Title: Emergent â€œlightâ€• and the high temperature superconductors

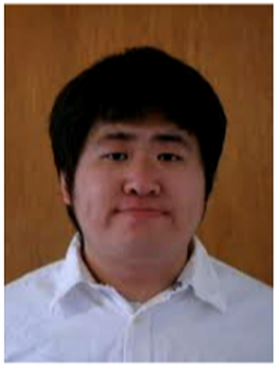
Date: Jan 19, 2016 03:30 PM

URL: http://pirsa.org/16010075

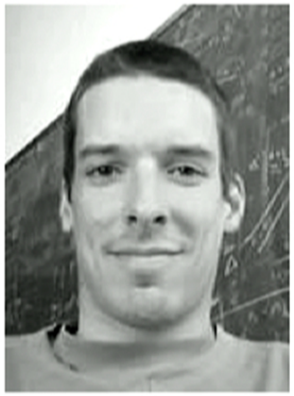
Abstract: <p>Long-range quantum entanglement is now being recognized as a key characteristic of many novel states of quantum matter. The description of this entanglement requires the introduction of emergent â€œgauge fieldsâ€•, much like those found in Maxwellâ€™s theory of light. I will highlight some recent experiments on the copper-based high temperature superconductors, and interpret them using theories of emergent gauge fields.</p>

Debanjan Chowdhury

Andrea Allais

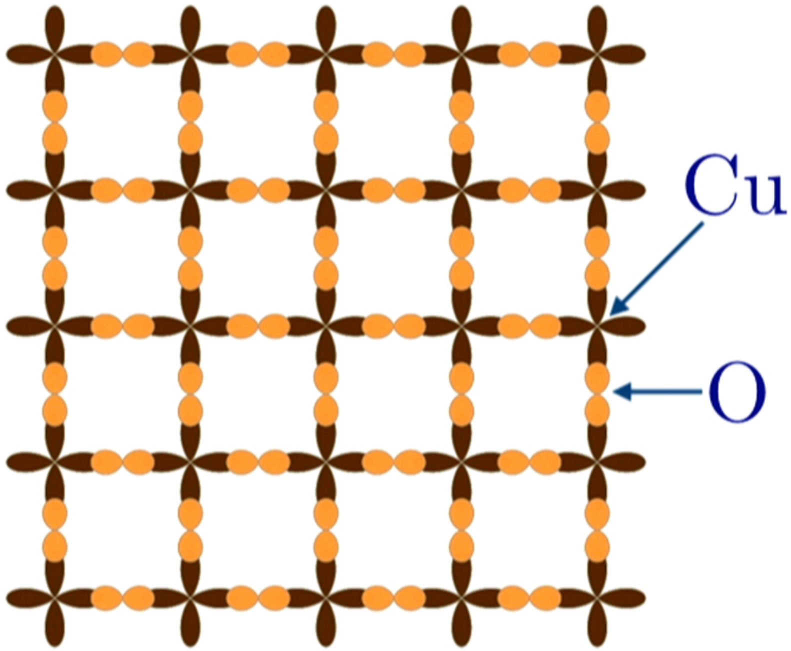


Yang Qi

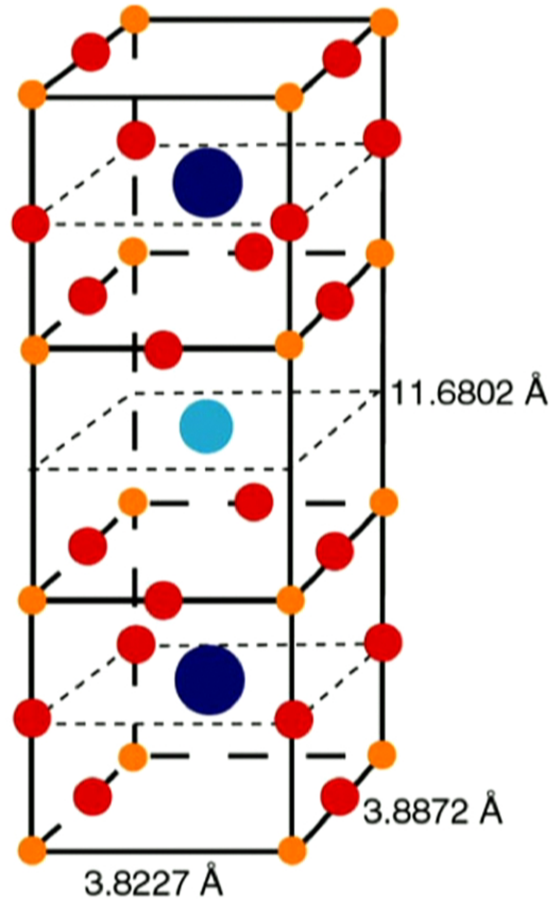


Matthias Punk

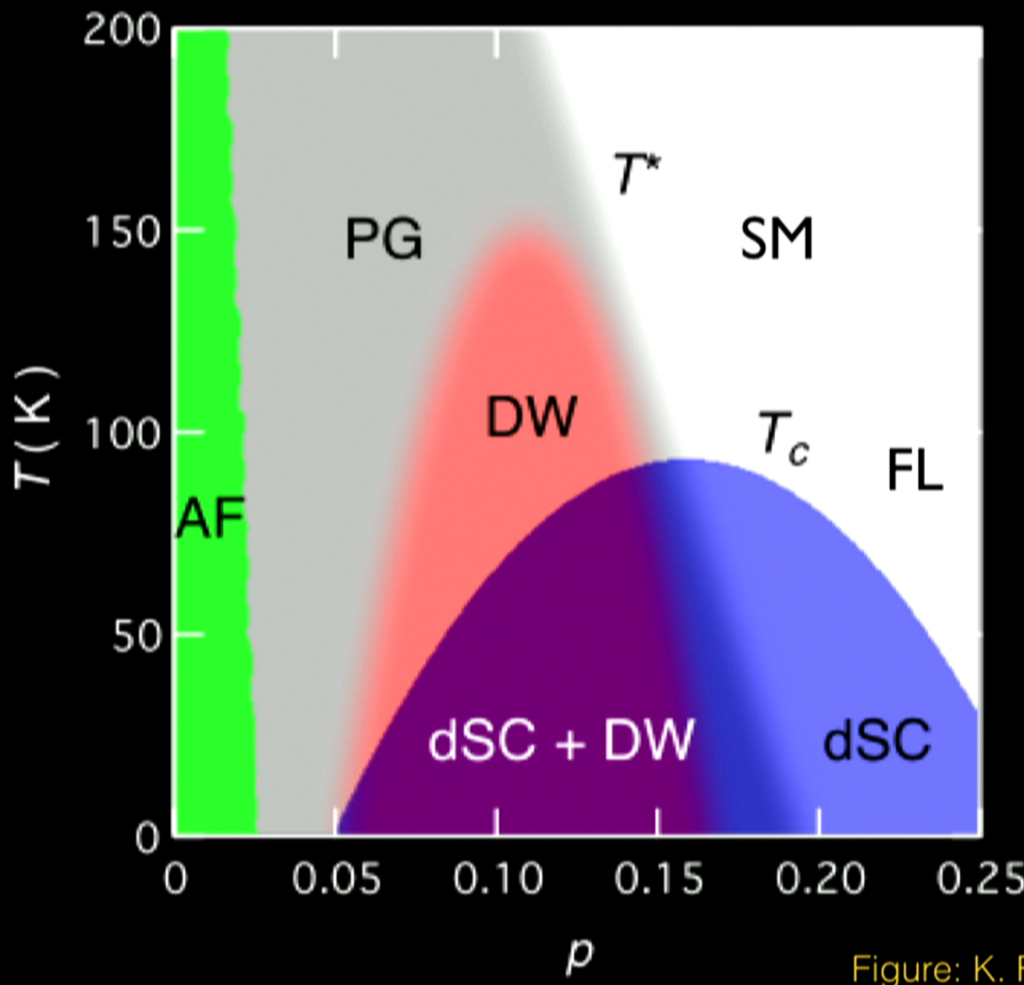
High temperature superconductors



CuO_2 plane



$YBa_2Cu_3O_{6+x}$



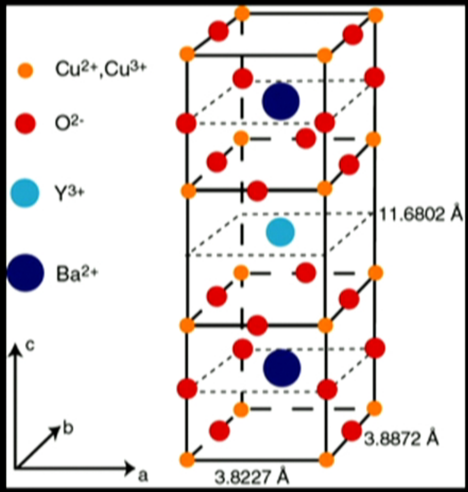


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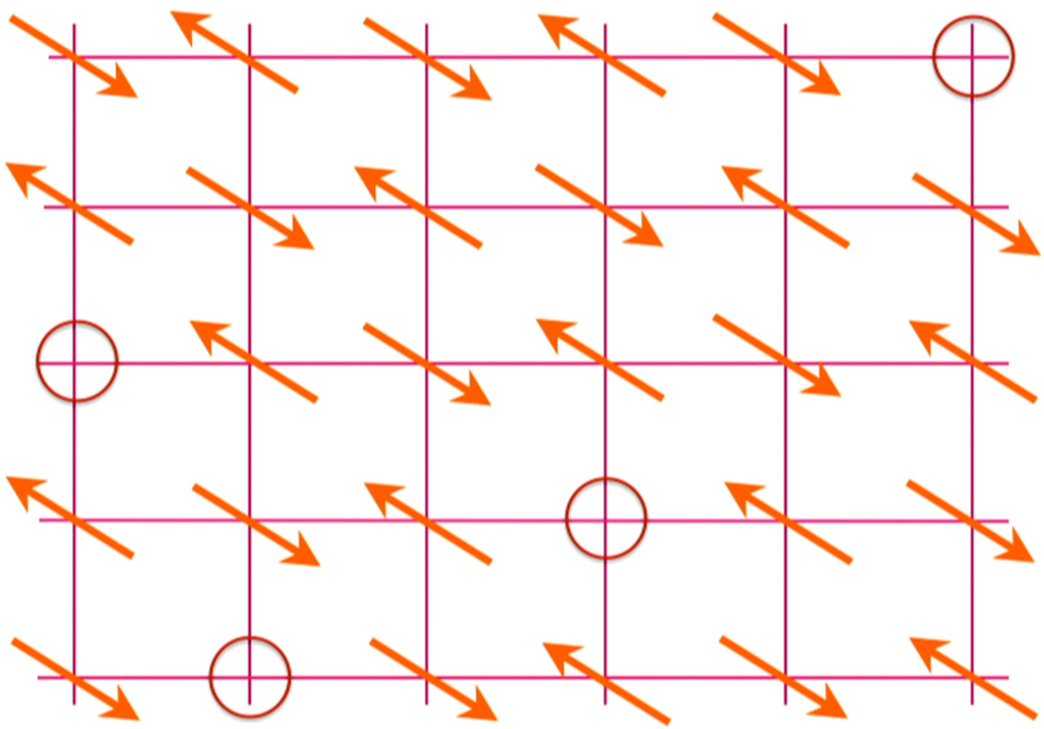
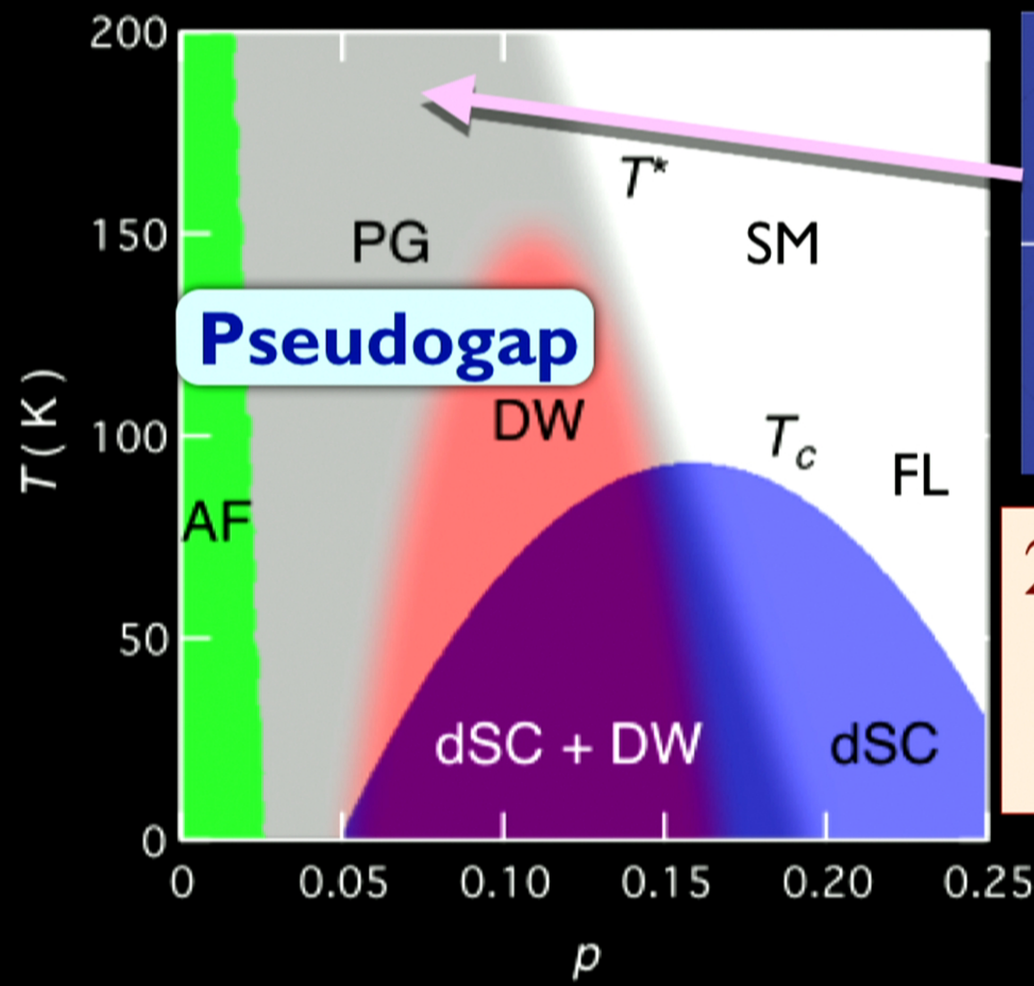
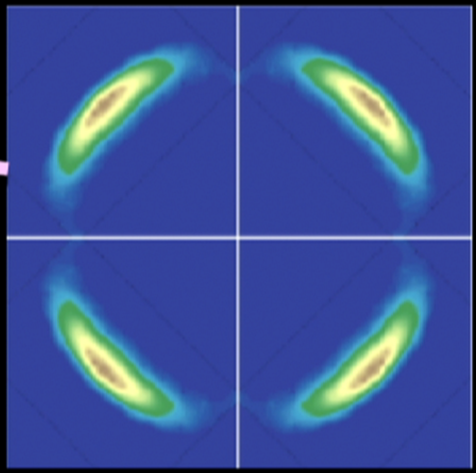
Figure: K. Fujita and J. C. Seamus Davis



Anti-ferromagnet with p holes per square

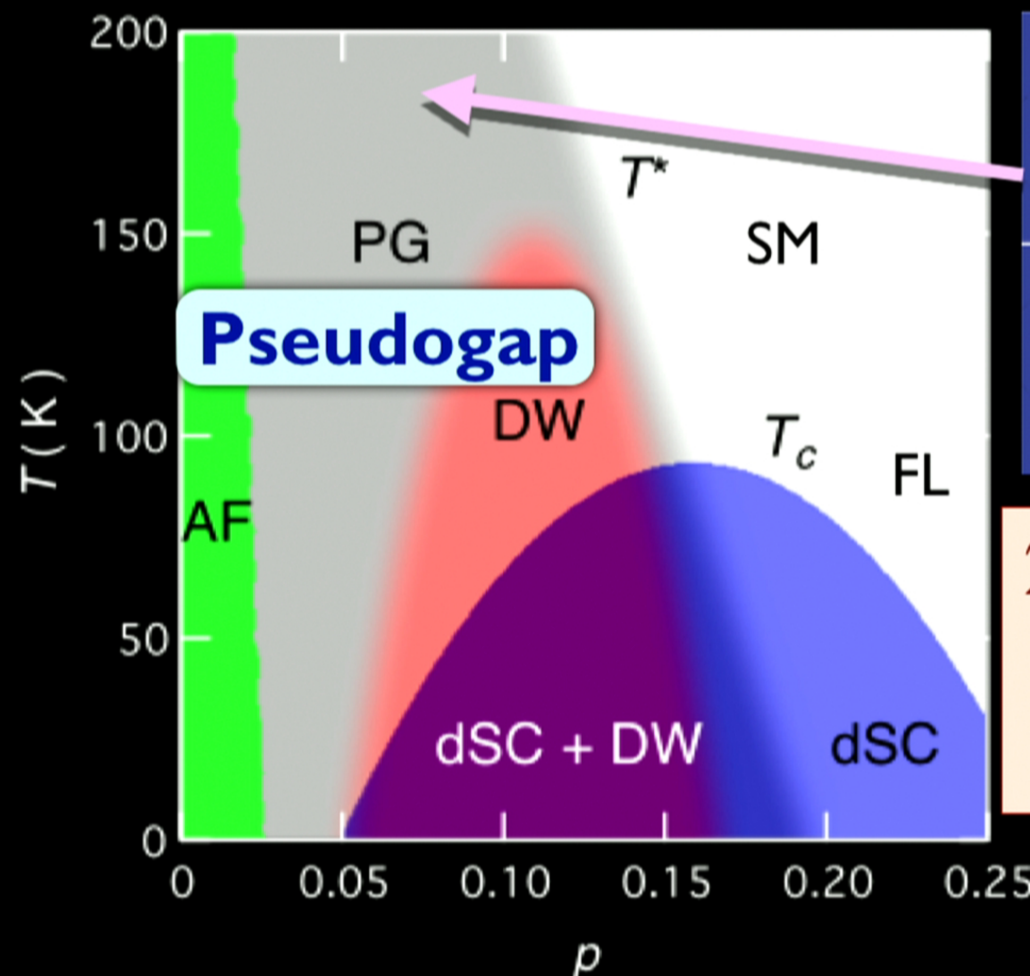
Kyle M. Shen, F. Ronning, D. H. Lu, F. Baumberger, N. J. C. Ingle, W. S. Lee, W. Meevasana, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi, Z.-X. Shen, Science **307**, 901 (2005)

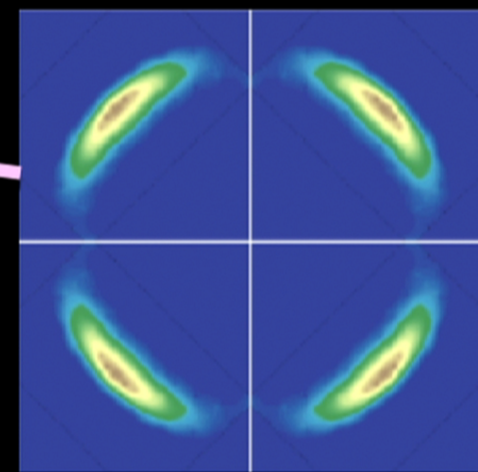




2. Pseudogap metal at low p

Kyle M. Shen, F. Ronning, D. H. Lu, F. Baumberger, N. J. C. Ingle, W. S. Lee, W. Meevasana, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi, Z.-X. Shen, Science **307**, 901 (2005)





2. Pseudogap metal at low p

Is the higher temperature pseudogap (with ``Fermi arc'' spectra) described by

(A) Thermal fluctuations of the low temperature orders (superconductivity, density wave, antiferromagnetism…)

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(C) The possibilities (A) and (B) are merely two limits of the same physics?

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(A) Thermal fluctuations of the low

Answer (B) must have "emergent" gauge fields, and these are (in principle) detectable in low temperature experiments. There are also qualitative differences between (A) and (B) at higher temperatures.

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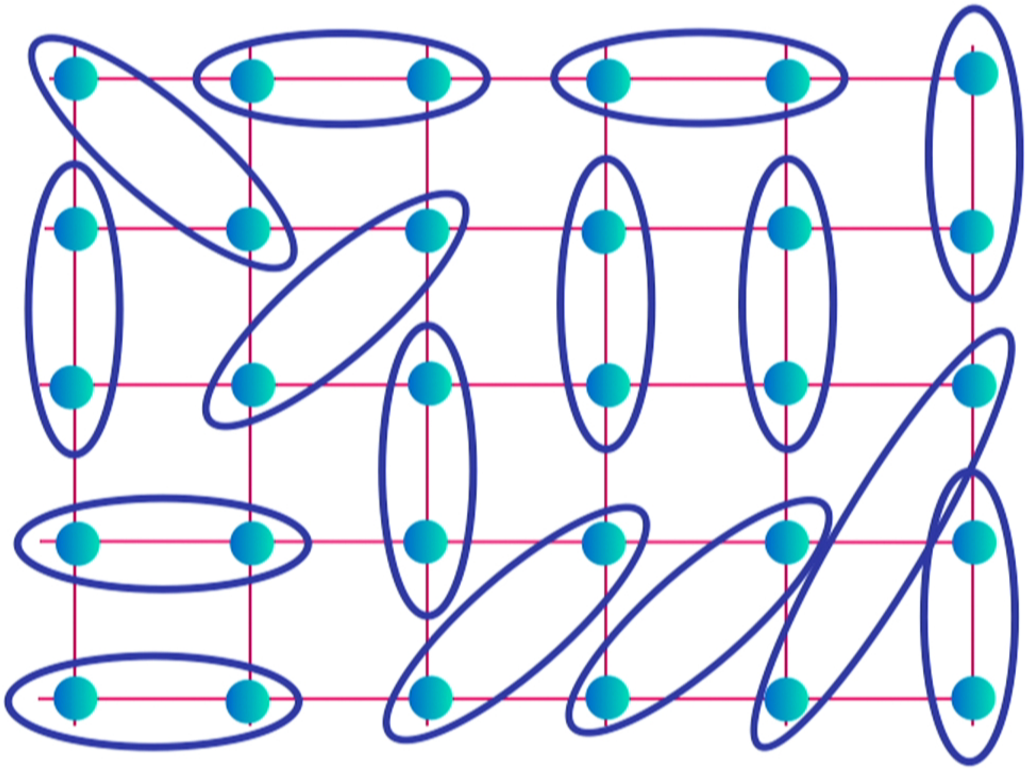
1. Emergent gauge fields and long-range entanglement in insulators

Insulating spin liquid

 $= \left(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle\right)/\sqrt{2}$



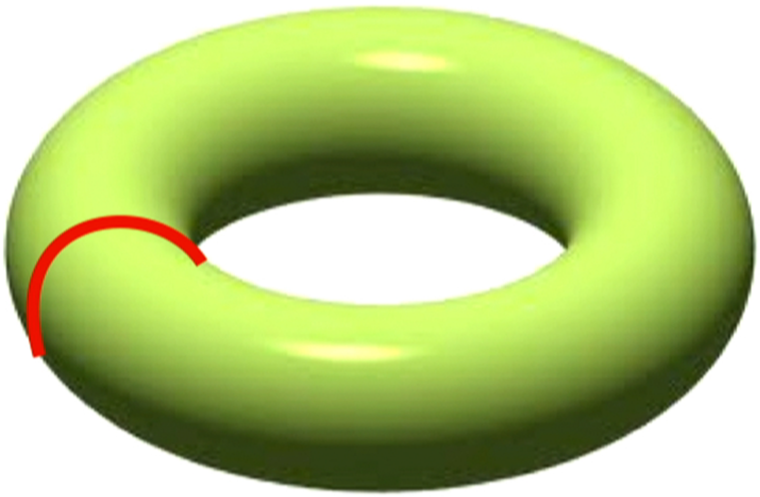
An insulator with emergent gauge fields and long-range entanglement

L. Pauling, Proceedings of the Royal Society London A **196**, 343 (1949)
P.W. Anderson, Materials Research Bulletin **8**, 153 (1973)

Ground state degeneracy

Place insulator on a torus;

Ground state degeneracy

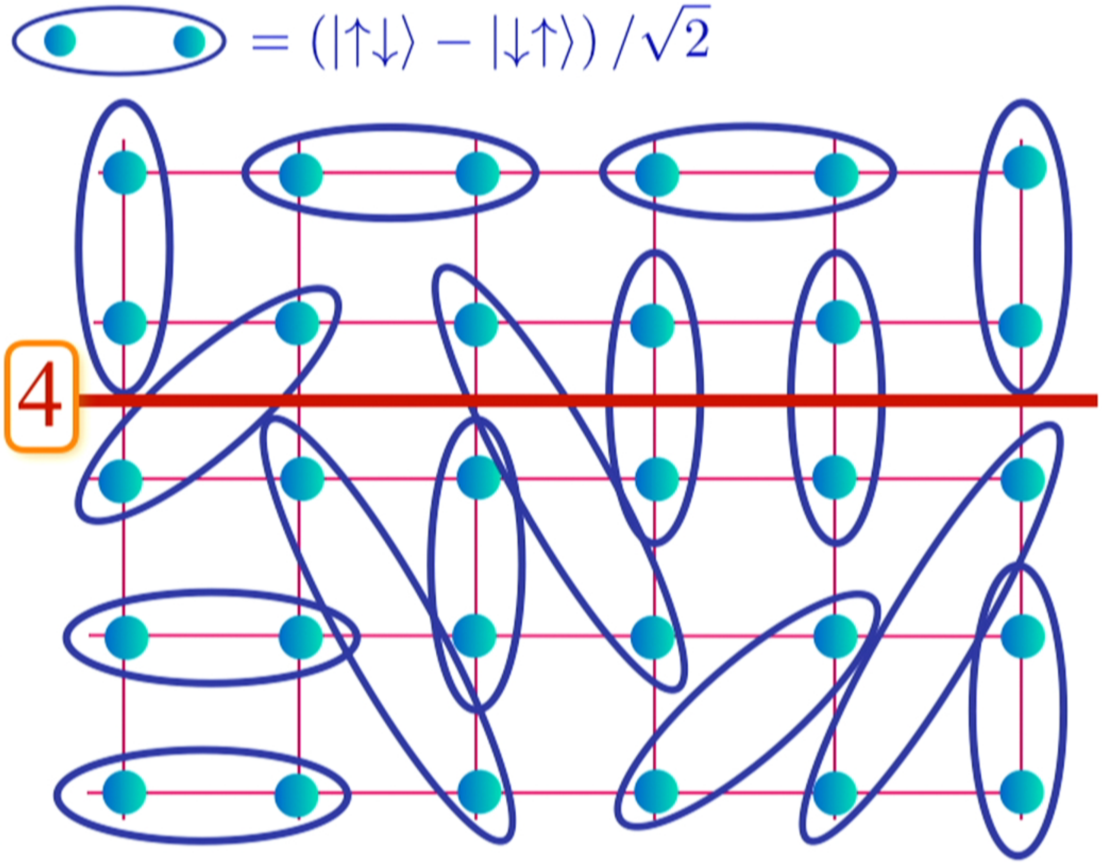


Place insulator on a torus;

obtain "topological" states nearly degenerate with the ground state: number of dimers crossing red line is conserved modulo 2

D.J. Thouless, PRB **36**, 7187 (1987)
S.A. Kivelson, D.S. Rokhsar and J.P. Sethna, Europhys. Lett. **6**, 353 (1988)

Ground state degeneracy



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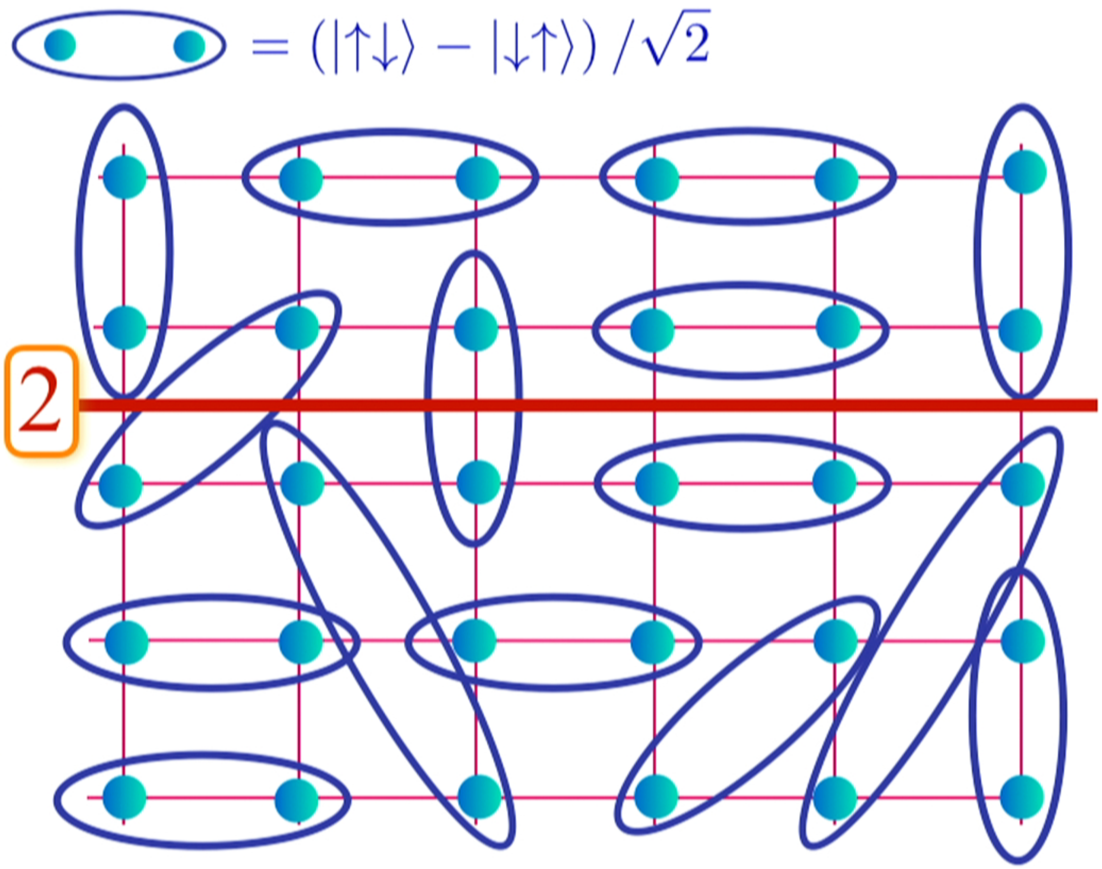

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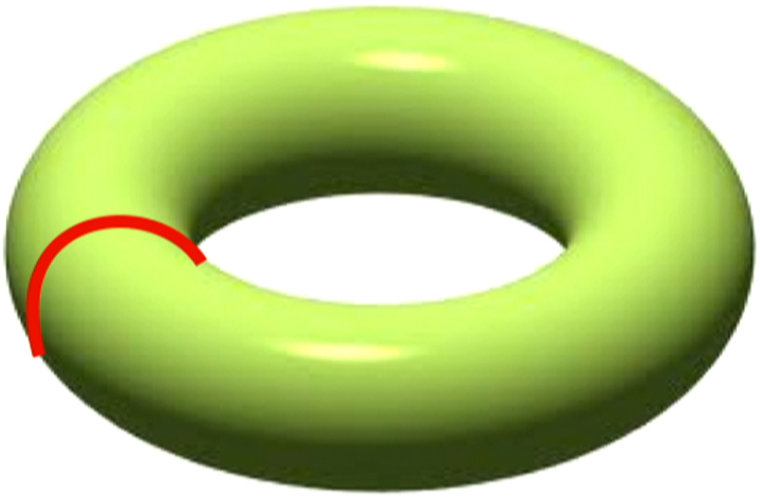

Place insulator on a torus; The degenerate states are conjugate to the flux of an emergent gauge field piercing the cycles of the torus

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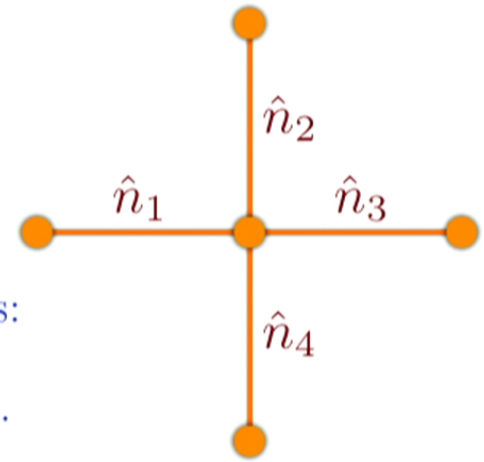
S.A. Kivelson, D.S. Rokhsar and J.P. Sethna, Europhys. Lett. **6**, 353 (1988)

Emergent gauge fields



Local constraint on dimer number operators:

$$\hat{n}_1 + \hat{n}_2 + \hat{n}_3 + \hat{n}_4 = 1.$$

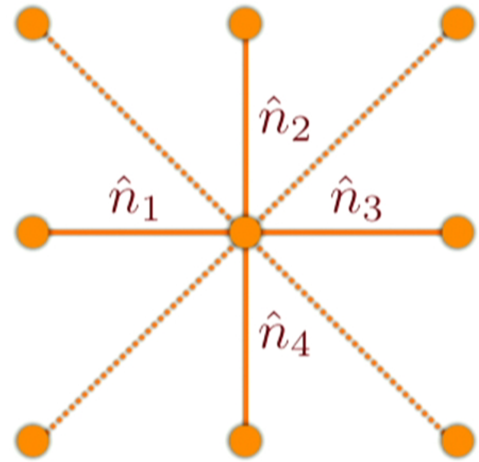
Identify dimer number with an 'electric' field, $\hat{E}_{i\alpha} = (-1)^{i_x + i_y}\, \hat{n}_{i\alpha}$, $(\alpha = x, y)$; the constraint becomes 'Gauss's Law':

$$\Delta_\alpha \hat{E}_{i\alpha} = (-1)^{i_x + i_y}.$$

The theory of the dimers is *compact* U(1) quantum electrodynamics in the presence of static background charges. The *compact* theory allows the analog of Dirac's magnetic monopoles as tunneling events/excitations.

G. Baskaran and P. W. Anderson, Phys. Rev. B **37**, 580(R) (1988)
E. Fradkin and S. A. Kivelson, Mod. Phys. Lett. B **4**, 225 (1990)

Emergent gauge fields



Including dimers connecting the same sublattice leads to a $\mathbb{Z}_2$ gauge theory in the presence of Berry phases of static background charges. This has a stable deconfined phase in 2+1 dimensions. By varying parameters it can undergoes a confinement transition to a valence bond solid, described by a frustrated Ising model.

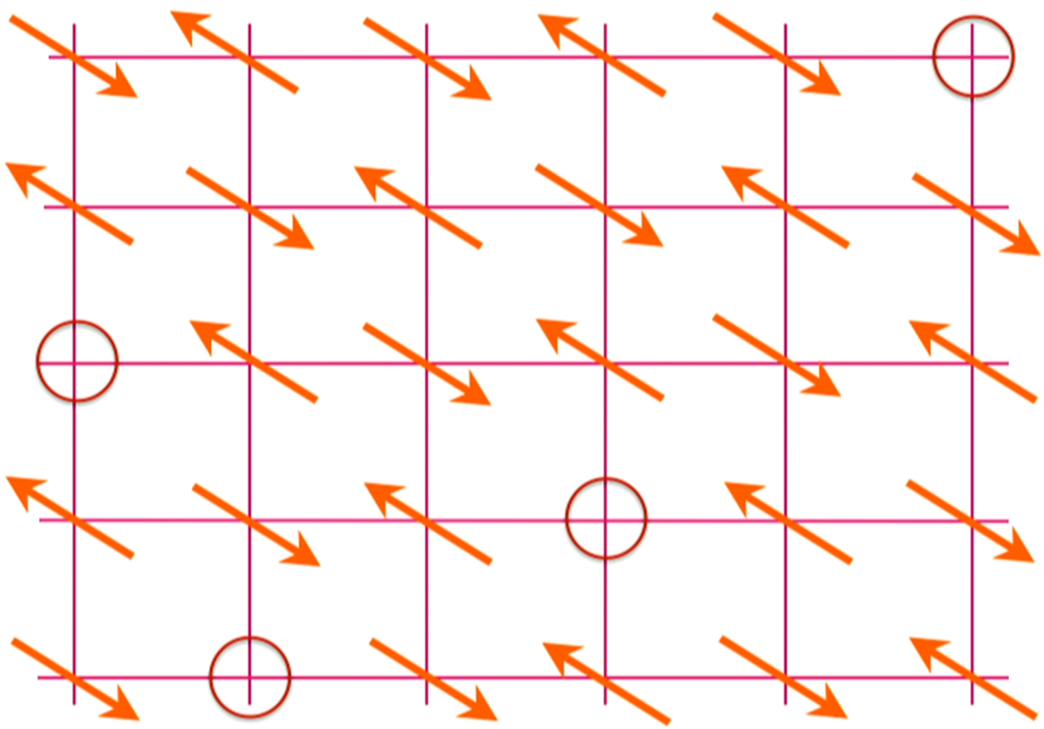
R. A. Jalabert and S. Sachdev, Phys. Rev. B **44**, 686 (1991)

S. Sachdev and M. Vojta, J. Phys. Soc. Jpn **69**, Supp. B, 1 (1999)

1. Emergent gauge fields and long-range entanglement in insulators

2. Fractionalized Fermi liquids (FL*)

Quasiparticles with a non-Luttinger volume, and emergent gauge fields



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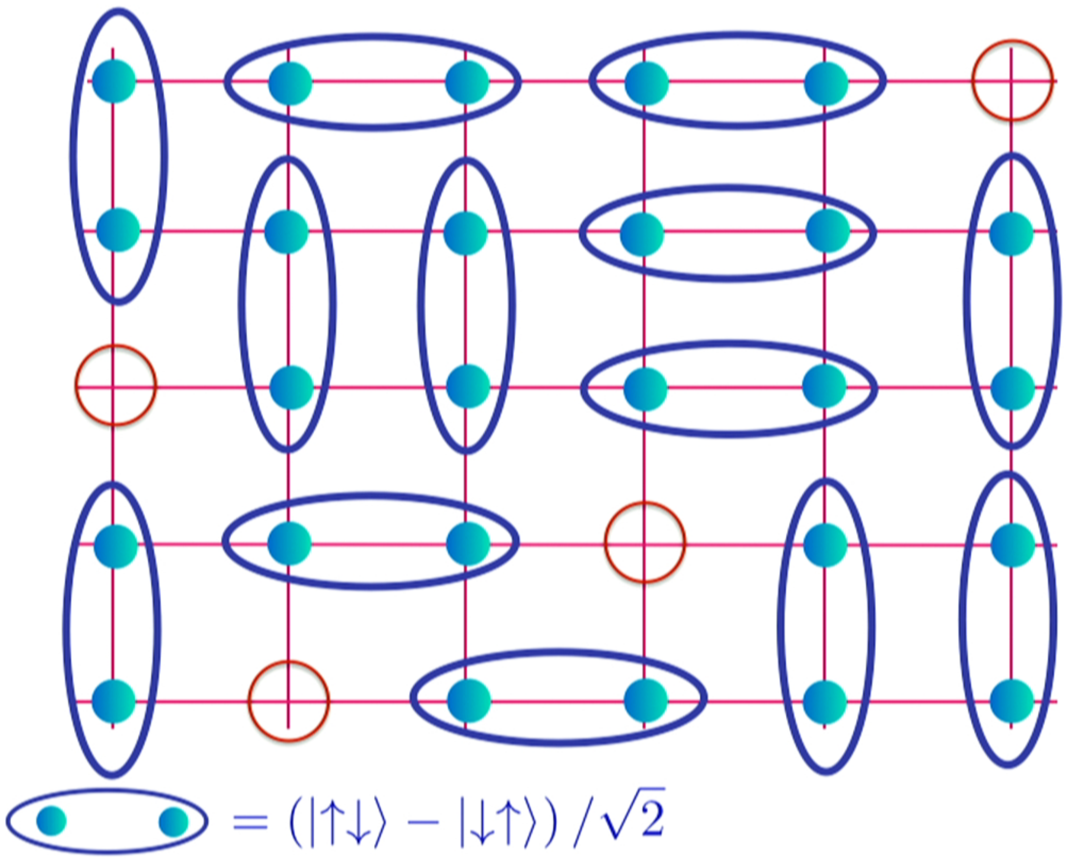

$= (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)/\sqrt{2}$

Spin liquid with density *p* of spinless, charge +e "holons". These can form a Fermi surface of size p, but this is not visible in electron photo-emission

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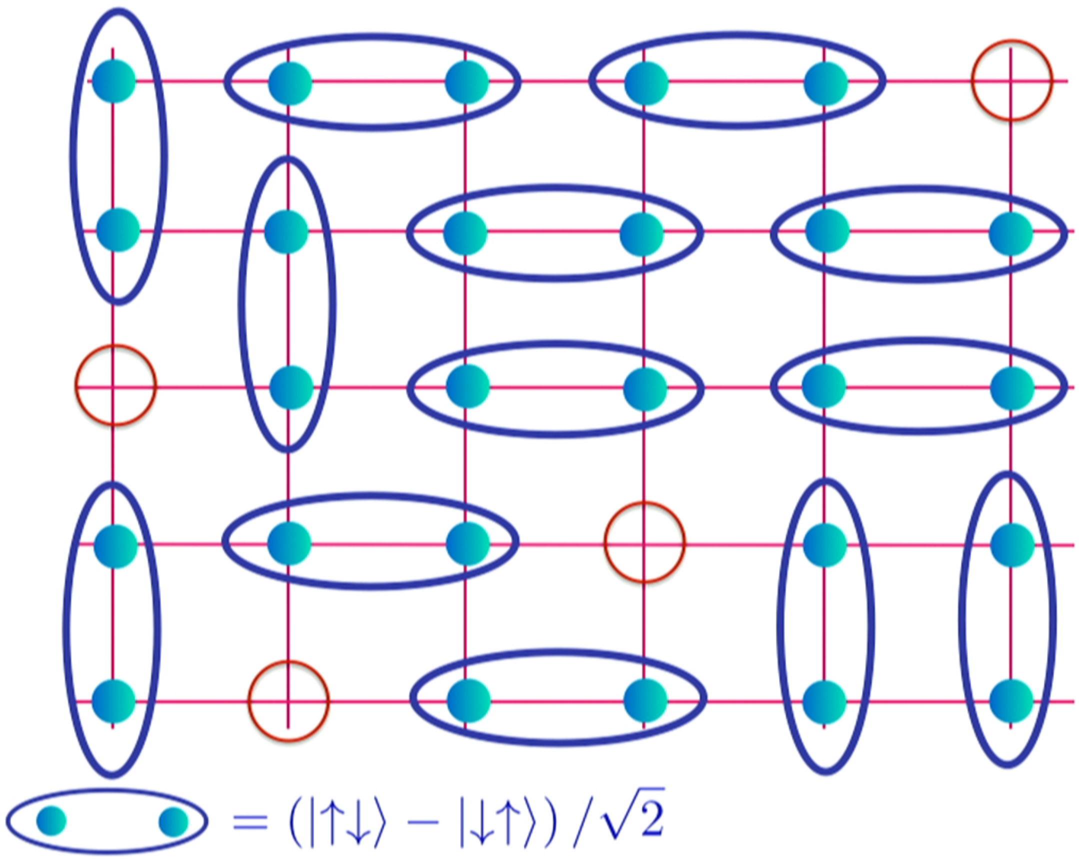

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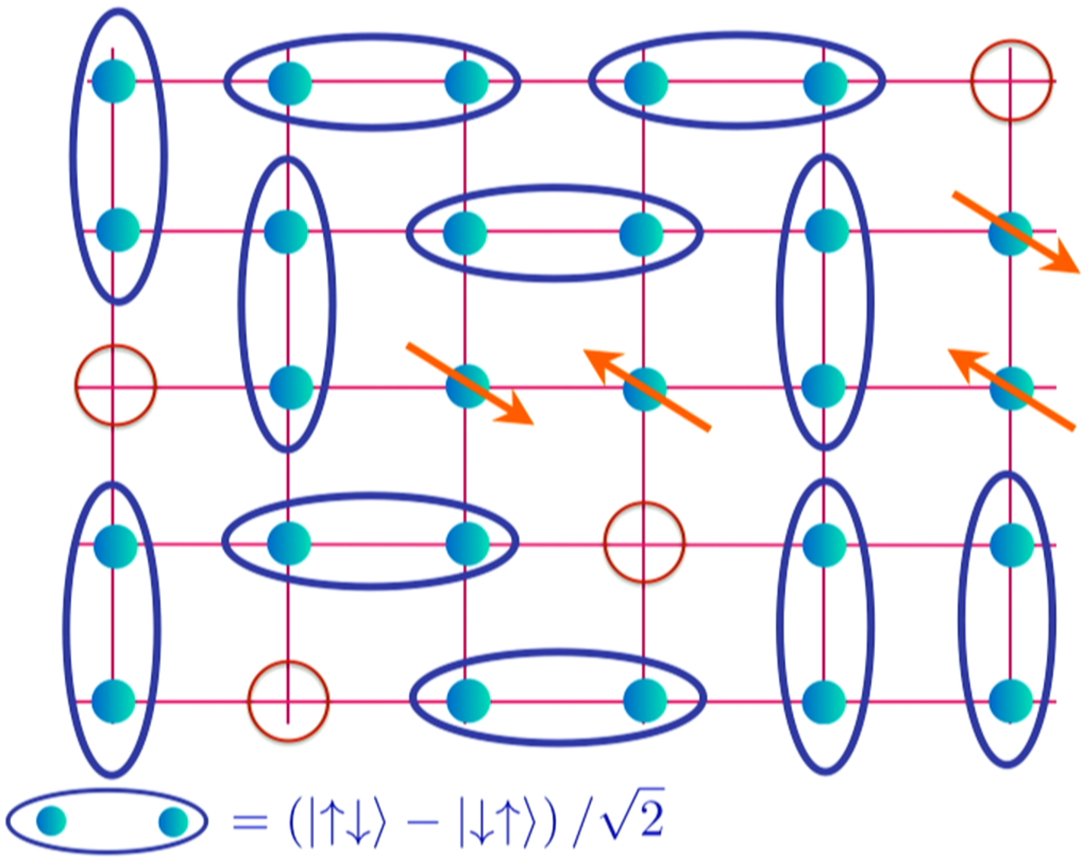
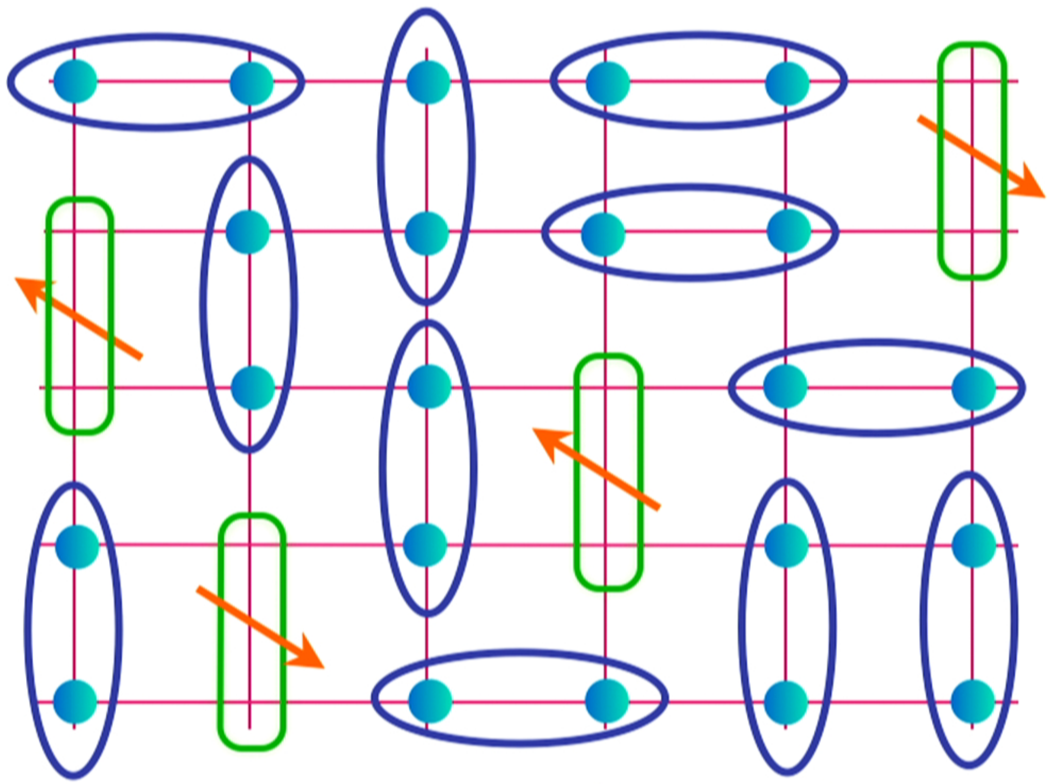


$$= \left(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle\right)/\sqrt{2}$$

Fractionalized Fermi liquid (FL*)

S. Sachdev PRB **49**, 6770 (1994); X.-G. Wen and P.A. Lee PRL **76**, 503 (1996)
R. K. Kaul, A. Kolezhuk, M. Levin, S. Sachdev, and T. Senthil, PRB **75**, 235122 (2007)



Mobile S=1/2, charge +e fermionic dimers: form a Fermi surface of size p visible in electron photo-emission

$$= \left(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle \right) / \sqrt{2}$$

$$= \left(|\uparrow \circ\rangle + |\circ \uparrow\rangle \right) / \sqrt{2}$$

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

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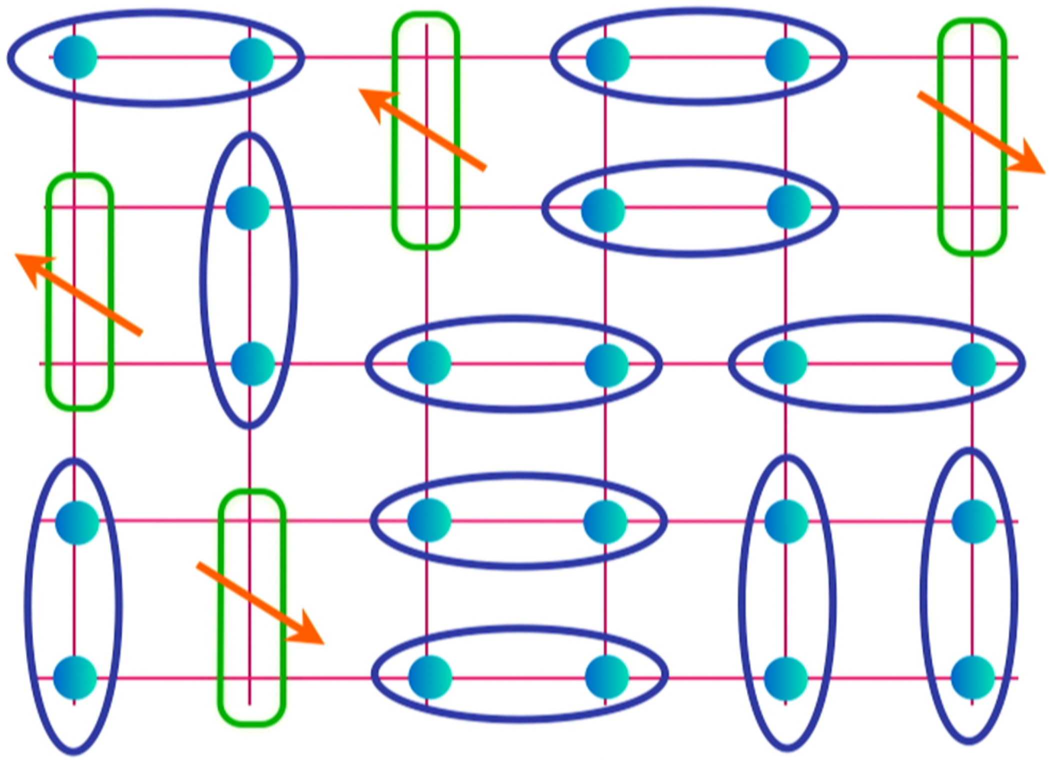

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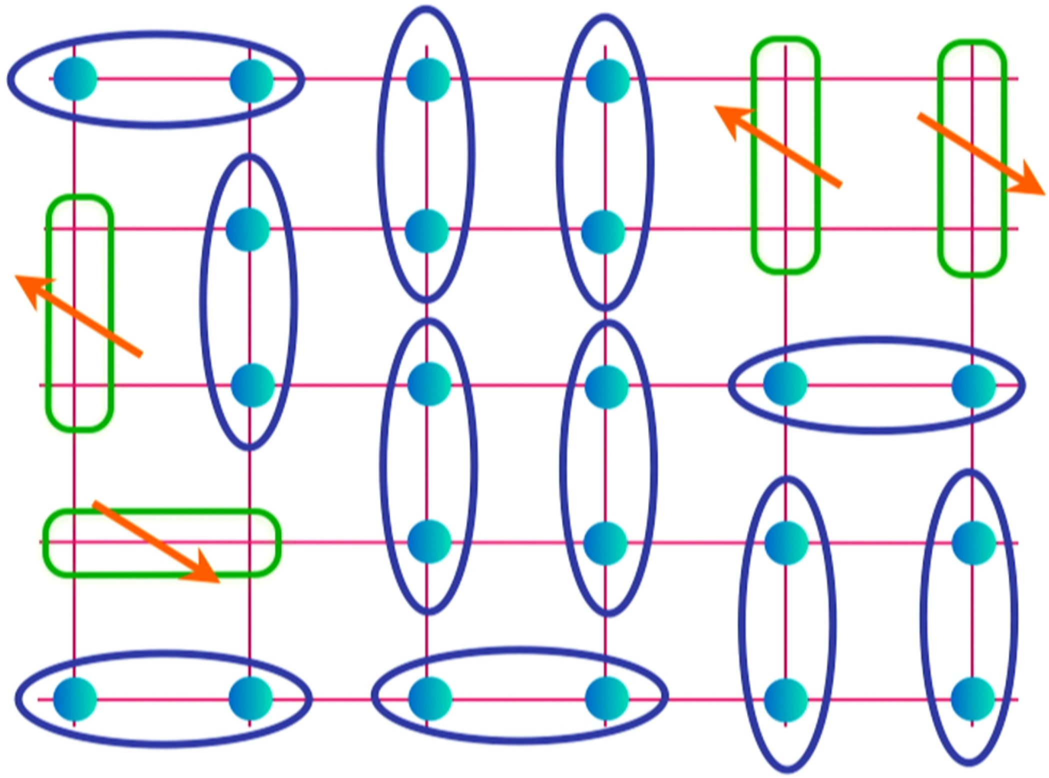

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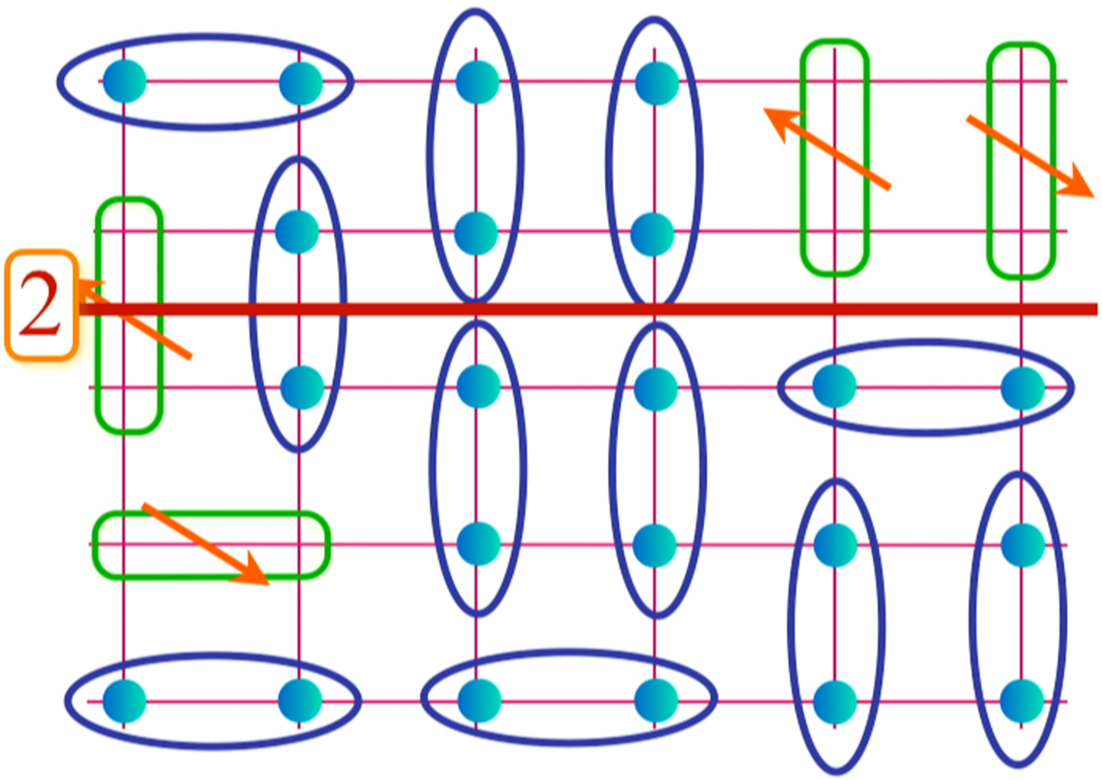

Place FL* on a torus:

obtain "topological" states nearly degenerate with quasiparticle states: number of dimers crossing red line is conserved modulo 2

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T. Senthil, M. Vojta, and S. Sachdev, *Phys. Rev. B* **69**, 035111 (2004)

Fractionalized Fermi liquid (FL*)

We have described a metal with:

- A Fermi surface of electrons enclosing volume p, and not the Luttinger volume of $1+p$
- Additional low energy quantum states on a torus not associated with quasiparticle excitations *i.e.* emergent gauge fields

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There is a general and fundamental relationship between these two characteristics.

M. Oshikawa, *Phys. Rev. Lett.* **84**, 3370 (2000)
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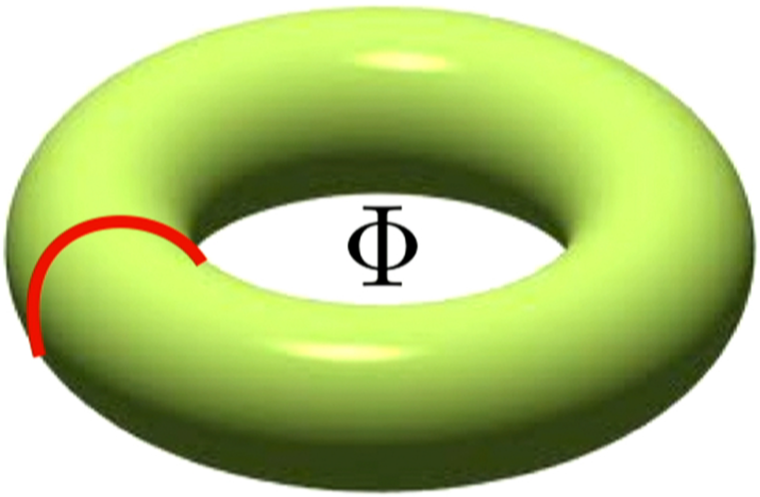

Following the evolution of the quantum state under adiabatic insertion of a flux quantum leads to a non-perturbative argument for the volume enclosed by the Fermi surface

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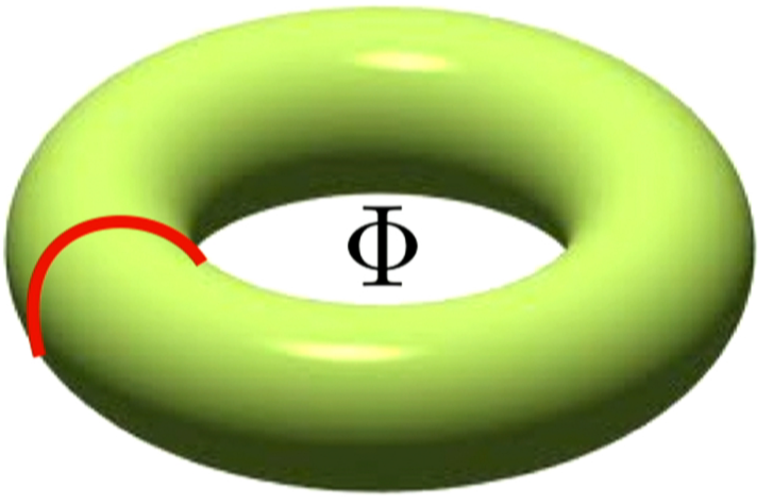

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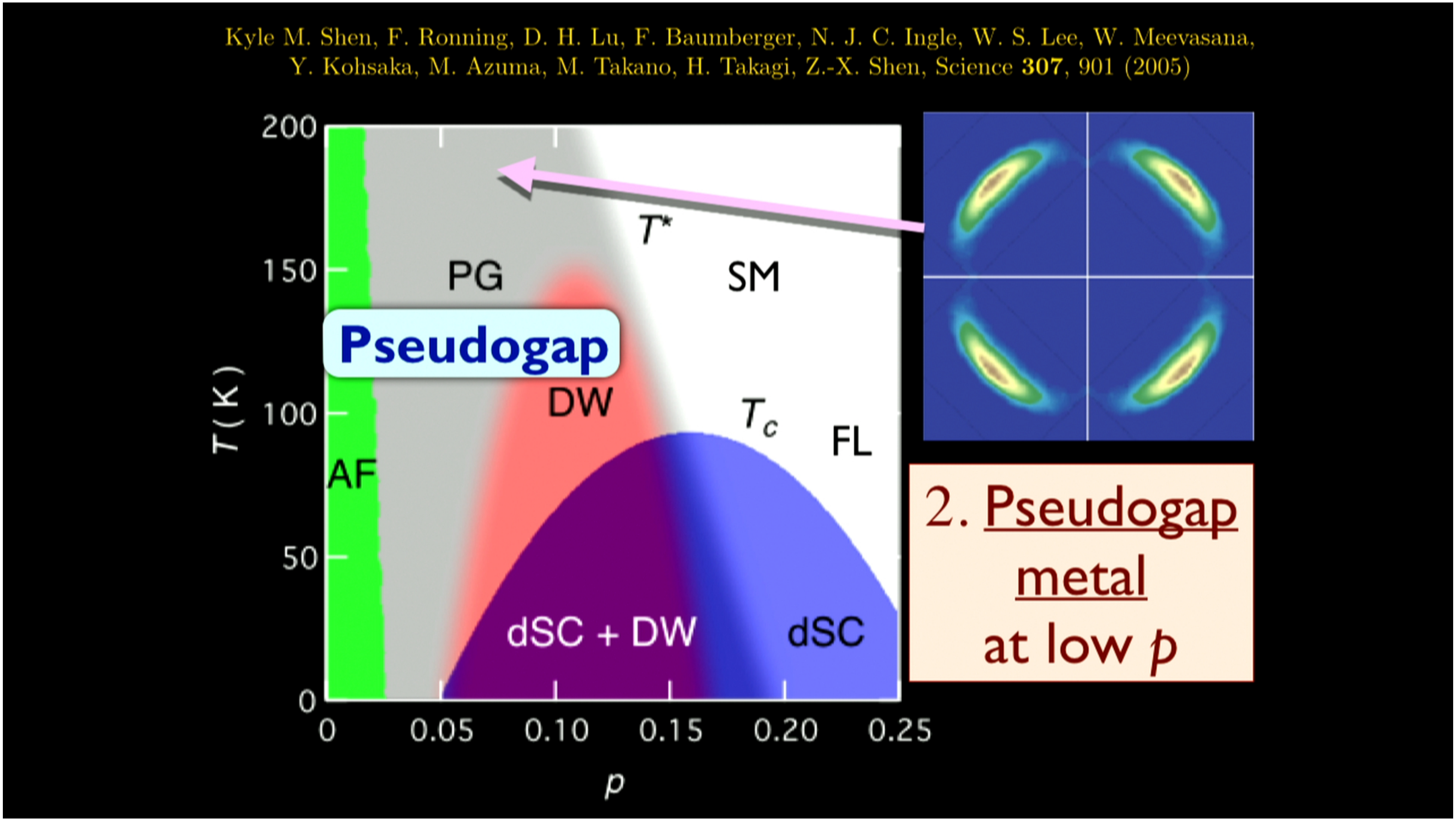

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200
150
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T (K)
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0.05
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0.20
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p
T*
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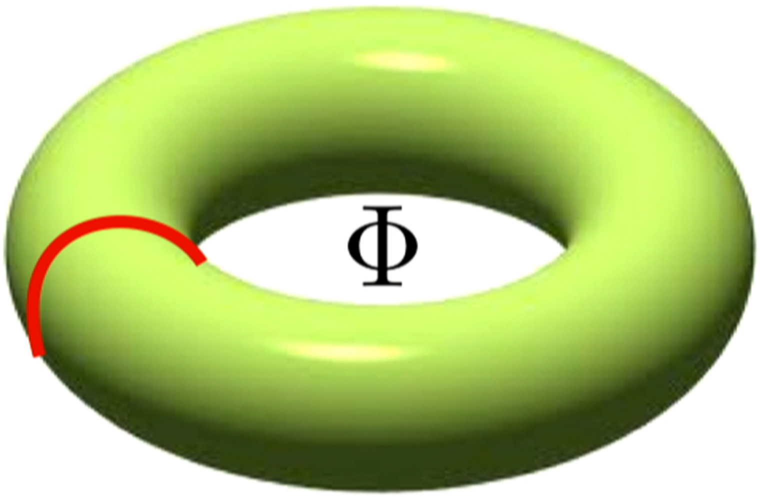
SM
Pseudogap
DW
T_c
FL
AF
dSC + DW
dSC
2. Pseudogap metal at low p

Fractionalized Fermi liquid (FL*)



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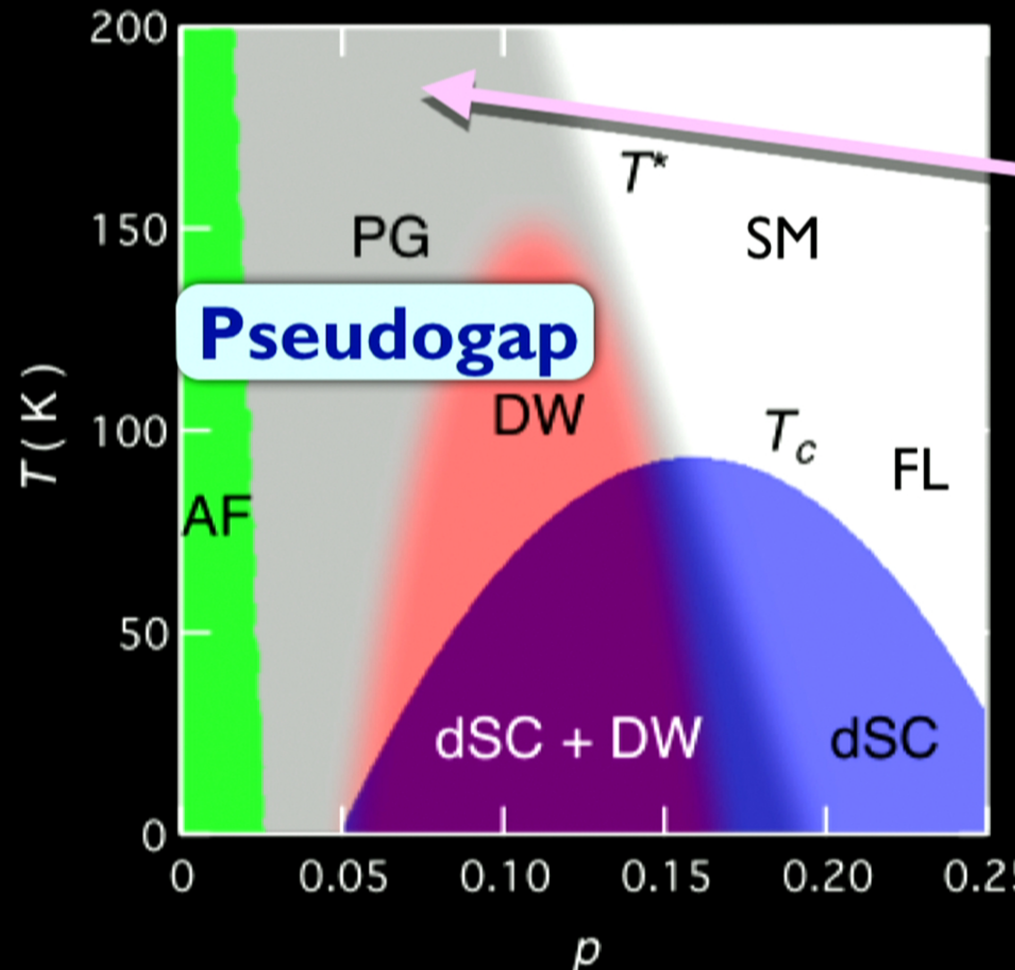
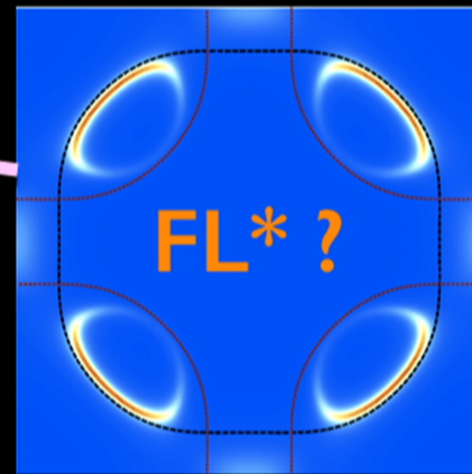
Y. Qi and S. Sachdev, Phys. Rev. B **81**, 115129 (2010)
M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)





A new metal — a fractionalized Fermi liquid (FL*) — with electron-like quasiparticles on a Fermi surface of size p

Optical evidence for Fermi surface of long-lived quasiparticles of density p

Spectroscopic evidence for Fermi liquid-like energy and temperature dependence of the relaxation rate in the pseudogap phase of the cuprates

Seyed Iman Mirzaei[a], Damien Stricker[a], Jason N. Hancock[a,b], Christophe Berthod[a], Antoine Georges[a,c,d], Erik van Heumen[a,e], Mun K. Chan[f], Xudong Zhao[f,g], Yuan Li[h], Martin Greven[f], Neven Barišić[f,i,j], and Dirk van der Marel[a,1]

PNAS 110, 5774 (2013)

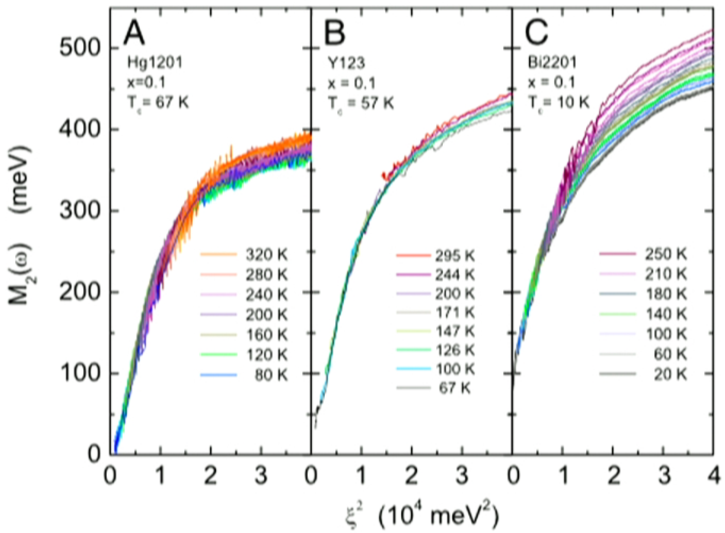


Fig. 6. Collapse of the frequency and temperature dependence of the relaxation rate of underdoped cuprate materials. Normal state $M_2(\omega, T)$ as a function of $\xi^2 \equiv (\hbar\omega)^2 + (p\pi k_B T)^2$

$$\sigma_{xx} \sim \frac{1}{(-i\omega + 1/\tau)}$$

$$\text{with } \frac{1}{\tau} \sim \omega^2 + T^2$$

Electrical evidence for Fermi surface of long-lived quasiparticles of density *p*

In-Plane Magnetoresistance Obeys Kohler's Rule in the Pseudogap Phase of Cuprate Superconductors

M. K. Chan,[1,*] M. J. Veit,[1] C. J. Dorow,[1,†] Y. Ge,[1] Y. Li,[1] W. Tabis,[1,2] Y. Tang,[1] X. Zhao,[1,3] N. Barišić,[1,4,5,‡] and M. Greven[1,§]

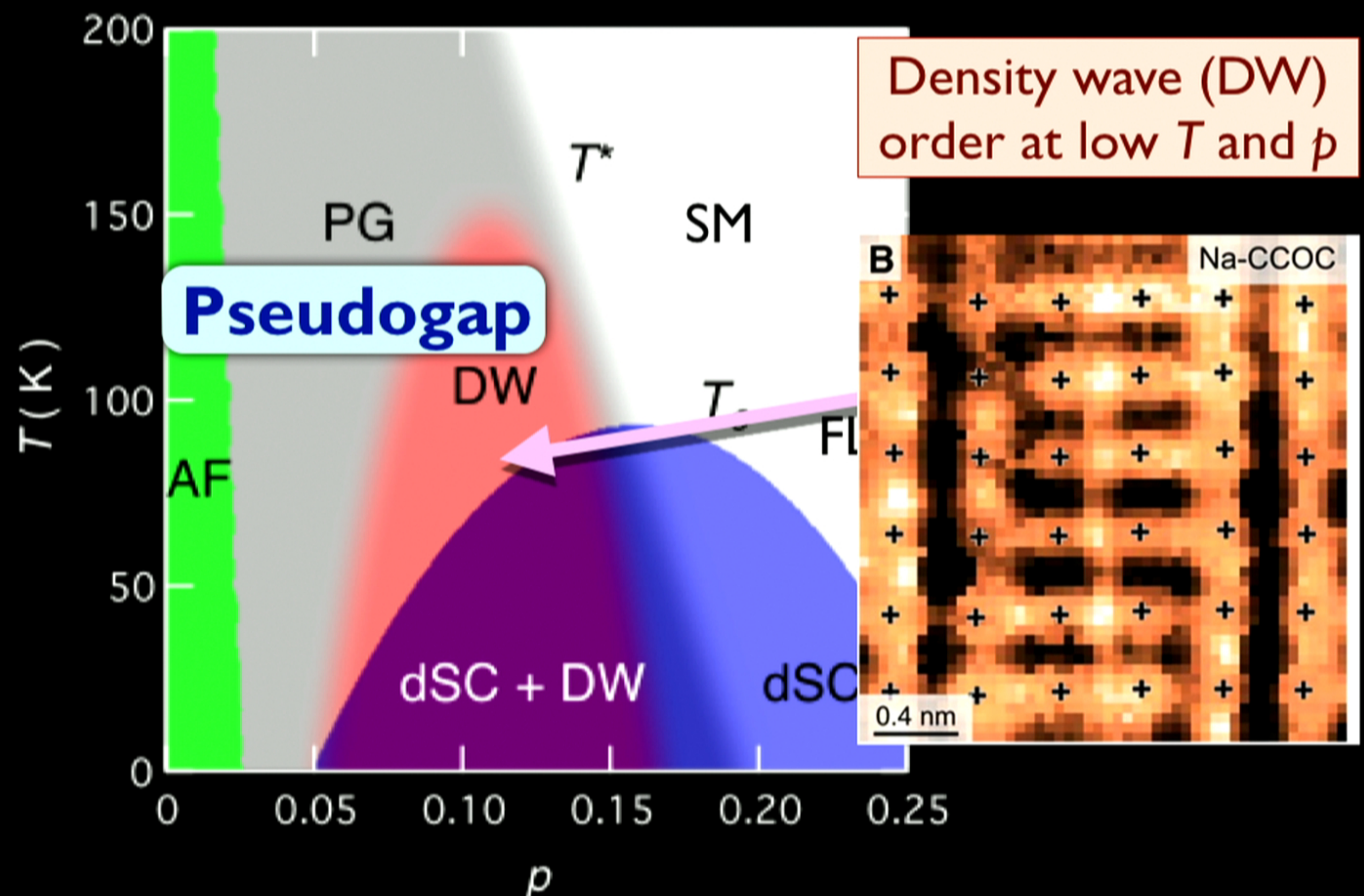
PRL 113, 177005 (2014)

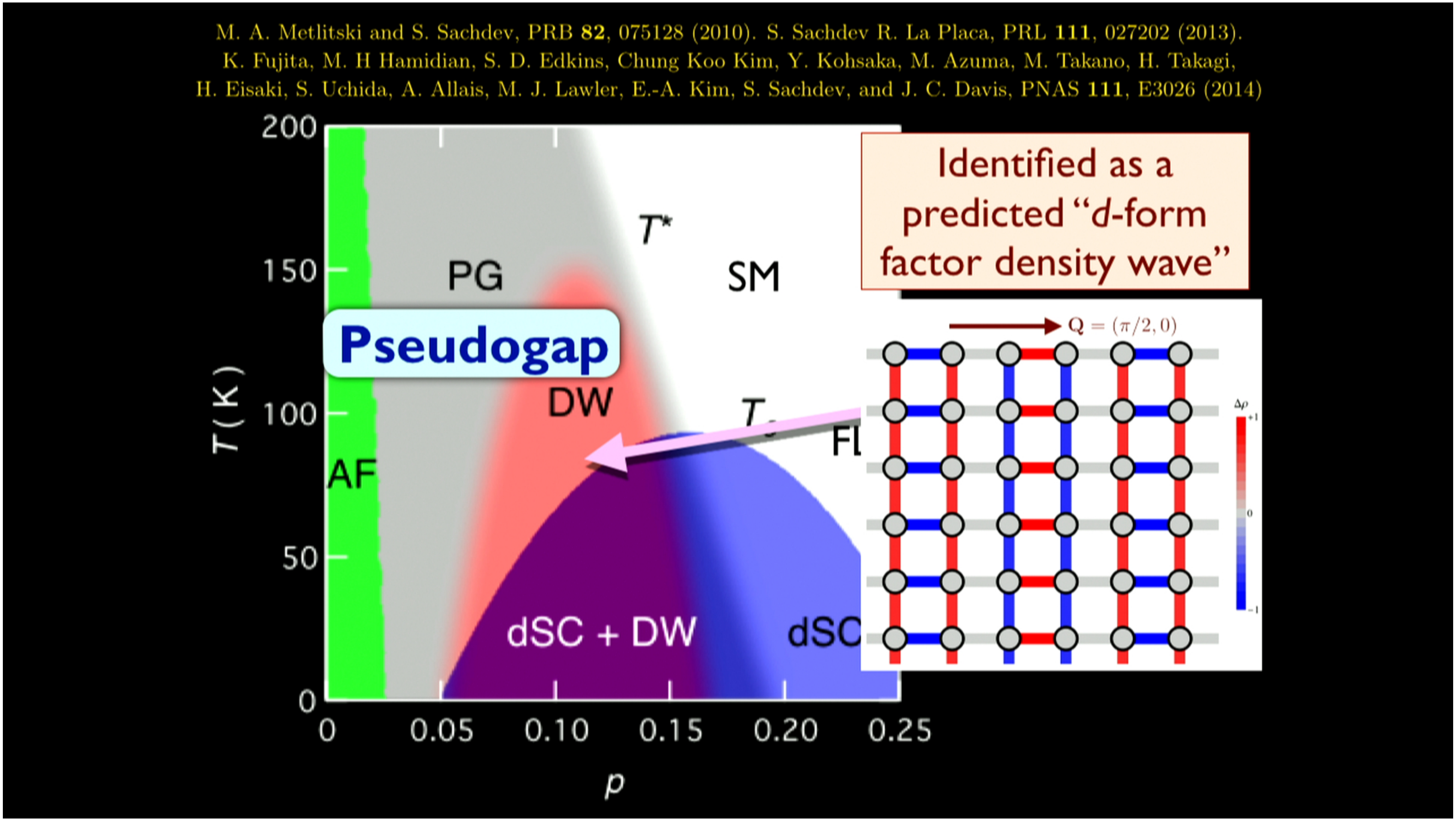
We report in-plane resistivity (ρ) and transverse magnetoresistance (MR) measurements for underdoped $HgBa_2CuO_{4+\delta}$ (Hg1201). Contrary to the long-standing view that Kohler's rule is strongly violated in underdoped cuprates, we find that it is in fact satisfied in the pseudogap phase of Hg1201. The transverse MR shows a quadratic field dependence, $\delta\rho/\rho_0 = aH^2$, with $a(T) \propto T^{-4}$. In combination with the observed $\rho \propto T^2$ dependence, this is consistent with a single Fermi-liquid quasiparticle scattering rate. We show that this behavior is typically masked in cuprates with lower structural symmetry or strong disorder effects.

$$\rho_{xx} \sim \frac{1}{\tau}(1 + aH^2\tau^2 + \ldots)$$

$$\text{with } \frac{1}{\tau} \sim T^2$$

Y. Kohsaka *et al.*, SCIENCE **315**, 1380 (2007)




M. A. Metlitski and S. Sachdev, PRB **82**, 075128 (2010). S. Sachdev R. La Placa, PRL **111**, 027202 (2013).
K. Fujita, M. H Hamidian, S. D. Edkins, Chung Koo Kim, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi,
H. Eisaki, S. Uchida, A. Allais, M. J. Lawler, E.-A. Kim, S. Sachdev, and J. C. Davis, PNAS **111**, E3026 (2014)
Identified as a predicted "*d*-form factor density wave"
Pseudogap
$Q = (\pi/2, 0)$
$\Delta\rho$
PG
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T^*
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T_c
FL
AF
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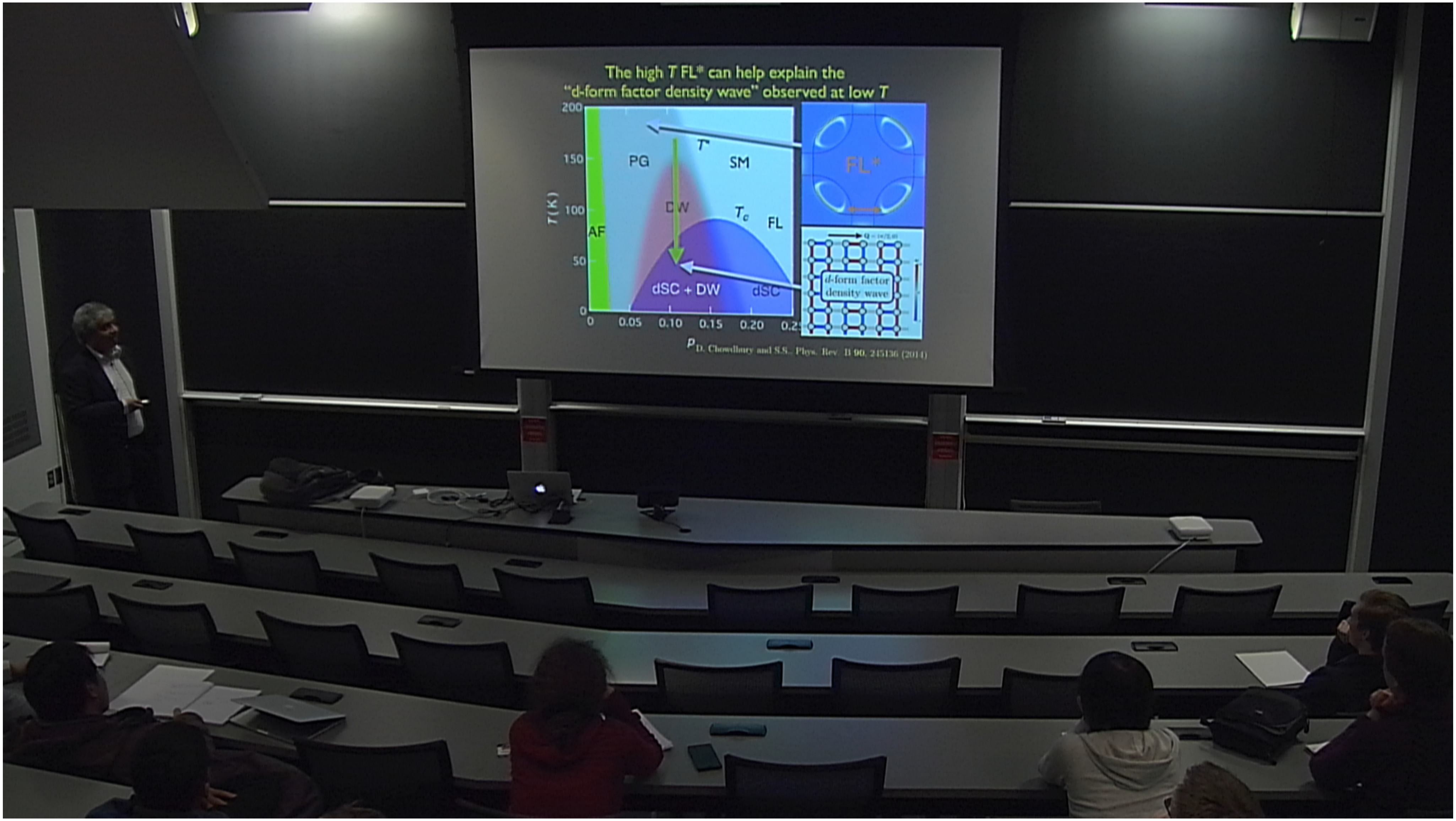
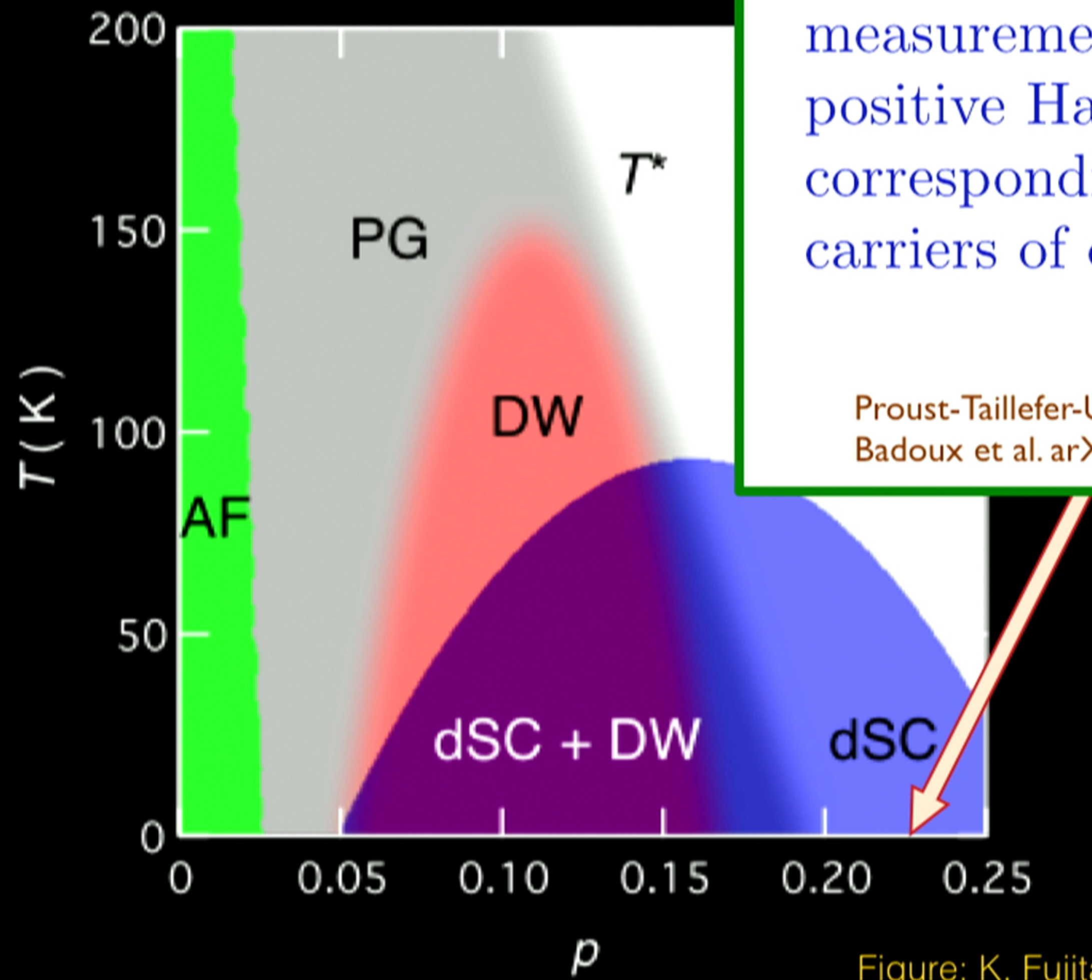
dSC
T (K)
p
200
150
100
50
0
0.05
0.10
0.15
0.20
0.25

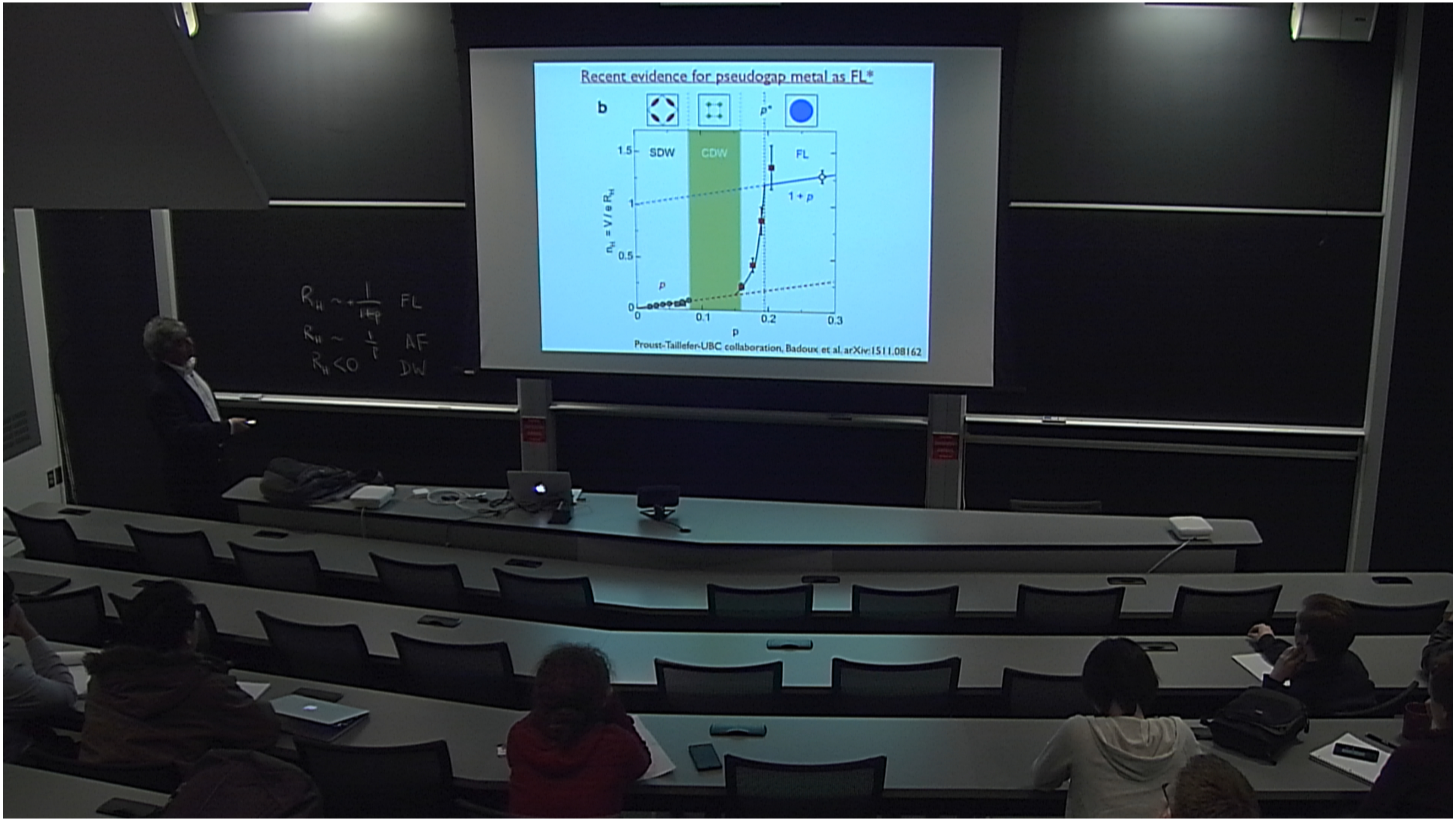

The high T FL* can help explain the
"d-form factor density wave" observed at low T
200
150
100
50
0
T (K)
PG
T*
SM
DW
Tc
FL
AF
dSC + DW
dSC
0
0.05
0.10
0.15
0.20
p
FL*
d-form factor density wave
D. Chowdhury and S.S., Phys. Rev. B 90, 245136 (2014)



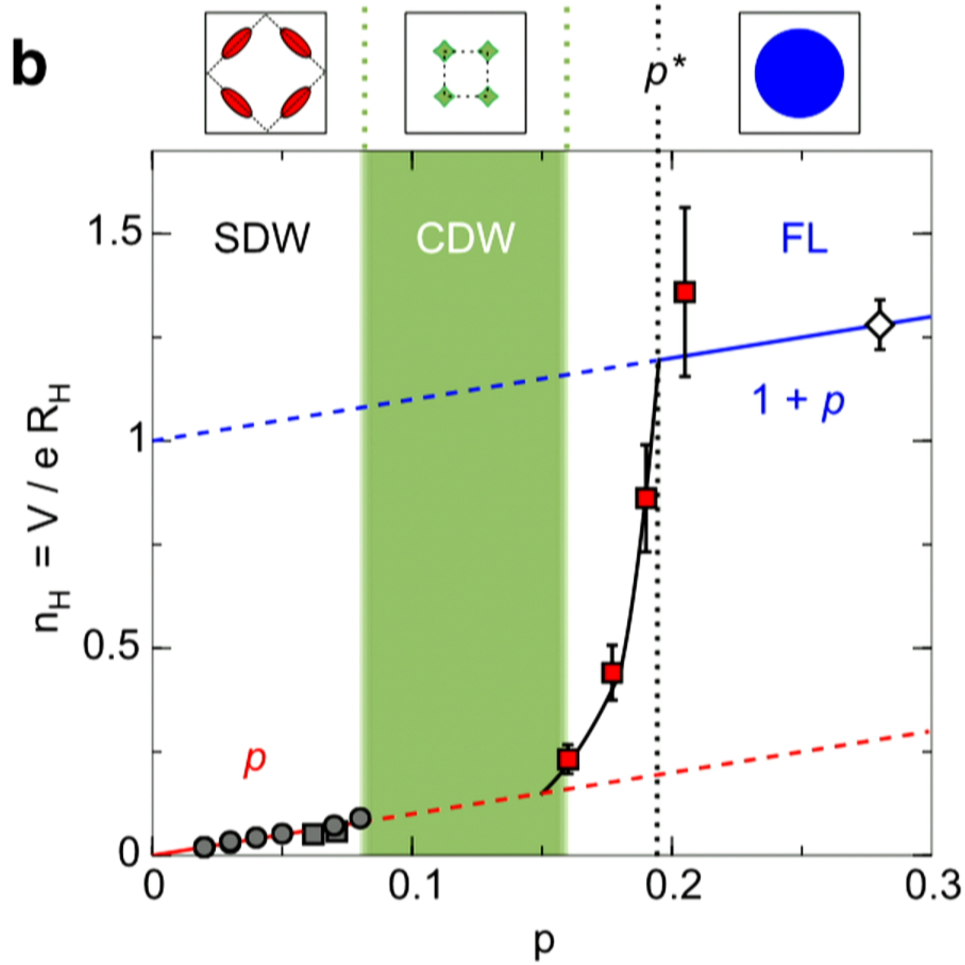
High field, low T measurements show a positive Hall co-efficient corresponding to carriers of density $1 + p$

Proust-Taillefer-UBC collaboration,
Badoux et al. arXiv:1511.08162

Figure: K. Fujita and J. C. Seamus Davis


Recent evidence for pseudogap metal as FL*
b
p*
SDW
CDW
FL
1 + p
p
n_H = V / e R_H
Proust-Taillefer-UBC collaboration, Badoux et al, arXiv:1511.08162

Recent evidence for pseudogap metal as FL*



Proust-Taillefer-UBC collaboration, Badoux et al. arXiv:1511.08162

Fractionalized Fermi liquid (FL*)

We have described a metal with:

- A Fermi surface of electrons enclosing volume p, and not the Luttinger volume of $1+p$
- Additional low energy quantum states on a torus not associated with quasiparticle excitations *i.e.* emergent gauge fields

There is a general and fundamental relationship between these two characteristics. Promising indications that such a metal describes the pseudogap of the cuprate supercondutors