

Title: Cosmology Theory: Inflation

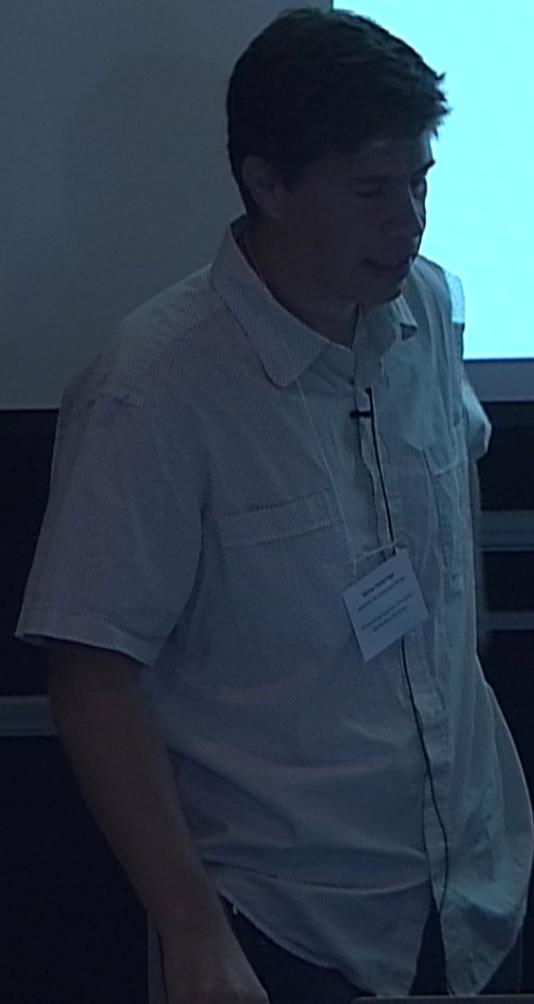
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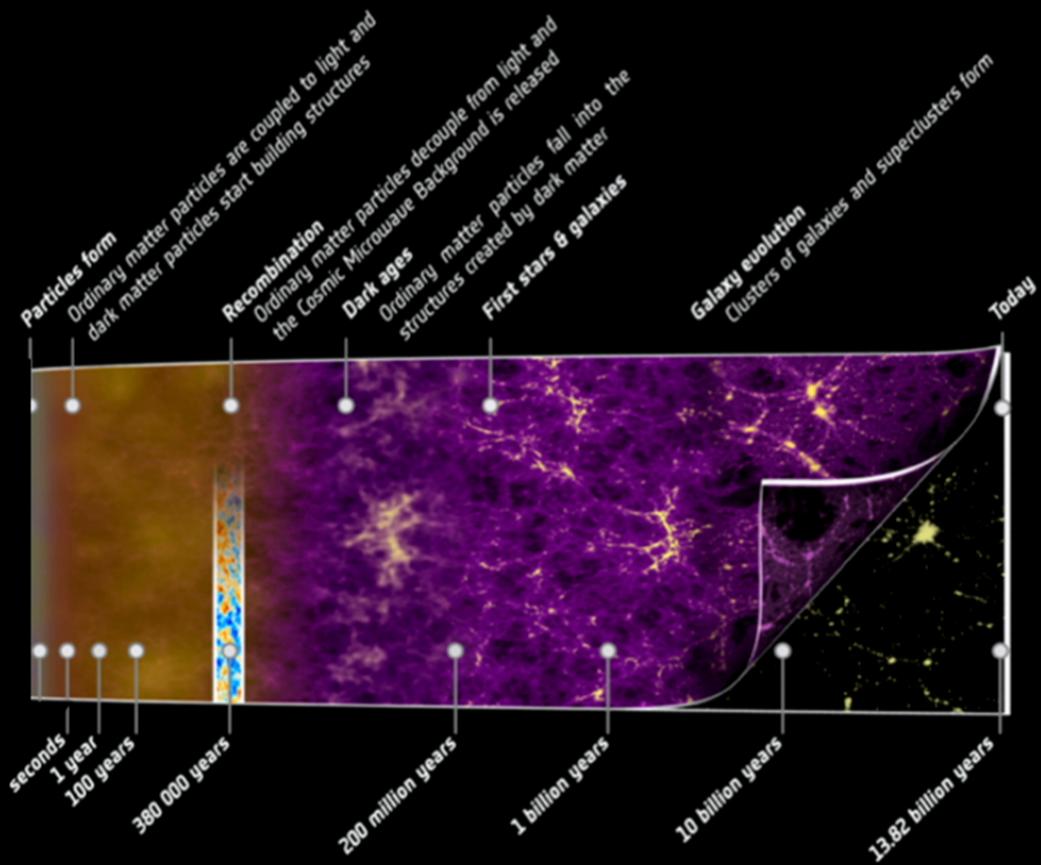
Abstract:

Inflation  
Large Scale Structure  
July 2015

$$(m_{\pi}/GeV)^{1/2}$$



# We live in the aftermath of a Big Bang



## FRW Background

$$ds^2 = a^2(\tau)[-d\tau^2 + dx^2] \quad ad\tau = dt$$

$$\mathcal{H}^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G a^2}{3} \rho$$

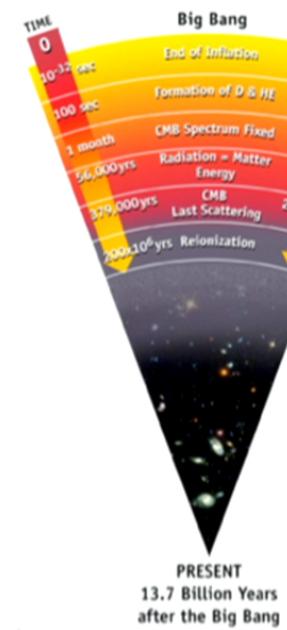
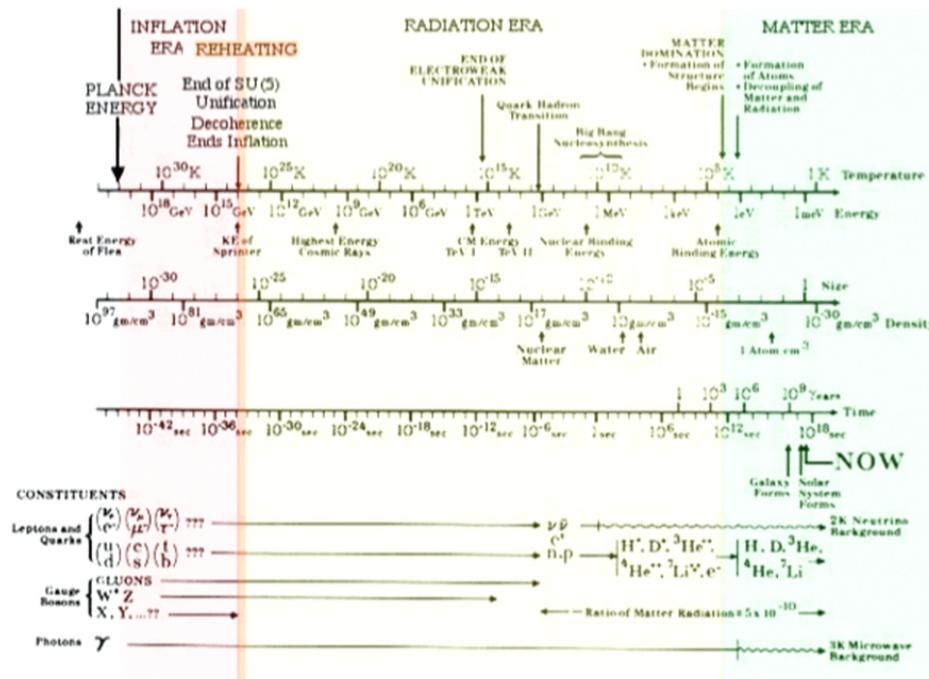
$$\dot{\rho} = 3\mathcal{H}(\rho + p)$$

$$\Omega = \frac{8\pi G}{3H^2} \rho \equiv \frac{\rho}{\rho_{\text{crit}}} \quad \rho \propto \Omega h^2 \equiv \omega \propto \frac{\rho}{\rho_\gamma}$$

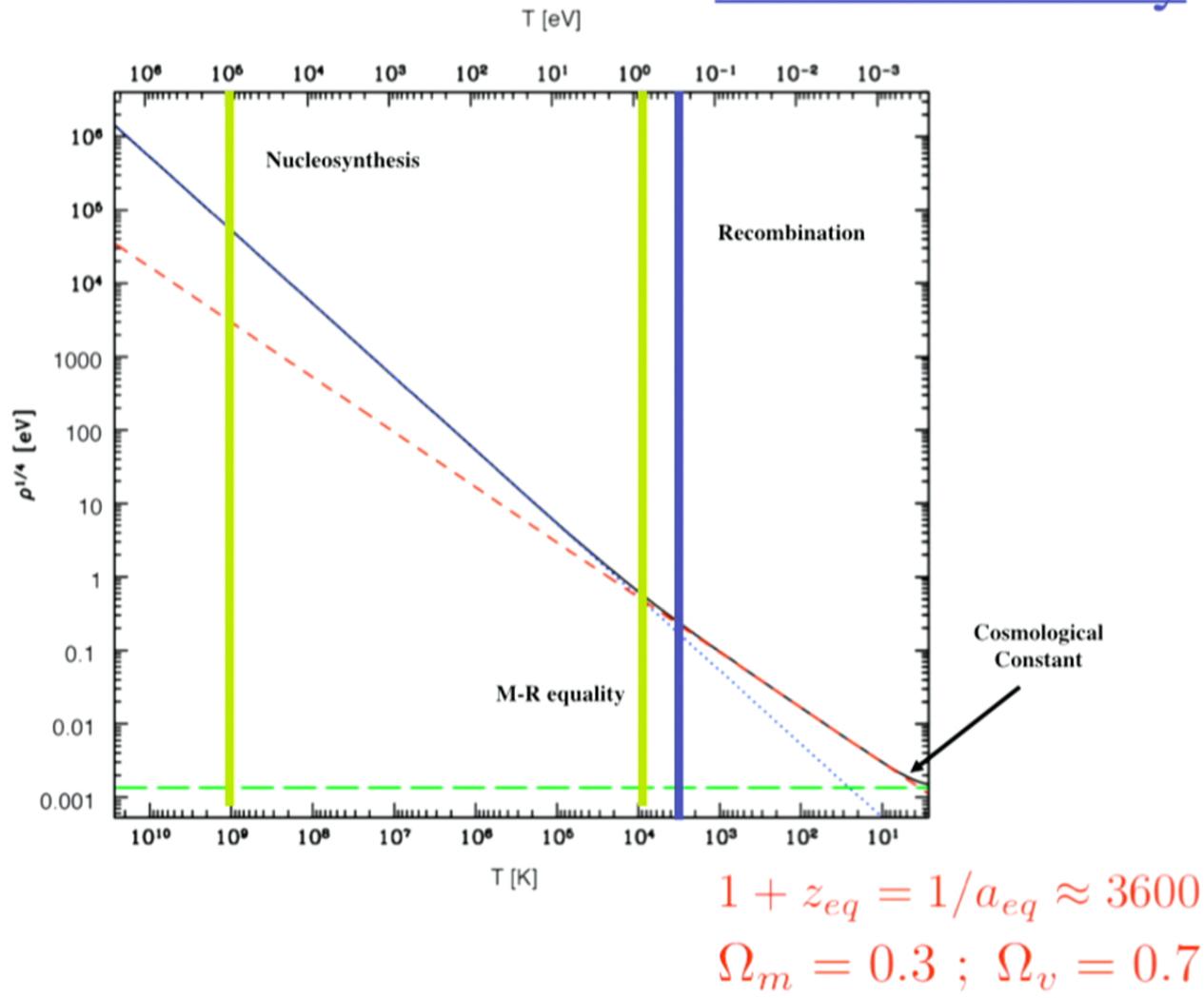
$$a(\tau) \propto \tau \quad (\text{Radiation era})$$

$$a(\tau) \propto \tau^2 \quad (\text{Matter era})$$

????



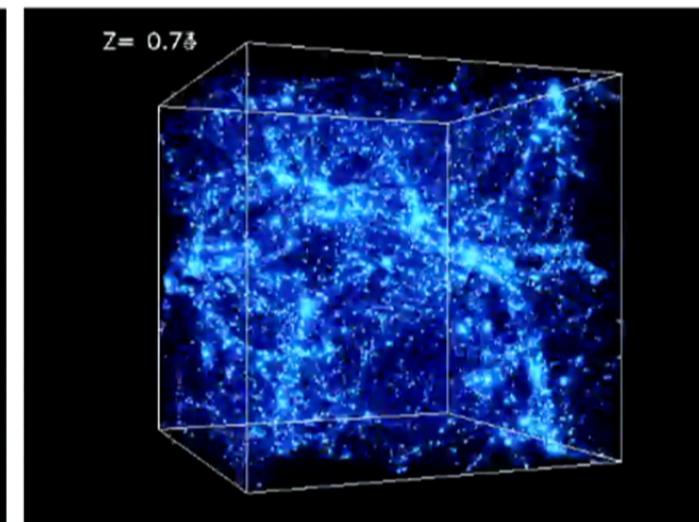
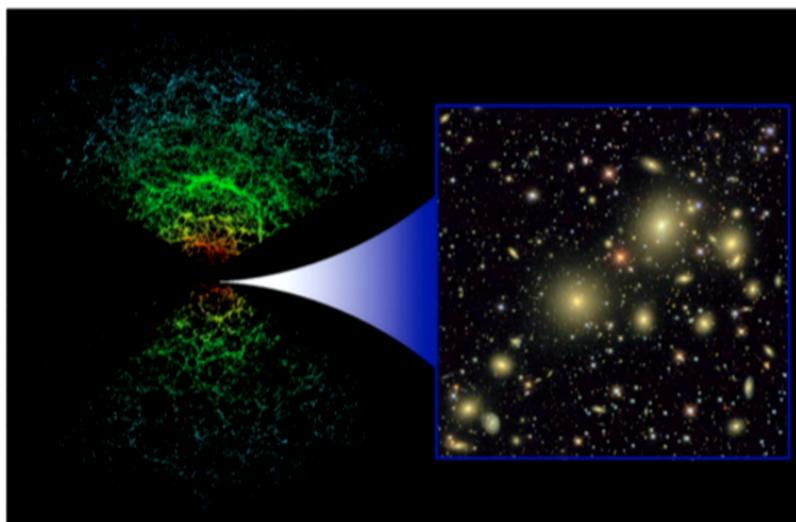
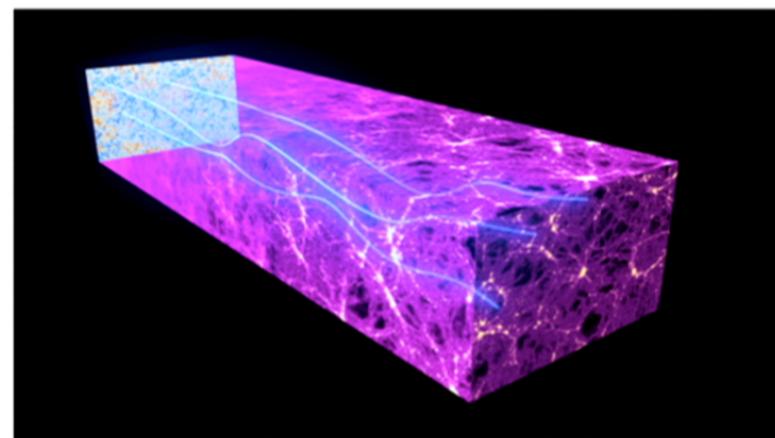
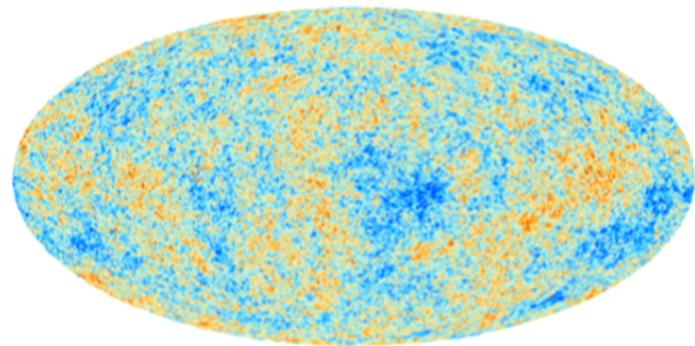
# Thermal History



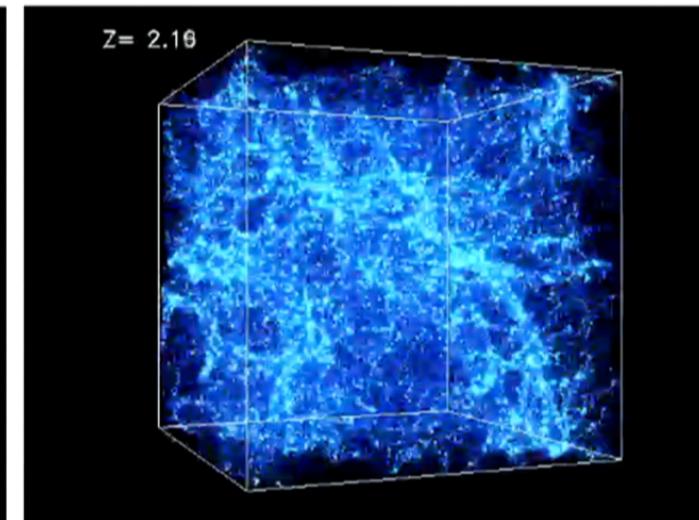
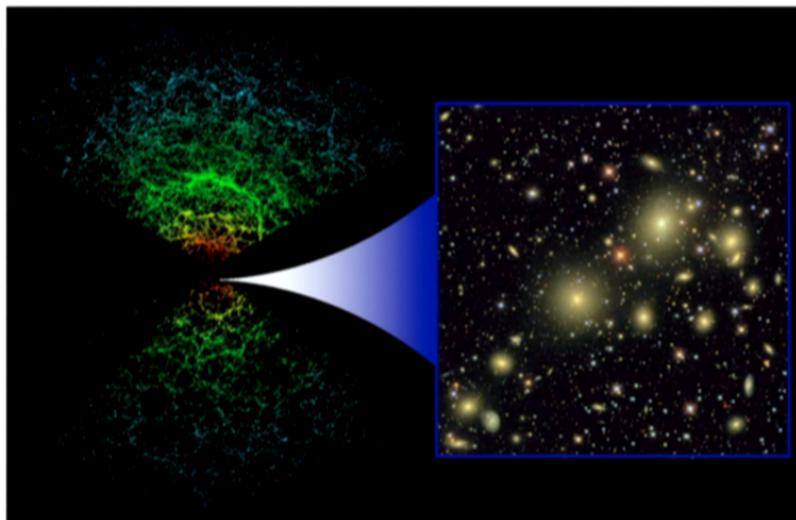
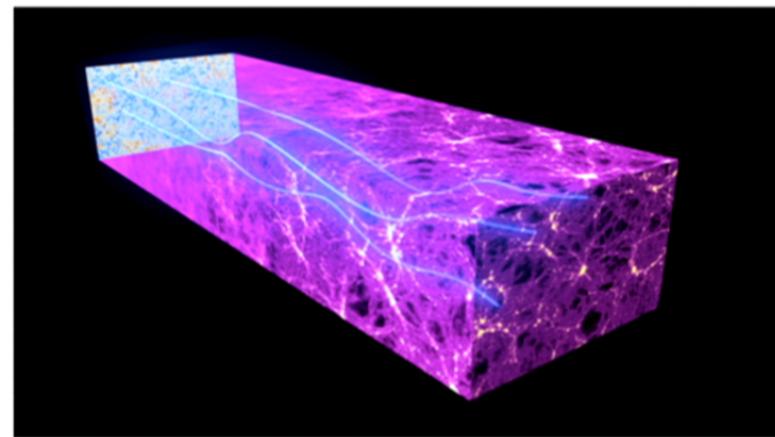
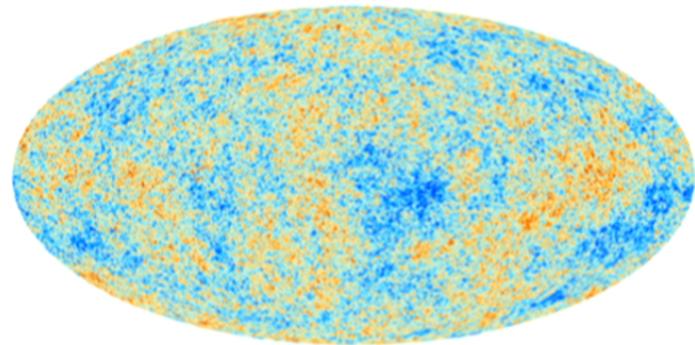
## Relics from the early stages of the HBB

1. BBN Nuclei
2. Cosmic Neutrino Background
3. CMB BB spectrum
4. Dark matter
5. Baryons
6. Others

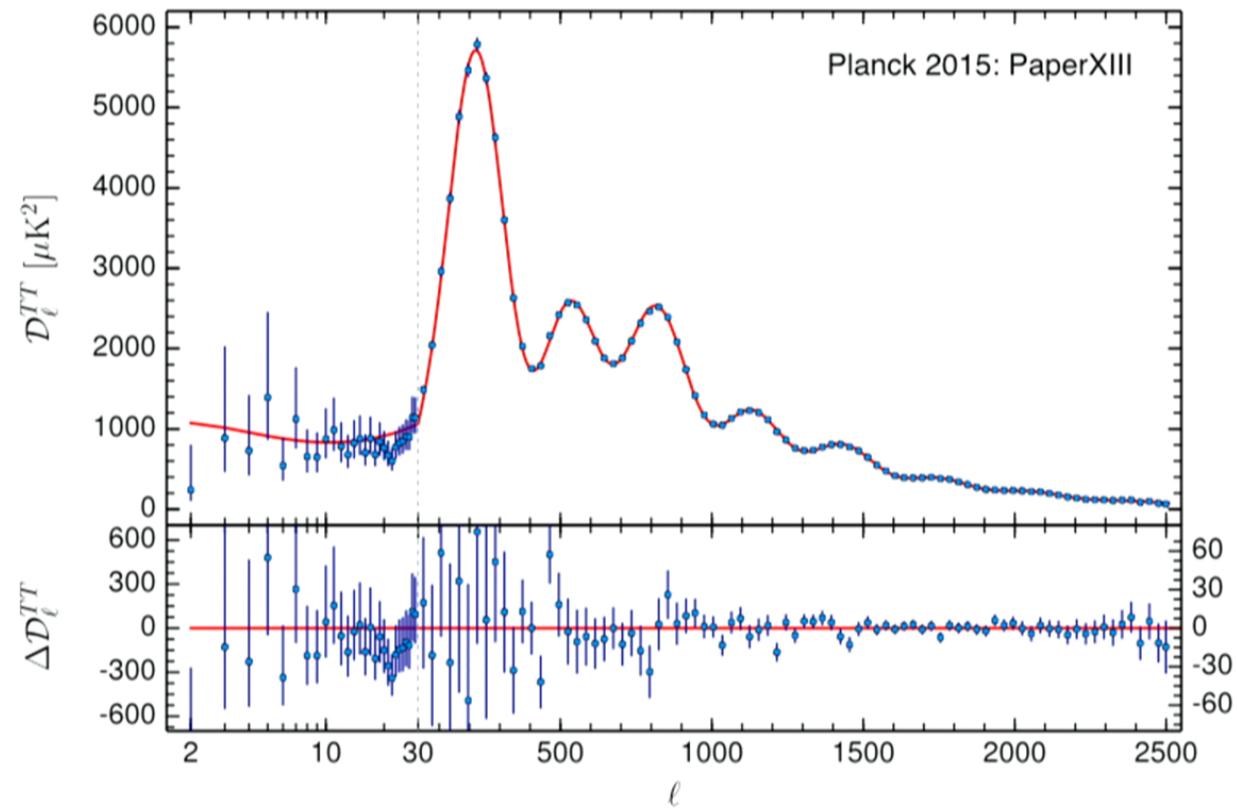
## The growth of structure

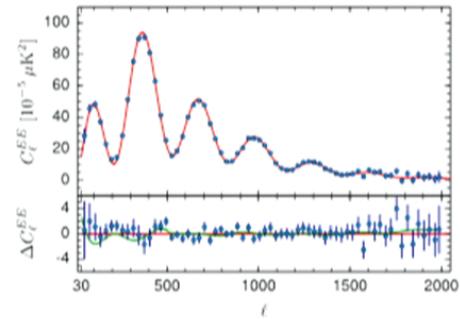
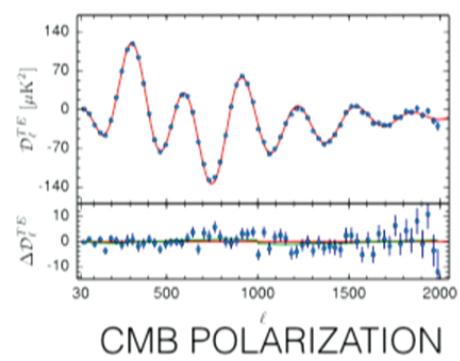


## The growth of structure

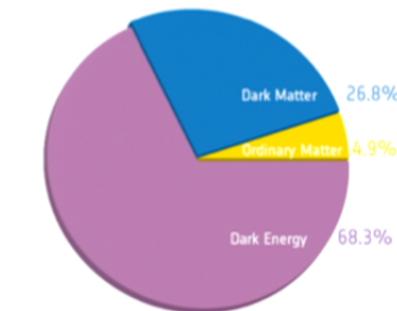
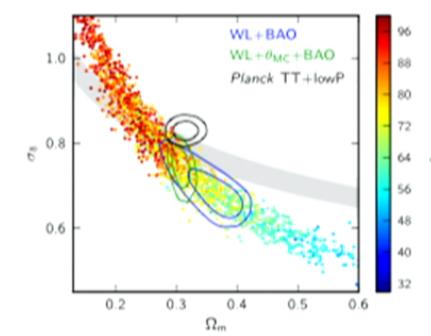
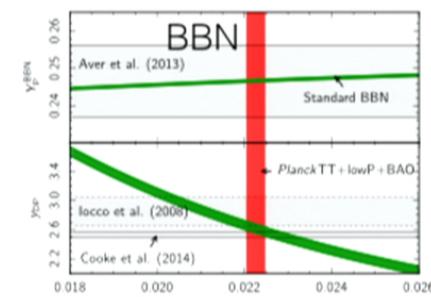
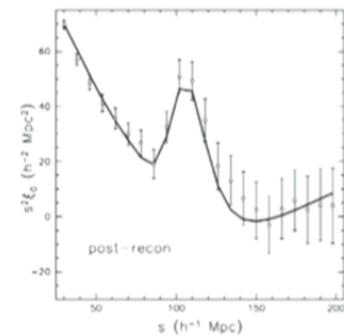
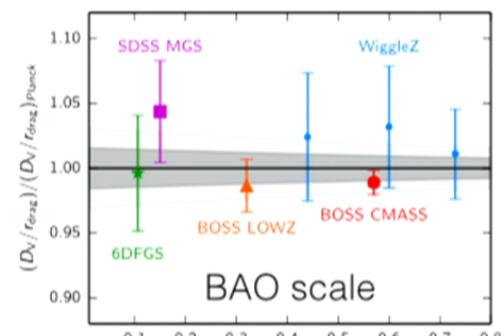
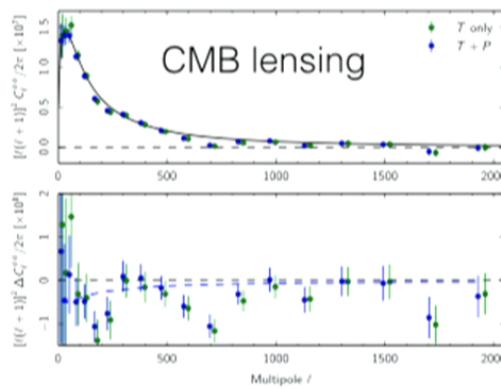
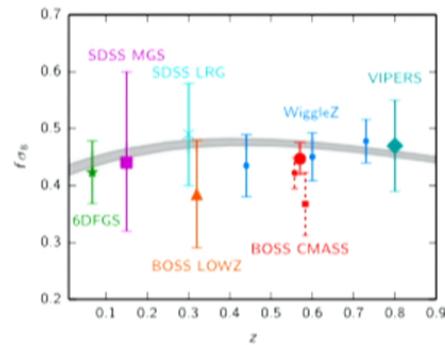


## Agreement between theory and data

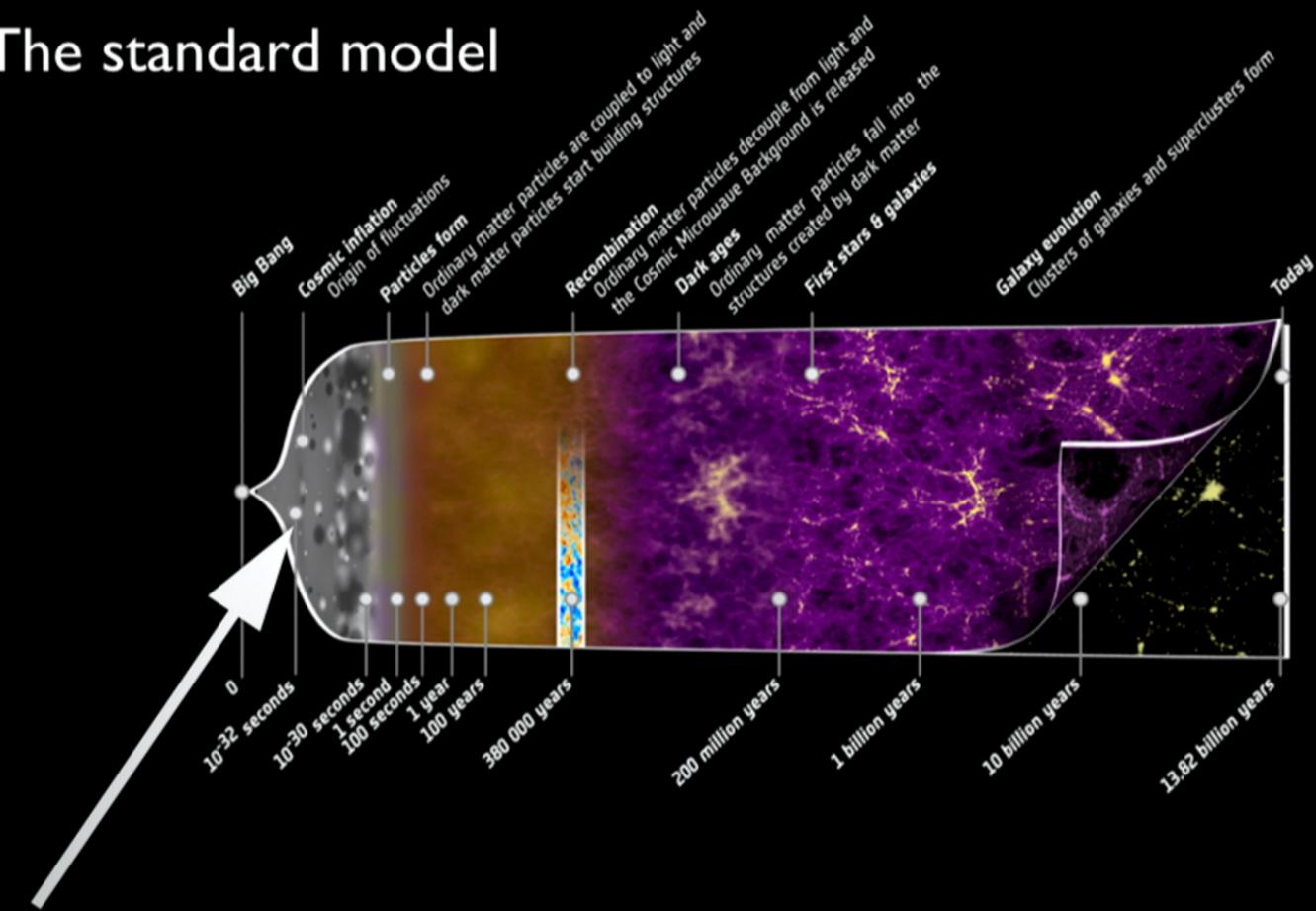




Growth of structure



# The standard model

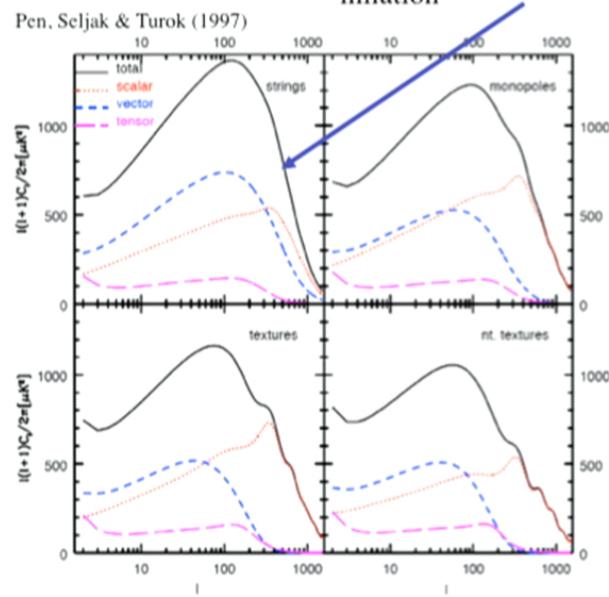


Why is the Universe so old/big? Attractor solution.  
Seeds for structure formation are quantum fluctuations of the clock.

## Fluctuations are primordial

### Causal Seeds

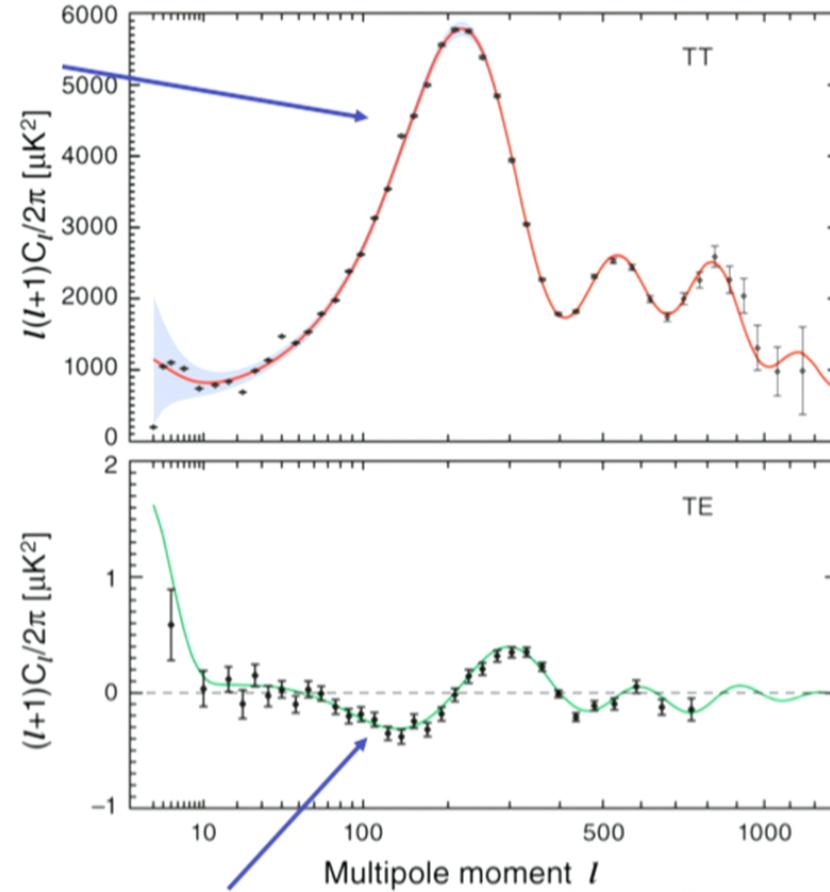
Pen, Seljak & Turok (1997)



Sharp acoustic peaks are difficult to create without inflation

Fluctuations are put in place before the Hot Big Bang starts. Although the theory for the origin of the fluctuations is bound to be speculative this fact is robust.

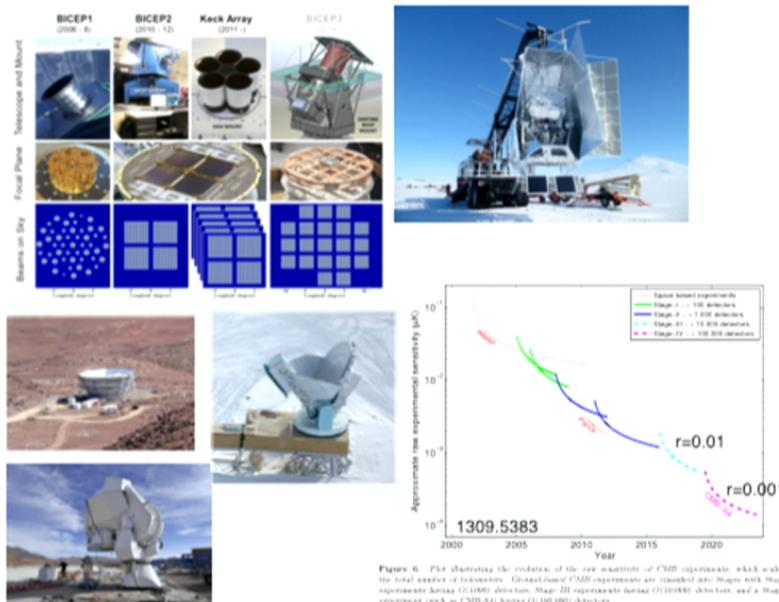
WMAP 7yrs



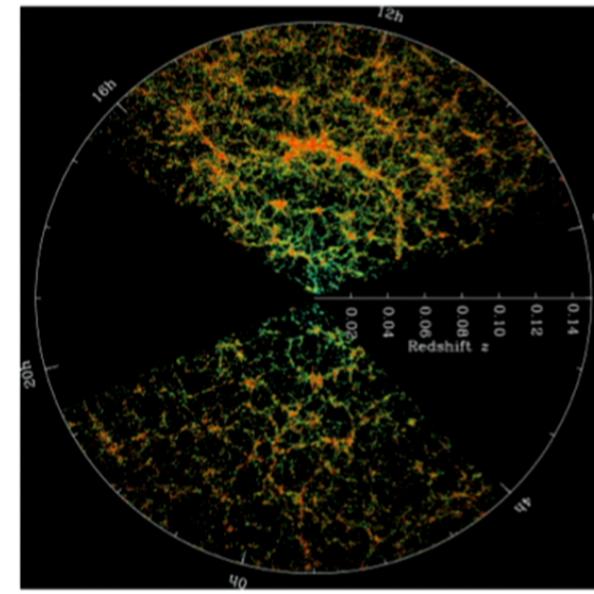
Hu & White (1996)  
Spergel & MZ (1997)  
Pieris et al WMAP (2003)

Negative peak imply fluctuations come from outside horizon

## Can we get a second fossil?



## Can we learn more about the scalar fluctuations?



## What we have learned so far

0. No curvature (1/2 percent level)

1. The seeds are primordial

---

2. Amplitude:  $\ln A_s = -19.932 \pm 0.034$

3. Slope:  $1 - n_s = 0.0355 \pm 0.0049$

---

4. No gravitational waves (10 percent level)

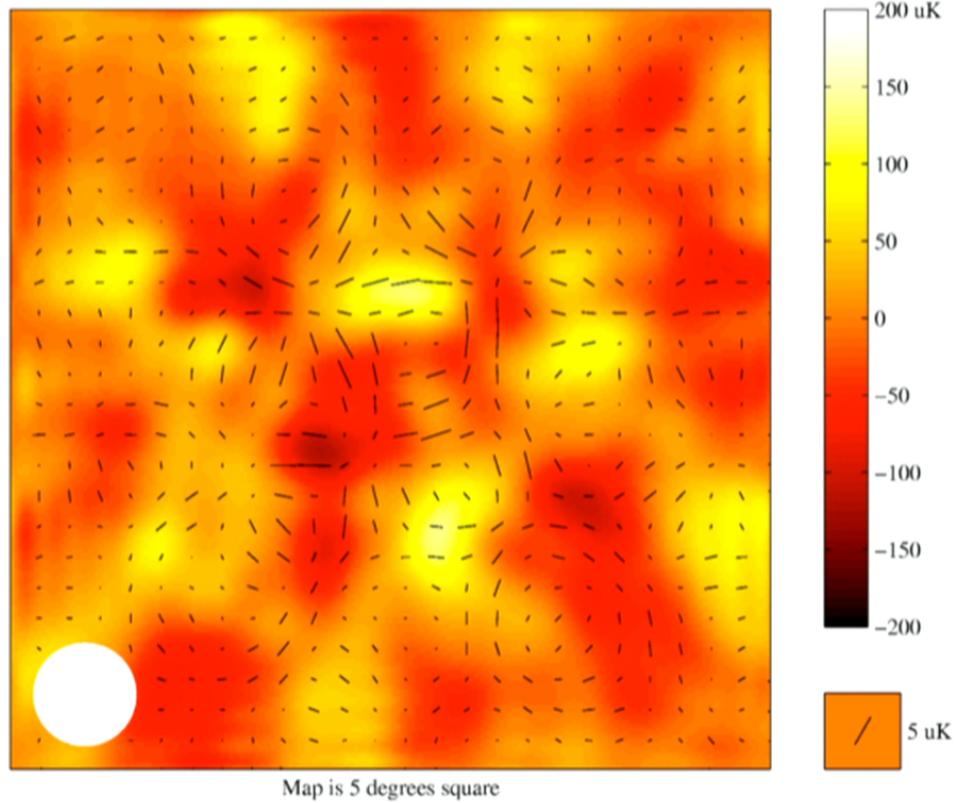
5. No fluctuation in composition (percent level)

6. No departures from Gaussianity

$$\frac{\text{Non-Gaussian}}{\text{Gaussian}} < 10^{-3} - 10^{-4}$$

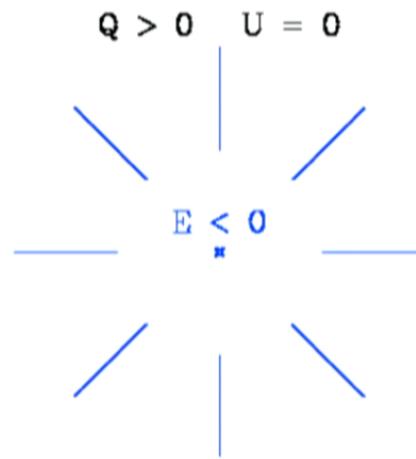
DASI

The Anisotropies are polarized

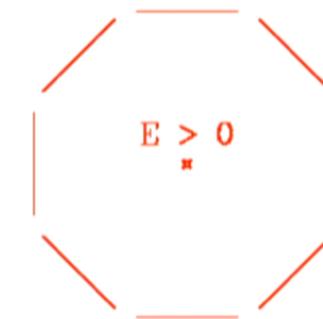


Kovac et al.  
[astro-ph/0209478](https://arxiv.org/abs/astro-ph/0209478)

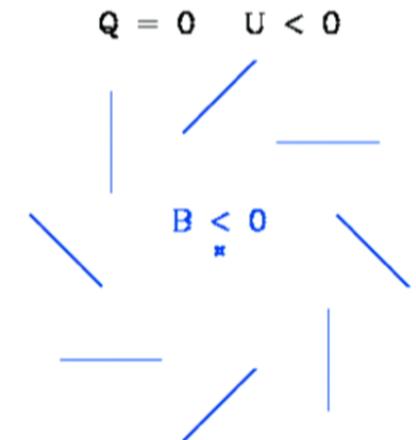
Density pert.  
&  
Gravity Waves



$Q < 0$     $U = 0$

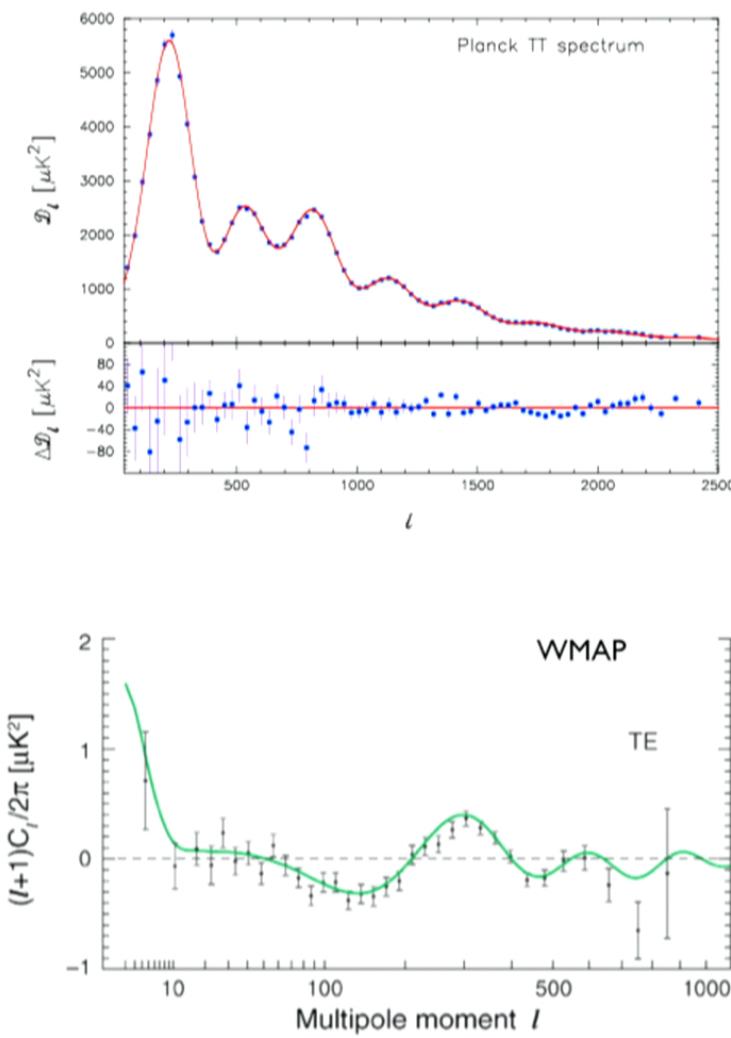


Gravity  
Waves



$Q = 0$     $U > 0$

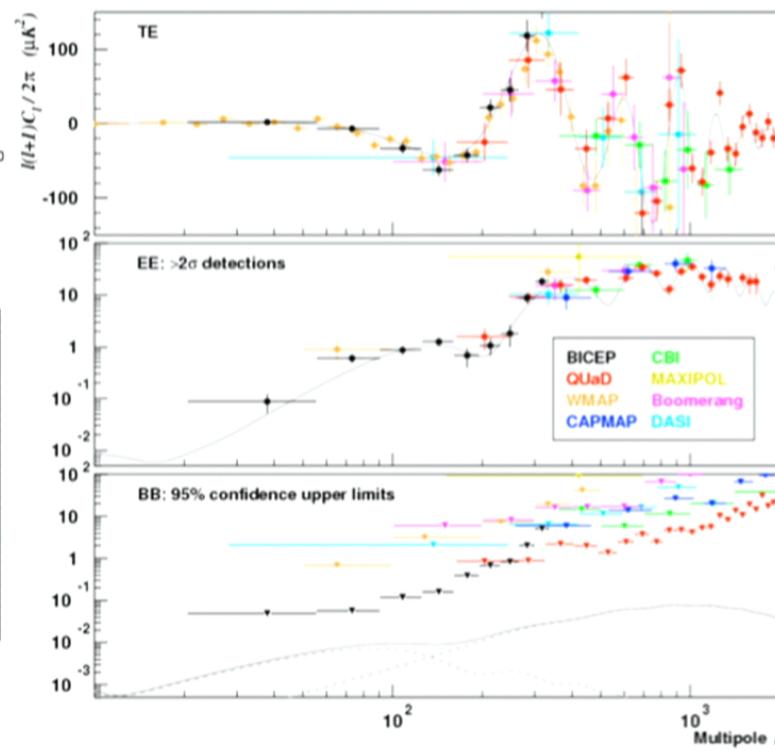


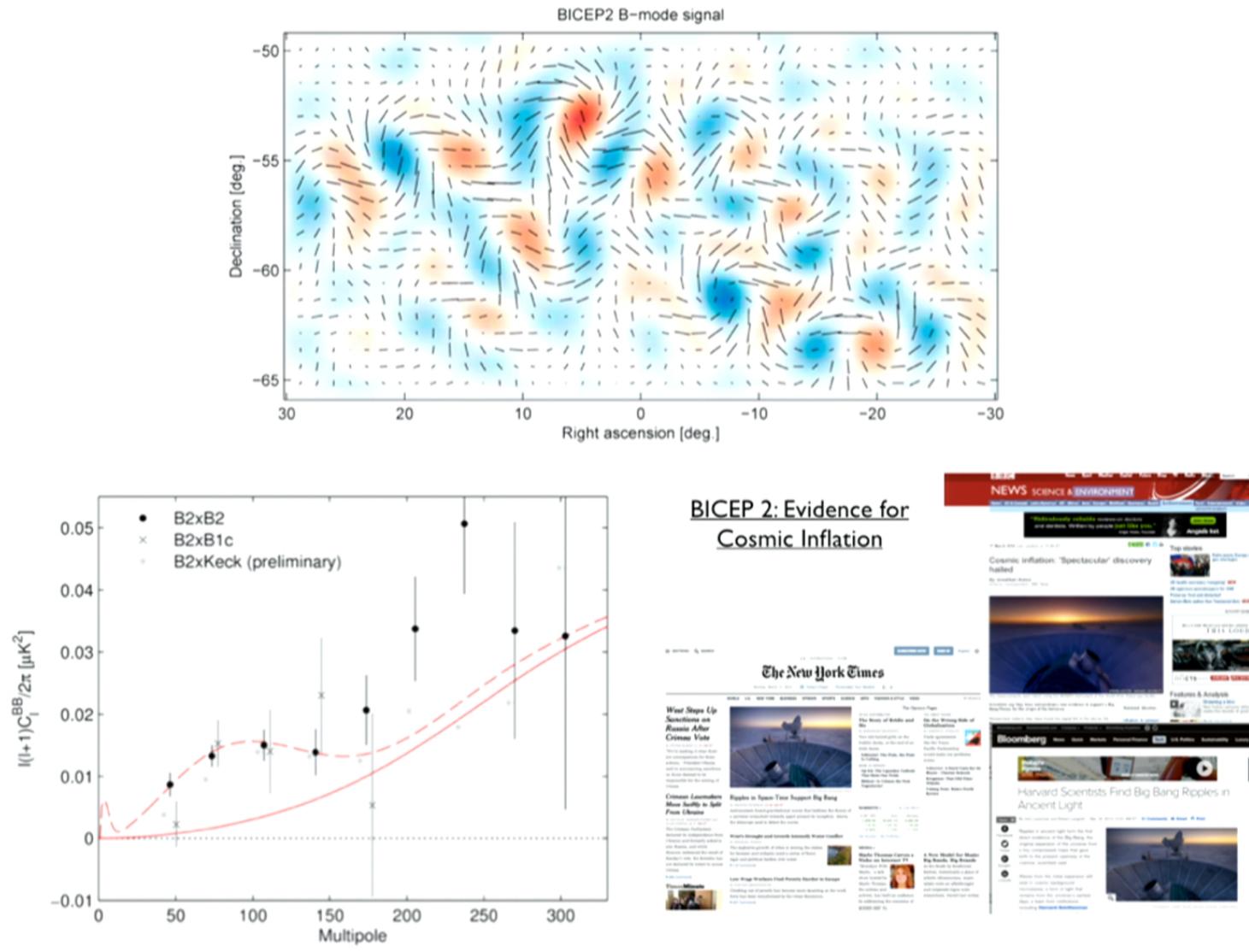


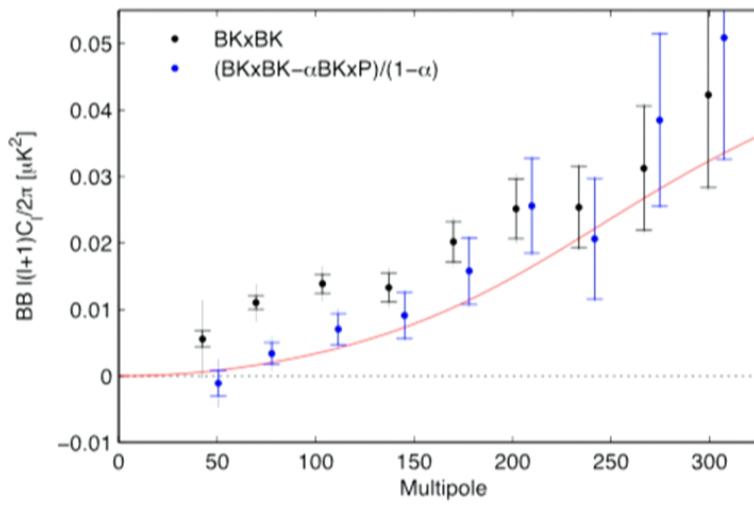
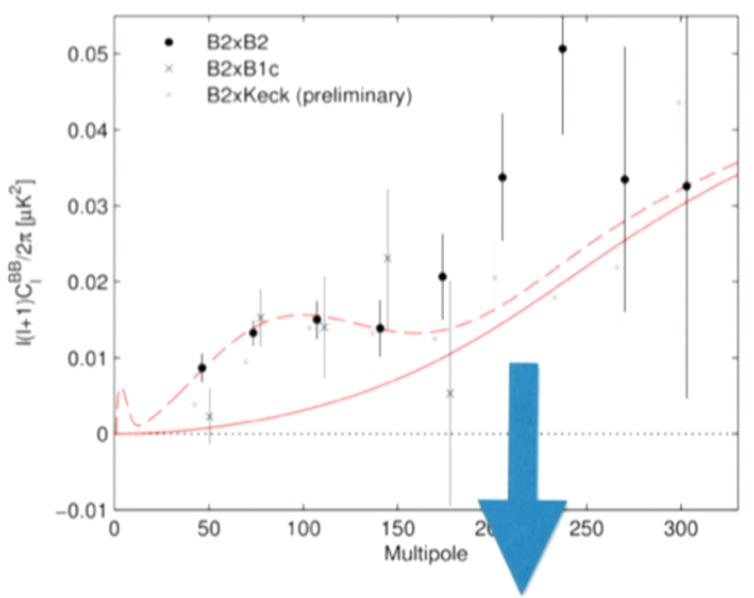
## State of the art prior to BICEP2

$$T \sim 10 \text{ to } 70 \mu\text{K}$$

$$E \sim 1 \text{ to } 5 \mu\text{K}$$







## What we have learned so far

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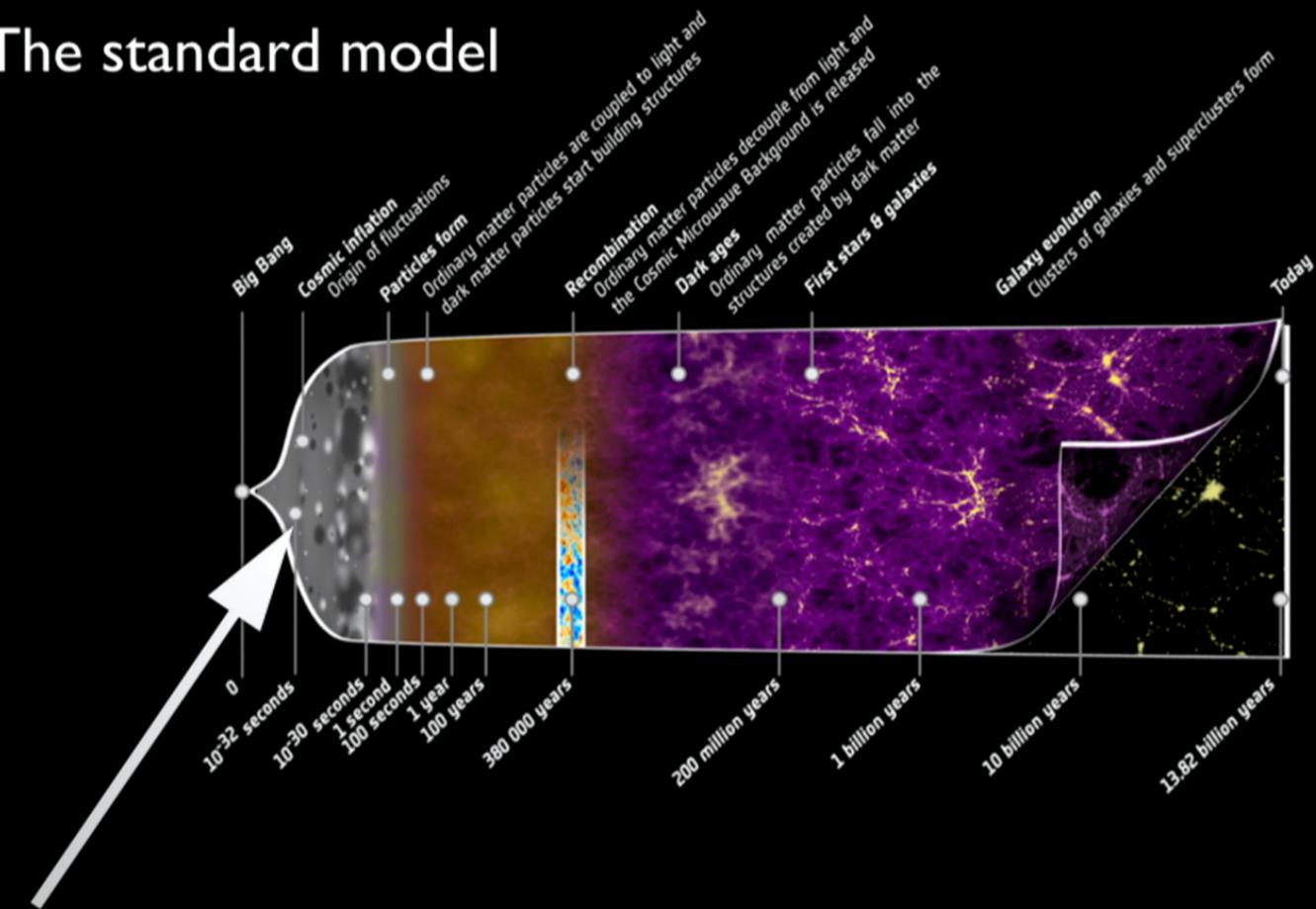
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# The standard model



Why is the Universe so old/big? Attractor solution.  
Seeds for structure formation are quantum fluctuations of the clock.

## Inflationary dynamics

Almost exponential expansion  
Only small departures from  
Cosmological Constant because  
Inflation has to end

$$ds^2 = -dt^2 + a^2(t)dx^2$$

$$H = \frac{\dot{a}}{a} \quad H^2 = \frac{V}{M_{pl}^2}$$

$$p = w\rho = (-1 + \epsilon)\rho$$

$$\epsilon = -\frac{\dot{H}}{H^2}$$

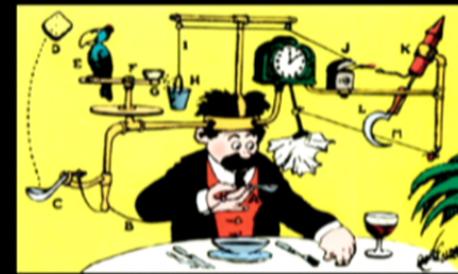
During this period the Universe must have expanded by roughly 60 enfolds

$$N = \ln(a_{\text{final}}/a_{\star}) \approx 60$$



Original models

Inflationary models require a clock



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## Big success of inflation

Quantum mechanics implies that the clock must fluctuate.

The Universe cannot be perfectly homogeneous.

Properties of the fluctuations are consistent with our best observations.

Potentially there is an additional fossil, a stochastic background of gravitational waves.

Calculations are under control.

## The origin of fluctuations

The clock fluctuations are “frozen” at horizon crossing (frequency of order  $H$ ). *We are probing the theory at an energy  $H$  which is roughly constant in time.* What we observe is the fluctuations in the expansion of one region relative to the other due to the clock fluctuations.

Amplitude of scalar and tensor fluctuations as a function of scale are determined by the expansion history during inflation.

$$\Delta_s^2(k) \equiv \Delta_{\mathcal{R}}^2(k) = \frac{1}{8\pi^2} \frac{H^2}{M_{\text{pl}}^2} \frac{1}{\varepsilon} \Big|_{k=aH}, \quad \text{wavenumber of fluctuations}$$
$$\Delta_t^2(k) \equiv 2\Delta_h^2(k) = \frac{2}{\pi^2} \frac{H^2}{M_{\text{pl}}^2} \Big|_{k=aH}, \quad \text{Frequency is of order Hubble}$$
$$\epsilon = -\frac{\dot{H}}{H^2}$$

Tensor to scalar ratio

$$r \equiv \frac{\Delta_t^2}{\Delta_s^2} = 16 \varepsilon_\star.$$

Scale dependence of fluctuations

$$\Delta_s^2(k) = \Delta_s^2(k_\star) \left( \frac{k}{k_\star} \right)^{n_s - 1}$$
$$n_s - 1 = \frac{1}{H} (2\dot{H}/H - \dot{\epsilon}/\epsilon)$$

Slope:  $1 - n_s = 0.0355 \pm 0.0049$    $(n_s - 1) \propto \frac{1}{N}$

?????

$$\Delta \propto \frac{H^2}{M_{pl}^2 \epsilon} \quad \epsilon = -\frac{\dot{H}}{H^2} = -\frac{d \ln H}{dN}$$

$$(n_s - 1) = \frac{d \ln \Delta}{d \ln k} = -2\epsilon - \frac{d \ln \epsilon}{dN}$$

$$\Delta_h \propto \frac{H^2}{M_{pl}^2} \quad r = 16\epsilon$$

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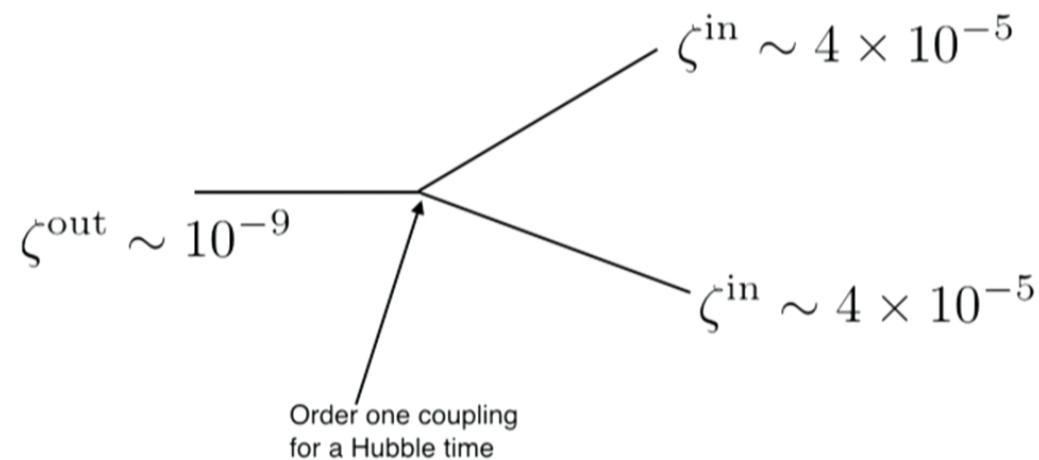
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$$\ln A_s = -19.932 \pm 0.034$$

### Higher order moments



Interactions produce a  $4 \times 10^{-5}$  corrections to what was already there.  
Detection requires  $10^9$  modes

$$\ln A_s = -19.932 \pm 0.034$$

### Higher order moments

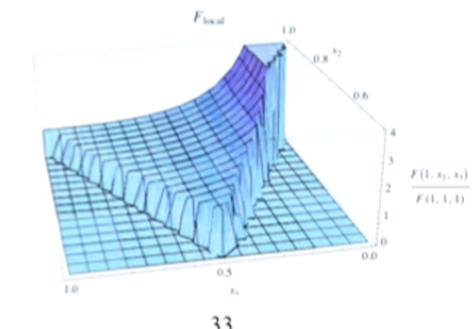
$$\zeta^{\text{out}} \sim 10^{-9}$$

$f_{NL}$

$$\zeta^{\text{in}} \sim 4 \times 10^{-5}$$

$$\zeta^{\text{in}} \sim 4 \times 10^{-5}$$

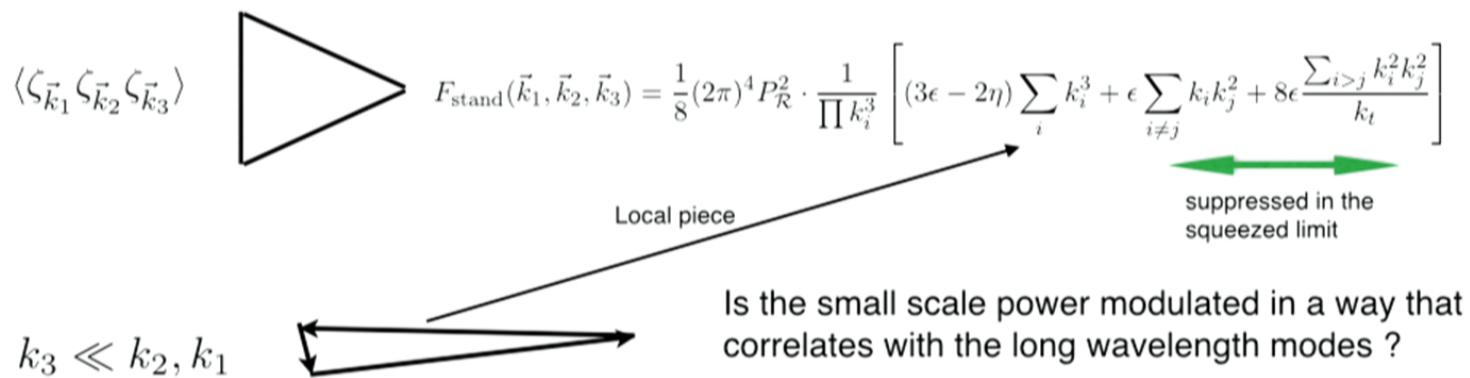
|                     | Independent KSW | ISW-lensing subtracted KSW      |
|---------------------|-----------------|---------------------------------|
| SMICA               |                 |                                 |
| Local . . . . .     | $9.8 \pm 5.8$   | <b><math>2.7 \pm 5.8</math></b> |
| Equilateral . . . . | $-37 \pm 75$    | <b><math>-42 \pm 75</math></b>  |
| Orthogonal . . . .  | $-46 \pm 39$    | <b><math>-25 \pm 39</math></b>  |



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## Three point-function in single field slow roll inflation

$$ds^2 = -dt^2 + a^2(t)e^{2\zeta(x,t)}dx^2$$



The small scale power is independent of the amplitude of the long mode.

This is a consequence of the “sequential hiding” of modes and attractor solution.

Local non-Gaussianity is analog to a fluctuation in composition but in something that is conserved.

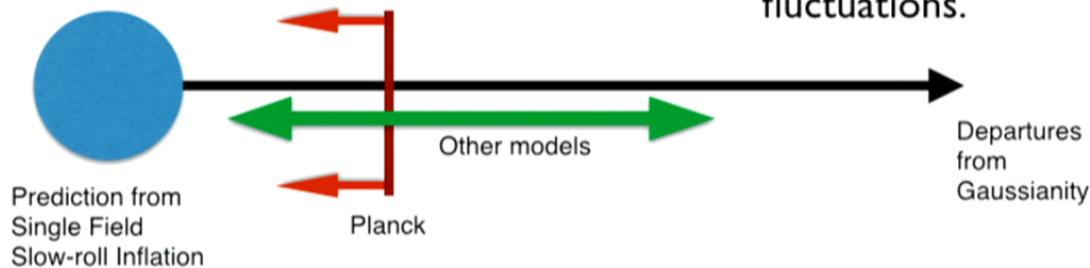
## Planck 2015

| $f_{NL}(KSW)$     |                |                        |
|-------------------|----------------|------------------------|
| Shape and method  | Independent    | ISW-lensing subtracted |
| SMICA ( $T$ )     |                |                        |
| Local .....       | $10.2 \pm 5.7$ | $2.5 \pm 5.7$          |
| Equilateral ..... | $-13 \pm 70$   | $-16 \pm 70$           |
| Orthogonal .....  | $-56 \pm 33$   | $-34 \pm 33$           |
| SMICA ( $T+E$ )   |                |                        |
| Local .....       | $6.5 \pm 5.0$  | $0.8 \pm 5.0$          |
| Equilateral ..... | $3 \pm 43$     | $-4 \pm 43$            |
| Orthogonal .....  | $-36 \pm 21$   | $-26 \pm 21$           |

## Target

$f_{NL}^{local} \leq 1$  Single field Inflation

$f_{NL}^{eq} \leq 1$  Slow-Roll single field Inflation



In the Standard story:

Local non-Gaussianity is zero because of attractor nature of inflation. Can only be true for clock.

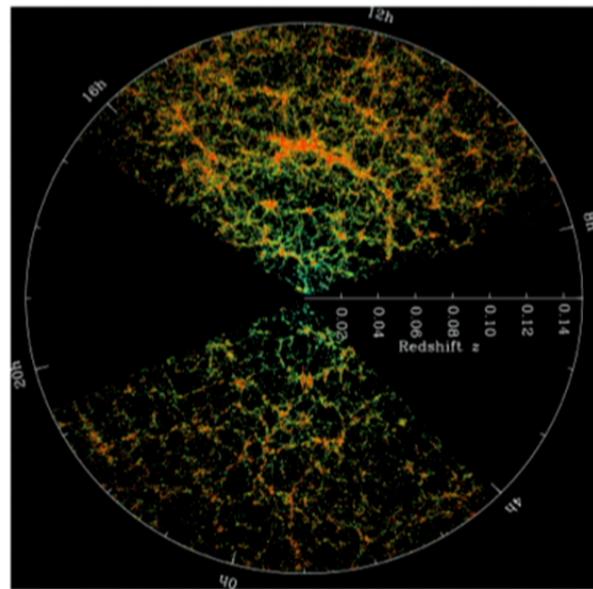
If the theory for the perturbations can also describe the background then equilateral non-G are small.

Equilateral part can be really tiny because we are looking at time delay fluctuations, actual change in the space-time is down by epsilon.

“Collapsed” non-Gaussianities are very small because we are seeing vacuum fluctuations.

## Can we improve over CMB?

We either constrain a different period during inflation to test if indeed things were approximately time translation invariant or we have to surpass the statistical precision of the CMB.

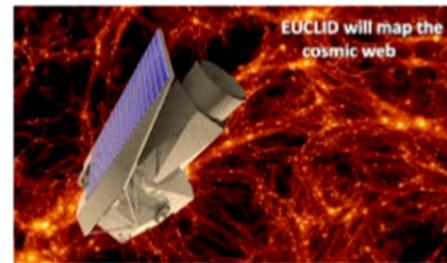


Constraints are statistical in nature, they scale as

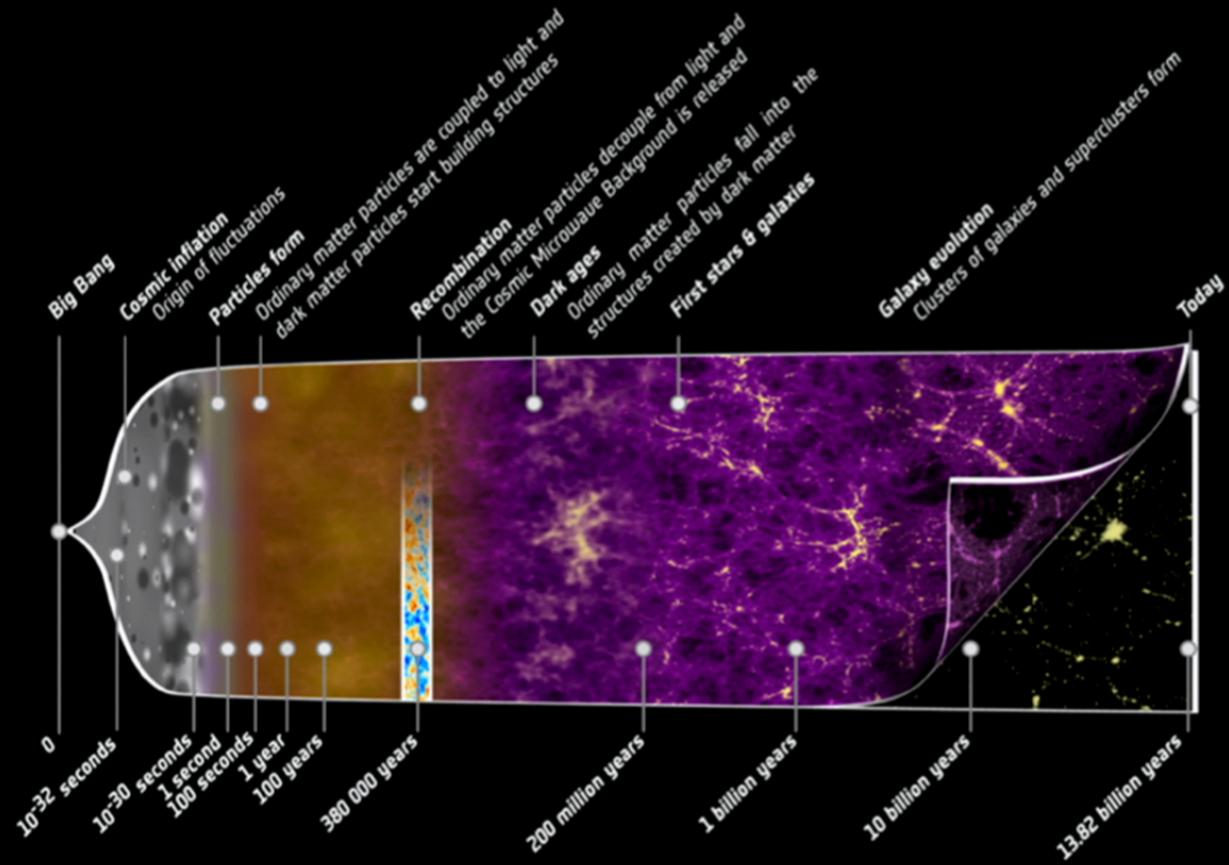
$$1/N_{\text{modes}}^{-1/2}$$

|                               | LSST                         | DESI   | Euclid   | SPHEREx                  | CHIME            |
|-------------------------------|------------------------------|--|--|--------------------------|------------------|
| Survey type                   | photo                        | spectro  | photo+spectro  | low-res spectro          | 21-cm            |
| Ground or space               | ground                       | ground   | space  | space                    | ground           |
| Previous surveys              | CFHTLS, DES, HSC             | BOSS, eBOSS, PFS                                   | no direct precursor                                    | PRIMUS, COMBO-17, COSMOS | GBT HIM          |
| Survey start                  | 2020                         | 2020   | 2018   | 2020                     | 2016             |
| Redshift-range                | $z < 3$ (1% sources above 3) | $z < 1.4$ , $2 < z < 3.5$ (Ly $\alpha$ )           | $z < 3$  | $z < 1.5$                | $0.75 < z < 2.5$ |
| Survey area [deg $^2$ ]       | 20k                          | 14k  | 15k  | 40k                      | 20k              |
| Approximate number of objects | $2 \times 10^9$ (WL sources) | $22 \times 10^6$ gal., $\sim 2.4 \times 10^5$ QSOs | $40 \times 10^6$ redshifts, $1.5 \times 10^9$ photo-zs | $15 \times 10^9$ pixels  | $10^7$ pixels    |
| Galaxy clustering             | ✓✓ <sup>°</sup>              | ✓  | ✓  | ✓                        | ✓                |
| Weak lensing                  | ✓                            |  | ✓  |                          | ✓                |
| RSD                           |                              | ✓  | ✓  | ✓✓                       | ✓✓               |
| Multi-tracer                  | ✓✓                           | ✓✓   | ✓✓   | ✓                        |                  |

**Table 2.** A selection of currently funded or planned surveys. Other important surveys not included in the table are PFS, JPAS, PAU, EMU. Relevant survey links [[LSST](#)],[[DESI](#)],[[Euclid](#)], [[UBC](#)],[[PFS](#)], [[JPAS](#)],[[PAU](#)], [[EMU](#)]. <sup>°</sup>Galaxy clustering is possible, but very strong radial degradation.



## Is inflation the final theory ?



A “multiverse” is an alternative

