Title: Experimental Quantum Error Correction

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Abstract: The last decade has seen the impressive development of quantum information science, both in theory and in experiment. There are many measures that can be used to assess the achievements in the field: new algorithms, new applications and larger quantum processors, to name a few. The discovery of quantum algorithms has demonstrated the potential power of quantum information.

As pointed out by Bill some years ago, to realize this potential requires the ability to overcome the imprecision and imperfection inherent in physical systems.

Quantum error correction (QEC) has provided a solution, showing that errors can be corrected with a reasonable amount of resources as long as their rate is sufficiently small. Implementing QEC protocols remains one of the most important challenges in QIP.

In the experimental arena, the quest to build quantum processors that could outperform their classical counterparts has led to many blueprint proposals for potential devices based on NMR, electron spin resonance, ion traps, atom traps, optics, superconducting devices and nitrogen-vacancy centres, among others. Many have demonstrated not only the possibility of controlling quantum bits, but also the ability to do so in practice, showing the progression of quantum information science from the blackboard to the laboratory. My presentation will give an overview of some of the recent results in quantum information science on the way to implement quantum error correction. I will show how noise can be characterise efficiently when our goal is to find suitable quantum error correcting codes. I will show demonstrations of control to implement some quantum error correcting codes and finally how can noise be extracted through algorithmic cooling. I will comments on some challenges that need to be solved and a path towards implementing many round of quantum error correction.



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Experimental Quantum Error Correction

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UnruhFest, Perimeter Institute, August 2015

Successes of Quantum Information Science



• Discovery of the power of quantum mechanics for information processing

-new language for quantum mechanics



- Discovery of how to control quantum systems
- Proof-of-concepts experiments

The Death of Q Computers... (1995)



a large number of states is important), not only must the coupling be small, but the time taken in the quantum calculation must be less than the thermal time scale \hbar/k_BT . For longer times the condition on the strength of the coupling to the external world becomes much more stringent.



Threshold theorem



A quantum computation can be as long as required with any desired accuracy using a reasonable amount of resources as long as the noise level is below a threshold value P < 10

> Knill et al.; Science, 279, 342, 1998 Kitaev, Russ. Math Survey 1997 Aharonov & Ben Or, ACM press Preskill, PRSL, 454, 257, 1998









Significance:

-imperfections and imprecisions are not fundamental objections to quantum computation -it gives criteria for scalability

-its requirements are a guide for experimentalists -it is a benchmark to compare different technologies



Q107+ e 11> (1)





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Ingredients for FTQEC

- Parallel operations
- Good quantum control
- Ability to extract entropy
- Knowledge of the noise
 - No lost of qubits
 - Independent or quasi independent errors
 - Depolarising model
 - Memory and gate errors
 - . . .

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and lots of qubits...

Progress in experimental QIP

• # of qubits vs time



Progress in experimental QIP

• # of qubits vs time



Adapted from Michael Mandelberg

• Increasing control of qubits

Table 1 Current performance of various qubits							
Type of qubit	T 2	Benchma	rking (%)	References			
		One qubit	Two qubits				
Infrared photon	0.1 ms	0.016	1	20			
Trapped ion Trapped neutral atom	15 s 3 s	0.48 [†] 5	0.7*	104-106 107			
Liquid molecule nuclear spins	2 s	0.01 [†]	0.47 [†]	108			
e ⁻ spin in GaAs quantum dot e ⁻ spins bound to ³¹ P: ²⁸ Si ²⁹ Si nuclear spins in ²⁸ Si NV centre in diamond	3 μs 0.6 s 25 s	5 5 5	5	43, 57 49 50 60 61 65			
Superconducting circuit	4 µs	0.7	10*	73, 79, 81, 109			

Measured T_2 times are shown, except for photons where T_2 is replaced by twice the hold-time (comparable to T_1) of a telecommunication-wavelength photon in fibre. Benchmarking values show approximate error rates for single or multi-qubit gates. Values marked with asterisks are found by quantum process or state tomography, and give the departure of the fidelity from 100%. Values marked with daggers are found with randomized benchmarking¹⁰. Other values are rough experimental gate error estimates. In the case of photons, two-qubit gates fail frequently but success is heralded; error rates shown are conditional on a heralded success. NV, nitrogen vacancy.

Ladd, T. D., et al., Nature, 464(7285), 45-53, 2010

Characterising noise

Usually we think of the circcuit model: Prepare a state, compute, measure



Other possibility is to use only generators of the Clifford group (generated by Hadamard, Phase gate and CNOT), with state preparation and measuremen in the computational basis:



and include the preparation of the magic state

$$\rho = \frac{1}{2} 1 \!\! 1 + \frac{1}{\sqrt{3}} (X + Y + Z)$$

Characterising noise for QIPs

How do we learn about the noise model?

- Assume first only for memory
- Focus on applying QEC
- Want to be efficient
- 1) Full process tomography operators

to be efficient
ocess tomography
$$\rho_{f} = \sum_{j} A_{j} \rho_{i} A_{j}^{\dagger} = \sum_{kl} \chi_{kl}^{\text{tensor product}} A_{kl} P_{k} \rho_{i} P_{l} = \begin{pmatrix} A_{j} \\ \dots \end{pmatrix} \rho_{i}$$

25

2) Can we get instead coarse grained values of the quantum process such as probability of 0 error (P_0) , 1 error (P_1) , 2 errors $(P_2),\ldots$ independent of which qubit is affected and the particular error (i.e. X/Y/Z).

- do process tomography and coarse grain \rightarrow not efficient
- find an efficient protocol, coarse graining \implies symmetrise

Characterising noise for QIPs

Coarse graining \implies imposing a symmetry

- ullet error independent of a particular qubit use permutations: π_s
- ullet average over X/Y/Z
 ightarrow "twirl" average over $SU(2)^{\otimes n}$

$$ho_f = \sum_{kl} \chi_{kl} \int d\mu(U) U^\dagger P_k U
ho_i U^\dagger P_l^\dagger U \ igvee ext{"2-design"}$$

$$ho_f = \sum_{kl} \chi_{kl} \sum_lpha C^\dagger_lpha P_k C_lpha
ho_i C^\dagger_lpha P_l^\dagger C_lpha$$

where C_{α} belongs to the Clifford group $\sim S\mathcal{P}$ with $\mathcal{P} = \{\mathbb{1}, X, Y, Z\}$, $\mathcal{S} = \{e^{-i\frac{\pi}{4}X}, e^{-i\frac{\pi}{4}Y}, e^{-i\frac{\pi}{4}Z}\}$

"Chernoff-bound"

$$\rho_{f} \approx \sum_{kl} \chi_{kl} \sum_{\alpha} C_{\alpha}^{\dagger} P_{k} C_{\alpha} \rho_{i} C_{\alpha}^{\dagger} P_{l}^{\dagger} C_{\alpha}$$

DiVincenzo et al., 2002, IEEE Trans. Inform. Theory 48, 580 Dankert, C., et al., PRA 80, 012304, 2009.

Characterising noise protocol

- start with the state $|000...\rangle$,
- implement the symmetrisation group and the Clifford group
- measure how many bits have been flipped.
- Repeat $\rightarrow P_0, P_1, ...$



see Emerson et al. Science 317, 1893, 2007

Experimental result



Emerson, RL et al., Science 317, 1893, 2007



Errors in Clifford gates

Adapt the idea to benchmark Clifford gates



 $f(\hat{M}_j, \mathcal{C}_i, \mathcal{U})$ is a measurement in a different classical basis we can then find P_0, P_1, \ldots in the gate \mathcal{U} .

Errors in Clifford gates

Use malonic acid in solid state

One qubit can be benchmarked using the Knill procedure:



and Clifford gates using the new procedure

	Target	Experiment	w	k _w	λw				Probability	of no error	F
	-0-	1-0-0	1	6	0.967 ± 0.010		50	. (a)		٨	
а	-0-	1-8-D	2	21	1.000 ± 0.009		25			A	0.983 +0.007
	-0-	x-[]-D	3	7	0.978 ± 0.017	L	0				
	<u>—ФШ</u>	HT-I	1	8	0.848 ± 0.022	1	50	. (b)			
b			2	21	0.883 ± 0.017	bability d	25			0.863 +0.013	
			3	8	0.799 ± 0.023		0				
		P	1	6	0.959 ± 0.014	Å.	50	. (1)		٨	
¢		1-2-82D	2	21	0.989 ± 0.013		25			A	0.973 +0.009
	-++[H]-	×-LHE-D	3	8	0.964 ± 0.016		0				
								0.7	0.8	0.9 1.	

Note: the difference between b) and c) is improving the pulse ("fixing")

Moussa, Silva, Laflamme PRL 109, 100503 (2012)



 kHz
 C1
 C2
 Cm

 C1
 6.380
 0.297
 0.780

 C2
 -0.025
 -1.533
 1.050

 Cm
 0.071
 0.042
 -5.650

Pirsa: 15080029

Benchmarking gates



Benchmarking gate

Two qubit comparison Summary table

System	Error Rate	Reference
Superconducting	0.006	Nature 508, 501 (2014)
Ion Trap	0.069/0.162	PRL 108, 260503 (2012)
Liquid-State NMR	0.005	NJP 11 013034 (2009)
Neutral Atoms	0.27	PRL 104, 010503 (2010)
lon trap	0.007	Nat. Phys. 4 463 (2008)
NV centre	0.11	Science 320 1326 (2008)
ESR	0.05	Nature 455 1085 (2008)
Linear Optics	0.10	PRL 93 080502 (2004)

QEC Experimental implementation



QEC progress

SSNMR

Control for two rounds (2011)



Demonstration of Sufficient Control for Two Rounds of Quantum Error Correction in a Solid State Ensemble Quantum Information Processor



(a) labeled PES a report on Breed using a Soft on the partial decoupling many the water involves under the results for the partial decoupling many the water involves under the results for the partial decoupling many the water involves under the results for the partial decoupling many the water involves under the results for the partial decoupling many the water involves under the results for the partial decoupling many the water involves under the results for the partial decoupling many the water involves and the results for the partial decoupling many the rest of the partial decoupling by a unitary operation that energies for 112 ales unitariant and a line the the second and the s pseudopure, statistical as verification of the statistic management fidelities in the theorem where interpretences and the statistic management fidelities in the cases where an end of the statistic and the statistic and the statistic and the statistical state, and the bound out from the first for the line as distributed over the various error-syndrome subsplated. In this else, the distant are of searching errors and the bound out of the searching errors and the searching State, and the bottom quoti carries in mormation to be calcoded. After the decoding fordaut restriction operations, which bottom quoties on C_1 and C_m , respectively, $(\sum_{i < j} \frac{\pi}{2} J_{i,j}(Z_i Z_j + X_i X_j + Y_i Y_j))$. An accurate natural Hamiltonian is necessary for high fidelity control and is restored to its initial state, while the top two qubits carry obtained from precise spectral fitting of (also shown) a protoninformation about which error had occurred; and (c) the procedecoupled ¹³C spectrum following polarization-transfer from dure for two rounds: U_p prepares X, Y, or Z inputs, and $U_s =$ the abundant protons. The central peak in each quintuplet is {II, XI, IX, XX} toggles between the different syndrome subspadue to natural abundance ¹³C nuclei present in the crystal at ces; i.e., the experiment is repeated 4 times, cycling through the $\sim 1\%$ (for more details see [7, 10] and references therein.) different U_s , and then the results are added, similar to a standard phase cycling procedure.

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QEC progress

SSNMR

Control for two rounds (2011)



Demonstration of Sufficient Control for Two Rounds of Quantum Error Correction in a Solid State Ensemble Quantum Information Processor



Osama Moussa,^{1,2,*} Jonathan Baugh,^{1,3} Colm A. Ryan,^{1,2} and Raymond Laflamme^{1,2,4}

FIG. 4 (color online). Summary of experimental results for the *partial decoupling* map: the system evolves under the natural Hamiltonian as well as 70 kHz decoupling fields that partially modulate the heteronuclear interactions (between the carbons and protons). Shown (on left) are the single-qubit entanglement fidelities in the cases where no encoding is employed (blue dots); or one round of the 3-bit code (red crosses); or two rounds of the 3-bit code (black asterisks), where the interaction interval is split to two equal intervals. The dashed lines are quadratic fits to the data and are included to guide the eye. Also shown (on right) is the signal after one round of error correction as distributed over the various error-syndrome subspaces. In this case, the dominant errors are phase flips on the top and bottom qubits, which are encoded on C_1 and C_m , respectively.

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Algorithmic cooling with a heat bath

Energy and disorder of a 3 qubit system (at equilibrium)

(
$ 000\rangle \rightarrow$	(1-p) ³						
$ 001\rangle \rightarrow$	р(1-р) ²						
$ 010\rangle \rightarrow$	p(1-p) ²						
$ 011\rangle \rightarrow$	$p^{2}(1-p)$						
$ 100\rangle \rightarrow$	p(1-p) ²						
$ 101\rangle \rightarrow$	$p^2(1-p)$						
$ 110\rangle \rightarrow$	$p^2(1-p)$						
$ 111\rangle \rightarrow$	p ³						



-Sorensen, Prog. Nuc. Mag. Res. Spect.21, 503, 1989 -Schulman and Vazirani. STOC, p322, 1998. -Boykin, Mor, Roychowdhury, Vatan, & Vrijen. Proc. Natl Acad. Sci. USA 99, 3388–3393 (2002). -Fernandez, Lloyd, Mor, & Roychowdhury. Int. J. Quant. Inform. 2, 461 (2004).

Algorithmic cooling with a heat bath







Irradiated malonic acid



Cooling with the help of e^-



Conclusion

In order to implement quantum error correction, we will need

- Good knowledge of the noise
- Good quantum control
- Ability to extract entropy
- Parallel operations

Recent experiments have demonstrated these elements individually but we need to pull them together.

It is only the beginning of experimental QEC.