^\mu \Sigma) = f \text{tr}(t^a \partial^\mu \pi) + \dots$$

$$j_R^{\mu a} = -i \frac{f^2}{2} \text{tr}(\Sigma t^a \partial^\mu \Sigma^\dagger) = \dots$$

$\sim \frac{1}{p_2}$

$\bar{Q} \gamma^\mu P_L t^a Q$

$\bar{Q} \gamma^\mu P_R t^a Q$

t^+

$\text{tr}(t^a \gamma^\mu \Pi) + \dots$

$$\langle \bar{\mu} \bar{\nu}_\mu | \mathcal{H}_{\text{int}} | \Pi^-(p) \rangle \sim \underbrace{\left[\langle \bar{\mu} \bar{\nu}_\mu | \bar{\mu} \gamma_\mu P_L \nu_\mu | 0 \rangle \right]}_{\text{standard}} \cdot \left[\langle 0 | \bar{u} \gamma^\mu P_L d | \Pi^-(p) \rangle \right]$$

$$\mathcal{H}_{\text{int}} = \frac{g^2}{m_W^2} (\bar{u} \gamma^\mu P_L d) (\bar{\mu} \gamma_\mu P_L \nu_\mu)$$

Symmetric under $U \rightarrow UR$, $d \rightarrow d + \sqrt{2} N \alpha$

$$m_u = 2.5 \text{ MeV}, \quad m_d = 5 \text{ MeV}$$

$$- \mathcal{L}_{\text{QCD}} = \bar{Q}_L M^T Q_R + \bar{Q}_R M Q_L, \quad M = \begin{pmatrix} m_u & 0 \\ 0 & m_d \end{pmatrix}$$

Pretend that $M \rightarrow R M L^\dagger$.

$$- \mathcal{L} = \underbrace{\frac{1}{2} \tilde{L}^3}_{\text{New dimensionful const}} \text{tr}(M \Sigma) + \text{hc} = \frac{1}{2} m_\pi^2 (\Pi^a)^2 = \frac{1}{2} \underbrace{\tilde{L}^3 (m_u + m_d)}_{\substack{\text{from } \mathcal{L}_{\text{QCD}} \\ \text{from } \mathcal{L}_{\text{eff}}}} \frac{1}{f_\pi^2} (\Pi^a)^2$$

$$f_\pi^2 m_\pi^2 = \tilde{L}^3 (m_u + m_d)$$

$$m_s \simeq 110 \text{ MeV} \quad (m_c \simeq 1.2 \text{ GeV}, \quad m_b \simeq 4.5 \text{ GeV})$$

$$SU(3)_L \times SU(3)_R \times U(1)_V, \text{ mix } u, d, s$$

$$\Pi^a t^a = \frac{1}{\sqrt{2}} \begin{pmatrix} \Pi^0/\sqrt{2} + \eta/\sqrt{6} & \Pi^+ & K^+ \\ \Pi^- & -\Pi^0/\sqrt{2} + \eta/\sqrt{6} & K^0 \\ K^- & \bar{K}^0 & -2\eta/\sqrt{6} \end{pmatrix}$$