

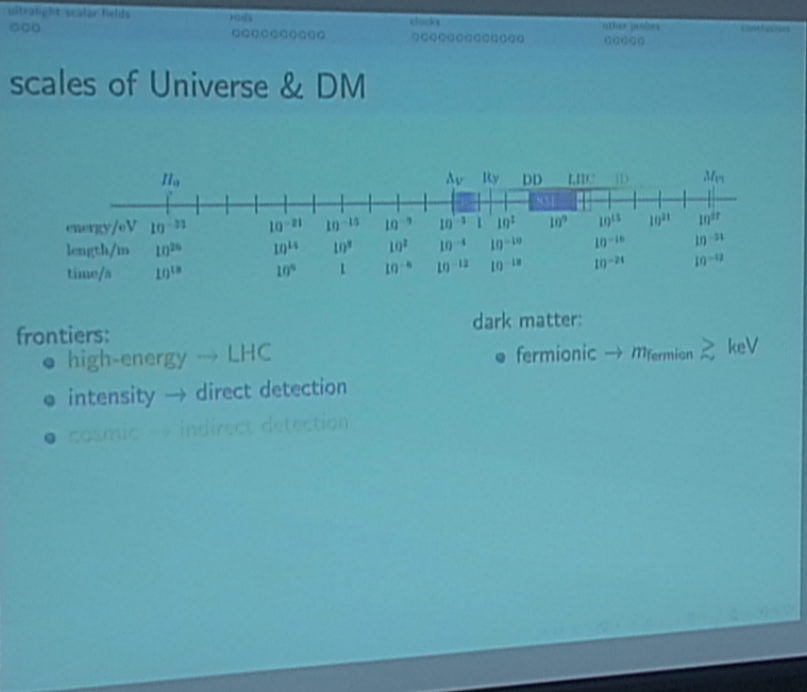
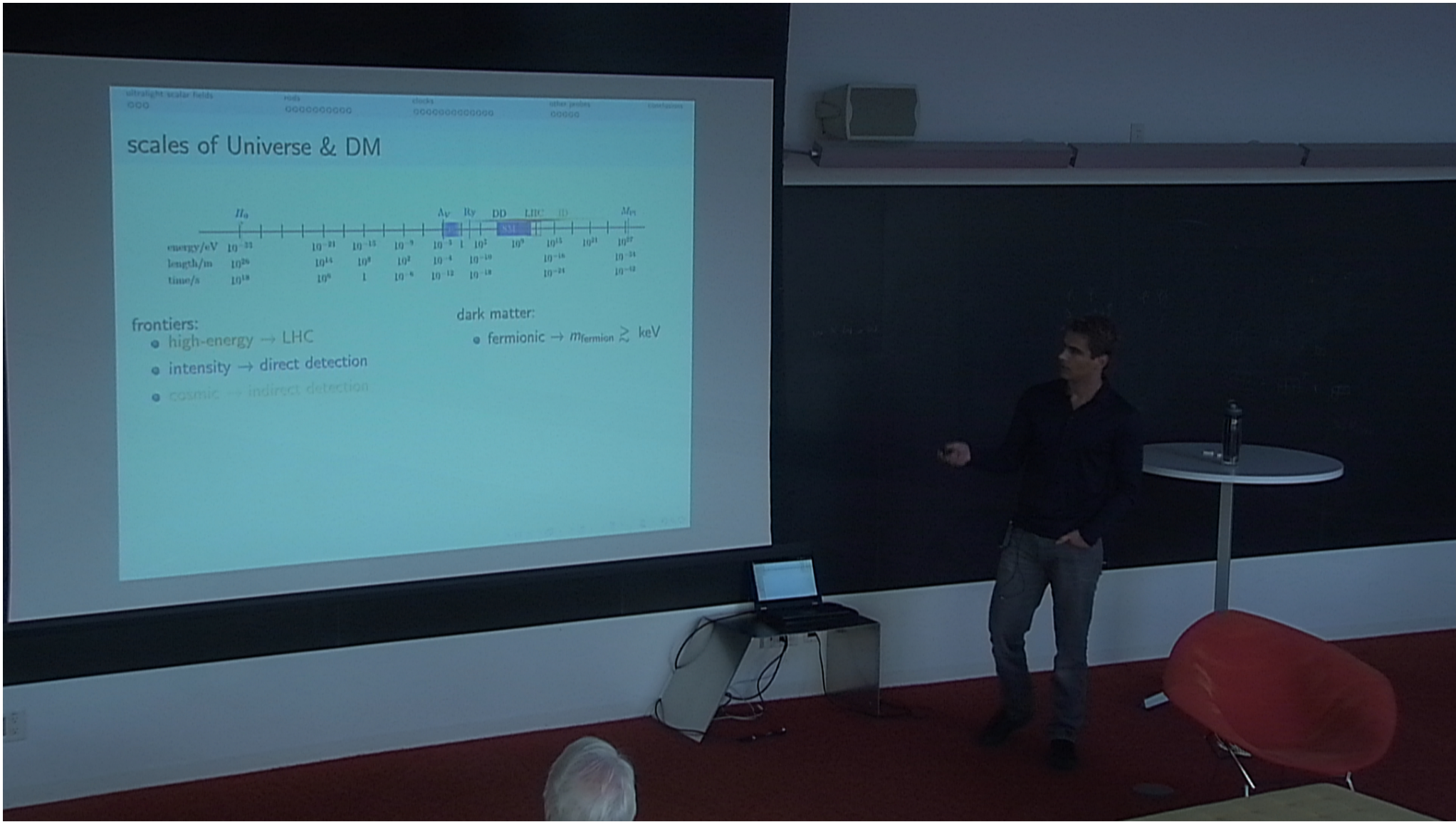
Title: Looking for light scalar dark matter with rods and clocks

Date: Feb 05, 2016 12:30 PM

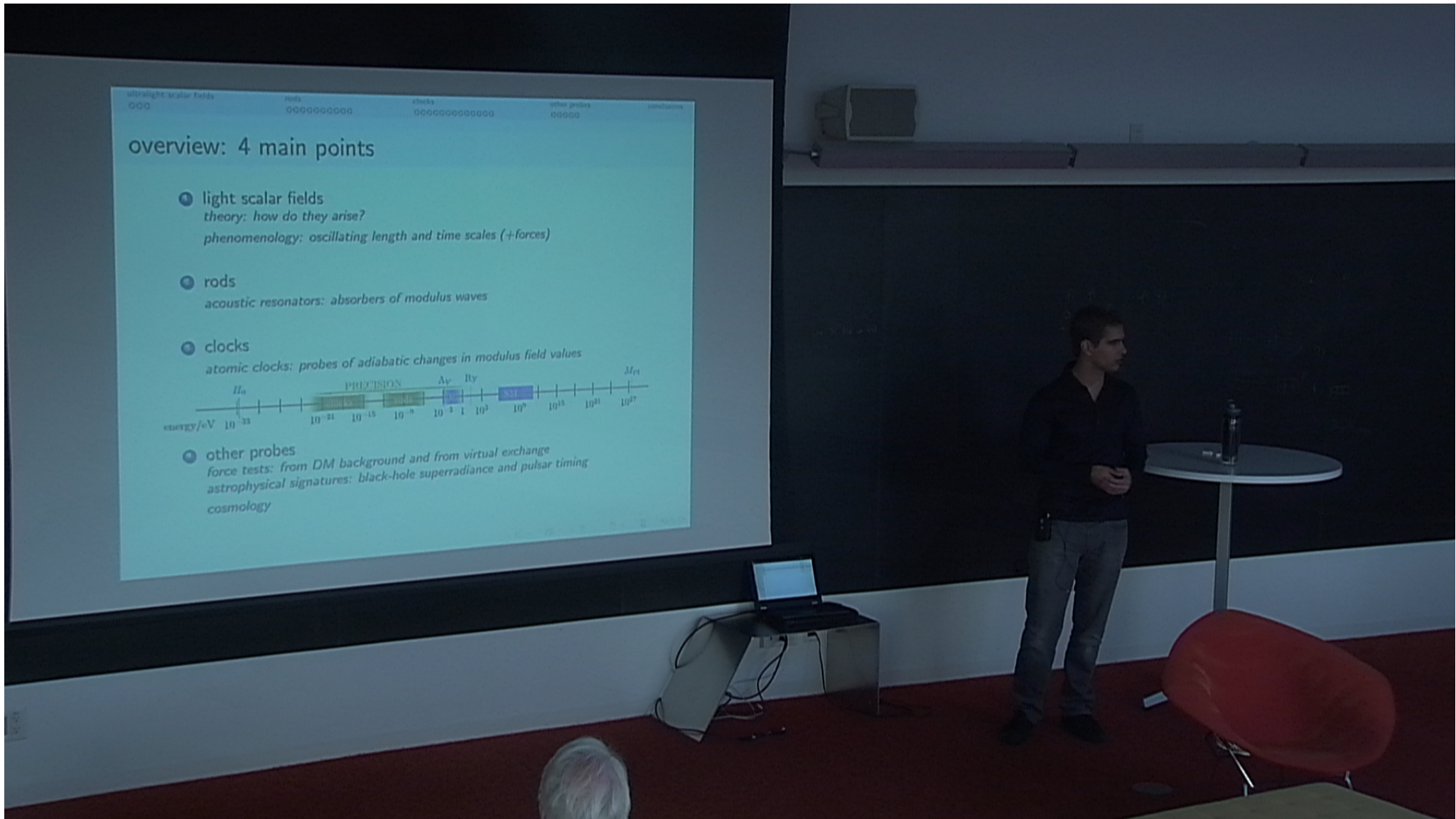
URL: <http://pirsa.org/16020099>

Abstract: <p>If the dark matter is made up of a bosonic particle, it can be ultralight, with a mass potentially much below 1 eV. Well-known DM candidates of this type include pseudoscalars like the QCD axion, and vectors such as hidden photons kinetically mixed with the Standard Model. Moduli, even-parity scalars with nonderivative couplings to the SM, can also be light dark matter. I will show that they cause tiny fractional oscillations of SM parameters, such as the electron mass and the fine-structure constant, in turn modulating length and time scales of atoms. Rods and clocks, used in gedanken experiments in relativity, have since transformed into actual precision instruments. The size of acoustic resonators and the frequency of optical clocks can now be measured to 1 part in  $10^{22}$  and  $10^{18}$ , respectively, and thus constitute sensitive probes of moduli. </p>

<p>In this talk, I will give an overview of the parameter space of modulus dark matter, and discuss the sensitivity of the proposed experiments compared to existing constraints from fifth-force tests.</p>



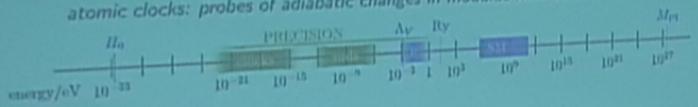




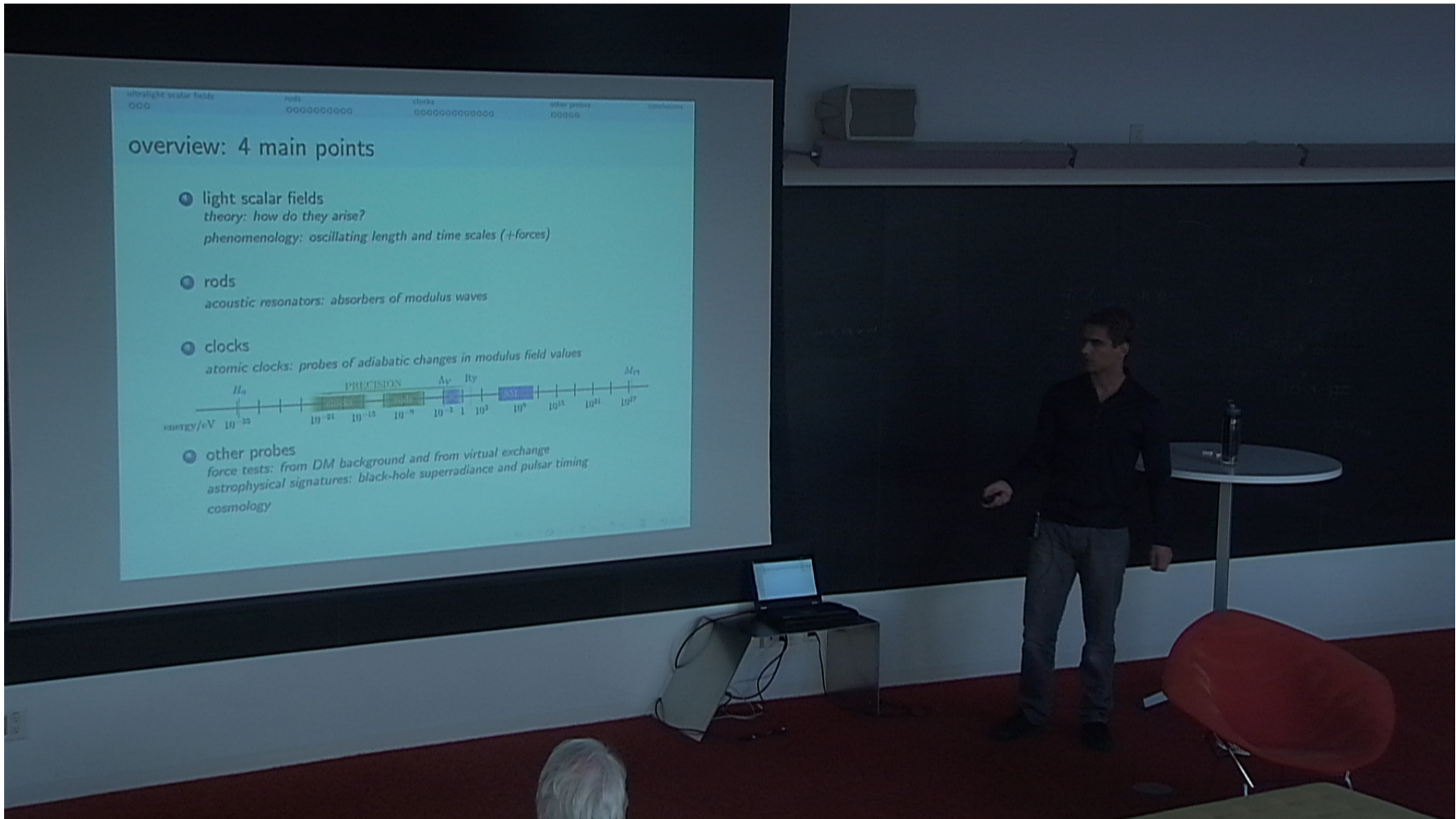
ultralight scalar fields  
 ○○○○ rods ○○○○○○○○○○ clocks ○○○○○○○○○○○○○○ other probes ○○○○○○ contributions

### overview: 4 main points

- 1 light scalar fields  
 theory: how do they arise?  
 phenomenology: oscillating length and time scales (+forces)
- 2 rods  
 acoustic resonators: absorbers of modulus waves
- 3 clocks  
 atomic clocks: probes of adiabatic changes in modulus field values
- 4 other probes  
 force tests: from DM background and from virtual exchange  
 astrophysical signatures: black-hole superradiance and pulsar timing  
 cosmology



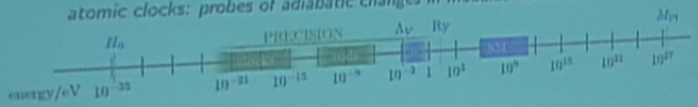




ultralight scalar fields  
 rods  
 clocks  
 other probes  
 conclusions

overview: 4 main points

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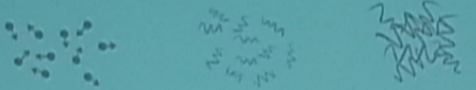




How do light scalars arise in the Universe?

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m_\phi^2 \phi^2$$

correspondence principle: classical wave description



$$\text{occ. \#} = \frac{\Delta N}{(\Delta x)^3 (\Delta p)^3} = \frac{n}{(\Delta p)^3} = \frac{\rho}{m(\Delta p)^3} \sim \frac{\rho}{m^4 v_{\text{vir}}^3} \approx 2 \times 10^3 \left(\frac{\text{eV}}{m_\phi}\right)^4$$

$$\rho_{\text{DM}} \approx 0.3 \text{ GeV m}^{-3} \quad v_{\text{vir}} \sim 10^{-3}$$

$$\phi(t, \mathbf{x}) \simeq \phi_0 \cos(m_\phi t - m_\phi \mathbf{v} \cdot \mathbf{x}) + \mathcal{O}(v^2) \text{ dispersion}$$

$$\rho = \frac{m_\phi^2 \phi_0^2}{2} = \rho_{\text{DM}} \Rightarrow \sqrt{4\pi G_N} \phi_0 \approx 6 \times 10^{-16} \left(\frac{10^{-15} \text{ eV}}{m_\phi}\right)$$

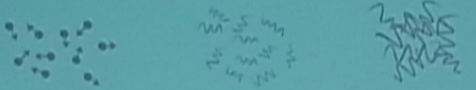




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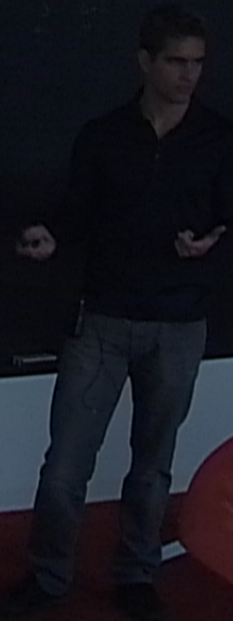


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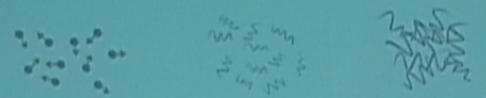




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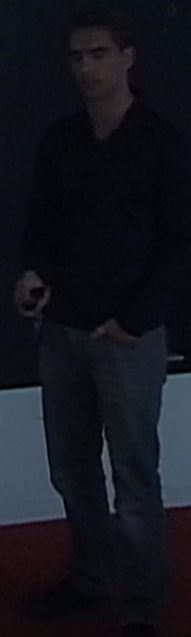


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How do light moduli arise in UV theories?

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m_\phi^2 \phi^2 + \sum_i d_i \sqrt{4\pi G_N} \phi \mathcal{O}_{SM,i} \quad (1)$$

- Higgs portal:  $A\phi H^\dagger H \Rightarrow d_m \sqrt{4\pi G_N} \sim \frac{\Lambda}{m_\mu}$  [arXiv:1003.2313]
- dilaton, least coupling principle:  $4\pi G_N \phi^2 \mathcal{O}_{SM}$  [arXiv:hep-th/9401069]
- QCD axion:  $d_{m_a} \sqrt{4\pi G_N} \sim \frac{f_{QCD}}{f_a}$
- radion component of extra-dimensional graviton
- any light Yukawa or gauge modulus!

Tuning?  $\Delta m_\phi^2 \sim \sum_i \frac{4\pi G_N}{16\pi^2} d_i^2 \left\{ \Lambda^4, m_i^2 \Lambda^2, \frac{y_i^2}{16\pi^2} \Lambda^4, \dots \right\}$





What are the observable effects of ultralight scalars?

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m_\phi^2 \phi^2 + \sqrt{4\pi G_N} \phi \left[ \underbrace{\frac{d_e}{4e^2} F_{\mu\nu} F^{\mu\nu}}_{\alpha \text{ changes}} - \underbrace{\frac{d_g \beta_3}{2g_3} G_{\mu\nu}^A G^{A\mu\nu}}_{\Lambda_{\text{QCD}} \text{ changes}} - d_{m_e} m_e \bar{e} e - \sum_{i=u,d} (d_{m_i} + \gamma_{m_i} d_g) m_i \bar{\psi}_i \psi_i \right]$$

- oscillating masses and couplings
  - $m_e(t) = m_e [1 + d_{m_e} \sqrt{4\pi G_N} \phi_0 \cos(m_\phi t)]$
  - $\alpha(t) = \alpha [1 + d_e \sqrt{4\pi G_N} \phi_0 \cos(m_\phi t)]$
  - length scales  $\propto$  Bohr radius =  $1/\alpha m_e$
  - frequency scales  $\sim \{ \alpha^2 m_e F(\alpha), \alpha^4 m_e^2 / m_p, \dots \}$
- equivalence-principle-violating forces
  - from scalar exchange:  $V_{AB} = -G_N \frac{m_A m_B}{r_{AB}} (1 + \alpha_A \alpha_B)$  [arXiv:1007.2792]
  - $\alpha_A \sim d_g + 10^{-1} d_{m_q} + 10^{-3} d_e + \frac{m_e}{m_p} d_{m_e} + \dots$
  - from DM:  $V_A = m_A [1 + \alpha_A \sqrt{4\pi G_N} \phi_0 \cos(m_\phi t - m_\phi \mathbf{v} \cdot \mathbf{x})]$
- purely gravitational effects
  - structure formation, black-hole superradiance, pulsar timing



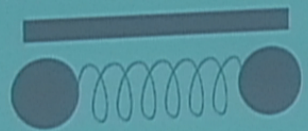
basic principle

$$L_0 \sim \frac{N}{\alpha m_e}$$

- tiny fractional change → macroscopic objects

$$h \equiv \frac{\delta L}{L_0} = \frac{\delta \alpha}{\alpha} + \frac{\delta m_e}{m_e} = (d_{m_e} + d_e) \sqrt{4\pi G_N \phi_0} \approx 10^{-18} (d_{m_e} + d_e) \left( \frac{10^{-12} \text{ eV}}{m_\phi} \right)$$

- (almost) no DC response → excite acoustic modes

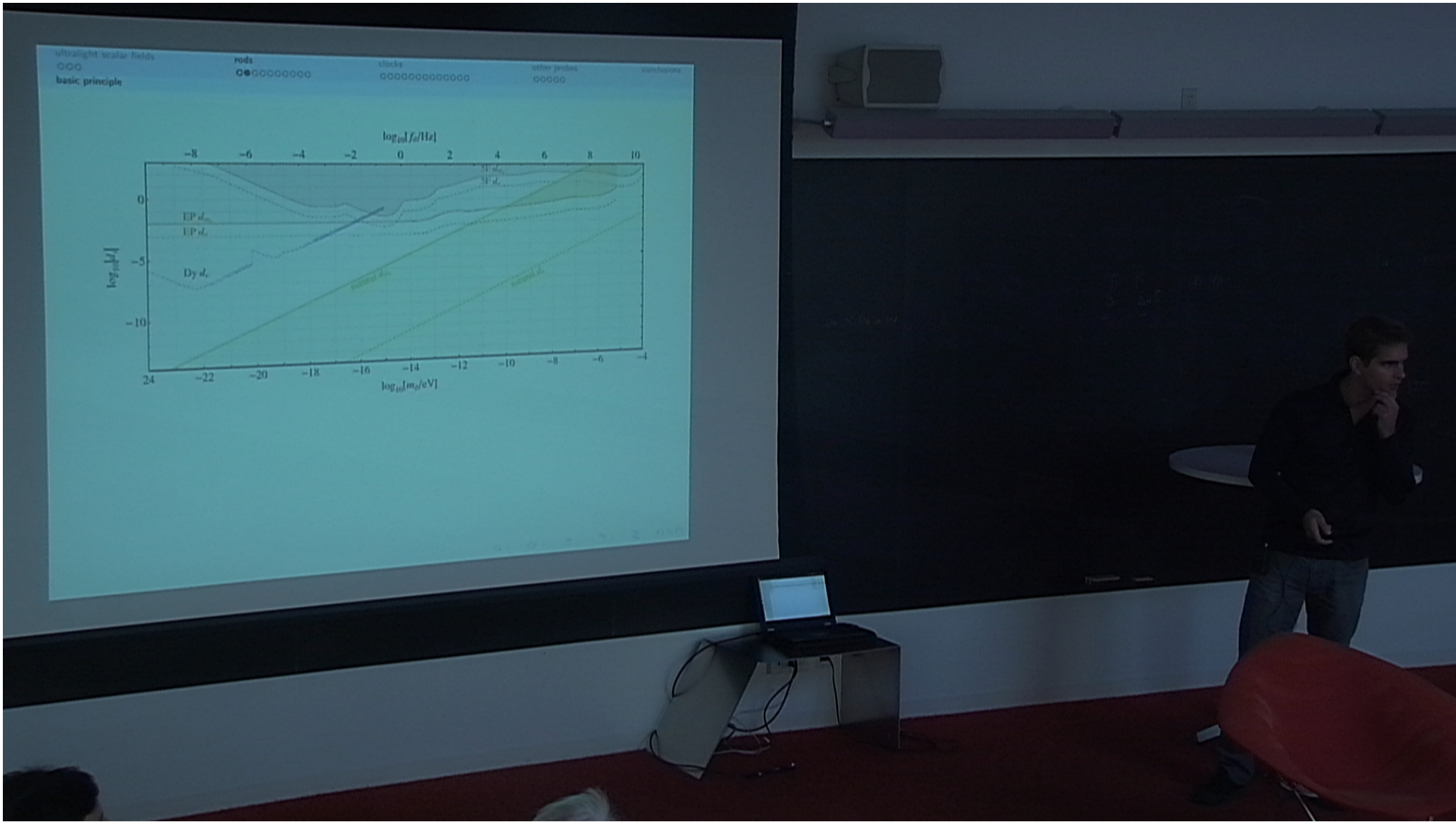


$$M \left[ \ddot{x} + \frac{\omega}{Q} \dot{x} + \omega^2 (x - L) \right] = F_{\text{noise}} \quad (D \equiv x - L)$$

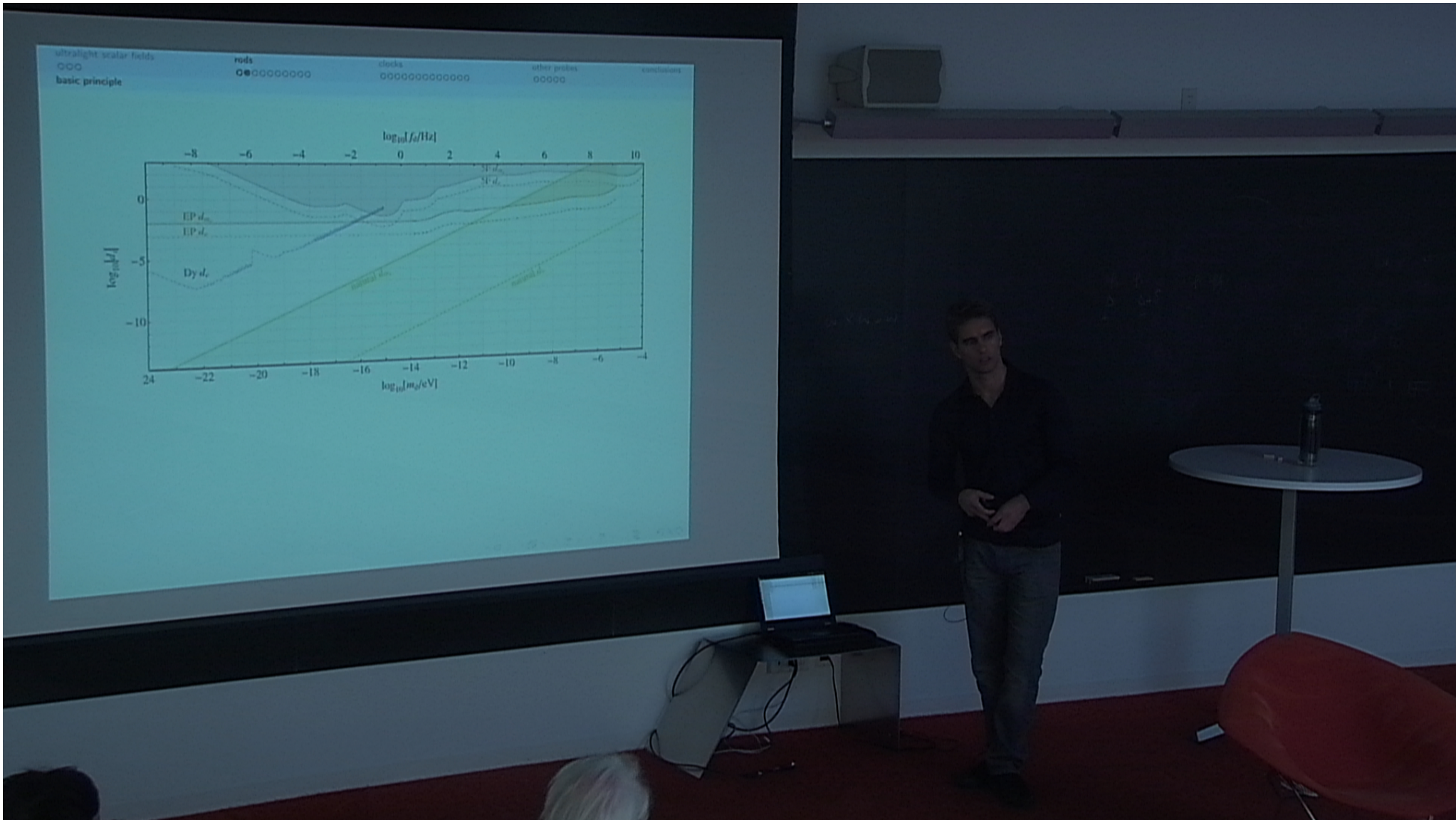
$$M \left[ \ddot{D} + \frac{\omega}{Q} \dot{D} + \omega^2 D \right] \simeq -M\ddot{L}_0 + F_{\text{noise}} = -ML_0 \ddot{h} + F_{\text{noise}}$$









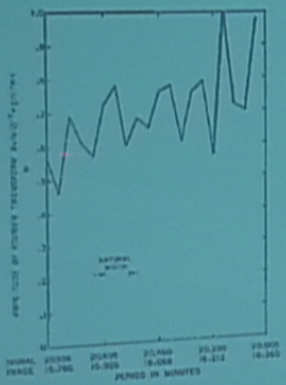




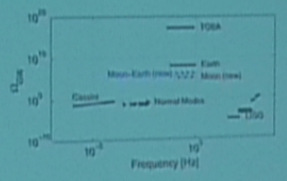
seismology

Earth:  $T = 20.46$  min,  
 $Q \approx 7,500$

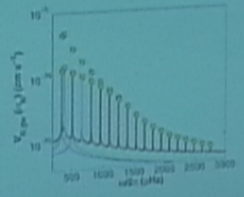
Earth crust + Moon [Coughlin, Harms (2014)]



[Weiss, Block (1967)]



Sun:  $Q \approx 10^8 - 10^4$  [Lopes, Silk (2014)]

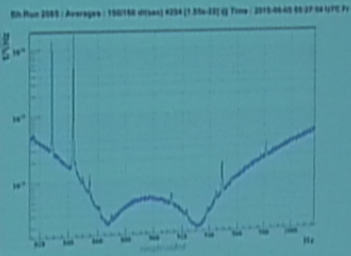
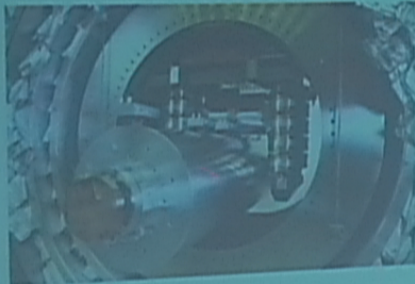




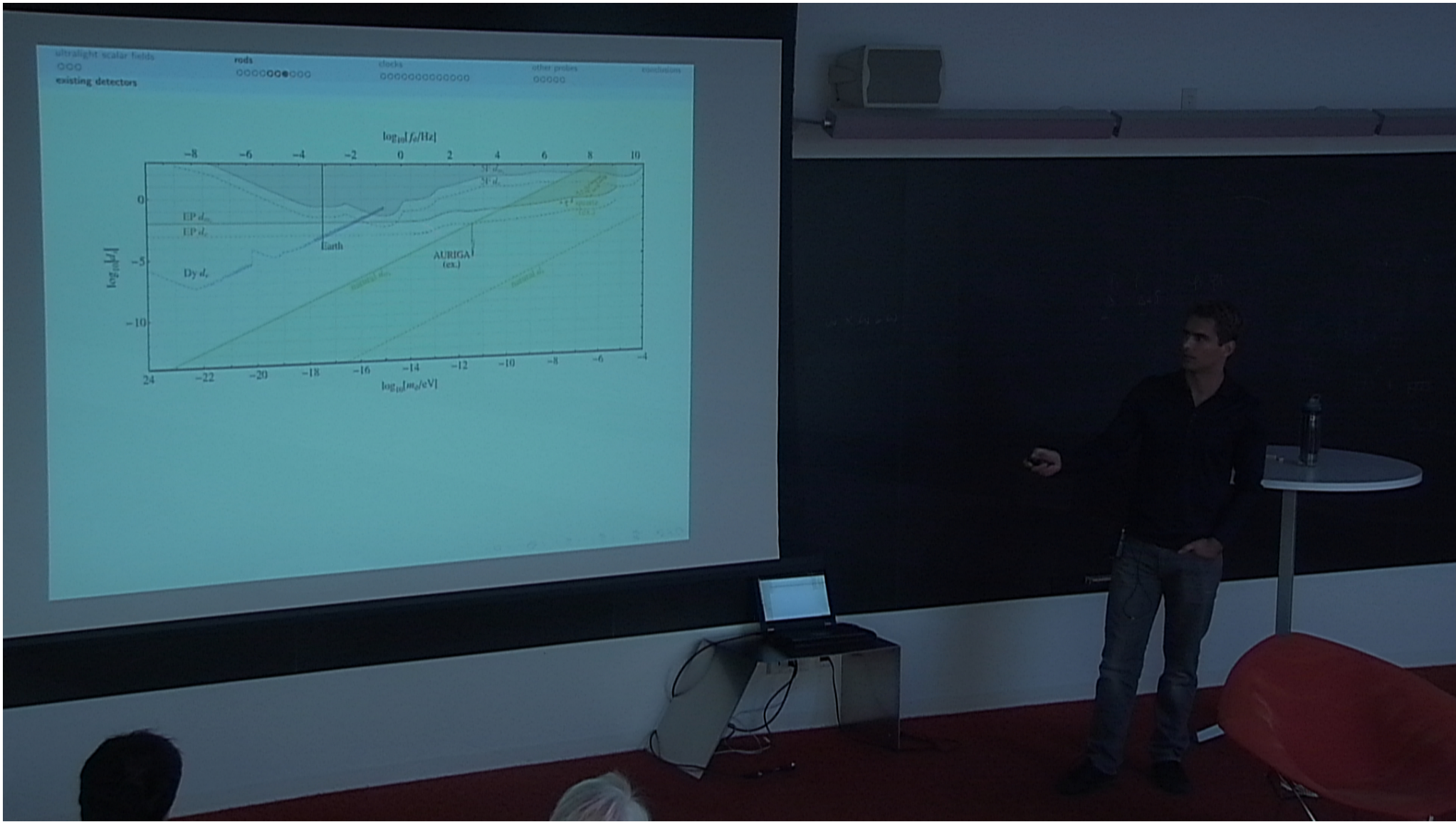
ultra-light scalar fields   rods   clocks   other probes   conclusions  
existing detectors

# AURIGA

+ many other kHz-class cylindrical antennas: NAUTILUS, EXPLORER, MiniGRAIL, Schenberg, ...

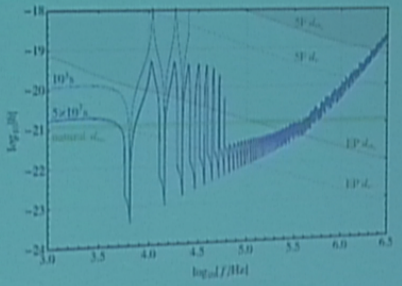
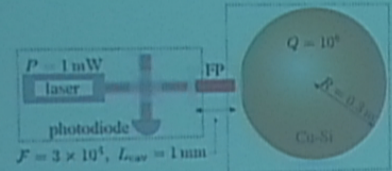








# Cu-Si sphere proposal



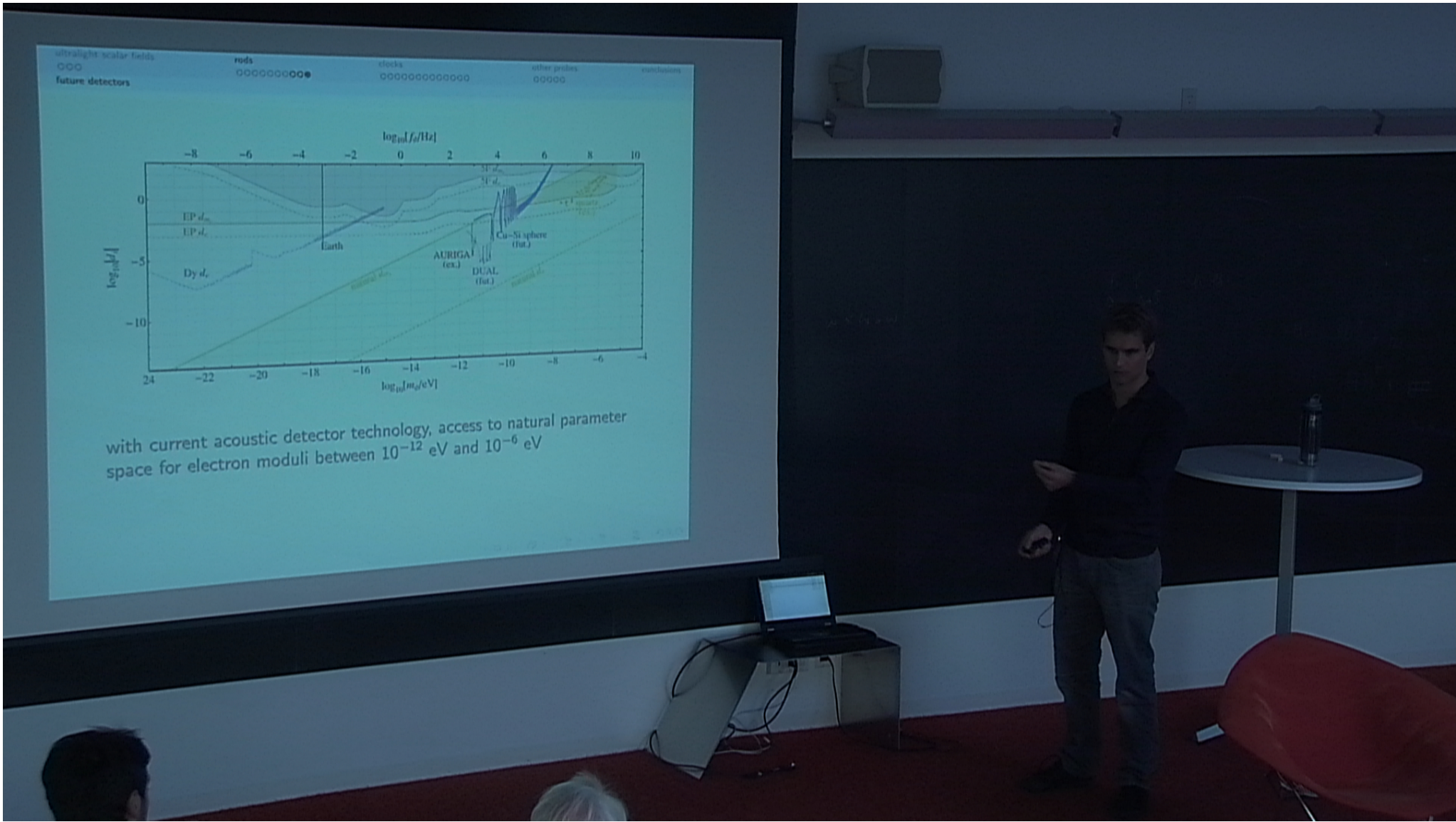
- broadband, non-resonant readout:  
 $\sqrt{S_{RR}} \approx 10^{-19} \text{ m Hz}^{-1/2} \sim \sqrt{\lambda / F^2 P}$
- multimode antenna:  
 $\omega_n \sim n\pi c / R$
- temperature tuning: 5%  $c$  variation between 4–100 K

thermal noise power:

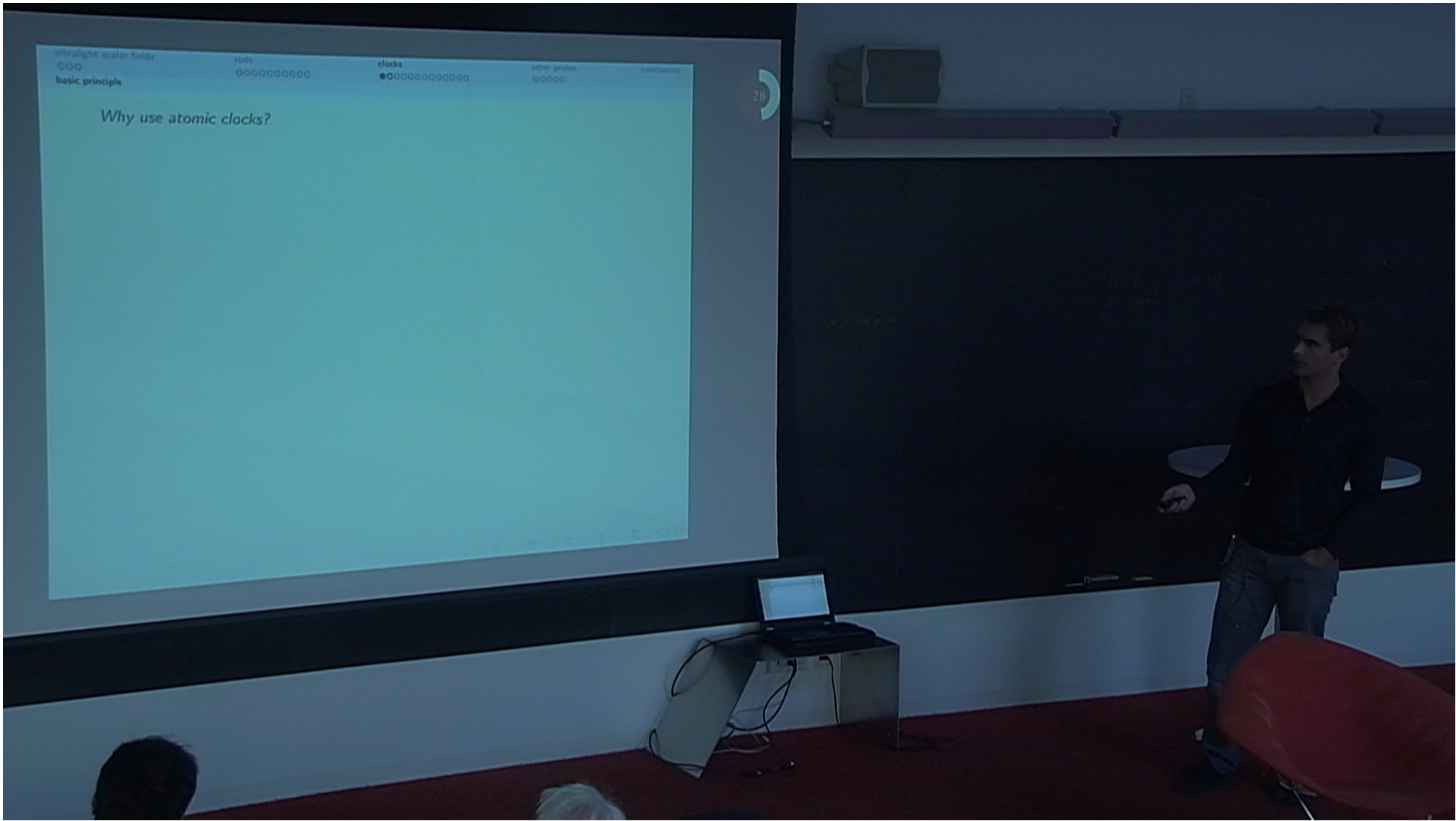
$$S_{hh}^{\text{th}} = \frac{4TR}{MQc^3} \frac{M_n}{k_n^3 J_n^2}$$



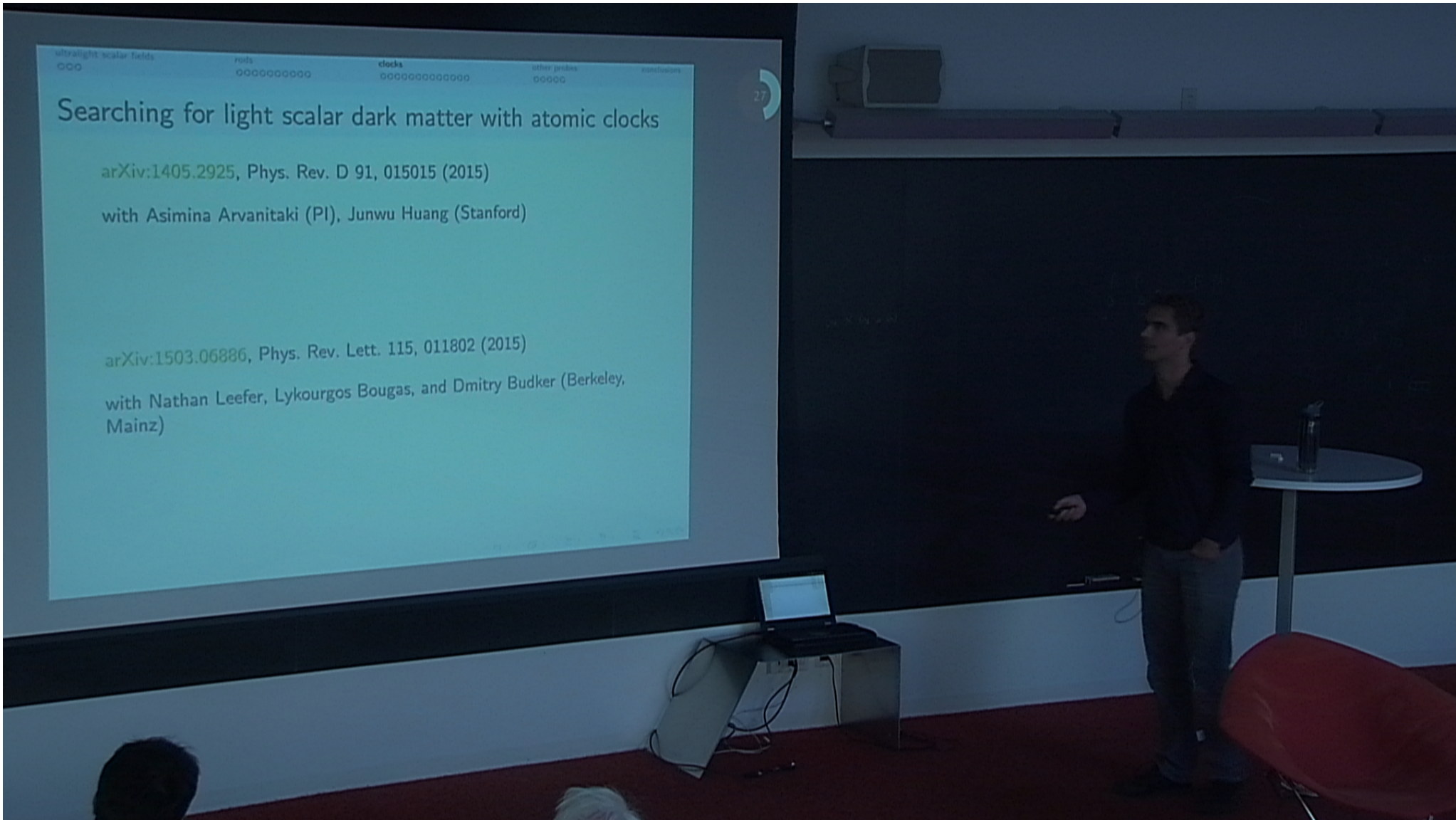




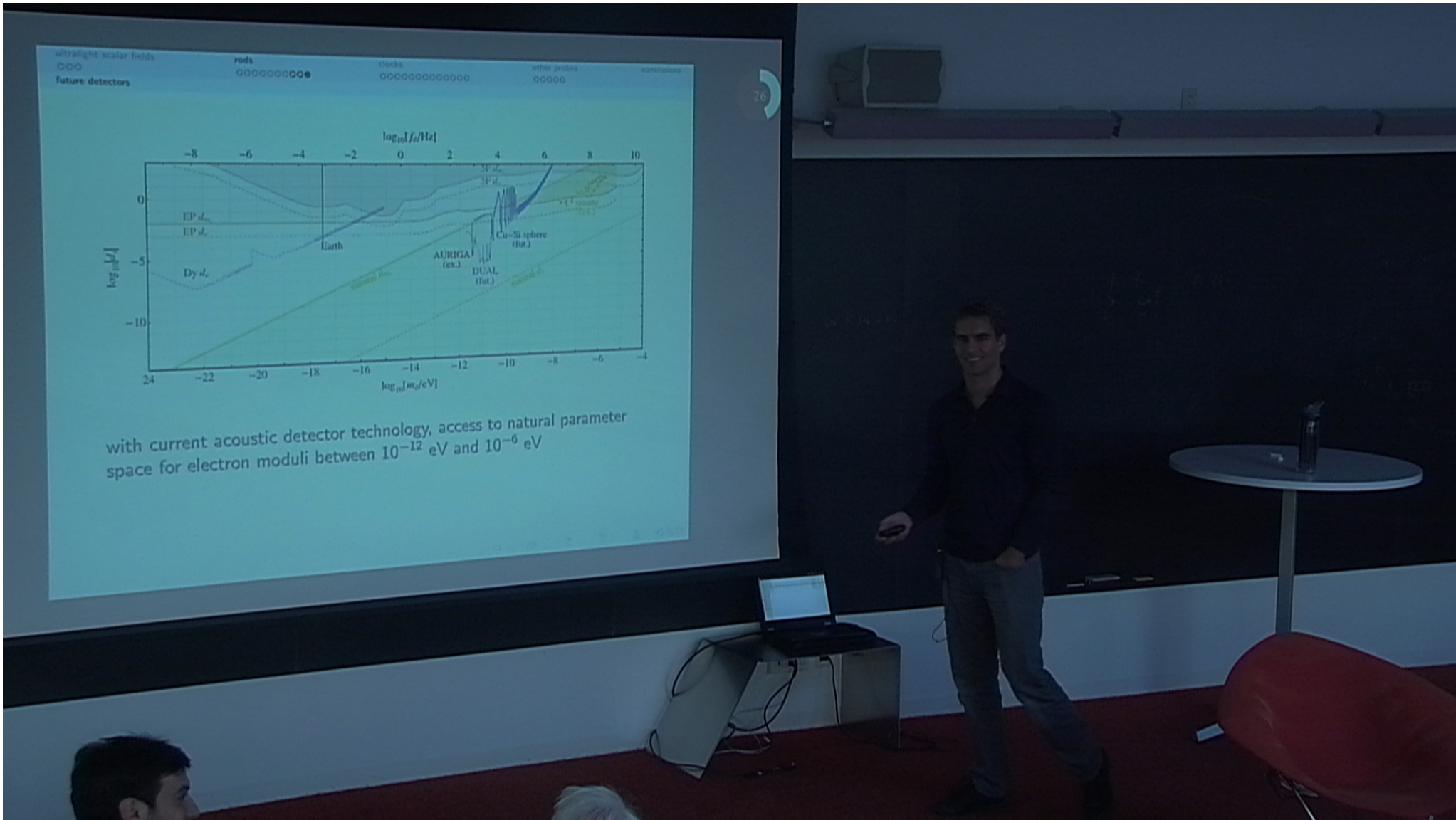












with current acoustic detector technology, access to natural parameter space for electron moduli between  $10^{-12}$  eV and  $10^{-6}$  eV



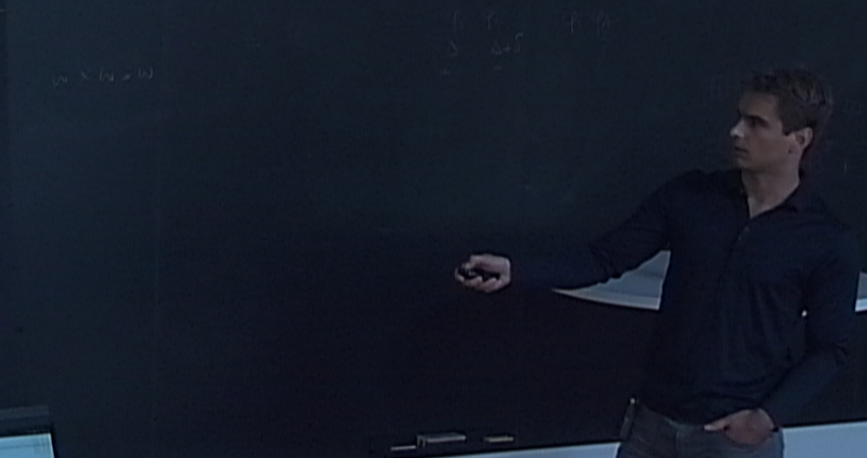
basic principle

How do atomic transition frequencies change with varying masses and couplings?

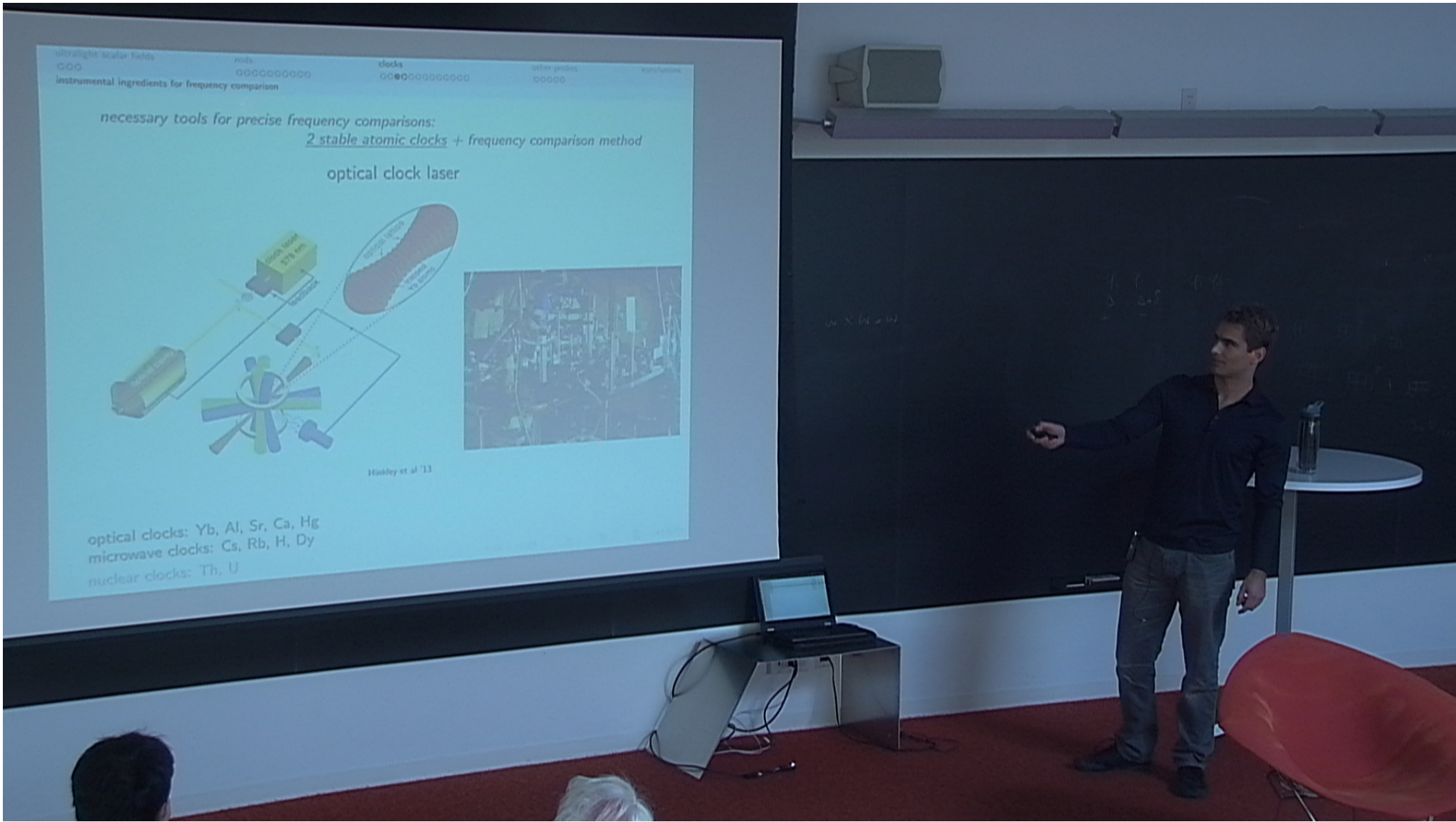
$$f_A \propto \left(\frac{m_e}{m_p}\right)^{\zeta_A} (\alpha)^{\xi_A+2} \quad (2)$$

$\zeta_A$ : 1 iff hyperfine;  $\xi_A$ : relativistic, spin-orbit, many-body, electric quadrupole effects

species	transition	$\lambda$ [nm]	short [ $\frac{10^{-15}}{\sqrt{2}}$ ]	long [ $10^{-18}$ ]	$\zeta_A$	$\xi_A$
$^{133}\text{Cs}$	hyperfine	$3.3 \cdot 10^7$	$2 \cdot 10^2$	360	1	2.83
$^{27}\text{Al}^+$	$3s^2 \ ^1S_0 \leftrightarrow 3s3p \ ^3P_0$	267	2.8	8.6	0	0.008
$^{87}\text{Sr}$	$5s^2 \ ^1S_0 \leftrightarrow 5s5p \ ^3P_0$	698	0.34	6.4	0	0.06
$^{171}\text{Yb}$	$6s^2 \ ^1S_0 \leftrightarrow 6s6p \ ^3P_0$	578	0.32	1.6	0	0.31
$^{88}\text{Sr}^+$	$5s \ ^2S_{1/2} \leftrightarrow 4d \ ^2D_{3/2}$	674	16	25	0	0.43
$^{171}\text{Yb}^+$	$4f^{14}6s \ ^2S_{1/2} \leftrightarrow 4f^{13}6s \ ^2F_{7/2}$	467	2.0	71	0	-5.30
$^{199}\text{Hg}^+$	$5d^{10}6s \ ^2S_{1/2} \leftrightarrow 5d^96s \ ^2D_{3/2}$	282	2.8	19	0	-3.19
$^{162}\text{Dy}$	$4f^{10}5d16s \leftrightarrow 4f^{9}5d^26s$	$4.0 \cdot 10^8$	$4.0 \cdot 10^5$	-	0	$8.5 \cdot 10^5$
$^{164}\text{Dy}$	$4f^{9}5d^26s \leftrightarrow 4f^{10}5d6s$	$1.3 \cdot 10^9$	$1.3 \cdot 10^7$	-	0	$-2.6 \cdot 10^5$
$^{229\text{th}}\text{Th}^{3+}$	nuclear	26	1	1	$10^5$	$10^4$









ultra-light scalar fields      rods      clocks      other probes      conclusions

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instrumental ingredients for frequency comparison

necessary tools for precise frequency comparisons:  
 2 stable atomic clocks + frequency comparison method

The diagram illustrates the Fourier transform of a pulse train. The top plot shows the electric field  $E(t)$  versus time  $t$ . It features three pulses, each with a duration of  $1/f_c$ . The time interval between the centers of the pulses is  $1/f_{rep}$ . The phase difference between the pulses is  $\Delta\phi/2\pi f_c$ . The bottom plot shows the electric field  $E(f)$  versus frequency  $f$ . It features a central peak at  $f_0 = f_{rep} \Delta\phi/2\pi$  with a width of  $1/T$ .

The blackboard contains some faint mathematical equations, including  $\omega \times (t) = \omega$  and  $\sum \Delta\phi$ . A lecturer is standing next to the blackboard, gesturing towards it.







ultrastraight scalar fields    rods    clocks    ultra probes    conclusions

dysprosium

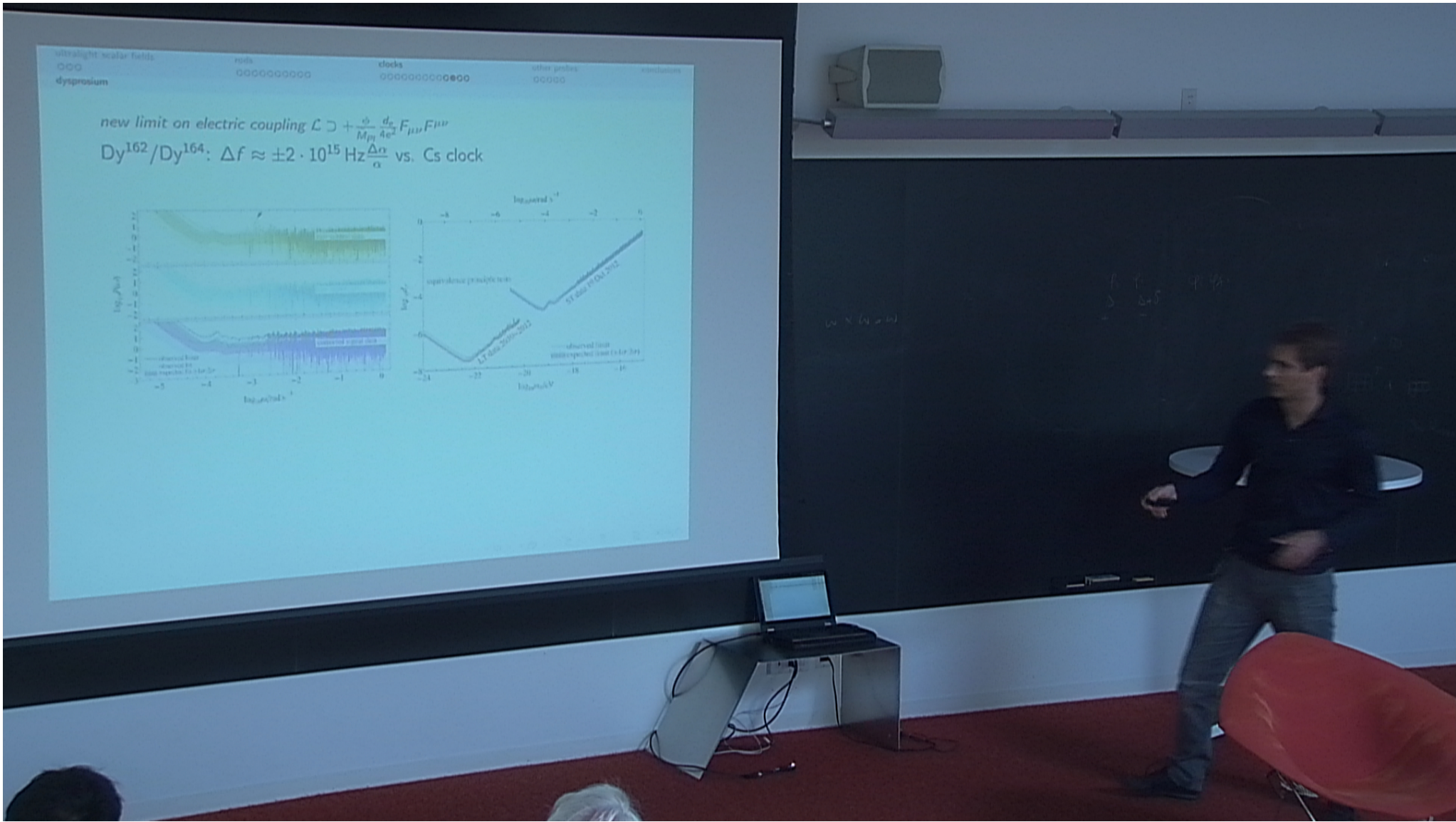
new limit on electric coupling  $\mathcal{L} \supset + \frac{\phi}{M_{Pl}} \frac{d_e}{4e^2} F_{\mu\nu} F^{\mu\nu}$

$Dy^{162}/Dy^{164}$ :  $\Delta f \approx \pm 2 \cdot 10^{15} \text{ Hz} \frac{\Delta\alpha}{\alpha}$  vs. Cs clock

The slide displays energy level diagrams for  $^{162}\text{Dy}$  and  $^{164}\text{Dy}$ . The left diagram shows the ground state splitting for  $J=8$  and  $J=9$  levels, with hyperfine splitting constants of  $41^{+10}\text{mK}$  and  $41^{+10}\text{mK}$  respectively. The right diagram shows the  $^{162}\text{Dy}$  and  $^{164}\text{Dy}$  clock transitions, with hyperfine splitting constants of  $41^{+10}\text{mK}$  and  $41^{+10}\text{mK}$  respectively. The experimental setup diagram (a-g) shows a sequence of optical elements: (a) input fiber, (b) 833 nm fiber, (c) 669 nm fiber, (d) lens, (e) fiber, (f) fiber, and (g) output fiber.

A blackboard with handwritten notes, including the equation  $\Delta f \approx \pm 2 \cdot 10^{15} \text{ Hz} \frac{\Delta\alpha}{\alpha}$ . A presenter in a dark shirt and light pants stands to the right of the blackboard, pointing towards the screen. A red chair is visible in the foreground.



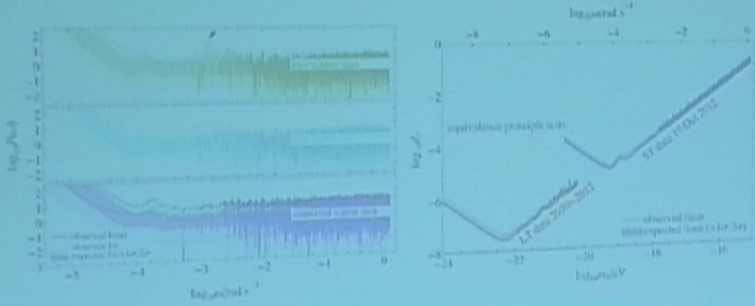


ultra-light scalar fields    rods    clocks    other probes    conclusions  
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dysprosium

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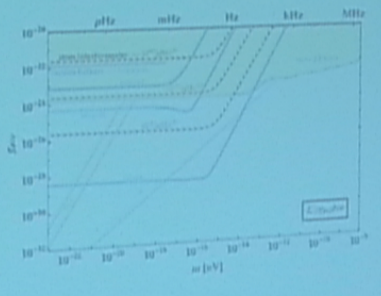
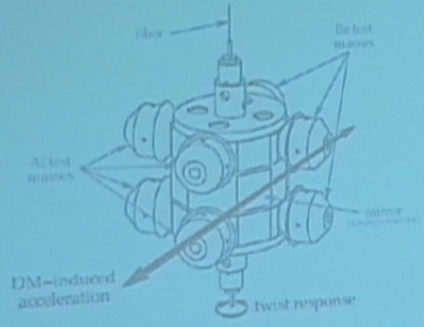


DM-induced forces

DM-induced forces in accelerometers

$$V_A = m_A \left[ 1 + \alpha_A \sqrt{4\pi G_N \phi_0} \cos(m_\phi t - m_\phi \mathbf{v} \cdot \mathbf{x}) \right]$$

$$\alpha_A \sim d_g + 10^{-1} d_{m_q} + 10^{-3} d_e + \frac{m_e}{2m_p} d_{m_e} + \dots$$



[arXiv:1512.06165]

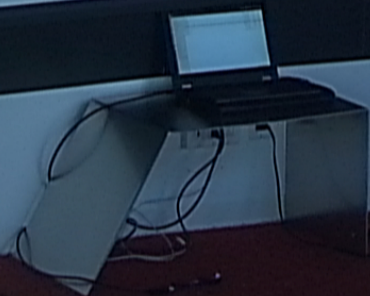
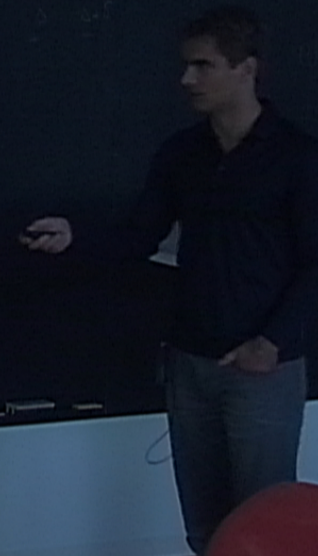
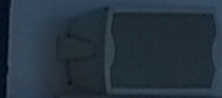




[arXiv:1411.2263]

## conclusions

- ① light moduli fields are good dark matter candidates and can arise in many extensions of the Standard Model
- ② **acoustic resonators** are sensitive probes of temporal changes in atomic length scales: **absorbers of modulus waves**
  - compilation of medium-band and tunable setups could cover to 6 decades in mass ( $f \gtrsim 100$  Hz)
  - (astero)seismology can provide a window at  $f \lesssim 1$  Hz
  - signal scales as  $\sqrt{\rho_\phi/\rho_{DM}}$ , linear in modulus couplings  $d_{m_e}, d_e$
  - current technology provides a reach way beyond existing constraints
  - already sensitive to natural parameter space for electron mass modulus!
- ③ **atomic clock pairs** are sensitive probes of temporal changes in atomic energy scales: **measures of modulus field values**
  - broadband searches sensitive to  $\gtrsim 8$  decades in mass ( $f \lesssim 1$  Hz)
  - signal scales as  $\sqrt{\rho_\phi/\rho_{DM}}$ , linear in modulus couplings  $d_g, d_{m_q}, d_{m_e}, d_e$
  - already leading limits on electromagnetic gauge modulus
  - future  $\rightarrow$  natural parameter space for quark mass modulus!
- ④ complimentary probes: equivalence principle tests, structure formation, superradiance, accelerometers, pulsar timing





[arXiv:1411.2263]

## conclusions

- 1 light moduli fields are good dark matter candidates and can arise in many extensions of the Standard Model
- 2 **acoustic resonators** are sensitive probes of temporal changes in atomic length scales: **absorbers of modulus waves**
  - compilation of medium-band and tunable setups could cover to 6 decades in mass ( $f \gtrsim 100$  Hz)
  - (astero)seismology can provide a window at  $f \lesssim 1$  Hz
  - signal scales as  $\sqrt{\rho_\phi/\rho_{DM}}$ , linear in modulus couplings  $d_{m_e}, d_e$
  - current technology provides a reach way beyond existing constraints
  - already sensitive to natural parameter space for electron mass modulus!
- 3 **atomic clock pairs** are sensitive probes of temporal changes in atomic energy scales: **measures of modulus field values**
  - broadband searches sensitive to  $\gtrsim 8$  decades in mass ( $f \lesssim 1$  Hz)
  - signal scales as  $\sqrt{\rho_\phi/\rho_{DM}}$ , linear in modulus couplings  $d_g, d_{m_q}, d_{m_e}, d_e$
  - already leading limits on electromagnetic gauge modulus
  - future  $\rightarrow$  natural parameter space for quark mass modulus!
- 4 complimentary probes: equivalence principle tests, structure formation, superradiance, accelerometers, pulsar timing

