

Title: PSI 2015/2016 Quantum Gravity - Lecture 1

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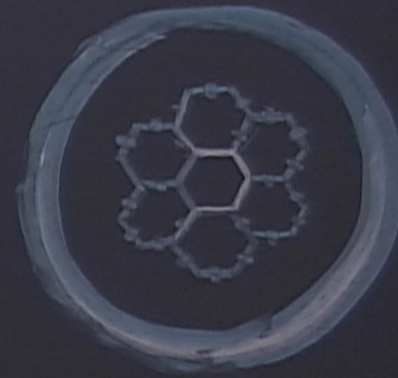
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Abstract:

# - Quantum Gravity - Overview

We will focus on 3D Euclidean Gravity  
with a zero cosmological constant.

- I - Introduction
- II - Action principles - 1<sup>st</sup> order action
- III - Symmetries - Gauge symmetries
- IV - Canonical Analysis - Equations of motion
- V - Quantum Geometry -
- VI - Spinfoam model
- VII - Outlook on 4D

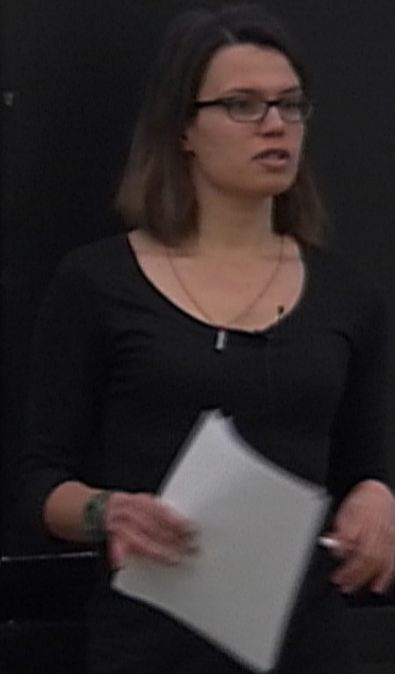


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[ Loop Quantum Gravity LQG  
Spinfoam SF ]

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## I. A What is Quantum Gravity?

• What we know about the elementary physical world?

⊕ → QM

→ Standard Model

⊗ → GR

# I. A What is Quantum Gravity?

What we know about the elementary physical world?

⊛ → QM

→ Standard Model

⊛ → GR

→ Dark matter

→ Unification

→ Quantum Gravity

Einstein spacetime = gravitational field

Gravity is a property of spacetime.

Quantum spacetime?

classical spacetime



→ Standard Model  
⊗ → GR

→ Unification  
→ Quantum Gravity

Einstein spacetime = gravitational field

Quantize a field  
without the presence of any  
background spacetime



→ diffeomorphism invariance



. GR : geometry is a manifestation  
of the gravitational field.

Theory of QG = Quantum Geometry

GR.

— quantum theory does prevent the measurability of the gravitational field in an arbitrary small region—

QM

→ Measure a field at  $x$ : precision  $L$   
 $\Delta x, \Delta p$  for particle

Heisenberg uncertainty principle  $\Delta x > \frac{\hbar}{\Delta p} \Rightarrow \Delta p > \frac{\hbar}{L}$   
 $\Delta p^2 > (\Delta p)^2 > \frac{\hbar^2}{L^2}$

Large momentum  $\Rightarrow$  large energy  $E$   
Relativistic limit  $E \sim cp$

+ GR

Energy acts as a gravitational mass  $M \sim \frac{E}{c^2}$

Energy concentrated in a sphere of radius  $R \sim \frac{GM}{c^2}$

GR.

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$$\Rightarrow L_{\min} = \sqrt{\frac{\hbar G}{c^3}} = L_{\text{plank}} \simeq 10^{-33} \text{ cm}$$



Energy acts as a quantum of mass  $\sim \frac{E}{c^2}$

Energy concentrated in a sphere of radius  $R \sim \frac{GM}{c^2}$

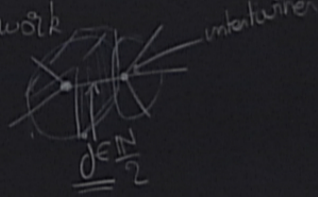
$$\Rightarrow L_{\min} = \sqrt{\frac{\hbar G}{c^3}} = L_{\text{Planck}} \approx 10^{-35} \text{ cm}$$

$\rightarrow$  Spacetime semi-classical approximation  $\Rightarrow$  Quantum space? Quantum time

Quantum states of spacetime

$\rightarrow$  LQG (4D)

Fundamental excitations of space  
Spinnetzwerk



SU(2)

+ Dynamics?  
Spin foam



## I.3 Why QG?

→ no calls from experimentally accessible situations.

$$\frac{F_{\text{grav}}}{F_{\text{electr}}} (\text{proton-electron}) = 10^{-40}.$$

References: Bianca lecture notes

\* R. Gambini and J. Pullin  
"A first course in LQG"  
(Oxford University Press)

\* C Rovelli & F. Vidotto  
An elementary introduction QG and Spin Foam theory

\* A. Perez