

Title: Astroparticle Physics Theory: Dark Matter Distribution in MW

Date: Jul 06, 2015 03:45 PM

URL: <http://pirsa.org/15070016>

Abstract:

DM MASS

$$10^{-22} \text{ eV} \lesssim m_\chi \lesssim 10^{59} \text{ eV}$$

lower bound:

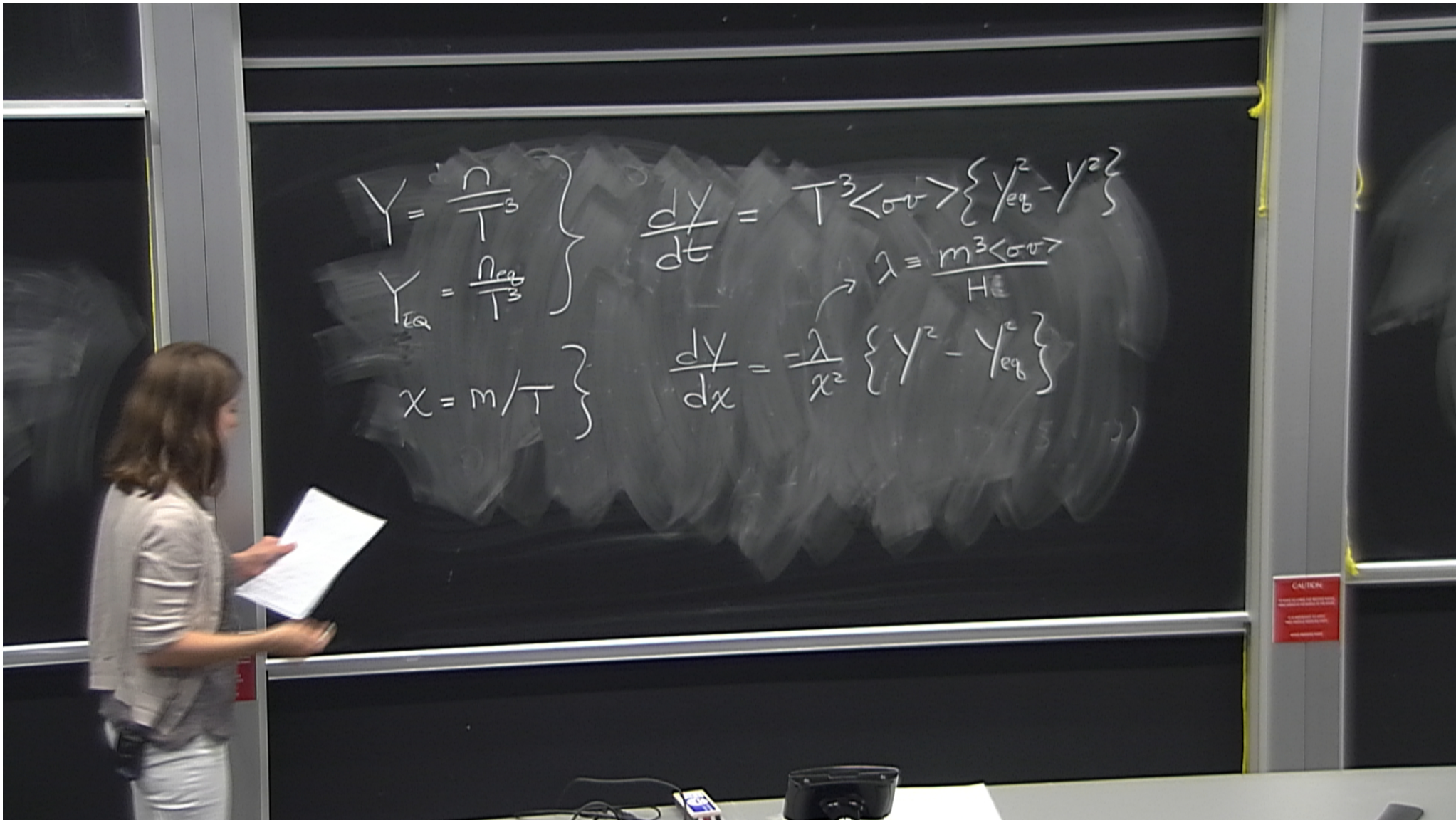
DM is ultralight boson

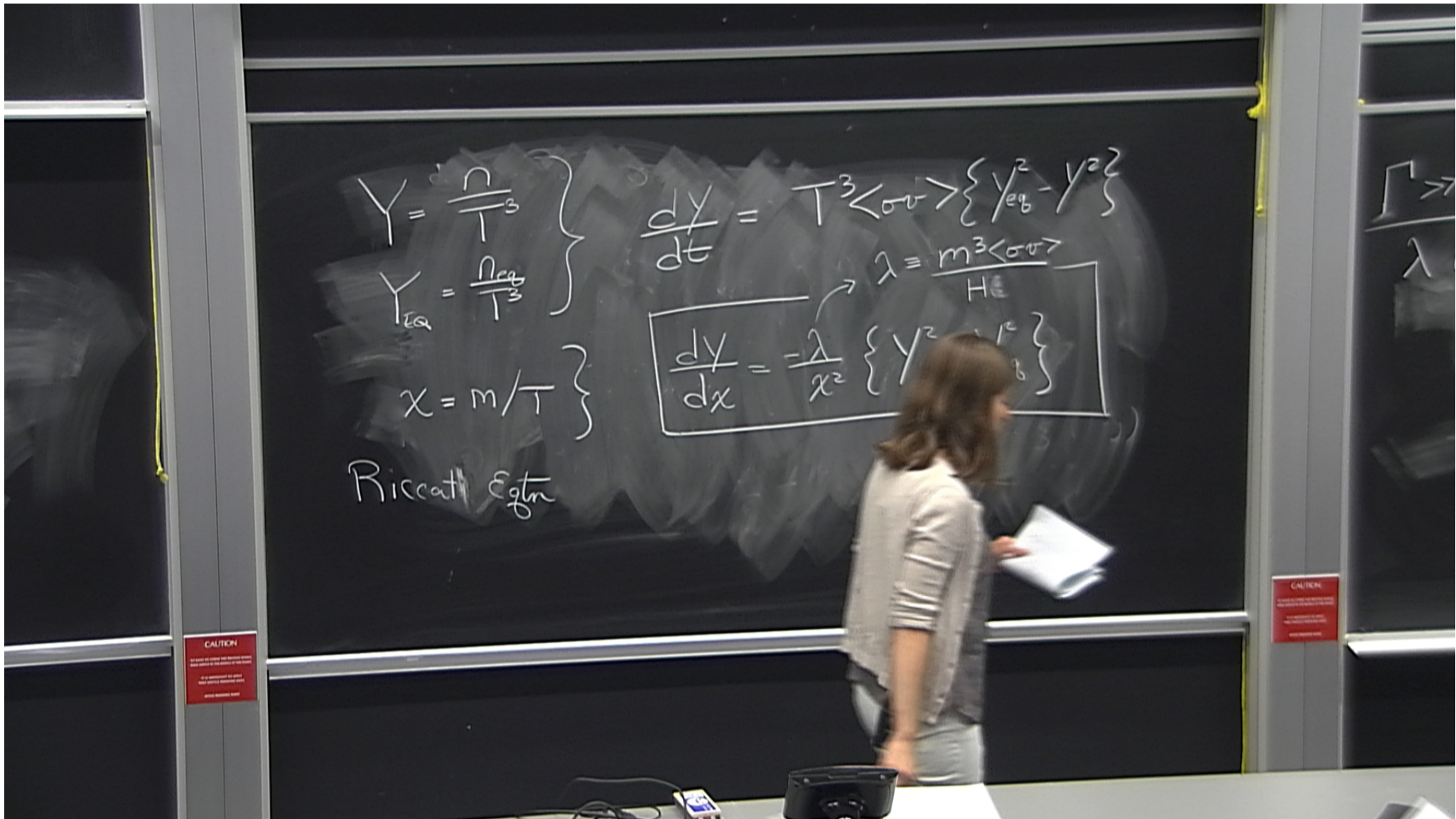
classical field

Stability of DM halo

upper bound: compact halo objects

microlensing limits





$$Y = \frac{n}{T^3}$$

$$Y_{eq} = \frac{n_{eq}}{T^3}$$

$$x = m/T$$

Riccati Eqtn

$$\frac{dY}{dt} = T^3 \langle \sigma \rangle \{ Y_{eq}^2 - Y^2 \}$$

$$\lambda = \frac{m^3 \langle \sigma \rangle}{H^2}$$

$$\frac{dY}{dx} = -\frac{\lambda}{x^2} \{ Y^2 - Y_{eq}^2 \}$$

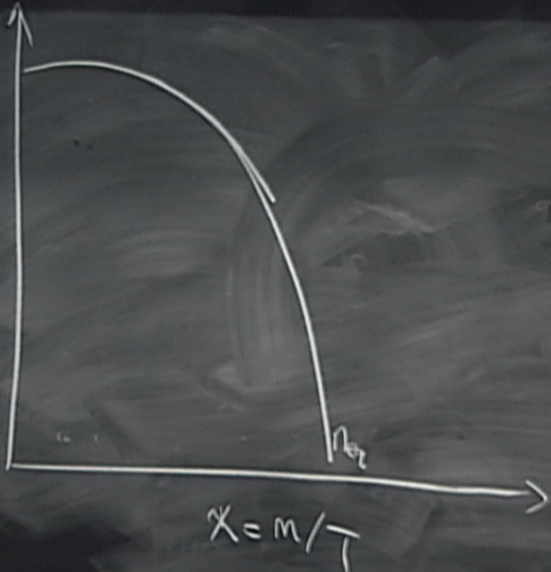
$$\frac{dY}{dt} = T^3 \langle \sigma \sigma \rangle \{ Y_{eq}^2 - Y^2 \}$$
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$$\Gamma \gg H$$

λ is large

Y tracks equilibrium value

$$v = \frac{c}{n}$$



CAUTION
DO NOT TOUCH THE SURFACE
OF THE LENS OR THE SURFACE
OF THE PRISM OR THE SURFACE
OF THE MIRROR.
HANDLE WITH CARE.

$$\langle \sigma \sigma \rangle \sim \left\{ \frac{1}{2} - \frac{1}{2} \right\}$$

$$\lambda \equiv \frac{m^3 \langle \sigma \sigma \rangle}{H^2}$$

$$\left\{ \frac{1}{2} - \frac{1}{2} \right\}$$

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λ is large
 Y tracks equilibrium value

$$\Gamma \ll H$$

$$\frac{dY}{dx} \approx -\frac{\lambda Y^2}{x^2}$$

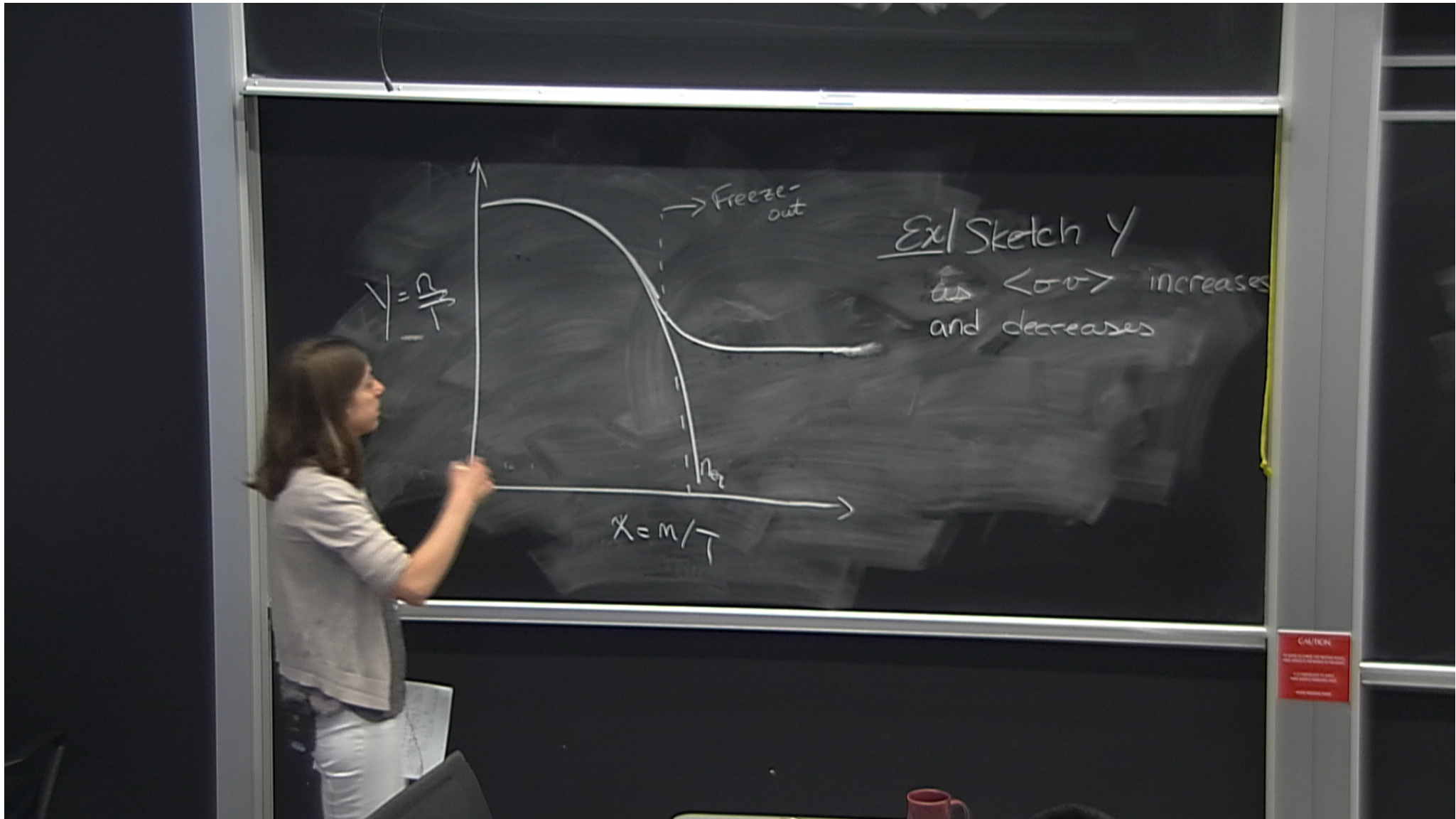
$$\Rightarrow \frac{1}{Y_\infty} - \frac{1}{Y_F} \approx \frac{\lambda}{x_F} \Rightarrow \frac{1}{Y_\infty} \approx \frac{\lambda}{x_F}$$

CAUTION

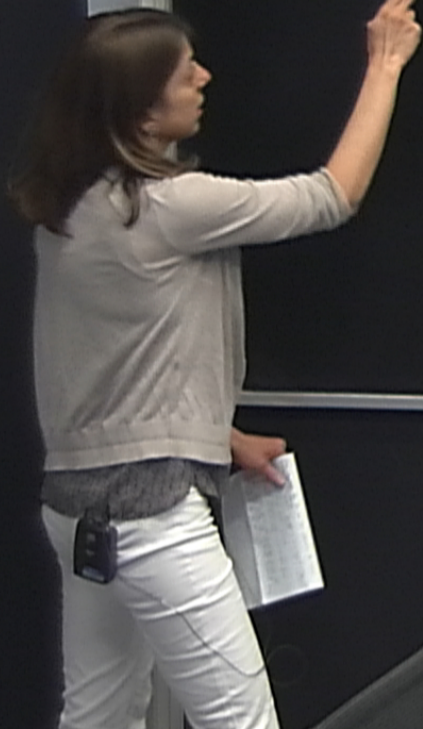


Ex Sketch Y

as $\langle \sigma v \rangle$ increases
and decreases



$$\Omega_x h^2 \approx \frac{0.1 \text{ pb}}{\langle \sigma_x v \rangle} \approx 0.1 \left(\frac{0.01}{\alpha} \right)^2 \left(\frac{M_x}{100 \text{ GeV}} \right)^2$$



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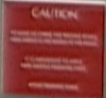
\downarrow
 0.1199 ± 0.0027

WIMP "MIRACLE"

lower bound $m_x \gtrsim \text{keVish}$ (WDM)

Upper bound $m_x \lesssim 100 \text{ TeV}$

partial wave unitarity constraints





$$\Omega_{\chi} h^2 \approx \frac{0.1 \text{ pb}}{\langle \sigma_{\chi\nu} \rangle} \approx 0.1 \left(\frac{0.01}{\alpha} \right)^2 \left(\frac{m_{\chi}}{100 \text{ GeV}} \right)^2$$

\Downarrow
 $199 \approx 0.0027$

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partial wave unitarity constraints

WIMP
 m_{χ}
 Boltzmann

scale factor

CAUTION

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How much of a miracle is this?

ex 1 | $\alpha \ll 1$ while α^2/m^2 fixed

WIMPLess
Feng+Kumar 0803.4196

ex 2 | Relic density is set by $3 \rightarrow 2$ annihilations
rather than $2 \rightarrow 2 \Rightarrow$ lighter DM masses (\sim GeVish)

Carlson, Machacek,
Hall

Hochberg et al
1402.5143

ex 3 | Asymmetric DM

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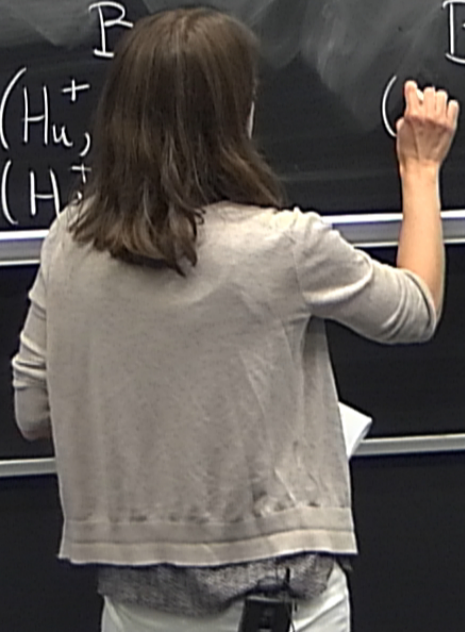
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ex 3 | Asymmetric DM

Case Study SUSY Neutrino
(natural WIMP candidate)

Supersymmetry: symmetry that relates bosons + fermions

<u>NAME</u>	<u>BOSON/SCALAR</u>	<u>SPIN-1/2</u>
winos, W bosons	W^\pm, W^0	$\tilde{W}^\pm, \tilde{W}^0$
bino, B boson	B (H_u^+ , H_d^+)	\tilde{B}^0



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Higgs, Higgsinos	(H_u^+, H_u^0) (H_d^+, H_d^0)	$(\tilde{H}_u^+, \tilde{H}_u^0)$ $(\tilde{H}_d^+, \tilde{H}_d^0)$

MIXING AFTER
ELECTROWEAK
SB

not diagonal

MASS EIGENSTATE

$$\bar{\chi}_i = c_1 \tilde{B} + c_2 \tilde{W} + c_3 \tilde{H}_u + c_4 \tilde{H}_d$$

NEUTRALINO

Charginos

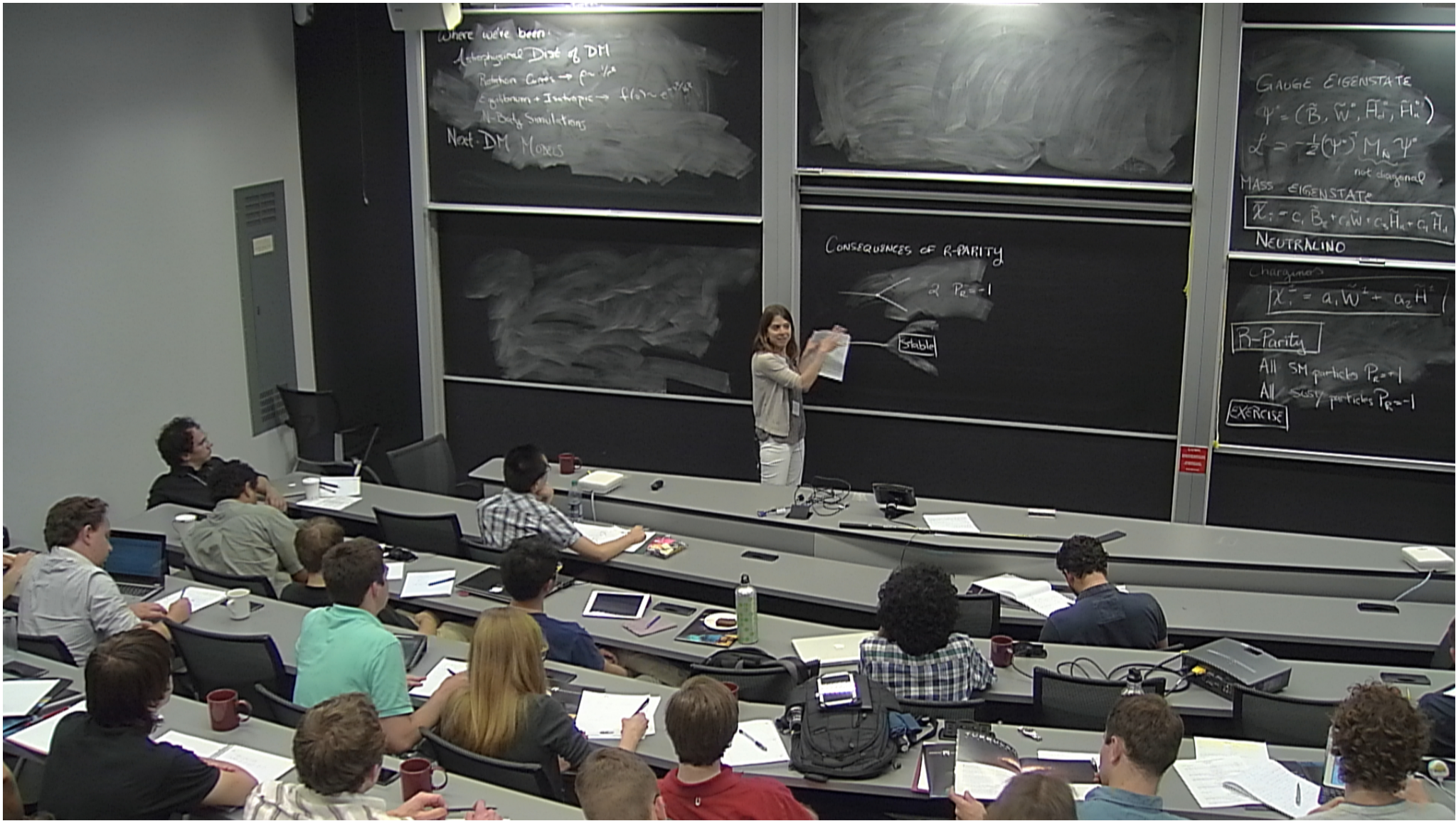
$$\chi_i^\pm = a_1 \tilde{W}^\pm + a_2 \tilde{H}^\pm$$

R-Parity

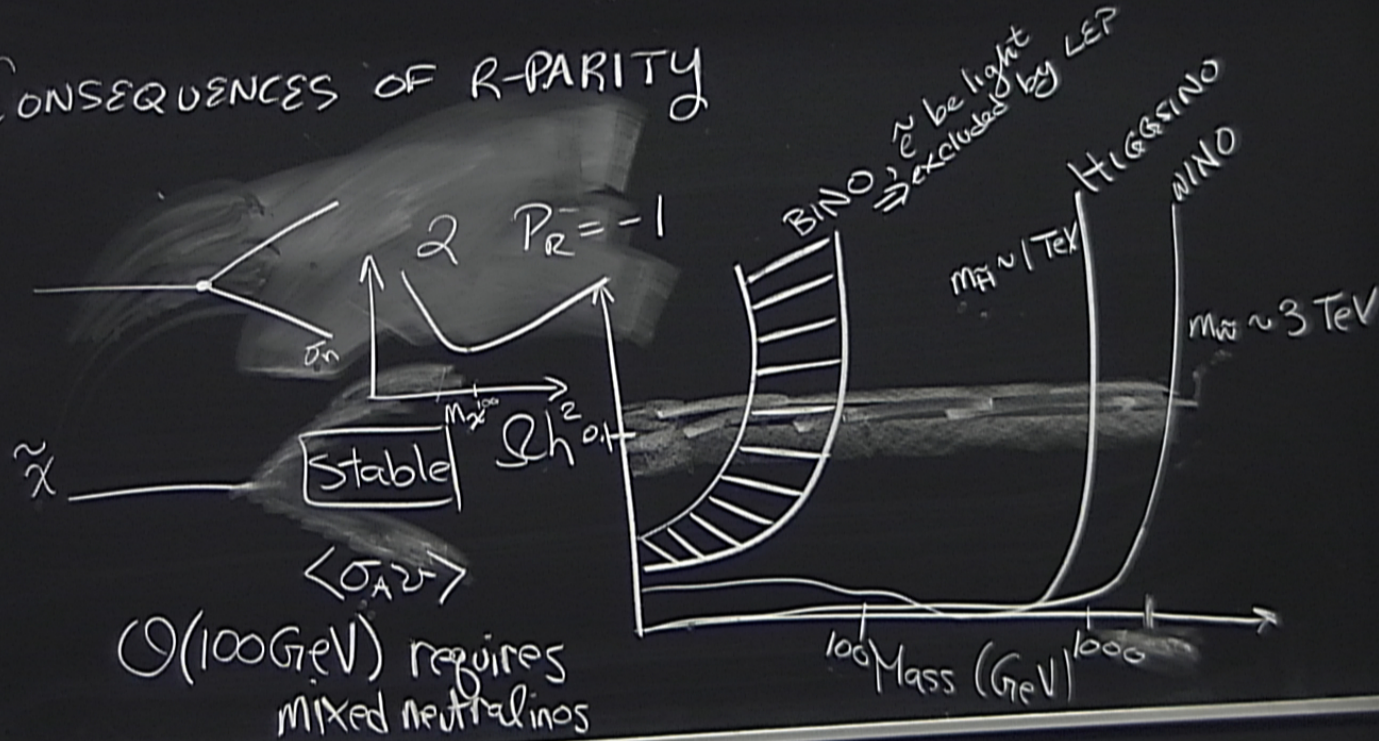
All SM particles $P_R = +1$

All SUSY particles $P_R = -1$

EXERCISE



CONSEQUENCES OF R-PARITY



$\chi_i =$
NEO

Charge
 χ

R-Par
All
All
EXERCISE

CAUTION

CAUTION

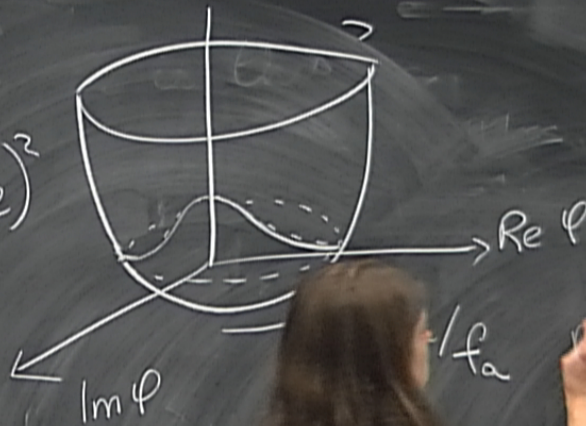
Promote $\Theta \rightarrow \frac{a}{f_a}$ ← axion field

Potential is minimized when $a=0$

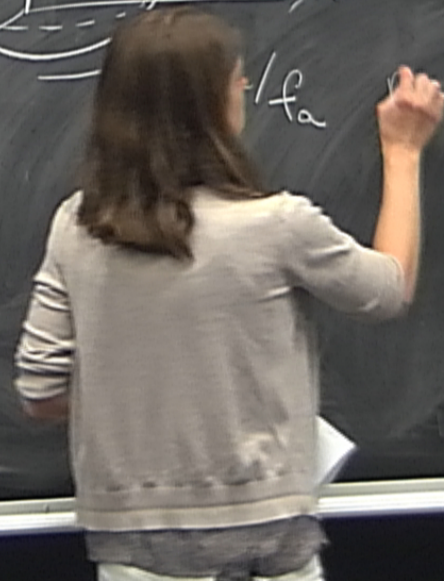
- 1) Very high energies, we introduce ψ that is charged $U(1)_{PQ}$
- 2) When $T \lesssim f_a$,

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$$V(\varphi) = \lambda (|\varphi|^2 - f_a/2)^2$$



3)

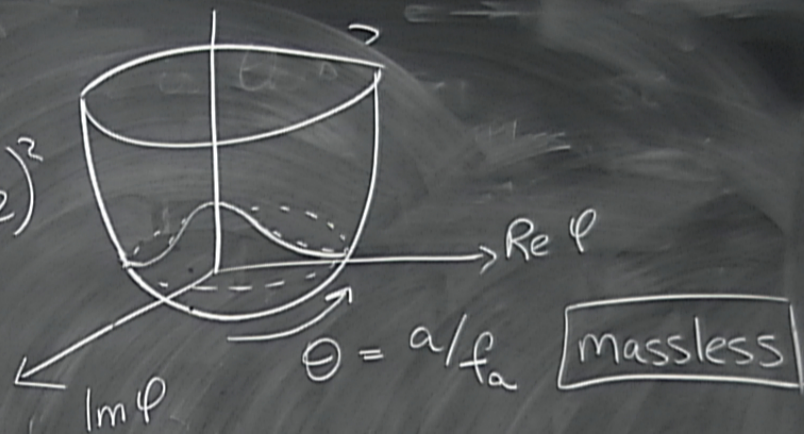


CAUTION

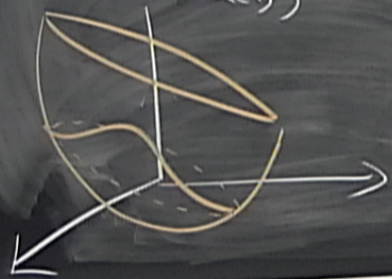
CAUTION

2) When $T \approx f_a$

$$V(\varphi) = \lambda \left(|\varphi|^2 - \frac{f_a}{2} \right)^2$$



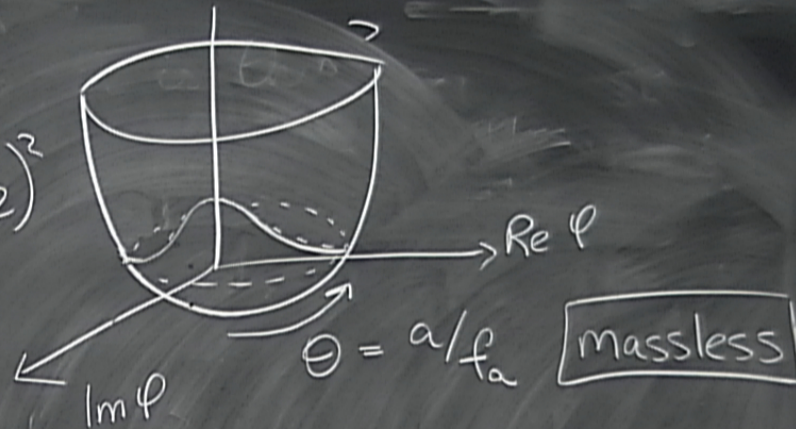
3) $T \sim \Lambda_{QCD}$, QCD instanton effects give axion mass



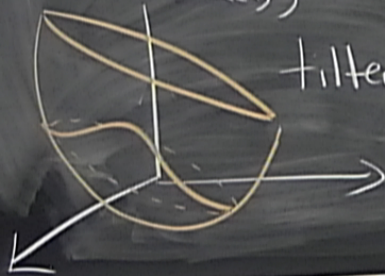
Mixed neutralinos $100 \text{ Mass (GeV)}^{1000}$

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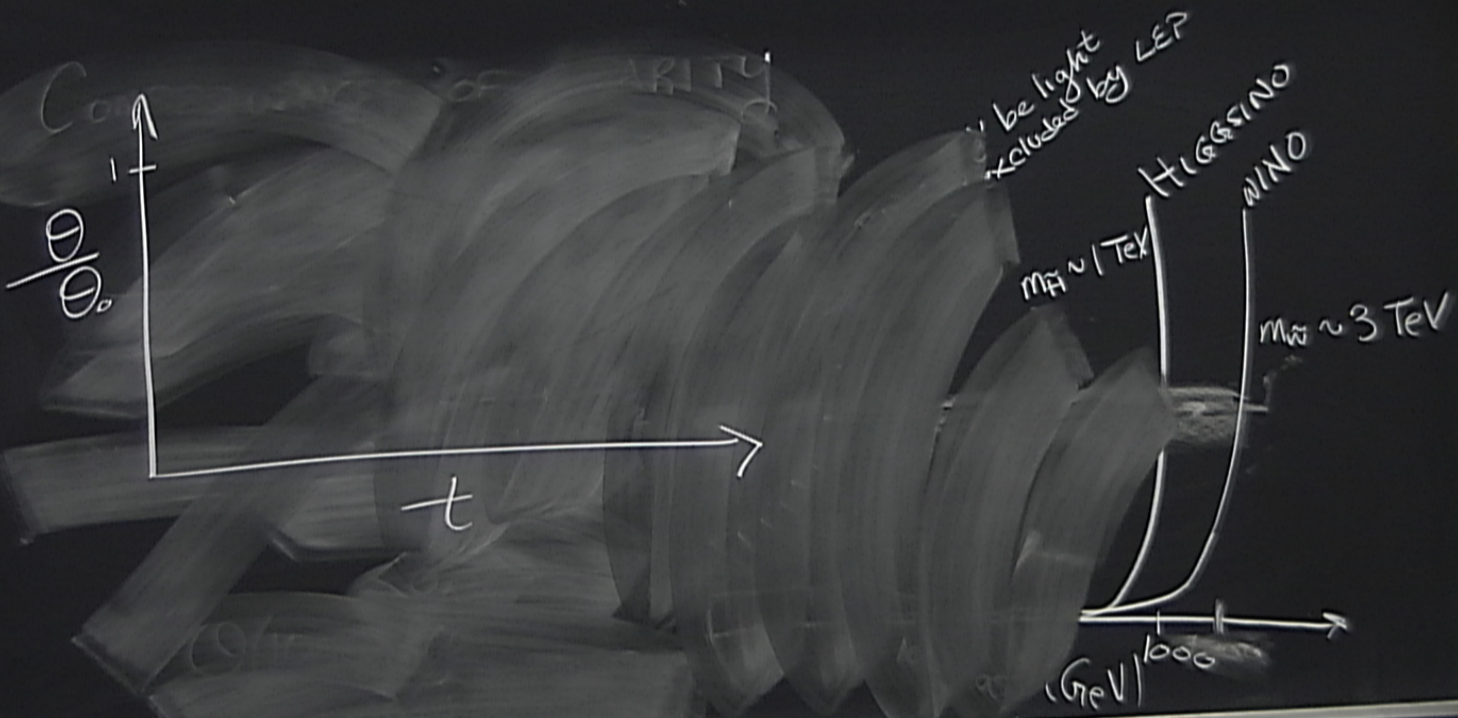
$$V(\varphi) = \lambda(|\varphi|^2 - f_a/2)^2$$



3) $T \sim \Lambda_{\text{QCD}}$, QCD instanton effects give axion mass
tilted potential

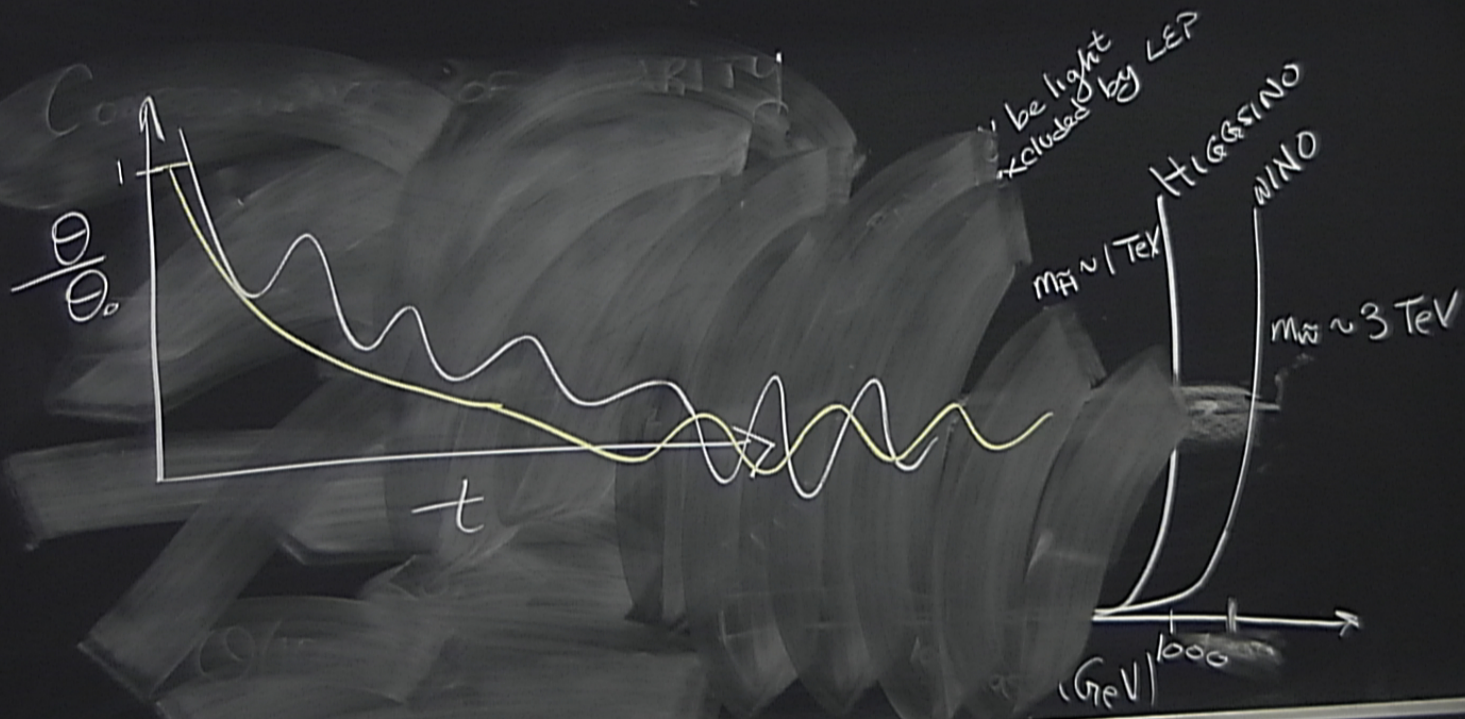


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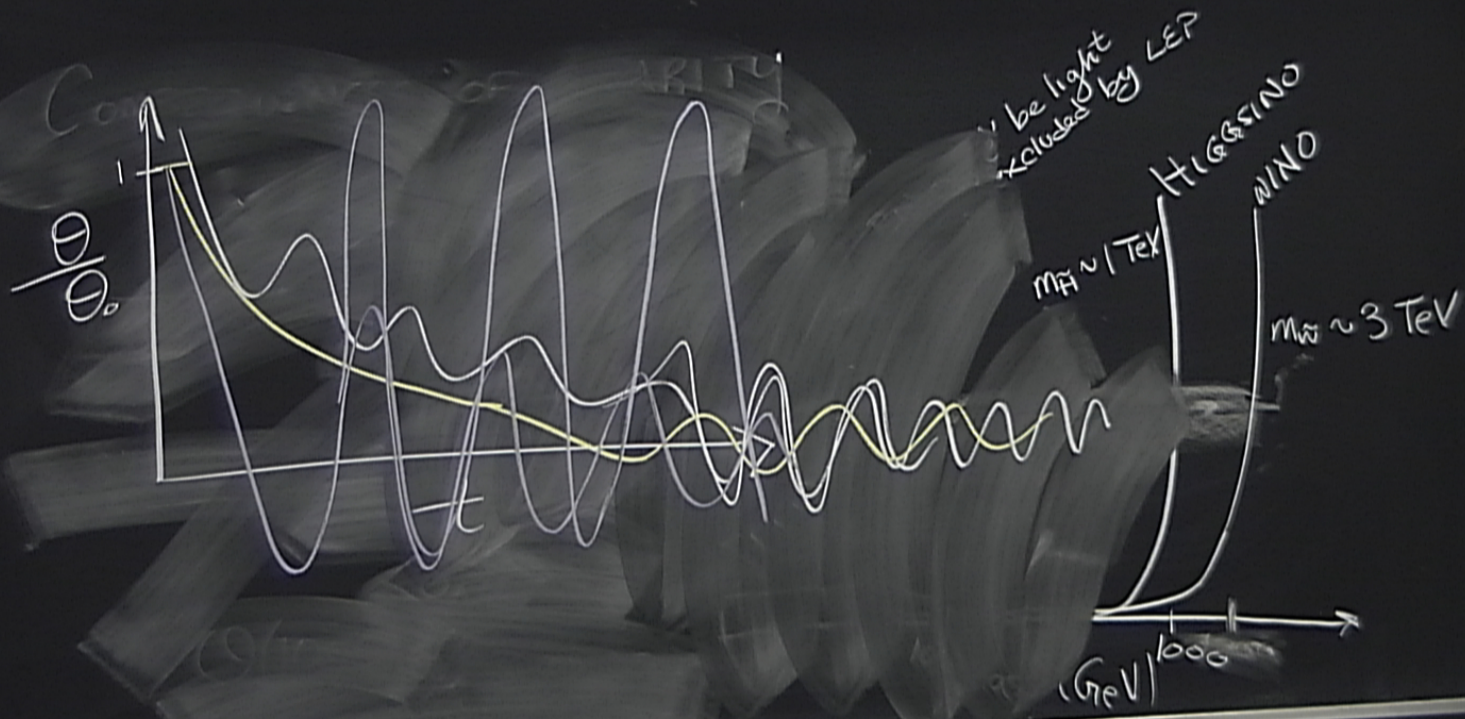


CAUTION

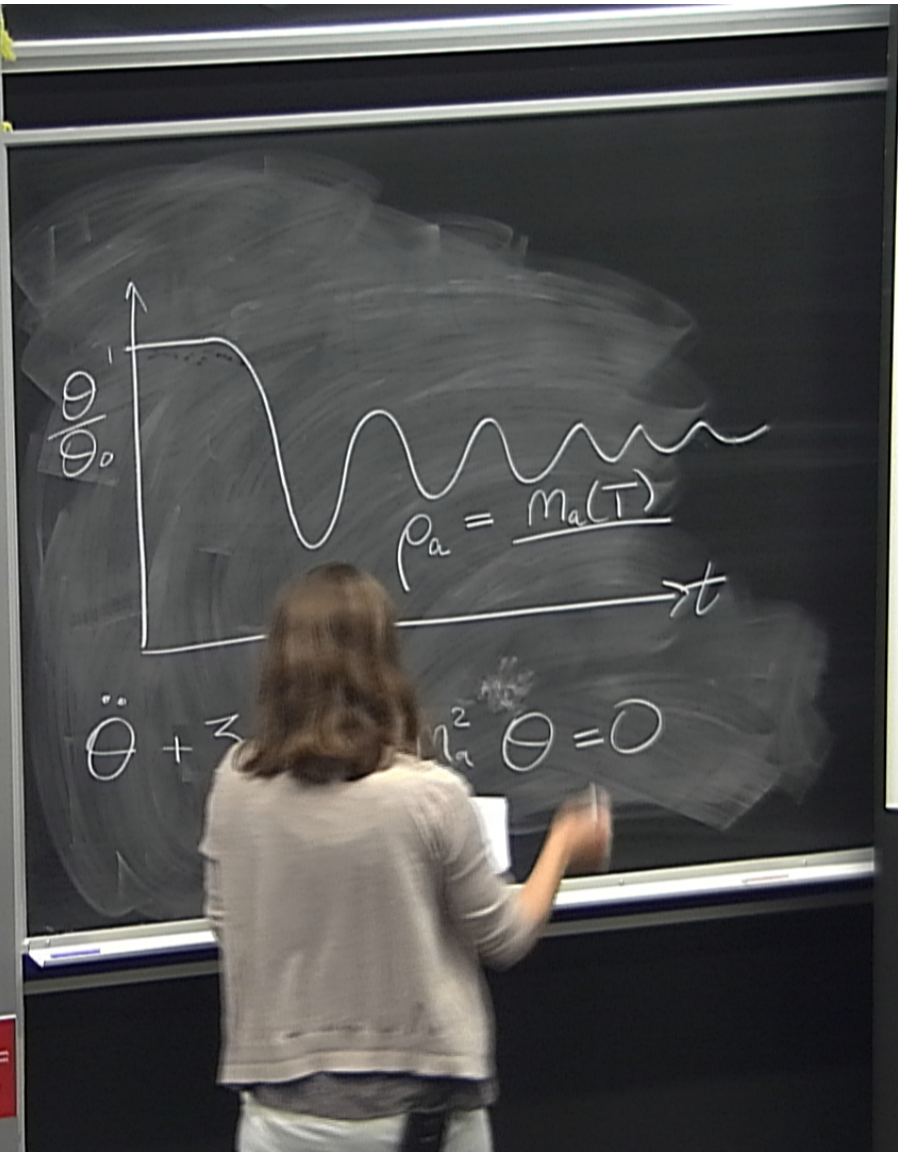
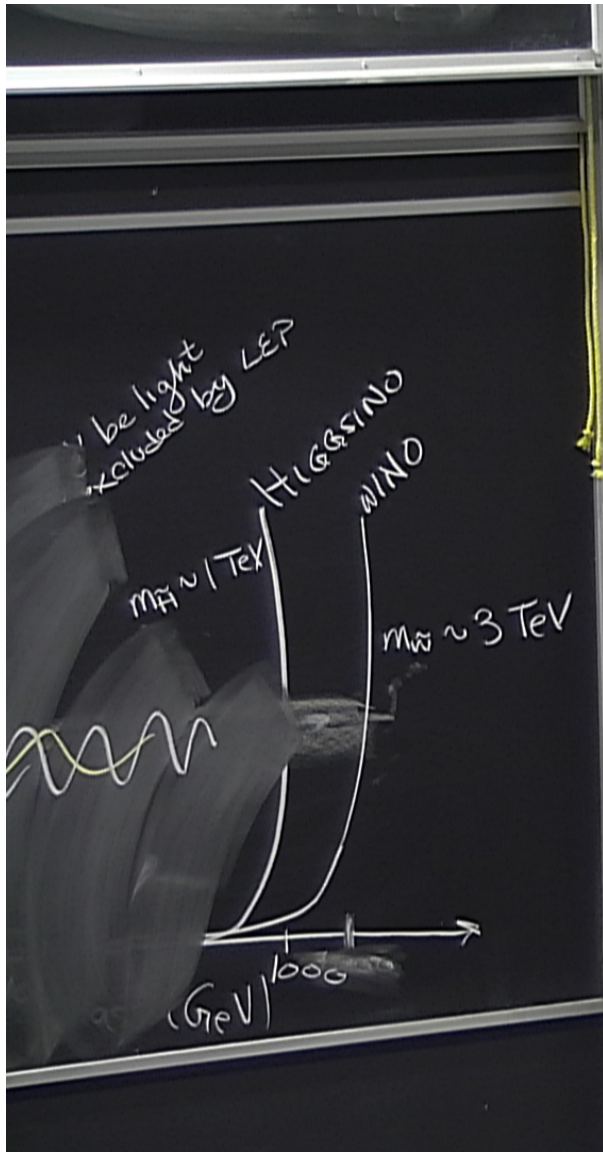
CAUTION



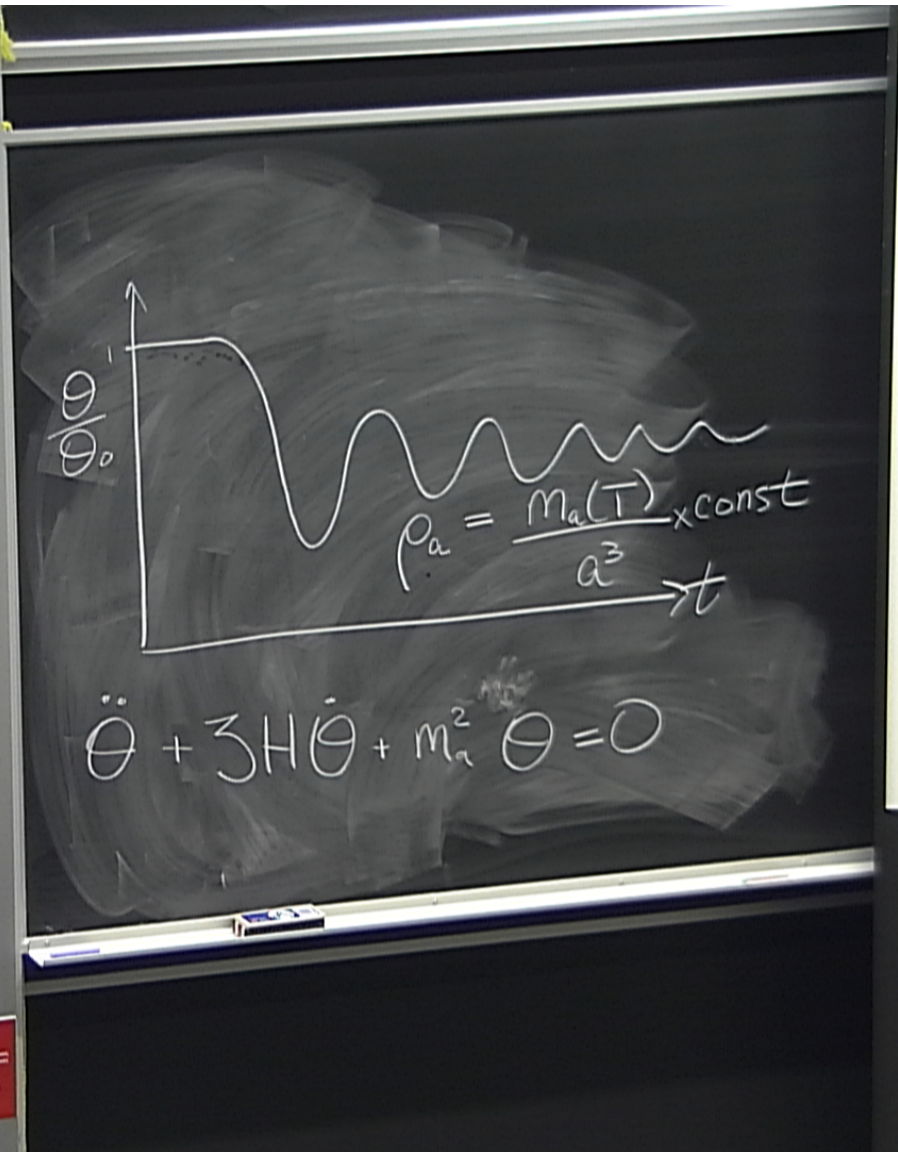
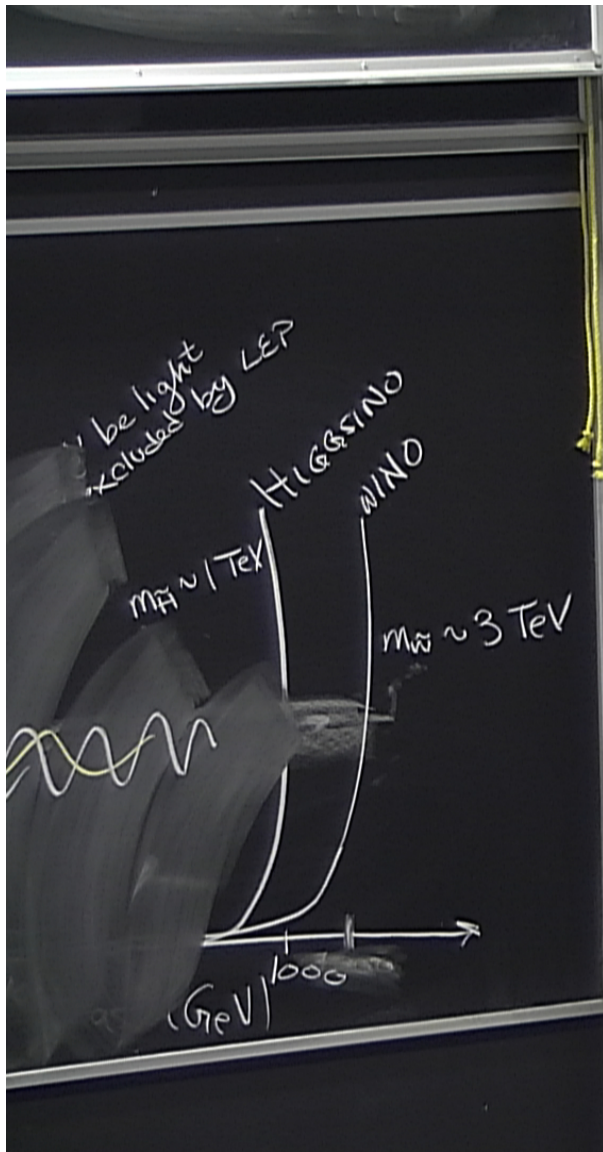
CAUTION
 Do not touch the board when the board is in use.
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CAUTION
 DO NOT TOUCH THE BOARD WHEN THE BOARD IS HOT.
 IT IS DANGEROUS TO TOUCH THE BOARD WHEN IT IS HOT.
 THANK YOU FOR YOUR ATTENTION.



CAUTION
Do not touch the chalkboard
with sharp objects or
use it as a support for
any other objects.

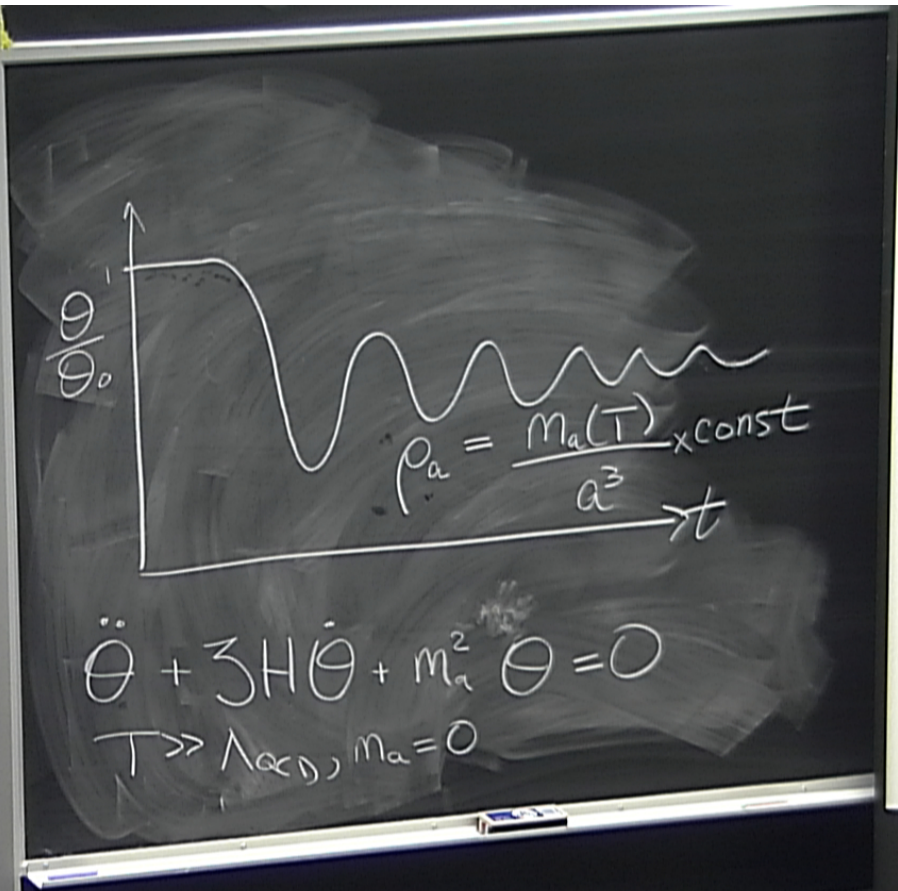
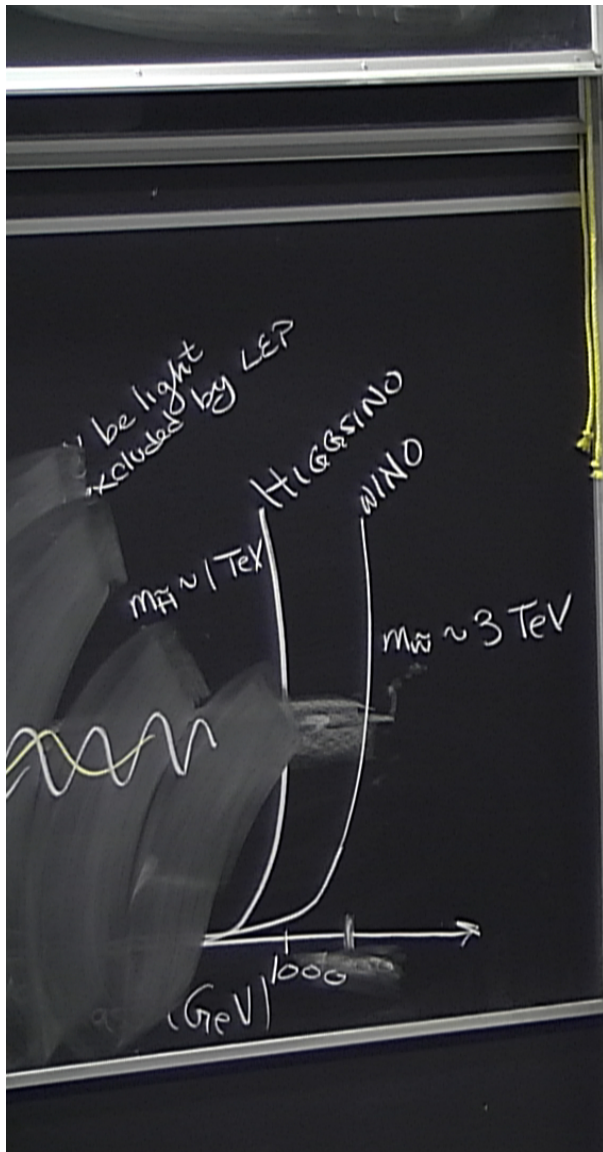


CAUTION

DO NOT TOUCH THE BOARD WHEN THE BOARD IS BEING USED BY OTHERS.

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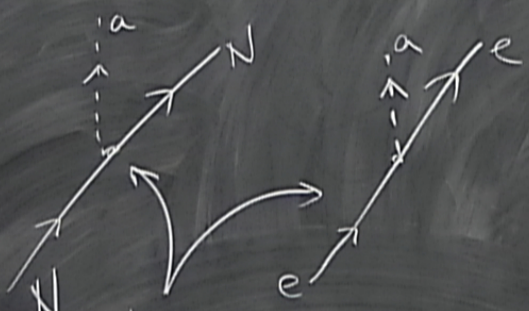


$$\ddot{\theta} + 3H\dot{\theta} + m_a^2 \theta = 0$$

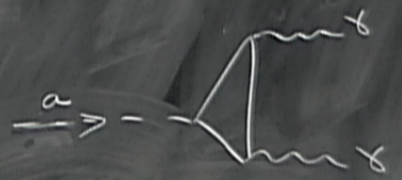
$T \gg \Lambda_{\text{QCD}}, m_a = 0$

CAUTION

$$m_a \approx 6 \times 10^{-10} \text{ eV} \left(\frac{10^{16} \text{ GeV}}{f_a} \right)$$



derivative couplings
w/ scale set by
 $1/f_a$



$f_a \leq 10^9 \text{ GeV}$
 $f_a \sim 10^{11} \text{ GeV}$] excluded