

Title: CMB Anomalies and Non-Gaussianity

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Abstract: When the primordial fluctuations are non-Gaussian and inflation lasts longer than the minimum number of e-folds, the likelihood that we observe mild deviations from isotropy increases. I will present a single framework that encompasses many of the most promising scenarios for generating a hemispherical power asymmetry. This framework allows a comparison of the observational evidence for various models, including some with a natural connection between large scale power suppression and power asymmetry.

Large Scale CMB anomalies as a signature of non-Gaussianity

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with
Saroj Adhikari
Adrienne Erickcek
(1508.xxxxx)

Non-Gaussianity and Statistical Isotropy

We only need

$$C(\hat{n}, \hat{n}') \equiv \langle \Delta T(\hat{n}) \Delta T(\hat{n}') \rangle$$

and it is given by

$$C(\hat{n}, \hat{n}') = C(\theta), \quad \theta = \arccos(\hat{n} \cdot \hat{n}')$$

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In harmonic space:

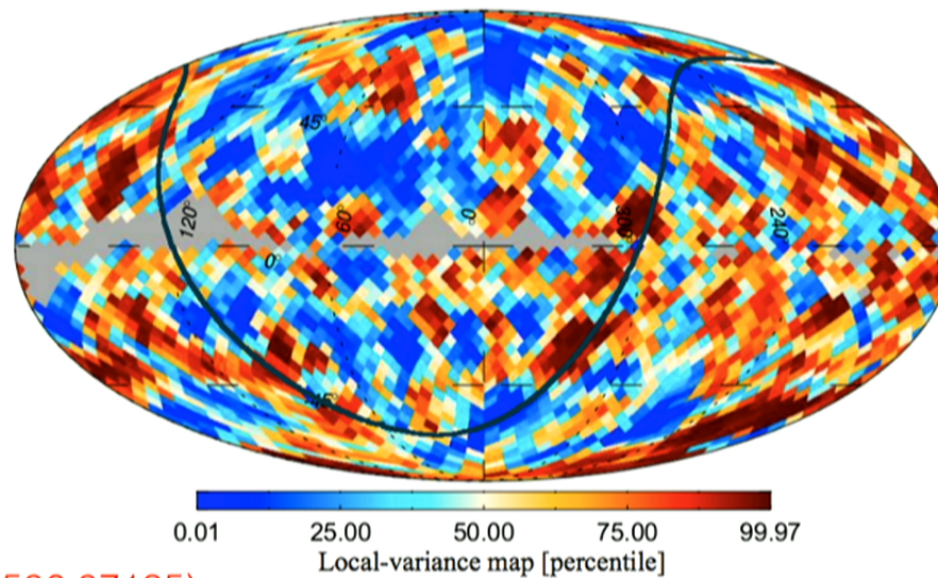
$$\Delta T(\hat{n}) = \sum_{l,m} a_{lm} Y_{lm}(\hat{n})$$

$$\langle a_{lm} a_{l'm'}^* \rangle = C_l \delta_{ll'} \delta_{mm'}$$

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The hemispherical power asymmetry

- The amplitude of fluctuations is different on two halves of the sky



Planck 2015 (1506.07135)

, 10 Aug 2015, PI

An equation for that?

$$\frac{\Delta T}{T}|_{\text{mod}}(\hat{n}) = (1 + A \hat{n} \cdot \hat{p}) \frac{\Delta T}{T}|_{\text{iso}}(\hat{n})$$

On large scales: $A \sim 0.07$

significance $\sim 3\sigma$

Akrami et al (1402.0870)
Planck 2013 (1303.5083)
Planck 2015 (1506.07135)

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So what?

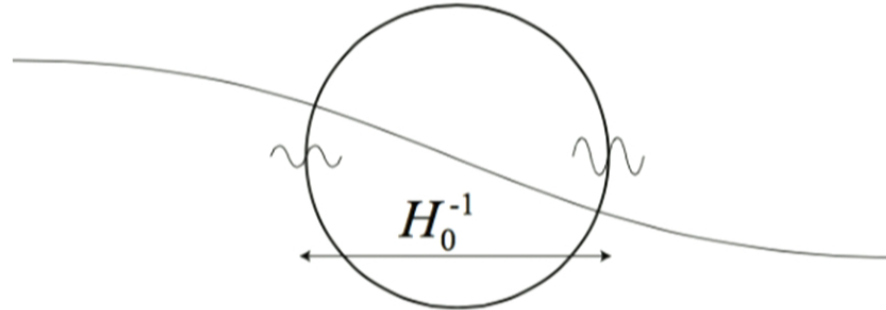
- A) just a fluke
- B) evidence of some departure from usual inflation lurking just outside the horizon
- C)

(A,B = Two reasons not to work on this???)

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The EKC idea

- Curvaton (or inflaton/curvaton) scenario
- Large amplitude super horizon fluctuation
- Non-Gaussianity: gradient \rightarrow power asymmm.

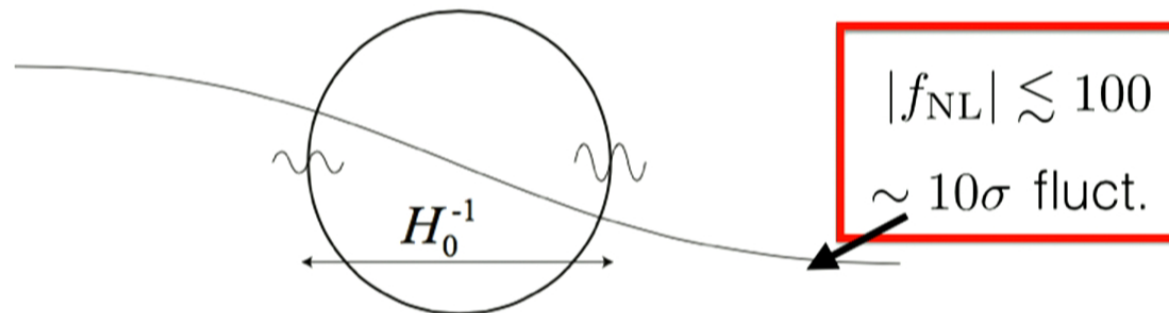


Erickcek, Kamionkowski, Carroll (0806.0377) Figure 1
(many iterations since)

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The EKC idea

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What we're doing

- Analytic expressions predicting probability of modulations from any isotropic, non-Gaussian model:
computing cosmic variance
- Claim: With non-Gaussianity, don't need lurking super-Hubble specialness
- Connection means: can use power modulations to constrain non-Gaussianity
- Given analytic pdfs, can do Bayesian model comparison to compare evidence for Gaussian vs NG models

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Formalizing EKC

- Local non-Gaussianity:

$$\Phi(x) = \phi(x) + f_{\text{NL}}(\phi^2 - \langle \phi^2 \rangle)$$

- long wavelength modes affect short wavelength modes:

(easily generalizes beyond the local ansatz)

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Formalizing EKC

Consistency-relation violating fNL
(Mirbabayi, Zaldarriaga 1409.4777)

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$$\Phi(x) = \phi(x) + f_{\text{NL}}(\phi^2 - \langle \phi^2 \rangle)$$

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$$P_{\Phi}(k, \mathbf{x}) = P_{\phi}(k) \left[1 + 4f_{\text{NL}} \int \frac{d^3 \mathbf{k}_{\ell}}{(2\pi)^3} \phi(\mathbf{k}_{\ell}) e^{i\mathbf{k}_{\ell} \cdot \mathbf{x}} \right]$$

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(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Formalizing EKC, cont'd

Expand the exponential:

$$e^{i\mathbf{k}_\ell \cdot \mathbf{x}} = 4\pi \sum_{LM} i^L j_L(k_\ell x) Y_{LM}^*(\hat{k}_\ell) Y_{LM}(\hat{n})$$

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Formalizing EKC, cont'd

Expand the exponential:

Then

$$P_{\Phi}(k, \hat{n}) = P_{\phi}(k) \left[1 + f_{\text{NL}} \sum_{LM} g_{LM} Y_{LM}(\hat{n}) \right]$$

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The monopole

Monopole shift: $L=0$

$$P_{\Phi}(k) = P_{\phi}(k) [1 + A_0] = P_{\phi}(k) \left[1 + f_{\text{NL}} \frac{g_{00}}{2\sqrt{\pi}} \right]$$

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$$P_{\Phi}(k) = P_{\phi}(k) [1 + A_0] = P_{\phi}(k) \left[1 + f_{\text{NL}} \frac{g_{00}}{2\sqrt{\pi}} \right]$$

IR sensitive

$$\langle g_{00}^2 \rangle = 64\pi \int \frac{dk_{\ell}}{k_{\ell}} \left[\frac{\sin(k_{\ell}x)}{k_{\ell}x} \right]^2 \mathcal{P}_{\phi}(k_{\ell})$$

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The dipole modulation

(L=1)

$$P_{\Phi}(k, \hat{n}) = P_{\phi}(k) \left[1 + f_{\text{NL}} \sum_{M=-1,0,1} g_{1M} Y_{1M}(\hat{n}) \right]$$

Monopole shift is absorbed
These are the observed quantities

Variance not IR sensitive:

$$\langle g_{1M} g_{1M}^* \rangle = 64\pi \int \frac{dk_{\ell}}{k_{\ell}} \left[\frac{\sin(k_{\ell}x)}{(k_{\ell}x)^2} - \frac{\cos(k_{\ell}x)}{k_{\ell}x} \right]^2 \mathcal{P}_{\phi}(k_{\ell})$$

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How big is the predicted dipole?

For a direction \hat{d}_i :

$$P_{\Phi}(k) = P_{\phi}(k) [1 + 2A_i \cos \theta]$$
$$\cos \theta = \hat{d}_i \cdot \hat{n}$$

$$A_i = \frac{1}{4} \sqrt{\frac{3}{\pi}} f_{\text{NL}} g_{10}$$

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The direction is arbitrary:

decompose the line of maximum asymmetry into three orthogonal components and report

$$A = (A_1^2 + A_2^2 + A_3^2)^{\frac{1}{2}}$$

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Probability of dipole modulation

$$p_{\chi}(A, \sigma) = \sqrt{\frac{2}{\pi}} \frac{A^2}{\sigma^3} \text{Exp} \left[\frac{-A^2}{2\sigma^2} \right]$$

$$\sigma = \sqrt{\sigma_{f_{\text{NL}}}^2 + \sigma_0^2}$$

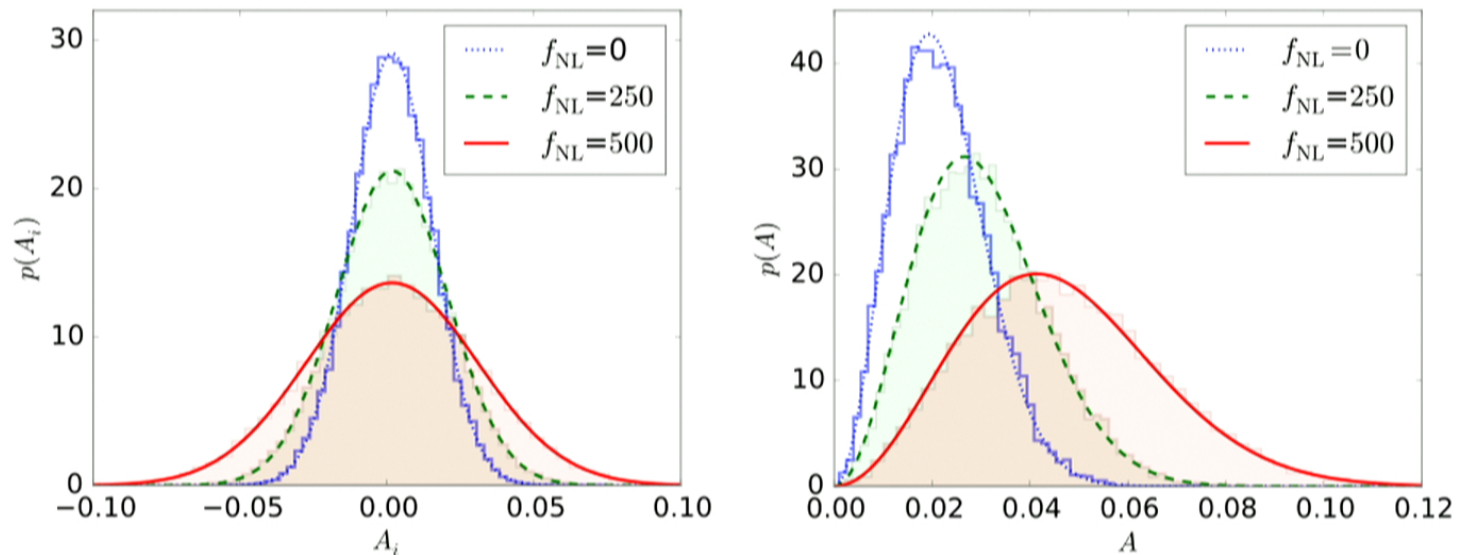
Calculated,
extrapolating our
observed power
spectrum to larger
scales

measured from
Gaussian maps

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Check: Probability of dipole modulation



10,000 simulated CMB maps (Sachs-Wolfe approx)
(Curves are analytic)

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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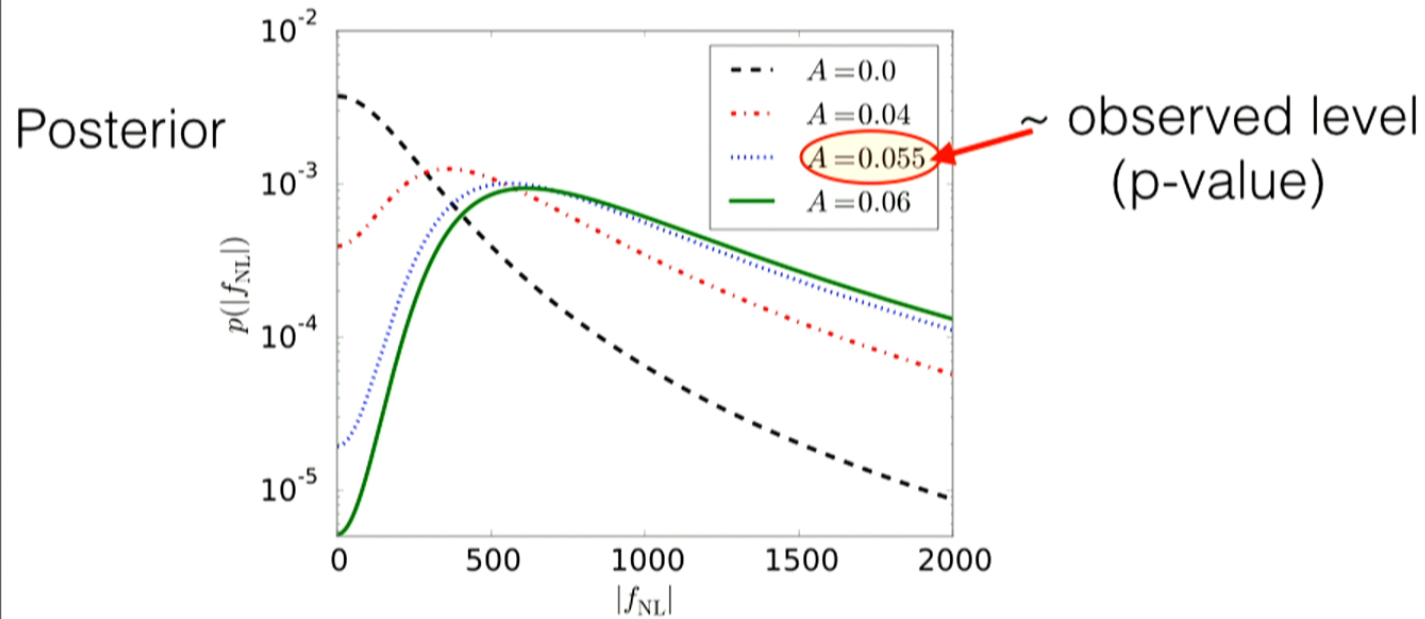
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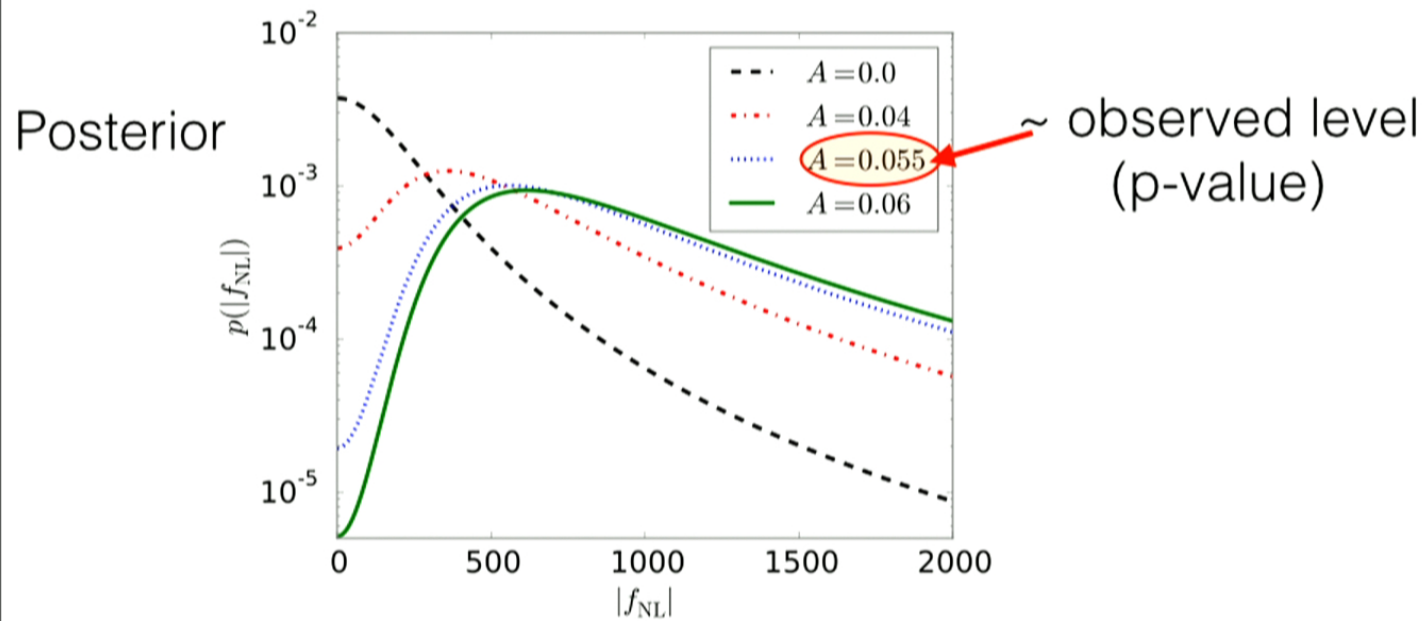
Using the asymmetry to constrain f_{NL}



(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Include large scale bispectrum constraints

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Include large scale bispectrum constraints

$$l \lesssim 100, \quad f_{\text{NL}} = -100 \pm 100$$

(Smith, Senatore, Zaldarriaga, 0901.2572)

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

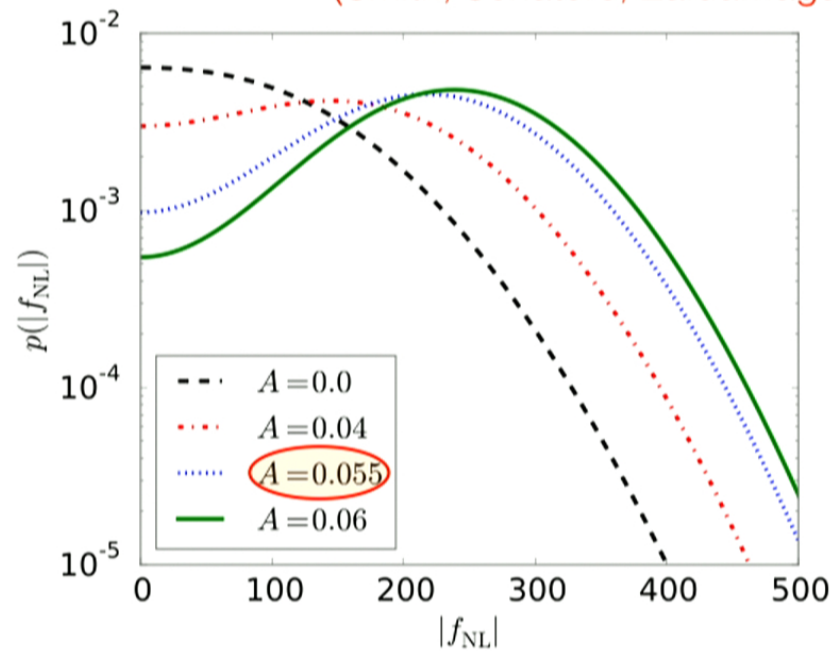
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Posterior



(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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Two-source model

$$P_{\Phi}(k) = P_{\Phi,\sigma}(k) + P_{\Phi,\varphi}(k)$$

$$\xi = P_{\Phi,\sigma}/P_{\Phi}$$

$$f_{\text{NL}} \rightarrow f_{\text{NL}}/\sqrt{\xi}$$

(ie, smaller observed NG gives same asymmetry)

$$\xi > A$$

ξ constrained by tensor-to-scalar ratio, LSS stochasticity

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Evidence for the NG vs Gaussian model?

A_{obs}	p -value	Bayes factor	$\ln B_{01}$
0.02	0.5511	1.1362	0.128
0.04	0.0381	0.6174	-0.482
0.05	0.0043	0.3211	-1.136
0.055	0.001	0.2012	-1.603
0.06	0.0003	0.1123	-2.186

$$|\ln B_{01}| = 5.0, 2.5$$

= {strong, moderate} evidence

Only weak evidence for the Non-Gaussian explanation

(Adhikari, Erickcek, Shandera, 1508.xxxxx)

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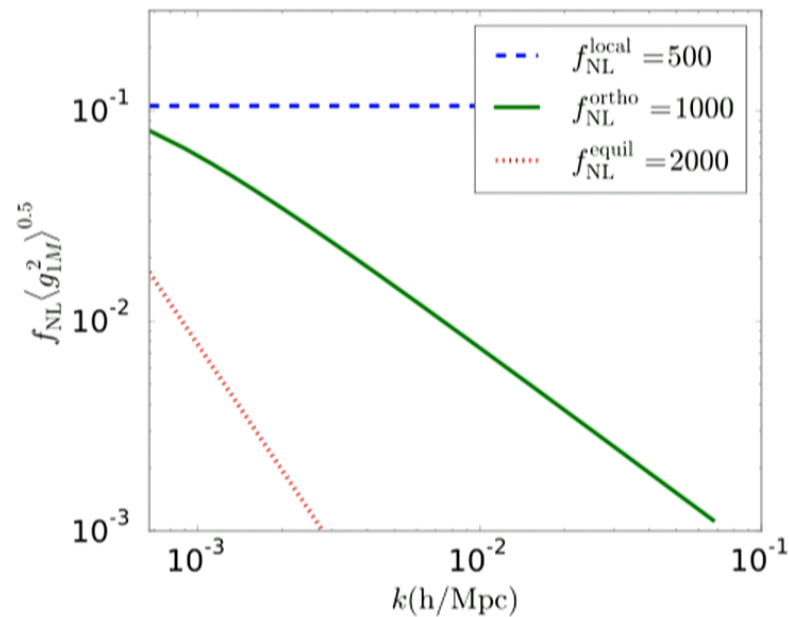
The scale-dependent power asymmetry

Any deviation from local ansatz gives scale-dependence

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Any deviation from local ansatz gives scale-dependence



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Scale-dependent modulations

$$P_{\Phi}(k, \mathbf{x}) = P_{\phi}(k) \left[1 + 4f_{\text{NL}}(k_0) \left(\frac{k}{k_0} \right)^{n_f} \int \frac{d^3 \mathbf{k}_\ell}{(2\pi)^3} \left(\frac{k_\ell}{k_0} \right)^{\alpha} \phi(\mathbf{k}_\ell) e^{i\mathbf{k}_\ell \cdot \mathbf{x}} \right]$$

$$\alpha \lesssim -1$$

Dipole modulation is IR divergent

$$n_f < 0$$

Dipole modulation decreases on small scales

$$\text{Natural scale-dependence: } \xi = P_{\Phi, \sigma} / P_{\Phi}$$

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A simple model

$$f_{\text{NL}}(k) = f_{\text{NL}}^0 \left(\frac{k}{k_0} \right)^{n_{f_{\text{NL}}}}$$

$$n_{f_{\text{NL}}} = 0.3_{-1.2}^{+1.9} \quad (95\% \text{ C.L.})$$

Becker, Huterer
1207.5788

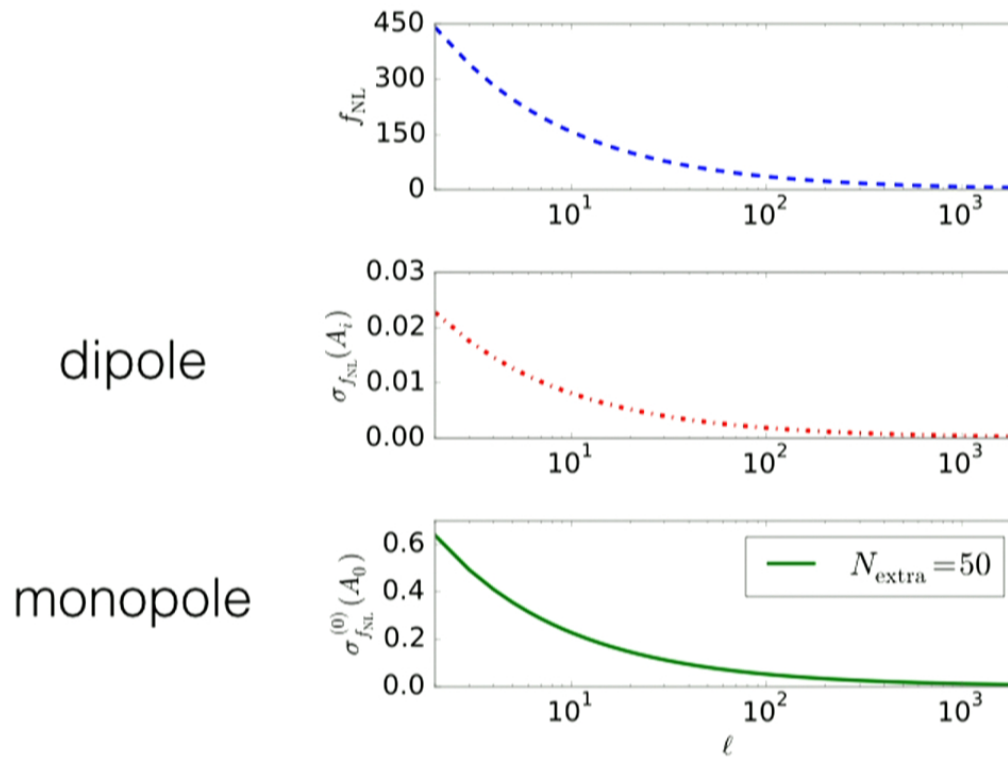
Now the monopole shift is also interesting
(Large scale power suppression)

$$P_{\Phi}(k) = P_{\phi}(k) [1 + A_0] = P_{\phi}(k) \left[1 + f_{\text{NL}} \frac{g_{00}}{2\sqrt{\pi}} \right]$$

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An example model

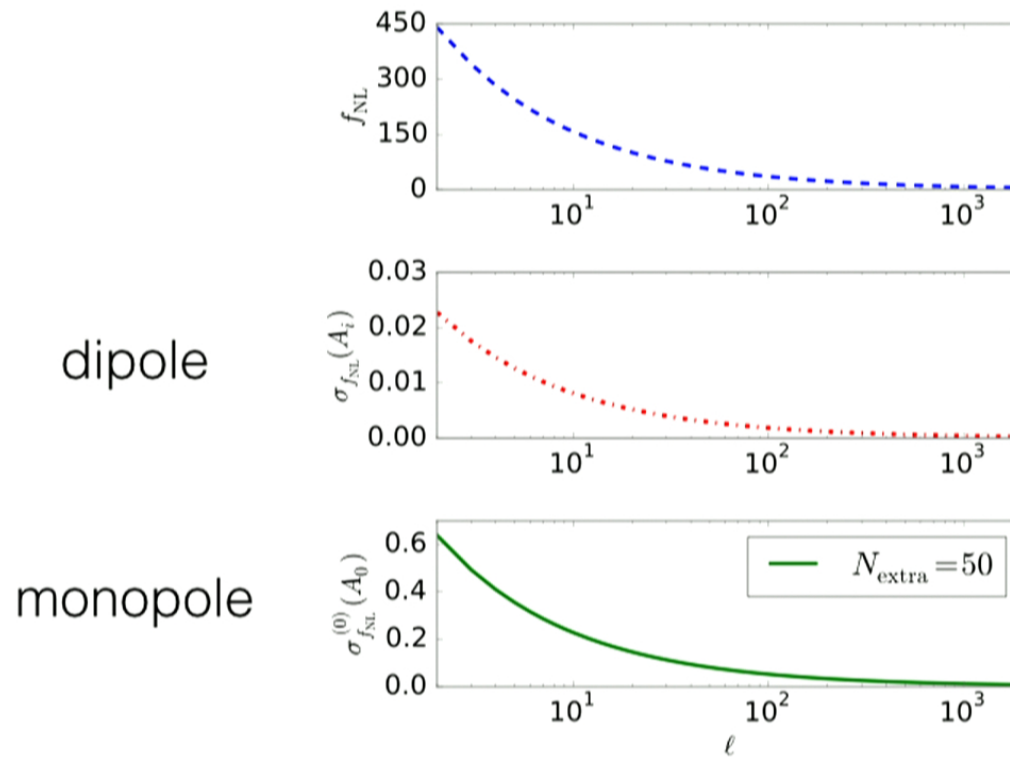
$$f_{\text{NL}}(\ell) = 50(\ell/60)^{-0.64}$$



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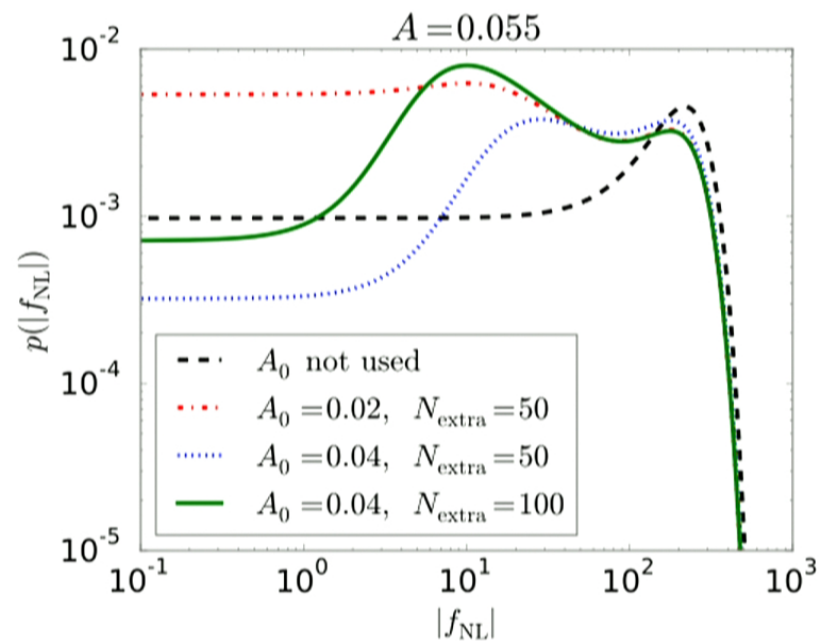
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Constraining non-Gaussianity using power modulations



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Evidence?

Fixed dipole: $A = 0.055$

$A_{0,obs}$	N_{extra}	Bayes factor	$\ln B_{01}$
-	-	0.2012	-1.603
0.02	50	1.107	0.102
0.04	50	0.0664	-2.712
0.04	100	0.1475	-1.914

$|\ln B_{01}| = 5.0, 2.5$
={strong, moderate}
evidence

Still only moderate evidence

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Could there be evidence for this model?

- Polarization data (+kSZ) can increase significance of the observed modulations
- Fits to bispectrum can constrain all shape parameters (future data $\ell > 100$)
- alignment of the GZ (super horizon mode) contribution to CMB quadropole, octopole and asymmetry direction

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Conclusions

- Evidence for Non-Gaussianity: isotropic bispectrum and power modulations should be considered together.
- Scale-dependent non-Gaussianity: an appealing fit
 - bispectrum + hemispherical power asymmetry + large scale power suppression
 - scale-dependence of modulation from NG is generic
 - A mixed curvaton/inflaton scenario: natural scale-dependence and small NG
- No special physics lurking just beyond the Hubble scale required

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